

# Better Consensus In The Bitcoin Model

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# Blockchains: Origin & Today

## Bitcoin: A Peer-to-Peer Electronic Cash System

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**Abstract.** A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone.

### 1. Introduction

Commerce on the Internet has come to rely almost exclusively on financial institutions serving as trusted third parties to process electronic payments. While the system works well enough for most transactions, it still suffers from the inherent weaknesses of the trust based model. Completely non-reversible transactions are not really possible, since financial institutions cannot avoid mediating disputes. The cost of mediation increases transaction costs, limiting the minimum practical transaction size and cutting off the possibility for small casual transactions, and there is a broader cost in the loss of ability to make non-reversible payments for non-reversible services. With the possibility of reversal, the need for trust spreads. Merchants must be wary of their customers, hassling them for more information than they would otherwise need. A certain percentage of fraud is accepted as unavoidable. These costs and payment uncertainties can be avoided in person by using physical currency, but no mechanism exists to make payments over a communications channel without a trusted party.

What is needed is an electronic payment system based on cryptographic proof instead of trust, allowing any two willing parties to transact directly with each other without the need for a trusted third party. Transactions that are computationally impractical to reverse would protect sellers from fraud, and routine escrow mechanisms could easily be implemented to protect buyers. In this paper, we propose a solution to the double-spending problem using a peer-to-peer distributed timestamp server to generate computational proof of the chronological order of transactions. The system is secure as long as honest nodes collectively control more CPU power than any cooperating group of attacker nodes.

## Top 100 Cryptocurrencies by Market Capitalization

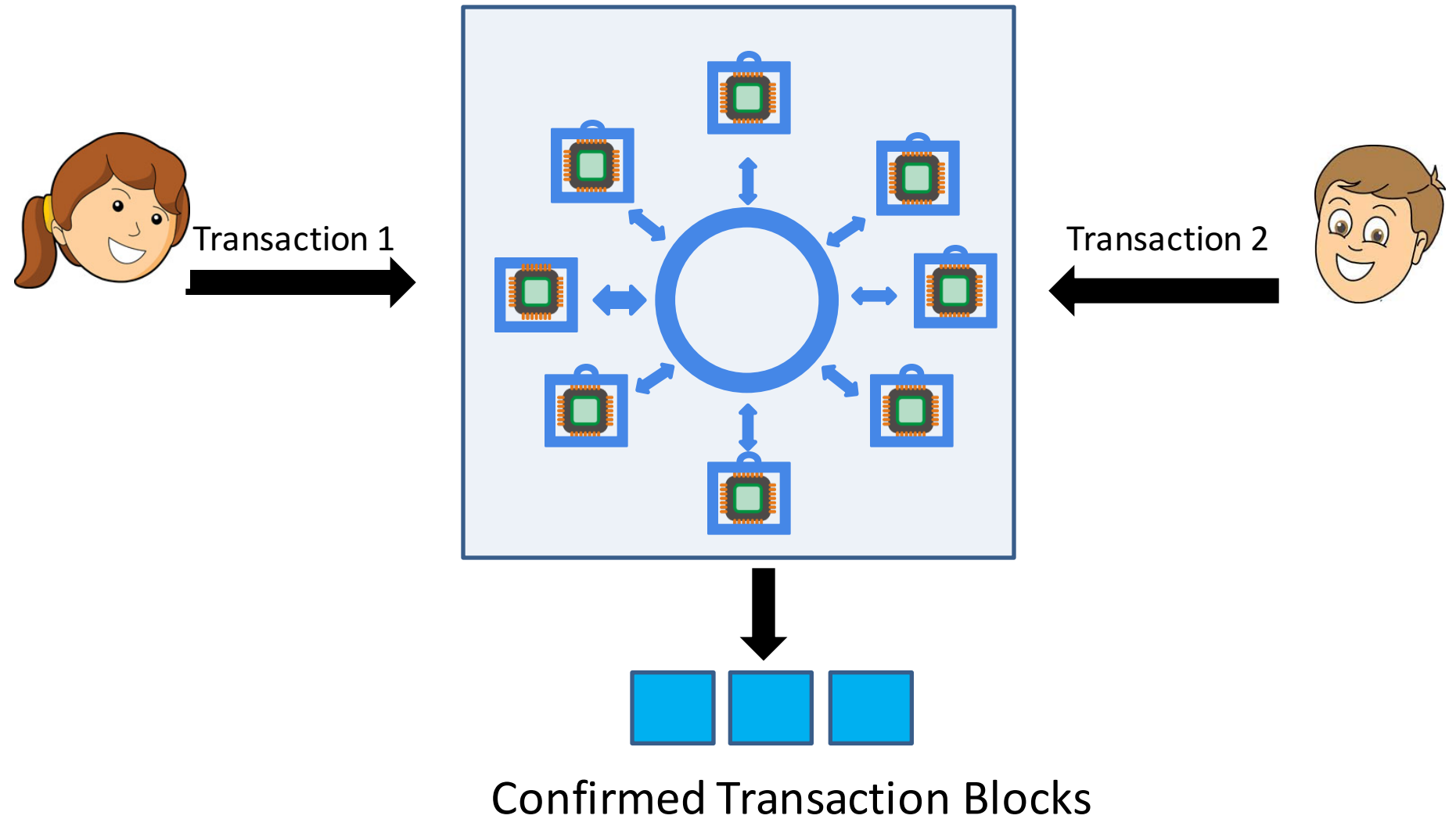
Cryptocurrencies ▾		Exchanges ▾	Watchlist	USD ▾	Next 100 →	View All	
#	Name	Market Cap	Price	Volume (24h)	Circulating Supply	Change (24h)	Price Graph (7d)
1	Bitcoin	\$59,580,761,374	\$3,399.59	\$4,939,435,528	17,525,862 BTC	-0.49%	
2	XRP	\$12,001,134,334	\$0.291508	\$356,976,506	41,169,202,069 XRP *	-0.25%	
3	Ethereum	\$10,974,571,873	\$104.75	\$2,280,623,059	104,766,118 ETH	-0.48%	
4	EOS	\$2,126,001,619	\$2.35	\$472,575,374	906,245,118 EOS *	-0.64%	
5	Bitcoin Cash	\$2,041,982,753	\$115.96	\$198,734,194	17,609,650 BCH	0.05%	
6	Tether	\$2,026,509,895	\$1.00	\$3,511,890,558	2,021,103,317 USDT *	0.10%	
7	Litecoin	\$2,000,776,268	\$33.14	\$636,413,250	60,369,927 LTC	0.12%	
8	TRON	\$1,712,362,099	\$0.025684	\$136,340,725	66,671,422,606 TRX	-0.61%	
9	Stellar	\$1,422,240,776	\$0.074196	\$114,737,113	19,168,570,823 XLM *	0.28%	
10	Binance Coin	\$1,101,770,088	\$7.80	\$84,783,682	141,175,490 BNB *	-4.79%	
11	Bitcoin SV	\$1,091,169,120	\$61.97	\$83,503,727	17,608,711 BSV	-1.61%	
12	Cardano	\$940,904,576	\$0.036290	\$12,298,410	25,927,070,538 ADA *	-0.51%	
13	Monero	\$777,519,153	\$43.36	\$46,156,605	16,777,423 XMR	0.27%	

2008

2019

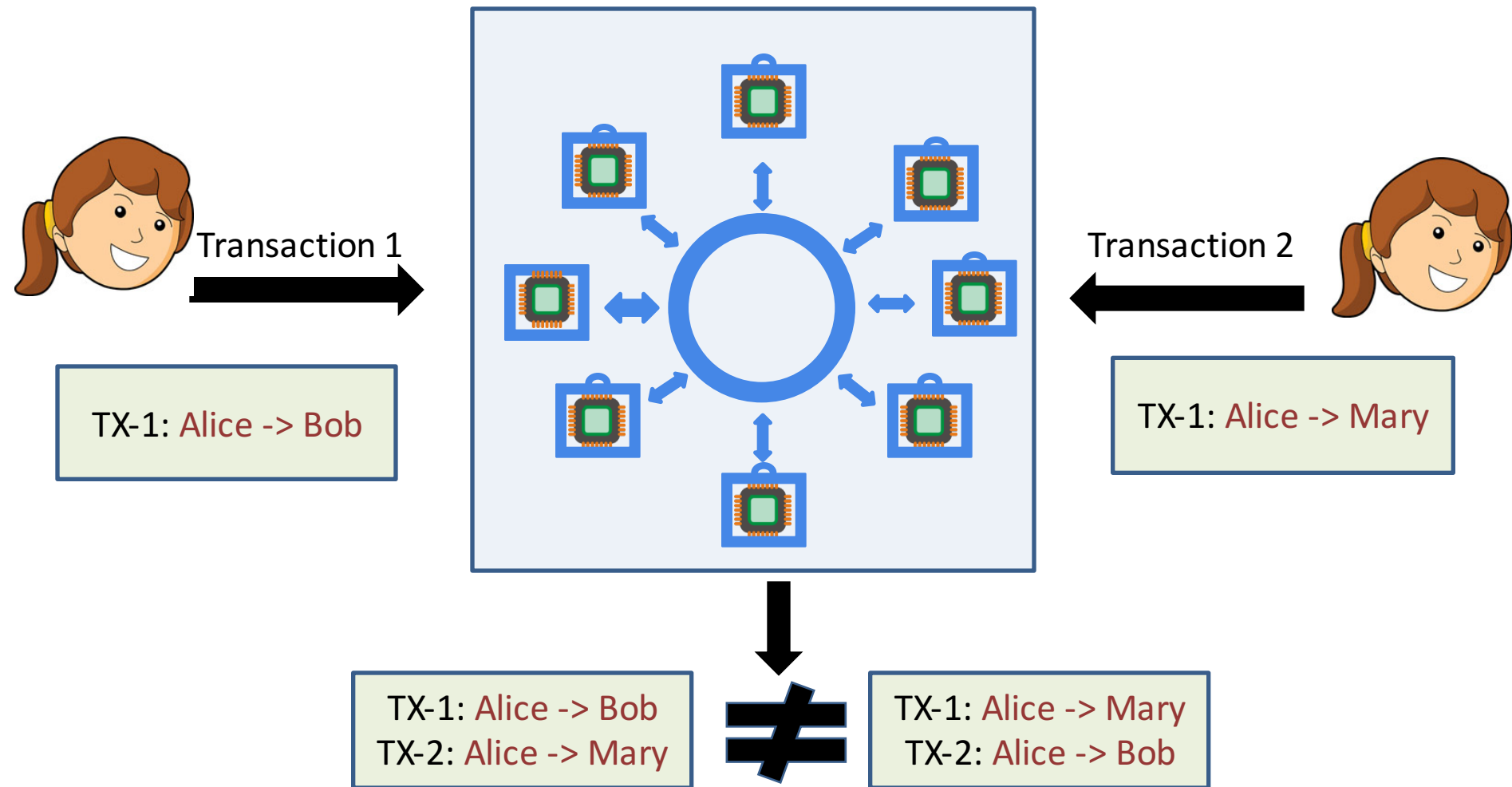
# The Blockchain Consensus Problem

# The Problem



# Key Challenge:

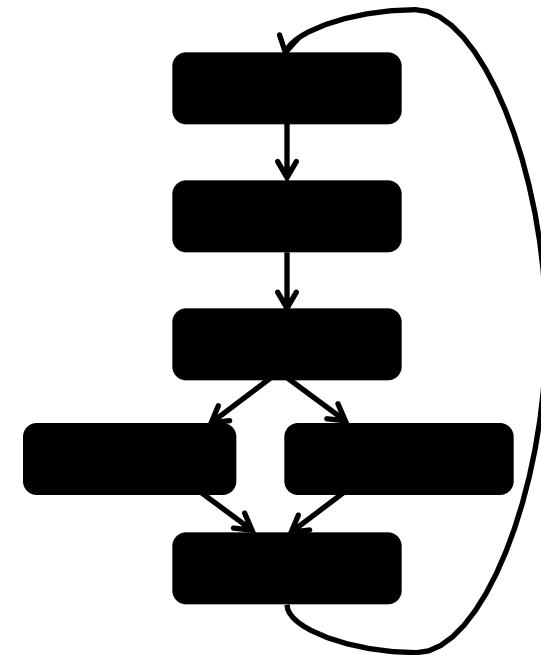
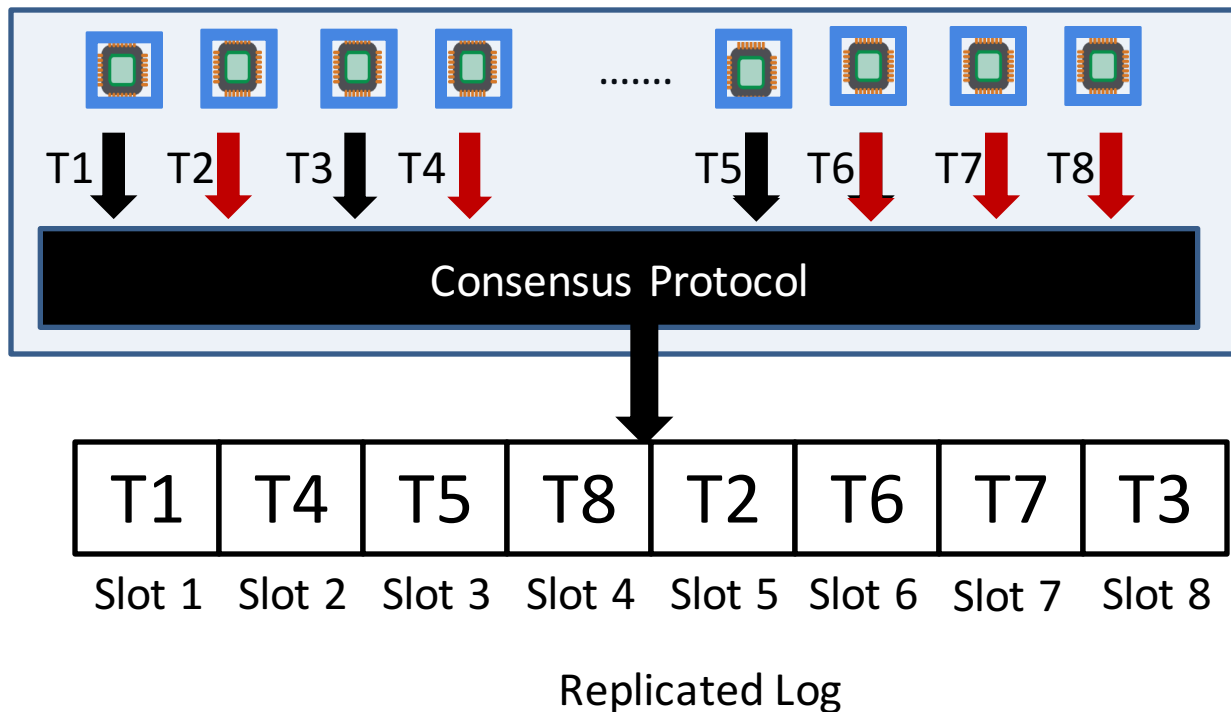
## Agreement over Transaction Ordering



Ordering Transactions is sufficient to prevent double-spends!

# Why Total Order?

- Replicated State Machines [*Lamport84, Schnieder90*]
  - Useful for backups, snapshots, distributed locks, ...
  - A sequence of commands transition from state to state



Deterministic  
State Machine

# Enables General-Purpose Computing

The screenshot displays the IDEX trading platform interface. At the top, the Ethlance logo is on the left, and navigation links for "Participate in Ethlance's governance processes: [Introducing the district0x Network](#)" and "How it works" are on the right. Below this, there are tabs for "For Sale", "Siring", "Gen 0", and "All Kitties". A search bar and the IDEX logo are visible. The interface includes a navigation bar with "DAY" mode selected, and links for "ETH PRICE: \$600.23 USD", "GAS PRICE: 15 GWEI", "EXCHANGE", "HELP", "NEW WALLET", and "UNLOCK WALLET". A green banner promotes "Share in the success of IDEX and Aurora with the AURA staking token" with a "LEARN MORE" button.

The main content area is divided into several sections:

- MARKETS:** A table listing various cryptocurrencies with columns for Coin, Price, Vol, Chg, and Name.
- AURA / ETH:** A detailed view of the AURA/ETH trading pair, including a table with Last Price, 24hr H, 24hr L, and 24hr Change, and a 24hr Volume.
- PRICE CHART:** A candlestick chart for AURA/ETH with various time frame options (1, 5, 15, 30, 1h, 2h, 6h, 1h).
- QUICK BALANCES:** A section for managing balances.
- BENEFITS:** A section for viewing benefits.

Coin	Price	Vol	Chg	Name
NPXS	0.00001302	4792.14	-1.31%	Pundi X
PAI	0.0002724	1832.89	-9.73%	PCHAIN
HOT	0.00000161	1437.45	-2.31%	HoloToken
REM	0.00003410	928.18	+4.52%	REMME
COU	0.00000059	827.05	-11.53%	Couchain

Last Price	24hr H	24hr L	24hr Change
0.00032812	0.00033199	0.00031301	+1.27263483%

24hr Volume:	AURA /
126565.618941135184821425	40.98401658699487643...

**Over 5 million smart contracts!**

NEXO	0.00027119	456.52	-8.97%	Nexo
SNTR	0.00000039	436.72	+2.46%	SilentNotary
EXC	0.00126515	426.54	+3.23%	Eximchain
BKX	0.0004698	376.68	-3.18%	BANKEX
PMNT	0.00000807	362.02	+93.54%	Paymon
MAN	0.00124550	294.63	-1.49%	MATRIX A...

Volume (false, 20) 4.29 n/a

charts by TradingView

5y 1y 6m 3m 1m 5d 1d 17:22:15 (UTC-4) % log auto

# The Bitcoin Model

- Assumptions:
  - A trusted “genesis” block
  - No pre-established identities, joining is **permissionless**
  - Network is synchronous (Blocks transmitted within some delay)
- Security Properties:
  - **Safety:** Nothing bad happens
    - **Stability:** A block once confirmed can't be changed
    - **Agreement:** All miners order blocks same way
  - **Liveness:** Honest blocks are accepted eventually
  - **Fairness:** Your confirmed blocks are proportional to your computational power



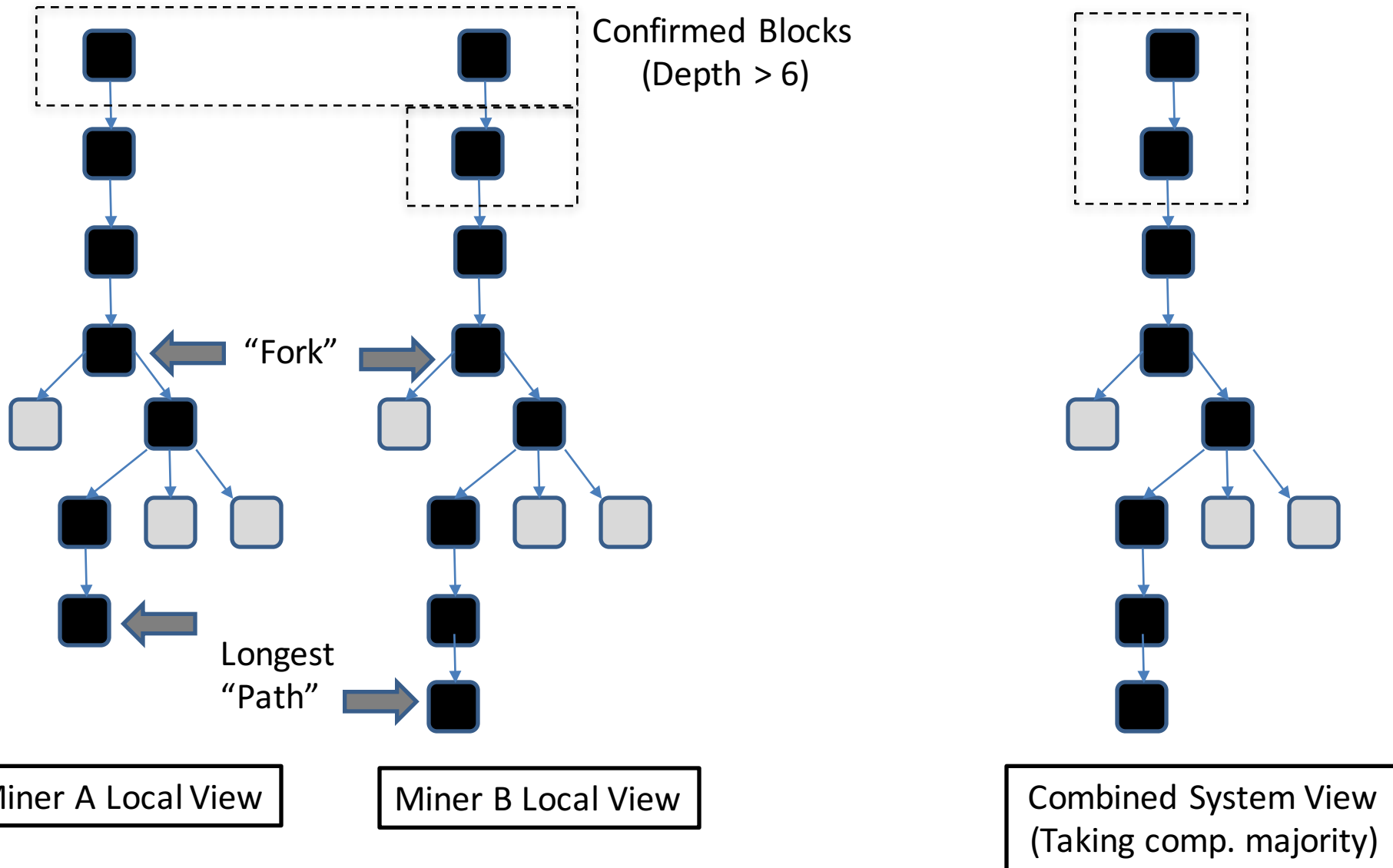
# Nakamoto Consensus Protocol

- Miners keep a local copy of the blockchain
- Miners solve a computational Proof-of-Work puzzle:



- Successful miners (usually one) broadcast solution
- Miners check the received solutions, and if valid:
  - Extend their chain with that block
- Confirm block on the longest chain after it is k-deep
  - Bitcoin proposes  $k = 6$

# Nakamoto Consensus: Overview



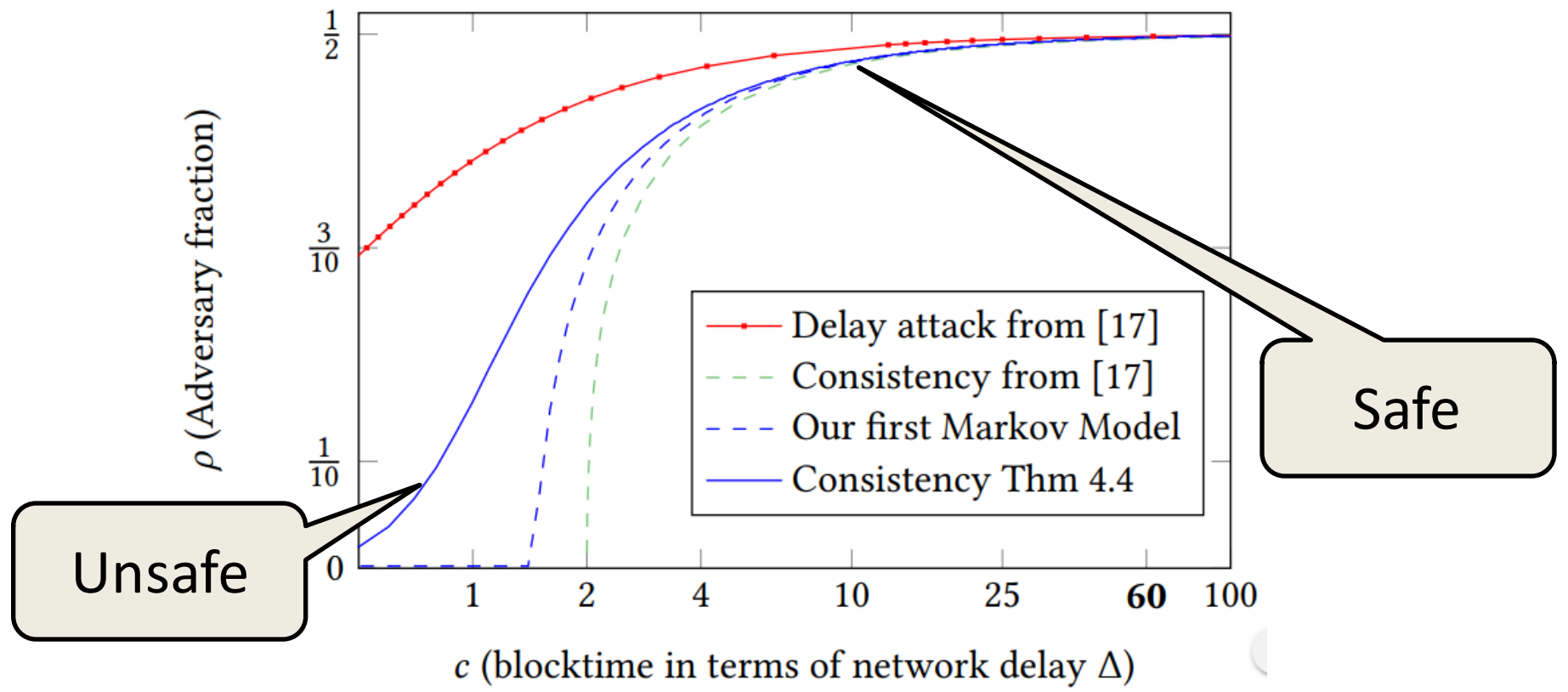
Can We Do Better?

# Fundamental Limits & Optimality: Latency

- Limit 1: *Block Propagation Delay* ( $\Delta$ )
- Optimal Transaction confirmation latency is  $\Theta(\Delta)$
- A random (ER) graph with  $N$  nodes and degree  $d$ 
  - Avg. hops between nodes =  $\boxed{(\log N)/(\log d)}$ 
    - Bitcoin  $N = 12,000$ ,  $d = 16$ , avg. hops = 3.36
    - Ethereum  $N = 35000$ ,  $d = 25$ , avg. hops = 3.25
    - (Hypothetical)  $N = 1M$ ,  $d=40$ , avg. hops = 4.29
  - $\Delta \sim \text{avg. hops} \times \text{hop latency}$ 
    - On Amazon EC2 (geo-distributed) about 1-2 seconds
    - Changes minimally with  $(N,d)$

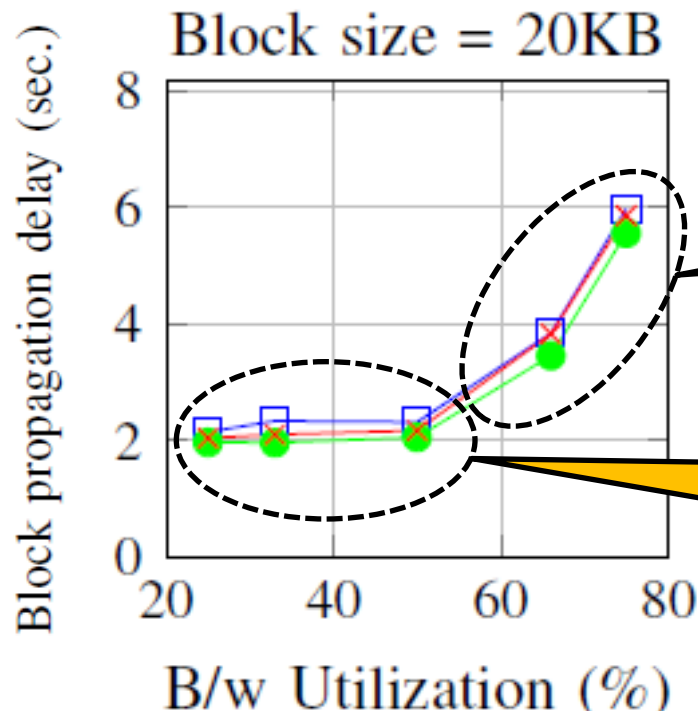
# Nakamoto Consensus: Safety & Liveness are Near-Optimal

- For Nakamoto consensus,
  - **Resilience** ( $f$ ) is “near-optimal” at blk. interval  $> 3\Delta$



# Fundamental Limits & Optimality: Throughput

- Limit 2: Broadcast Throughput ( $\beta$ )
- Transactions per second =  $\beta$  / transaction size
- An experiment showing  $\Delta$  (un)correlation with  $\beta$



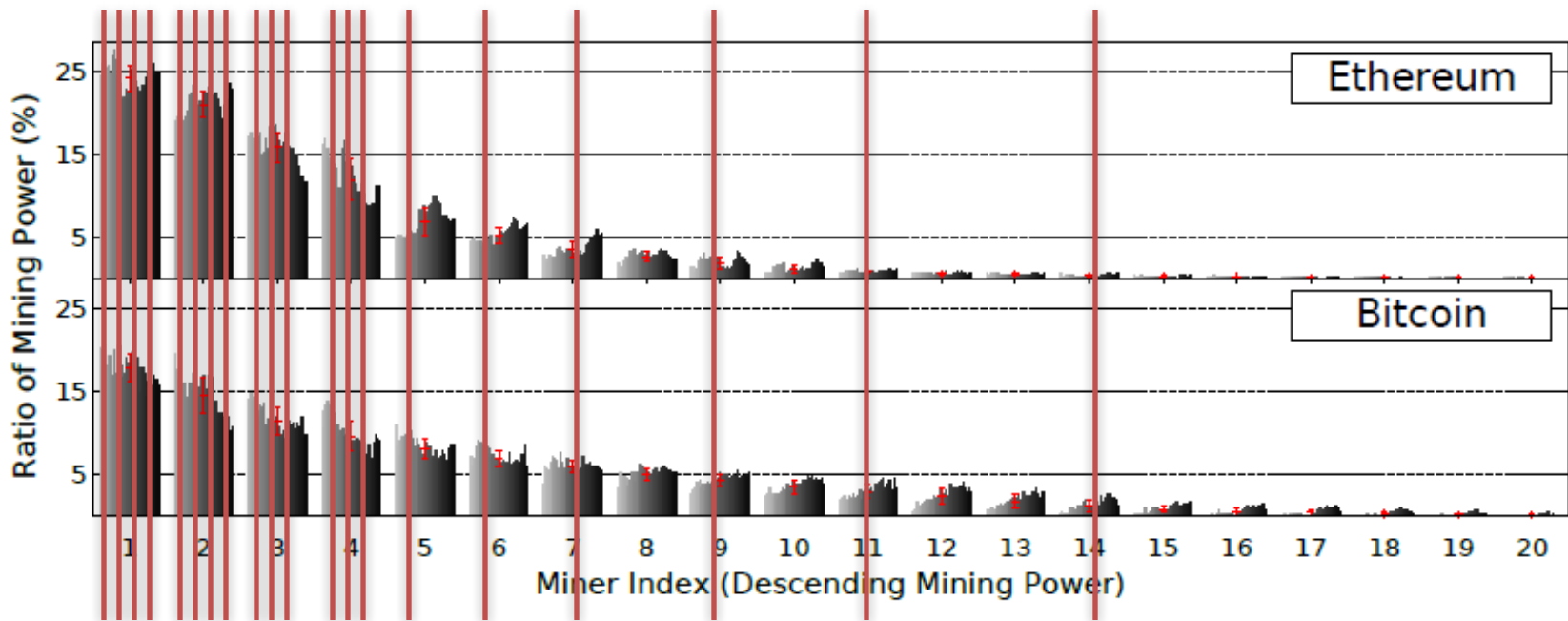
$\Delta$  increases linear to  $\beta$   
**(Bandwidth-bound)**

No increase in  $\Delta$  as  $\beta$  increases  
**(Latency-bound)**

—□— 8Mbps; —●— 16Mbps; —×— 20Mbps

# Fundamental Limits & Optimality: Decentralization

- In anonymous, permissionless setup
  - Mining concentration reflects “real” wealth distribution



- Goal of decentralization: Maximize miners/sec
- Optimal Decentralization is  $\Theta(\beta)$

# Nakamoto Consensus: Not Optimal In Throughput & Decentralization



- 2-4 Kilobytes / second
- 6-12 TXs per second
- 3-60 minutes latency

- Support limited computations
- Outages and Unavailability
- A cryptoKitties app clogged the entire network

**Demand from Practice: 1,200 - 50,000 TXs/s**

The PayPal logo, featuring the word 'PayPal' in a bold, italicized, sans-serif font with a trademark symbol.





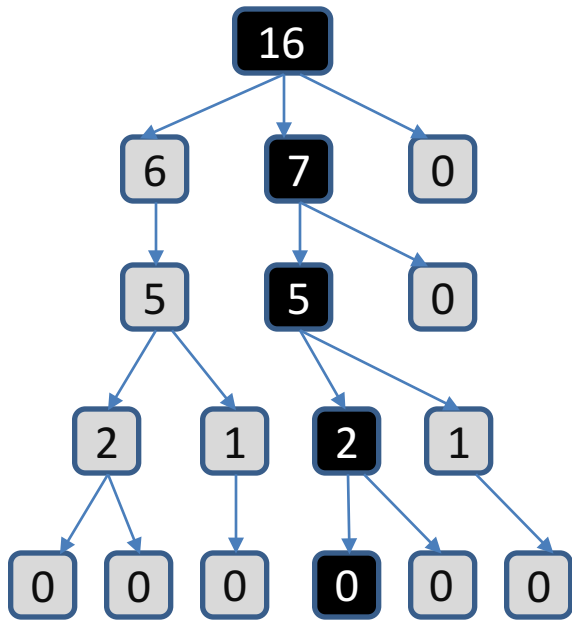
# Towards Better Consensus Protocols

# Extending Nakamoto: With Large Blocks

- Increase block size (e.g Bitcoin-NG)
  - May achieve near-optimal throughput, latency, resilience
    - Needs a careful implementation
  - Poor decentralization:
    - A single block proposer broadcasts tens of thousands of TXs
    - Number of miners participating is not  $\Theta(\beta)$

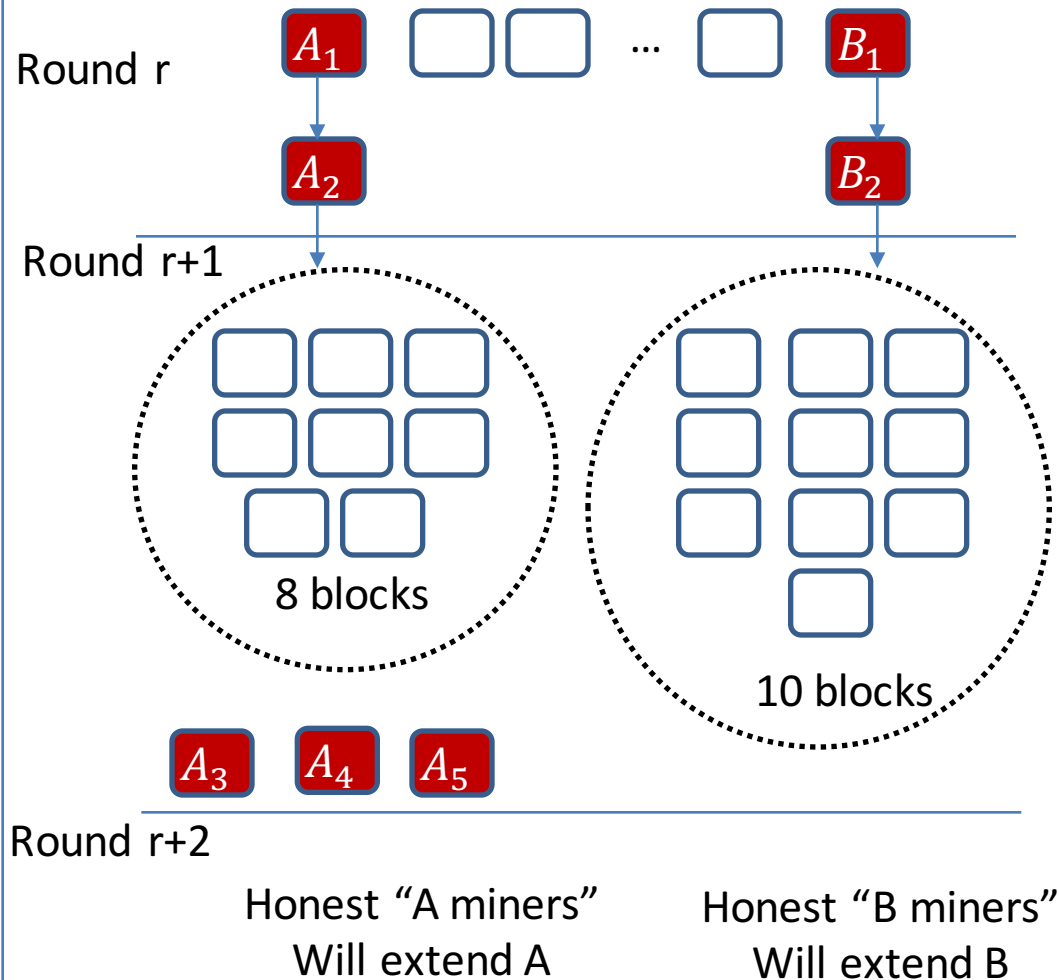
# Extending Nakamoto With Smaller Block Interval

## The GHOST protocol

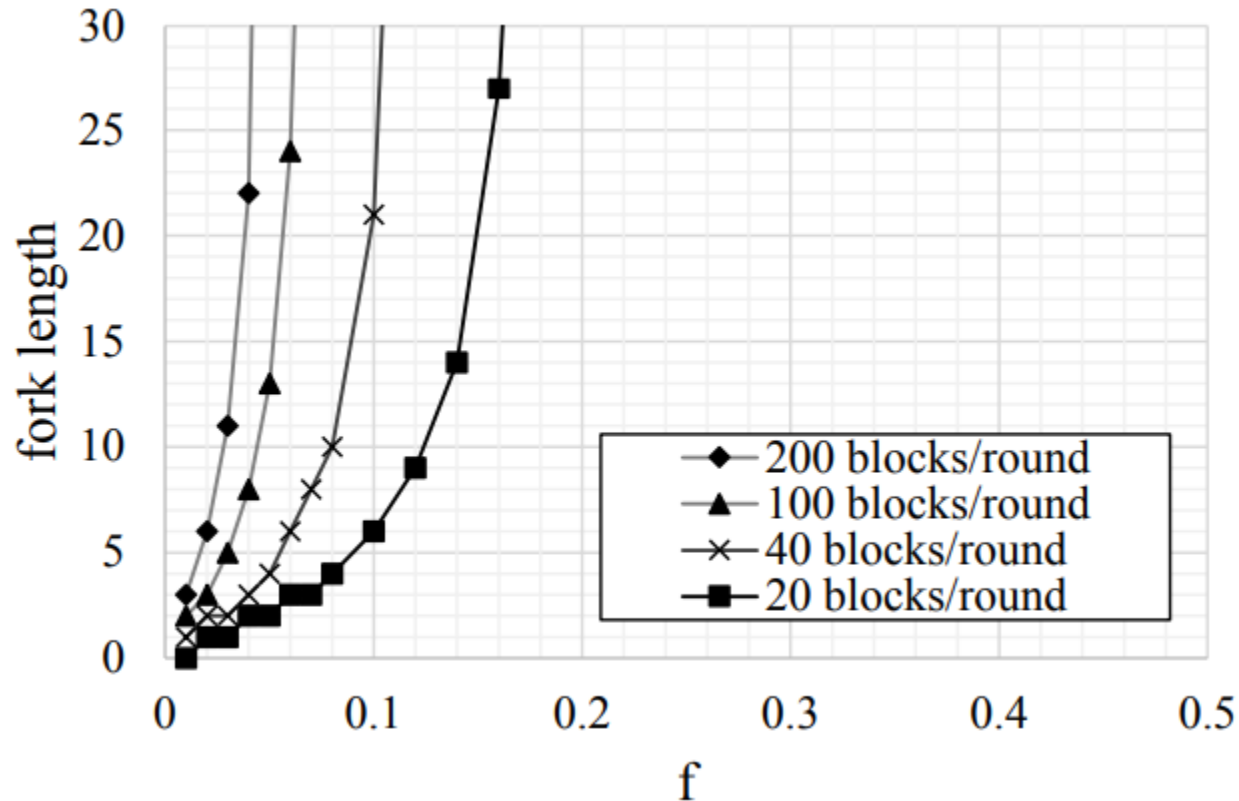


“Heaviest” rather than longest chain

## Active Balancing Attack on GHOST



# Attack Effectiveness on GHOST

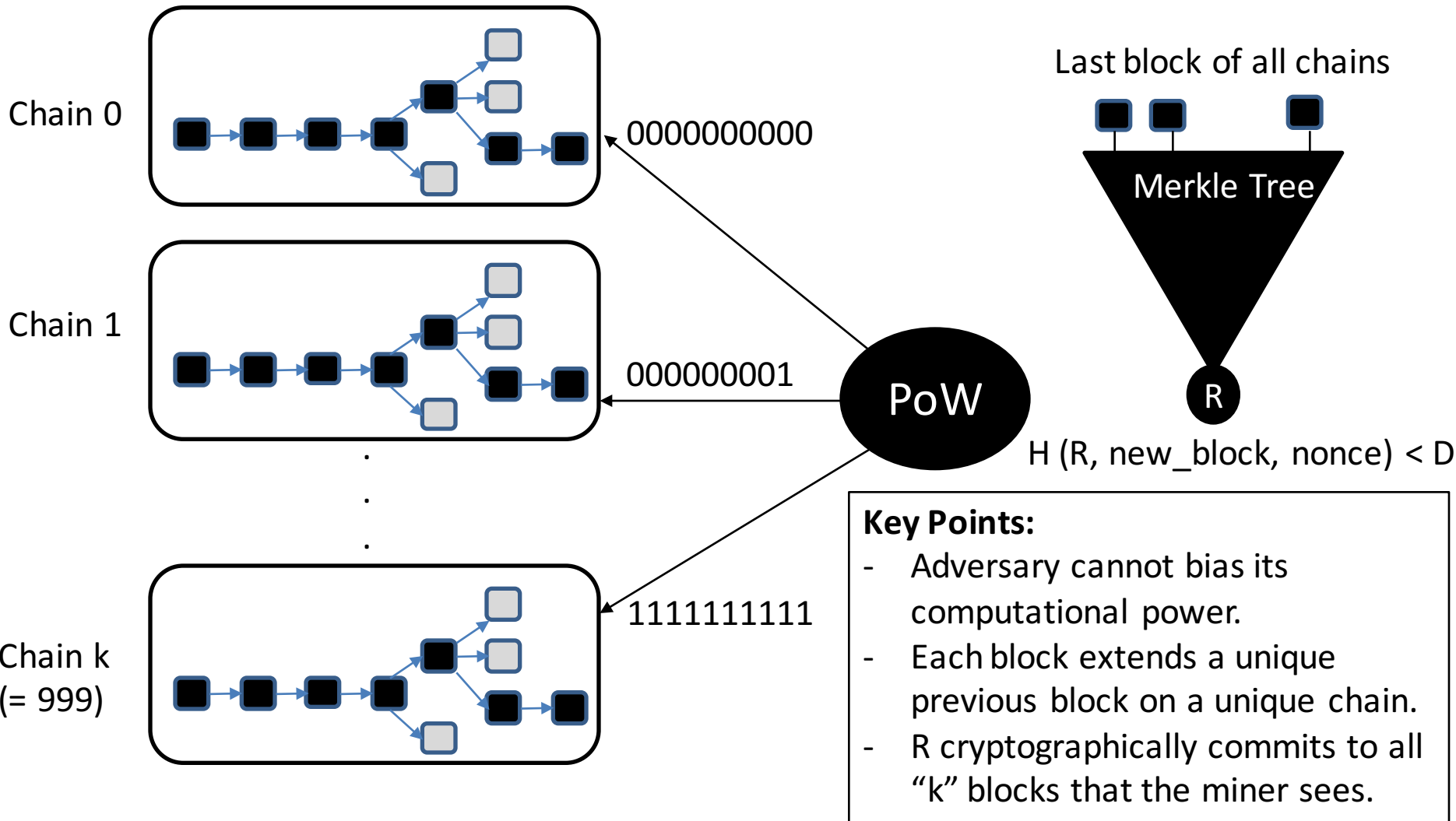


# A Principled Approach To Scale Nakamoto

# Key Observations

- There is a safe way to run Nakamoto
  - Tolerates  $f \sim 0.5$  if block interval exceeds  $3\Delta$
  - Have established proofs from prior works
- Independence of Design Parameters
  - Block interval depends only on desired  $f$  and  $\Delta$
  - Confirmation latency depends only on block interval
  - Throughput depends only on available bandwidth ( $\beta$ )
  - Decentralization depends only on number of blocks/sec.

# The OHIE Protocol: Run “k” parallel chains!

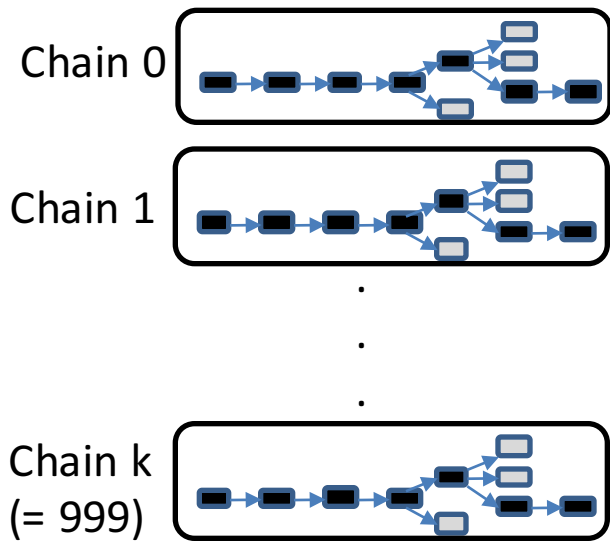


# The OHIE Protocol

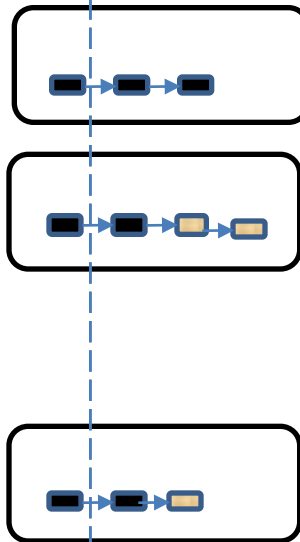
- Construction is simple and modular
- Safety and Liveness Proof:
  - Reduces to that of Bitcoin backbone protocol
  - Intuition:
    - Probabilistic process on each chain is identical to Bitcoin
    - Each block extends a single prior block
    - The state that the block extends can't be forged
  - Takes  $\Theta(\log k)$  more confirmation blocks (union bound)



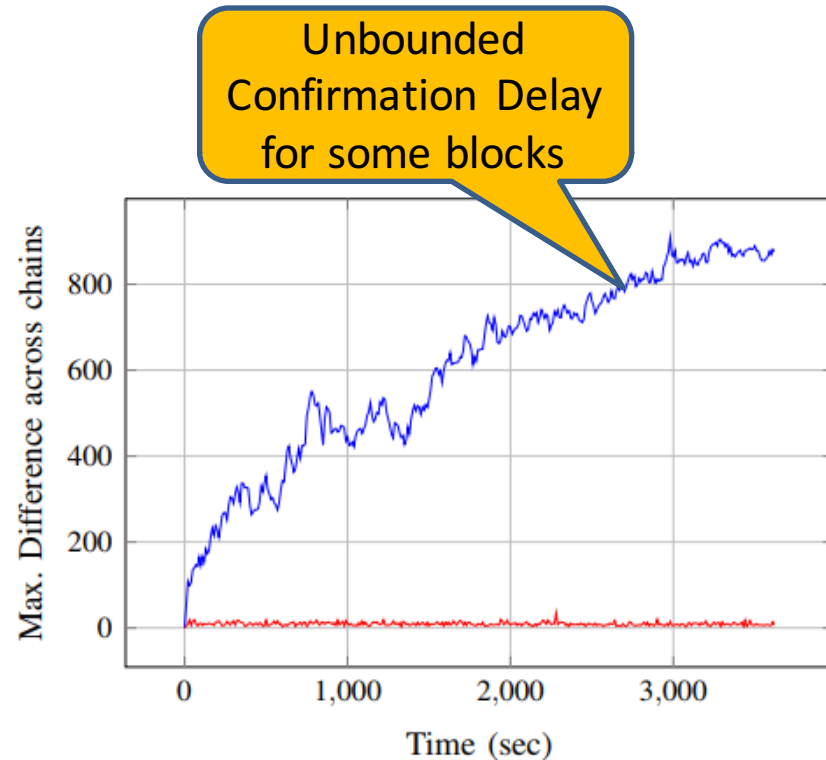
# Total Ordering Across Chains?



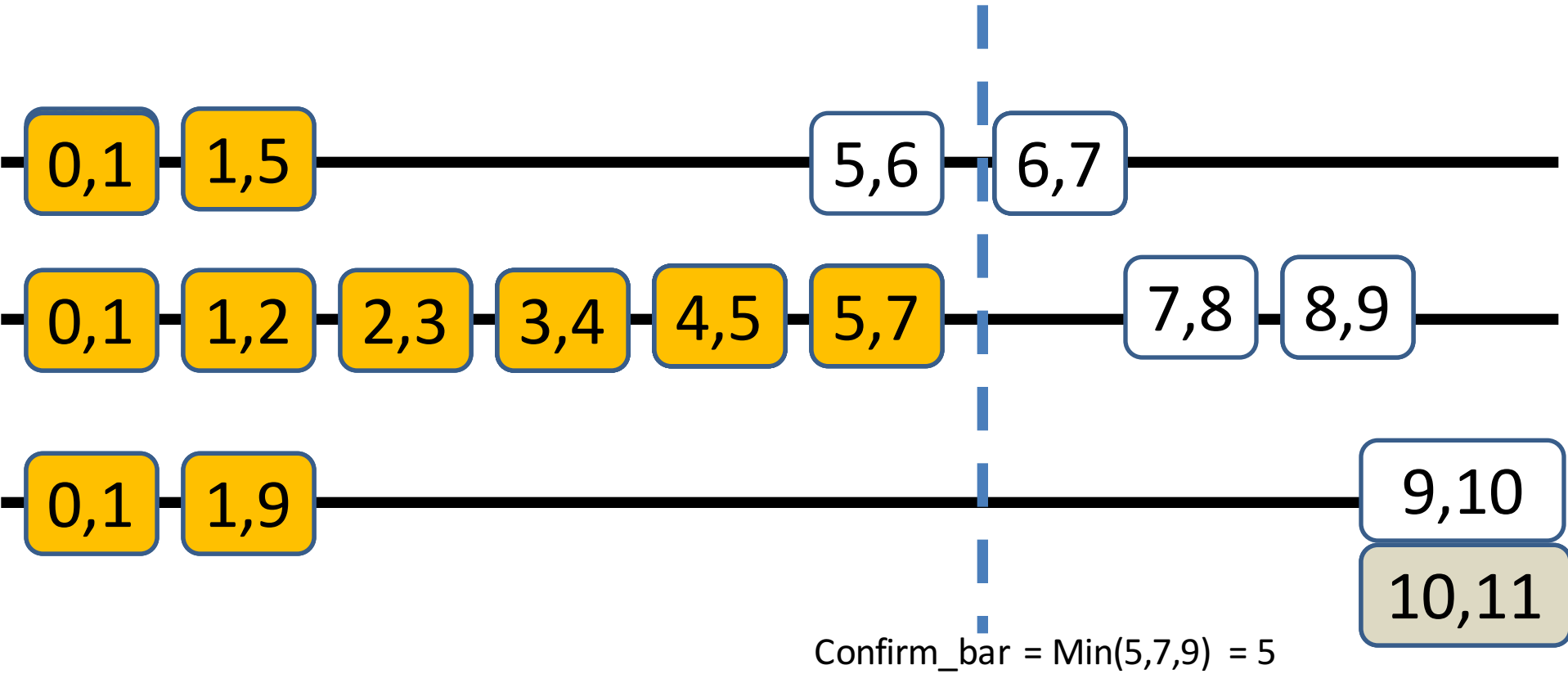
Order by chain ID



Order by Position, tie-breaking on chain ID

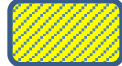
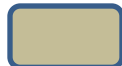



# Total Ordering Scheme In OHIE



$Confirm\_bar = \text{Min}(5,7,9) = 5$

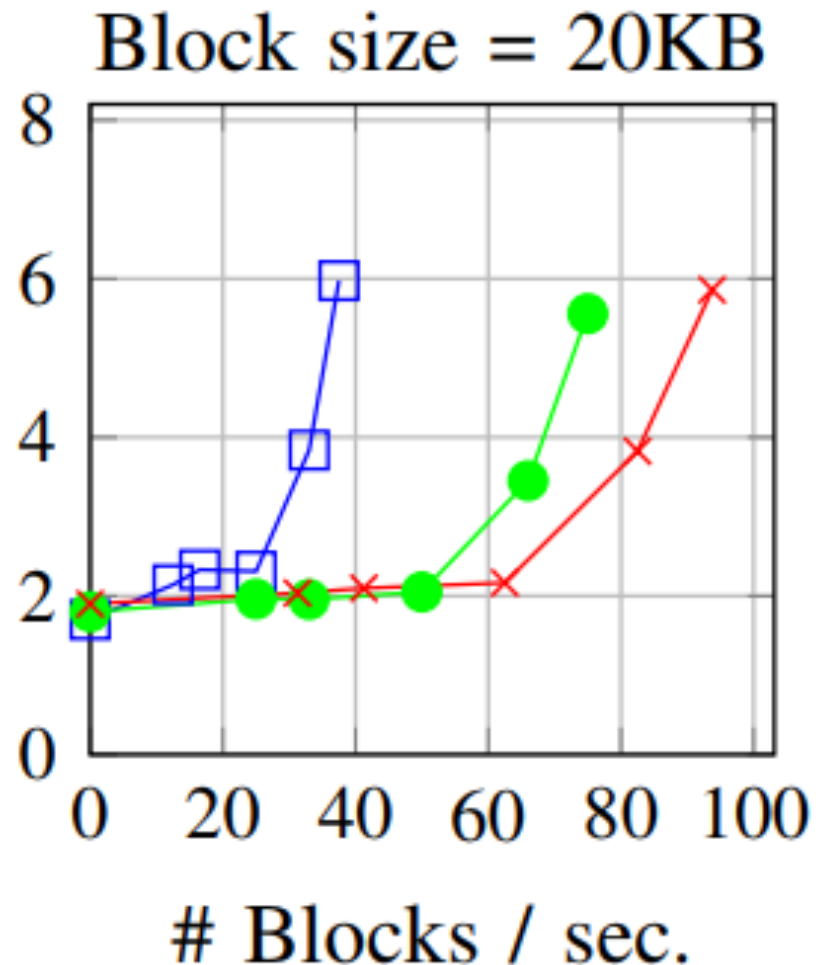
Num. of confirmations per chain (T) = 2

-  Partially confirmed (embedded T blocks deep)
-  Trailing (max next\_rank)
-  Fully confirmed

Safety & Liveness Proofs in paper

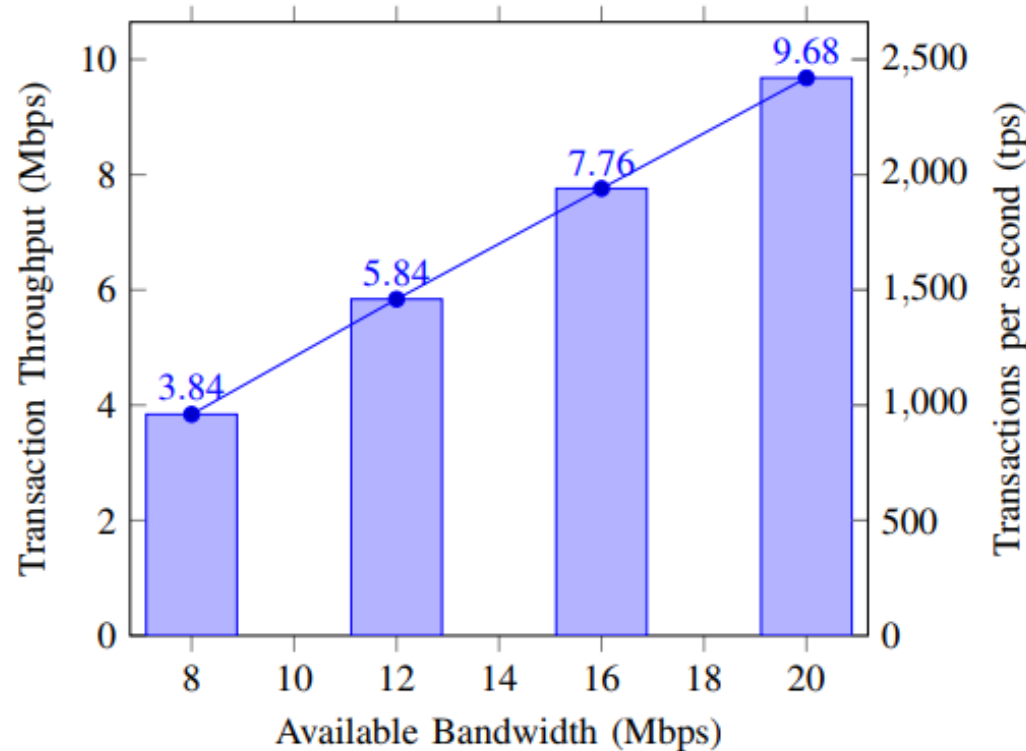
# Prototype & Micro Experiments

- Less than 5 KLOC of code
- Micro Experiments
  - 1000 miners, 20 Mbps
- Critical Observations:
  - Block propagation delay ( $\Delta$ ) proportional to graph diameter (1-2 seconds)
  - **Parallel broadcasts don't impact latency ( $\Delta$ )**



# Macro Experiments: Linear Scaling with Available Bandwidth

- 50,000 miners, 20 Mbps, resilience ( $f$ )  $\sim 0.46$

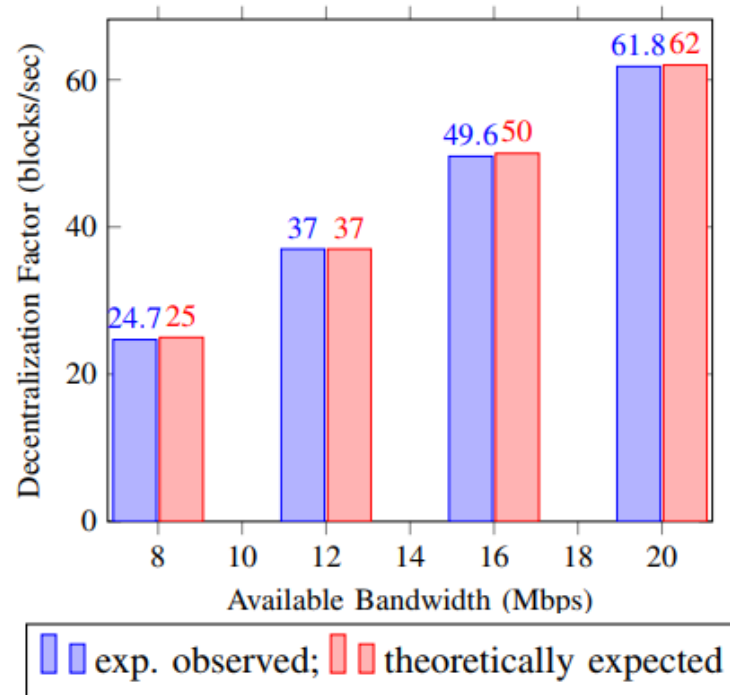


$$\text{Num. of chains } (k) = 0.5 \cdot 3\Delta \cdot \frac{\beta}{\text{block size}}$$

$3\Delta$  implies  $f \sim 0.46$

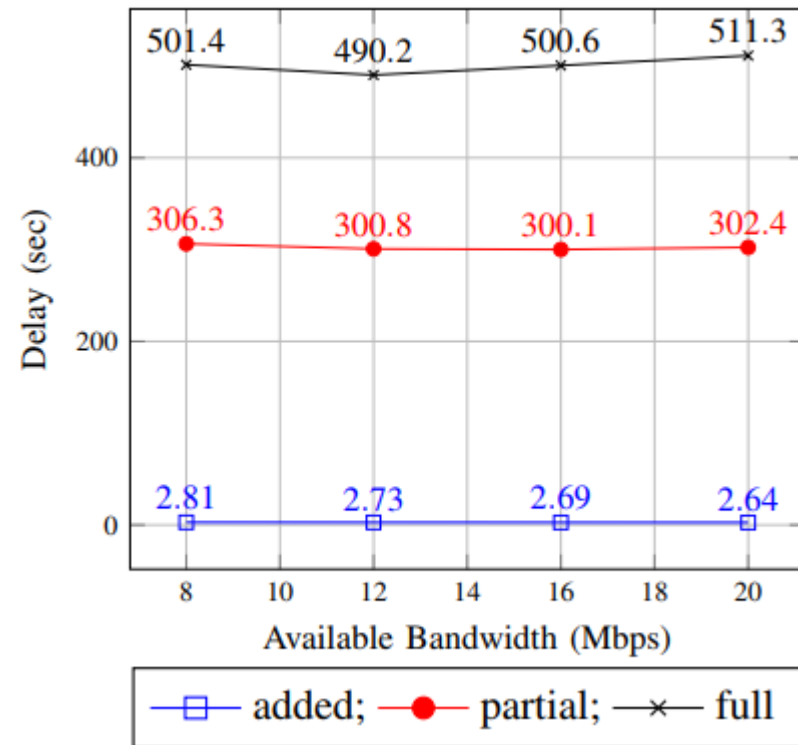
# Macro Experiments: Decentralization

- 50,000 miners, 20 Mbps,  $f \sim 0.46$
- Decentralization: Scales linearly with bandwidth
  - $k > 60$  blocks per second



# Macro Experiments: Confirmation Delay

- 50,000 miners,  $f \sim 0.46$
- Confirmation Delay
  - **Under 10 minutes ( $3\Delta T$ )**
  - Independent of throughput!  
(once we fix “k”)
- Conf. Blks ( $T$ ) = 15 - 30
  - $T_{BTC} + \Theta(\log k)$



# Security vs. Performance: State-of-the-art

Approach	Resilience	Throughput	Decentralization	Latency
Nakamoto with reduced block intervals	$f < \frac{1}{3}$	Low	Medium	Good
Nakamoto with large blocks	$f < \frac{1}{2}$	High	Low	Medium
AlgoRand (with BA) [SOSP'17]	$f < \frac{1}{5}$	High	Low	Good

60 proposers per sec

30 secs.

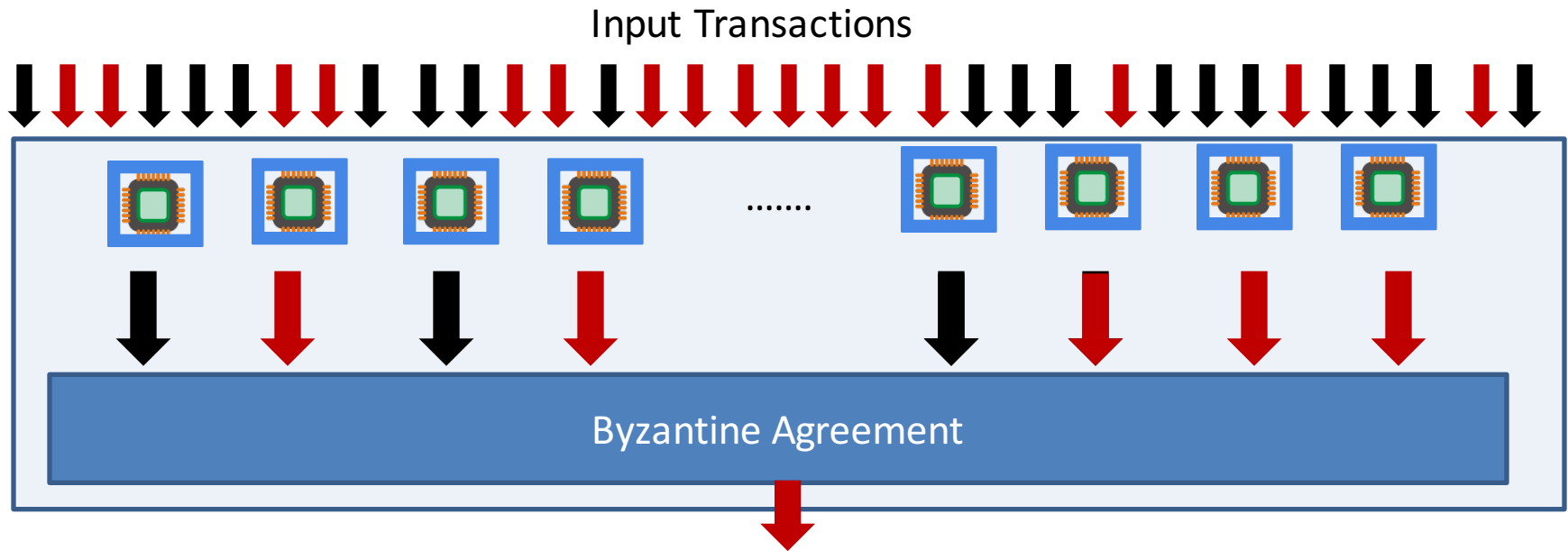
10 mins

State-of-the-practice



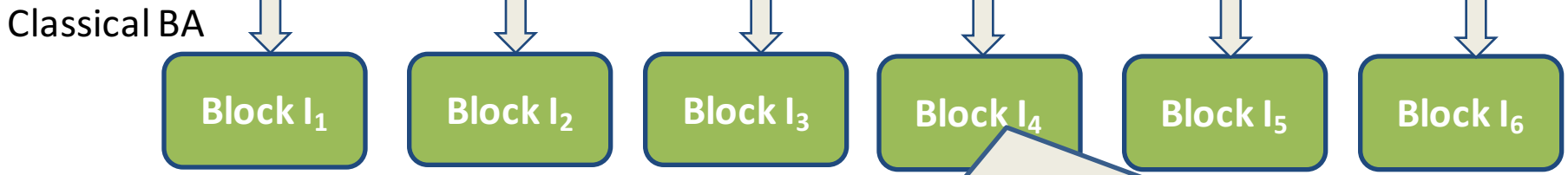
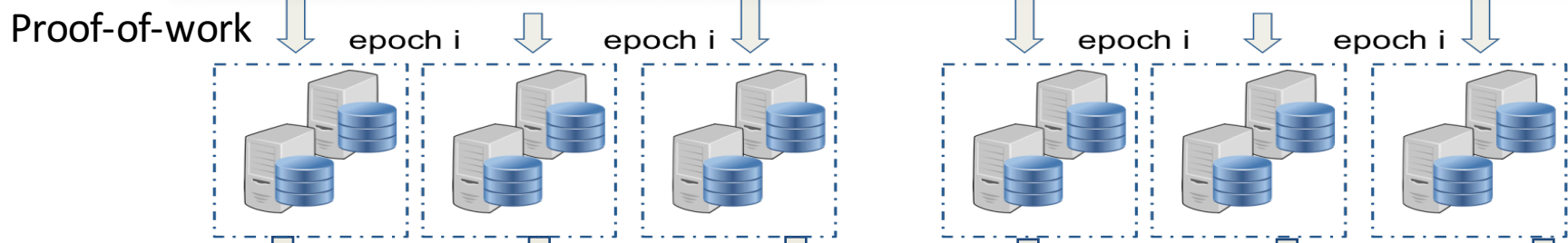
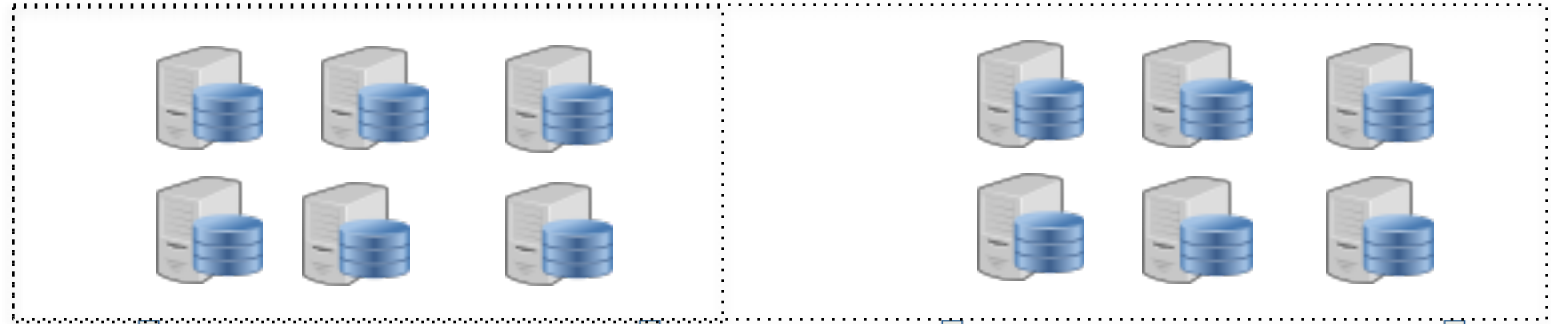
# Repurposing BA Protocols?

- Agree on 1 block per round with standard BFT / BA
- Honest miners sign that block with round id.



- Challenge: Participants must be known a-priori
  - Chicken-n-egg: Agreeing on participants is itself...

# Proof-of-work for Sharding



More computation Power, More Blocks

# Commercialized as the Zilliqa public blockchain platform



# of Transactions

779695

Transaction Rate (tps)

481.50

Transactions

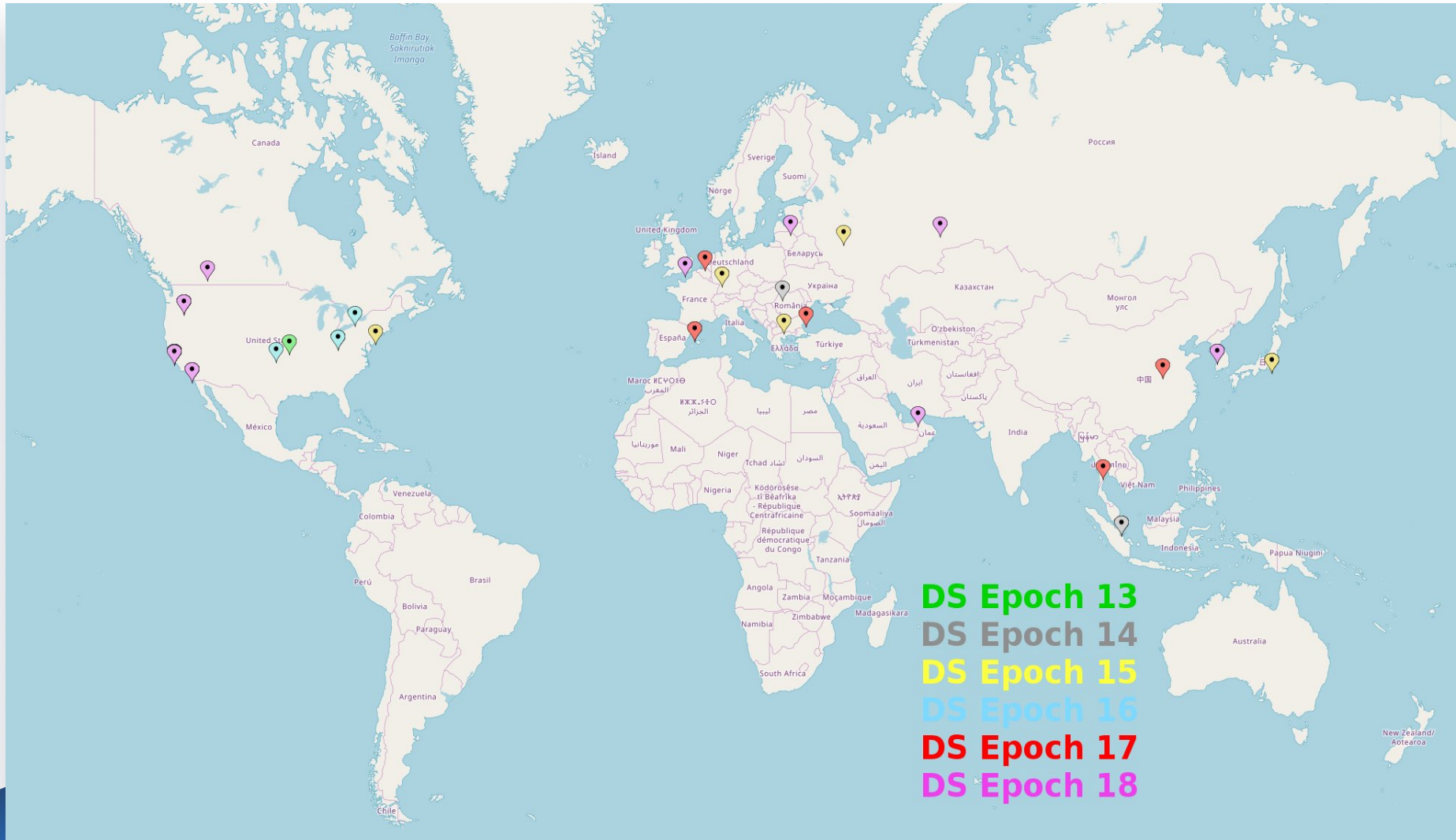
Transaction Hash

- 8F21407FE0B6E7309042B006575CC5
- 495FF76C80CC44B487CB567F8D7B33
- 2E8BCABF0F5B4ABC8D258A8667F6A98
- 8D52C BCE0E2C08BA85E067AB991F96F
- 789C575FF5CD0EBB9C248FDD07B342
- 3A5110502D258C867644035F28DE7955
- 7295DE1E92F82950519163B6FD8336B
- 027AAD3E55DA98B92221FAF31CE9C36
- 222CFFE490C06364EBFC0514DFF22EC

BlockNum	
3	F39F62388E
2	0C0BFD618
1	1739FA85A
0	D476CEE0

See All

# Open to public mining (Feb 2019)



# Takeaways

- Decentralized Systems propose exciting algorithmic problems
  - Build better crypto, distributed algorithms, verification tools, ...
- Is there an Optimal Consensus Protocol?
  - Latency  $\Theta(\Delta)$ , Throughput  $\Theta(\beta)$ , Decentralization  $\Theta(\beta)$ , Res.  $f \sim 0.5$
  - Simplicity
  - Improve the constants
- Need for new models and drawing new connections:
  - Consistency & Isolation properties offered by blockchains
  - Sybil resistance mechanisms: Proof-of-Stake vs. Proof-of-Work
  - Incentive mechanism design: Fairness, Variance, ...
  - Trusting Off-chain computations

# Thank you!

## Collaborators:

- Loi Luu (PhD, NUS & CEO – Kyber Network)
- Haifeng Yu (Prof, NUS)
- Ivica Nikolic (Postdoc, NUS)
- Seth Gilbert (Prof., NUS)
- Hrishikesh Olickel (UG, Yale-NUS)
- Roumu Hou (UG, NUS)