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LOGIC AND EQUATIONS FOR THE
REAL-TIME COMPUTATION OF THE LUNAR
MODULE DESCENT PLANNING TABLE

By William A. Sullivan,
Orbital Mission Analysis Branch

(This revision supersedes MSC
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MISSION PLANNING AND ANALYSIS DIVISION
MANNED SPACECRAFT CENTER
HOUSTON, TEXAS

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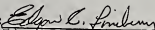
PROJECT APOLLO

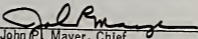
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OF THE LUNAR MODULE DESCENT PLANNING TABLE

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LOGIC AND EQUATIONS FOR THE REAL-TIME COMPUTATION
OF THE LUNAR MODULE DESCENT PLANNING TABLE

By William A. Sullivan

SUMMARY AND INTRODUCTION

This internal note presents the revised logic and equations for the lunar module (IM) descent planning processor (IDPP) which replaces that in reference 1. The enclosed flow charts define the processor for the lunar landing mission real-time computer system. The IDPP computes maneuver sequences to be executed by the command and service modules (CSM) and the IM to yield a set of desired orbital conditions at the point of IM descent ignition or a desired CSM orbital plane at the time of IM lift-off. The output of the IDPP will be used to compute the IM descent planning table for real-time mission planning.

ABBREVIATIONS

APPLY	subroutine that computes and applies maneuvers based on input platform ΔV components
ASP	apside shift, altitude adjustment, and plane-change maneuver
ASH	apside shift and altitude adjustment maneuver
CHAPLA	subroutine that computes plane-change maneuver
CIA	circularization at an apsis maneuver
CIR	circularization maneuver
CNODE	subroutine that searches for a common node between two orbits
CSM	command and service modules
DOI	descent orbit injection maneuver
HO1	first maneuver in a double Hohmann sequence
HO2	second maneuver in a double Hohmann sequence
LATLON	subroutine that computes selenocentric position from selenographic position

LDPP	lunar module descent planning processor
LDPT	lunar module descent planning table
LLTPR	subroutine that predicts the time of lunar landing
LM	lunar module
PC	plane-change maneuver
PCC	plane change and circularization maneuver
PPC	prelaunch plane-change maneuver
SAC	subroutine that computes apsis and circularization maneuvers
SEAP	subroutine that iterates to find an upcoming apsis point
STCIR	subroutine that iterates to find a specified radius in a given orbit
STLO	subroutine that iterates to find a vehicle time of arrival at an input longitude
TIMA	subroutine that iterates to find a vehicle time of arrival at an argument of latitude

LUNAR MODULE DESCENT PLANNING PROCESSOR

The LDPP computes maneuver sequences based on flight controller decisions. There are seven modes of operations from which to choose. Each of these modes may contain more than one sequence. Each sequence may or may not have more than one maneuver. The following table presents a list of maneuver sequences in each mode.

Mode	Maneuver	Sequence		
		1	2	3
1	1	PC	PCC	ASP
	2	DOI	DOI	CIA
	3	--	--	DOI
2	1	ASH	CIR	--
	2	DOI	DOI	--
3	1	ASH	--	--
	2	CIA	--	--
	3	DOI	--	--
4	1	DOI	--	--
5	1	PC	HO1	HO1
	2	HO1	PC	HO2
	3	HO2	HO2	PC
	4	DOI	DOI	DOI
6		Go to powered descent		
7	1	PFC		

These maneuver sequences are designed to give the flight controller the ability to correct a non-nominal CSM orbit after lunar orbit insertion and to place the CSM orbital plane over the IM landing site before IM lift-off. The LDPP has the capability to compute maneuvers to change the apocynthion and pericynthion heights, shift the line-of-apsides and place the CSM orbital plane over a desired landing site using an input azimuth. The processor also computes a LM DOI maneuver based on a desired landing site position. To compute these maneuvers the LDPP assumes that the vehicles are docked for all maneuvers prior to DOI and are undocked for DOI and all following maneuvers.

When computing in modes 1 through 5, the flight controller is given the option of simulating powered descent; in mode 6, however, only a powered descent simulation is available. Mode 7 is used to compute a maneuver to place the CSM orbital plane over the IM landing site at

the time of IM lift-off. To compute these maneuvers, the IDPP calls three specialized subroutines. The subroutines are SAC (spacecraft apsis and circularization), CHAPLA (change spacecraft plane), and LLTPR (lunar landing time prediction routine). Flow charts for the LDPP, SAC, CHAPLA, and LLTPR are presented in appendices A, B, C, and D, respectively. After all computation is completed in the IDPP, the IM descent planning table (IDPT) is then displayed. The IDPT displays maneuvers and descent trajectory parameters. From these displayed quantities the flight controller can decide whether or not the total maneuver plan is acceptable. If the plan is acceptable, the flight controller can transfer it to the mission plan table where it becomes an integral part of the over-all mission plan.

Subroutine SAC computes a maneuver to shift the line-of-apsides and change apocynthion and pericyynthion height or circularize the CSM orbit.

Subroutine CHAPLA computes a maneuver to place the CSM orbital track over a desired landing site with or without a specified azimuth.

Subroutine LLTPR (ref. 2) computes the time of the DOI maneuver based on a desired landing site and a CSM vector before the maneuver.

The LDPP uses the lunar satellite analytic ephemeris generator, ISAEG, (ref. 3) for vehicle ephemeris prediction and IM descent guidance equations of reference 3 for powered descent simulation. Several other special purpose trajectory subroutines are called. These are APPLY (ref. 4), CNODE (ref. 5), STAP, STLO, STCIR (ref. 6), TTMA (ref. 7), and LATLON (ref. 8).

APPENDIX A
IDPP FLOW CHART

SYMBOLS FOR IDPP FLOW CHART

Input Constants

π	3.141592...
μ	lunar gravitational potential
R_{moon}	mean lunar radius
ζ_{θ}	angular iteration tolerance
ζ_t	time iteration tolerance
\bar{g}	average acceleration of gravity

Input Variables

MODE	maneuver routine flag; if
MODE = 1,	compute CSM phase change sequence
MODE = 2,	compute single CSM maneuver sequence
MODE = 3,	compute double CSM maneuver sequence
MODE = 4,	compute IM maneuver sequence
MODE = 5,	compute double Hohmann plane change CSM maneuver sequence
MODE = 6,	compute IM powered-descent trajectory
MODE = 7,	compute CSM prelaunch plane-change maneuver sequence
IDO	maneuver sequence flag; when
MODE = 1 and	
IDO = -1,	compute plane-change maneuver only
IDO = 0,	compute plane change and circularization maneuver
IDO = 1,	compute plane-change maneuver combined with the first maneuver of a CSM two-maneuver sequence to circularize the CSM orbit at an input altitude.
MODE = 2 and	
IDO = 0,	compute CSM maneuver to establish an apsis and an input altitude at the DOI maneuver point

IDO = 1, compute CSM maneuver to circularize orbit
at an input altitude

MODE = 3 and

IDO = -1, compute CSM two-maneuver sequence with
the first maneuver performed at an input
time and the second maneuver performed at
an input altitude to circularize the orbit

IDO = 1, compute CSM two-maneuver sequence with the first
maneuver performed at an apsis and the second
maneuver performed at an input altitude to cir-
cularize the orbit

MODE = 5 and

IDO = -1, compute CSM three-maneuver sequence so that
the first maneuver is a plane change and the
following pair is a double Hohmann to a
circular orbit at an input altitude

IDO = 0, compute CSM three-maneuver sequence so that
the first maneuver initiates a double Hohmann,
the second is a plane change, and the third
completes the double Hohmann to a circular
orbit at an input altitude.

IDO = 1, compute CSM three-maneuver sequence so that
the first two maneuvers constitute a double
Hohmann to a circular orbit at an input
altitude and the third is a plane change.

I_{PD} powered-descent simulation flag

IPD = 0, simulate powered descent

IPD = 1, do not simulate powered descent

I_{AZ} descent azimuth flag

I_{AZ} = 0, descent azimuth is not specified

I_{AZ} = 1, descent azimuth is specified

I_{TPD} powered-descent time flag

I_{TPD} = 0, let powered descent compute time to ignite

I_{TPD} = 1, input time for Powered-descent ignition

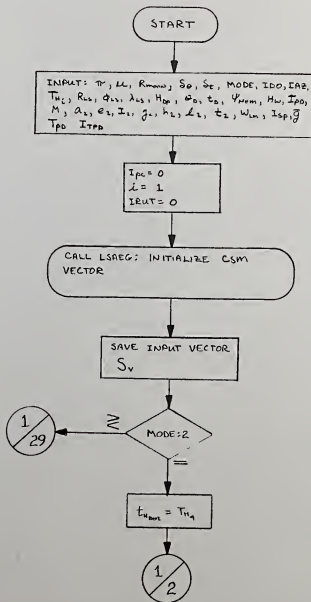
T_{PD}	time for powered descent ignition
TH	table of threshold times
M	number of dwell orbits desired between DOI and powered-descent ignition
$R_{IS}, \phi_{IS}, \lambda_{IS}$	radius, latitude, and longitude of the desired landing site
H_{DP}	altitude of point of descent ignition
θ_D	powered-flight arc of descent
t_D	powered-flight time of descent
ψ_{nom}	descent azimuth desired
H_W	altitude wanted at apsis
I_{SP}	average specific impulse of IM descent engine
W_{IM}	initial weight of IM
$\left. \begin{matrix} a_2, e_2, I_2, \epsilon_2 \\ h_2, \lambda_2, t_2 \end{matrix} \right\}$	CSM state vector and time

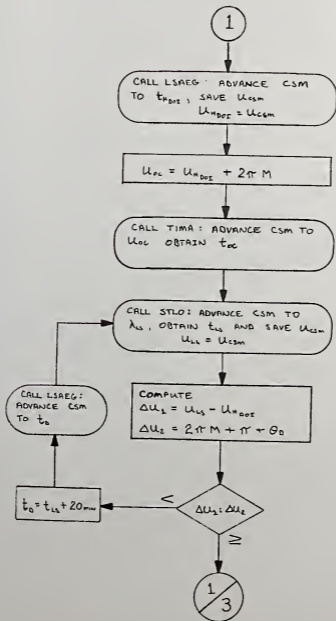
Output Variables

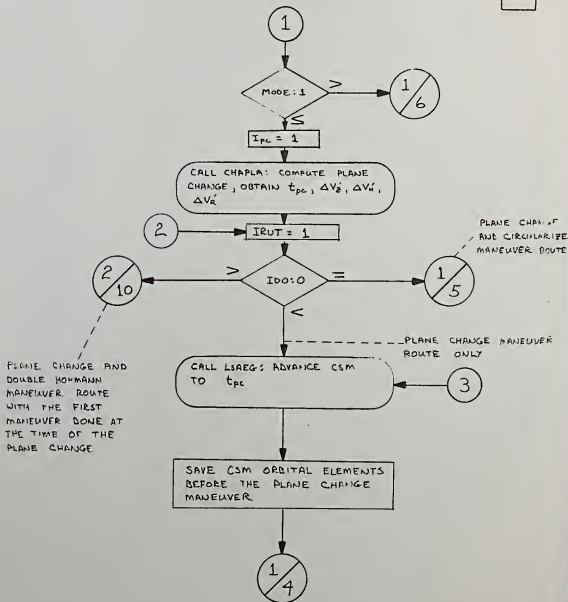
i	number of maneuver computed
ΔV_i	delta V costs of each maneuver
Y_i	yaw angle of each maneuver
P_i	pitch angle of each maneuver
T_{Mi}	time of each maneuver

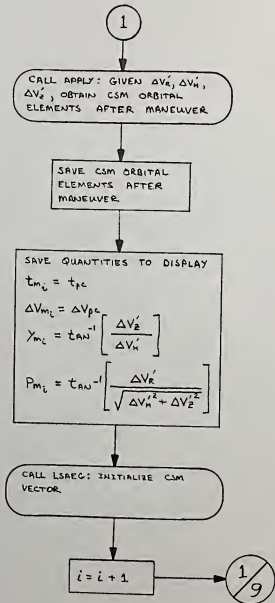
LDPP FLOW CHART

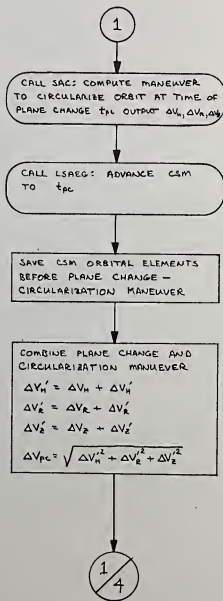
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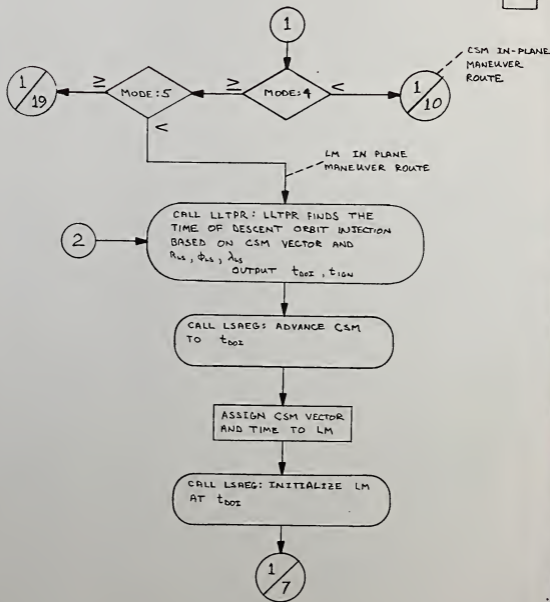


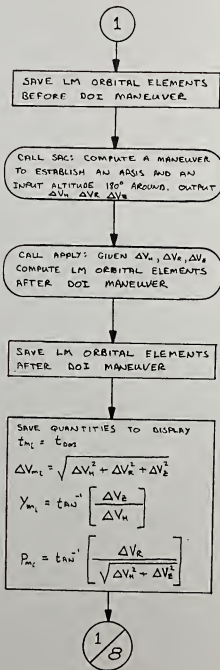


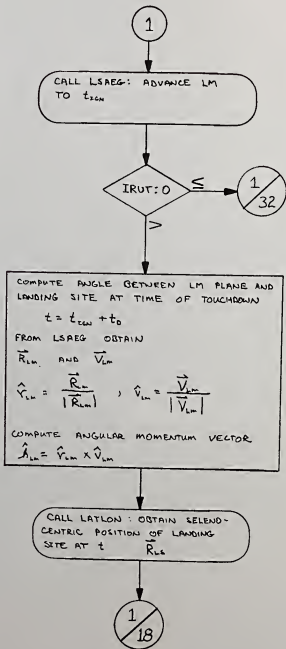


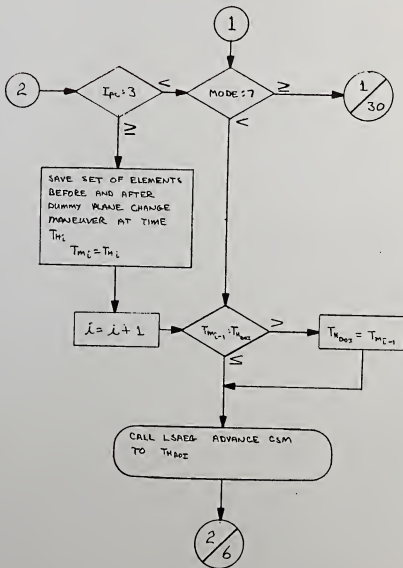


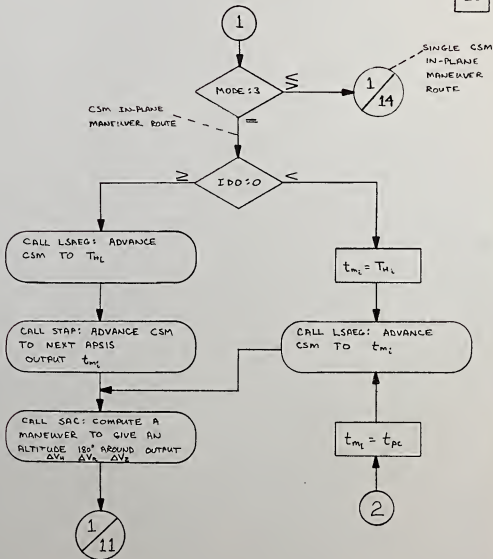


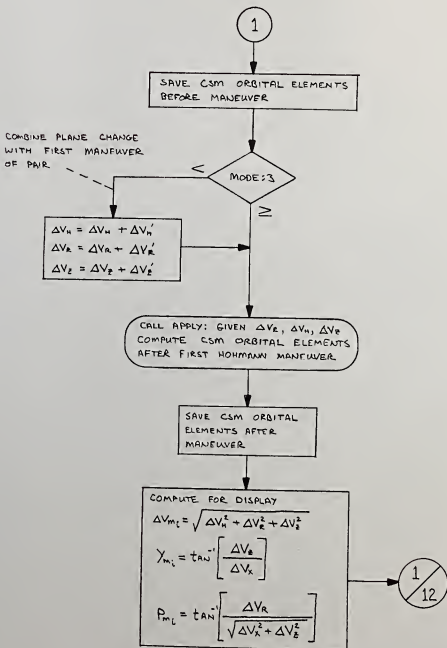


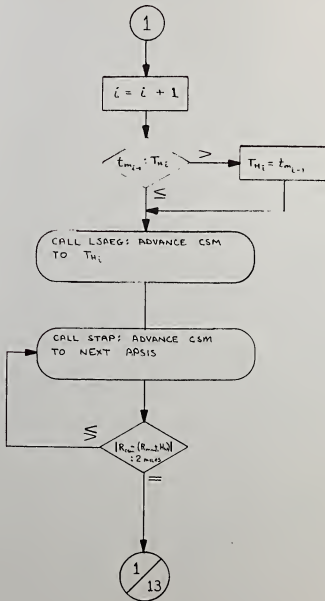


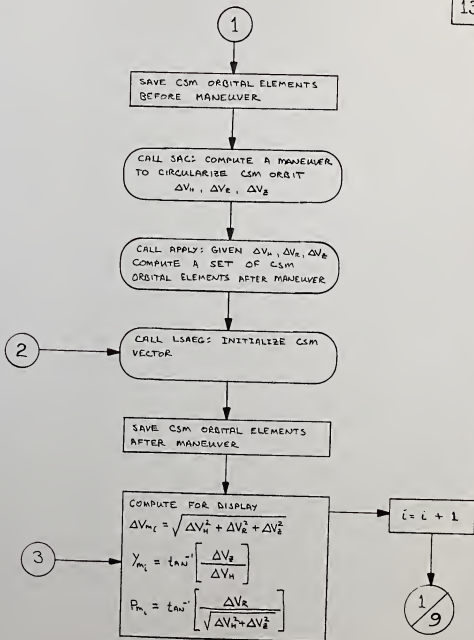


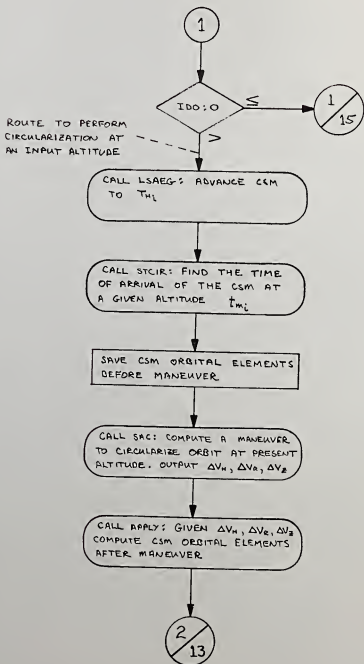


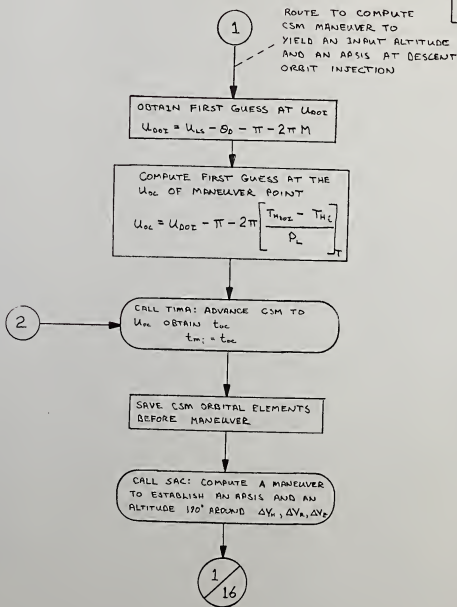


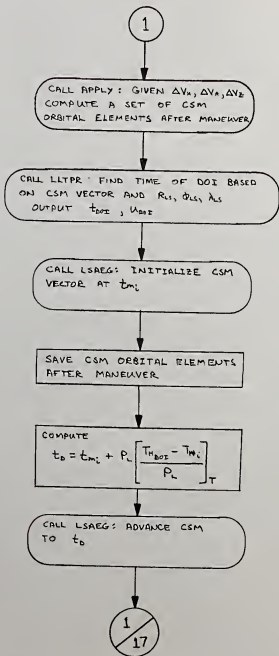


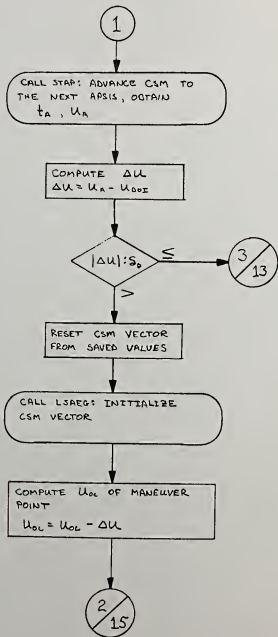












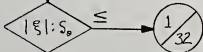
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COMPUTE \hat{r}_p , A UNIT VECTOR THROUGH THE POINT OF CLOSEST APPROACH, WHICH IS THE PROJECTION OF \vec{r}_{L_1} IN THE LM PLANE

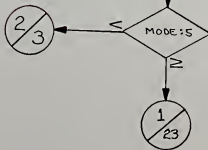
$$\hat{r}_s = \frac{\vec{r}_{L_1}}{|\vec{r}_{L_1}|} \quad ; \quad \vec{Q} = \hat{r}_{s3} \times \hat{h}_{lm}$$

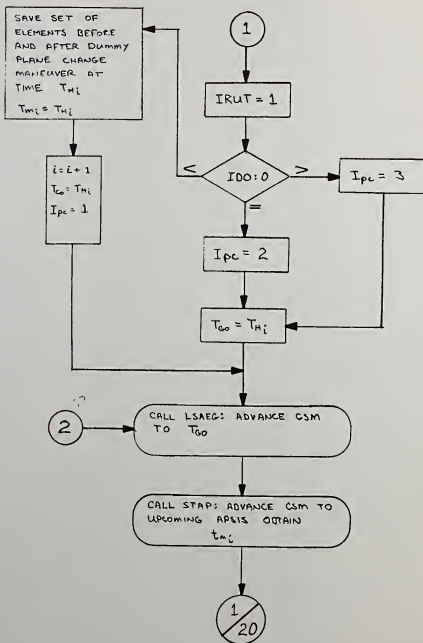
$$\hat{c} = \frac{\vec{Q}}{|\vec{Q}|} \quad ; \quad \hat{r}_p = \hat{h}_{lm} \times \hat{c}$$

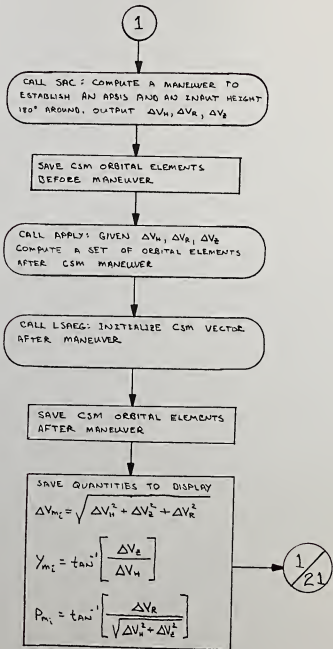
$$\hat{r}_p = \frac{\vec{r}_p}{|\vec{r}_p|} \quad ; \quad \xi = \cos^{-1}[\hat{r}_p \cdot \hat{r}_{s3}]$$

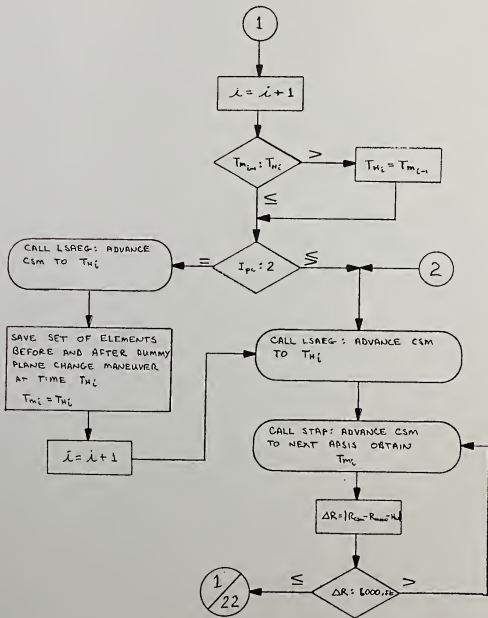


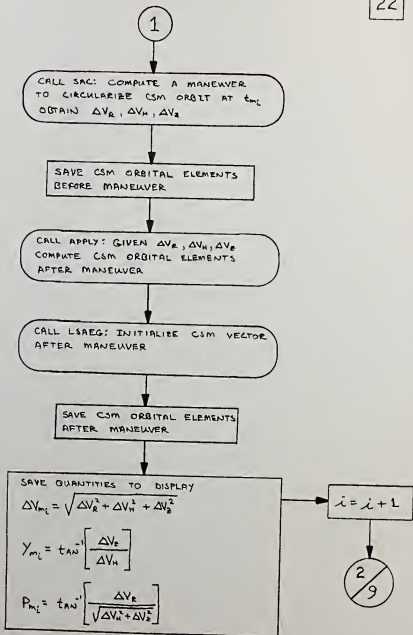
CALL CHARLA; COMPUTE NEW PLANE.
CHANGE MANEUVER, OBTAIN t_{pc} , ΔV_{L_1} , ΔV_{L_2}

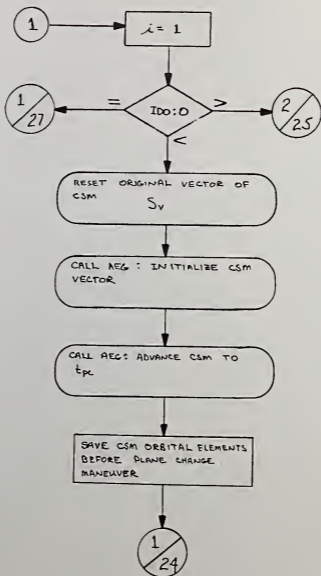


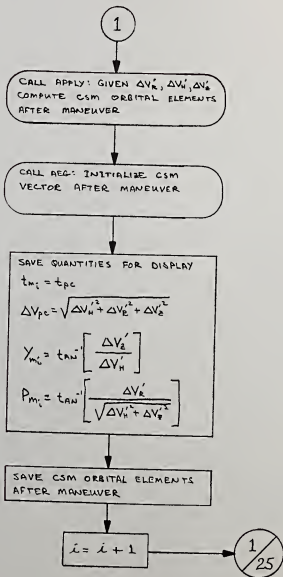


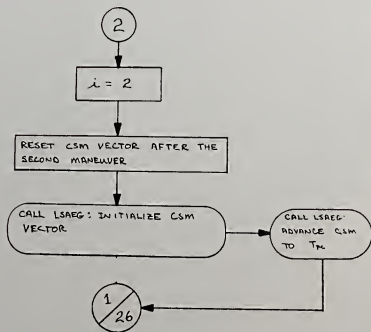
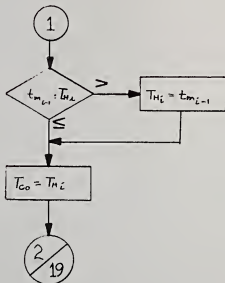


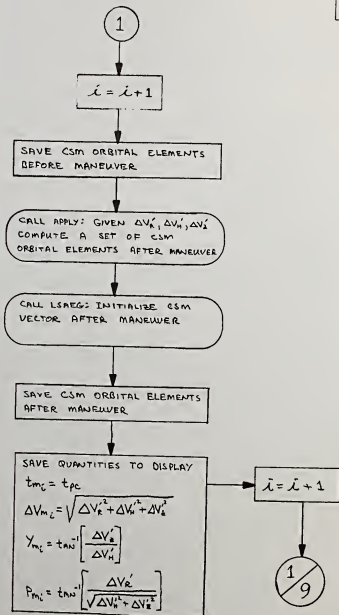


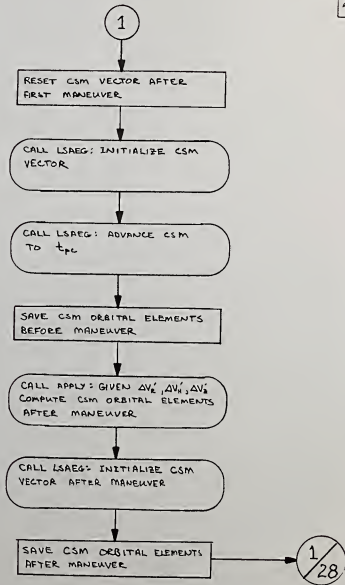


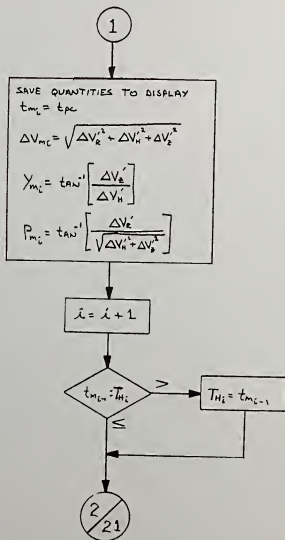


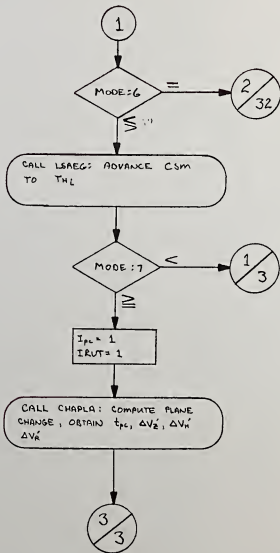


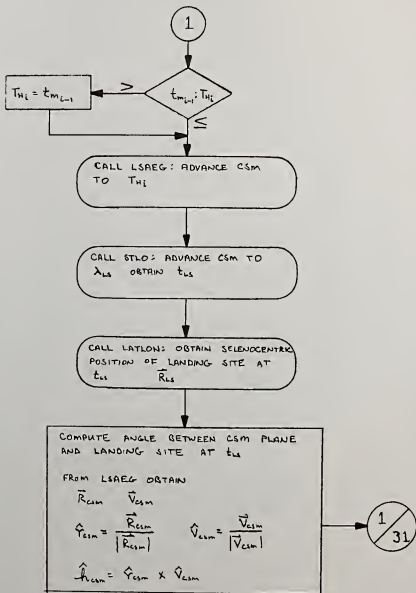


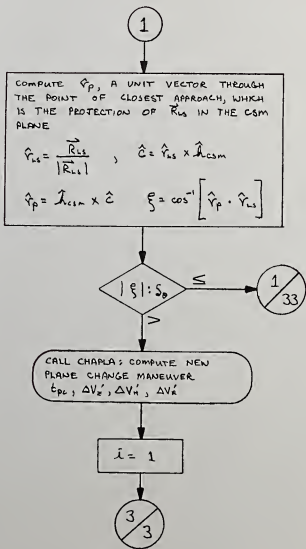


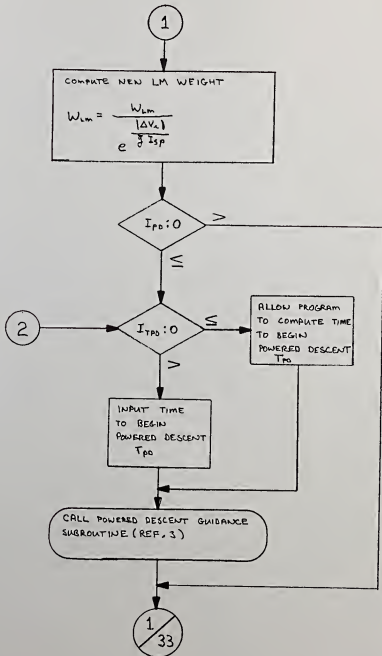


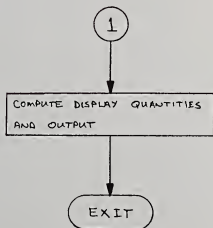












APPENDIX B
SAC FLOW CHART

SYMBOLS FOR SAC FLOW CHART

Input Constants

π 3.141592...
 μ lunar gravitational potential
 R_{moon} mean lunar radius

Input Variables

L vehicle number; if
 L = 1, the IM is maneuvering
 L = 2, the CSM is maneuvering

H_W height wanted at an apsis, or circular altitude wanted

J routine flag; if
 J = 0, compute maneuver to yield H_W at an apsis 180° away from maneuver
 J = 1, compute maneuver to circularize at input altitude

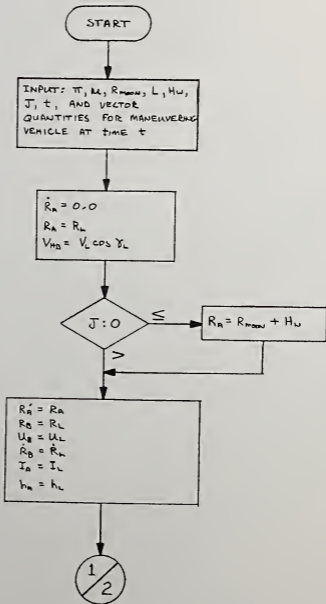
t time of maneuver

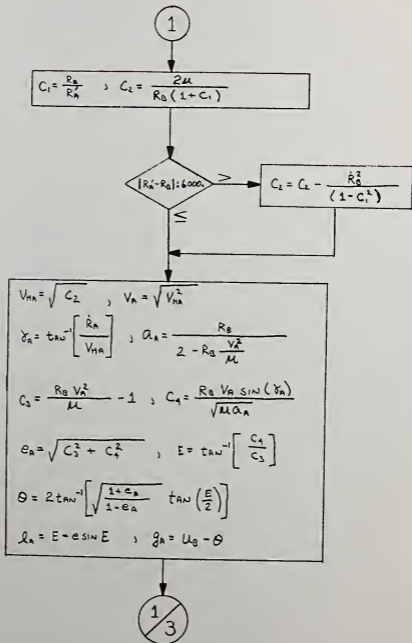
ISAEG vector input for maneuvering vehicle at time t

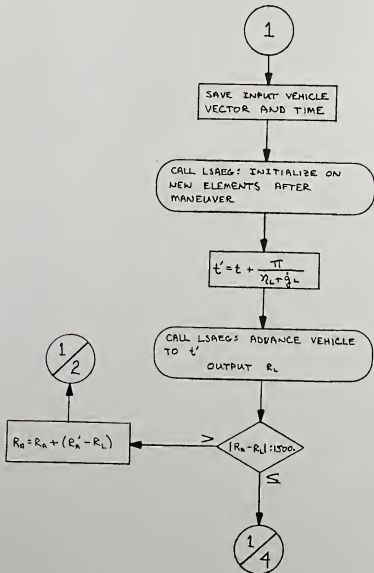
Output Variables

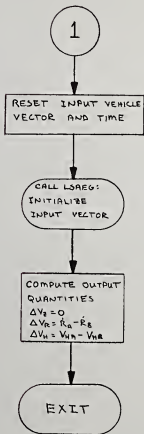
$\left. \begin{array}{l} \Delta V_H, \Delta V_R, \\ \Delta V_Z \end{array} \right\}$ delta V costs in platform coordinate systems

SAC FLOW CHART









APPENDIX C
CHAPLA FLOW CHART

SYMBOLS FOR CHAPLA FLOW CHART

Input Constants

π 3.141592...
 C_t iteration tolerance or time

Input Variables

L vehicle number, if
 L = 1, IM is maneuvering
 L = 2, CSM is maneuvering
 IWA flag that determines azimuth; if
 IWA = 0, the azimuth is not specified
 IWA = 1, the azimuth is specified
 I number of maneuvers in sequence
 I_{PC} number of the plane-change maneuver
 I_{GO} input flag
 IGO = 0, compute plane change as if it were only maneuver
 being done
 IGO = 1, compute plane change as part of maneuver
 sequence
 ψ_{nom} descent azimuth desired
 $\left. \begin{matrix} R_{IS}, \phi_{IS}, \\ \lambda_S \end{matrix} \right\}$ radius, latitude, and longitude of desired landing site
 E_i, k, j table of elements before and after all maneuvers in
 sequence
 i = number of maneuver
 k = before or after index (k = 1, elements before;
 k = 2, elements after)
 j = element counter
 $\left. \begin{matrix} T_M \\ (i = 1, I) \end{matrix} \right\}$ table of maneuver times

T_{H_1} ($k = 1, I$) table of threshold times

$\left. \begin{array}{l} a_L, e_L, l_L, \\ s_L, h_L, t_L, t_L \end{array} \right\}$ maneuvering vehicle state vector and time

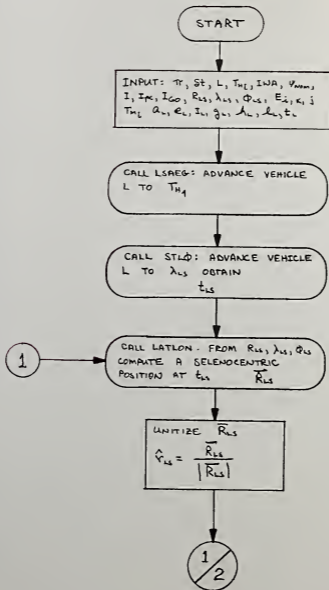
Output Variables

$\Delta V_H, \Delta V_R, \Delta V_Z$ maneuver delta V costs in platform coordinate system

t_m maneuver time

CHAPLA FLOW CHART

1



1

FROM AEG OBTAIN

$$\vec{R}_L = (x_L, y_L, z_L)$$

$$\vec{V}_L = (\dot{x}_L, \dot{y}_L, \dot{z}_L)$$

UNITIZE \vec{R}_L AND \vec{V}_L

$$\hat{r}_L = \frac{\vec{R}_L}{|\vec{R}_L|} \quad ; \quad \hat{v}_L = \frac{\vec{V}_L}{|\vec{V}_L|}$$

COMPUTE ANGULAR MOMENTUM VECTOR

$$\vec{H}_L = \hat{r}_L \times \hat{v}_L \quad ; \quad \hat{h}_L = \frac{\vec{H}_L}{|\vec{H}_L|}$$

COMPUTE \hat{r}_p , A UNIT VECTOR THROUGH THE POINT OF CLOSEST APPROACH, WHICH IS THE PROJECTION OF \vec{R}_L IN THE COM PLANE

$$Q = \hat{r}_L \times \hat{h}_L \quad , \quad \hat{c} = \frac{Q}{|Q|}$$

$$\vec{R}_p = \hat{h}_L \times \hat{c} \quad , \quad \hat{r}_p = \frac{\vec{R}_p}{|\vec{R}_p|}$$

1
3

1

COMPUTE ANGULAR DISTANCE VEHICLE
IS AWAY FROM THE POINT OF
CLOSEST APPROACH

 θ

$$\theta = \cos^{-1} [\hat{r}_p \cdot \hat{r}_L]$$

TO DETERMINE THE SIGN ON θ ,

$$\vec{h}_0 = \hat{r}_L \times \hat{r}_p, \quad \hat{h}_0 = \frac{\vec{h}_0}{|\vec{h}_0|}$$

OBTAIN THE SIGN ON THE Z
COMPONENT OF \hat{h}_0 AND \hat{r}_L

$$s_1 = \frac{h_{0z}}{|h_{0z}|} \quad s_2 = \frac{r_{Lz}}{|r_{Lz}|}$$

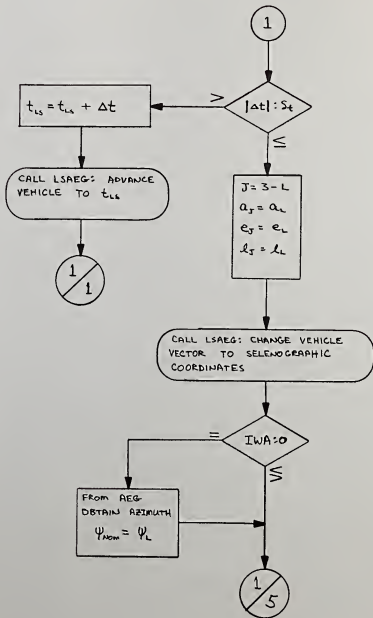
SO THAT

$$\theta = \theta \left[\frac{s_1}{s_2} \right]$$

NOW COMPUTE Δt

$$\Delta t = \frac{\theta}{\dot{\theta}_L}$$

1
4



1

COMPUTE INCLINATION, NODE, AND
ARGUMENT OF PERIGEE FOR DUMMY
ORBIT

$$I_J = \cos^{-1}(\sin \psi_{nom} \cos \phi_{LS})$$

$$u_w = \tan^{-1} \left[\frac{\sin \phi_{LS} \sin \psi_{nom}}{-\cos I_J \cos \psi_{nom}} \right]$$

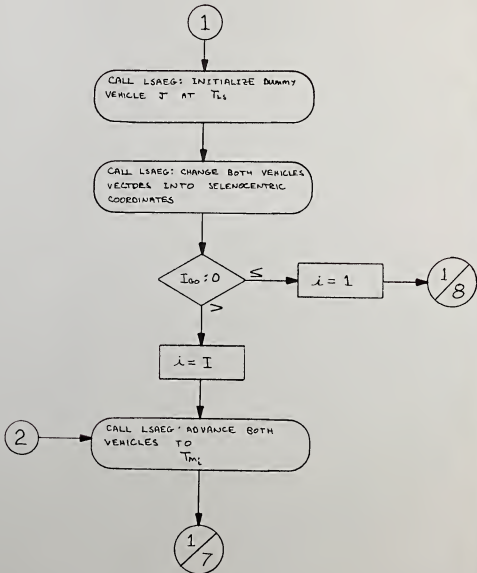
MAKE $u_w > 0$

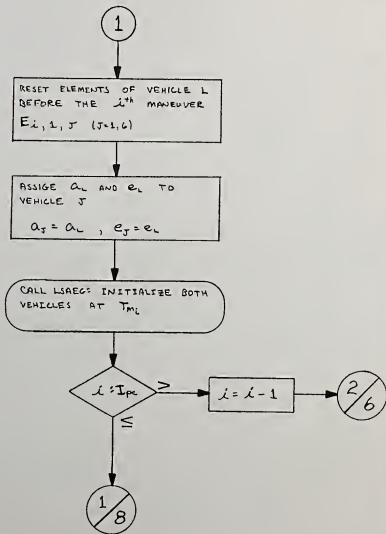
$u_w < 2\pi$

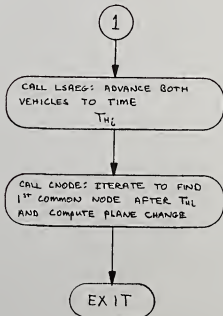
$$h_J = h_{LS} - u_w + 2 \tan^{-1} \left[\tan \frac{\phi_{LS}}{2} \left\{ \frac{\sin \left(\frac{1}{2} (\psi_{nom} - \frac{\pi}{2}) \right)}{\sin \left(\frac{1}{2} (\psi_{nom} + \frac{\pi}{2}) \right)} \right\} \right]$$

$$g_J = g_L - 2 \tan^{-1} \left[\tan \left(\frac{h_J - h_L}{2} \right) \left\{ \frac{\sin \left(\frac{1}{2} (\pi - I_J - I_L) \right)}{\sin \left(\frac{1}{2} (\pi - I_J + I_L) \right)} \right\} \right]$$

~~1~~
6







APPENDIX D
LITPR FLOW CHART

SYMBOLS FOR LLTPR FLOW CHART

Input Constants

π	3.141592...
μ	lunar gravitational potential
R_{moon}	mean lunar radius
$\delta\theta$	angular iteration tolerance

Input Variables

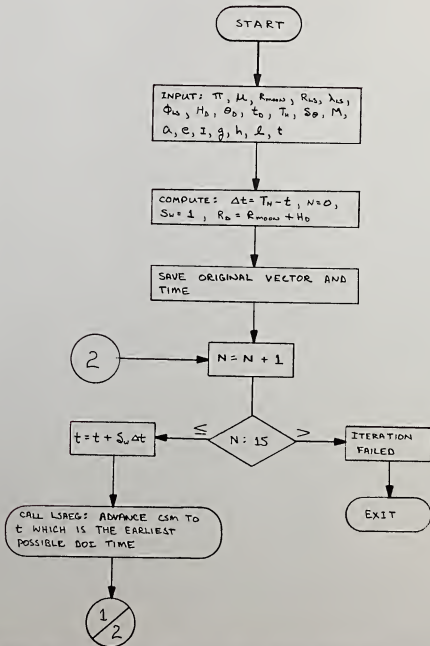
$R_{\text{IS}}, \lambda_{\text{IS}}, \phi_{\text{IS}}$	} position of desired landing site
H_{D}	height of descent ignition
θ_{D}	powered-flight arc of descent
t_{D}	powered-flight time of descent
T_{H}	threshold time for descent
a, e, I, g, h, ℓ, t	} CSM state vector and time
M	number of dwell orbits desired between DOI and descent ignition

Output Variable

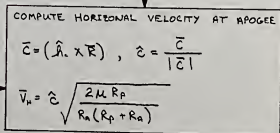
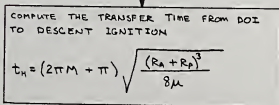
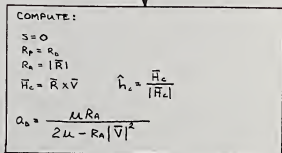
t_{DOI}	time of descent orbit injection
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FLOW CHART OF LLTPR

1

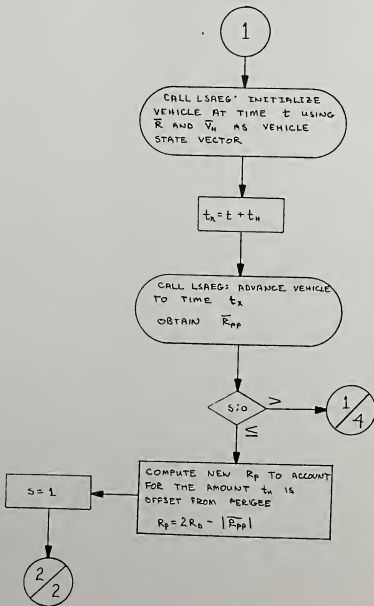


1

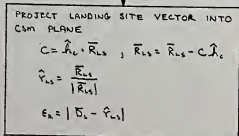
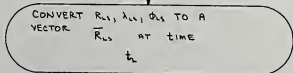
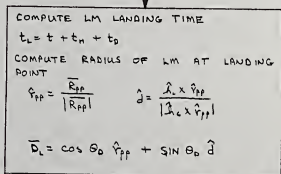


2

1/3

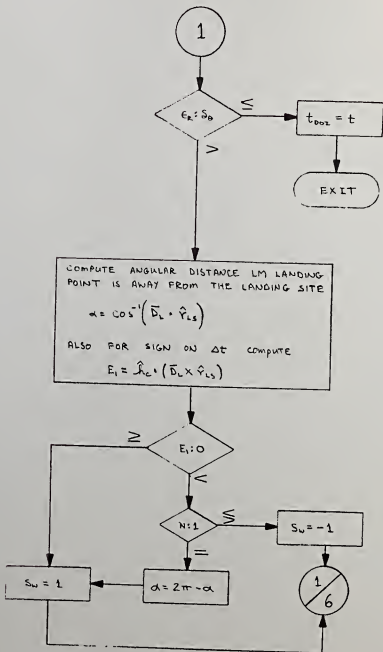


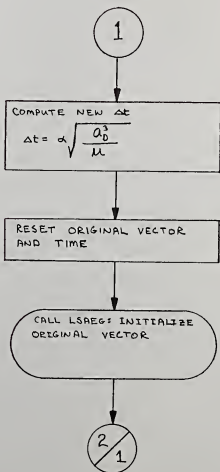
1



1

5





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