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Nielsen, Ulrik Dam

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# A Concise Account of Techniques Available for Shipboard Sea State Estimation

Ulrik Dam Nielsen<sup>1,2\*</sup>

<sup>1</sup>DTU Mechanical Engineering, Technical University of Denmark, DK-2800 Kgs. Lyngby, Denmark

<sup>2</sup>Centre for Autonomous Marine Operations and Systems, AMOS-NTNU, NO-7491 Trondheim, Norway

ABSTRACT. This article gives a review of techniques applied to make sea state estimation on the basis of measured responses on a ship. The general concept of the procedures is similar to that of a classical wave buoy, which exploits a linear assumption between waves and the associated motions. In the frequency domain, this assumption yields the mathematical relation between the measured motion spectra and the directional wave spectrum. The analogy between a buoy and a ship is clear, and the author has worked on this *wave buoy analogy* for about fifteen years. In the article, available techniques for shipboard sea state estimation are addressed, but with a focus on only the wave buoy analogy. Most of the existing work is based on methods established in the frequency domain but, to counteract disadvantages of the frequency-domain procedures, newer studies are working also on procedures formulated directly in the time domain. Sample results from several studies are included, and the main findings from these are mentioned.

7 Key words: Sea state estimation; Wave buoy analogy; Vessel responses; Frequency domain; Time domain.

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# 1. INTRODUCTION

In today's maritime world, the operation of ships requires careful monitoring of the related costs while, at the same time, ensuring a high level of safety. Shipboard decision support systems may enable a ship's crew to reduce costs and minimise risks while sailing, so that the performance is optimised. A ship's performance with respect to safety and fuel efficiency is in general negatively influenced by the encountered waves. Consequently, it is of particular importance to estimate the surrounding sea state, and any shipboard decision support system needs to have information about the encountered waves as input for the system to be the most accurate and reliable.

<sup>\*</sup>Email: udn@mek.dtu.dk

Trustful means for sea state estimation include floating wave buoys, which are primary tools used to collect statistical ocean wave data. However, wave buoys are not practical for a sailing ship requiring (precise) sea state information in real-time and at its actual geographical position. On the other hand, the analogy between a ship and a floating buoy naturally suggests to using the ship itself as a kind of wave buoy. Thus, a number of research studies have explored this 'wave buoy analogy' in the past, and the author of the present paper has worked extensively on the topic for about the last fifteen years.

This paper presents a concise account of techniques for shipboard sea state estimation using measured vessel responses, resembling the concept of a traditional wave buoy. Moreover, newly developed ideas for shipboard sea state estimation are introduced. The account, or review, is not necessarily complete, as it primarily reflects the author's personal experience and background; obtained alone and together with national as well as international colleagues. However, it is believed that the author has come across most of the work carried out within the particular field, so other fundamental studies, not related to the present author, will also be cited; without the ambition to list every single reference from the literature.

Although other means for shipboard sea state estimation exist, based on, e.g., the use of X-band navigational radars or over-the-bow looking devices, those means will not be mentioned herein and, hence, shipboard sea state estimation refers in the following to only the wave buoy analogy, where sea state estimation is conducted on the basis of measured vessel responses. Onwards, *sea state estimation* will at most places be shortened by SSE.

1.1. Past Work and Literature. Until the 1970'ies, little work on shipboard SSE had been done, but early 34 researches (e.g. Lindemann and Nordenstrøm, 1975; Lindemann et al., 1977; Robinson, 1990; Debord and 35 Hennessy, 1990; Francescutto, 1993) on in-service monitoring systems combined with decision support 36 tools emphasised the need for estimates of the on-site sea state; at the actual position of the advancing 37 vessel. Some of the initial studies on shipboard SSE (Takekuma and Takahashi, 1973; Pinkster, 1978) did 38 not consider ships with forward speed, and although attempts were made to introduce forward speed in 39 shipboard SSE, notably by Japanese studies (Isobe et al., 1984; Kobune and Hashimoto, 1986; Hirayama, 40 1987; Iseki et al., 1992; Saito et al., 2000; Maeda et al., 2001), the first study to strictly consider the Doppler 41 shift, implying a 1-to-3 relationship between encounter frequency and wave frequency for certain conditions 42 in following sea, was made by Iseki and Ohtsu (2000). Since then several studies with good results have 43 been published for ships with forward speed (Iseki and Terada, 2002; Iseki, 2004; Nielsen, 2006; Nielsen 44 and Stredulinksy, 2012; Nielsen and Iseki, 2012; Nielsen et al., 2013; Montazeri et al., 2016a; Montazeri, 45 2016); all considering full-scale data of different vessels. A number of studies have also been made in 46 relation to station keeping and dynamic positioning, where shipboard SSE has been made with success for 47

ships without forward speed (Waals et al., 2002; Tannuri et al., 2003; Pascoal et al., 2007; Simos et al., 2007;
Sparano et al., 2008; Pascoal and Soares, 2009).

1.2. Content and Composition of Paper. Different mathematical models exist for the wave buoy analogy, and the main principles will be outlined in Section 2. It is shown that shipboard SSE can be carried out either in the frequency domain or in the time domain, and, based on the setting, Sections 3 and 4 provide summaries of the fundamental assumptions and the different mathematical models which are applied depending on the particular domain, being it time or frequency. Sample results taken from several of the author's previous application studies, relating to both frequency and time domain calculations, are included in Section 5. Finally, concluding remarks are given in Section 6.

### 2. WAVE BUOY ANALOGY

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Most of today's marine vessels are instrumented with sensors to record, e.g., global motion components such as heave, pitch, and vertical acceleration at specific position(s) relative to the centre of gravity. In this sense, vessels resemble classical wave buoys; although the latter typically have much simpler geometrical forms compared to the hull of a ship. Anyhow, the response recordings from marine vessels can be processed to facilitate estimation of the on-site sea state, making the analogy to floating wave buoys by relating the measurements and the sea state through a mathematical model, see Figure 1.



FIGURE 1. Combination of wave-induced response measurements and a mathematical model can be used to deduce information about the on-site sea state. (Nielsen et al., 2016)

64 2.1. Main Assumption. In mild and moderate wave climate, the wave-induced six degrees-of-freedom
 65 motion of a ship and associated structural loads are often assumed to be linear with the incident waves,

meaning that the amplitudes of those responses are proportional to the wave amplitudes in regular waves.
 Consequently, the responses can be quantified in irregular waves by adding together results from regular
 waves with different amplitudes, wavelengths and propagation directions.

The linear assumption between waves and associated responses facilitates the use of transfer functions, or response amplitude operators (RAOs), that express how waves are *transferred* into responses. State-of-theart techniques for calculation of RAOs include 3-dimensional panel codes considering potential wave theory; sometimes supplemented with CFD based on the full set of Navier-Stoke's equations and/or considering other nonlinear effects. Nonetheless, strip theory calculations are still widely used, due to their adequate degree of approximation, and often they provide good results.

In theory, RAOs are not necessarily accurate in severe waves, where a nonlinear relationship between waves and responses would/could occur. In practice, however, many studies have shown that even in severer wave conditions, RAOs can be still used to calculate responses of ships.

2.2. Frequency and Time Domain Approaches. The majority of previous work on the wave buoy analogy
(e.g. Hua and Palmquist, 1994; Iseki and Ohtsu, 2000; Tannuri et al., 2003; Nielsen, 2006, 2008b; Pascoal
et al., 2007; Montazeri et al., 2016a) is based on a solution formulated entirely in the frequency domain.
This is illustrated in Figure 2, where a response spectrum is combined with RAOs, using spectral analysis,
so that an estimate of the sea state is given in terms of a wave (energy) spectrum. Studies have shown that, in
practice, wave estimation is improved by (optimally) selecting a set of three simultaneous vessel responses (Nielsen, 2006).



FIGURE 2. Main principle of the wave buoy analogy when it is formulated in the frequency domain. (Nielsen et al., 2016)

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<sup>85</sup> Instead of a solution formulated in the frequency domain, derived by use of spectral analysis and with pos-

sible disadvantages, it has been suggested by Nielsen et al. (2015, 2016) to make the fitting of the *measured* 

87 response and the corresponding theoretically calculated one directly in the time domain (Fig. 3). In this

sense, the approach is similar to a previous work by Pascoal and Soares (2009) that also formulate the gov-

<sup>89</sup> erning equation directly in the time domain. However, the latter method (Pascoal and Soares, 2009), based

on Kalman filtering, relies completely on availability of accurate RAOs, which is the main difference to the former works (Nielsen et al., 2015, 2016) as will be outlined in Section 4.



FIGURE 3. Conceptually, the wave buoy analogy can be formulated directly in the time domain to give the actual wave elevation at the site of the vessel. (Nielsen et al., 2016)

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In the next two sections, 3 and 4, the fundamentals of the techniques used for, respectively, frequency domain and time domain shipboard SSE are briefly described. As such, the sections can be read separately and have to some extent been formulated as stand-alone sections, which means that repetitions of fundamental assumptions and background occur.

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# 3. FREQUENCY DOMAIN APPROACHES FOR SSE

Shipboard SSE is often considered in the frequency domain. Strictly speaking, the linear assumption about 97 waves and associated responses needs, in this case, to be supplemented with additional assumptions: Firstly, 98 the ocean waves and associated responses represent ergodic random processes (e.g. Ochi, 1990), so that 99 stationarity, in a stochastic sense, applies within a certain period of response records at each estimation 100 sequence. Secondly, the speed and the course of the ship (relative to waves) are constant in that period. Thus, 101 response measurements from the particular period can be processed by spectral analysis using standard Fast 102 Fourier Transformation (FFT) or multivariate autoregressive procedures (Nielsen, 2005, 2006), where the 103 latter may sometimes be chosen because of the ability to automatically select the appropriate amount of 104 smoothing; based on an order selection criterion. Traditionally, the mathematical model of shipboard SSE 105 has then been formulated in terms of a comparison between the measured and the theoretically calculated 106 spectral energy distribution of the considered responses. 107

<sup>108</sup> 3.1. Comparison of Spectral Energy Distribution. A set of ship responses is considered, and the complex-<sup>109</sup> valued transfer functions,  $H_i(\omega_e, \chi)$  and  $H_j(\omega_e, \chi)$  for the i-th and j-th responses, yield the theoretical rela-<sup>110</sup> tionship between the i-th and the j-th components of the response spectra  $S_{ij}(\omega_e)$  and the directional wave <sup>111</sup> spectrum  $E(\omega_e, \chi)$  through the following integral equation

$$S_{ij}(\omega_e) = \int_{-\pi}^{\pi} H_i(\omega_e, \chi) \overline{H_j(\omega_e, \chi)} E(\omega_e, \chi) d\chi$$
(1)

where  $\omega_e$  and  $\chi$  are the encounter wave frequency and the relative wave heading, respectively, and the bar 112 denotes the complex conjugate. The theoretical relationship expressed by Eq. (1) can be directly compared to 113 a set of corresponding measured response spectra. Thus, the comparison constitutes the governing equation 114 of the estimation problem that can be solved mathematically as a minimisation. It is vital to note that the 115 wave spectrum is advantageously estimated in the wave frequency ( $\omega$ ) domain. This means that the speed-116 of-advance - the so-called triple-valued function - problem in following sea needs to be considered. This 117 problem, governed by the Doppler Shift, has been properly incorporated by Iseki and Ohtsu (2000), and in 118 doing so, the mathematical relation between encountered (wave) frequency and true frequency is secured; 119

$$\omega_e = \omega - \omega^2 A$$
 ,  $A = \frac{U}{g} \cos \chi$  (2)

where U is the forward speed of the ship, and g is the acceleration of gravity. The *triple-valued function* problem exists when  $\omega_e < \frac{1}{4A}$  since, in this case, three wave frequencies correspond to one (positive) encounter frequency.

It should be understood that the left-hand side of Eq. (1) is estimated by measured data while the right-hand side is obtained through theoretical calculations. Consequently, a minimisation problem can be formulated and, casting the expressions into matrix notation, the objective is to minimise

$$\chi^{2}(\mathbf{x}) \equiv \|\mathbf{A}\mathbf{f}(\mathbf{x}) - \mathbf{b}\|^{2}$$
(3)

where  $\|\cdot\|$  represents the  $L_2$  norm. In the equation, the vector function  $\mathbf{f}(\mathbf{x})$  expresses the wave spectrum  $E(\omega, \chi)$  and the vector  $\mathbf{b}$  contains the elements of the measured response spectra  $S_{ij}(\omega_e)$ , while the coefficient matrix  $\mathbf{A}$  basically has its elements derived from the complex-valued transfer functions. Details are given by Nielsen (2006).

The minimisation problem given by Eq. (3) can be handled by different approaches. Two approaches that have received particular interest are formed by *Bayesian modelling* and *parametric modelling*. Bayesian modelling relies on finding the spectral components of a (discrete) frequency-directional wave spectrum, whereas parametric modelling assumes the directional wave spectrum to be formed by a set of parameterised wave spectra, e.g., JONSWAP using directional spreading parameters. Reports about the two procedures have been given in many studies (Iseki and Ohtsu, 2000; Iseki and Terada, 2002; Nielsen, 2006, 2008b;
Pascoal and Soares, 2008; Tannuri et al., 2003; Pascoal et al., 2007; Simos et al., 2007), considering both
simulated data and full-scale measurements with and without forward speed; and comparisons between the
two modelling procedures have also been made. However, as pointed out by Nielsen and Stredulinksy
(2012) and Nielsen et al. (2013), the two approaches should not been seen as competitors but rather as
complementary, since each procedure has its own advantages and disadvantages.

141 3.2. Energy Equivalence: Comparison of Spectral Moments. In a recent PhD study, Montazeri (2016) 142 suggests to formulate the governing equation from an energy conservation point-of-view, since the integrated 143 variant of Eq. (1) is considered. Thus, the mathematical model is based on an equivalence of the spectral 144 moments calculated by integrating the two sides of Eq. (1) with respect to frequency. Again, a *set* of 145 responses is considered simultaneously using cross-coupling terms so that the governing equations read

$$\int_{\omega_{e,l}}^{\omega_{e,h}} S_{ij}(\omega_e) \, d\omega_e = \int_{\omega_l}^{\omega_h} \int_{-\pi}^{\pi} H_i(\omega,\chi) \, \overline{H_j(\omega,\chi)} E(\omega,\chi) \, d\chi d\omega \tag{4}$$

where indices l and h correspond to lower and higher frequency limits, respectively. The actual values of these limits are determined through a partitioning technique (Montazeri, 2016) introduced to separately estimate wind sea and swell components of the wave system, see Figure 4. The details of this technique are given by Montazeri et al. (2016a) and Montazeri (2016), but it is noteworthy that the *ocean wave system* is expressed through the sum of two parameterised wave spectra; one for swell and one for wind sea, and each taking the form  $S_{wave}(\omega)$  of a general unidirectional spectrum for developing seas (Boukhanovsky and Soares, 2009):

$$S_{wave}(\omega) = \alpha g^2 \omega^{-r} \exp(-\beta \omega^{-n}) \gamma^{\exp\left[\frac{-(\frac{\omega}{\omega_p}-1)^2}{2\sigma^2}\right]}$$
(5)

where the fitting parameters are  $[\alpha, \beta, \gamma, \sigma, \omega_p, r, n]$ . A directional spectrum is obtained as

$$E(\omega, \theta) = S_{wave}(\omega)D(\theta|\omega) \tag{6}$$

with D(...) being a spreading function for wave direction  $\theta$ ; satisfying the normality condition

 $\int_{-\pi}^{\pi} D(\theta|\omega) d\theta = 1$ . In its physical understanding, the equal sign in Eq. (4) should be read like "nearly equal to", so that the values of the fitting parameters, including the spreading function, are optimised by minimising the difference between the left- and right-hand sides of Eq. (4), with the wave spectrum  $E(\omega, \chi)$ specified by Eq. (6)\*; leaving all details to Montazeri et al. (2016a) and Montazeri (2016).

For the set of governing equations (Eq. 4) it is important to note that the right-hand side is explicitly written with account to the true (wave) frequency; and *not* the encounter frequency as is the case of the left-hand side

<sup>\*</sup>Wave direction  $\theta$  will be directly related to relative wave heading  $\chi$  taking ship course into account.



FIGURE 4. Spectral partitioning of wave spectrum into swell and wind sea components. (Montazeri, 2016)

that represents the measurements. This particular formulation, with no need to transform between the two frequency domains for the theoretical calculation (i.e., the right-hand side), is possible since the energy must be the same in the two domains. Consequently, the exclusive consideration of equations based on energy conservation has the (positive) effect that the 1-to-3 relationship between encounter and wave frequency in following sea has not to be considered.

Compared to the other frequency-domain principle, outlined in subsection 3.1, the ambition with the 'energyequivalence principle', as stated by the authors (Montazeri, Nielsen and Jensen, 2016), is partly to make a practical robust procedure and partly to increase the computational efficiency of the wave buoy analogy; obviously, not compromising the ability to provide accurate sea state estimates.

3.3. Disadvantages of Frequency Domain Approaches. The outcome of the wave buoy analogy, when 170 formulated in the frequency domain, consists of the on-site wave system's complete energy distribution, 171 with frequency and directional information, and thus the approach is applicable to general decision support 172 systems for safe and efficient marine operations. As reported in the literature, reasonable estimates of the 173 wave spectrum can be expected (Nielsen, 2006, 2008b; Nielsen and Stredulinksy, 2012; Nielsen et al., 2013; 174 Montazeri et al., 2016a), but the accuracy of the estimated sea state depends inherently on reliable trans-175 fer functions. Furthermore, the accuracy is highly dependent on the required spectral (response) analysis; 176 hence, stationarity, or not, of the measurements may potentially influence the outcome (Møgster, 2015; Iseki 177 and Nielsen, 2015). In principle, stationary operational conditions are necessary because a minimum time 178 window, in the order 10-15 minutes, is needed to perform the spectral analysis. The reason is that if condi-179 tions are not stationary during the considered period, either because of a changing sea state or, more likely, 180 as a result of speed and/or heading changes of the vessel, the sea state estimates are likely to be unreliable. 181 Moreover, the need for a certain minimum time period has another consequence, as it implies that estimates, 182

strictly speaking, are not real-time but will be backdated; which in turn may negatively influence response
 predictions made ahead of measurements, as discussed by Nielsen and Iseki (2015).

Altogether, these disadvantages of the frequency domain approaches have initiated studies where the solution, i.e. sea state estimate, is sought for directly in the time domain; to better accommodate partly nonstationary conditions. Moreover, work exists, in the time domain, to estimate the peak period of the sea state, with no other input than the response signal itself (Belleter et al., 2015; Brodtkorb et al., 2015). In the following, one of the time domain approaches looks at coupling this entirely "signal-based" estimation concept with the use of RAOs in a *stepwise procedure* to partly mitigate the fact that RAOs are always imperfect to some degree.

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### 4. TIME DOMAIN APPROACHES FOR SSE

The central point of the procedures is a formulation of the estimation problem directly in the time domain, where focus is on real-time sea state updates obtained from continuous response measurements, with no need to consider a past measurement period.

Until now, only few works consider approaches for shipboard SSE directly in the time domain and, so 196 far, the procedures, like those formulated in the frequency domain, rely on availability of accurate RAOs. 197 Indeed, this is so for an elaborate procedure, building on a framework established by Kalman filtering, which 198 will be addressed subsequently. However, as will be noted further below, it is possible to make a stepwise 199 estimation procedure which couples an entirely *signal-based* procedure, estimating the peak wave period, 200 with a model-based procedure, estimating wave height and phase. Herein, the signal-based step has no 201 need for RAOs, whereas the model-based step makes use of RAOs. In the following, the two conceptually 202 different approaches, based on, respectively, Kalman filtering and the stepwise procedure, will be concisely 203 accounted for. 204

4.1. Wave Estimation Based on Kalman Filtering. An interesting study has been presented by Pascoal and Soares (2009) that propose a (high-speed) estimation algorithm established in a framework governed by Kalman filtering. Herein, the waves in-phase and quadrature components are introduced as the state variables, which means that (intrinsic) information about the actual wave elevation process is included in the solution. The mathematical details of the procedure are given by Pascoal and Soares (2009), so the following contains just a brief summary of the approach.<sup>†</sup>

<sup>&</sup>lt;sup>†</sup>The present author has started recently to also work on this concept.

The in-phase and quadrature components of a regular wave from (discrete) direction  $\theta_n$ , at discrete time k, constitute a set of state variables  $X_k = [x_1, x_2]_n^T$ . Relying on the electric filter analogy (St.Denis and Pierson, 1953), an irregular wave would be the sum of a (large) number of regular waves, implying that the associated sea state can be given in terms of an equivalent number of sets of state variables. In normal conditions, a sea state will be just very slowly varying and the hypothesis is that the *state* (in a Kalmancontext) at a next discrete time is as the present, except possibly for some variation due to the state noise  $\xi_k$ . Thus, the state equation reads

$$X_{k+1} = X_k + \xi_k \tag{7}$$

The state equation is supplemented with a measurement equation and, as the wave estimation is based on sensor recordings r of m available wave-induced responses, this equation is given by

$$r_{mk} = C_{mk}X_k + \psi_{mk} \tag{8}$$

where  $C_{mk}$  is the measurement matrix *transferring* the states into a response (output) that is to be compared 220 with a corresponding one available from measurement, while  $\psi_{mk}$  is the measurement noise because of 221 a sensor's limited capability. The equation is basically the equivalent of Eq. (1), but formulated in the 222 time domain, and Eq. (8) represents, analogously, a linear relationship between a single harmonic wave 223 component and an associated response component. As a consequence, the measurement matrix  $C_{mk}$  can 224 therefore be composed by the available (complex-valued) transfer functions H. The specific composition 225 of the matrix is realised by expressing the measurement equation in its physical understanding, writing 226 the irregular response r as the sum of  $n_f$  harmonic components, each represented in a total of  $n_{\theta}$  wave 227 directions: 228

$$r = \operatorname{Re}\left(\sum_{j=1}^{n_f} \sum_{i=1}^{n_\theta} H_{ji} \times \left(X_{2j-1,i} + \sqrt{-1}X_{2j,i}\right) \times \left(\cos(\omega_j t) + \sqrt{-1}\sin(\omega_j t)\right)\right)$$
(9)

From the equivalence between Eq. (8) and Eq. (9) it can be seen how the elements of the measurement matrix should be assigned. Part of the matrix is shown below for the j-th frequency, i-th direction, m-th response and k-th time instant, respectively

$$C_{jimk} = \left[ \operatorname{Re}[H_{jim}] \cos(\omega_j k \Delta t) - \operatorname{Im}[H_{jim}] \sin(\omega_j k \Delta t) \dots - \operatorname{Im}[H_{jim}] \cos(\omega_j k \Delta t) - \operatorname{Re}[H_{jim}] \sin(\omega_j k \Delta t) \right]^T$$
(10)

where  $\Delta t$  denotes used sampling time. The full matrix at any point in time  $t_k = k\Delta t$  is built by concatenating the submatrices  $C_{jim}$ , leaving k as the only free index (Pascoal and Soares, 2009).

The application of the Kalman filter (e.g. Brown and Hwang, 1992) involves the standard prediction and update cycles, and Pascoal and Soares (2009) carefully address many important aspects to consider when implementing the solution scheme in practice; including points about stabilisation of solution, conditioning
 of matrices, tuning of filter gain, etc.

It is important to mention that Pascoal and Soares (2009) consider station-kept ships, without forward speed, 238 implying that the frequency  $\omega$  in Eq. (9) is the (true) wave frequency. Thus, it is trivial to transform the wave 239 spectrum,  $S(\omega_e)$ , estimated in encounter domain to  $S(\omega)$  in the true domain. Although the extension to 240 including forward speed is elementary, the practical incorporation is by no means straight-forward because of 241 the Doppler shift (Eq. 2), leading to a 1-to-3 relationship between encounter and true frequency in following 242 waves when  $\omega_e < \frac{1}{4A}$ , cf. Eq. (2). The basic problem is identical to what is handled by the approach(es) 243 formulated in the frequency domain (Section 3). However, it is not possible to use the same type of solution-244 scheme because of the different domains (frequency vs. time). In a new study by Pascoal et al. (2016), the 245 effect of forward speed is reportedly included, but the article does not draft an actual implementation of it. 246 On the other hand, one possible method to deal with the Doppler shift for ships having forward speed is 247 suggested in a recent MSc study by Ding (2016), supervised by the present author. This MSc study shows 248 how forward speed can be successfully included, so that the transformation of the wave spectrum from 249 encounter to true domain is secured, but the implementation is restricted to long-crested waves. Hence, the 250 extension to real ocean waves, i.e. full-scale experimental data, remains. The 'transformation problem' (for 251 long-crested waves) is summarised in the following. 252

In case of nonzero forward speed, and for all waves approaching forward of 'beam sea', the transformation 253 of the wave spectrum,  $S(\omega_e)$ , in the encounter domain to  $S(\omega)$  in the true (frequency) domain is trivial, 254 as Eq. (2) yields a 1-to-1 relationship. For waves approaching behind of 'beam sea' and  $\omega_e < \frac{1}{4A}$ , the 255 transformation is non-trivial, since Eq. (2) yields a 1-to-3 relationship; in case of a 1-to-1 relationship 256 the transformation is straight-forward and identical to the former situation. If the 1-to-3 relationship oc-257 curs, the (suggested) solution is derived by considering the illustration shown in Figure 5. The estimated 258 spectral ordinate  $\hat{S}(\omega_e) = A_{e1}$  in encounter-frequency domain is considered. Accordingly, the particular 259 ordinate needs to be transferred into three ordinates in the (true) wave-frequency domain;  $\hat{S}(\omega_1) = A_{\omega_1}$ , 260  $\hat{S}(\omega_2) = A_{\omega 2}$ , and  $\hat{S}(\omega_3) = A_{\omega 3}$ , where (only) the frequencies  $\{\omega_1, \omega_2, \omega_3\}$  are known, whereas the values 261  $\{A_{\omega 1}, A_{\omega 2}, A_{\omega 3}\}$  are unknown. However, for any parameterised spectrum,  $S^*(\omega|H_s, T_z, ...)$ , known fre-262 quencies imply known spectral values, if the standard wave parameters  $(H_s, T_z, ...)$  are also known. Thus, 263 ratios between the spectral ordinates of the parameterised spectrum in the true domain and in the encounter 264 domain, respectively, can be formed at the three known frequencies: 265

$$\frac{S^*(\omega_1)}{S^*_e(\omega_e)}, \qquad \frac{S^*(\omega_2)}{S^*_e(\omega_e)}, \qquad \frac{S^*(\omega_3)}{S^*_e(\omega_e)} \tag{11}$$



FIGURE 5. Transformation of wave spectrum. (Lewandowski, 2004)

taking note that  $S_e^*(\omega_e) = S^*(\omega_1) + S^*(\omega_2) + S^*(\omega_3)$ , cf. Figure 5. It may now be stated, or assumed, that the relative distribution of energy in the parameterised spectrum  $S^*(\omega)$  reflects the distribution of the estimated "true" spectrum  $\hat{S}(\omega)$ . Hence, ratios similar to Eq. (11) can be formed from the estimated spectrum, and, relying on the stated assumption, the following expressions are derived:

$$\frac{\hat{S}(\omega_1)}{\hat{S}(\omega_e)} \doteq \frac{S^*(\omega_1)}{S^*(\omega_1) + S^*(\omega_2) + S^*(\omega_3)}$$
(12)

$$\frac{\hat{S}(\omega_2)}{\hat{S}(\omega_e)} \doteq \frac{S^*(\omega_2)}{S^*(\omega_1) + S^*(\omega_2) + S^*(\omega_3)}$$
(13)

$$\frac{\hat{S}(\omega_3)}{\hat{S}(\omega_e)} \doteq \frac{S^*(\omega_3)}{S^*(\omega_1) + S^*(\omega_2) + S^*(\omega_3)}$$
(14)

where the symbol " $\doteq$ " expresses that the *ratios* are assumed to be identical; not necessarily with a match between the pairs of numerators and the pairs of denominators, respectively, on the left- and right-hand sides. In Eqs. (12)-(14), the estimated *encounter* wave spectral ordinate  $\hat{S}(\omega_e)$  is formed by the complex wave amplitude, which is the output of the Kalman filtering approach. Thus, the estimated wave spectral ordinates  $\hat{S}(\omega_i)$  at the three given wave frequencies  $\omega_i$ , i = 1, 2, 3 can be calculated.

4.2. Wave Estimation Based on a Stepwise Procedure. New conceptual ideas for time-domain-based
shipboard SSE were addressed recently (Bjerregård, 2014; Nielsen et al., 2015), and one particular method
has been further studied by Nielsen et al. (2016). Stepwise, the method provides, first, the (characteristic)
wave period obtained solely from a measured response signal. In the second step, the method combines the

use of measurements and corresponding RAOs to estimate wave amplitude and phase (of a regular wave train). The partial independency of RAOs is representing a great advantage, as using them in real-world applications always is associated with uncertainty due to incomplete knowledge about the input conditions, i.e. speed, wave heading, draft, etc.; not to mention (in)accuracies in the calculation of the RAOs themselves.



FIGURE 6. Estimation of wave elevation using nonlinear least squares fitting (NLLS) together with a 'frequency estimator'. (Nielsen et al., 2016)

The details of the stepwise procedure are left to Nielsen et al. (2016), but the principle of the procedure 283 is summarised by the block diagram in Fig. 6. The "input" to the marine craft is a wave elevation signal 284  $\zeta(t)$  and the "output",  $\rho(t)$ , is a corresponding motion response. From the motion response, the method 285 provides, in the first step, the characteristic frequency  $\hat{\omega}$  of the wave signal, and subsequently, in the second 286 step, wave amplitude  $\hat{\zeta}_a$  and phase  $\hat{\varepsilon}_a$  are estimated, using a fitted value of the response amplitude  $\hat{\rho}_a$  and 287 the inverse,  $RAO_{\rho}^{-1}(\hat{\omega})$ , of the corresponding transfer function. The 'Frequency estimator' is based on 288 techniques developed within control theory (Aranovskiy et al., 2007; Belleter et al., 2015), whereas the 289 estimated response amplitude  $\hat{\rho}_a$  is found from a recursive nonlinear least squares (NLLS) optimisation 290 (Nielsen et al., 2016). The estimation process is made on short sequences of data (5-7 wave periods), but 291 a new estimation is made on shorter intervals, so that the analysis is a based on a "moving window" of 292 data recordings, enabling real-time updates/estimates of the wave elevation. However, it is important to 293 emphasise that the procedure is still far from mature to be applicable in sea state estimation from full-scale 294 measurements data of ships, since the method, so far, is limited to handle only the estimation of regular wave 295 trains based on corresponding response measurements from a ship without forward speed. 296

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# 5. APPLICATION STUDIES

The previous sections have summarised different approaches for shipboard SSE, using the vessel itself as a wave buoy. In the past, the author has made numerous studies, alone and with colleagues, applying the aforementioned approaches both on simulated response data and on full-scale recordings for estimating the on-site sea state. However, the present section has *not* the aim to widely discuss or show the outcome of the studies and analyses; neither by words nor graphically. Instead, the purpose of this section is to point out some main findings from the mentioned studies dealing both with the frequency and the time domain approaches.

5.1. Frequency Domain SSE. Two main concepts for sea state estimation in the frequency domain were 305 outlined in Section 3; (a) one based on a direct comparison of measured and theoretically calculated response 306 spectra, and (b) another based on *energy equivalence* focusing on spectral moments. In case of the former 307 concept (a), the sea state estimate is obtained by solving for each spectral ordinate of the wave spectrum; 308 either by Bayesian modelling, strictly minimising a discrete version of Eq. (1), or by parametric modelling, 309 optimising a set of sea state parameters of a given parameterised wave spectrum. In the concept based on 310 energy equivalence (b), the sea state estimate is obtained by optimising also for a set of wave parameters, 311 but considering the integrated variant of Eq. (1). 312

5.1.1. *Direct Comparison of Spectral Energy Distribution*. As outlined in Subsection 3.1, Bayesian or parametric modelling is applied to produce an estimate of the on-site sea state from comparison between spectra
of corresponding responses. In either case, the final outcome is a frequency-directional wave spectrum as
illustrated in Figure 7.



FIGURE 7. *Typical wave spectrum obtained by wave buoy analogy; integrated frequency spectrum (top) and directional spectrum (bottom).* Nielsen et al. (2013)

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It is the author's experience that the two techniques - Bayesian and parametric modelling - generally produce 317 results with little deviation; in particular when integrated sea state parameters (significant wave height, 318 peak period, mean wave direction, etc.) are considered. This has been confirmed in an extensive study by 319 Nielsen et al. (2013), where more than 100 hours of response data from an in-service large container ship 320 (L = 349.0 m, B = 42.8 m, T = 14.5 m) were analysed. Specifically, it was shown that daily statistics 321 of integrated wave parameters agree well between the two sets of results. It is noteworthy that sea state 322 estimates by other means, in this case wave radar data and hindcast studies, respectively, produced similar 323 results. Figure 7 shows sample plots of the estimated wave spectrum corresponding to one particular instant 324 in time (17:30 UTC, 12. Aug. 2011) based on 15 minutes of past measurements data; the results of Bayesian 325 (Hs = 2.2 m) and parametric (Hs = 2.0 m) modelling are included. The whole data set, that is, all estimations 326 are summarised in Figure 8, where the correlation between results of Bayesian and Parametric modelling, 327 including wave radar data, is shown. Results are given for the significant wave height, the zero up-crossing 328 period and the relative wave heading (180 deg. is head sea, positive values indicate waves from starboard 329 side). 330



FIGURE 8. Correlations between estimates of integrated wave parameters as obtained by different shipboard techniques, including parametric (PAR) and Bayesian (Bay) model-ling, respectively, and wave radar (Wamos).

In another comprehensive study by Nielsen and Stredulinksy (2012), focus was made on parametric mod-331 elling alone. In this study, sea trials motion data from a small research vessel (L = 71.5 m, B = 12.8 m, 332 T = 4.8 m) together with data from traditional wave buoys were analysed, and the purpose was to examine 333 the sensitivity of sea state estimates by using sets of different vessel responses as input for the wave buoy 334 analogy. The trials were carried out in the sea off Nova Scotia, Canada, with the detailed paths shown in 335 Figure 9. Sample results are seen in Figure 10, where estimates by the wave buoy analogy (parametric 336 modelling) are compared with measurements by a Triaxys<sup>TM</sup> buoy. The plots are produced for one spe-337 cific set of responses {roll angle, pitch angle, lateral acceleration} relative to the ship's COG, and it can be 338 seen, that in these cases, the agreement is good; even for the multi-modal case shown at the right-hand side. 339



FIGURE 9. Voyage map, including detailed paths of individual trials.(Stredulinsky, 2010)

However, as pointed out in several publications (Tannuri et al., 2003; Pascoal et al., 2007; Simos et al., 2007;



FIGURE 10. Estimated wave spectra (WBA) and 'measured' spectra (Triaxys). (Nielsen and Stredulinksy, 2012)

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Sparano et al., 2008), and thoroughly analysed by Nielsen and Stredulinksy (2012), the selection of different combinations of motion components may significantly influence the sea state estimates from the wave buoy analogy. It is therefore of a particular concern to make sure that the most sensible set of motions/responses always is (automatically) selected. On the other hand, it is by no means straight-forward how to develop such a selection process, automatically and in real-time providing the best combination of responses; and work in this area is still ongoing with auspicious results in a newly publication by Montazeri et al. (2016b) that introduce an approach based on *local sensitivity analysis*.

In terms of accuracy and general results in previous studies, it is difficult for the author to favour the one modelling procedure to the other, and the computational efficiency of the methods is also comparable. Typically, an estimate is provided in about 5 minutes on a standard PC (Intel(R) Core(TM) i7-4600U @ 2.10 GHz). In practice, this means that "real-time" updates of sea states are possible, as a sea state, for most purposes, is taken to be stationary for periods of approximately 20 minutes; only accounting for the sea state
 itself and not any change in vessel speed and/or heading which would lead to nonstationary responses.

The most notable difference between the two procedures is probably the ability of the Bayesian method to (better) estimate wave spectra which do not follow "standard parametric shapes", since each spectral component of the wave spectrum is solved for (i.e. estimated) individually. On the other hand, for most practical cases, a *summation* of parameterised wave spectra like, for instance, JONSWAP can be fitted to represent most ocean wave spectra, like it was seen in Figure 10 for the multi-modal case on the right-hand side.

5.1.2. Energy Equivalence: Comparison of Spectral Moments. In the recently developed method, based on 360 energy equivalence, the ambition by the authors (Montazeri et al., 2016a) was partly to make a practical 361 robust procedure and partly to increase the computational efficiency of the wave buoy analogy; without 362 affecting the ability to provide accurate sea state estimates. This ambition is strived for by optimising the 363 wave parameters of a parameterised spectrum, containing a swell system and a wind sea system, using a 364 partitioning technique to estimate separately the individual systems. Clearly, due to its recent development, 365 the method needs to be further tested but, based on preliminary analyses of simulated data, promising results 366 have been obtained. The performance of the method has been examined thoroughly by Montazeri et al. 367 (2016a), testing the method's capability to estimate both unimodal and bimodal wave spectra, generated by 368 pure wind sea and, respectively, mixed sea (wind + swell) conditions. In the study, simulations of motion 369 responses were carried out for a container ship (L = 349.0 m, B = 42.8 m, T = 14.5 m) similar to that 370 studied in the previous subsection. Sample results of the study can be seen from Table 1, which presents the 371 outcome of four test cases, M to P, all representing a mixed sea condition, with a wind sea and a swell part. 372 From the table, the true wave parameters for both parts appear;  $H_s$  is significant wave height,  $T_p$  is peak 373 period of the particular spectrum (wind sea or swell),  $\mu$  is relative wave heading,  $s_{max}$  is maximum spreading 374 parameter (Montazeri et al., 2016a). In the analysis, the true parameters have been used to simulate 15 375 stochastic wave realisations, including corresponding sets of vessel responses, for each case. Subsequently, 376 one set of vessel responses at a time has been used as input for the estimation method, and the outcome is 377 a set of corresponding estimated wave parameters. Thus, mean values and associated standard deviations 378 were obtained for the 15 realisations of each case (M, N, O, P). It is noteworthy that the sensitivity to the 379 used set of transfer functions, i.e. RAOs, was investigated by using RAOs calculated by two different sets of 380 software, say, I and II; but except from that the RAOs have been computed for the same responses under the 381 exact same input conditions with respect to draft, speed, etc. In the one situation, labelled 'RAO1', the RAOs 382 of software I were used to both simulate the stochastic wave realisations and to subsequently estimate the sea 383

Case		Wind sea				Swell			
		$H_s(m)$	$T_p(s)$	$\mu({ m deg.})$	S <sub>max</sub>	$\overline{H_s(\mathbf{m})}$	$T_p(s)$	$\mu({ m deg.})$	s <sub>max</sub>
Ι	True	3	8	45	10	5	15	-135	25
	mean (RAO1)	3.1	8.8	66	15	5.2	15	-160	33
	mean (RAO2)	4	8.5	52	15	4.2	15	-101	60
	std (RAO1)	0.7	0.49	10	0	0.6	0.5	12	5.8
	std (RAO2)	0.3	0.55	1.5	5	0.8	0.4	13	20
J	True	3	8	-90	10	5	15	90	25
	mean (RAO1)	3.2	8.6	-106	18	4.4	16.6	98	27
	mean (RAO2)	3.6	9.2	-92	20	3.8	15.1	120	47
	std (RAO1)	0.57	0.75	22	2	1.3	1	7.6	14
	std (RAO2)	0.25	1.3	17	0	0.08	0.6	30	20
К	True	3	8	135	10	5	15	45	25
	mean (RAO1)	2.3	7.3	120	12	5.5	13	49	65
	mean (RAO2)	3.4	6.7	141	15	5.8	12	3	64
	std (RAO1)	0.5	0.8	13	0	0.4	0.1	14	20
	std (RAO2)	0.2	0.2	10	3	0.5	0.1	16	23
L	True	3	8	90	10	5	15	180	25
	mean (RAO1)	3.6	9.1	89	15	5.3	16	174	49
	mean (RAO2)	3.3	6.8	100	18	5.8	14	176	59
	std (RAO1)	0.5	0.1	2	0	0.9	2.7	4	28
	std (RAO2)	1	0.9	2	4	0.8	0.6	11	12

TABLE 1. True and estimated wave parameters obtained in a comprehensive simulation study focusing on SSE based on energy equivalence. (Montazeri et al., 2016a)

state. In the other situation, labelled 'RAO2', RAOs of software I were used for the simulation part, whereas 384 RAOs of software II were used in the estimation part. This latter situation resembles a situation close(r) 385 to reality, since the 'input conditions' are never exactly known during full-scale operational service. On 386 average, the best estimates are observed for 'RAO1'; both in terms of mean values and standard deviations. 387 However, the important point in this context is that reasonable estimates are found even for 'RAO2'; and the 388 differences between the results of 'RAO1' and 'RAO2' are barely noticeable from Table 1. Altogether, good 389 agreement is found between the true and the estimated wave parameters and the study proves both robustness 390 and computational efficiency of the proposed method. A number of other interesting findings are reported 391 by the original paper (Montazeri et al., 2016a), but no further remarks are given in the present review. 392

5.2. **Time domain SSE.** The number of studies focusing on the time domain procedures, Kalman filtering and the stepwise procedure, respectively, are (still) limited compared to the number of frequency-domain studies. In the future, this is likely to change and the present subsection briefly summarises some of the existing work that further elaborations may rely on.

5.2.1. *Kalman Filtering*. In the first study (Pascoal and Soares, 2009), where Kalman filtering was applied, the implementation was made for the zero-forward speed case only, and just numerical simulations of motion data were studied. Similar to any of the frequency domain procedure, the introduction of advance speed in

the Kalman filtering approach is elementary, in theory; however, in practice, the implementation is by no 400 means straight-forward. The study by Pascoal et al. (2016) addresses partly the effect of forward speed, but 401 only in a "qualitative manner", since the work does not describe any details about the actual implementation 402 of advance speed. On the other hand, the practical implementation of the advance-speed problem was the 403 very topic of a recent MSc thesis by Ding (2016), supervised by the present author. The MSc study shows 404 how forward speed can be successfully included, but the implementation is restricted to long-crested waves, 405 and, as a consequence, simulation data is studied only for which reason there is still further work to be made. 406 One test case from the study is shown in Figure 11, which applies for a container vessel (L = 175.0 m, 407 B = 25.4 m, T = 9.5 m) at speed 10 knots in stern quartering waves. The plot shows the statistics, i.e. 408 average, of totally fifty estimations with the same true input wave parameters:  $H_s = 4.0 \text{ m}, T_z = 10.0 \text{ s},$ 409  $\chi = 045$  deg. The individual estimation is based on a set of simulations of two responses, heave and pitch, 410 realised from a wave elevation process with the given (true) wave parameters. As can be seen from the plot, 411 the agreement between the estimated spectrum and the true spectrum is, on average, good; both in terms of 412 the total area under the spectra (= energy of the wave system), measured by the significant wave height, and 413 the location of the spectra' peak, taken as the peak frequency. However, while the estimated peak frequency 414 consistently agrees well with the true peak frequency, some variation in the amount of energy is observed; 415 seen from the dashed lines representing the lower and upper extremes of the estimated spectra considering all 416 fifty outcomes. Evaluated by numbers, the mean significant wave height is  $\hat{H}_s = 3.7$  m with the coefficient 417 of variation being 0.17. 418



FIGURE 11. Wave estimation using Kalman filtering. Full lines indicate 'average spectrum', while dashed lines represent lowest and highest energy content in estimated spectrum, obtained from fifty sets of estimations. (Ding, 2016)

5.2.2. Stepwise Procedure. The stepwise method is limited to handle only the estimation of regular wave 419 trains from corresponding response measurements on a ship without forward speed. However, very prom-420 ising results have been found in simulation studies and from model-scale experiments outlined by Nielsen 421 et al. (2015) and Nielsen et al. (2016), respectively. In the former studies, one of the test cases focuses on a 422 container ship (L = 349.0 m, B = 42.8 m, T = 14.5 m) being exposed to a regular wave train described 423 by a wave frequency  $\omega = 0.6$  rad/s and an amplitude  $\zeta_a$ . The value of the amplitude is initially 1.0 m but 424 increases to  $\zeta_a = 2.0$  m during a short period of time [300;320] s. The simulation of the wave train includes 425 measurement noise, taken as Gaussian white noise produced with a 12 dB SNR and, with this "seaway" as 426 input, the heave response is simulated in bow-quartering long-crested waves (relative wave heading equal to 427 135 deg). The wave amplitude estimate, from one simulation, is shown in Figure 12a, where the stairs are 428 explained because estimation is made on short sequences of data (5-7 wave periods), cf. subsection 4.2. The 429 complete reconstruction of the wave elevation process can be seen in Figure 12b. The plots show that the 430 wave parameters, including the actual time history, are estimated with good accuracy. The reason to test on 431 a case with a somewhat nonphysical sudden change in wave amplitude is merely to evaluate the estimation 432 method's ability to handle nonstationary data; one of the most important capabilities of the method, since 433 the method was developed to possess this very property. Indeed, a good result is achieved, and other similar 434 test cases, but with an abrupt change in wave frequency instead, show equally good behaviour. 435

The stepwise method has also been tested with experimental data (Nielsen et al., 2016), where a 1:30 scalemodel of a platform supply vessel has been exposed to regular waves in the model-basin at the Marine Cybernetics Laboratory (MCLab) at NTNU, Trondheim, cf. Figure 13.

A number of test cases were considered in the experiments and one is presented in Figures 14 and 15. Spe-439 cifically, this test case involves wave estimation based on measurements of the heave response in beam sea 440 condition, see Figure 14, where wave amplitude and period were fixed at  $\{2.0 \text{ cm}, 1.2 \text{ s}\}$  and  $\{3.0 \text{ cm}, 1.7 \text{ s}\}$ , 441 denoted by Case D and Case E, respectively. In both situations, the actual wave train has been estimated 442 from 200 seconds data recordings and the results are seen in Figure 15, where the individual plot represents 443 a zoom of a time window selected arbitrarily from the full estimation sequence lasting 200 seconds in both 444 cases. In the plots the true amplitude levels are indicated, and it is seen that the estimated results are good. 445 For the two cases, the estimated (mean) wave periods are  $T_{est} = 1.21$  s and  $T_{est} = 1.71$  s, which agree 446 nicely with the true periods. In the model-basin, the wave elevation is usually measured by a wave probe 447 but, unfortunately, the probe was malfunctioning on the days when the experiments were conducted. Con-448 449 sequently, no comparisons can be made between the estimated wave elevation and the actual true one. As another remark, it should be noted that the "simulations-only" examples, addressed by Nielsen et al. (2015), 450



(a) Estimated wave amplitude (full line) and true one







FIGURE 12. Sea state estimation based on heave response of a container vessel exposed to bow-quartering regular waves (U = 0 knots), including measurement noise (12 dB SNR).



FIGURE 13. *Experimental facilities at the Marine Cybernetics Laboratory, NTNU.* (Brodtkorb et al., 2015)

were studying also the capability to handle nonstationary conditions, such as sudden changes to the (true) wave parameters of the wave train to be estimated. The same kind of experiments cannot not be made in the model-testing facility, since it is possible only to change the control mechanism of the wave generator after a full stop.



FIGURE 14. Samples of time history recordings of the response measurements. Cases D and E represents the heave motion. In the post-analysis, the measurements have been averaged to zero-mean. (Nielsen et al., 2016)



FIGURE 15. *Estimation of wave elevation history from model-scale experiments*. (Nielsen et al., 2016)

Obviously, the stepwise estimation method must be extended before it has practical relevance as a means for 455 shipboard SSE along with the other techniques addressed in the present paper. Two notable points in future 456 suggested studies are: (1) The extension to consider regular wave trains composed by two wave components 457 could be beneficial, as it would provide knowledge about how to handle estimation of an irregular wave 458 train made up by a (very) large number of regular wave components. Specifically, work could address the 459 use of several notch or bandpass filters to select individual harmonic components from a wave spectrum, 460 and then use a 'regular wave estimator', like the developed one, for each component. (2) The combina-461 tion/consideration of several responses simultaneously, e.g., {heave; roll; pitch} could (possibly) be used to 462 estimate also the relative wave heading. 463

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# 6. CONCLUDING REMARKS

Procedures for shipboard sea state estimation based on measured vessel responses have been studied and 465 developed since the 1970'ies. The concept of the wave buoy analogy is still not widely used in practice, 466 but it is the author's opinion that generally it has matured to a level that would be applicable for shipboard 467 decision support systems. The concept offers a reasonable alternative to the other shipboard estimating 468 means, i.e. wave radars, but the concept has lower costs and requires no (or very little) calibration compared 469 to wave radars. On the other hand, the wave buoy analogy still has weak points which need to be further 470 addressed. Notably, the ability to handle nonstationary data, which may compromise accuracy/reliability of 471 real-time sea state estimates. Moreover, it would be beneficial to be able to automatically select the best 472 combination of available vessel responses; taking into account the effect of different operational conditions. 473 In the same context, clearly there is a need to introduce fault detection and fault tolerance since, by nature, 474 all sensor signals will be faulty at times. Obviously, and beyond doubt, this point is of importance to not 475 only the wave buoy analogy, but to all components of shipboard monitoring and decision support systems. It 476 is also important to point out, when using a ship as a wave buoy, the inherent limited capability to estimate 477 waves not necessarily felt by the ship, because of the ship's motion characteristics making it a wave filter. 478 This issue is touched in a number of previous work (Nielsen, 2006, 2007; Pascoal and Soares, 2008) and a 479 means to mitigate partly the problem is to use a response such as the relative wave height (Nielsen, 2008a); 480 based on the instantaneous distance from a fixed point at/on the hull to the sea surface, measured e.g. by 481 pressure transducers (below the water line) and/or distance meters mounted on the railing. In the same line, 482 it could be interesting to consider sensor fusion, since generally wave radars are considered to yield accurate 483 estimates of wave period and direction but not always wave height; leaving out any other pro/cons related to 484 the use of wave radars. In case of sensor fusion, the Kalman filter approach offers a good setting (Pascoal 485 and Soares, 2009). Finally, efforts should look into associating uncertainty measures on the particular wave 486 parameter estimates by the wave buoy analogy. 487

The immediate use of sea state estimates onboard a ship is directly coupled to navigational guidance and decision support to the ship's master and crew, where focus is on safety and fuel consumption. In a somewhat bigger perspective other uses of shipboard sea state estimations are, for instance, linked to:

491 492 • Ships' operational profiles in a short-term sense and during their lifetime; where an issue is whether a ship meets the wave scenarios as it was designed for, notably with respect to safety and speed.

• On-shore performance evaluation of a ship and entire fleets; shipping companies should be able to make more qualified fuel performance evaluations and comparisons when (reliable) wave data at actual position(s) is available. Added resistance in waves; related to the previous point, it is desirable to have knowledge about and
 to improve models for calculating the added resistance in waves, where experimental data is still
 scarce.

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• Global network of 'wave recorders'; the total number of ships navigating the oceans is very large and, if connected in a network, an enormous amount of wave data/statistics becomes available.

Investigation of accidents; a sort of 'black box' could be installed on ships like it is known from the
 aviation industry. Thus, with information about responses as well as wave conditions, weather- and
 wave-induced accidents would be easier to investigate and analyse.

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