
REPAINT: Knowledge Transfer in Deep Reinforcement Learning

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Abstract

Accelerating learning processes for complex tasks by leveraging previously learned tasks has been one of the most challenging problems in reinforcement learning, especially when the similarity between source and target tasks is low. This work proposes REpresentation And INstance Transfer (REPAINT) algorithm for knowledge transfer in deep reinforcement learning. REPAINT not only transfers the representation of a pre-trained teacher policy in the on-policy learning, but also uses an advantage-based experience selection approach to transfer useful samples collected following the teacher policy in the off-policy learning. Our experimental results on several benchmark tasks show that REPAINT significantly reduces the total training time in generic cases of task similarity. In particular, when the source tasks are dissimilar to, or sub-tasks of, the target tasks, REPAINT outperforms other baselines in both training-time reduction and asymptotic performance of return scores.

1. Introduction

In the past few years, deep reinforcement learning (RL) has become more ubiquitous in solving sequential decision-making problems for many real-world applications, such as game playing (OpenAI et al., 2019; Silver et al., 2016), robotics (Kober et al., 2013; OpenAI et al., 2018), and autonomous driving (Sallab et al., 2017). However, most RL methods train an agent from scratch, typically requiring a huge amount of time and computing resources. Accelerating the learning processes for complex tasks has been one of the most challenging problems in RL (Kaelbling et al., 1996; Sutton & Barto, 2018). The computational cost of learning grows as the task complexity increases in the real-world applications. Therefore, it is desirable for a learning algorithm to leverage knowledge acquired in one task to

improve performance on other tasks.

Transfer learning has achieved significant success in computer vision, natural language processing, and other knowledge engineering areas (Pan & Yang, 2009). In transfer learning, the source (teacher) and target (student) tasks are not necessarily drawn from the same distribution (Taylor et al., 2008a). The unseen target task may be a simple task which is similar to the previously trained tasks, or a complex task with traits borrowed from significantly different source tasks. Despite the prevalence of direct weight transfer, knowledge transfer from pre-trained agents for RL tasks has not been gaining much attention until recently (Barreto et al., 2019; Ma et al., 2018; Schmitt et al., 2018; Lazaric, 2012; Taylor & Stone, 2009). However, many transfer RL algorithms are designed to select similar tasks or samples from a set of source tasks, or learn representations of source tasks. Hence they perform well only when the target tasks are similar to the source tasks, but are usually not helpful when the task similarity is low or the target tasks are much more complex than the source tasks.

In this work, we propose an algorithm, i.e., REpresentation And INstance Transfer (REPAINT), to address the aforementioned problem. The algorithm introduces an off-policy instance transfer learning and combines it with an on-policy representation transfer. The main contributions of this paper are as follows. (1) We develop an advantage-based experience selection approach in the off-policy instance transfer, which helps improve the sample efficiency by only transferring the useful instances. (2) The REPAINT algorithm is simple to implement and can be naturally extended to any policy gradient-based RL algorithms. In addition, we also provide two variants of REPAINT for actor-critic RL and an extension to Q-learning. (3) We clarify that our REPAINT algorithm exploits the (semantic) relatedness between the source samples and target tasks, instead of the task/sample similarities that most transfer RL methods exploit. (4) On several transfer learning tasks, we empirically demonstrate that REPAINT significantly reduces the training time needed to achieve certain performance level in generic cases of task similarity. Moreover, when the source tasks are dissimilar to, or sub-tasks of, complex target tasks, REPAINT greatly outperforms other baseline methods in both training-time reduction and asymptotic return scores.

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2. Related Work: Transfer Learning in RL

This section only introduces the related work on transfer learning for RL. We will discuss the connection between our proposed algorithm and other related work in Section 4. In transfer learning for RL, most algorithms either assume specific forms of reward functions or perform well only when the teacher and student tasks are similar. Additionally, very few algorithms are designated to actor-critic RL.

Transfer learning algorithms in RL can be characterized by the definition of transferred knowledge, which contains the *parameters* of the RL algorithm, the *representation* of the trained policy, and the *instances* collected from the environment (Lazaric, 2012). When the teacher and student tasks share the same state-action space and they are considered similar (Ferns et al., 2004; Phillips, 2006), *parameter transfer* is the most straightforward approach, namely, one can initialize the policy or value network in the student tasks by that from teacher tasks (Mehta et al., 2008; Rajendran et al., 2015). Parameter transfer with different state-action variables is more complex, where the crucial aspect is to find a suitable mapping from the teacher state-action space to the student state-action space (Gupta et al., 2017; Talvitie & Singh, 2007; Taylor et al., 2008b).

Many transfer learning algorithms fall into the category of *representation transfer*, where the algorithm learns a specific representation of the task or the solution, and the transfer algorithm performs an abstraction process to fit it into the student task. Konidaris et al. (2012) uses the *reward shaping* approach to learn a portable shaping function for knowledge transfer, while some other works use neural networks for feature abstraction (Duan et al., 2016; Parisotto et al., 2015; Zhang et al., 2018). *Policy distillation* (Rusu et al., 2015), or its variants, is another popular choice for learning the teacher task representation, where the student policy aims to mimic the behavior of pre-trained teacher policies during its own learning process (Schmitt et al., 2018; Yin & Pan, 2017). Recently, *successor representation* has been widely used in transfer RL, in which the rewards are assumed to share some common features, so that the value function can be simply written as a linear combination of the *successor features* (SFs) (Barreto et al., 2017; Madarasz & Behrens, 2019). Barreto et al. (2019) extends the method of using SFs and generalised policy improvement in Q-learning (Sutton & Barto, 2018) to more general environments. Borsa et al. (2018), Ma et al. (2018), and Schaul et al. (2015a) learn a universal SF approximator for transfer.

The basic idea of *instance transfer* algorithms is that the transfer of teacher samples may improve the learning on student tasks. Lazaric et al. (2008) and Tirinzoni et al. (2018) selectively transfer samples on the basis of the compliance between tasks in a model-free algorithm, while Taylor et al. (2008a) studies how a model-based algorithm can benefit

from samples coming from the teacher task.

In this work, we propose a representation-instance transfer algorithm to handle the generic cases of task similarity in RL. The algorithm is also naturally fitted for actor-critic framework and can be easily extended to other RL algorithms.

3. Background: Actor-Critic RL

A general RL agent interacting with environment can be modeled in a Markov decision process (MDP), which is defined by a tuple $M = (S, A, p, r, \gamma)$, where S and A are sets of states and actions, respectively. The state transfer function $p(\cdot|s, a)$ maps a state and action pair to a probability distribution over states. $r : S \times A \times S \rightarrow \mathbb{R}$ denotes the reward function that determines a reward received by the agent for a transition from (s, a) to s' . The discount factor, $\gamma \in [0, 1]$, provides means to obtain a long-term objective. Specifically, the goal of an RL agent is to learn a policy π that maps a state to a probability distribution over actions at each time step t , so that $a_t \sim \pi(\cdot|s_t)$ maximizes the accumulated discounted return $\sum_{t \geq 0} \gamma^t r(s_t, a_t, s_{t+1})$.

To address this problem, a popular choice to adopt is the model-free actor-critic architecture, e.g., Konda & Tsitsiklis (2000); Degris et al. (2012); Mnih et al. (2016); Schulman et al. (2015a; 2017), where the critic estimates the value function and the actor updates the policy distribution in the direction suggested by the critic. The actor-critic methods usually rely on the *advantage function*, which is computed by $A^\pi(s, a) = Q^\pi(s, a) - V^\pi(s)$, where $Q^\pi(s, a) := \mathbb{E}_{a_i \sim \pi(\cdot|s_i)} \left[\sum_{i \geq t} \gamma^{i-t} r(s_i, a_i, s_{i+1}) | s, a \right]$ is the Q (action value) function and $V^\pi(s) := \mathbb{E}_\pi \left[\sum_{i \geq t} \gamma^{i-t} r_{i+1} | s_t = s \right]$ is the state value function.

Intuitively, the advantage can be taken as the extra reward that could be obtained by taking a particular action a . In deep RL, the critic and actor functions are usually parameterized by neural networks. Then the policy gradient methods can be used to update the actor network. For example, in the clipped proximal policy optimization (Clipped PPO) (Schulman et al., 2017), the policy’s objective function is defined to be the minimum between the standard surrogate objective and an ϵ clipped objective:

$$L_{\text{clip}}(\theta) = \mathbb{E}_t \left[\min \left(\ell_\theta(s_t, a_t) \cdot \hat{A}_t, \text{clip}_\epsilon(\ell_\theta(s_t, a_t)) \cdot \hat{A}_t \right) \right], \quad (3.1)$$

where the policy π is parameterized by θ , \hat{A}_t are the advantage estimates, and $\ell_\theta(\cdot, \cdot)$ is the likelihood ratio that

$$\ell_\theta(s_t, a_t) = \frac{\pi_\theta(a_t|s_t)}{\pi_{\theta_{\text{old}}}(a_t|s_t)}.$$

Additionally, the function clip_ϵ truncates $\ell_\theta(\cdot, \cdot)$ to the range of $(1 - \epsilon, 1 + \epsilon)$.

4. The REPAINT Algorithm

We now describe our knowledge transfer algorithm, i.e., REPAINT, for actor-critic RL framework, which is provided in Algorithm 1. Without loss of generality, we demonstrate the policy update using Clipped PPO, and use a single teacher policy in the knowledge transfer. In practice, it can be directly applied to any policy gradient-based RL algorithms, and it is straightforward to have multiple teacher policies in transfer. More discussion can be found later in this section.

In REPAINT with actor-critic RL, the critic update uses traditional supervised regression, which is exactly the same as Clipped PPO. However, there are two core concepts underlying our actor update, i.e., on-policy representation transfer learning and off-policy instance transfer learning. The on-policy representation transfer employs a policy distillation approach (Schmitt et al., 2018). In the off-policy instance transfer, we update the actor by an off-policy objective L_{ins} and using an *advantage-based experience selection* on \mathcal{S} , the replay buffer for teacher instances. The proposed experience selection approach is used to select samples that have high *semantic relatedness*, instead of high similarity, to the target task. We defer the discussion to Section 5.2.

4.1. On-policy Representation Transfer: Kickstarting

In order to boost the initial performance of an agent, we use the policy distillation approach adopted in a kickstarting training pipeline (Schmitt et al., 2018; Rusu et al., 2015) for on-policy representation transfer. The main idea is to employ an auxiliary loss function which encourages the student policy to be close to the teacher policy on the trajectories sampled by the student. Given a teacher policy π_{teacher} , we introduce the auxiliary loss as $L_{\text{aux}}(\theta) = H(\pi_{\text{teacher}}(a|s) \parallel \pi_{\theta}(a|s))$, where $H(\cdot \parallel \cdot)$ is the cross-entropy. Then the policy distillation adds the above loss to the Clipped PPO objective function, i.e., (3.1), weighted at optimization iteration k by the scaling $\beta_k \geq 0$:

$$L_{\text{rep}}^k(\theta) = L_{\text{clip}}(\theta) - \beta_k L_{\text{aux}}(\theta). \quad (4.1)$$

In our experiments, the weighting parameter β_k is relatively large at early iterations, and vanishes as k increases, which is expected to improve the initial performance of the agent while keeping it focused on the current task in later epochs.

4.2. Off-policy Instance Transfer: Advantage-based Experience Selection

Note that the kickstarting aims to replicate the behavior of teacher policy in the early training stage, so that it can improve the agent’s initial performance. However, when the target task is very different from the source task, kickstarting usually does not lead to much improvement. To address this, we now propose the off-policy instance transfer with an approach called advantage-based experience selection.

Algorithm 1 REPAINT with Clipped PPO

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Initialize  $\nu, \theta$ , and load teacher policy  $\pi_{\text{teacher}}(\cdot)$ 
Set hyper-parameters  $\zeta, \alpha_1, \alpha_2$ , and  $\beta_k$  in (4.1)
for iteration  $k = 1, 2, \dots$  do
    Set  $\theta_{\text{old}} \leftarrow \theta$ 
    Collect samples  $\mathcal{S} = \{(s, a, s', r)\}$  using  $\pi_{\theta_{\text{old}}}(\cdot)$ 
    Collect samples  $\tilde{\mathcal{S}} = \{(\tilde{s}, \tilde{a}, \tilde{s}', \tilde{r})\}$  using  $\pi_{\text{teacher}}(\cdot)$ 
    Fit state-value network  $V_{\nu}$  using only  $\mathcal{S}$  to update  $\nu$ 
    Compute advantage estimates  $\hat{A}_1, \dots, \hat{A}_T$  for  $\mathcal{S}$  and
     $\hat{A}'_1, \dots, \hat{A}'_{T'}$  for  $\tilde{\mathcal{S}}$ 
    for  $t=1, \dots, T'$  do // experience selection
        if  $\hat{A}'_t < \zeta$  then
            Remove  $\hat{A}'_t$  and the corresponding transition
             $(\tilde{s}_t, \tilde{a}_t, \tilde{s}_{t+1}, \tilde{r}_t)$  from  $\tilde{\mathcal{S}}$ 
        Compute sample gradient of  $L_{\text{rep}}^k(\theta)$  in (4.1) using  $\mathcal{S}$ 
        Compute sample gradient of  $L_{\text{ins}}(\theta)$  in (4.2) using  $\tilde{\mathcal{S}}$ 
        Update policy network by
    
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$$\theta \leftarrow \theta + \alpha_1 \nabla_{\theta} L_{\text{rep}}^k(\theta) + \alpha_2 \nabla_{\theta} L_{\text{ins}}(\theta)$$

In the off-policy instance transfer, we form a replay buffer $\tilde{\mathcal{S}}$ by collecting training samples following the teacher policy π_{teacher} , but compute the rewards using current reward function from the target task. Since the samples are obtained from a different distribution, we do not use those samples to update the state value (critic) network. In order to improve the sample efficiency, when updating the policy (actor) network, we select the transitions based on the advantage values and only use the samples that have advantages greater than a given threshold ζ . Moreover, since the teacher policy has been used in collecting roll-outs, we compute the objective without the auxiliary cross-entropy loss, but replace $\pi_{\theta_{\text{old}}}$ with π_{teacher} in (3.1) for off-policy learning, which leads to the following objective function:

$$L_{\text{ins}}(\theta) = \hat{\mathbb{E}}_t \left[\min \left(\rho_{\theta}(s_t, a_t) \cdot \hat{A}'_t, \text{clip}_{\epsilon}(\rho_{\theta}(s_t, a_t)) \cdot \hat{A}'_t \right) \right], \quad (4.2)$$

where ρ_{θ} now is given by $\rho_{\theta}(s_t, a_t) = \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\text{teacher}}(a_t|s_t)}$. The idea of advantage-based experience selection is simple but effective. As mentioned before, the advantage can be viewed as the extra reward that could be obtained by taking a particular action. Therefore, since the advantages are computed under the reward function of the target task, the state-action transitions with high advantage values can be viewed as “good” samples for transfer, no matter how different the source and target tasks are. By retaining only the good samples from replay buffer $\tilde{\mathcal{S}}$, the agent can focus on learning useful behavior for current task, which as a result can improve the sample efficiency in knowledge transfer.

Related work on experience selection. We note that although the experience selection approach has not been used

in knowledge transfer before, it is related to the prioritized experience replay (PER) (Schaul et al., 2015b), which prioritizes the transitions in replay buffer by the temporal-difference (TD) error, and utilizes importance sampling for the off-policy evaluation. In comparison, our method uses experience selection in the actor-critic framework, where the replay buffer is erased after each training iteration. Unlike the stochastic prioritization which imposes the probability of sampling, our method directly filters out most of the transitions from replay buffer and equally prioritizes the remaining data, which further improves the sample efficiency. In addition, our method performs policy update without importance sampling. All transitions in a batch have the same weight, since the importance can be reflected by their advantage values. The empirical comparison among PER and several experience selection approaches can be found in Section 6.2.

As another related work, Self-Imitation Learning (SIL) (Oh et al., 2018) provides an off-policy actor-critic algorithm that learns to reproduce the agent’s past good decisions. It selects past experience based on the gap between the off-policy Monte-Carlo return and the agent’s value estimate, and only uses samples with positive gaps to update both the actor and the critic. Similar approach can also be seen in Q-filter (Nair et al., 2018). In comparison, other than that REPAINT uses an advantage-based experience selection instead of the return gap, our method introduces a more general threshold ζ , while SIL fixes it to be zero. Moreover, the positive-gap samples are also used to update the critic in SIL, but we only fit the state values by on-policy data for following the correct distribution. Motivated by the justification that SIL is equivalent to a lower-bound soft-Q-learning, we also present the extension of REPAINT with Q-learning in this paper, which is given in Section A.

Again, we want to remark that our proposed advantage-based experience selection has a different formulation with the existing methods. Moreover, to the best of our knowledge, it is the first time that the advantage-based filtering has been applied to the knowledge transfer for RL.

4.3. Discussion and Extension

In regards to the proposed REPAINT algorithm, we want to remark that the policy distillation weight β_k and advantage filtering threshold ζ are task specific. They are dependent with the one-step rewards. To this end, one can consider to normalize reward functions in practice, so that the one-step rewards are in the same scale. In general, larger β_k encourages the agent to better match the teacher policy, and larger ζ leads to that fewer samples are kept for policy update, which in result makes current learning concentrate more on the high-advantage experience. The empirical investigations on these two parameters can be found later.

So far, we have demonstrated the REPAINT algorithm using only a single teacher policy in the knowledge transfer and the objective function from Clipped PPO. Indeed, it is straightforward to using multiple teacher policies, or even using different teacher policies for representation transfer and instance transfer. In addition, REPAINT can be directly applied to any policy gradient-based RL algorithms, such as A2C (Sutton et al., 2000), A3C (Mnih et al., 2016), TRPO (Schulman et al., 2015a) and REINFORCE (Williams, 1992). In Section A, we will provide the discussion in more details. We also present an extension of the REPAINT algorithm with Q-learning there.

5. Theoretical Justification and Analysis Related to REPAINT

This section introduces some theoretical results and justifications that are related to the proposed algorithm, from which we hope to clarify REPAINT in greater depth. The detailed discussion of Theorem 5.1 and Theorem 5.2 can be found in Sections D and E from appendix, respectively.

5.1. Convergence Results

We first discuss the convergence of REPAINT without any experience selection approach, and then consider how the experience selection from teacher policy impacts the policy update. To simplify the illustration without loss of generality, we consider the objective for the actor-critic to be $J_{\text{RL}}(\theta) = \mathbb{E}_t[Q^{\pi_\theta}(s, a) \log \nabla \pi_\theta(a|s)]$ instead of $L_{\text{clip}}(\theta)$, and modify the objectives for representation transfer and instance transfer accordingly (denoted by J_{rep} and J_{ins}). The convergence of representation transfer can be easily obtained, as it is equivalent to the convergence of other actor-critic methods. Our instance transfer learning fits into the framework of the off-policy actor-critic (Degris et al., 2012; Zhang et al., 2019). Following Holzleitner et al. (2020), under certain commonly used assumptions, we can prove the convergence of the off-policy instance transfer.

Theorem 5.1. Suppose the critic is updated by TD residuals, and the actor π_θ is updated based on the objective $J_{\text{ins}}(\theta)$. Fix a starting point (θ_0, ν_0) and construct the associated neighborhood $W_0 \times U_0$ as in Section D. Assume the loss functions satisfy Assumptions D.1-D.3, and the learning rates for critic and actor satisfy Assumption D.4. Then (θ_n, ν_n) converges to a local optimum almost surely as $n \rightarrow \infty$ via online stochastic gradient descent (SGD).

In addition, we also want to show the convergence rate for REPAINT, if a good approximation for the critic is available. Again, we assume that the the experience selection approach is not used. We also assume the learning rates α_1 and α_2 are iteration-dependent (denoted by $\alpha_{1,k}$ and $\alpha_{2,k}$). Let K_ϵ be the smallest number of updates k required to attain a

function gradient smaller than ϵ , i.e.,

$$K_\epsilon = \min\{k : \inf_{0 \leq m \leq k} \mathcal{F}(\theta_m) < \epsilon\},$$

with $A_k := \alpha_{2,k}/\alpha_{1,k}$ and

$$\begin{aligned} \mathcal{F}(\theta_m) = & \|\nabla J_{\text{rep}}(\theta_m)\|^2 + A_k \|\nabla J_{\text{ins}}(\theta_m)\|^2 \\ & + (1 + A_k) \nabla J_{\text{rep}}^T(\theta_m) \nabla J_{\text{ins}}(\theta_m). \end{aligned}$$

Note that the hyper-parameter A_k can be determined by how much one wants to learn from instance transfer against the representation transfer. If A is set to be 1, then we can get $\mathcal{F}(\theta_m) = \|\nabla J_{\text{rep}}(\theta_m) + \nabla J_{\text{ins}}(\theta_m)\|^2$.

Theorem 5.2. Suppose the learning rate for representation transfer satisfies $\alpha_{1,k} = k^{-a}$ for $a > 0$, and the critic update satisfies Assumption E.5. When the critic bias converges to zero as $\mathcal{O}(k^{-b})$ for some $b \in (0, 1]$, we can find an integer $T(b, k)$ such that $T(b, k)$ critic updates occur per actor update. Then the actor sequence satisfies

$$K_\epsilon \leq \mathcal{O}(\epsilon^{-1/l}), \text{ where } l = \min\{a, 1 - a, b\}.$$

Despite greatly improving the sample efficiency, the experience selection introduces bias by changing the distribution in an uncontrolled fashion. In practice, to mitigate it, we can adopt REPAINT in the early training stage, and then reduce to traditional actor-critic algorithms. As a consequence, the agent first learns useful teacher behavior to achieve good initial performance, and focuses on the target task afterwards.

5.2. Semantic Relatedness vs. Task Similarity

Most transfer learning algorithms for RL are built based on the *similarity* between source and target tasks, and perform well only when the tasks are similar. If samples from two MDPs are given, some metrics can be defined to compute or learn the task similarity, e.g., the Kantorovich distance-based metric (Song et al., 2016), the restricted Boltzmann machine distance measure (Ammar et al., 2014), the policy overlap (Carroll & Seppi, 2005), and the task compliance and sample relevance (Lazaric et al., 2008). In general, the similarity is usually unknown before getting any samples, unless other information is given. For example, the methods using successor features (Barreto et al., 2019; Borsa et al., 2018; Schaul et al., 2015a) assume that the reward functions among tasks are a linear combination of some common features, namely, $r(s, a, s') = \sum_i w_i \phi_i(s, a, s')$ with fixed ϕ_i 's. Then the similarity can be characterized by the distance of the weight vectors.

In this paper, we aim to show that REPAINT handles generic cases of task similarity. Therefore, we do not use any similarity information during transfer. Instead, REPAINT falls into exploiting the *relatedness* for knowledge transfer, a concept

that has been used in some other machine learning areas, e.g., multi-task learning (Caruana, 1997) and meta-learning (Achille et al., 2019). The difference between relatedness and similarity in transfer learning can be analogous to the difference between semantic relatedness and lexicographical similarity in languages. More specifically, no matter how different the source and target tasks are, we can always select related samples from the source tasks that are useful for learning the target tasks. In REPAINT, the relatedness is just defined by the advantage values of source samples under target reward function and state values. Moreover, the cross-entropy weights β_k and the experience selection threshold ζ are used to control the contribution from the source task. We will compare REPAINT against a similarity-based transfer learning algorithm (Lazaric et al., 2008) in Section 6.2.

6. Experiments

According to Taylor & Stone (2009), the *performance* of transfer learning (TL) can be measured by: (1) the improvement of the agent's initial performance when learning from a pre-trained policy; (2) the improvement of final performance and total accumulated reward after transfer; and (3) the reduction of training convergence time or the learning time needed by the agent to achieve a specified performance level. In this paper, we are particularly interested in the last metric, i.e., the training time reduction, since one cannot always expect the return score improvement, especially when the source tasks are very different from the target tasks.

In this section, we conduct experiments for answering following questions. (1) When the source (teacher) tasks are similar to the target (student) tasks, it is expected that most TL methods perform well. Can REPAINT also achieve good TL performance? (2) When the task similarity is low, can REPAINT still reduce the training time of the target tasks? (3) When the source tasks are only sub-tasks of the complex target tasks, is REPAINT still helpful? (4) Are both on-policy representation transfer and off-policy instance transfer necessary for REPAINT? (5) How do other experience selection (prioritization) approaches perform on REPAINT? (6) How do the hyper-parameters β_k and ζ change the TL performance? Is REPAINT robust to them?

A metric to quantify the task similarity level is required for answering those questions. For simplicity, we assume in the experiments that the state and action spaces stay the same between teacher and student tasks, and the reward functions have the form of linear combination of some common features. Then we use the cosine distance function to define the task similarity, namely, the similarity between two tasks with reward functions $r_1(s, a, s') = \phi(s, a, s')^\top \mathbf{w}_1$ and $r_2(s, a, s') = \phi(s, a, s')^\top \mathbf{w}_2$ can be computed as

$$\text{sim}(r_1, r_2) = \frac{\mathbf{w}_1 \cdot \mathbf{w}_2}{\|\mathbf{w}_1\| \|\mathbf{w}_2\|}. \quad (6.1)$$

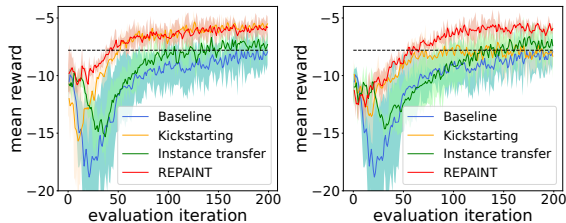


Figure 1. Evaluation performance for MuJoCo-Reacher, averaged across five runs. We consider both teacher task is similar to (left) and different from (right) the target task.

We say the two tasks are *similar* if $\text{sim}(r_1, r_2) > 0$. Otherwise (≤ 0), they are considered to be *different (dissimilar)*. In addition, if some feature weights are zero in a reward function, the corresponding task can be viewed as a *sub-task* of other tasks that have non-zero feature weights.

6.1. Experimental Setup

To assess the REPAINT algorithm, we use three platforms across multiple benchmark tasks with increasing complexity for experiments, i.e., Reacher and Ant environments in MuJoCo simulator (Todorov, 2016), single-car and multi-car racings in AWS DeepRacer simulator (Balaji et al., 2019), and *BuildMarines* and *FindAndDefeatZerglings* mini-games in StarCraft II environments (Vinyals et al., 2017). More detailed descriptions of the environments are given in Section B. The first four questions mentioned above will be answered across all environments. We use simpler environments, i.e., MuJoCo-Reacher and DeepRacer single-car, to answer the last two questions, as it is easier to interpret the results without extra complexity and environment noise.

In order to compare the performance of REPAINT with other methods and demonstrate that REPAINT improves sample efficiency during transfer, we should guarantee that REPAINT does not use more samples for transfer in each iteration. Therefore, we employ an alternating REPAINT with Clipped PPO in experiments, where we adopt on-policy representation transfer and off-policy instance transfer alternately on odd and even numbered iterations. The algorithm is presented in Section A (Algorithm 2). The study of different alternating ratios has also been provided in Section C.1. In addition, one can find in Section B the hyper-parameters we used for reproducing our results.

6.2. Continuous Action Control in MuJoCo

MuJoCo-Reacher. In the target task, the agent is rewarded by getting close to the goal point with less movement. As an ablation study, we first compare REPAINT against training with only kickstarting or instance transfer and with no prior knowledge (baseline), based on two teacher tasks. The first teacher policy is trained with simi-

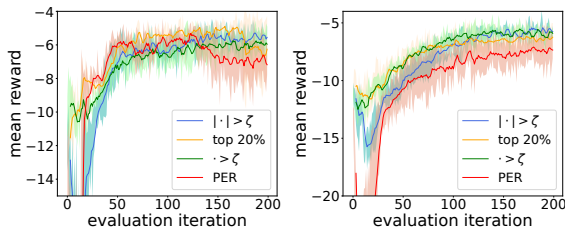


Figure 2. Comparison of different experience selection (prioritization) approaches. Left: similar tasks. Right: dissimilar tasks.

lar reward function but a higher weight on the movement penalty, where we set it to be 3 as an example, so that the cosine similarity is positive. Another teacher policy is trained in a dissimilar task, where the agent is penalized when it is close to the goal. In this case, the cosine similarity is zero. After each training iteration, we evaluate the policy for another 20 episodes. The evaluation performance is presented in Figure 1¹. REPAINT outperforms baseline algorithm and instance transfer in both cases of task similarity, regarding the training time reduction, asymptotic performance, and the initial performance boosting. Although kickstarting can improve the initial performance, it has no performance gain in convergence when the teacher behavior is opposed to the expected target behavior (see right sub-figure). In contrast, although the instance transfer does not boost the initial performance, it surpasses the baseline performance asymptotically in both cases.

We also compare the performance of several experience selection rules in REPAINT, including high absolute values ($|\cdot| > \zeta$), top 20% of transitions in ranking (top 20%), our proposed rule ($\cdot > \zeta$), and PER (Schaul et al., 2015b). For PER, we used the advantage estimates to compute the prioritization instead of TD errors for a fair comparison, and slightly tuned the hyper-parameters. From Figure 2, we can observe that the proposed selection rule and top 20% rule perform better than others on the initial performance, where only the most related samples are selected for policy update. Moreover, PER does not work as well as other approaches, especially when the task similarity is low, since it includes low-advantage teacher samples which have no merits for the student policy to learn. Therefore, we suggest to use the proposed selection rule with a threshold ζ or the ranking-based rule with a percentage threshold.

In order to showcase that our REPAINT algorithm exploits the (semantic) relatedness between source samples and target tasks, while most of other TL algorithms exploit the sample similarities, we make a comparison with an exist-

¹The black dashed lines in here and other figures indicate the best return score of training from scratch (baseline), by which one can see how fast each method achieves a certain performance level. More quantitative results can be found in Table 1.

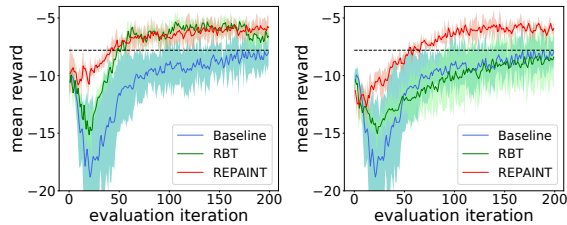


Figure 3. Comparison of relevance-based transfer (RBT) and REPAINT. Left: similar tasks. Right: dissimilar tasks.

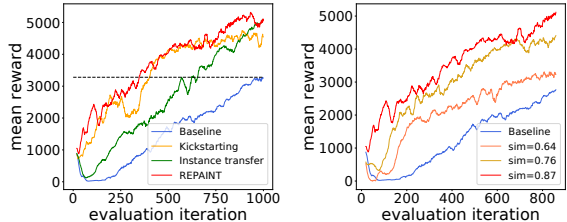
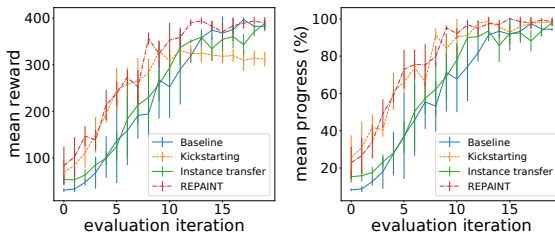


Figure 4. Evaluation performance for MuJoCo-Ant, averaged across three runs. Left: Model performance with same teacher that is pre-trained from a similar task. Right: REPAINT performance with different teacher policies (cosine similarities between source and target tasks are given). The plots are smoothed for visibility.

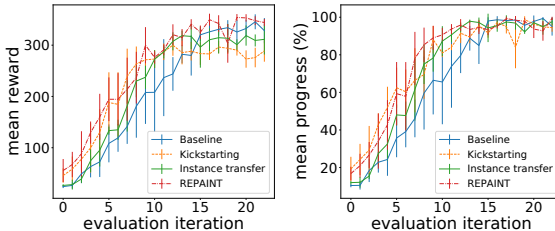
ing method here. Lazaric et al. (2008) defined some metrics of task compliance and sample relevance and proposed an instance transfer algorithm based on that. We call it relevance-based transfer (RBT). We incorporate kickstarting with RBT, and compare its TL performance with REPAINT in Figure 3. When a similar task is used in knowledge transfer, RBT works well. However, when the target task is very different from the source task, although RBT attempts to transfer the most similar samples, it has no performance gain over the baseline training. The performance of REPAINT is significantly better than RBT in this case.

MuJoCo-Ant. In this target task, the agent is rewarded by survival and moving forward, and penalized by control and contact cost. The teacher policies are all trained from similar tasks, where the reward functions have higher weights on moving forward. We train each model for 1000 iterations, and evaluate each iteration for another 5 episodes. The results are shown in Figure 4². From the left sub-figure, we can again observe that, when task similarity is positive, training with REPAINT or kickstarting significantly improves the initial performance and reduces the learning cost of achieving a certain performance level. We also evaluate the transfer performance from the similar source tasks with different levels of cosine similarities. We set the forward coefficients in the reward function of teacher tasks

²We noticed that in MuJoCo-Ant, the variances of evaluation across different runs are very large. Hence we only show the mean values and omit the error bars in Figure 4.



(a) Outer-lane reward task with inner-lane teacher



(b) Inner-lane reward task with outer-lane teacher

Figure 5. Evaluation performance for DeepRacer single-car time-trial race, including mean accumulated rewards and mean progress (lap completion percentage), averaged across five runs.

to be 3, 5, and 10, corresponding to the cosine similarities of 0.87, 0.76, and 0.64, respectively. The results in the right sub-figure indicate that task similarity impacts the overall training performance, even when they are all related. Pre-trained teacher policies from more similar tasks can better contribute to the transfer performance. In addition, we present more results in Section C.2, showing that REPAINT is robust to the threshold parameter.

6.3. Autonomous Racing in AWS DeepRacer

Single-car time trial. In this experiment, we use two different reward functions, one of which rewards the agent when it is in the inner lane and penalizes when in the outer lane, and the other reward function does the opposite. When we use one reward in the student task, we provide the teacher policy that is trained with the other reward. Therefore, the cosine similarity of teacher and target tasks is negative.

We evaluate the policy for 5 episodes after each iteration. The evaluation performance is presented in Figure 5, where both average return and progress (percentage of a lap the agent accomplished when it went out of track) are given. Although upon convergence, all models can finish a lap without going off-track, REPAINT and kickstarting again significantly boost the initial performance. However, when the teacher task is very different from the target task, training with kickstarting cannot improve the final performance via transfer. In contrast, instance transfer can still reduce the training convergence time with a final performance better than kickstarting (though with small margins in this example). Due to the page limit, we present the study on the effect of different cross-entropy weights β_k and instance

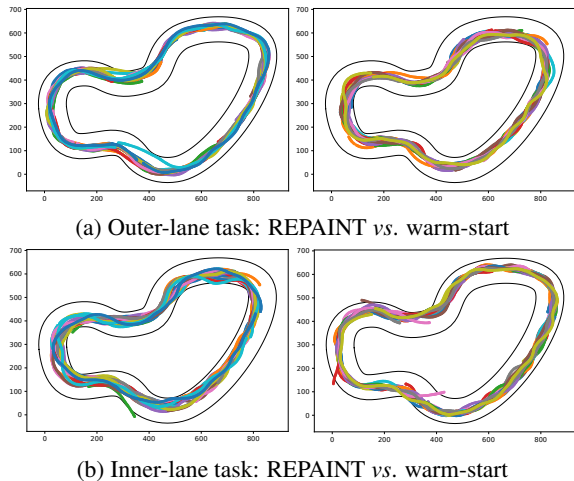


Figure 6. Trajectories of policy evaluations. In each of (a) and (b), evaluation of the models trained from REPAINT is visualized on the left and that trained with warm-start is on the right.

filtering thresholds ζ in Section C.3 of appendix.

We also want to compare the REPAINT algorithm, which is a *representation-instance* transfer algorithm, with a widely-used *parameter* transfer approach, i.e., warm-start. In warm-start, the agent initializes with parameters from the teacher policy and conducts the RL algorithm after that. When the target task is similar to the teacher task, it usually works well. But here we compare the two algorithms in the DeepRacer single-car experiment, where the two tasks are significantly different. Figure 6 visualizes the trajectories of the agent on the track during evaluations. Each model is trained for two hours and evaluated for another 20 episodes. From both cases, we can see that although the two reward functions encode totally different behaviors, REPAINT can still focus on current task while learning from the teacher policy. This again indicates the effectiveness of the advantage-based experience selection in the instance transfer. In comparison, training with warm-start cannot get rid of the unexpected behavior at convergence due to the reason that it may be stuck at some local optima. Therefore, initialization with previously trained policies can sometimes jump-start the training with good initial performance, but the method contributes to the final performance only when two tasks are highly similar.

Racing against bot cars. The REPAINT algorithm is still helpful when the RL agent needs to learn multiple skills in a task. In the multi-car racing, the agent has to keep on the track while avoiding crashes with bot cars in order to obtain high rewards. We first train a teacher policy which is good at object avoidance, namely, the agent is rewarded when it keeps away from all bot cars, and gets a penalty when the agent is too close to a bot car and heads towards to it. Then in target tasks, we use two different reward functions

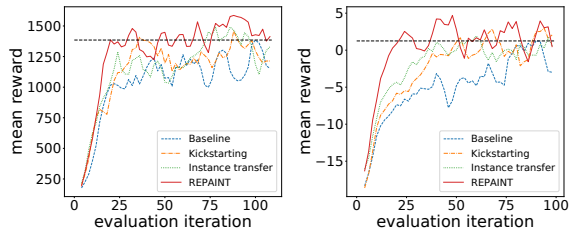


Figure 7. Evaluation performance for DeepRacer multi-car racing against bot cars, averaged across three runs. Left: Task with advanced reward. Right: Task with progress-based reward. The plots are smoothed for visibility.

to assess the models. First, we use an *advanced reward* where other than keeping on track and object avoidance, it also penalizes the agent when it detects some bot car from the camera and is in the same lane with the bot. The evaluation performance is shown in Figure 7 (left). Since the environment has high randomness, such as agent and bot car initial locations and bot car lane changing, we only report average results. One can observe that REPAINT outperforms other baselines regarding the training time needed for certain performance level and the asymptotic performance. Another target task with a *progress-based reward* is also investigated, where the agent is only rewarded based on its completion progress, but gets large penalty when it goes off-track or crashes with bot cars. Since maximizing the completion progress involves bot car avoidance, the teacher task can be seen as either a different task or a sub-task. The results are provided in Figure 7 (right). When the target task is complex and the reward is simple (sparse) as in this case, it is sometimes difficult for the agent to learn a good policy as it lacks guidance from the reward on its actions. From the sub-figure, we can again see that training with REPAINT not only largely reduces the convergence time, but also improves the asymptotic performance compared to other models.

6.4. More Complex Tasks: StarCraft II Environments

At last, we also conduct the ablation study on a more complex transfer learning task using StarCraft II Learning Environments (Vinyals et al., 2017). The teacher policy is trained on the *BuildMarines* mini-game, where the agent is given a limited base and is tasked to maximize the number of marines trained. Then the target task builds upon *BuildMarines* to include the *FindAndDefeatZerglings* mini-game, denoted as *BuildMarines+FindAndDefeatZerglings* (*BM+FDZ*). That is, on top of learning how to build marines, the agent must learn to use the built marines to explore the whole map, and try to find and defeat Zerglings that are randomly scattered across the map. Note that the map of *BM+FDZ* is larger than that of *BuildMarines*, so that although the state and action spaces are the same, the initial

Table 1. Summary of the experimental results.

Env.	Teacher type	Target score	K_{Baseline}	K_{KS}		K_{IT}		K_{REPAINT}		Best scores		
				(pct. reduced)	(pct. reduced)	(pct. reduced)	(pct. reduced)	KS	IT	REPAINT		
Reacher	similar	-7.4	173	51 (71%)	97 (44%)	42 (76%)	-5.3	-5.9	-5.4			
	different			73 (58%)	127 (27%)	51 (71%)	-6.9	-6.4	-5.2			
Ant	similar	3685	997	363 (64%)	623 (38%)	334 (66%)	5464	5172	5540			
Single-car	different	394	18	Not achieved	Not achieved	13 (28%)	331	388	396			
	different	345	22	Not achieved	Not achieved	15 (32%)	300	319	354			
Multi-car	sub-task	1481	100	34 (66%)	75 (25%)	29 (71%)	1542	1610	1623			
	diff/sub-task	2.7	77	66 (14%)	53 (31%)	25 (68%)	4.9	4.2	6.1			
StarCraft II	sub-task	112	95	92 (3%)	24 (75%)	6 (94%)	125	312	276			

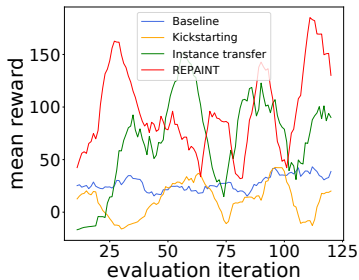


Figure 8. Evaluation performance for StarCraft II environments. The source task is a sub-task of the target task but uses a different map. The plots are smoothed for visibility.

feature maps (observations) between the two tasks are not identical. Therefore, the knowledge transfer between the two tasks is not straightforward. Other details of the environments and reward functions can be found in Section B.

Figure 8 shows the evaluation results for REPAINT and other methods. We want to first remark that it is a known issue that when *BuildMarines* mini-game is involved, the RL performance has large variance, which can also be observed in Figure 6 of Vinyals et al. (2017). From the figure, we can again see that when the source task is a sub-task of a complex target task, the kickstarting method cannot transfer well. In contrast, the instance transfer and the REPAINT algorithm quickly transfer the knowledge of building marines to the target task by selecting the samples with high semantic relatedness. Moreover, they have achieved significantly higher rewards than training from scratch or kickstarting.

7. Summary and Future Work

In this work, we have proposed a knowledge transfer algorithm for RL. The REPAINT algorithm performs an on-policy representation transfer for the pre-trained teacher policies and an off-policy instance transfer for the samples collected following teacher policies. We develop an advantage-based experience selection approach in the in-

stance transfer for selecting the samples that have high semantic relatedness to the target tasks. The idea of experience selection based on sample relatedness is simple but effective, and this is the first time that it is applied to knowledge transfer in RL.

We provide a summary of the experimental results in Table 1. The teacher type indicates whether the teacher task is a sub-task of or similar to the target task, based on the cosine similarity (6.1). The target score is the best performance that the baseline model can achieve. Then we provide the number of training iterations needed by each model to reach the target score. The models include training with baseline, kickstarting (KS), instance transfer (IT), and REPAINT. In Section C.5, we also provide the data of wall-clock time. Although we are more interested in the training time reduction from TL, we present the best scores that each knowledge transfer model can achieve in the table. The kickstarting model performs well only when the tasks are similar or the target task is simple. While the instance transfer model can transfer related samples, it does not boost the initial performance. In contrast, the superior performance for REPAINT is observed regardless of the task similarity. It significantly reduces the training time for each target task, and also improves the final return scores in most tasks.

In future work, we aim to study how REPAINT can automatically learn the task similarity, and spontaneously determine the best β_k and ζ values in the training based on the similarity. Our preliminary results in Section C.3 indicate that when the task similarity is low, larger β_k values may reduce the asymptotic performance of the agent. Moreover, we are also interested in the dependency of transfer performance on the neural network architectures. We provide some preliminary experimental results in Section C.4.

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