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## PALINDROMIAL EQUIVALENCE: ONE THEOREM AND TWO PROBLEMS

Let A be an alphabet,  $A^*$  be a set of all words in A. A word  $\nu$  is called a *subword* of a word w if  $\nu$  can be obtained by striking out some letters from w. For a word  $w = a_1 a_2 \dots a_{n-1} a_n$ , put  $\tilde{w} = a_n a_{n_1} \dots a_2 a_1$ . A word w is called a *palindrome* if  $\tilde{w} = w$ .

Given a word  $w \in A^*$ , denote by Pal (w) the set of all subwords of w that are palindromes. The words  $\nu$ , w are called *palindromially equivalent* if Pal  $(\nu) = Pal (w)$ .

**Theorem.** Let |A| = 2,  $\nu, w \in A^*$ . Then  $\nu, w$  are palindromially equivalent if and only if  $\nu = w$  or  $\nu = \tilde{w}$ .

**Problem 1.** Describe the classes of palindromial equivalence on  $A^*$  for |A| = 3.

Let  $A = \{a, b\}, w \in A^*, w = a_1 a_2 \dots a_n$ . Put  $\bar{a} = b, \bar{b} = a, \bar{w} = \bar{a}_1 \bar{a}_2 \dots \bar{a}_n$ . A word w is called an *antipalindrome* if  $\tilde{w} = \bar{w}$ .

**Problem 2.** Describe the classes of antipalindromial equivalence on  $A^*$ .

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