

# Model Checking of Strategic Timed Temporal Logics (Extended Abstract)

Wojciech Penczek<sup>1</sup>

<sup>1</sup> *Zespół Teorii Systemów Rozproszonych i Obliczeniowych  
Instytut Podstaw Informatyki PAN  
ul. Jana Kazimierza 5  
01-248 Warszawa*

## 1. Multi-agent Systems and ATL

Autonomous agents provide a powerful paradigm for modelling and analysing socio-technical systems. They encompass networks of communicating agents that make autonomous decisions based on AI methods. Modeling strategic behaviors in a real-time context is crucial for ensuring the safety and security of agent systems. Alternating-time temporal logic (**ATL**<sup>\*</sup>) and its fragment **ATL** [1, 2] are logics that enable reasoning about strategic interactions in such systems by extending the framework of temporal logic with the game-theoretic concept of *strategic ability*. Therefore, **ATL** allows us to express statements about what groups of agents can achieve. These properties are useful for specifying, verifying, and reasoning about interactions in agent systems [11, 12, 7], as well as security and usability in e-voting protocols [5, 9]. They have become particularly relevant due to very active development of algorithms and tools for verification [15, 6, 8, 10], where the “correctness” is defined in terms of strategic ability.

## 2. Timed extensions of ATL and SCTL

In this lecture we investigate timed extensions of strategic logics including **ATL** and **ATL**<sup>\*</sup>. We begin with discussing the syntax and semantics of **ATL** and its discrete time extension **TATL** [14, 13]. Then, we introduce two new strategy logics: Strategic **CTL** (**SCTL**) and its timed extension Strategic Timed **CTL** (**STCTL**) [4]. Each (timed) strategy logic is interpreted over two types of structures: models of synchronous (Time) Multi-Agent Systems MAS and of asynchronous (Time) Multi-Agent Systems AMAS. We consider two semantics related to information: imperfect (i) and perfect (I), and two semantics related to recall: imperfect (r) and perfect (R). Additionally, Time MAS and Time AMAS can be either discrete (D) or continuous (C). The lecture focuses on the model checking problem for **SCTL** and **STCTL**, considering all the semantics mentioned above, and comparing their complexity with other strategy logics. Notably, we demonstrate that **SCTL** is more expressive than **ATL** for all semantics, including

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*PNSE'23, International Workshop on Petri Nets and Software Engineering, 2023*

✉ [penczek@ipipan.waw.pl](mailto:penczek@ipipan.waw.pl) (W. Penczek)

🌐 <https://home.ipipan.waw.pl/w.penczek/> (W. Penczek)



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the timed versions as well. Furthermore, we analyze the model checking problem for different combinations of semantics. For instance, the model checking problem for  $\mathbf{SCTL}_{ir}$  has the same complexity as for  $\mathbf{ATL}_{ir}$ , and the model checking problem for  $\mathbf{STCTL}_{ir}$  has the same complexity as for  $\mathbf{TCTL}$ . Additionally, we provide a practical demonstration of the feasibility of  $\mathbf{STCTL}_{ir}$  model checking using IMITATOR [3].

**Acknowledgements** This work was funded by the CNRS IEA project MoSART, and by NCBR Poland & FNR Luxembourg under the PolLux/FNR-CORE project SpaceVote (POLLUX-XI/14/SpaceVote/2023).

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