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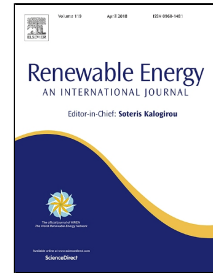
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1 Optimization under Uncertainty of a Biomass-Integrated Renewable Energy  
2 Microgrid with Energy Storage

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7 **Nomenclature**

**Abbreviations**

MG	microgrid
CHP	combined heat and power
BCHP	biomass-based CHP
GS	biomass gasifier
ICE	internal combustion engine
WT	wind turbine
PV	photovoltaic
ES	energy storage
BT	battery
PGS	producer gas storage
TES	thermal energy storage
HOB	heat-only boiler
MCS	Monte Carlo simulation
COE	cost of energy
PDF	probability density function

**Symbols**

E	electricity demand (kWh)
H	heat demand (kWh)
Z	net acquisition cost (\$)
P	purchase and installation (capital) cost (\$)
O&M	operation & maintenance cost (\$/kWh)
F	feedstock or fuel cost (\$/kWh)
C	hourly capital cost (\$/h)
M	rated capacity (kW)
N	expected life (years)
s	economic scaling factor
T	length of planning horizon (h)
V	set of all system components that contribute to capital cost
U	set of all system components that contribute to O&M cost
x	decision variable: hourly energy flow (kWh/h)

**Superscripts and subscripts**

t	time step (s)
p	actual facility

o	reference facility
i	index of installed units that contribute to capital cost
j	index of installed units that contribute to O&M and fuel cost
chr	charging
dis	discharging
min	minimum charging and discharging rate (kWh/h)
max	maximum charging and discharging rate (kWh/h)

8

9 **Abstract**

10 Deterministic constrained optimization and stochastic optimization approaches were used  
 11 to evaluate uncertainties in biomass-integrated microgrids supplying both electricity and heat. An  
 12 economic linear programming model with a sliding time window was developed to assess design  
 13 and scheduling of biomass combined heat and power (BCHP) based microgrid systems. Other  
 14 available technologies considered within the microgrid were small-scale wind turbines,  
 15 photovoltaic modules (PV), producer gas storage, battery storage, thermal energy storage and  
 16 heat-only boilers. As an illustrative example, a case study was examined for a conceptual utility  
 17 grid-connected microgrid application in Davis, California. The results show that for the  
 18 assumptions used, a BCHP/PV with battery storage combination is the most cost effective design  
 19 based on the assumed energy load profile, local climate data, utility tariff structure, and technical  
 20 and financial performance of the various components of the microgrid. Monte Carlo simulation  
 21 was used to evaluate uncertainties in weather and economic assumptions, generating a  
 22 probability density function for the cost of energy.

23 **Keywords:** microgrids, renewables integration, combined heat and power, biomass, modeling,  
 24 energy storage, uncertainty, stochastic analysis

25 **1. Introduction**

26 Microgrids (MG) are smaller distribution networks usually installed close to the end  
 27 users, and frequently contain hybrid energy resources, storage devices, and controllable loads.  
 28 The traditional power grid is generally a large-scale centralized network where power plants  
 29 generate high voltage electricity that is transferred and distributed to lower voltage end users. A  
 30 significant fraction of electrical energy is dissipated in delivery due to the long distances between  
 31 generator and load. Microgrids have been developed around the world as a means to address the  
 32 high penetration level of renewable generation and reduce greenhouse gas emissions while  
 33 attempting to address supply-demand balancing at a more local level [1].

34 The electricity generation of microgrid via solar PV and wind turbines depends, of course,  
 35 on the total solar radiation and the wind speed in general. Due to the stochastic nature of these  
 36 renewable energy resources, load behaviors, and market prices, a dispatchable generation unit is  
 37 frequently included that can be turned on or off or modulated to adjust power output accordingly.  
 38 The most common dispatchable units are diesel, natural gas, or biomass powered engine-  
 39 generators. Moreover, an energy storage system is adopted in most cases to neutralize mismatch  
 40 between generation and demand and tackle the uncertainty of demand forecasts. Energy storage

41 provides the necessary means to shift the microgrid supply to a higher market price period based  
42 on the time of use. As an alternative to energy storage, load shifting can be applied to match  
43 demand with renewable energy generation. Load shedding may also be feasible, or other types of  
44 generation added to ensure demand is satisfied [2]. MG can also be operated with connection to  
45 the central power grid, in which case the central grid is used as a backup to reduce or eliminate  
46 the need for local storage, or while completely disconnected from the central grid or islanded [3].  
47 When connected, the customer sometimes has the option of selling surplus electricity back to the  
48 utility grid operator under a net metering, feed-in, or other power purchase agreement.

49 In microgrid applications, both manufacturers and customers are interested to know the  
50 optimal capacity of the associated components of the system and the dispatch strategy to use in  
51 order to minimize cost and environmental impacts. Due to the computational complexity, a  
52 number of software packages have been developed to assist in microgrid design and assessment  
53 including HOMER [4-8] and DER-CAM [9-11]. Rohit et al. [12] proposed a hybrid off-grid  
54 system for a rural application with HOMER. Braslavsky et al. [13] presented an economic model  
55 of a shopping center, developed in DER-CAM, using on-site-specific demand, tariffs, and  
56 performance data for each technology option available.

57 Furthermore, substantial studies on microgrid optimal design and operation are typically  
58 formulated as minimization or maximization problem constrained by energy demand, capacity  
59 limits, ramping rate, and startup or shutdown times [14-21], and most address electricity only  
60 although thermal loads may also exist. Both thermal and electrical load profiles can fluctuate  
61 hourly and seasonally and utility tariff prices for natural gas and electricity may change  
62 dynamically as well. In these cases, electricity-led assumptions cannot guarantee an optimal  
63 solution overall. A number of modeling studies incorporating CHP units in the microgrid have  
64 considered both electricity and thermal demand [22-29] but few address biomass integration  
65 including separation of the fuel production and power generation components.

66 Variables that are subject to uncertainty in microgrid design and operation include  
67 unscheduled maintenance, climatic conditions (e.g. wind and cloudiness), and energy market  
68 prices and demands [30-40]. Model prediction control and receding horizon control (RHC) are  
69 frequently used to predict and make decisions under uncertainty [41-47]. Jiang and Fei addressed  
70 the problem of adopting multiple CHPs for cost reduction in microgrid using hierarchical  
71 optimization [48]. Xie et al. [49] developed a look-ahead optimal control algorithm for  
72 dispatching the generation units with the objective of minimizing both generation and  
73 environmental costs. Silvente et al. [50] used the RHC approach to analyze uncertainty in both  
74 energy generation and demand. Monte Carlo simulation (MCS) has been widely used to evaluate  
75 the reliability of a microgrid by generating data from fixed probability distributions of stochastic  
76 variables, such as wind speed, solar irradiance, customer demands, and others [51-55].

77 Currently most of the CHP integrated microgrid sizing and scheduling studies have  
78 assumed the CHP system as a single unit. However, where a fuel generation unit, such as a  
79 biomass gasifier, is deployed, producer gas production and electricity generation can also be  
80 treated as two separate and independent processes. The producer gas after biomass gasification  
81 can be used directly to fuel an internal combustion engine, microturbine, or another prime mover  
82 for power generation, and also used in a furnace or boiler for heat generation to offset utility  
83 natural gas demand [56]. Most studies considering energy storage include thermal storage or  
84 battery; separate gas storage is typically not considered, instead relying on pipeline supply as the



108 The electricity demand is met by the sum of the BCHP, WT, PV generation and the BT  
 109 discharge, within their operating limits and constraints. The electricity generated via the PV  
 110 array and WT depends on the solar radiation and the wind speed in general. The power from the  
 111 BCHP, WT and PV modules is allowed to charge the BT, depending on the operating strategy  
 112 selected. Producer gas from the BCHP unit is assumed to be purified and cooled, and can be used  
 113 directly as fuel for the engine-generator sets and the boiler, stored in the producer gas storage  
 114 tank, or simply flared for disposal if no economic demand exists and storage is at full capacity  
 115 [57]. The PGS can be charged when the energy demand is low and discharge during high  
 116 demand to improve system reliability. It can also be deployed to increase export electricity under  
 117 a power purchase agreement to raise system revenue when the utility price is high if on a time of  
 118 use tariff. For internal combustion reciprocating-type engines, heat for other uses can typically  
 119 be recovered from the engine cooling jacket, exhaust, and potentially the engine surfaces in a  
 120 combined heat and power mode. The recovered heat can be employed for a number of purposes,  
 121 including direct heat utilization but also chilling, cooling, and additional electricity generation in  
 122 a combined cycle mode although the latter is not included here. Similar to PGS, the recovered  
 123 thermal energy can be used immediately or stored in a thermal energy storage system, in this  
 124 case a warm water tank is assumed. The auxiliary HOB operates to make up any heat shortage,  
 125 with heat otherwise supplied from producer gas burned directly from the gasifier, producer gas  
 126 taken from storage (PGS), or utility natural gas.

127 For utility grid-connected scenarios, any electricity or heat supply deficits from the  
 128 microgrid are satisfied by purchasing electricity or natural gas from the utility. In some  
 129 circumstances surplus electricity from the microgrid is available for delivery to the utility under a  
 130 net metering, feed-in tariff, or other power purchase arrangement generating revenue for the  
 131 microgrid operation.

## 132 2.2. Microgrid component modeling

### 133 2.2.1. BCHP

134 BCHP is assumed to operate as a load following power plant and alter its output to meet  
 135 varying demands within the capacity limit.

$$136 P_{\text{BCHP}}(t) = f(\text{load}) \quad (1)$$

137 In the case of BCHP, routine maintenance is required, but there is also the risk of  
 138 unscheduled outages due to mechanical and other failures. In this study both the gasifier and  
 139 engine are assumed to have a certain failure risk for unscheduled maintenance and would not be  
 140 available for generation. The gasifier and engine failures are assumed to be independent, so that  
 141 the gasifier or the engine may be available when the other fails. Both the gasifier and engine  
 142 operation are treated as binary being either on (1) or off (0) with variable capacity when the units  
 143 are on. The probability density function of the Bernoulli distribution is used to represent the  
 144 stochastic nature of gasifier and engine.

$$145 f(O) = \begin{cases} 1 & \text{for } P_f \leq x < 1 \\ 0 & \text{for } 0 \leq x \leq P_f \end{cases} \quad (2)$$

146 Where  $f(O)$  is the operating mode of the gasifier or engine (independent);  $P_f$  is the failure chance  
 147 of gasifier or engine.

### 148 2.2.2. Wind turbine

149 Wind power generation depends on wind speed and the interference of the turbine with  
150 the wind. The output power of the turbine can be one of these three values [44]:

$$151 P_{wt}(t) = \begin{cases} 0 & \text{if } V(t) < V_{cutin} \text{ or } V(t) > V_{cutout} \\ \frac{1}{2}C_p\rho A_{wt}V(t)^3 & \text{if } V_{cutin} < V(t) < V_{rated} \\ \frac{1}{2}C_p\rho A_{wt}V_{rated}^3 & \text{if } V_{rated} < V(t) < V_{cutout} \end{cases} \quad (3)$$

152 Where  $P_{wt}$  is the mechanical output power of the turbine (W),  $\rho$  is air density ( $\text{kg}/\text{m}^3$ ),  $A_{wt}$  is the  
153 turbine swept area ( $\text{m}^2$ ),  $V$  is the undisturbed wind speed (m/s),  $C_p$  is the performance coefficient  
154 (or power coefficient) of the turbine, and  $V_{cutin}$ ,  $V_{rated}$  and  $V_{cutout}$  are the cut in, rated, and cut out  
155 wind speed (m/s) of the turbine.

156 Probability density functions (PDF) were used to characterize the stochastic behavior of  
157 wind speed. The wind speed over a predefined time period was estimated using a Weibull PDF  
158 [55].

$$159 f(V) = \frac{k}{c} \left(\frac{V}{c}\right)^{k-1} \exp\left(-\left(\frac{V}{c}\right)^k\right) \quad (4)$$

$$160 k = \left(\frac{\sigma}{\mu}\right)^{-1.086} \quad (5)$$

$$161 c = \frac{\mu}{\Gamma(1 + k^{-1})}$$

162 (6)

163 Where  $f(V)$  is the frequency rate of wind velocity;  $c$  is the Weibull scale parameter, a measure of  
164 the characteristic wind speed of the distribution;  $k$  is the Weibull shape parameter and specifies  
165 the shape of a Weibull distribution, taking on a value of between 1 and 3;  $\mu$  is the mean wind  
166 speed (m/s) and  $\sigma$  is the standard deviation of the wind speed (m/s). The parameters  $k$  and  $c$  can  
167 be computed from  $\mu$  and  $\sigma$ . A small value for  $k$  signifies highly variable winds, while constant  
168 winds are characterized by a larger  $k$ .

### 169 2.2.3. Photovoltaic module

170 The output power of the PV is given by the following equation [58] :

$$171 P_{pv}(t) = \eta_{pv} A_{pv} S \quad (7)$$

172 Where  $P_{pv}$  is the output power of the PV (W),  $\eta_{pv}$  denotes the conversion efficiency of the PV  
173 array (%) including the intrinsic module efficiency and array shading factor as appropriate,  $A_{pv}$  is  
174 the array area ( $\text{m}^2$ ), and  $S$  is the solar radiation, treated as a random variable ( $\text{W}/\text{m}^2$ ).

175 Solar irradiation is a stochastic variable that depends on the weather conditions and  
176 possible changes in shading throughout the day. Local shading or terrain effects that may also



177 influence the resource availability are highly site-specific and not part of this analysis. The  
 178 probabilistic nature of solar irradiance is considered to follow a beta PDF [59].

$$179 \quad f(S) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha) + \Gamma(\beta)} S^{(\alpha-1)} (1-S)^{\beta-1}, \quad \alpha \geq 0, \beta \geq 0 \quad (8)$$

$$180 \quad \beta = (1 - \mu) \left( \frac{\mu(1 + \mu)}{\sigma^2} - 1 \right) \quad (9)$$

$$181 \quad \alpha = \frac{\mu\beta}{1 - \mu}$$

182 (10)

183 Where  $\alpha$  and  $\beta$  are the function parameters and  $S$  is the horizontal solar irradiance ( $\text{kW}/\text{m}^2$ );  $\alpha$   
 184 and  $\beta$  are calculated from the mean and standard deviation of solar irradiance  $\mu$  and  $\sigma$ . Similar to  
 185 the wind speed, an hourly average solar irradiance is used.

#### 186 2.2.4. Energy storage

187 As an energy storage device, the battery storage injects power to the microgrid when the  
 188 local generation is insufficient and absorbs power from the microgrid when the local generation  
 189 is abundant or a model decision criterion indicates that saving the electrical energy for the future  
 190 hours would increase net economic benefit. Producer gas storage can be charged when the  
 191 producer gas production is abundant or a model decision criterion decides that storing the  
 192 producer gas for future generation either as electricity or heat would improve the value of the  
 193 objective function. Thermal energy storage was modeled as sensible heat storage, using water as  
 194 the storage medium, and considering only energy flows through the warm water storage tank.

### 195 2.3. Mathematical formulation

#### 196 2.3.1. Decision variables

197 Decision variables express the microgrid operating modes and the energy flows ( $\text{kWh}/\text{h}$ )  
 198 between system components. The  $x$  variables define the energy flows throughout the microgrid  
 199 system, each labeled with a subscript denoting the specific energy transfer (Fig. 1). The variables  
 200 mentioned, along with other energy transfers, are now defined according to this notation. Each  
 201 hour of the analysis involves 31 decision variables (Table 1).

202 Table 1 Decision variables.

Decision variables	Energy Flow from	Energy Flow in to	
BCHP	x1	gasifier	
	x2	gasifier	gas storage
	x3	gas storage	
	x4	gas storage	engine
	x5		engine
	x6	engine	electricity demand
	x7	electricity grid	electricity demand
	x8		electricity demand
	x9	gasifier	engine

	x10	gasifier	boiler
	x11	storage	boiler
	x12		boiler
	x13	natural gas grid	boiler
	x14	boiler	
	x15	engine heat recovery	thermal demand
	x16	thermal production	
	x17	thermal production	thermal storage
	x18	thermal production	heating demand
	x19	thermal storage	heating demand
	x20		heating demand
	x21	gasifier	flare
	x22	engine	electricity grid
	x23	engine	battery
WT	x24	wind turbine	electricity demand
	x25	wind turbine	electricity grid
	x26	wind turbine	battery
PV	x27	solar panel	electricity demand
	x28	solar panel	electricity grid
	x29	solar panel	battery
BT	x30		battery
	x31	battery	electricity demand

203

204 **2.3.2. Objective function**

205 The optimization in this case is developed from the objective to minimize the cost of  
 206 energy of over a particular time horizon (T) using an hourly time base. The objective function is  
 207 formulated as:

$$208 \text{ Min COE} = \frac{Z}{\sum_{t=1}^T (E_{\text{load}}^t + H_{\text{load}}^t)}$$

209 (11)

210 Where Z is the net energy supply cost (\$);  $E_{\text{load}}$  and  $H_{\text{load}}$  are the electricity and heating demand  
 211 (kWh); T is the length of the planning horizon (h) and t is the time step.

212 The net energy supply cost consists of the levelized fixed or capital costs of the system,  
 213 the feedstock and fuel supply costs, and all operating and maintenance (O&M) costs, all resolved  
 214 to a uniform cost of energy considering the time value of money. Capital and O&M costs in  
 215 general are subject to economies of scale and hence influenced by the size of the units included  
 216 in the system [60]. Feedstock and O&M costs assumed not to be subject to economies of scale  
 217 although in practice pricing may depend on supply quantities.

$$218 \quad Z = \sum_{t=1}^T \left( \sum_{i \in V} C_i^t + \sum_{j \in U} (O\&M_j^t + F_j^t) * x_j^t \right) \quad (12)$$

$$219 \quad C_i = \frac{P_i \quad ir(1 + ir)^N}{8760(1 + ir)^N - 1}$$

220 (13)

$$221 \quad \frac{P_p}{P_o} = \left( \frac{M_p}{M_o} \right)^s \quad (14)$$

222 Where V is the set of all installed system components that contribute to capital cost; i is the index  
 223 for all the installed units that contribute to capital cost; U is the set of all energy flows that create  
 224 O&M and fuel cost; j is the index for the energy flows that create O&M and fuel cost; C is the  
 225 hourly leveled capital cost (\$); O&M and F are the hourly O&M and fuel cost of energy flow j  
 226 at time t (\$/kWh); x is the energy flow (kWh); P is the overnight purchase and installation cost  
 227 that is influenced by an economy of scale defined by the value of s ( $0 \leq s \leq 1$ ) [61]; ir is the  
 228 interest rate, and N is expected life time (y). The constant 8760 is the conversion for the number  
 229 of hours per year and is uncorrected for leap years. For the equation defining the economy of  
 230 scale, P<sub>p</sub> is the capital cost of facility or unit under consideration within the microgrid; P<sub>o</sub> is the  
 231 known capital cost of a reference facility or unit of the same type, M<sub>p</sub> is the rated capacity of the  
 232 unit under consideration; M<sub>o</sub> is the rated capacity of the reference unit.

### 233 2.3.3. Constraints

234 All energy flows ( $x_{1-31}$ ) are signed with lower (zero) and upper bounds with the latter  
 235 being the maximum acceptable capacities. The electricity balance constraints the electrical  
 236 demand to be satisfied by BCHP, WT, PV, BT or the grid power. The heat balance constraints  
 237 the heating demand to be satisfied by the producer gas powered boiler, the natural gas powered  
 238 boiler, the heat recovered from engine generator set, or some combination of these sources.  
 239 Therefore, the energy balances at time t for the microgrid can be written as follows:

$$240 \quad x_6^t + x_7^t + x_{24}^t + x_{27}^t + x_{31}^t = E_{load}^t \quad (15)$$

$$241 \quad x_{20}^t = H_{load}^t \quad (16)$$

242 The BT and PGS storage levels at the current time step t depend on the storage level at  
 243 previous time step (t-1) and the current charging or discharging rate. The BT and PGS energy  
 244 balances are:

$$245 \quad BT^t = BT^{t-1} + x_{30}^t - x_{31}^t \quad (17)$$

$$246 \quad PGS^t = PGS^{t-1} + x_2^t - x_3^t \quad (18)$$

247 Where BT<sup>t</sup> and PGS<sup>t</sup> are the energy storage level at current time step t, BT<sup>t-1</sup> and PGS<sup>t-1</sup>  
 248 the amounts of energy stored in BT and PGS at previous time step t-1.

249 Storage level constraints require that storage levels should be in the range between the  
 250 minimum and maximum determined safety and economy. The constraints of charging and

251 discharging indicate the changing rate for BT and PGS should be within the upper and lower  
 252 limits. The maximum charge and discharge rate is for the model developed here assumed to be  
 253 half of the rated capacity. The charging and discharging efficiencies of BT and PGS are assumed  
 254 small although this is not a general constraint of the model. The constraints for TES are as same  
 255 as BT and PGS.

$$256 \quad BT_{\min} \leq BT^t \leq BT_{\max} \quad (19)$$

$$257 \quad BT_{\text{chr}_{\min}} \leq x_{30}^t \leq BT_{\text{chr}_{\max}} \quad (20)$$

$$258 \quad BT_{\text{dis}_{\min}} \leq x_{31}^t \leq BT_{\text{dis}_{\max}} \quad (21)$$

$$259 \quad PGS_{\min} \leq PGS^t \leq PGS_{\max} \quad (22)$$

$$260 \quad PGS_{\text{chr}_{\min}} \leq x_2^t \leq PGS_{\text{chr}_{\max}} \quad (23)$$

$$261 \quad PGS_{\text{dis}_{\min}} \leq x_3^t \leq PGS_{\text{dis}_{\max}} \quad (24)$$

262 Where  $BT_{\min}$  and  $BT_{\max}$  are the minimum and maximum allowed BT energy storage level  
 263 at any time, and the same goes for PGS;  $\text{chr}_{\max}$  and  $\text{dis}_{\max}$  are the maximum allowed charging and  
 264 discharging rates;  $\text{chr}_{\min}$  and  $\text{dis}_{\min}$  are the minimum allowed charging and discharging rates.

265 The power ramping constraint, expressed in kWh per hour, indicates how much a  
 266 generator can change its output between two successive time steps.

$$267 \quad |x_1^t - x_1^{t-1}| \leq G_{\text{ramp}_{\text{rate}}} \quad (25)$$

$$268 \quad |x_6^t - x_6^{t-1}| \leq E_{\text{ramp}_{\text{rate}}} \quad (26)$$

269 Where  $x_1$  is the biomass gasifier production at time  $t$ ;  $x_6$  is the ICE production at time  $t$ ;  $G_{\text{ramp}_{\text{rate}}}$   
 270 and  $E_{\text{ramp}_{\text{rate}}}$  are the ramping rates of the gasifier and the engine-generator, which is  
 271 related to the capacity and type.

272 Some decision variables are coupling with each other and constrained by energy balance,  
 273 for example:

$$274 \quad x_1^t = x_2^t + x_9^t + x_{10}^t + x_{21}^t \quad (27)$$

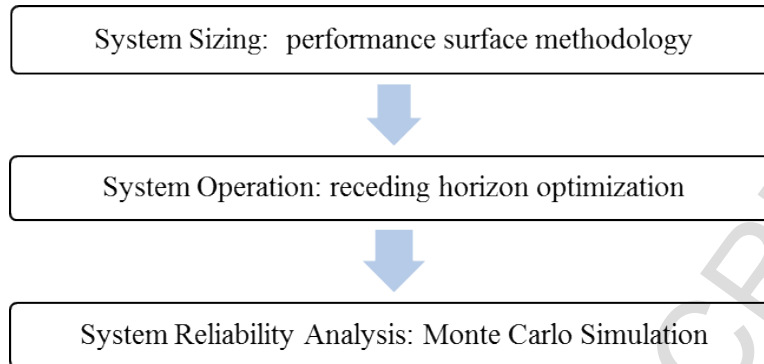
276 Where  $x_2$ ,  $x_9$ ,  $x_{10}$ , and  $x_{21}$  represents the energy flow out of biomass gasifier to either gas storage,  
 277 engine, boiler, or flare, respectively (Table 5). Similar energy balance constraints are shown in  
 278 Fig. 1.

279 This mathematical formulation of the system design and unit commitment problem is a  
 280 linear convex optimization problem. The model implementation was here solved using  
 281 MATLAB with its optimization toolbox (MATLAB 2016a, Mathworks, Natick, Massachusetts).<sup>1</sup>

<sup>1</sup> mention of a specific tradename does not constitute an endorsement by the University of California.

## 282 2.4. Solution method

283 The model discussed here chains a deterministic planning optimization module with a  
 284 stochastic module (Fig. 2).



285

286

Fig. 2. Microgrid optimization modules.

### 287 2.4.1. Performance surface method

288 The model is first solved deterministically to derive the optimal wind and solar capacities  
 289 for each proposed microgrid scenario. The capacity of WT and PV units is gradually increased  
 290 from none to 250 kW (with 10 kW of increment) in a search for the optimal capacity yielding  
 291 minimum cost with the rest of units fixed. The criterion of selecting the best hybrid energy  
 292 system combination for a proposed site is based on minimizing the cost for different renewable  
 293 combinations, the output of the optimal sizing and operation being the preferred set of WT and  
 294 PV modules. The entire procedure is repeated for all the possible combinations. The combination  
 295 with the lowest cost overall is selected as optimal design for each scenario.

### 296 2.4.2. Sliding time window

297 Once all the unit capacity has been fixed, the dispatch of the available units to meet  
 298 demand at the lowest cost is required. The hourly operation strategy of the different hybrid  
 299 configurations is determined by using linear constrained optimization. The sizing and operating  
 300 strategies are interdependent so a different set of component configurations is analyzed in each  
 301 hybrid combination to find the optimal hybrid system.

302 A sliding time window method is used to first determine the optimal operation of all  
 303 microgrid components [43, 50]. For the examples included here, a 4-hour time window is used  
 304 with known electrical and heat demand. Each hour has a total of 31 solution variables (Fig. 1),  
 305 which for a 4-hour horizon requires solving for 124 variables. Within each time window, linear  
 306 optimization is applied to obtain the gasifier, gas storage, engine, boiler, thermal storage, WT,  
 307 PV and BT operation giving the minimum operating cost. Only the solution for the first hour is  
 308 retained to compute the actual generation and cost. At the same time, the new initial conditions  
 309 of all the energy storage devices including the BT, PGS, TES units are updated. The time  
 310 window is then incremented by one hour, and the process repeated for the entire time horizon (27  
 311 hours for a 24 hour period). The sliding time window approach is summarized in the following  
 312 steps (Fig. 3).

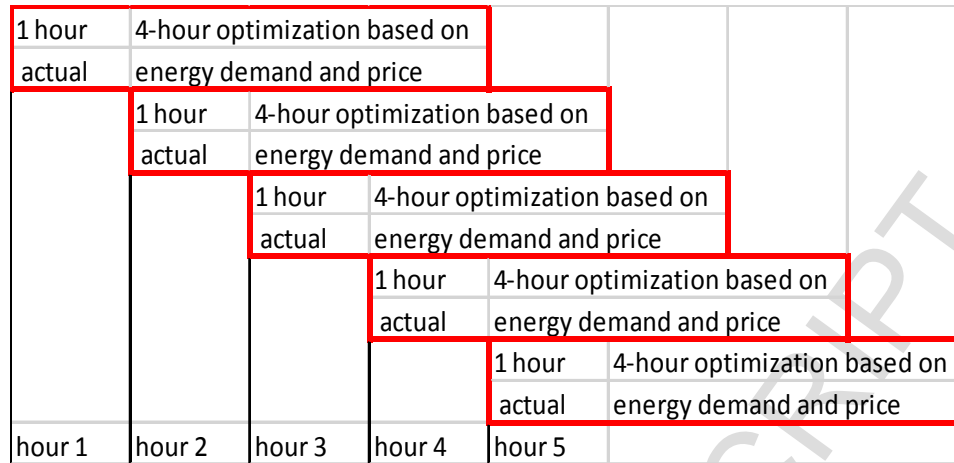


Fig. 3. Sliding window method (4-hour window illustrated over a period of 5 hours).

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1. Specify initial conditions of energy storages.
2. Optimize the system operation as outlined above for the period from  $t_{\text{initial}}$  to  $t_{\text{initial}} + T$  ( $T$ : sliding time window width).
3. Obtain the optimal operating points of all units.
4. Set the operating conditions of the first hour of the window to the optimal conditions.
5. Update energy storage conditions.
6. Slide the window 1 hour forward in time.
7. Repeat from step 2.

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#### 2.4.3. Monte Carlo simulation

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Monte Carlo simulation was conducted to generate a finite number of possible outcomes based on the probability distributions of assumed stochastic parameters. A total of 1000 Monte Carlo simulations were used to generate the cost of energy distributions for each scenario. The distribution of simulated outcomes for the 1000 realizations of the COE provided the risk profile.

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### 3. Model application

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#### 3.1. Case study definition

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The input data for the model were divided into the following categories: 1) customer information (load profile and weather data), 2) technical information (physical characteristics and specifications of all units, efficiency, heat to power ratio, power generation PDF, etc.), 3) financial information (capital cost, O&M cost, fuel costs, tariff rate). In the deterministic model, the output of the model is the optimal microgrid design and dispatch (based on the COE values). In the stochastic model, the output of the model is the probability distribution of COE.

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For the case study located in Davis, California, a typical winter daily residential electricity load profile from the local utility was scaled up and used for analysis. A winter daily thermal demand profile from the UC Davis campus was scaled down to represent thermal energy usage (Fig. 4). The studied microgrid scale is around 100 kW. Therefore, the input load profiles are scaled up or down to the desired range. For the scenario analyses, the peak and base load demand for electricity and heating were in the range of 72-200 kW and 50-172 kW, respectively. Davis hourly solar and wind data in February were obtained from the California Irrigation Management Information System (CIMIS).

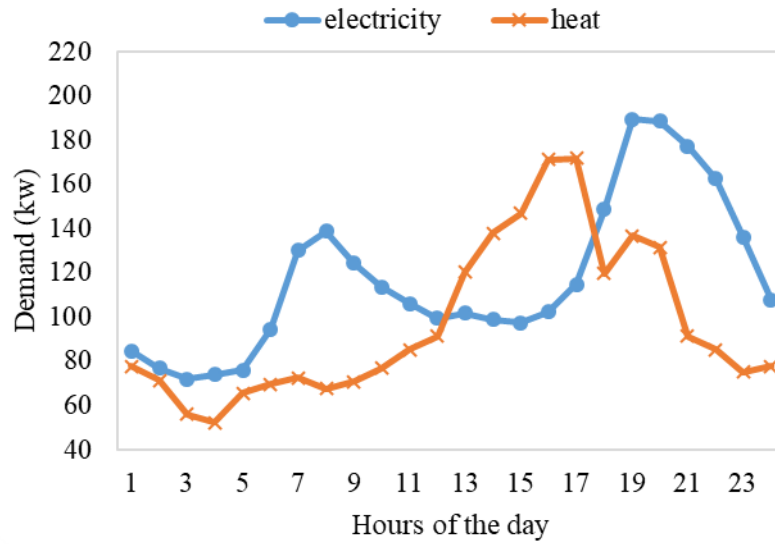


Fig. 4. Model hourly electricity and heat demand for February in Davis, California.

Technical and economic parameters for the wind turbines and PV assumed here are based on a 10 kW unit capacity. The efficiency and cost of the power converters have been included in the overall PV and wind turbines' efficiencies and costs. All parameters assumed for B CHP is based on a 100 kW unit capacity. All units are assumed to subject to 20 years life time and 6% of interest rate (Table 2).

Table 2 Technical parameters and cost assumptions for components of the microgrid [62-65].

	Parameters	Unit	Value
<b>All units</b>	Discount/interest rate	%	6
	Economic life	years	20
	Economic scale factor	-	0.9
<b>BCHP</b>	Rated power	kW	100
	Capital cost	\$/kW	4500
	O & M cost	\$/kWh	0.03
	Feedstock cost	\$/kWh	0.02
	Electricity efficiency	-	0.3
	Heat recovery factor	-	0.6
<b>WT</b>	Reference module rated power	kW	10
	Reference module rotor diameter	m	7
	Capital cost	\$/kW	2154
	O & M cost	\$/kWh	0.005
	Fuel cost	\$/kWh	0
	Cut-in wind speed	m/s	2.5
Cut-off wind speed	m/s	50	

	Rated wind speed	m/s	11
	Air density	kg/m <sup>3</sup>	1.23
	Betz Coefficient	-	0.593
<b>PV</b>	Reference module rated power	kW	10
	Reference module surface area	m <sup>2</sup>	64
	Capital cost	\$/kW	3463
	O & M cost	\$/kWh	0.005
	Fuel cost	\$/kWh	0
	Electricity efficiency	-	0.2
<b>BT</b>	Rated capacity	kWh	200
	Capital cost	\$/kWh	255
	O & M cost	\$/kWh	0
	Round trip efficiency	-	0.9
<b>PGS</b>	Rated capacity	kWh	200
	Capital cost	\$/kWh	80
	O & M cost	\$/kWh	0.005
	Round trip efficiency	-	1
<b>HOB</b>	Rated power	kW	150
	Capital cost	\$/kW	120
	O & M cost (\$/kWh)	\$/kWh	0.005
	Efficiency	-	0.85

353 Both capital and operating costs are also subject to uncertainty. An assumption was made  
 354 here that all the capital and O&M costs are uniformly distributed over the range from zero to  
 355 twice the reference cost, the lower bound representing an extreme incentive case with a high  
 356 subsidy. The gasifier and engine are both assumed to have 5% of failure risk for unscheduled  
 357 maintenance and would not be available for generation. The shape and scale factors for Weibull  
 358 and Beta distribution are estimated by the curve fitting function in Matlab based on historical  
 359 wind speed and solar irradiance data. Table 3 lists the 13 uncertainty parameters and their  
 360 associated PDFs.

361 Table 3 Stochastic parameters and assumed PDF.

Stochastic parameter	PDF	PDF specifications
BCHP Capital cost (\$/kW)	Uniform	[0,9000]
WT Capital cost (\$/kW)	Uniform	[0,4308]
PV Capital cost (\$/kW)	Uniform	[0,6926]
BT Capital cost (\$/kW)	Uniform	[0,510]
GS O&M cost (\$/kWh)	Uniform	[0,0.04]
ICE O&M cost (\$/kWh)	Uniform	[0,0.02]
WT O&M cost (\$/kWh)	Uniform	[0,0.01]



PV O&M cost (\$/kWh)	Uniform	[0,0.01]
BT O&M cost (\$/kWh)	Uniform	[0,0.002]
Wind speed (m/s)	Weibull	Shape factor k=1.6337; scale factor c=2.7813
Solar irradiance (w/m <sup>2</sup> )	Beta	Shape factor a=0.0058; scale factor b=0.070
GS availability	Bernoulli	P <sub>f</sub> = 0.05
ICE availability	Bernoulli	P <sub>f</sub> = 0.05

362 For TOU rates, the price of electricity changes by time of day (Table 4). For natural gas,  
 363 the price is assumed to be constant throughout the day. The electricity buyback price is assumed  
 364 to be \$0.04/kWh based on the net surplus compensation rate approved by the California Public  
 365 Utilities Commission (CPUC) [66].

366 Table 4 Electricity tariff rate

Energy Source	Category	Tariff rate (\$/ kWh)	Time
Electricity Buy	off-peak	0.22	00:00-09:59 am; 09:00-11:59 pm
	partial-peak	0.30	10:00-11:59 am; 07:00-08:59 pm
	peak	0.40	12:00-06:59 pm
Electricity Sell	all day	0.04	N/A
Natural gas Buy	all day	0.08	N/A

367 Five design configuration scenarios were selected to investigate various aspects of the  
 368 biomass integrated microgrid optimization (Table 5). All are utility grid interconnected, installed  
 369 with a 200 kW HOB and a 200 kWh TES. A net energy metering agreement is included with  
 370 compensation for surplus electricity delivered from the microgrid to the utility. BCHP, PV and  
 371 WT are allowed for connection to a utility meter. Scenario 1 includes only wind and PV  
 372 generation with battery storage. This option is a good alternative for locations with very limited  
 373 heat demand but abundant wind and solar resources, or areas without abundant biomass  
 374 resources. Scenario 2 includes all the all three renewable sources but without producers gas  
 375 storage. Scenario 3 also includes all three renewable sources with a full complement of producer  
 376 gas, thermal, and battery storage but the biomass component is insufficient to meet peak load by  
 377 itself. Scenario 4 is the same as Scenario 3 but with added BCHP capacity, in this case a  
 378 duplicate unit for a total biomass generation of 200 kW, slightly higher than peak load. Scenario  
 379 5 is the presumed conventional system and supplies energy demands entirely from the utility  
 380 electricity and natural gas grids.

381 Table 5 System components of the 5 proposed scenarios (●=unit included, x=unit excluded).

Scenario	BCHP_1	BCHP_2	WT	PV	PGS	BT
1	x	x	●	●	x	●
2	●	x	●	●	x	●
3	●	x	●	●	●	●
4	●	●	●	●	●	●
5	x	x	x	x	x	x

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## 383 3.2. Deterministic model results

## 384 3.2.1. Optimal microgrid design

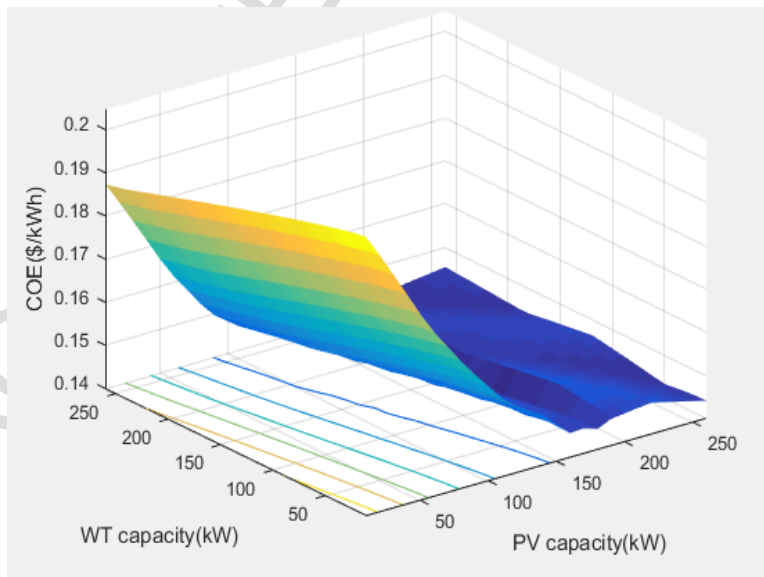
385 The lowest COE was found among all the possible combinations of WT and PV modules  
 386 (WT: 0-250 kW; PV: 0-250 kW) (Table 6).

387 Table 6 Optimal system combinations.

Scenarios	System Configuration	Optimal WT Installed units	Optimal PV Installed units
1	BCHP (0), PGS (0), BT (200)	180	170
2	BCHP (100), PGS (0), BT (200)	0	160
3	BCHP (100), PGS(200), BT(200)	0	160
4	BCHP (200), PGS(200), BT(200)	0	130
5	BCHP (0), PGS(0), BT(0)	N/A	N/A

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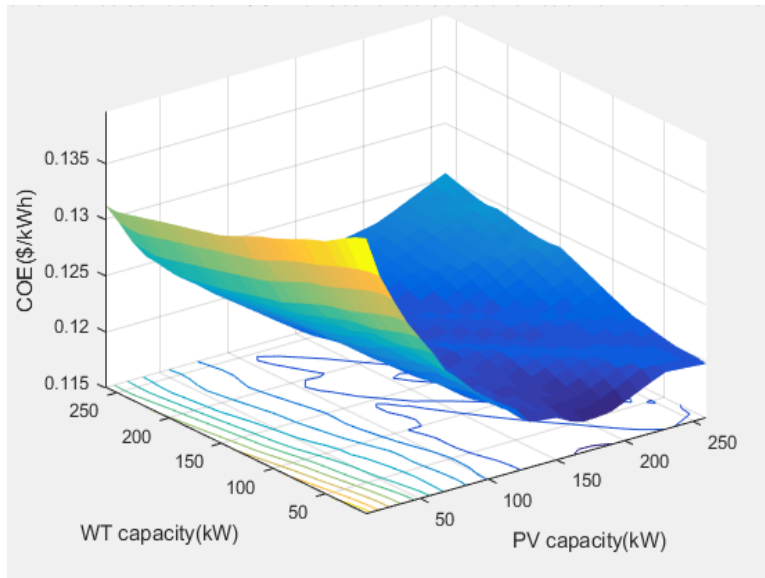
389 Figs.5-8 illustrate the 3D surface of cost response as a function of the capacities of WT  
 390 and PV for scenarios 1 to 4. The optimum WT and PV capacity can be found around the  
 391 minimum points in the figures. For scenario 1, when no BCHP is considered, the model yields  
 392 the lowest cost with 180 kW of wind capacity and 170 kW of PV capacity. For scenarios 2, 3 and  
 393 4, when BCHP is included, no wind capacity is adopted for the cost structure assumed. The  
 394 reference installed capital cost for PV was assumed to be \$3165/kW with \$0.005/kWh for O&M;  
 395 for wind, the reference capital cost was \$2175/kW with \$0.005/kWh for O&M. Although the  
 396 wind is assumed to have a lower capital cost, the wind speed profile for the site selected (Davis,  
 397 California) has only 9 hours of the day with speeds above 2.5 m/s, the cut-in wind speed. Hence,  
 398 generation is low and generation cost exceeds that of PV. From an economic viewpoint, PV and  
 399 BCHP are the most attractive technology for this site under these cost assumptions. The optimal  
 400 outcomes will in general differ depending on location. Comparing scenarios 2 and 3, no change  
 401 in installed PV capacity is associated with the addition of producer gas storage. For scenario 4,  
 402 with an oversized 200 kW BCHP, the optimal PV capacity declines to 130 kW.



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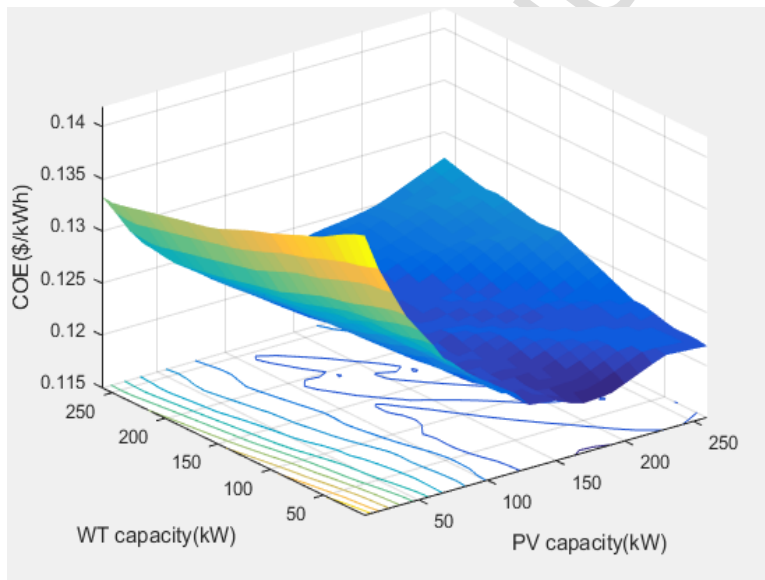
Fig. 5. COE surface of scenario 1 as a function of WT and PV capacities.



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Fig. 6. COE surface of scenario 2 as a function of WT and PV capacities.



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Fig. 7. COE surface of scenario 3 as a function of WT and PV capacities.

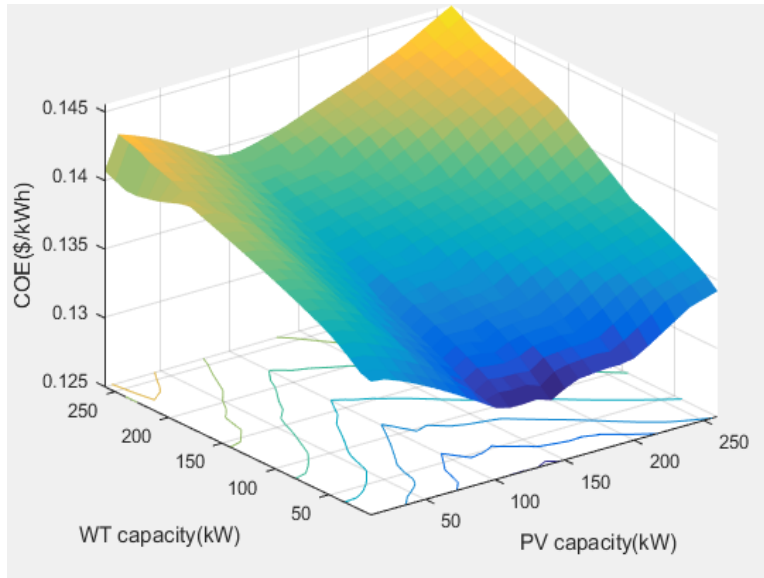


Fig. 8. COE surface of scenario 4 as a function of WT and PV capacities.

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411 For the assumptions used in these examples, the total cost of the optimal system  
 412 configuration varies from a low of \$0.1182/kWh for Scenario 2, the 100 kW BCHP with 200  
 413 kWh battery storage scenario, to a high of \$0.2029/kWh for Scenario 5, the utility only supply  
 414 scenario. Scenario 4, with a 200 kW BCHP capacity and 130 kW of PV achieves 100%  
 415 renewable supply through the microgrid with no utility purchase, but is higher in generation cost  
 416 than the hybrid microgrids of Scenarios 2 and 3 relying on both microgrid and utility generation.  
 417 Because of the boiler's installation, there is also installation cost in scenario 5 (Table 7).

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Table 7 Optimal COE values and cost composition for 5 scenarios.

Composition of total cost (\$)	scenario 1	scenario 2	scenario 3	scenario 4	scenario 5
Installation	239.75	259.91	263.37	334.94	7.70
O&M+Fuel	19.44	276.51	281.33	342.99	11.60
Electricity purchase	290.26	55.18	55.18	0.00	804.42
Natural gas purchase	218.44	28.44	28.45	0.00	218.44
Net metering credit	-16.48	-12.77	-10.95	-5.01	0.00
Daily total cost	751.40	607.27	617.37	672.91	1042.16
<b>COE (\$/kWh)</b>	<b>0.1462</b>	<b>0.1182</b>	<b>0.1202</b>	<b>0.1310</b>	<b>0.2029</b>

421

422 Fig. 9 illustrates the economic results for the proposed 5 scenarios. Even with additional  
 423 capital and installation costs, the introduction of BCHP reduces the need for electricity and  
 424 natural gas purchases, and the overall total cost and COE are decreased through this on-site  
 425 generation. In addition, the producer gas storage does not lead to obvious economic gains, due to  
 426 the low cost assumed for purchased natural gas.

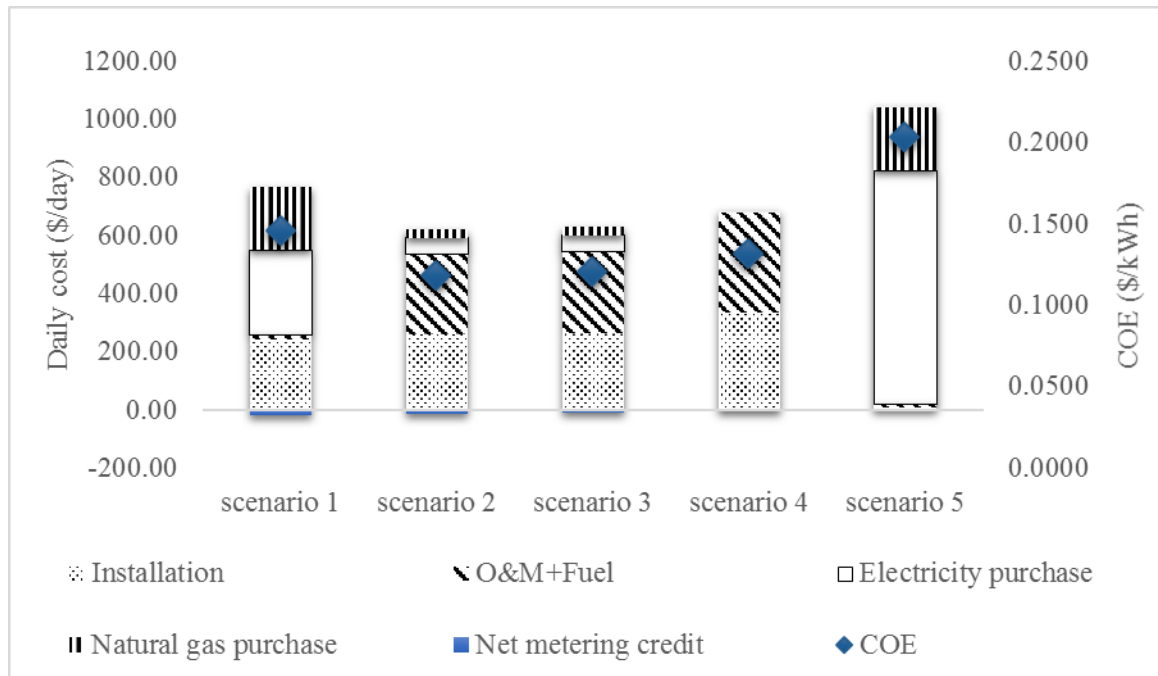


Fig. 9. COE values and cost composition for various scenarios.

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To evaluate the effect of demand patterns from other times of the year on the optimal microgrid configuration, the model was also tested using daily electrical and thermal load data for summer. The lowest cost, \$0.1136/kWh, is also found for scenario 2 employing the 100 kW BCHP with solar PV and battery storage. Scenario 1, with a 170 kW wind turbine capacity and 130 kW of PV achieves a COE of \$0.1349/kWh, which is lower than the COE of scenario 1 in winter. That is because the heating demand is much lower in summer and the influence from the absence of a heat source in scenario 1 is minimized. For the same reason, the COE of scenario 4, with a 200 kW gasifier, is \$0.1390/kWh in summer, which is higher compared to the COE in winter.

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### 3.2.2. Optimal microgrid dispatch

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Figs. 10-13 illustrate the optimal energy flows from the BChP, WT, PV, and BT units as well as the grid to the demand during the selected 24 hour period. These graphs show the optimal dynamic operation based on the cost minimization.

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For scenario 1, when no BChP is adopted, most of the electricity during midnight to early morning is supplied by purchasing electricity from the utility due to the absence of PV generation and low wind speed (<2.5 m/s) for the data set selected. The morning peak load demand occurs between 07:00 to 09:00 am coinciding with an increasing time of use tariff; therefore, the BT is used to balance the demand in conjunction with PV. From 10:00 am to 16:00 pm, all of the electricity is generated from PV. After 07:00 pm, PV generation declines while as does the wind generation and import of grid power again increases to meet the nighttime demand (Fig.10).

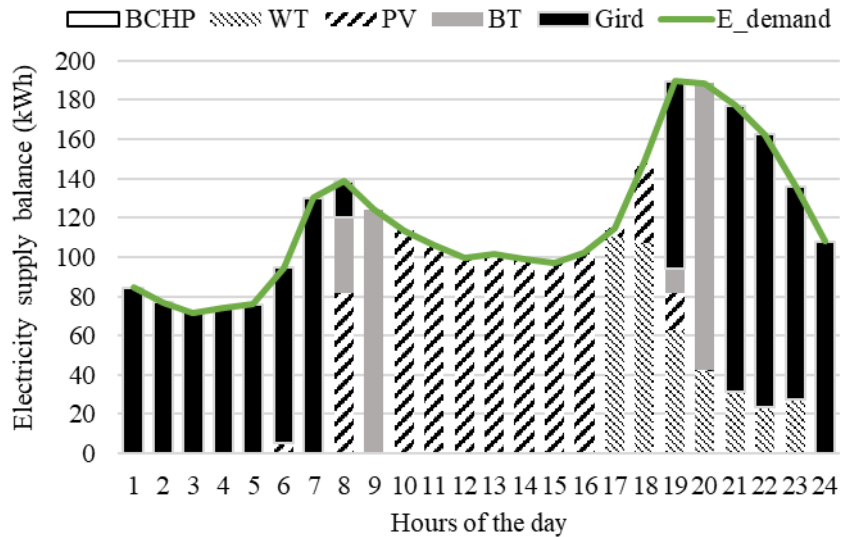
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Scenarios 2 and 3 show similar optimal operating schedules except for the addition of the BChP that carries most of the demand not met by PV. Grid electricity is purchased after 20:00

452 when both BT reserve is depleted, PV is absent and the residual demand exceeds the 100 kW  
 453 supply from the BCHP unit (Figs. 11-12).

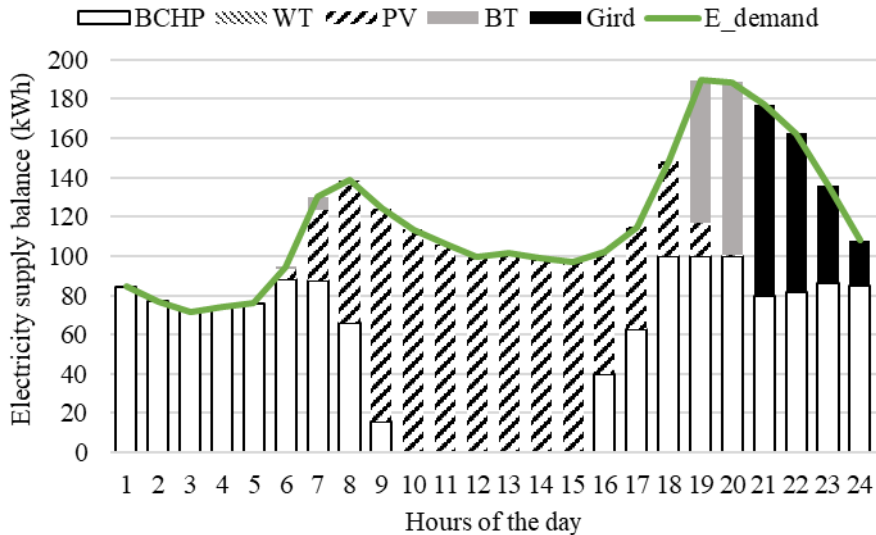
454 Scenario 4 considers the case of having an oversized BCHP (200 kW) in the microgrid.  
 455 In this case the BCHP is large enough to meet virtually all the nighttime demand when lower  
 456 cost PV generation is absent with the exception of a small contribution from the battery in the  
 457 later evening. No grid power is purchased and the microgrid independently meets the full system  
 458 demand (Fig. 13).



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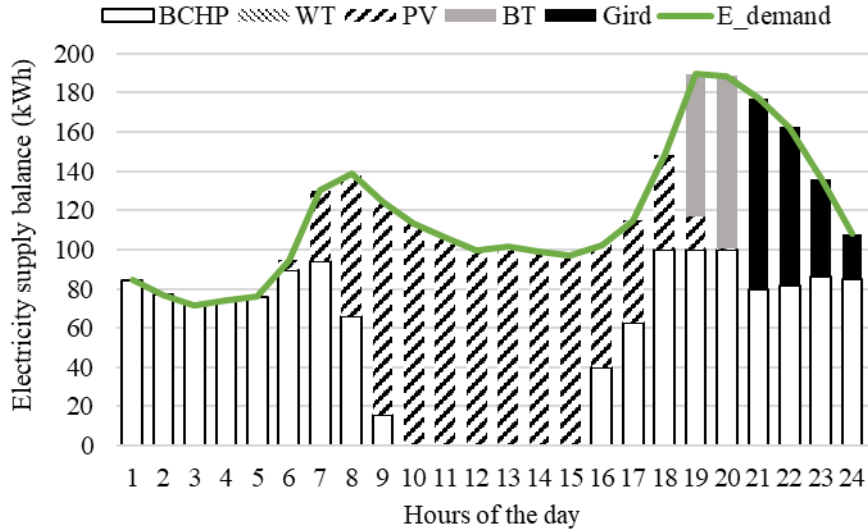
Fig. 10. Optimal electricity supply for scenario 1.



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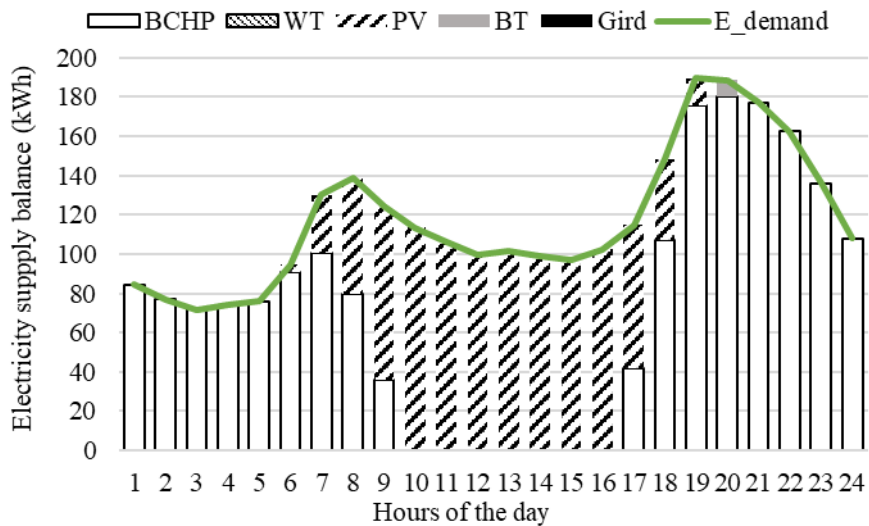
Fig. 11. Optimal electricity supply for scenario 2.



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Fig. 12. Optimal electricity supply for scenario 3.



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Fig. 13. Optimal electricity supply for scenario 4.

### 467 3.3. Sensitivity analyses

468 Sensitivity analyses were performed on BT capacity, electricity and natural gas prices,  
 469 and energy demands. The analysis was based on the results obtained from the most optimistic  
 470 WT and PV capacities giving the lowest cost.

#### 471 3.3.1. Effects of battery capacity

472 To study the effect of battery capacity on the COE, the battery energy storage was varied  
 473 from 0 to 300 kWh. The upper limit corresponds to the storage size of charging the battery with  
 474 100 kWh/h for 3 h. Because the sliding time window width is 4 h, the BT should be able to store  
 475 at least 3 h of production. Fig. 14 illustrates COE as a function of the battery size for the 4  
 476 scenarios with the optimal capacity of WT and PV. For scenarios 1, 2 and 3, the COE decreases



477 as the storage size increases. The larger the storage, the less purchased electricity is required by  
 478 the customer during the higher tariff period. At approximately 125 kWh, the COE begins to  
 479 increase due to the limitation of the gasifier capacity. With increasing length of the prediction  
 480 window, part of the storage capacity becomes redundant. For example, if with an 80 kW engine-  
 481 generator set and a 12 hours sliding time window, even if 100% of the model generation is  
 482 stored over the first 11 hours, the optimal BT capacity will not be 880 kWh, but instead will be  
 483 something less to still meet the demand over the model interval.

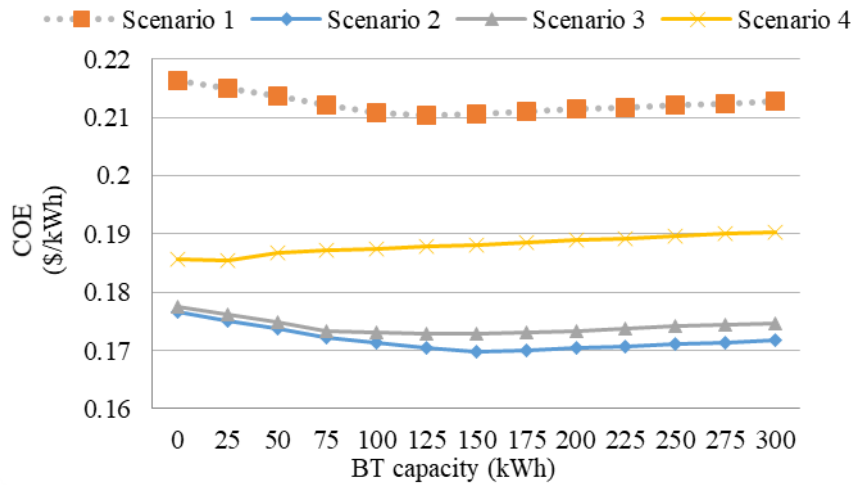


Fig. 14. COE as a function of battery capacity.

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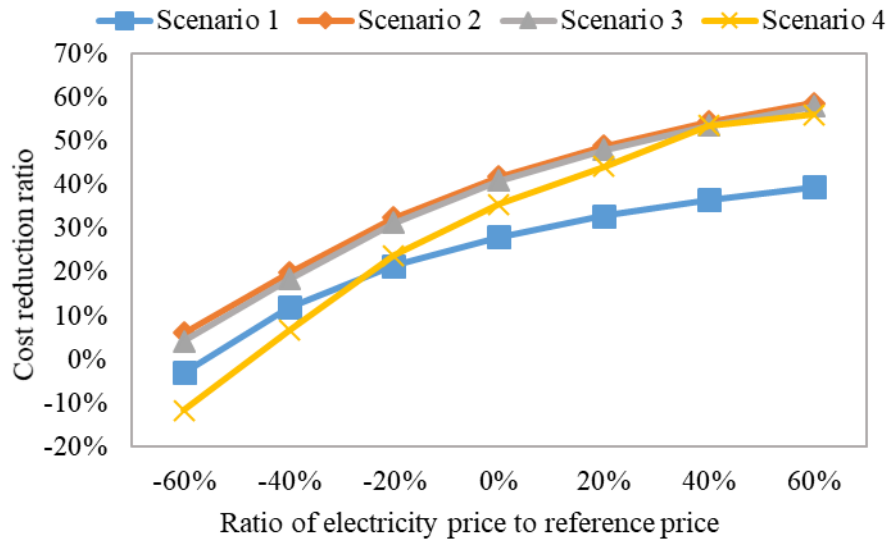
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### 486 3.3.2. Effects of electricity and natural gas price

487 Fig. 15 and Fig. 16 show the results for the cost reduction ratio obtained by changing the  
 488 electricity and natural gas price from 60% below to 60% above the reference prices. The  
 489 microgrid provides greater cost savings as the price of purchased electricity increases (Fig. 15).  
 490 However, the marginal benefit of having the microgrid declines with increasing grid price. A  
 491 breakeven point is found for scenarios 1 and 4 at grid prices that are 55 and 45% lower than the  
 492 assumed base case or reference price (negative cost reduction ratios indicate a preference for  
 493 utility grid purchase). Moreover, although scenario 4 has the lowest cost savings at lower grid  
 494 prices, as the grid price increases this scenario eventually achieves the same savings as scenarios  
 495 2 and 3 and breaks even with scenario 1 at a grid price about 20% lower than the reference price.  
 496 If the electricity price is reduced more than 20%, the no-BCHP case, scenario 1, is preferred. As  
 497 the purchased electricity price continues to increase, the larger BCHP capacity becomes more  
 498 attractive.

499 For scenario 1, as natural gas price changes from 60% below to 60% above the reference  
 500 price, the COE cost reduction ratio decreases from 32% to 25% due to the lack of heat recovery  
 501 from a BCHP unit (Fig. 16). For scenarios 2, 3 and 4, the BCHP heat recovery and producer gas  
 502 can almost meet the full heat demand, therefore, increasing natural gas price does not influence  
 503 the COE reduction ratio and a nearly positive linear relationship develops over the remainder of  
 504 the cost range.

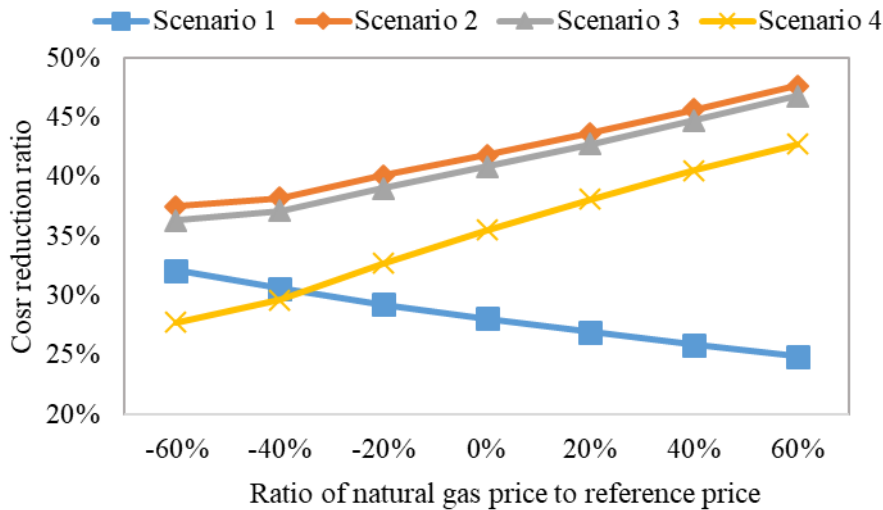




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Fig. 15. COE reduction ratio as a function of increased electricity price.



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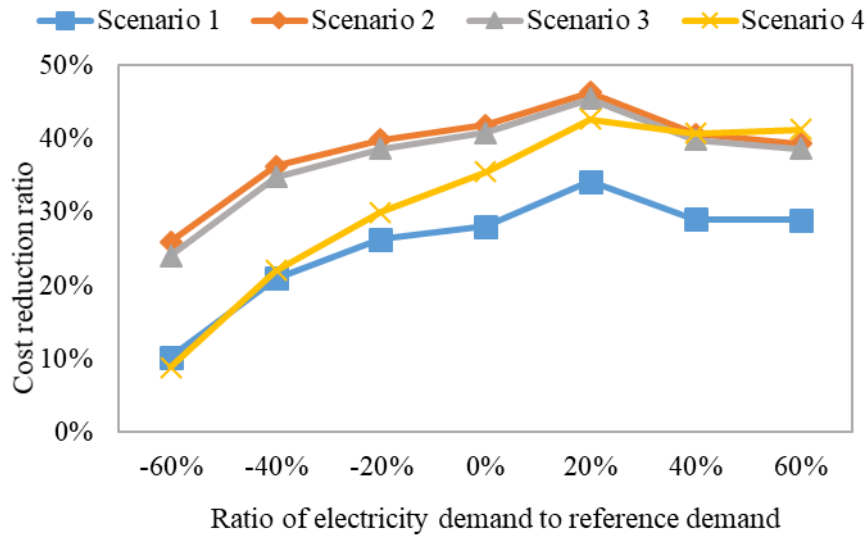
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Fig. 16. COE reduction ratio as a function of increased natural gas price.

### 509 3.3.3. Effects of demand changes

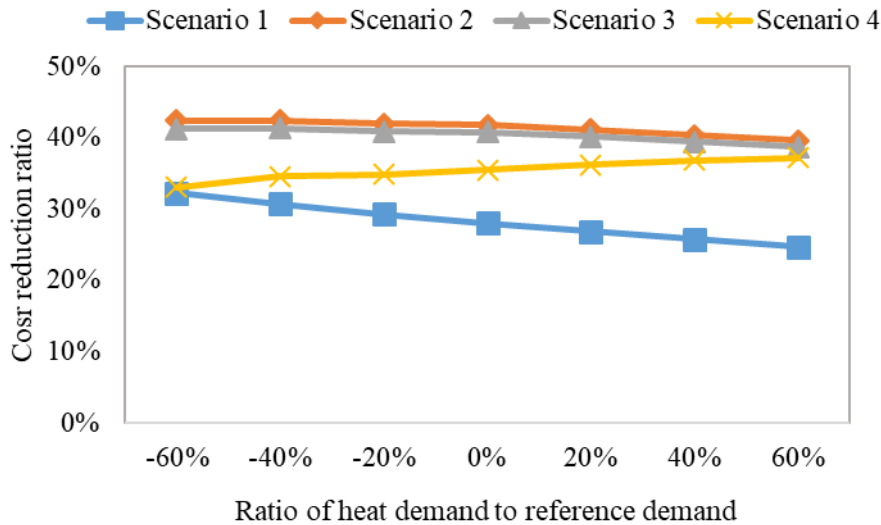
510 Fig. 17 and Fig. 18 show the results for the cost reduction ratio obtained by changing the  
 511 electricity and heat demand from 60% below to 60% above the reference values. The model  
 512 yields a maximum cost reduction at around a 20% increase in the base electricity demand. At this  
 513 demand level, the microgrid capacity is fully utilized for an overall improvement in cost of  
 514 generation (Fig. 17). For the case of no BCHP or only a single BCHP unit is installed, the cost  
 515 reduction ratio decreases slightly as the heat demand increases (Fig. 18). The overall impact on  
 516 the COE is minor for scenarios 2 and 3, however, because the only heat resource in the microgrid  
 517 is from BCHP (no electric resistance heating), which is absent in scenario 1, the COE becomes  
 518 more sensitive to heat demand. For scenario 4, with 200 kW BCHP capacity, even when the heat  
 519 demand is increased by 60% and the peak load is slightly over 200 kW, the microgrid still

520 supplies most of the thermal energy from engine heat recovery and the boiler. Therefore,  
 521 increasing the heat demand does not require much additional natural gas and a positive  
 522 relationship results in contrast to that for scenario 1.



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Fig. 17. COE reduction ratio as a function of increased electricity demand.



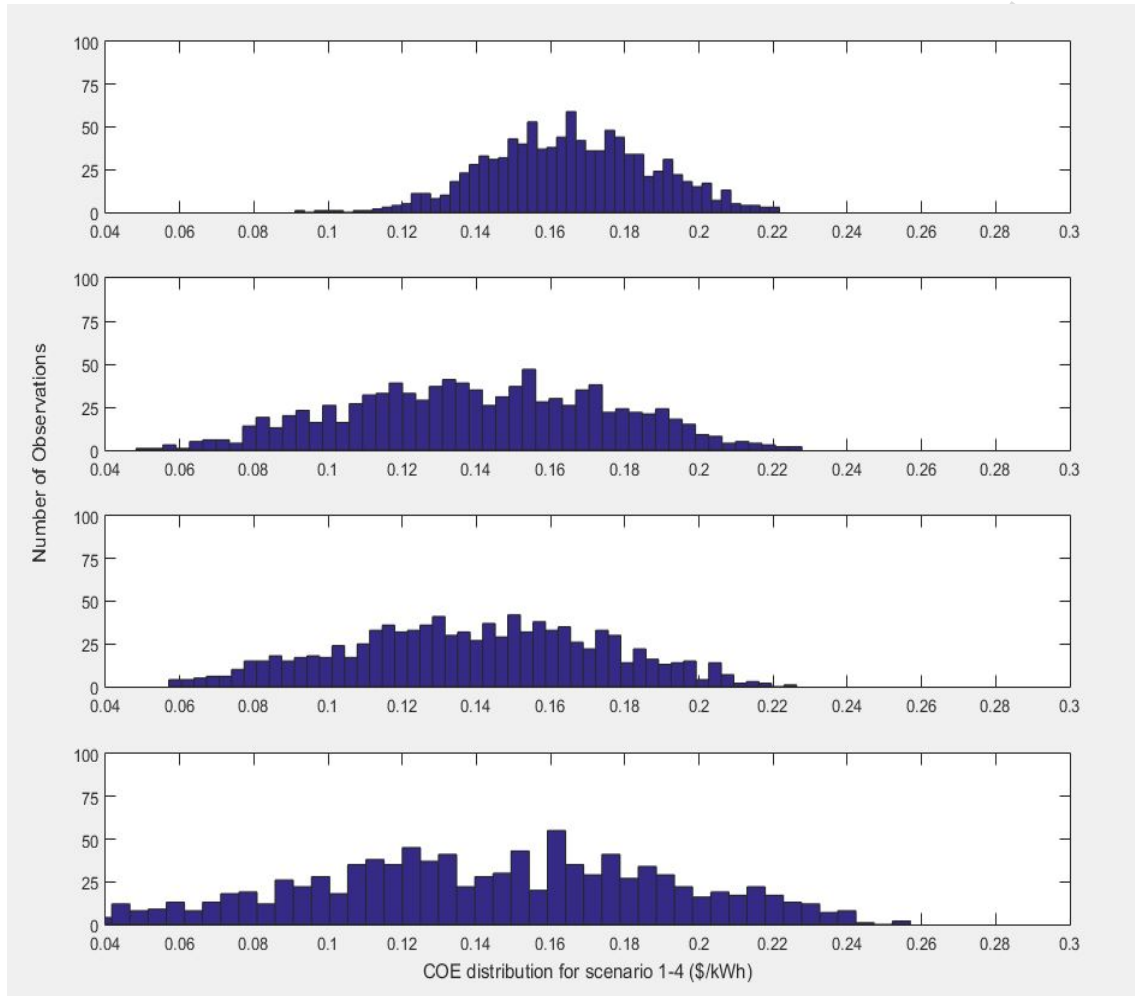
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Fig. 18. COE reduction ratio as a function of increased heat demand.

### 527 3.4. Stochastic model results

528 Many of the technical and economic assumptions used in the model are subject to  
 529 uncertainty as well as variability. To assess the potential risk associated with decisions around a  
 530 particular microgrid design, a stochastic model was developed employing Monte Carlo  
 531 simulation for COE. Histograms from the Monte Carlo simulations are presented in Fig. 19. The  
 532 BCHP scenario distributions (scenarios 2-4) are centered at lower COE even with a 5%  
 533 possibility of the gasifier and/or engine failure than for the microgrid without BCHP (scenario 1).

534 The 200 kW BCHP case (scenario 4) shows the widest variation in COE with cost mostly  
 535 ranging between 0.01 and 0.26 \$/kWh, a width of \$0.25/kWh while the scenario 2 and 3 span  
 536 about \$0.17/kWh. The no BCHP case (scenario 1) shows the narrowest variation in COE around  
 537 the mean of \$0.13/kWh.



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Fig. 19. COE probability distribution of scenario 1-4.

540 Table 8 shows statistics for these and other important results from the Monte Carlo  
 541 simulations including descriptive statistics of the scenario distributions, the probabilities  
 542 associated with any microgrid scenario reaching the optimal situation (deterministic COE), and  
 543 the probability that any microgrid scenario will be preferred over the conventional utility grid  
 544 supply (scenario 5). Note that scenario 4 has the highest probability, about 46%, of reaching the  
 545 optimal COE. There is a better than 28 and 31% chance that the COE of scenarios 2 and 3 are  
 546 less than or equal to the optimal value. For scenario 1, the probability of achieving the optimal  
 547 COE is only about 20%, however, the distribution of COE is narrower around the mean. Even  
 548 with uncertainty in the renewable generation, the microgrid options still yield odds of having  
 549 lower COE than the utility supply only option (scenario 5) under the assumptions used.

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Table 8 COE results from MCS.

Scenario	COE values from MCS (\$/kWh)				P( $\leq$ optimum COE)	P( $\leq$ COE of Scenario 5)
	Min	Max	Mean	Range		
1	0.0911	0.2217	0.1653	0.1306	19.80%	96.00%
2	0.0482	0.2278	0.1402	0.1796	28.00%	>99.9%
3	0.0570	0.2263	0.1391	0.1693	30.60%	>99.9%
4	0.0123	0.2570	0.1427	0.2447	45.89%	>99.9%

553

554 From the deterministic optimization analysis, scenario 2 has the lowest COE,  
 555 nevertheless, if all the uncertainty factors are considered, scenario 3 provides the opportunity to  
 556 achieve the lowest COE overall, albeit with reasonably low probability. With a 4-hour sliding  
 557 time window, and the large BCHP capacity, any gasifier or engine failure in any but the first  
 558 hour while the utility TOU electricity price is high, allows the BT and PGS storage to  
 559 accommodate the lack of BCHP generation. For scenario 2, with the smaller 100 kW BCHP unit  
 560 and no PGS, accommodation cannot be fully provided by the BT. Scenario 2 is also more  
 561 dependent on solar energy than scenario 3 and 4, consequently, the uncertainty from solar  
 562 radiation is reflected in the higher minimum cost for scenario 2. Scenario 4 also shows a much  
 563 wider range of possible outcomes. To illustrate, the expected COE from scenario 2 is lower than  
 564 scenario 4, but the odds of achieving that cost are lower. The microgrid design should consider  
 565 the odds of obtaining performance below expectations and understand the tolerable risk.

### 566 3.5. Sensitivity analysis of stochastic variables

567 Sensitivities of the results are presented for the three main power generation units, BCHP,  
 568 WT and PV (Table 9). Changing the BCHP capital cost by 15% from the reference value results  
 569 in average changes of 2.62, 2.00 and 9.87% in the mean COE for scenarios 2-4. When the BCHP  
 570 O&M cost was changed by 15%, the average changes were 2.82, 4.89 and 6.96% in mean COE  
 571 for these same scenarios 2-4. It is apparent that the BCHP investment and O&M cost uncertainty  
 572 is more sensitive in the COE of scenario 4. With respect to the O&M cost, for each scenario, the  
 573 COE varies by less than 5% indicating that COE is less sensitive to O&M cost category,  
 574 although BCHP O&M cost is more sensitive than the WT and PV O&M costs.

575 The variation in wind speed and solar radiation yield greater than 5% change in the final  
 576 cost for scenario 1, however, solar radiation does not show significant influence on the other  
 577 scenarios. Therefore, in terms of total cost, the variation in market price is more important than  
 578 the variations in wind speed and solar irradiance at the site if there is a BCHP on site.

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Table 9 Sensitivity analysis of the MCS results.

Case	Mean COE increase/decrease vs. baseline			
	1	2	3	4
+15% BCHP Capital cost	-	2.62%	2.00%	9.87%
+15% WT Capital cost	2.38%	-	-	-
+15% PV Capital cost	2.28%	3.93%	2.34%	9.56%
+15% BCHP O&M cost	-	2.82%	4.89%	6.96%
+15% WT O&M cost	0.00%	-	-	-
+15% PV O&M cost	0.63%	-1.93%	-0.07%	0.92%
+15% Wind speed	-6.36%	-	-	-
+15% Solar irradiance	-7.03%	-3.44%	-0.36%	3.06%

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#### 587 4. Summary and conclusions

588 A sliding time window optimization modeling approach was applied to the optimal  
 589 design and dispatch scheduling of a renewable microgrid supplying both heat and electricity. A  
 590 model microgrid was evaluated with biomass combined heat and power, wind and solar  
 591 electricity generation, gas-fired boiler, and battery electric, producer gas, and thermal energy  
 592 storage included.

593 For the economic assumptions employed, BCHP can significantly improve the cost-  
 594 efficiency of such a microgrid when compared with utility-supplied grid electricity and natural  
 595 gas to meet the electrical and heat demands. While for the example location used the mean wind  
 596 speed was low and wind generation was not selected as optimal, other locations may show  
 597 superior wind performance. In the optimal scheduling, the inclusion of batteries allows storing  
 598 electrical energy when utility time of use rates are low and electricity purchase is acceptable, and  
 599 satisfying demand from storage when the utility rates are high.

600 Sensitivity analyses show how battery capacity can be optimized. Utility electricity and  
 601 natural gas prices, as well as energy demand levels all have a significant impact on microgrid  
 602 design decisions. Cost breakeven points exist for the microgrid against the more conventional  
 603 utility supply scenario depend on utility pricing, demand, and supply capacities.

604 The optimum dispatch was evaluated under uncertainty using the probability density  
 605 functions anticipated for the primary parameters of concern. Monte Carlo simulation was then  
 606 used to generate the probability distribution of COE as an indicator of risk. The lowest cost  
 607 option may also have a higher risk of failing to reach the expected design performance.  
 608 Sensitivity analysis indicated a greater sensitivity to capital cost than the O&M cost for the range  
 609 of assumptions evaluated. The model provides a means to determine the major risk factors in the  
 610 microgrid design and weigh the various advantages and disadvantages of each microgrid  
 611 configuration. Further work will compare optimized scenarios based on both short-term and  
 612 annual performance and include the uncertainties arising from demand-side management to alter  
 613 both electricity and heat demand in a combined optimization.

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- A model was developed to optimize the design of a biomass-integrated renewable energy microgrid employing combined heat and power with energy storage.
- A receding horizon optimization with Monte Carlo simulation was proposed to evaluate optimal microgrid design and dispatch under uncertainty.
- The model application provides a means to determine major risk factors associated with alternative design integration and operating strategies.