

# Package ‘bvhar’

October 11, 2024

**Type** Package

**Title** Bayesian Vector Heterogeneous Autoregressive Modeling

**Version** 2.1.2

**Description** Tools to model and forecast multivariate time series including Bayesian Vector heterogeneous autoregressive (VHAR) model by Kim & Baek (2023) (<[doi:10.1080/00949655.2023.2281644](https://doi.org/10.1080/00949655.2023.2281644)>). 'bvhar' can model Vector Autoregressive (VAR), VHAR, Bayesian VAR (BVAR), and Bayesian VHAR (BVHAR) models.

**License** GPL (>= 3)

**URL** <https://yeunkim.github.io/package/bvhar/>,  
<https://github.com/yeunkim/bvhar>

**BugReports** <https://github.com/yeunkim/bvhar/issues>

**Suggests** covr, GIGrv, knitr, parallel, rmarkdown, testthat (>= 3.0.0)

**Encoding** UTF-8

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**Imports** lifecycle, magrittr, Rcpp, ggplot2, tidyr, tibble, dplyr,  
foreach, purrr, stats, optimParallel, posterior, bayesplot

**LinkingTo** BH (>= 1.84.0-0), Rcpp, RcppEigen(>= 0.3.4.0.0)

**VignetteBuilder** knitr

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---

autoplot.bvhardynsp     *Dynamic Spillover Indices Plot*

---

### Description

Draws dynamic directional spillover plot.

### Usage

```
## S3 method for class 'bvhardynsp'
autoplot(
  object,
  type = c("tot", "to", "from", "net"),
  hcol = "grey",
  hsize = 1.5,
  row_facet = NULL,
  col_facet = NULL,
  ...
)
```

### Arguments

object	A bvhardynsp object
type	Index to draw
hcol	color of horizontal line = 0 (By default, grey)
hsize	size of horizontal line = 0 (By default, 1.5)
row_facet	nrow of <code>ggplot2::facet_wrap()</code>
col_facet	ncol of <code>ggplot2::facet_wrap()</code>
...	Additional

---

autoplot.bvharirf     *Plot Impulse Responses*

---

### Description

Draw impulse responses of response ~ impulse in the facet.

### Usage

```
## S3 method for class 'bvharirf'
autoplot(object, ...)
```

**Arguments**

object            A bvhairf object  
 ...              Other arguments passed on the `ggplot2::geom_path()`.

**Value**

A ggplot object

**See Also**

[irf\(\)](#)

---

autoplot.bvharsp            *Plot the Result of BVAR and BVHAR MCMC*

---

**Description**

Draw BVAR and BVHAR MCMC plots.

**Usage**

```
## S3 method for class 'bvharsp'
autoplot(
  object,
  type = c("coef", "trace", "dens", "area"),
  pars = character(),
  regex_pars = character(),
  ...
)
```

**Arguments**

object            A bvharsp object  
 type             The type of the plot. Posterior coefficient (coef), Trace plot (trace), kernel density plot (dens), and interval estimates plot (area).  
 pars             Parameter names to draw.  
 regex\_pars      Regular expression parameter names to draw.  
 ...              Other options for each `bayesplot::mcmc_trace()`, `bayesplot::mcmc_dens()`, and `bayesplot::mcmc_areas()`.

**Value**

A ggplot object

---

autoplot.normaliw      *Residual Plot for Minnesota Prior VAR Model*

---

### Description

This function draws residual plot for covariance matrix of Minnesota prior VAR model.

### Usage

```
## S3 method for class 'normaliw'
autoplot(object, hcol = "grey", hsize = 1.5, ...)
```

### Arguments

object	A normaliw object
hcol	color of horizontal line = 0 (By default, grey)
hsize	size of horizontal line = 0 (By default, 1.5)
...	additional options for geom_point

### Value

A ggplot object

---

autoplot.predbvhar      *Plot Forecast Result*

---

### Description

Plots the forecasting result with forecast regions.

### Usage

```
## S3 method for class 'predbvhar'
autoplot(
  object,
  type = c("grid", "wrap"),
  ci_alpha = 0.7,
  alpha_scale = 0.3,
  x_cut = 1,
  viridis = FALSE,
  viridis_option = "D",
  NROW = NULL,
  NCOL = NULL,
  ...
)
```

```
## S3 method for class 'predbvhar'
autolayer(object, ci_fill = "grey70", ci_alpha = 0.5, alpha_scale = 0.3, ...)
```

### Arguments

object	A predbvhar object
type	Divide variables using <code>ggplot2::facet_grid()</code> ("grid": default) or <code>ggplot2::facet_wrap()</code> ("wrap")
ci_alpha	Transparency of CI
alpha_scale	Scale of transparency parameter (alpha) between the two layers. alpha of CI ribbon = alpha_scale * alpha of path (By default, .5)
x_cut	plot x axes from x_cut for visibility
viridis	If TRUE, scale CI and forecast line using <code>ggplot2::scale_fill_viridis_d()</code> and <code>ggplot2::scale_colour_viridis_d()</code> , respectively.
viridis_option	Option for viridis string. See option of <code>ggplot2::scale_colour_viridis_d</code> . Choose one of c("A", "B", "C", "D", "E"). By default, D.
NROW	nrow of <code>ggplot2::facet_wrap()</code>
NCOL	ncol of <code>ggplot2::facet_wrap()</code>
...	additional option for <code>ggplot2::geom_path()</code>
ci_fill	color of CI

### Value

A ggplot object  
A ggplot layer

---

autoplot.summary.bvharsp

*Plot the Heatmap of SSVS Coefficients*

---

### Description

Draw heatmap for SSVS prior coefficients.

### Usage

```
## S3 method for class 'summary.bvharsp'
autoplot(object, point = FALSE, ...)
```

### Arguments

object	A summary.bvharsp object
point	Use point for sparsity representation
...	Other arguments passed on the <code>ggplot2::geom_tile()</code> .

**Value**

A ggplot object

---

autoplot.summary.normaliw

*Density Plot for Minnesota Prior VAR Model*

---

**Description**

This function draws density plot for coefficient matrices of Minnesota prior VAR model.

**Usage**

```
## S3 method for class 'summary.normaliw'
autoplot(
  object,
  type = c("trace", "dens", "area"),
  pars = character(),
  regex_pars = character(),
  ...
)
```

**Arguments**

object	A <code>summary.normaliw</code> object
type	The type of the plot. Trace plot ( <code>trace</code> ), kernel density plot ( <code>dens</code> ), and interval estimates plot ( <code>area</code> ).
pars	Parameter names to draw.
regex_pars	Regular expression parameter names to draw.
...	Other options for each <code>bayesplot::mcmc_trace()</code> , <code>bayesplot::mcmc_dens()</code> , and <code>bayesplot::mcmc_areas()</code> .

**Value**

A ggplot object

**Description**

**[Experimental]** This function sets lower and upper bounds for [set\\_bvar\(\)](#), [set\\_bvhar\(\)](#), or [set\\_weight\\_bvhar\(\)](#).

**Usage**

```
bound_bvhar(  
  init_spec = set_bvhar(),  
  lower_spec = set_bvhar(),  
  upper_spec = set_bvhar()  
)  
  
## S3 method for class 'boundbvharemp'  
print(x, digits = max(3L, getOption("digits") - 3L), ...)  
  
is.boundbvharemp(x)  
  
## S3 method for class 'boundbvharemp'  
knit_print(x, ...)
```

**Arguments**

<code>init_spec</code>	Initial Bayes model specification
<code>lower_spec</code>	Lower bound Bayes model specification
<code>upper_spec</code>	Upper bound Bayes model specification
<code>x</code>	boundbvharemp object
<code>digits</code>	digit option to print
<code>...</code>	not used

**Value**

boundbvharemp [class](#)

bvar\_flat

*Fitting Bayesian VAR(p) of Flat Prior***Description**

This function fits BVAR(p) with flat prior.

**Usage**

```

bvar_flat(
  y,
  p,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvar_flat(),
  include_mean = TRUE,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarflat'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarflat'
logLik(object, ...)

## S3 method for class 'bvarflat'
AIC(object, ...)

## S3 method for class 'bvarflat'
BIC(object, ...)

is.bvarflat(x)

## S3 method for class 'bvarflat'
knit_print(x, ...)

```

**Arguments**

y	Time series data of which columns indicate the variables
p	VAR lag
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.

thinning	Thinning every thinning-th iteration
bayes_spec	A BVAR model specification by <code>set_bvar_flat()</code> .
include_mean	Add constant term (Default: TRUE) or not (FALSE)
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvarflat object
digits	digit option to print
...	not used
object	A bvarflat object

### Details

Ghosh et al. (2018) gives flat prior for residual matrix in BVAR.

Under this setting, there are many models such as hierarchical or non-hierarchical. This function chooses the most simple non-hierarchical matrix normal prior in Section 3.1.

$$A | \Sigma_e \sim MN(0, U^{-1}, \Sigma_e)$$

where U: precision matrix (MN: **matrix normal**).

$$p(\Sigma_e) \propto 1$$

### Value

`bvar_flat()` returns an object `bvarflat` class. It is a list with the following components:

**coefficients** Posterior Mean matrix of Matrix Normal distribution

**fitted.values** Fitted values

**residuals** Residuals

**mn\_prec** Posterior precision matrix of Matrix Normal distribution

**iw\_scale** Posterior scale matrix of posterior inverse-wishart distribution

**iw\_shape** Posterior shape of inverse-wishart distribution

**df** Numer of Coefficients: mp + 1 or mp

**p** Lag of VAR

**m** Dimension of the time series

**obs** Sample size used when training = totobs - p

**totobs** Total number of the observation

**process** Process string in the bayes\_spec: BVAR\_Flat

**spec** Model specification (bvhar\_spec)

**type** include constant term (const) or not (none)

**call** Matched call

**prior\_mean** Prior mean matrix of Matrix Normal distribution: zero matrix

**prior\_precision** Prior precision matrix of Matrix Normal distribution:  $U^{-1}$

**y0**  $Y_0$

**design**  $X_0$

**y** Raw input (matrix)

## References

- Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).
- Litterman, R. B. (1986). *Forecasting with Bayesian Vector Autoregressions: Five Years of Experience*. *Journal of Business & Economic Statistics*, 4(1), 25.

## See Also

- `set_bvar_flat()` to specify the hyperparameters of BVAR flat prior.
- `coef.bvarflat()`, `residuals.bvarflat()`, and `fitted.bvarflat()`
- `predict.bvarflat()` to forecast the BVHAR process

---

 bvar\_horseshoe

*Fitting Bayesian VAR(p) of Horseshoe Prior*


---

## Description

**[Deprecated]** This function fits BVAR(p) with horseshoe prior.

## Usage

```
bvar_horseshoe(
  y,
  p,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_horseshoe(),
  include_mean = TRUE,
  minnesota = FALSE,
  algo = c("block", "gibbs"),
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarhs'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarhs'
knit_print(x, ...)
```

**Arguments**

<code>y</code>	Time series data of which columns indicate the variables
<code>p</code>	VAR lag
<code>num_chains</code>	Number of MCMC chains
<code>num_iter</code>	MCMC iteration number
<code>num_burn</code>	Number of burn-in (warm-up). Half of the iteration is the default choice.
<code>thinning</code>	Thinning every thinning-th iteration
<code>bayes_spec</code>	Horseshoe initialization specification by <code>set_horseshoe()</code> .
<code>include_mean</code>	Add constant term (Default: TRUE) or not (FALSE)
<code>minnesota</code>	Minnesota type
<code>algo</code>	Ordinary gibbs sampling (gibbs) or blocked gibbs (Default: block).
<code>verbose</code>	Print the progress bar in the console. By default, FALSE.
<code>num_thread</code>	<b>[Experimental]</b> Number of threads
<code>x</code>	bvarhs object
<code>digits</code>	digit option to print
<code>...</code>	not used

**Value**

`bvar_horseshoe` returns an object named `bvarhs` [class](#). It is a list with the following components:

**coefficients** Posterior mean of VAR coefficients.

**covmat** Posterior mean of covariance matrix

**psi\_posterior** Posterior mean of precision matrix  $\Psi$

**pip** Posterior inclusion probabilities.

**param** `posterior::draws_df` with every variable: alpha, lambda, tau, omega, and eta

**param\_names** Name of every parameter.

**df** Numer of Coefficients:  $m_p + 1$  or  $m_p$

**p** Lag of VAR

**m** Dimension of the data

**obs** Sample size used when training = `totobs - p`

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. `VAR_Horseshoe`

**type** include constant term (const) or not (none)

**algo** Usual Gibbs sampling (gibbs) or fast sampling (fast)

**spec** Horseshoe specification defined by `set_horseshoe()`

**chain** The numer of chains

**iter** Total iterations

**burn** Burn-in  
**thin** Thinning  
**group** Indicators for group.  
**num\_group** Number of groups.  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input

## References

Carvalho, C. M., Polson, N. G., & Scott, J. G. (2010). *The horseshoe estimator for sparse signals*. *Biometrika*, 97(2), 465-480.

Makalic, E., & Schmidt, D. F. (2016). *A Simple Sampler for the Horseshoe Estimator*. *IEEE Signal Processing Letters*, 23(1), 179-182.

---

bvar_minnesota	<i>Fitting Bayesian VAR(p) of Minnesota Prior</i>
----------------	---

---

## Description

This function fits BVAR(p) with Minnesota prior.

## Usage

```
bvar_minnesota(
  y,
  p = 1,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvar(),
  scale_variance = 0.05,
  include_mean = TRUE,
  parallel = list(),
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarmn'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarhm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

```

## S3 method for class 'bvarmn'
logLik(object, ...)

## S3 method for class 'bvarmn'
AIC(object, ...)

## S3 method for class 'bvarmn'
BIC(object, ...)

is.bvarmn(x)

## S3 method for class 'bvarmn'
knit_print(x, ...)

## S3 method for class 'bvarhm'
knit_print(x, ...)

```

### Arguments

y	Time series data of which columns indicate the variables
p	VAR lag (Default: 1)
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A BVAR model specification by <a href="#">set_bvar()</a> .
scale_variance	Proposal distribution scaling constant to adjust an acceptance rate
include_mean	Add constant term (Default: TRUE) or not (FALSE)
parallel	List the same argument of <a href="#">optimParallel::optimParallel()</a> . By default, this is empty, and the function does not execute parallel computation.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvarhm object
digits	digit option to print
...	not used
object	A bvarmn object

### Details

Minnesota prior gives prior to parameters  $A$  (VAR matrices) and  $\Sigma_e$  (residual covariance).

$$\begin{aligned}
 A \mid \Sigma_e &\sim MN(A_0, \Omega_0, \Sigma_e) \\
 \Sigma_e &\sim IW(S_0, \alpha_0)
 \end{aligned}$$

(MN: **matrix normal**, IW: **inverse-wishart**)

**Value**

bvar\_minnesota() returns an object bvarmn [class](#). It is a list with the following components:

**coefficients** Posterior Mean  
**fitted.values** Fitted values  
**residuals** Residuals  
**mn\_mean** Posterior mean matrix of Matrix Normal distribution  
**mn\_prec** Posterior precision matrix of Matrix Normal distribution  
**iw\_scale** Posterior scale matrix of posterior inverse-Wishart distribution  
**iw\_shape** Posterior shape of inverse-Wishart distribution ( $\alpha_0 - \text{obs} + 2$ ).  $\alpha_0$ : nrow(Dummy observation) - k  
**df** Numer of Coefficients: mp + 1 or mp  
**m** Dimension of the time series  
**obs** Sample size used when training = totobs - p  
**prior\_mean** Prior mean matrix of Matrix Normal distribution:  $A_0$   
**prior\_precision** Prior precision matrix of Matrix Normal distribution:  $\Omega_0^{-1}$   
**prior\_scale** Prior scale matrix of inverse-Wishart distribution:  $S_0$   
**prior\_shape** Prior shape of inverse-Wishart distribution:  $\alpha_0$   
**y0**  $Y_0$   
**design**  $X_0$   
**p** Lag of VAR  
**totobs** Total number of the observation  
**type** include constant term (const) or not (none)  
**y** Raw input (matrix)  
**call** Matched call  
**process** Process string in the bayes\_spec: BVAR\_Minnesota  
**spec** Model specification (bvhar\_spec)

It is also normaliw and bvharmod class.

**References**

- Bañbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. Journal of Applied Econometrics, 25(1).
- Giannone, D., Lenza, M., & Primiceri, G. E. (2015). *Prior Selection for Vector Autoregressions*. Review of Economics and Statistics, 97(2).
- Litterman, R. B. (1986). *Forecasting with Bayesian Vector Autoregressions: Five Years of Experience*. Journal of Business & Economic Statistics, 4(1), 25.
- KADIYALA, K.R. and KARLSSON, S. (1997), *NUMERICAL METHODS FOR ESTIMATION AND INFERENCE IN BAYESIAN VAR-MODELS*. J. Appl. Econ., 12: 99-132.
- Karlsson, S. (2013). *Chapter 15 Forecasting with Bayesian Vector Autoregression*. Handbook of Economic Forecasting, 2, 791-897.
- Sims, C. A., & Zha, T. (1998). *Bayesian Methods for Dynamic Multivariate Models*. International Economic Review, 39(4), 949-968.

**See Also**

- `set_bvar()` to specify the hyperparameters of Minnesota prior.
- `summary.normaliw()` to summarize BVAR model

**Examples**

```
# Perform the function using etf_vix dataset
fit <- bvar_minnesota(y = etf_vix[,1:3], p = 2)
class(fit)

# Extract coef, fitted values, and residuals
coef(fit)
head(residuals(fit))
head(fitted(fit))
```

---

bvar\_ssvs

*Fitting Bayesian VAR(p) of SSVS Prior*


---

**Description**

**[Deprecated]** This function fits BVAR(p) with stochastic search variable selection (SSVS) prior.

**Usage**

```
bvar_ssvs(
  y,
  p,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = choose_ssvs(y = y, ord = p, type = "VAR", param = c(0.1, 10), include_mean
    = include_mean, gamma_param = c(0.01, 0.01), mean_non = 0, sd_non = 0.1),
  init_spec = init_ssvs(type = "auto"),
  include_mean = TRUE,
  minnesota = FALSE,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarssvs'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarssvs'
knit_print(x, ...)
```

**Arguments**

y	Time series data of which columns indicate the variables
p	VAR lag
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A SSVS model specification by <code>set_ssvs()</code> . By default, use a default semiautomatic approach <code>choose_ssvs()</code> .
init_spec	SSVS initialization specification by <code>init_ssvs()</code> . By default, use OLS for coefficient and cholesky factor while 1 for dummies.
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). By default, FALSE.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	<b>[Experimental]</b> Number of threads
x	bvarssvs object
digits	digit option to print
...	not used

**Details**

SSVS prior gives prior to parameters  $\alpha = \text{vec}(A)$  (VAR coefficient) and  $\Sigma_e^{-1} = \Psi\Psi^T$  (residual covariance).

$$\alpha_j \mid \gamma_j \sim (1 - \gamma_j)N(0, \kappa_{0j}^2) + \gamma_j N(0, \kappa_{1j}^2)$$

$$\gamma_j \sim \text{Bernoulli}(q_j)$$

and for upper triangular matrix  $\Psi$ ,

$$\psi_{jj}^2 \sim \text{Gamma}(\text{shape} = a_j, \text{rate} = b_j)$$

$$\psi_{ij} \mid w_{ij} \sim (1 - w_{ij})N(0, \kappa_{0,ij}^2) + w_{ij}N(0, \kappa_{1,ij}^2)$$

$$w_{ij} \sim \text{Bernoulli}(q_{ij})$$

**Value**

bvar\_ssvs returns an object named bvarssvs `class`. It is a list with the following components:

**coefficients** Posterior mean of VAR coefficients.

**chol\_posterior** Posterior mean of cholesky factor matrix

**covmat** Posterior mean of covariance matrix

**omega\_posterior** Posterior mean of omega

**pip** Posterior inclusion probability

**param** `posterior::draws_df` with every variable: alpha, eta, psi, omega, and gamma

**param\_names** Name of every parameter.

**df** Numer of Coefficients:  $mp + 1$  or  $mp$

**p** Lag of VAR

**m** Dimension of the data

**obs** Sample size used when training =  $totobs - p$

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. VAR\_SSVS

**type** include constant term (const) or not (none)

**spec** SSVS specification defined by `set_ssvs()`

**init** Initial specification defined by `init_ssvs()`

**chain** The numer of chains

**iter** Total iterations

**burn** Burn-in

**thin** Thinning

**group** Indicators for group.

**num\_group** Number of groups.

**y0**  $Y_0$

**design**  $X_0$

**y** Raw input

## References

- George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.
- George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.
- Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.

bvar\_sv

*Fitting Bayesian VAR-SV***Description**

**[Deprecated]** This function fits VAR-SV. It can have Minnesota, SSVS, and Horseshoe prior.

**Usage**

```
bvar_sv(
  y,
  p,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvar(),
  sv_spec = set_sv(),
  intercept = set_intercept(),
  include_mean = TRUE,
  minnesota = TRUE,
  save_init = FALSE,
  convergence = NULL,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarsv'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarsv'
knit_print(x, ...)
```

**Arguments**

y	Time series data of which columns indicate the variables
p	VAR lag
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A BVAR model specification by <a href="#">set_bvar()</a> , <a href="#">set_ssvs()</a> , or <a href="#">set_horseshoe()</a> .
sv_spec	<b>[Experimental]</b> SV specification by <a href="#">set_sv()</a> .
intercept	<b>[Experimental]</b> Prior for the constant term by <a href="#">set_intercept()</a> .

include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). By default, TRUE.
save_init	Save every record starting from the initial values (TRUE). By default, exclude the initial values in the record (FALSE), even when num_burn = 0 and thinning = 1. If num_burn > 0 or thinning != 1, this option is ignored.
convergence	Convergence threshold for rhat < convergence. By default, NULL which means no warning.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvarsv object
digits	digit option to print
...	not used

### Details

Cholesky stochastic volatility modeling for VAR based on

$$\Sigma_t^{-1} = L^T D_t^{-1} L$$

, and implements corrected triangular algorithm for Gibbs sampler.

### Value

bvar\_sv() returns an object named bvarsv [class](#).

**coefficients** Posterior mean of coefficients.

**chol\_posterior** Posterior mean of contemporaneous effects.

**param** Every set of MCMC trace.

**param\_names** Name of every parameter.

**group** Indicators for group.

**num\_group** Number of groups.

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**p** VAR lag

**m** Dimension of the data

**obs** Sample size used when training = totobs - p

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. VHAR\_SSVS\_SV, VHAR\_Horseshoe\_SV, or VHAR\_minnesota-part\_SV

**type** include constant term (const) or not (none)

**spec** Coefficients prior specification

**sv** log volatility prior specification

**intercept** Intercept prior specification

**init** Initial values  
**chain** The number of chains  
**iter** Total iterations  
**burn** Burn-in  
**thin** Thinning  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input  
 If it is SSVS or Horseshoe:  
**pip** Posterior inclusion probabilities.

## References

Carriero, A., Chan, J., Clark, T. E., & Marcellino, M. (2022). *Corrigendum to “Large Bayesian vector autoregressions with stochastic volatility and non-conjugate priors” [J. Econometrics 212 (1)(2019) 137-154]*. *Journal of Econometrics*, 227(2), 506-512.

Chan, J., Koop, G., Poirier, D., & Tobias, J. (2019). *Bayesian Econometric Methods (2nd ed., Econometric Exercises)*. Cambridge: Cambridge University Press.

Cogley, T., & Sargent, T. J. (2005). *Drifts and volatilities: monetary policies and outcomes in the post WWII US*. *Review of Economic Dynamics*, 8(2), 262-302.

Gruber, L., & Kastner, G. (2022). *Forecasting macroeconomic data with Bayesian VARs: Sparse or dense? It depends!* arXiv.

---

 bvhar\_horseshoe

*Fitting Bayesian VHAR of Horseshoe Prior*


---

## Description

**[Deprecated]** This function fits VHAR with horseshoe prior.

## Usage

```

bvhar_horseshoe(
  y,
  har = c(5, 22),
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_horseshoe(),
  include_mean = TRUE,
  minnesota = c("no", "short", "longrun"),
  algo = c("block", "gibbs"),

```

```

    verbose = FALSE,
    num_thread = 1
)

## S3 method for class 'bvharhs'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharhs'
knit_print(x, ...)

```

### Arguments

<code>y</code>	Time series data of which columns indicate the variables
<code>har</code>	Numeric vector for weekly and monthly order. By default, <code>c(5, 22)</code> .
<code>num_chains</code>	Number of MCMC chains
<code>num_iter</code>	MCMC iteration number
<code>num_burn</code>	Number of burn-in (warm-up). Half of the iteration is the default choice.
<code>thinning</code>	Thinning every thinning-th iteration
<code>bayes_spec</code>	Horseshoe initialization specification by <code>set_horseshoe()</code> .
<code>include_mean</code>	Add constant term (Default: TRUE) or not (FALSE)
<code>minnesota</code>	Minnesota type
<code>algo</code>	Ordinary gibbs sampling ( <code>gibbs</code> ) or blocked gibbs (Default: <code>block</code> ).
<code>verbose</code>	Print the progress bar in the console. By default, FALSE.
<code>num_thread</code>	<b>[Experimental]</b> Number of threads
<code>x</code>	<code>bvharhs</code> object
<code>digits</code>	digit option to print
<code>...</code>	not used

### Value

`bvhar_horseshoe` returns an object named `bvarhs` [class](#). It is a list with the following components:

**coefficients** Posterior mean of VHAR coefficients.

**covmat** Posterior mean of covariance matrix

**psi\_posterior** Posterior mean of precision matrix  $\Psi$

**param** `posterior::draws_df` with every variable: alpha, lambda, tau, omega, and eta

**param\_names** Name of every parameter.

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**p** 3 (The number of terms. It contains this element for usage in other functions.)

**week** Order for weekly term

**month** Order for monthly term

**m** Dimension of the data

**obs** Sample size used when training = totobs - p  
**totobs** Total number of the observation  
**call** Matched call  
**process** Description of the model, e.g. VHar\_Horseshoe  
**type** include constant term (const) or not (none)  
**algo** Usual Gibbs sampling (gibbs) or fast sampling (fast)  
**spec** Horseshoe specification defined by `set_horseshoe()`  
**chain** The number of chains  
**iter** Total iterations  
**burn** Burn-in  
**thin** Thinning  
**group** Indicators for group.  
**num\_group** Number of groups.  
**HARtrans** VHar linear transformation matrix  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input

## References

Kim, Y. G., and Baek, C. (n.d.). Working paper.

---

 bvhar\_minnesota

*Fitting Bayesian VHar of Minnesota Prior*


---

## Description

This function fits BVHar with Minnesota prior.

## Usage

```

bvhar_minnesota(
  y,
  har = c(5, 22),
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvhar(),
  scale_variance = 0.05,
  include_mean = TRUE,
  parallel = list(),

```

```

    verbose = FALSE,
    num_thread = 1
)

## S3 method for class 'bvharhm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharhm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharhm'
logLik(object, ...)

## S3 method for class 'bvharhm'
AIC(object, ...)

## S3 method for class 'bvharhm'
BIC(object, ...)

is.bvharhm(x)

## S3 method for class 'bvharhm'
knit_print(x, ...)

## S3 method for class 'bvharhm'
knit_print(x, ...)

```

### Arguments

y	Time series data of which columns indicate the variables
har	Numeric vector for weekly and monthly order. By default, <code>c(5, 22)</code> .
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A BVHAR model specification by <code>set_bvhar()</code> (default) or <code>set_weight_bvhar()</code> .
scale_variance	Proposal distribution scaling constant to adjust an acceptance rate
include_mean	Add constant term (Default: TRUE) or not (FALSE)
parallel	List the same argument of <code>optimParallel::optimParallel()</code> . By default, this is empty, and the function does not execute parallel computation.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvharhm object
digits	digit option to print
...	not used
object	A bvharhm object

**Details**

Apply Minnesota prior to Vector HAR:  $\Phi$  (VHAR matrices) and  $\Sigma_e$  (residual covariance).

$$\begin{aligned}\Phi \mid \Sigma_e &\sim MN(M_0, \Omega_0, \Sigma_e) \\ \Sigma_e &\sim IW(\Psi_0, \nu_0)\end{aligned}$$

(MN: **matrix normal**, IW: **inverse-wishart**)

There are two types of Minnesota priors for BVHAR:

- VAR-type Minnesota prior specified by `set_bvhar()`, so-called BVHAR-S model.
- VHAR-type Minnesota prior specified by `set_weight_bvhar()`, so-called BVHAR-L model.

**Value**

`bvhar_minnesota()` returns an object `bvhar` **class**. It is a list with the following components:

**coefficients** Posterior Mean

**fitted.values** Fitted values

**residuals** Residuals

**mn\_mean** Posterior mean matrix of Matrix Normal distribution

**mn\_prec** Posterior precision matrix of Matrix Normal distribution

**iw\_scale** Posterior scale matrix of posterior inverse-wishart distribution

**iw\_shape** Posterior shape of inverse-Wishart distribution ( $\nu_0 - \text{obs} + 2$ ).  $\nu_0$ : `nrow(Dummy observation) - k`

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**m** Dimension of the time series

**obs** Sample size used when training = `totobs - 22`

**prior\_mean** Prior mean matrix of Matrix Normal distribution:  $M_0$

**prior\_precision** Prior precision matrix of Matrix Normal distribution:  $\Omega_0^{-1}$

**prior\_scale** Prior scale matrix of inverse-Wishart distribution:  $\Psi_0$

**prior\_shape** Prior shape of inverse-Wishart distribution:  $\nu_0$

**y0**  $Y_0$

**design**  $X_0$

**p** 3, this element exists to run the other functions

**week** Order for weekly term

**month** Order for monthly term

**totobs** Total number of the observation

**type** include constant term (`const`) or not (`none`)

**HARtrans** VHAR linear transformation matrix:  $C_{HAR}$

**y** Raw input (`matrix`)

**call** Matched call

**process** Process string in the bayes\_spec: BVHAR\_MN\_VAR (BVHAR-S) or BVHAR\_MN\_VHAR (BVHAR-L)

**spec** Model specification (bvhar\_spec)

It is also normaliw and bvharmod class.

## References

Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. Journal of Statistical Computation and Simulation, 94(6), 1139-1157.

## See Also

- [set\\_bvhar\(\)](#) to specify the hyperparameters of BVHAR-S
- [set\\_weight\\_bvhar\(\)](#) to specify the hyperparameters of BVHAR-L
- [summary.normaliw\(\)](#) to summarize BVHAR model

## Examples

```
# Perform the function using etf_vix dataset
fit <- bvhar_minnesota(y = etf_vix[,1:3])
class(fit)

# Extract coef, fitted values, and residuals
coef(fit)
head(residuals(fit))
head(fitted(fit))
```

---

 bvhar\_ssvs

*Fitting Bayesian VHAR of SSVS Prior*


---

## Description

**[Deprecated]** This function fits BVAR(p) with stochastic search variable selection (SSVS) prior.

## Usage

```
bvhar_ssvs(
  y,
  har = c(5, 22),
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = choose_ssvs(y = y, ord = har, type = "VHAR", param = c(0.1, 10),
    include_mean = include_mean, gamma_param = c(0.01, 0.01), mean_non = 0, sd_non = 0.1),
  init_spec = init_ssvs(type = "auto"),
  include_mean = TRUE,
```

```

minnesota = c("no", "short", "longrun"),
verbose = FALSE,
num_thread = 1
)

## S3 method for class 'bvharssvs'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharssvs'
knit_print(x, ...)

```

### Arguments

y	Time series data of which columns indicate the variables
har	Numeric vector for weekly and monthly order. By default, c(5, 22).
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of warm-up (burn-in). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A SSVS model specification by <code>set_ssvs()</code> . By default, use a default semiautomatic approach <code>choose_ssvs()</code> .
init_spec	SSVS initialization specification by <code>init_ssvs()</code> . By default, use OLS for coefficient and cholesky factor while 1 for dummies.
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). Two type: short type and longrun type. By default, no.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	<b>[Experimental]</b> Number of threads
x	bvharssvs object
digits	digit option to print
...	not used

### Details

SSVS prior gives prior to parameters  $\alpha = \text{vec}(A)$  (VAR coefficient) and  $\Sigma_e^{-1} = \Psi\Psi^T$  (residual covariance).

$$\alpha_j \mid \gamma_j \sim (1 - \gamma_j)N(0, \kappa_{0j}^2) + \gamma_j N(0, \kappa_{1j}^2)$$

$$\gamma_j \sim \text{Bernoulli}(q_j)$$

and for upper triangular matrix  $\Psi$ ,

$$\psi_{jj}^2 \sim \text{Gamma}(\text{shape} = a_j, \text{rate} = b_j)$$

$$\begin{aligned}\psi_{ij} | w_{ij} &\sim (1 - w_{ij})N(0, \kappa_{0,ij}^2) + w_{ij}N(0, \kappa_{1,ij}^2) \\ w_{ij} &\sim \text{Bernoulli}(q_{ij})\end{aligned}$$

Gibbs sampler is used for the estimation.

## Value

bvhar\_ssvs returns an object named bvharssvs [class](#). It is a list with the following components:

**coefficients** Posterior mean of VAR coefficients.  
**chol\_posterior** Posterior mean of cholesky factor matrix  
**covmat** Posterior mean of covariance matrix  
**omega\_posterior** Posterior mean of omega  
**pip** Posterior inclusion probability  
**param** `posterior::draws_df` with every variable: alpha, eta, psi, omega, and gamma  
**param\_names** Name of every parameter.  
**df** Numer of Coefficients:  $3m + 1$  or  $3m$   
**p** 3 (The number of terms. It contains this element for usage in other functions.)  
**week** Order for weekly term  
**month** Order for monthly term  
**m** Dimension of the data  
**obs** Sample size used when training = `totobs - p`  
**totobs** Total number of the observation  
**call** Matched call  
**process** Description of the model, e.g. `VHAR_SSVS`  
**type** include constant term (`const`) or not (`none`)  
**spec** SSVS specification defined by `set_ssvs()`  
**init** Initial specification defined by `init_ssvs()`  
**chain** The numer of chains  
**iter** Total iterations  
**burn** Burn-in  
**thin** Thinning  
**group** Indicators for group.  
**num\_group** Number of groups.  
**HARtrans** VHAR linear transformation matrix  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input

## References

Kim, Y. G., and Baek, C. (n.d.). Working paper.

bvhar\_sv

*Fitting Bayesian VHAR-SV***Description**

**[Deprecated]** This function fits VHAR-SV. It can have Minnesota, SSVS, and Horseshoe prior. This function is deprecated. Use `vhar_bayes()` with `cov_spec = set_sv()` option.

**Usage**

```

bvhar_sv(
  y,
  har = c(5, 22),
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvhar(),
  sv_spec = set_sv(),
  intercept = set_intercept(),
  include_mean = TRUE,
  minnesota = c("longrun", "short", "no"),
  save_init = FALSE,
  convergence = NULL,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvhar_sv'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvhar_sv'
knit_print(x, ...)

```

**Arguments**

<code>y</code>	Time series data of which columns indicate the variables
<code>har</code>	Numeric vector for weekly and monthly order. By default, <code>c(5, 22)</code> .
<code>num_chains</code>	Number of MCMC chains
<code>num_iter</code>	MCMC iteration number
<code>num_burn</code>	Number of burn-in (warm-up). Half of the iteration is the default choice.
<code>thinning</code>	Thinning every thinning-th iteration
<code>bayes_spec</code>	A BVHAR model specification by <code>set_bvhar()</code> (default) <code>set_weight_bvhar()</code> , <code>set_ssvs()</code> , or <code>set_horseshoe()</code> .
<code>sv_spec</code>	<b>[Experimental]</b> SV specification by <code>set_sv()</code> .

intercept	<b>[Experimental]</b> Prior for the constant term by <code>set_intercept()</code> .
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). Two type: short type and longrun (default) type. You can also set no.
save_init	Save every record starting from the initial values (TRUE). By default, exclude the initial values in the record (FALSE), even when <code>num_burn = 0</code> and <code>thinning = 1</code> . If <code>num_burn &gt; 0</code> or <code>thinning != 1</code> , this option is ignored.
convergence	Convergence threshold for <code>rhat &lt; convergence</code> . By default, NULL which means no warning.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvarsv object
digits	digit option to print
...	not used

### Details

Cholesky stochastic volatility modeling for VHAR based on

$$\Sigma_t = L^T D_t^{-1} L$$

### Value

`bvhar_sv()` returns an object named `bvharsv` class. It is a list with the following components:

**coefficients** Posterior mean of coefficients.

**chol\_posterior** Posterior mean of contemporaneous effects.

**param** Every set of MCMC trace.

**param\_names** Name of every parameter.

**group** Indicators for group.

**num\_group** Number of groups.

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**p** 3 (The number of terms. It contains this element for usage in other functions.)

**week** Order for weekly term

**month** Order for monthly term

**m** Dimension of the data

**obs** Sample size used when `training = totobs - p`

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. `VHAR_SSVS_SV`, `VHAR_Horseshoe_SV`, or `VHAR_minnesota-part_SV`

**type** include constant term (`const`) or not (`none`)

**spec** Coefficients prior specification

**sv** log volatility prior specification  
**init** Initial values  
**intercept** Intercept prior specification  
**chain** The number of chains  
**iter** Total iterations  
**burn** Burn-in  
**thin** Thinning  
**HARtrans** VHar linear transformation matrix  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input  
 If it is SSVS or Horseshoe:  
**pip** Posterior inclusion probabilities.

## References

Kim, Y. G., and Baek, C. (n.d.). Working paper.

---

choose\_bayes

*Finding the Set of Hyperparameters of Bayesian Model*

---

## Description

**[Experimental]** This function chooses the set of hyperparameters of Bayesian model using `stats::optim()` function.

## Usage

```

choose_bayes(
  bayes_bound = bound_bvhar(),
  ...,
  eps = 1e-04,
  y,
  order = c(5, 22),
  include_mean = TRUE,
  parallel = list()
)
  
```

**Arguments**

bayes_bound	Empirical Bayes optimization bound specification defined by <code>bound_bvhar()</code> .
...	Additional arguments for <code>stats::optim()</code> .
eps	Hyperparameter eps is fixed. By default, 1e-04.
y	Time series data
order	Order for BVAR or BVHAR. p of <code>bvar_minnesota()</code> or har of <code>bvhar_minnesota()</code> . By default, c(5, 22) for har.
include_mean	Add constant term (Default: TRUE) or not (FALSE)
parallel	List the same argument of <code>optimParallel::optimParallel()</code> . By default, this is empty, and the function does not execute parallel computation.

**Value**

bvharemp `class` is a list that has

... Many components of `stats::optim()` or `optimParallel::optimParallel()`

**spec** Corresponding bvhar spec

**fit** Chosen Bayesian model

**ml** Marginal likelihood of the final model

**References**

Giannone, D., Lenza, M., & Primiceri, G. E. (2015). *Prior Selection for Vector Autoregressions*. *Review of Economics and Statistics*, 97(2).

Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. *Journal of Statistical Computation and Simulation*, 94(6), 1139-1157.

**See Also**

- `bound_bvhar()` to define L-BFGS-B optimization bounds.
- Individual functions: `choose_bvar()`

---

choose\_bvar

*Finding the Set of Hyperparameters of Individual Bayesian Model*

---

**Description**

Instead of these functions, you can use `choose_bayes()`.

**Usage**

```

choose_bvar(
  bayes_spec = set_bvar(),
  lower = 0.01,
  upper = 10,
  ...,
  eps = 1e-04,
  y,
  p,
  include_mean = TRUE,
  parallel = list()
)

choose_bvhar(
  bayes_spec = set_bvhar(),
  lower = 0.01,
  upper = 10,
  ...,
  eps = 1e-04,
  y,
  har = c(5, 22),
  include_mean = TRUE,
  parallel = list()
)

## S3 method for class 'bvharemp'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.bvharemp(x)

## S3 method for class 'bvharemp'
knit_print(x, ...)

```

**Arguments**

bayes_spec	Initial Bayes model specification.
lower	<b>[Experimental]</b> Lower bound. By default, .01.
upper	<b>[Experimental]</b> Upper bound. By default, 10.
...	not used
eps	Hyperparameter eps is fixed. By default, 1e-04.
y	Time series data
p	BVAR lag
include_mean	Add constant term (Default: TRUE) or not (FALSE)
parallel	List the same argument of <code>optimParallel::optimParallel()</code> . By default, this is empty, and the function does not execute parallel computation.
har	Numeric vector for weekly and monthly order. By default, c(5, 22).

x                   bvharemp object  
 digits             digit option to print

### Details

Empirical Bayes method maximizes marginal likelihood and selects the set of hyperparameters. These functions implement L-BFGS-B method of `stats::optim()` to find the maximum of marginal likelihood.

If you want to set lower and upper option more carefully, deal with them like as in `stats::optim()` in order of `set_bvar()`, `set_bvhar()`, or `set_weight_bvhar()`'s argument (except eps). In other words, just arrange them in a vector.

### Value

bvharemp class is a list that has

- `stats::optim()` or `optimParallel::optimParallel()`
- chosen bvhar spec set
- Bayesian model fit result with chosen specification
  - ... Many components of `stats::optim()` or `optimParallel::optimParallel()`
  - spec** Corresponding bvhar spec
  - fit** Chosen Bayesian model
  - ml** Marginal likelihood of the final model

### References

- Byrd, R. H., Lu, P., Nocedal, J., & Zhu, C. (1995). *A limited memory algorithm for bound constrained optimization*. SIAM Journal on scientific computing, 16(5), 1190-1208.
- Gelman, A., Carlin, J. B., Stern, H. S., & Rubin, D. B. (2013). *Bayesian data analysis*. Chapman and Hall/CRC.
- Giannone, D., Lenza, M., & Primiceri, G. E. (2015). *Prior Selection for Vector Autoregressions*. Review of Economics and Statistics, 97(2).
- Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. Journal of Statistical Computation and Simulation, 94(6), 1139-1157.

---

choose_ssvs	<i>Choose the Hyperparameters Set of SSVS-VAR using a Default Semiautomatic Approach</i>
-------------	--

---

### Description

**[Deprecated]** This function chooses  $(\tau_{0i}, \tau_{1i})$  and  $(\kappa_{0i}, \kappa_{1i})$  using a default semiautomatic approach.

**Usage**

```

choose_ssvs(
  y,
  ord,
  type = c("VAR", "VHAR"),
  param = c(0.1, 10),
  include_mean = TRUE,
  gamma_param = c(0.01, 0.01),
  mean_non = 0,
  sd_non = 0.1
)

```

**Arguments**

y	Time series data of which columns indicate the variables.
ord	Order for VAR or VHAR.
type	Model type (Default: VAR or VHAR).
param	Preselected constants $c_0 \ll c_1$ . By default, 0.1 and 10 (See Details).
include_mean	Add constant term (Default: TRUE) or not (FALSE).
gamma_param	Parameters (shape, rate) for Gamma distribution. This is for the output.
mean_non	Prior mean of unrestricted coefficients. This is for the output.
sd_non	Standard deviance of unrestricted coefficients. This is for the output.

**Details**

Instead of using subjective values of  $(\tau_{0i}, \tau_{1i})$ , we can use

$$\tau_{ki} = c_k VAR(\hat{OLS})$$

It must be  $c_0 \ll c_1$ .

In case of  $(\omega_{0ij}, \omega_{1ij})$ ,

$$\omega_{kij} = c_k = VAR(\hat{OLS})$$

similarly.

**Value**

ssvsinput object

**References**

- George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.
- George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.
- Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.

---

choose_var	<i>Choose the Best VAR based on Information Criteria</i>
------------	--

---

**Description**

This function computes AIC, FPE, BIC, and HQ up to  $p = \text{lag\_max}$  of VAR model.

**Usage**

```
choose_var(y, lag_max = 5, include_mean = TRUE, parallel = FALSE)
```

**Arguments**

y	Time series data of which columns indicate the variables
lag_max	Maximum Var lag to explore (default = 5)
include_mean	Add constant term (Default: TRUE) or not (FALSE)
parallel	Parallel computation using <code>foreach::foreach()</code> ? By default, FALSE.

**Value**

Minimum order and information criteria values

---

coef	<i>Coefficient Matrix of Multivariate Time Series Models</i>
------	--

---

**Description**

By defining `stats::coef()` for each model, this function returns coefficient matrix estimates.

**Usage**

```
## S3 method for class 'varlse'
coef(object, ...)

## S3 method for class 'vharlse'
coef(object, ...)

## S3 method for class 'bvarmn'
coef(object, ...)

## S3 method for class 'bvarflat'
coef(object, ...)

## S3 method for class 'bvharmn'
coef(object, ...)
```

```
## S3 method for class 'bvhar'
coef(object, ...)

## S3 method for class 'summary.bvhar'
coef(object, ...)
```

### Arguments

object	Model object
...	not used

### Value

matrix object with appropriate dimension.

---

compute\_dic

*Deviance Information Criterion of Multivariate Time Series Model*

---

### Description

Compute DIC of BVAR and BVHAR.

### Usage

```
compute_dic(object, ...)

## S3 method for class 'bvar'
compute_dic(object, n_iter = 100L, ...)
```

### Arguments

object	Model fit
...	not used
n_iter	Number to sample

### Details

Deviance information criteria (DIC) is

$$-2 \log p(y | \hat{\theta}_{bayes}) + 2p_{DIC}$$

where  $p_{DIC}$  is the effective number of parameters defined by

$$p_{DIC} = 2(\log p(y | \hat{\theta}_{bayes}) - E_{post} \log p(y | \theta))$$

Random sampling from posterior distribution gives its computation,  $\theta_i \sim \theta | y, i = 1, \dots, M$

$$p_{DIC}^{computed} = 2(\log p(y | \hat{\theta}_{bayes}) - \frac{1}{M} \sum_i \log p(y | \theta_i))$$

**Value**

DIC value.

**References**

Gelman, A., Carlin, J. B., Stern, H. S., & Rubin, D. B. (2013). *Bayesian data analysis*. Chapman and Hall/CRC.

Spiegelhalter, D.J., Best, N.G., Carlin, B.P. and Van Der Linde, A. (2002). *Bayesian measures of model complexity and fit*. Journal of the Royal Statistical Society: Series B (Statistical Methodology), 64: 583-639.

---

compute\_logml

*Extracting Log of Marginal Likelihood*

---

**Description**

Compute log of marginal likelihood of Bayesian Fit

**Usage**

```
compute_logml(object, ...)
```

```
## S3 method for class 'bvarmn'
compute_logml(object, ...)
```

```
## S3 method for class 'bvharmn'
compute_logml(object, ...)
```

**Arguments**

object	Model fit
...	not used

**Details**

Closed form of Marginal Likelihood of BVAR can be derived by

$$p(Y_0) = \pi^{-mn/2} \frac{\Gamma_m((\alpha_0 + n)/2)}{\Gamma_m(\alpha_0/2)} \det(\Omega_0)^{-m/2} \det(S_0)^{\alpha_0/2} \det(\hat{V})^{-m/2} \det(\hat{\Sigma}_e)^{-(\alpha_0+n)/2}$$

Closed form of Marginal Likelihood of BVHAR can be derived by

$$p(Y_0) = \pi^{-ms_0/2} \frac{\Gamma_m((d_0 + n)/2)}{\Gamma_m(d_0/2)} \det(P_0)^{-m/2} \det(U_0)^{d_0/2} \det(\hat{V}_{HAR})^{-m/2} \det(\hat{\Sigma}_e)^{-(d_0+n)/2}$$

**Value**

log likelihood of Minnesota prior model.

**References**

Giannone, D., Lenza, M., & Primiceri, G. E. (2015). *Prior Selection for Vector Autoregressions*. *Review of Economics and Statistics*, 97(2).

---

confusion

*Evaluate the Sparsity Estimation Based on Confusion Matrix*

---

**Description**

This function computes FDR (false discovery rate) and FNR (false negative rate) for sparse element of the true coefficients given threshold.

**Usage**

```
confusion(x, y, ...)
```

```
## S3 method for class 'summary.bvharsp'
confusion(x, y, truth_thr = 0, ...)
```

**Arguments**

x	summary.bvharsp object.
y	True inclusion variable.
...	not used
truth_thr	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

**Details**

When using this function, the true coefficient matrix  $\Phi$  should be sparse.

In this confusion matrix, positive (0) means sparsity. FP is false positive, and TP is true positive. FN is false negative, and FN is false negative.

**Value**

Confusion table as following.

True-estimate	Positive (0)	Negative (1)
Positive (0)	TP	FN
Negative (1)	FP	TN

## References

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

---

conf\_fdr

*Evaluate the Sparsity Estimation Based on FDR*

---

## Description

This function computes false discovery rate (FDR) for sparse element of the true coefficients given threshold.

## Usage

```
conf_fdr(x, y, ...)
```

```
## S3 method for class 'summary.bvharsp'
conf_fdr(x, y, truth_thr = 0, ...)
```

## Arguments

x	summary.bvharsp object.
y	True inclusion variable.
...	not used
truth_thr	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

## Details

When using this function, the true coefficient matrix  $\Phi$  should be sparse. False discovery rate (FDR) is computed by

$$FDR = \frac{FP}{TP + FP}$$

where TP is true positive, and FP is false positive.

## Value

FDR value in confusion table

## References

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

## See Also

[confusion\(\)](#)

---

`conf_fnr`*Evaluate the Sparsity Estimation Based on FNR*

---

**Description**

This function computes false negative rate (FNR) for sparse element of the true coefficients given threshold.

**Usage**

```
conf_fnr(x, y, ...)
```

```
## S3 method for class 'summary.bvharsp'  
conf_fnr(x, y, truth_thr = 0, ...)
```

**Arguments**

<code>x</code>	summary.bvharsp object.
<code>y</code>	True inclusion variable.
<code>...</code>	not used
<code>truth_thr</code>	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

**Details**

False negative rate (FNR) is computed by

$$FNR = \frac{FN}{TP + FN}$$

where TP is true positive, and FN is false negative.

**Value**

FNR value in confusion table

**References**

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

**See Also**

[confusion\(\)](#)

---

conf_fscore	<i>Evaluate the Sparsity Estimation Based on F1 Score</i>
-------------	---

---

## Description

This function computes F1 score for sparse element of the true coefficients given threshold.

## Usage

```
conf_fscore(x, y, ...)  
  
## S3 method for class 'summary.bvharsp'  
conf_fscore(x, y, truth_thr = 0, ...)
```

## Arguments

x	summary.bvharsp object.
y	True inclusion variable.
...	not used
truth_thr	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

## Details

The F1 score is computed by

$$F_1 = \frac{2precision \times recall}{precision + recall}$$

## Value

F1 score in confusion table

## See Also

[confusion\(\)](#)

---

 conf\_prec

*Evaluate the Sparsity Estimation Based on Precision*


---

**Description**

This function computes precision for sparse element of the true coefficients given threshold.

**Usage**

```
conf_prec(x, y, ...)

## S3 method for class 'summary.bvharsp'
conf_prec(x, y, truth_thr = 0, ...)
```

**Arguments**

x	summary.bvharsp object.
y	True inclusion variable.
...	not used
truth_thr	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

**Details**

If the element of the estimate  $\hat{\Phi}$  is smaller than some threshold, it is treated to be zero. Then the precision is computed by

$$precision = \frac{TP}{TP + FP}$$

where TP is true positive, and FP is false positive.

**Value**

Precision value in confusion table

**References**

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

**See Also**

[confusion\(\)](#)

---

`conf_recall`*Evaluate the Sparsity Estimation Based on Recall*

---

### Description

This function computes recall for sparse element of the true coefficients given threshold.

### Usage

```
conf_recall(x, y, ...)
```

```
## S3 method for class 'summary.bvharsp'  
conf_recall(x, y, truth_thr = 0L, ...)
```

### Arguments

<code>x</code>	summary.bvharsp object.
<code>y</code>	True inclusion variable.
<code>...</code>	not used
<code>truth_thr</code>	Threshold value when using non-sparse true coefficient matrix. By default, 0 for sparse matrix.

### Details

Precision is computed by

$$recall = \frac{TP}{TP + FN}$$

where TP is true positive, and FN is false negative.

### Value

Recall value in confusion table

### References

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

### See Also

[confusion\(\)](#)

---

divide_ts	<i>Split a Time Series Dataset into Train-Test Set</i>
-----------	--

---

**Description**

Split a given time series dataset into train and test set for evaluation.

**Usage**

```
divide_ts(y, n_ahead)
```

**Arguments**

y	Time series data of which columns indicate the variables
n_ahead	step to evaluate

**Value**

List of two datasets, train and test.

---

dynamic_spillover	<i>Dynamic Spillover</i>
-------------------	--------------------------

---

**Description**

This function gives connectedness table with h-step ahead normalized spillover index (a.k.a. variance shares).

**Usage**

```
dynamic_spillover(object, n_ahead = 10L, ...)

## S3 method for class 'bvhardynsp'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvhardynsp'
knit_print(x, ...)

## S3 method for class 'olsmod'
dynamic_spillover(object, n_ahead = 10L, window, num_thread = 1, ...)

## S3 method for class 'normaliw'
dynamic_spillover(
  object,
  n_ahead = 10L,
```

```

    window,
    num_iter = 1000L,
    num_burn = floor(num_iter/2),
    thinning = 1,
    num_thread = 1,
    ...
)

## S3 method for class 'ldltmod'
dynamic_spillover(
  object,
  n_ahead = 10L,
  window,
  sparse = FALSE,
  num_thread = 1,
  ...
)

## S3 method for class 'svmod'
dynamic_spillover(object, n_ahead = 10L, sparse = FALSE, num_thread = 1, ...)

```

### Arguments

object	Model object
n_ahead	step to forecast. By default, 10.
...	not used
x	bvhardynsp object
digits	digit option to print
window	Window size
num_thread	<b>[Experimental]</b> Number of threads
num_iter	Number to sample MNIW distribution
num_burn	Number of burn-in
thinning	Thinning every thinning-th iteration
sparse	<b>[Experimental]</b> Apply restriction. By default, FALSE.

### References

Diebold, F. X., & Yilmaz, K. (2012). *Better to give than to receive: Predictive directional measurement of volatility spillovers*. *International Journal of forecasting*, 28(1), 57-66.

---

`etf_vix`*CBOE ETF Volatility Index Dataset*

---

**Description**

Chicago Board Options Exchange (CBOE) Exchange Traded Funds (ETFs) volatility index from FRED.

**Usage**`etf_vix`**Format**

A data frame of 1006 row and 9 columns:

From 2012-01-09 to 2015-06-27, 33 missing observations were interpolated by `stats::approx()` with `linear`.

**GVZCLS** Gold ETF volatility index

**VVFXICLS** China ETF volatility index

**OVXCLS** Crude Oil ETF volatility index

**VXEEMCLS** Emerging Markets ETF volatility index

**EVZCLS** EuroCurrency ETF volatility index

**VXSLVCLS** Silver ETF volatility index

**VXGDVCLS** Gold Miners ETF volatility index

**VXXLECLS** Energy Sector ETF volatility index

**VXEWZCLS** Brazil ETF volatility index

**Details**

Copyright, 2016, Chicago Board Options Exchange, Inc.

Note that, in this data frame, dates column is removed. This dataset interpolated 36 missing observations (nontrading dates) using `imputeTS::na_interpolation()`.

**Source**

Source: <https://www.cboe.com>

Release: [https://www.cboe.com/us/options/market\\_statistics/daily/](https://www.cboe.com/us/options/market_statistics/daily/)

## References

Chicago Board Options Exchange, CBOE Gold ETF Volatility Index (GVZCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/GVZCLS>, July 31, 2021.

Chicago Board Options Exchange, CBOE China ETF Volatility Index (VXFXICLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXFXICLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE Crude Oil ETF Volatility Index (OVXCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/OVXCLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE Emerging Markets ETF Volatility Index (VXEEMCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXEEMCLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE EuroCurrency ETF Volatility Index (EVZCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/EVZCLS>, August 2, 2021.

Chicago Board Options Exchange, CBOE Silver ETF Volatility Index (VXSLVCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXSLVCLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE Gold Miners ETF Volatility Index (VXGDXCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXGDXCLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE Energy Sector ETF Volatility Index (VXXLECLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXXLECLS>, August 1, 2021.

Chicago Board Options Exchange, CBOE Brazil ETF Volatility Index (VXEZWCLS), retrieved from FRED, Federal Reserve Bank of St. Louis; <https://fred.stlouisfed.org/series/VXEZWCLS>, August 2, 2021.

---

fitted

*Fitted Matrix from Multivariate Time Series Models*

---

## Description

By defining `stats::fitted()` for each model, this function returns fitted matrix.

## Usage

```
## S3 method for class 'varlse'  
fitted(object, ...)
```

```
## S3 method for class 'vharlse'  
fitted(object, ...)
```

```
## S3 method for class 'bvarmn'
fitted(object, ...)

## S3 method for class 'bvarflat'
fitted(object, ...)

## S3 method for class 'bvharmn'
fitted(object, ...)
```

### Arguments

object	Model object
...	not used

### Value

matrix object.

---

forecast_expand	<i>Out-of-sample Forecasting based on Expanding Window</i>
-----------------	--

---

### Description

This function conducts expanding window forecasting.

### Usage

```
forecast_expand(object, n_ahead, y_test, num_thread = 1, ...)

## S3 method for class 'olsmod'
forecast_expand(object, n_ahead, y_test, num_thread = 1, ...)

## S3 method for class 'normaliw'
forecast_expand(object, n_ahead, y_test, num_thread = 1, use_fit = TRUE, ...)

## S3 method for class 'ldltmod'
forecast_expand(
  object,
  n_ahead,
  y_test,
  num_thread = 1,
  level = 0.05,
  sparse = FALSE,
  lpl = FALSE,
  use_fit = TRUE,
  ...
)
```

```
## S3 method for class 'svmod'
forecast_expand(
  object,
  n_ahead,
  y_test,
  num_thread = 1,
  level = 0.05,
  use_sv = TRUE,
  sparse = FALSE,
  lp1 = FALSE,
  use_fit = TRUE,
  ...
)
```

### Arguments

object	Model object
n_ahead	Step to forecast in rolling window scheme
y_test	Test data to be compared. Use <code>divide_ts()</code> if you don't have separate evaluation dataset.
num_thread	<b>[Experimental]</b> Number of threads
...	Additional arguments.
use_fit	<b>[Experimental]</b> Use object result for the first window. By default, TRUE.
level	Specify alpha of confidence interval level $100(1 - \alpha)$ percentage. By default, .05.
sparse	<b>[Experimental]</b> Apply restriction. By default, FALSE.
lp1	<b>[Experimental]</b> Compute log-predictive likelihood (LPL). By default, FALSE.
use_sv	Use SV term

### Details

Expanding windows forecasting fixes the starting period. It moves the window ahead and forecast h-ahead in `y_test` set.

### Value

`predbvhar_expand` [class](#)

### References

Hyndman, R. J., & Athanasopoulos, G. (2021). *Forecasting: Principles and practice* (3rd ed.). OTEXTS. <https://otexts.com/fpp3/>

---

`forecast_roll`*Out-of-sample Forecasting based on Rolling Window*

---

**Description**

This function conducts rolling window forecasting.

**Usage**

```
forecast_roll(object, n_ahead, y_test, num_thread = 1, ...)
```

```
## S3 method for class 'bvharcv'
```

```
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

```
is.bvharcv(x)
```

```
## S3 method for class 'bvharcv'
```

```
knit_print(x, ...)
```

```
## S3 method for class 'olsmod'
```

```
forecast_roll(object, n_ahead, y_test, num_thread = 1, ...)
```

```
## S3 method for class 'normaliw'
```

```
forecast_roll(object, n_ahead, y_test, num_thread = 1, use_fit = TRUE, ...)
```

```
## S3 method for class 'ldlmod'
```

```
forecast_roll(  
  object,  
  n_ahead,  
  y_test,  
  num_thread = 1,  
  level = 0.05,  
  sparse = FALSE,  
  lpl = FALSE,  
  use_fit = TRUE,  
  ...  
)
```

```
## S3 method for class 'svmod'
```

```
forecast_roll(  
  object,  
  n_ahead,  
  y_test,  
  num_thread = 1,  
  level = 0.05,  
  use_sv = TRUE,  
  sparse = FALSE,  
)
```

```

    lp1 = FALSE,
    use_fit = TRUE,
    ...
)

```

### Arguments

object	Model object
n_ahead	Step to forecast in rolling window scheme
y_test	Test data to be compared. Use <code>divide_ts()</code> if you don't have separate evaluation dataset.
num_thread	<b>[Experimental]</b> Number of threads
...	not used
x	bvharcv object
digits	digit option to print
use_fit	<b>[Experimental]</b> Use object result for the first window. By default, TRUE.
level	Specify alpha of confidence interval level 100(1 - alpha) percentage. By default, .05.
sparse	<b>[Experimental]</b> Apply restriction. By default, FALSE.
lp1	<b>[Experimental]</b> Compute log-predictive likelihood (LPL). By default, FALSE.
use_sv	Use SV term

### Details

Rolling windows forecasting fixes window size. It moves the window ahead and forecast h-ahead in `y_test` set.

### Value

`predbvhar_roll` [class](#)

### References

Hyndman, R. J., & Athanasopoulos, G. (2021). *Forecasting: Principles and practice* (3rd ed.). OTEXTS.

**Description**

Compute FPE of VAR(p) and VHAR

**Usage**

```
FPE(object, ...)

## S3 method for class 'varlse'
FPE(object, ...)

## S3 method for class 'vharlse'
FPE(object, ...)
```

**Arguments**

object	Model fit
...	not used

**Details**

Let  $\tilde{\Sigma}_e$  be the MLE and let  $\hat{\Sigma}_e$  be the unbiased estimator (covmat) for  $\Sigma_e$ . Note that

$$\tilde{\Sigma}_e = \frac{n-k}{T} \hat{\Sigma}_e$$

Then

$$FPE(p) = \left(\frac{n+k}{n-k}\right)^m \det \tilde{\Sigma}_e$$

**Value**

FPE value.

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

fromse *Evaluate the Estimation Based on Frobenius Norm*

---

### Description

This function computes estimation error given estimated model and true coefficient.

### Usage

```
fromse(x, y, ...)  
  
## S3 method for class 'bvharsp'  
fromse(x, y, ...)
```

### Arguments

x	Estimated model.
y	Coefficient matrix to be compared.
...	not used

### Details

Consider the Frobenius Norm  $\|\cdot\|_F$ . let  $\hat{\Phi}$  be  $nrow \times k$  the estimates, and let  $\Phi$  be the true coefficients matrix. Then the function computes estimation error by

$$MSE = 100 \frac{\|\hat{\Phi} - \Phi\|_F}{nrow \times k}$$

### Value

Frobenius norm value

### References

Bai, R., & Ghosh, M. (2018). High-dimensional multivariate posterior consistency under global-local shrinkage priors. *Journal of Multivariate Analysis*, 167, 157-170.

---

`geom_eval`*Adding Test Data Layer*

---

**Description**

This function adds a layer of test dataset.

**Usage**

```
geom_eval(data, colour = "red", ...)
```

**Arguments**

<code>data</code>	Test data to draw, which has the same format with the train data.
<code>colour</code>	Color of the line (By default, red).
<code>...</code>	Other arguments passed on the <code>ggplot2::geom_path()</code> .

**Value**

A ggplot layer

---

`gg_loss`*Compare Lists of Models*

---

**Description**

Draw plot of test error for given models

**Usage**

```
gg_loss(  
  mod_list,  
  y,  
  type = c("mse", "mae", "mape", "mase"),  
  mean_line = FALSE,  
  line_param = list(),  
  mean_param = list(),  
  viridis = FALSE,  
  viridis_option = "D",  
  NROW = NULL,  
  NCOL = NULL,  
  ...  
)
```

**Arguments**

<code>mod_list</code>	Lists of forecast results (predbvhar objects)
<code>y</code>	Test data to be compared. should be the same format with the train data and <code>predict\$forecast</code> .
<code>type</code>	Loss function to be used (mse: MSE, mae: MAE, mape: MAPE, mase: MASE)
<code>mean_line</code>	Whether to draw average loss. By default, FALSE.
<code>line_param</code>	Parameter lists for <code>ggplot2::geom_path()</code> .
<code>mean_param</code>	Parameter lists for average loss with <code>ggplot2::geom_hline()</code> .
<code>viridis</code>	If TRUE, scale CI and forecast line using <code>ggplot2::scale_fill_viridis_d()</code> and <code>ggplot2::scale_colour_viridis_d</code> , respectively.
<code>viridis_option</code>	Option for viridis string. See option of <code>ggplot2::scale_colour_viridis_d</code> . Choose one of <code>c("A", "B", "C", "D", "E")</code> . By default, D.
<code>NROW</code>	nrow of <code>ggplot2::facet_wrap()</code>
<code>NCOL</code>	ncol of <code>ggplot2::facet_wrap()</code>
<code>...</code>	Additional options for <code>geom_loss</code> ( <code>inherit.aes</code> and <code>show.legend</code> )

**Value**

A ggplot object

**See Also**

- `mse()` to compute MSE for given forecast result
- `mae()` to compute MAE for given forecast result
- `mape()` to compute MAPE for given forecast result
- `mase()` to compute MASE for given forecast result

---

 HQ

*Hannan-Quinn Criterion*


---

**Description**

Compute HQ of VAR(p), VHAR, BVAR(p), and BVHAR

**Usage**

```
HQ(object, ...)

## S3 method for class 'logLik'
HQ(object, ...)

## S3 method for class 'varlse'
HQ(object, ...)
```

```
## S3 method for class 'vharlse'
HQ(object, ...)

## S3 method for class 'bvarmn'
HQ(object, ...)

## S3 method for class 'bvarflat'
HQ(object, ...)

## S3 method for class 'bvharln'
HQ(object, ...)
```

### Arguments

object	A logLik object or Model fit
...	not used

### Details

The formula is

$$HQ = -2 \log p(y | \hat{\theta}) + k \log \log(T)$$

which can be computed by `AIC(object, ..., k = 2 * log(log(nobs(object))))` with `stats::AIC()`.

Let  $\tilde{\Sigma}_e$  be the MLE and let  $\hat{\Sigma}_e$  be the unbiased estimator (covmat) for  $\Sigma_e$ . Note that

$$\tilde{\Sigma}_e = \frac{n - k}{T} \hat{\Sigma}_e$$

Then

$$HQ(p) = \log \det \Sigma_e + \frac{2 \log \log n}{n} (\text{number of freely estimated parameters})$$

where the number of freely estimated parameters is  $pm^2$ .

### Value

HQ value.

### References

- Hannan, E.J. and Quinn, B.G. (1979). *The Determination of the Order of an Autoregression*. Journal of the Royal Statistical Society: Series B (Methodological), 41: 190-195.
- Hannan, E.J. and Quinn, B.G. (1979). *The Determination of the Order of an Autoregression*. Journal of the Royal Statistical Society: Series B (Methodological), 41: 190-195.
- Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.
- Quinn, B.G. (1980). *Order Determination for a Multivariate Autoregression*. Journal of the Royal Statistical Society: Series B (Methodological), 42: 182-185.

---

init_ssvs	<i>Initial Parameters of Stochastic Search Variable Selection (SSVS) Model</i>
-----------	--

---

## Description

**[Deprecated]** Set initial parameters before starting Gibbs sampler for SSVS.

## Usage

```
init_ssvs(
  init_coef,
  init_coef_dummy,
  init_chol,
  init_chol_dummy,
  type = c("user", "auto")
)

## S3 method for class 'ssvsinit'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.ssvsinit(x)

## S3 method for class 'ssvsinit'
knit_print(x, ...)
```

## Arguments

init_coef	Initial coefficient matrix. Initialize with an array or list for multiple chains.
init_coef_dummy	Initial indicator matrix (1-0) corresponding to each component of coefficient. Initialize with an array or list for multiple chains.
init_chol	Initial cholesky factor (upper triangular). Initialize with an array or list for multiple chains.
init_chol_dummy	Initial indicator matrix (1-0) corresponding to each component of cholesky factor. Initialize with an array or list for multiple chains.
type	<b>[Experimental]</b> Type to choose initial values. One of user (User-given) and auto (OLS for coefficients and 1 for dummy).
x	ssvsinit
digits	digit option to print
...	not used

**Details**

Set SSVS initialization for the VAR model.

- `init_coef`:  $(kp + 1) \times m$   $A$  coefficient matrix.
- `init_coef_dummy`:  $kp \times m$   $\Gamma$  dummy matrix to restrict the coefficients.
- `init_chol`:  $k \times k$   $\Psi$  upper triangular cholesky factor, which  $\Psi\Psi^\top = \Sigma_e^{-1}$ .
- `init_chol_dummy`:  $k \times k$   $\Omega$  upper triangular dummy matrix to restrict the cholesky factor.

Denote that `init_chol` and `init_chol_dummy` should be upper\_triangular or the function gives error.

For parallel chain initialization, assign three-dimensional array or three-length list.

**Value**

ssvsinit object

**References**

George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.

George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.

Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.

---

irf.varlse

*Impulse Response Analysis*

---

**Description**

Computes responses to impulses or orthogonal impulses

**Usage**

```
## S3 method for class 'varlse'
irf(object, lag_max = 10, orthogonal = TRUE, impulse_var, response_var, ...)
```

```
## S3 method for class 'vharlse'
irf(object, lag_max = 10, orthogonal = TRUE, impulse_var, response_var, ...)
```

```
## S3 method for class 'bvharirf'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

```
irf(object, lag_max, orthogonal, impulse_var, response_var, ...)
```

```
is.bvharirf(x)
```

```
## S3 method for class 'bvharirf'
knit_print(x, ...)
```

### Arguments

object	Model object
lag_max	Maximum lag to investigate the impulse responses (By default, 10)
orthogonal	Orthogonal impulses (TRUE) or just impulses (FALSE)
impulse_var	Impulse variables character vector. If not specified, use every variable.
response_var	Response variables character vector. If not specified, use every variable.
...	not used
x	bvharirf object
digits	digit option to print

### Value

bvharirf [class](#)

### Responses to forecast errors

If orthogonal = FALSE, the function gives  $W_j$  VMA representation of the process such that

$$Y_t = \sum_{j=0}^{\infty} W_j \epsilon_{t-j}$$

### Responses to orthogonal impulses

If orthogonal = TRUE, it gives orthogonalized VMA representation

$$\Theta$$

. Based on variance decomposition (Cholesky decomposition)

$$\Sigma = PP^T$$

where  $P$  is lower triangular matrix, impulse response analysis if performed under MA representation

$$y_t = \sum_{i=0}^{\infty} \Theta_i v_{t-i}$$

Here,

$$\Theta_i = W_i P$$

and  $v_t = P^{-1} \epsilon_t$  are orthogonal.

### References

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

**See Also**

VARtoVMA()

VHARtoVMA()

---

`is.stable`*Stability of the process*

---

**Description**

Check the stability condition of coefficient matrix.

**Usage**

```
is.stable(x, ...)

## S3 method for class 'varlse'
is.stable(x, ...)

## S3 method for class 'vharlse'
is.stable(x, ...)

## S3 method for class 'bvarmn'
is.stable(x, ...)

## S3 method for class 'bvarflat'
is.stable(x, ...)

## S3 method for class 'bvharln'
is.stable(x, ...)
```

**Arguments**

<code>x</code>	Model fit
<code>...</code>	not used

**Details**

VAR(p) is stable if

$$\det(I_m - Az) \neq 0$$

for  $|z| \leq 1$ .

**Value**

logical class

logical class

## References

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

 mae

*Evaluate the Model Based on MAE (Mean Absolute Error)*


---

## Description

This function computes MAE given prediction result versus evaluation set.

## Usage

```
mae(x, y, ...)
```

```
## S3 method for class 'predbvhar'
```

```
mae(x, y, ...)
```

```
## S3 method for class 'bvharcv'
```

```
mae(x, y, ...)
```

## Arguments

x	Forecasting object
y	Test data to be compared. should be the same format with the train data.
...	not used

## Details

Let  $e_t = y_t - \hat{y}_t$ . MAE is defined by

$$MSE = mean(|e_t|)$$

Some researchers prefer MAE to MSE because it is less sensitive to outliers.

## Value

MAE vector corresponding to each variable.

## References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. *International Journal of Forecasting*, 22(4), 679-688.

---

mape	<i>Evaluate the Model Based on MAPE (Mean Absolute Percentage Error)</i>
------	--

---

### Description

This function computes MAPE given prediction result versus evaluation set.

### Usage

```
mape(x, y, ...)
```

```
## S3 method for class 'predbvhar'
```

```
mape(x, y, ...)
```

```
## S3 method for class 'bvharcv'
```

```
mape(x, y, ...)
```

### Arguments

x	Forecasting object
y	Test data to be compared. should be the same format with the train data.
...	not used

### Details

Let  $e_t = y_t - \hat{y}_t$ . Percentage error is defined by  $p_t = 100e_t/Y_t$  (100 can be omitted since comparison is the focus).

$$MAPE = mean(|p_t|)$$

### Value

MAPE vector corresponding to each variable.

### References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

mase *Evaluate the Model Based on MASE (Mean Absolute Scaled Error)*

---

### Description

This function computes MASE given prediction result versus evaluation set.

### Usage

```
mase(x, y, ...)
```

```
## S3 method for class 'predbvhar'
```

```
mase(x, y, ...)
```

```
## S3 method for class 'bvharcv'
```

```
mase(x, y, ...)
```

### Arguments

x	Forecasting object
y	Test data to be compared. should be the same format with the train data.
...	not used

### Details

Let  $e_t = y_t - \hat{y}_t$ . Scaled error is defined by

$$q_t = \frac{e_t}{\sum_{i=2}^n |Y_i - Y_{i-1}| / (n-1)}$$

so that the error can be free of the data scale. Then

$$MASE = \text{mean}(|q_t|)$$

Here,  $Y_i$  are the points in the sample, i.e. errors are scaled by the in-sample mean absolute error ( $\text{mean}(|e_t|)$ ) from the naive random walk forecasting.

### Value

MASE vector corresponding to each variable.

### References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

mrae

*Evaluate the Model Based on MRAE (Mean Relative Absolute Error)*


---

**Description**

This function computes MRAE given prediction result versus evaluation set.

**Usage**

```
mrae(x, pred_bench, y, ...)
```

```
## S3 method for class 'predbvar'
```

```
mrae(x, pred_bench, y, ...)
```

```
## S3 method for class 'bvharcv'
```

```
mrae(x, pred_bench, y, ...)
```

**Arguments**

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

**Details**

Let  $e_t = y_t - \hat{y}_t$ . MRAE implements benchmark model as scaling method. Relative error is defined by

$$r_t = \frac{e_t}{e_t^*}$$

where  $e_t^*$  is the error from the benchmark method. Then

$$MRAE = mean(|r_t|)$$

**Value**

MRAE vector corresponding to each variable.

**References**

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

`mse`*Evaluate the Model Based on MSE (Mean Square Error)*

---

### Description

This function computes MSE given prediction result versus evaluation set.

### Usage

```
mse(x, y, ...)  
  
## S3 method for class 'predbvhar'  
mse(x, y, ...)  
  
## S3 method for class 'bvharcv'  
mse(x, y, ...)
```

### Arguments

<code>x</code>	Forecasting object
<code>y</code>	Test data to be compared. should be the same format with the train data.
<code>...</code>	not used

### Details

Let  $e_t = y_t - \hat{y}_t$ . Then

$$MSE = mean(e_t^2)$$

MSE is the most used accuracy measure.

### Value

MSE vector corresponding to each variable.

### References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

predict

*Forecasting Multivariate Time Series*

---

### Description

Forecasts multivariate time series using given model.

### Usage

```
## S3 method for class 'varlse'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'vharlse'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'bvarmn'
predict(object, n_ahead, n_iter = 100L, level = 0.05, num_thread = 1, ...)

## S3 method for class 'bvharmn'
predict(object, n_ahead, n_iter = 100L, level = 0.05, num_thread = 1, ...)

## S3 method for class 'bvarflat'
predict(object, n_ahead, n_iter = 100L, level = 0.05, num_thread = 1, ...)

## S3 method for class 'bvarssvs'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'bvharssvs'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'bvarhs'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'bvharhs'
predict(object, n_ahead, level = 0.05, ...)

## S3 method for class 'bvarldlt'
predict(
  object,
  n_ahead,
  level = 0.05,
  num_thread = 1,
  sparse = FALSE,
  warn = FALSE,
  ...
)
```

```
## S3 method for class 'bvharldlt'
predict(
  object,
  n_ahead,
  level = 0.05,
  num_thread = 1,
  sparse = FALSE,
  warn = FALSE,
  ...
)

## S3 method for class 'bvarsv'
predict(
  object,
  n_ahead,
  level = 0.05,
  num_thread = 1,
  use_sv = TRUE,
  sparse = FALSE,
  warn = FALSE,
  ...
)

## S3 method for class 'bvharsv'
predict(
  object,
  n_ahead,
  level = 0.05,
  num_thread = 1,
  use_sv = TRUE,
  sparse = FALSE,
  warn = FALSE,
  ...
)

## S3 method for class 'predbvhar'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.predbvhar(x)

## S3 method for class 'predbvhar'
knit_print(x, ...)
```

### Arguments

object	Model object
n_ahead	step to forecast
level	Specify alpha of confidence interval level 100(1 - alpha) percentage. By default,

	.05.
...	not used
n_iter	Number to sample residual matrix from inverse-wishart distribution. By default, 100.
num_thread	Number of threads
sparse	<b>[Experimental]</b> Apply restriction. By default, FALSE. Give CI level (e.g. .05) instead of TRUE to use credible interval across MCMC for restriction.
warn	Give warning for stability of each coefficients record. By default, FALSE.
use_sv	Use SV term
x	predbvhar object
digits	digit option to print

### Value

predbvhar [class](#) with the following components:

**process** object\$process

**forecast** forecast matrix

**se** standard error matrix

**lower** lower confidence interval

**upper** upper confidence interval

**lower\_joint** lower CI adjusted (Bonferroni)

**upper\_joint** upper CI adjusted (Bonferroni)

**y** object\$y

### n-step ahead forecasting VAR(p)

See pp35 of Lütkepohl (2007). Consider h-step ahead forecasting (e.g.  $n + 1, \dots, n + h$ ).

Let  $y_{(n)}^T = (y_n^T, \dots, y_{n-p+1}^T, 1)$ . Then one-step ahead (point) forecasting:

$$\hat{y}_{n+1}^T = y_{(n)}^T \hat{B}$$

Recursively, let  $\hat{y}_{(n+1)}^T = (\hat{y}_{n+1}^T, y_n^T, \dots, y_{n-p+2}^T, 1)$ . Then two-step ahead (point) forecasting:

$$\hat{y}_{n+2}^T = \hat{y}_{(n+1)}^T \hat{B}$$

Similarly, h-step ahead (point) forecasting:

$$\hat{y}_{n+h}^T = \hat{y}_{(n+h-1)}^T \hat{B}$$

How about confident region? Confidence interval at h-period is

$$y_{k,t}(h) \pm z_{(\alpha/2)} \sigma_k(h)$$

Joint forecast region of  $100(1 - \alpha)\%$  can be computed by

$$\{(y_{k,1}, y_{k,h}) \mid y_{k,n}(i) - z_{(\alpha/2h)}\sigma_n(i) \leq y_{n,i} \leq y_{k,n}(i) + z_{(\alpha/2h)}\sigma_k(i), i = 1, \dots, h\}$$

See the pp41 of Lütkepohl (2007).

To compute covariance matrix, it needs VMA representation:

$$Y_t(h) = c + \sum_{i=h}^{\infty} W_i \epsilon_{t+h-i} = c + \sum_{i=0}^{\infty} W_{h+i} \epsilon_{t-i}$$

Then

$$\Sigma_y(h) = MSE[y_t(h)] = \sum_{i=0}^{h-1} W_i \Sigma_\epsilon W_i^T = \Sigma_y(h-1) + W_{h-1} \Sigma_\epsilon W_{h-1}^T$$

### n-step ahead forecasting VHAR

Let  $T_{HAR}$  is VHAR linear transformation matrix. Since VHAR is the linearly transformed VAR(22), let  $y_{(n)}^T = (y_n^T, y_{n-1}^T, \dots, y_{n-21}^T, 1)$ .

Then one-step ahead (point) forecasting:

$$\hat{y}_{n+1}^T = y_{(n)}^T T_{HAR} \hat{\Phi}$$

Recursively, let  $\hat{y}_{(n+1)}^T = (\hat{y}_{n+1}^T, y_n^T, \dots, y_{n-20}^T, 1)$ . Then two-step ahead (point) forecasting:

$$\hat{y}_{n+2}^T = \hat{y}_{(n+1)}^T T_{HAR} \hat{\Phi}$$

and h-step ahead (point) forecasting:

$$\hat{y}_{n+h}^T = \hat{y}_{(n+h-1)}^T T_{HAR} \hat{\Phi}$$

### n-step ahead forecasting BVAR(p) with minnesota prior

Point forecasts are computed by posterior mean of the parameters. See Section 3 of Bańbura et al. (2010).

Let  $\hat{B}$  be the posterior MN mean and let  $\hat{V}$  be the posterior MN precision.

Then predictive posterior for each step

$$y_{n+1} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n)}^T A), \Sigma_e \otimes (1 + y_{(n)}^T \hat{V}^{-1} y_{(n)}))$$

$$y_{n+2} \mid \Sigma_e, y \sim N(\text{vec}(\hat{y}_{(n+1)}^T A), \Sigma_e \otimes (1 + \hat{y}_{(n+1)}^T \hat{V}^{-1} \hat{y}_{(n+1)}))$$

and recursively,

$$y_{n+h} \mid \Sigma_e, y \sim N(\text{vec}(\hat{y}_{(n+h-1)}^T A), \Sigma_e \otimes (1 + \hat{y}_{(n+h-1)}^T \hat{V}^{-1} \hat{y}_{(n+h-1)}))$$

### n-step ahead forecasting BVHAR

Let  $\hat{\Phi}$  be the posterior MN mean and let  $\hat{\Psi}$  be the posterior MN precision.

Then predictive posterior for each step

$$y_{n+1} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n)}^T \tilde{T}^T \Phi), \Sigma_e \otimes (1 + y_{(n)}^T \tilde{T} \hat{\Psi}^{-1} \tilde{T} y_{(n)}))$$

$$y_{n+2} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n+1)}^T \tilde{T}^T \Phi), \Sigma_e \otimes (1 + y_{(n+1)}^T \tilde{T} \hat{\Psi}^{-1} \tilde{T} y_{(n+1)}))$$

and recursively,

$$y_{n+h} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n+h-1)}^T \tilde{T}^T \Phi), \Sigma_e \otimes (1 + y_{(n+h-1)}^T \tilde{T} \hat{\Psi}^{-1} \tilde{T} y_{(n+h-1)}))$$

### n-step ahead forecasting VAR(p) with SSVS and Horseshoe

The process of the computing point estimate is the same. However, predictive interval is achieved from each Gibbs sampler sample.

$$y_{n+1} \mid A, \Sigma_e, y \sim N(\text{vec}(y_{(n)}^T A), \Sigma_e)$$

$$y_{n+h} \mid A, \Sigma_e, y \sim N(\text{vec}(\hat{y}_{(n+h-1)}^T A), \Sigma_e)$$

### n-step ahead forecasting VHAR with SSVS and Horseshoe

The process of the computing point estimate is the same. However, predictive interval is achieved from each Gibbs sampler sample.

$$y_{n+1} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n)}^T \tilde{T}^T \Phi), \Sigma_e \otimes (1 + y_{(n)}^T \tilde{T} \hat{\Psi}^{-1} \tilde{T} y_{(n)}))$$

$$y_{n+h} \mid \Sigma_e, y \sim N(\text{vec}(y_{(n+h-1)}^T \tilde{T}^T \Phi), \Sigma_e \otimes (1 + y_{(n+h-1)}^T \tilde{T} \hat{\Psi}^{-1} \tilde{T} y_{(n+h-1)}))$$

### References

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George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.

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Huber, F., Koop, G., & Onorante, L. (2021). *Inducing Sparsity and Shrinkage in Time-Varying Parameter Models*. Journal of Business & Economic Statistics, 39(3), 669-683.

print.summary.bvharsp *Summarizing BVAR and BVHAR with Shrinkage Priors*

## Description

Conduct variable selection.

## Usage

```
## S3 method for class 'summary.bvharsp'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'summary.bvharsp'
knit_print(x, ...)

## S3 method for class 'ssvsmod'
summary(object, method = c("pip", "ci"), threshold = 0.5, level = 0.05, ...)

## S3 method for class 'hsmod'
summary(object, method = c("pip", "ci"), threshold = 0.5, level = 0.05, ...)

## S3 method for class 'ngmod'
summary(object, level = 0.05, ...)
```

## Arguments

x	summary.bvharsp object
digits	digit option to print
...	not used
object	Model fit
method	Use PIP (pip) or credible interval (ci).
threshold	Threshold for posterior inclusion probability
level	Specify alpha of credible interval level 100(1 - alpha) percentage. By default, .05.

**Value**

summary.ssvsmod object  
 hsmod object  
 ngmod object

**References**

- George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.
- George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.
- Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.
- O'Hara, R. B., & Sillanpää, M. J. (2009). *A review of Bayesian variable selection methods: what, how and which*. Bayesian Analysis, 4(1), 85-117.

---

 relmae

---

*Evaluate the Model Based on RelMAE (Relative MAE)*


---

**Description**

This function computes RelMAE given prediction result versus evaluation set.

**Usage**

```
relmae(x, pred_bench, y, ...)

## S3 method for class 'predbvhar'
relmae(x, pred_bench, y, ...)

## S3 method for class 'bvharcv'
relmae(x, pred_bench, y, ...)
```

**Arguments**

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

**Details**

Let  $e_t = y_t - \hat{y}_t$ . RelMAE implements MAE of benchmark model as relative measures. Let  $MAE_b$  be the MAE of the benchmark model. Then

$$RelMAE = \frac{MAE}{MAE_b}$$

where  $MAE$  is the MAE of our model.

**Value**

RelMAE vector corresponding to each variable.

**References**

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

 relspne

---

*Evaluate the Estimation Based on Relative Spectral Norm Error*


---

**Description**

This function computes relative estimation error given estimated model and true coefficient.

**Usage**

```
relspne(x, y, ...)
```

```
## S3 method for class 'bvharasp'
relspne(x, y, ...)
```

**Arguments**

x	Estimated model.
y	Coefficient matrix to be compared.
...	not used

**Details**

Let  $\|\cdot\|_2$  be the spectral norm of a matrix, let  $\hat{\Phi}$  be the estimates, and let  $\Phi$  be the true coefficients matrix. Then the function computes relative estimation error by

$$\frac{\|\hat{\Phi} - \Phi\|_2}{\|\Phi\|_2}$$

**Value**

Spectral norm value

**References**

Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).

---

residuals

*Residual Matrix from Multivariate Time Series Models*


---

**Description**

By defining `stats::residuals()` for each model, this function returns residual.

**Usage**

```
## S3 method for class 'varlse'
residuals(object, ...)

## S3 method for class 'vharlse'
residuals(object, ...)

## S3 method for class 'bvarmn'
residuals(object, ...)

## S3 method for class 'bvarflat'
residuals(object, ...)

## S3 method for class 'bvharmn'
residuals(object, ...)
```

**Arguments**

object	Model object
...	not used

**Value**

`matrix` object.

---

rmafe	Evaluate the Model Based on RMAFE
-------	-----------------------------------

---

### Description

This function computes RMAFE (Mean Absolute Forecast Error Relative to the Benchmark)

### Usage

```
rmafe(x, pred_bench, y, ...)

## S3 method for class 'predbvhar'
rmafe(x, pred_bench, y, ...)

## S3 method for class 'bvharcv'
rmafe(x, pred_bench, y, ...)
```

### Arguments

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

### Details

Let  $e_t = y_t - \hat{y}_t$ . RMAFE is the ratio of L1 norm of  $e_t$  from forecasting object and from benchmark model.

$$RMAFE = \frac{\text{sum}(\|e_t\|)}{\text{sum}(\|e_t^{(b)}\|)}$$

where  $e_t^{(b)}$  is the error from the benchmark model.

### Value

RMAFE vector corresponding to each variable.

### References

- Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. *International Journal of Forecasting*, 22(4), 679-688.
- Bañbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. *Journal of Applied Econometrics*, 25(1).
- Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).

---

rmape

*Evaluate the Model Based on RMAPE (Relative MAPE)*


---

### Description

This function computes RMAPE given prediction result versus evaluation set.

### Usage

```
rmape(x, pred_bench, y, ...)

## S3 method for class 'predbvhar'
rmape(x, pred_bench, y, ...)

## S3 method for class 'bvharcv'
rmape(x, pred_bench, y, ...)
```

### Arguments

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

### Details

RMAPE is the ratio of MAPE of given model and the benchmark one. Let  $MAPE_b$  be the MAPE of the benchmark model. Then

$$RMAPE = \frac{mean(MAPE)}{mean(MAPE_b)}$$

where  $MAPE$  is the MAPE of our model.

### Value

RMAPE vector corresponding to each variable.

### References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

---

 rmase

*Evaluate the Model Based on RMASE (Relative MASE)*


---

### Description

This function computes RMASE given prediction result versus evaluation set.

### Usage

```
rmase(x, pred_bench, y, ...)

## S3 method for class 'predbvar'
rmase(x, pred_bench, y, ...)

## S3 method for class 'bvharcv'
rmase(x, pred_bench, y, ...)
```

### Arguments

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

### Details

RMASE is the ratio of MAPE of given model and the benchmark one. Let  $MASE_b$  be the MAPE of the benchmark model. Then

$$RMASE = \frac{mean(MASE)}{mean(MASE_b)}$$

where  $MASE$  is the MASE of our model.

### Value

RMASE vector corresponding to each variable.

### References

Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. International Journal of Forecasting, 22(4), 679-688.

rmsfe

*Evaluate the Model Based on RMSFE***Description**

This function computes RMSFE (Mean Squared Forecast Error Relative to the Benchmark)

**Usage**

```
rmsfe(x, pred_bench, y, ...)

## S3 method for class 'predbvhar'
rmsfe(x, pred_bench, y, ...)

## S3 method for class 'bvharcv'
rmsfe(x, pred_bench, y, ...)
```

**Arguments**

x	Forecasting object to use
pred_bench	The same forecasting object from benchmark model
y	Test data to be compared. should be the same format with the train data.
...	not used

**Details**

Let  $e_t = y_t - \hat{y}_t$ . RMSFE is the ratio of L2 norm of  $e_t$  from forecasting object and from benchmark model.

$$RMSFE = \frac{\text{sum}(\|e_t\|)}{\text{sum}(\|e_t^{(b)}\|)}$$

where  $e_t^{(b)}$  is the error from the benchmark model.

**Value**

RMSFE vector corresponding to each variable.

**References**

- Hyndman, R. J., & Koehler, A. B. (2006). *Another look at measures of forecast accuracy*. *International Journal of Forecasting*, 22(4), 679-688.
- Bañbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. *Journal of Applied Econometrics*, 25(1).
- Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).

**Description**

Set hyperparameters of Bayesian VAR and VHAR models.

**Usage**

```
set_bvar(sigma, lambda = 0.1, delta, eps = 1e-04)
set_bvar_flat(U)
set_bvhar(sigma, lambda = 0.1, delta, eps = 1e-04)
set_weight_bvhar(sigma, lambda = 0.1, eps = 1e-04, daily, weekly, monthly)

## S3 method for class 'bvhar-spec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.bvhar-spec(x)

## S3 method for class 'bvhar-spec'
knit_print(x, ...)
```

**Arguments**

sigma	Standard error vector for each variable (Default: sd)
lambda	Tightness of the prior around a random walk or white noise (Default: .1)
delta	Persistence (Default: Litterman sets 1 = random walk prior, White noise prior = 0)
eps	Very small number (Default: 1e-04)
U	Positive definite matrix. By default, identity matrix of dimension ncol(X0)
daily	Same as delta in VHAR type (Default: 1 as Litterman)
weekly	Fill the second part in the first block (Default: 1)
monthly	Fill the third part in the first block (Default: 1)
x	bvhar-spec object
digits	digit option to print
...	not used

**Details**

- Missing arguments will be set to be default values in each model function mentioned above.
- `set_bvar()` sets hyperparameters for `bvar_minnesota()`.
- Each `delta` (vector), `lambda` (length of 1), `sigma` (vector), `eps` (vector) corresponds to  $\delta_j$ ,  $\lambda$ ,  $\delta_j$ ,  $\epsilon$ .

$\delta_i$  are related to the belief to random walk.

- If  $\delta_i = 1$  for all  $i$ , random walk prior
- If  $\delta_i = 0$  for all  $i$ , white noise prior

$\lambda$  controls the overall tightness of the prior around these two prior beliefs.

- If  $\lambda = 0$ , the posterior is equivalent to prior and the data do not influence the estimates.
- If  $\lambda = \infty$ , the posterior mean becomes OLS estimates (VAR).

$\sigma_i^2/\sigma_j^2$  in Minnesota moments explain the data scales.

- `set_bvar_flat` sets hyperparameters for `bvar_flat()`.
- `set_bvhar()` sets hyperparameters for `bvhar_minnesota()` with VAR-type Minnesota prior, i.e. BVHAR-S model.
- `set_weight_bvhar()` sets hyperparameters for `bvhar_minnesota()` with VHAR-type Minnesota prior, i.e. BVHAR-L model.

**Value**

Every function returns `bvharspec` class. It is the list of which the components are the same as the arguments provided. If the argument is not specified, NULL is assigned here. The default values mentioned above will be considered in each fitting function.

**process** Model name: BVAR, BVHAR

**prior** Prior name: Minnesota (Minnesota prior for BVAR), Hierarchical (Hierarchical prior for BVAR), MN\_VAR (BVHAR-S), MN\_VHAR (BVHAR-L), Flat (Flat prior for BVAR)

**sigma** Vector value (or `bvharriorspec` class) assigned for sigma

**lambda** Value (or `bvharriorspec` class) assigned for lambda

**delta** Vector value assigned for delta

**eps** Value assigned for epsilon

`set_weight_bvhar()` has different component with `delta` due to its different construction.

**daily** Vector value assigned for daily weight

**weekly** Vector value assigned for weekly weight

**monthly** Vector value assigned for monthly weight

**Note**

By using `set_psi()` and `set_lambda()` each, hierarchical modeling is available.

## References

- Bañbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. *Journal of Applied Econometrics*, 25(1).
- Litterman, R. B. (1986). *Forecasting with Bayesian Vector Autoregressions: Five Years of Experience*. *Journal of Business & Economic Statistics*, 4(1), 25.
- Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).
- Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. *Journal of Statistical Computation and Simulation*, 94(6), 1139-1157.
- Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. *Journal of Statistical Computation and Simulation*, 94(6), 1139-1157.

## See Also

- lambda hyperprior specification [set\\_lambda\(\)](#)
- sigma hyperprior specification [set\\_psi\(\)](#)

## Examples

```
# Minnesota BVAR specification-----
bvar_spec <- set_bvar(
  sigma = c(.03, .02, .01), # Sigma = diag(.03^2, .02^2, .01^2)
  lambda = .2, # lambda = .2
  delta = rep(.1, 3), # delta1 = .1, delta2 = .1, delta3 = .1
  eps = 1e-04 # eps = 1e-04
)
class(bvar_spec)
str(bvar_spec)
# Flat BVAR specification-----
# 3-dim
# p = 5 with constant term
# U = 500 * I(mp + 1)
bvar_flat_spec <- set_bvar_flat(U = 500 * diag(16))
class(bvar_flat_spec)
str(bvar_flat_spec)
# BVHAR-S specification-----
bvhar_var_spec <- set_bvhar(
  sigma = c(.03, .02, .01), # Sigma = diag(.03^2, .02^2, .01^2)
  lambda = .2, # lambda = .2
  delta = rep(.1, 3), # delta1 = .1, delta2 = .1, delta3 = .1
  eps = 1e-04 # eps = 1e-04
)
class(bvhar_var_spec)
str(bvhar_var_spec)
# BVHAR-L specification-----
bvhar_vhar_spec <- set_weight_bvhar(
  sigma = c(.03, .02, .01), # Sigma = diag(.03^2, .02^2, .01^2)
  lambda = .2, # lambda = .2
  eps = 1e-04, # eps = 1e-04
```

```

daily = rep(.2, 3), # daily1 = .2, daily2 = .2, daily3 = .2
weekly = rep(.1, 3), # weekly1 = .1, weekly2 = .1, weekly3 = .1
monthly = rep(.05, 3) # monthly1 = .05, monthly2 = .05, monthly3 = .05
)
class(bvhar_vhar_spec)
str(bvhar_vhar_spec)

```

---

set_dl	<i>Dirichlet-Laplace Hyperparameter for Coefficients and Contemporaneous Coefficients</i>
--------	---

---

### Description

**[Experimental]** Set DL hyperparameters for VAR or VHAR coefficient and contemporaneous coefficient.

### Usage

```

set_dl(dir_grid = 100L, shape = 0.01, rate = 0.01)

## S3 method for class 'dlspec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.dlspec(x)

```

### Arguments

dir_grid	Griddy gibbs grid size for Dirichlet hyperparameter
shape	Gamma shape
rate	Gamma rate
x	dlspec
digits	digit option to print
...	not used

### Value

dlspec object

### References

Bhattacharya, A., Pati, D., Pillai, N. S., & Dunson, D. B. (2015). *Dirichlet-Laplace Priors for Optimal Shrinkage*. *Journal of the American Statistical Association*, 110(512), 1479-1490.

Korobilis, D., & Shimizu, K. (2022). *Bayesian Approaches to Shrinkage and Sparse Estimation*. *Foundations and Trends® in Econometrics*, 11(4), 230-354.

---

set_horseshoe	<i>Horseshoe Prior Specification</i>
---------------	--------------------------------------

---

### Description

Set initial hyperparameters and parameter before starting Gibbs sampler for Horseshoe prior.

### Usage

```
set_horseshoe(local_sparsity = 1, group_sparsity = 1, global_sparsity = 1)

## S3 method for class 'horseshoespec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.horseshoespec(x)

## S3 method for class 'horseshoespec'
knit_print(x, ...)
```

### Arguments

local_sparsity	Initial local shrinkage hyperparameters
group_sparsity	Initial group shrinkage hyperparameters
global_sparsity	Initial global shrinkage hyperparameter
x	horseshoespec
digits	digit option to print
...	not used

### Details

Set horseshoe prior initialization for VAR family.

- local\_sparsity: Initial local shrinkage
- group\_sparsity: Initial group shrinkage
- global\_sparsity: Initial global shrinkage

In this package, horseshoe prior model is estimated by Gibbs sampling, initial means initial values for that gibbs sampler.

### References

- Carvalho, C. M., Polson, N. G., & Scott, J. G. (2010). The horseshoe estimator for sparse signals. *Biometrika*, 97(2), 465-480.
- Makalic, E., & Schmidt, D. F. (2016). *A Simple Sampler for the Horseshoe Estimator*. *IEEE Signal Processing Letters*, 23(1), 179-182.

---

set_intercept	<i>Prior for Constant Term</i>
---------------	--------------------------------

---

**Description**

Set Normal prior hyperparameters for constant term

**Usage**

```
set_intercept(mean = 0, sd = 0.1)

## S3 method for class 'interceptspec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.interceptspec(x)

## S3 method for class 'interceptspec'
knit_print(x, ...)
```

**Arguments**

mean	Normal mean of constant term
sd	Normal standard deviation for constant term
x	interceptspec object
digits	digit option to print
...	not used

---

set_lambda	<i>Hyperpriors for Bayesian Models</i>
------------	--

---

**Description**

Set hyperpriors of Bayesian VAR and VHAR models.

**Usage**

```
set_lambda(mode = 0.2, sd = 0.4, param = NULL, lower = 1e-05, upper = 3)

set_psi(shape = 4e-04, scale = 4e-04, lower = 1e-05, upper = 3)

## S3 method for class 'bvharriorspec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.bvharriorspec(x)

## S3 method for class 'bvharriorspec'
knit_print(x, ...)
```

**Arguments**

mode	Mode of Gamma distribution. By default, .2.
sd	Standard deviation of Gamma distribution. By default, .4.
param	Shape and rate of Gamma distribution, in the form of c(shape, rate). If specified, ignore mode and sd.
lower	<b>[Experimental]</b> Lower bound for <code>stats::optim()</code> . By default, 1e-5.
upper	<b>[Experimental]</b> Upper bound for <code>stats::optim()</code> . By default, 3.
shape	Shape of Inverse Gamma distribution. By default, (.02)^2.
scale	Scale of Inverse Gamma distribution. By default, (.02)^2.
x	bvharriorspec object
digits	digit option to print
...	not used

**Details**

In addition to Normal-IW priors `set_bvar()`, `set_bvhar()`, and `set_weight_bvhar()`, these functions give hierarchical structure to the model.

- `set_lambda()` specifies hyperprior for  $\lambda$  (lambda), which is Gamma distribution.
- `set_psi()` specifies hyperprior for  $\psi/(\nu_0 - k - 1) = \sigma^2$  (sigma), which is Inverse gamma distribution.

The following set of (mode, sd) are recommended by Sims and Zha (1998) for `set_lambda()`.

- (mode = .2, sd = .4): default
- (mode = 1, sd = 1)

Giannone et al. (2015) suggested data-based selection for `set_psi()`. It chooses (0.02)^2 based on its empirical data set.

**Value**

bvharriorspec object

**References**

Giannone, D., Lenza, M., & Primiceri, G. E. (2015). *Prior Selection for Vector Autoregressions*. *Review of Economics and Statistics*, 97(2).

**Examples**

```
# Hierarchy BVAR specification-----
set_bvar(
  sigma = set_psi(shape = 4e-4, scale = 4e-4),
  lambda = set_lambda(mode = .2, sd = .4),
  delta = rep(1, 3),
  eps = 1e-04 # eps = 1e-04
)
```

---

 set\_ldlt

*Covariance Matrix Prior Specification*


---

**Description**

**[Experimental]** Set prior for covariance matrix.

**Usage**

```

set_ldlt(ig_shape = 3, ig_scl = 0.01)

set_sv(ig_shape = 3, ig_scl = 0.01, initial_mean = 1, initial_prec = 0.1)

## S3 method for class 'covspec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.covspec(x)

is.svspec(x)

is.ldltspec(x)

```

**Arguments**

ig_shape	Inverse-Gamma shape of Cholesky diagonal vector. For SV ( <a href="#">set_sv()</a> ), this is for state variance.
ig_scl	Inverse-Gamma scale of Cholesky diagonal vector. For SV ( <a href="#">set_sv()</a> ), this is for state variance.
initial_mean	Prior mean of initial state.
initial_prec	Prior precision of initial state.
x	covspec
digits	digit option to print
...	not used

**Details**

[set\\_ldlt\(\)](#) specifies LDLT of precision matrix,

$$\Sigma^{-1} = L^T D^{-1} L$$

[set\\_sv\(\)](#) specifies time varying precision matrix under stochastic volatility framework based on

$$\Sigma_t^{-1} = L^T D_t^{-1} L$$

## References

Carriero, A., Chan, J., Clark, T. E., & Marcellino, M. (2022). *Corrigendum to “Large Bayesian vector autoregressions with stochastic volatility and non-conjugate priors” [J. Econometrics 212 (1)(2019) 137-154]*. *Journal of Econometrics*, 227(2), 506-512.

Chan, J., Koop, G., Poirier, D., & Tobias, J. (2019). *Bayesian Econometric Methods (2nd ed., Econometric Exercises)*. Cambridge: Cambridge University Press.

---

set_ng	<i>Normal-Gamma Hyperparameter for Coefficients and Contemporaneous Coefficients</i>
--------	--

---

## Description

**[Experimental]** Set NG hyperparameters for VAR or VHAR coefficient and contemporaneous coefficient.

## Usage

```
set_ng(
  shape_sd = 0.01,
  group_shape = 0.01,
  group_scale = 0.01,
  global_shape = 0.01,
  global_scale = 0.01,
  contem_global_shape = 0.01,
  contem_global_scale = 0.01
)

## S3 method for class 'ngspec'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.ngspec(x)
```

## Arguments

shape_sd	Standard deviation used in MH of Gamma shape
group_shape	Inverse gamma prior shape for coefficient group shrinkage
group_scale	Inverse gamma prior scale for coefficient group shrinkage
global_shape	Inverse gamma prior shape for coefficient global shrinkage
global_scale	Inverse gamma prior scale for coefficient global shrinkage
contem_global_shape	Inverse gamma prior shape for contemporaneous coefficient global shrinkage
contem_global_scale	Inverse gamma prior scale for contemporaneous coefficient global shrinkage

x	ngspec
digits	digit option to print
...	not used

**Value**

ngspec object

**References**

Chan, J. C. C. (2021). *Minnesota-type adaptive hierarchical priors for large Bayesian VARs*. *International Journal of Forecasting*, 37(3), 1212-1226.

Huber, F., & Feldkircher, M. (2019). *Adaptive Shrinkage in Bayesian Vector Autoregressive Models*. *Journal of Business & Economic Statistics*, 37(1), 27-39.

Korobilis, D., & Shimizu, K. (2022). *Bayesian Approaches to Shrinkage and Sparse Estimation*. *Foundations and Trends® in Econometrics*, 11(4), 230-354.

---

set_ssvs	<i>Stochastic Search Variable Selection (SSVS) Hyperparameter for Coefficients Matrix and Cholesky Factor</i>
----------	---

---

**Description**

Set SSVS hyperparameters for VAR or VHAR coefficient matrix and Cholesky factor.

**Usage**

```
set_ssvs(
  coef_spike = 0.1,
  coef_slab = 5,
  coef_spike_scl = 0.01,
  coef_slab_shape = 0.01,
  coef_slab_scl = 0.01,
  coef_mixture = 0.5,
  coef_s1 = c(1, 1),
  coef_s2 = c(1, 1),
  mean_non = 0,
  sd_non = 0.1,
  shape = 0.01,
  rate = 0.01,
  chol_spike = 0.1,
  chol_slab = 5,
  chol_spike_scl = 0.01,
  chol_slab_shape = 0.01,
  chol_slab_scl = 0.01,
  chol_mixture = 0.5,
```

```

    chol_s1 = 1,
    chol_s2 = 1
  )

## S3 method for class 'ssvsinput'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

is.ssvsinput(x)

## S3 method for class 'ssvsinput'
knit_print(x, ...)

```

### Arguments

coef_spike	<b>[Deprecated]</b> Standard deviance for Spike normal distribution. Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
coef_slab	<b>[Deprecated]</b> Standard deviance for Slab normal distribution. Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
coef_spike_scl	Scaling factor (between 0 and 1) for spike sd which is Spike sd = c * slab sd
coef_slab_shape	Inverse gamma shape for slab sd
coef_slab_scl	Inverse gamma scale for slab sd
coef_mixture	<b>[Deprecated]</b> Bernoulli parameter for sparsity proportion. Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
coef_s1	First shape of coefficients prior beta distribution
coef_s2	Second shape of coefficients prior beta distribution
mean_non	<b>[Deprecated]</b> Prior mean of unrestricted coefficients Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
sd_non	<b>[Deprecated]</b> Standard deviance for unrestricted coefficients Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
shape	Gamma shape parameters for precision matrix (See Details).
rate	Gamma rate parameters for precision matrix (See Details).
chol_spike	Standard deviance for Spike normal distribution, in the cholesky factor. Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
chol_slab	Standard deviance for Slab normal distribution, in the cholesky factor. Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.
chol_spike_scl	Scaling factor (between 0 and 1) for spike sd which is Spike sd = c * slab sd in the cholesky factor
chol_slab_shape	Inverse gamma shape for slab sd in the cholesky factor
chol_slab_scl	Inverse gamma scale for slab sd in the cholesky factor
chol_mixture	<b>[Deprecated]</b> Bernoulli parameter for sparsity proportion, in the cholesky factor (See Details). Will be deleted when <code>bvar_ssvs()</code> and <code>bvhar_ssvs()</code> are removed in the package.

chol_s1	First shape of cholesky factor prior beta distribution
chol_s2	Second shape of cholesky factor prior beta distribution
x	ssvsinput
digits	digit option to print
...	not used

### Details

Let  $\alpha$  be the vectorized coefficient,  $\alpha = \text{vec}(A)$ . Spike-slab prior is given using two normal distributions.

$$\alpha_j \mid \gamma_j \sim (1 - \gamma_j)N(0, \tau_{0j}^2) + \gamma_j N(0, \tau_{1j}^2)$$

As spike-slab prior itself suggests, set  $\tau_{0j}$  small (point mass at zero: spike distribution) and set  $\tau_{1j}$  large (symmetric by zero: slab distribution).

$\gamma_j$  is the proportion of the nonzero coefficients and it follows

$$\gamma_j \sim \text{Bernoulli}(p_j)$$

- coef\_spike:  $\tau_{0j}$
- coef\_slab:  $\tau_{1j}$
- coef\_mixture:  $p_j$
- $j = 1, \dots, mk$ : vectorized format corresponding to coefficient matrix
- If one value is provided, model function will read it by replicated value.
- coef\_non: vectorized constant term is given prior Normal distribution with variance  $cI$ . Here, coef\_non is  $\sqrt{c}$ .

Next for precision matrix  $\Sigma_e^{-1}$ , SSVS applies Cholesky decomposition.

$$\Sigma_e^{-1} = \Psi\Psi^T$$

where  $\Psi = \{\psi_{ij}\}$  is upper triangular.

Diagonal components follow the gamma distribution.

$$\psi_{jj}^2 \sim \text{Gamma}(\text{shape} = a_j, \text{rate} = b_j)$$

For each row of off-diagonal (upper-triangular) components, we apply spike-slab prior again.

$$\psi_{ij} \mid w_{ij} \sim (1 - w_{ij})N(0, \kappa_{0,ij}^2) + w_{ij}N(0, \kappa_{1,ij}^2)$$

$$w_{ij} \sim \text{Bernoulli}(q_{ij})$$

- shape:  $a_j$
- rate:  $b_j$
- chol\_spike:  $\kappa_{0,ij}$
- chol\_slab:  $\kappa_{1,ij}$
- chol\_mixture:  $q_{ij}$
- $j = 1, \dots, mk$ : vectorized format corresponding to coefficient matrix
- $i = 1, \dots, j-1$  and  $j = 2, \dots, m$ :  $\eta = (\psi_{12}, \psi_{13}, \psi_{23}, \psi_{14}, \dots, \psi_{34}, \dots, \psi_{1m}, \dots, \psi_{m-1,m})^T$
- chol\_ arguments can be one value for replication, vector, or upper triangular matrix.

**Value**

ssvsinput object

**References**

- George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.
- George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.
- Ishwaran, H., & Rao, J. S. (2005). *Spike and slab variable selection: Frequentist and Bayesian strategies*. The Annals of Statistics, 33(2).
- Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.

---

 sim\_gig

 Generate Generalized Inverse Gaussian Distribution
 

---

**Description**

This function samples  $GIG(\lambda, \psi, \chi)$  random variates.

**Usage**

```
sim_gig(num_sim, lambda, psi, chi)
```

**Arguments**

num_sim	Number to generate
lambda	Index of modified Bessel function of third kind.
psi	Second parameter of GIG. Should be positive.
chi	Third parameter of GIG. Should be positive.

**Details**

The density of  $GIG(\lambda, \psi, \chi)$  considered here is as follows.

$$f(x) = \frac{(\psi/\chi)^{(\lambda/2)}}{2K_{\lambda}(\sqrt{\psi\chi})} x^{\lambda-1} \exp\left(-\frac{1}{2}\left(\frac{\chi}{x} + \psi x\right)\right)$$

where  $x > 0$ .

**References**

- Hörmann, W., Leydold, J. *Generating generalized inverse Gaussian random variates*. Stat Comput 24, 547-557 (2014).
- Leydold, J, Hörmann, W.. *GIGrv: Random Variate Generator for the GIG Distribution*. R package version 0.8 (2023).

---

sim\_horseshoe\_var      *Generate Horseshoe Parameters*

---

## Description

**[Deprecated]** This function generates parameters of VAR with Horseshoe prior.

## Usage

```
sim_horseshoe_var(
  p,
  dim_data = NULL,
  include_mean = TRUE,
  minnesota = FALSE,
  method = c("eigen", "chol")
)

sim_horseshoe_vhar(
  har = c(5, 22),
  dim_data = NULL,
  include_mean = TRUE,
  minnesota = c("no", "short", "longrun"),
  method = c("eigen", "chol")
)
```

## Arguments

p	VAR lag
dim_data	Specify the dimension of the data if hyperparameters of bayes_spec have constant values.
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Only use off-diagonal terms of each coefficient matrices for restriction. In sim_horseshoe_var() function, use TRUE or FALSE (default). In sim_horseshoe_vhar() function, no (default), short type, or longrun type.
method	Method to compute $\Sigma^{1/2}$ .
har	Numeric vector for weekly and monthly order. By default, c(5, 22).

---

sim_iw	<i>Generate Inverse-Wishart Random Matrix</i>
--------	---

---

**Description**

This function samples one matrix IW matrix.

**Usage**

```
sim_iw(mat_scale, shape)
```

**Arguments**

mat_scale	Scale matrix
shape	Shape

**Details**

Consider  $\Sigma \sim IW(\Psi, \nu)$ .

1. Upper triangular Bartlett decomposition:  $k \times k$  matrix  $Q = [q_{ij}]$  upper triangular with
  - (a)  $q_{ii}^2 \chi_{\nu-i+1}^2$
  - (b)  $q_{ij} \sim N(0, 1)$  with  $i < j$  (upper triangular)
2. Lower triangular Cholesky decomposition:  $\Psi = LL^T$
3.  $A = L(Q^{-1})^T$
4.  $\Sigma = AA^T \sim IW(\Psi, \nu)$

**Value**

One  $k \times k$  matrix following IW distribution

---

sim_matgaussian	<i>Generate Matrix Normal Random Matrix</i>
-----------------	---

---

**Description**

This function samples one matrix gaussian matrix.

**Usage**

```
sim_matgaussian(mat_mean, mat_scale_u, mat_scale_v, u_prec)
```

**Arguments**

mat_mean	Mean matrix
mat_scale_u	First scale matrix
mat_scale_v	Second scale matrix
u_prec	If TRUE, use mat_scale_u as its inverse.

**Details**

Consider  $n \times k$  matrix  $Y_1, \dots, Y_n \sim MN(M, U, V)$  where  $M$  is  $n \times k$ ,  $U$  is  $n \times n$ , and  $V$  is  $k \times k$ .

1. Lower triangular Cholesky decomposition:  $U = PP^T$  and  $V = LL^T$
2. Standard normal generation:  $s \times m$  matrix  $Z_i = [z_{ij} \sim N(0, 1)]$  in row-wise direction.
3.  $Y_i = M + PZ_iL^T$

This function only generates one matrix, i.e.  $Y_1$ .

**Value**

One  $n \times k$  matrix following MN distribution.

---

sim\_mncoef

*Generate Minnesota BVAR Parameters*

---

**Description**

This function generates parameters of BVAR with Minnesota prior.

**Usage**

```
sim_mncoef(p, bayes_spec = set_bvar(), full = TRUE)
```

**Arguments**

p	VAR lag
bayes_spec	A BVAR model specification by <a href="#">set_bvar()</a> .
full	Generate variance matrix from IW (default: TRUE) or not (FALSE)?

**Details**

Implementing dummy observation constructions, Bańbura et al. (2010) sets Normal-IW prior.

$$A \mid \Sigma_e \sim MN(A_0, \Omega_0, \Sigma_e)$$

$$\Sigma_e \sim IW(S_0, \alpha_0)$$

If `full = FALSE`, the result of  $\Sigma_e$  is the same as input (`diag(sigma)`).

**Value**

List with the following component.

**coefficients** BVAR coefficient (MN)

**covmat** BVAR variance (IW or diagonal matrix of sigma of bayes\_spec)

**References**

Bañbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. *Journal of Applied Econometrics*, 25(1).

Karlsson, S. (2013). *Chapter 15 Forecasting with Bayesian Vector Autoregression*. *Handbook of Economic Forecasting*, 2, 791-897.

Litterman, R. B. (1986). *Forecasting with Bayesian Vector Autoregressions: Five Years of Experience*. *Journal of Business & Economic Statistics*, 4(1), 25.

**See Also**

- `set_bvar()` to specify the hyperparameters of Minnesota prior.

**Examples**

```
# Generate (A, Sigma)
# BVAR(p = 2)
# sigma: 1, 1, 1
# lambda: .1
# delta: .1, .1, .1
# epsilon: 1e-04
set.seed(1)
sim_mncoef(
  p = 2,
  bayes_spec = set_bvar(
    sigma = rep(1, 3),
    lambda = .1,
    delta = rep(.1, 3),
    eps = 1e-04
  ),
  full = TRUE
)
```

---

 sim\_mniw

*Generate Normal-IW Random Family*


---

**Description**

This function samples normal inverse-wishart matrices.

**Usage**

```
sim_mniw(num_sim, mat_mean, mat_scale_u, mat_scale, shape, u_prec = FALSE)
```

**Arguments**

num_sim	Number to generate
mat_mean	Mean matrix of MN
mat_scale_u	First scale matrix of MN
mat_scale	Scale matrix of IW
shape	Shape of IW
u_prec	If TRUE, use mat_scale_u as its inverse. By default, FALSE.

**Details**

Consider  $(Y_i, \Sigma_i) \sim MIW(M, U, \Psi, \nu)$ .

1. Generate upper triangular factor of  $\Sigma_i = C_i C_i^T$  in the upper triangular Bartlett decomposition.
2. Standard normal generation:  $n \times k$  matrix  $Z_i = [z_{ij} \sim N(0, 1)]$  in row-wise direction.
3. Lower triangular Cholesky decomposition:  $U = P P^T$
4.  $A_i = M + P Z_i C_i^T$

---

 sim\_mnormal

*Generate Multivariate Normal Random Vector*


---

**Description**

This function samples  $n \times$  multi-dimensional normal random matrix.

**Usage**

```
sim_mnormal(
  num_sim,
  mu = rep(0, 5),
  sig = diag(5),
  method = c("eigen", "chol")
)
```

**Arguments**

num_sim	Number to generate process
mu	Mean vector
sig	Variance matrix
method	Method to compute $\Sigma^{1/2}$ . Choose between eigen (spectral decomposition) and chol (cholesky decomposition). By default, eigen.

**Details**

Consider  $x_1, \dots, x_n \sim N_m(\mu, \Sigma)$ .

1. Lower triangular Cholesky decomposition:  $\Sigma = LL^T$
2. Standard normal generation:  $Z_{i1}, Z_{in} \stackrel{iid}{\sim} N(0, 1)$
3.  $Z_i = (Z_{i1}, \dots, Z_{in})^T$
4.  $X_i = LZ_i + \mu$

**Value**

T x k matrix

---

sim_mnvhar_coef	<i>Generate Minnesota BVAR Parameters</i>
-----------------	---

---

**Description**

This function generates parameters of BVAR with Minnesota prior.

**Usage**

```
sim_mnvhar_coef(bayes_spec = set_bvhar(), full = TRUE)
```

**Arguments**

**bayes\_spec** A BVHAR model specification by `set_bvhar()` (default) or `set_weight_bvhar()`.  
**full** Generate variance matrix from IW (default: TRUE) or not (FALSE)?

**Details**

Normal-IW family for vector HAR model:

$$\Phi \mid \Sigma_e \sim MN(M_0, \Omega_0, \Sigma_e)$$

$$\Sigma_e \sim IW(\Psi_0, \nu_0)$$

**Value**

List with the following component.

**coefficients** BVHAR coefficient (MN)

**covmat** BVHAR variance (IW or diagonal matrix of sigma of bayes\_spec)

**References**

Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. Journal of Statistical Computation and Simulation, 94(6), 1139-1157.

**See Also**

- `set_bvhar()` to specify the hyperparameters of VAR-type Minnesota prior.
- `set_weight_bvhar()` to specify the hyperparameters of HAR-type Minnesota prior.

**Examples**

```
# Generate (Phi, Sigma)
# BVHAR-S
# sigma: 1, 1, 1
# lambda: .1
# delta: .1, .1, .1
# epsilon: 1e-04
set.seed(1)
sim_mnvhar_coef(
  bayes_spec = set_bvhar(
    sigma = rep(1, 3),
    lambda = .1,
    delta = rep(.1, 3),
    eps = 1e-04
  ),
  full = TRUE
)
```

---

 sim\_mvt

---

*Generate Multivariate t Random Vector*


---

**Description**

This function samples  $n \times k$  multi-dimensional t-random matrix.

**Usage**

```
sim_mvt(num_sim, df, mu, sig, method = c("eigen", "chol"))
```

**Arguments**

num_sim	Number to generate process.
df	Degrees of freedom.
mu	Location vector
sig	Scale matrix.
method	Method to compute $\Sigma^{1/2}$ . Choose between eigen (spectral decomposition) and chol (cholesky decomposition). By default, eigen.

**Value**

T x k matrix

---

sim_ssvs_var	<i>Generate SSVS Parameters</i>
--------------	---------------------------------

---

### Description

**[Deprecated]** This function generates parameters of VAR with SSVS prior.

### Usage

```
sim_ssvs_var(
  bayes_spec,
  p,
  dim_data = NULL,
  include_mean = TRUE,
  minnesota = FALSE,
  mn_prob = 1,
  method = c("eigen", "chol")
)

sim_ssvs_vhar(
  bayes_spec,
  har = c(5, 22),
  dim_data = NULL,
  include_mean = TRUE,
  minnesota = c("no", "short", "longrun"),
  mn_prob = 1,
  method = c("eigen", "chol")
)
```

### Arguments

bayes_spec	A SSVS model specification by <a href="#">set_ssvs()</a> .
p	VAR lag
dim_data	Specify the dimension of the data if hyperparameters of bayes_spec have constant values.
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Only use off-diagonal terms of each coefficient matrices for restriction. In <code>sim_ssvs_var()</code> function, use TRUE or FALSE (default). In <code>sim_ssvs_vhar()</code> function, no (default), short type, or longrun type.
mn_prob	Probability for own-lags.
method	Method to compute $\Sigma^{1/2}$ .
har	Numeric vector for weekly and monthly order. By default, <code>c(5, 22)</code> .

### Value

List including coefficients.

**VAR(p) with SSVS prior**

Let  $\alpha$  be the vectorized coefficient of VAR(p).

$$(\alpha \mid \gamma)$$

$$(\gamma_i)$$

$$(\eta_j \mid \omega_j)$$

$$(\omega_{ij})$$

$$(\psi_{ii}^2)$$

**VHAR with SSVS prior**

Let  $\phi$  be the vectorized coefficient of VHAR.

$$(\phi \mid \gamma)$$

$$(\gamma_i)$$

$$(\eta_j \mid \omega_j)$$

$$(\omega_{ij})$$

$$(\psi_{ii}^2)$$

**References**

- George, E. I., & McCulloch, R. E. (1993). *Variable Selection via Gibbs Sampling*. Journal of the American Statistical Association, 88(423), 881-889.
- George, E. I., Sun, D., & Ni, S. (2008). *Bayesian stochastic search for VAR model restrictions*. Journal of Econometrics, 142(1), 553-580.
- Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. Journal of the American Statistical Association, 114(526).
- Koop, G., & Korobilis, D. (2009). *Bayesian Multivariate Time Series Methods for Empirical Macroeconomics*. Foundations and Trends® in Econometrics, 3(4), 267-358.

---

sim_var	<i>Generate Multivariate Time Series Process Following VAR(p)</i>
---------	---

---

### Description

This function generates multivariate time series dataset that follows VAR(p).

### Usage

```
sim_var(
  num_sim,
  num_burn,
  var_coef,
  var_lag,
  sig_error = diag(ncol(var_coef)),
  init = matrix(0L, nrow = var_lag, ncol = ncol(var_coef)),
  method = c("eigen", "chol"),
  process = c("gaussian", "student"),
  t_param = 5
)
```

### Arguments

num_sim	Number to generated process
num_burn	Number of burn-in
var_coef	VAR coefficient. The format should be the same as the output of <code>coef()</code> from <code>var_lm()</code>
var_lag	Lag of VAR
sig_error	Variance matrix of the error term. By default, <code>diag(dim)</code> .
init	Initial $y_1, \dots, y_p$ matrix to simulate VAR model. Try <code>matrix(0L, nrow = var_lag, ncol = dim)</code> .
method	Method to compute $\Sigma^{1/2}$ . Choose between <code>eigen</code> (spectral decomposition) and <code>chol</code> (cholesky decomposition). By default, <code>eigen</code> .
process	Process to generate error term. <code>gaussian</code> : Normal distribution (default) or <code>student</code> : Multivariate t-distribution.
t_param	<b>[Experimental]</b> argument for MVT, e.g. DF: 5.

### Details

1. Generate  $\epsilon_1, \epsilon_n \sim N(0, \Sigma)$
2. For  $i = 1, \dots, n$ ,

$$y_{p+i} = (y_{p+i-1}^T, \dots, y_i^T, 1)^T B + \epsilon_i$$

3. Then the output is  $(y_{p+1}, \dots, y_{n+p})^T$

Initial values might be set to be zero vector or  $(I_m - A_1 - \dots - A_p)^{-1}c$ .

**Value**

T x k matrix

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

 sim\_vhar

---

*Generate Multivariate Time Series Process Following VAR(p)*


---

**Description**

This function generates multivariate time series dataset that follows VAR(p).

**Usage**

```
sim_vhar(
  num_sim,
  num_burn,
  vhar_coef,
  week = 5L,
  month = 22L,
  sig_error = diag(ncol(vhar_coef)),
  init = matrix(0L, nrow = month, ncol = ncol(vhar_coef)),
  method = c("eigen", "chol"),
  process = c("gaussian", "student"),
  t_param = 5
)
```

**Arguments**

num_sim	Number to generated process
num_burn	Number of burn-in
vhar_coef	VAR coefficient. The format should be the same as the output of <code>coef()</code> from <code>var_lm()</code>
week	Weekly order of VHAR. By default, 5.
month	Weekly order of VHAR. By default, 22.
sig_error	Variance matrix of the error term. By default, <code>diag(dim)</code> .
init	Initial $y_1, \dots, y_p$ matrix to simulate VAR model. Try <code>matrix(0L, nrow = month, ncol = dim)</code> .
method	Method to compute $\Sigma^{1/2}$ . Choose between <code>eigen</code> (spectral decomposition) and <code>chol</code> (cholesky decomposition). By default, <code>eigen</code> .
process	Process to generate error term. <code>gaussian</code> : Normal distribution (default) or <code>student</code> : Multivariate t-distribution.
t_param	<b>[Experimental]</b> argument for MVT, e.g. DF: 5.

**Details**

Let  $M$  be the month order, e.g.  $M = 22$ .

1. Generate  $\epsilon_1, \epsilon_n \sim N(0, \Sigma)$

2. For  $i = 1, \dots, n$ ,

$$y_{M+i} = (y_{M+i-1}^T, \dots, y_i^T, 1)^T C_{HAR}^T \Phi + \epsilon_i$$

3. Then the output is  $(y_{M+1}, \dots, y_{n+M})^T$

4. For  $i = 1, \dots, n$ ,

$$y_{p+i} = (y_{p+i-1}^T, \dots, y_i^T, 1)^T B + \epsilon_i$$

5. Then the output is  $(y_{p+1}, \dots, y_{n+p})^T$

Initial values might be set to be zero vector or  $(I_m - A_1 - \dots - A_p)^{-1}c$ .

**Value**

T x k matrix

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

spillover

*h-step ahead Normalized Spillover*

---

**Description**

This function gives connectedness table with h-step ahead normalized spillover index (a.k.a. variance shares).

**Usage**

```
spillover(object, n_ahead = 10L, ...)

## S3 method for class 'bvharspillover'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharspillover'
knit_print(x, ...)

## S3 method for class 'olsmod'
spillover(object, n_ahead = 10L, ...)

## S3 method for class 'normaliw'
spillover(
  object,
  n_ahead = 10L,
```

```

    num_iter = 5000L,
    num_burn = floor(num_iter/2),
    thinning = 1L,
    ...
)

## S3 method for class 'bvarldlt'
spillover(object, n_ahead = 10L, sparse = FALSE, ...)

## S3 method for class 'bvharldlt'
spillover(object, n_ahead = 10L, sparse = FALSE, ...)

```

### Arguments

object	Model object
n_ahead	step to forecast. By default, 10.
...	not used
x	bvharspillover object
digits	digit option to print
num_iter	Number to sample MNIW distribution
num_burn	Number of burn-in
thinning	Thinning every thinning-th iteration
sparse	<b>[Experimental]</b> Apply restriction. By default, FALSE.

### References

Diebold, F. X., & Yilmaz, K. (2012). *Better to give than to receive: Predictive directional measurement of volatility spillovers*. *International Journal of forecasting*, 28(1), 57-66.

---

spne

*Evaluate the Estimation Based on Spectral Norm Error*

---

### Description

This function computes estimation error given estimated model and true coefficient.

### Usage

```

spne(x, y, ...)

## S3 method for class 'bvharssp'
spne(x, y, ...)

```

**Arguments**

x	Estimated model.
y	Coefficient matrix to be compared.
...	not used

**Details**

Let  $\|\cdot\|_2$  be the spectral norm of a matrix, let  $\hat{\Phi}$  be the estimates, and let  $\Phi$  be the true coefficients matrix. Then the function computes estimation error by

$$\|\hat{\Phi} - \Phi\|_2$$

**Value**

Spectral norm value

**References**

Ghosh, S., Khare, K., & Michailidis, G. (2018). *High-Dimensional Posterior Consistency in Bayesian Vector Autoregressive Models*. *Journal of the American Statistical Association*, 114(526).

---

stableroot	<i>Roots of characteristic polynomial</i>
------------	---

---

**Description**

Compute the character polynomial of coefficient matrix.

**Usage**

```

stableroot(x, ...)

## S3 method for class 'varlse'
stableroot(x, ...)

## S3 method for class 'vharlse'
stableroot(x, ...)

## S3 method for class 'bvarmn'
stableroot(x, ...)

## S3 method for class 'bvarflat'
stableroot(x, ...)

## S3 method for class 'bvharmn'
stableroot(x, ...)

```

**Arguments**

x	Model fit
...	not used

**Details**

To know whether the process is stable or not, make characteristic polynomial.

$$\det(I_m - Az) = 0$$

where  $A$  is VAR(1) coefficient matrix representation.

**Value**

Numeric vector.

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

summary.normaliw

*Summarizing Bayesian Multivariate Time Series Model*


---

**Description**

summary method for normaliw class.

**Usage**

```
## S3 method for class 'normaliw'
summary(
  object,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  verbose = FALSE,
  num_thread = 1,
  ...
)

## S3 method for class 'summary.normaliw'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'summary.normaliw'
knit_print(x, ...)
```

**Arguments**

object	A normaliw object
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
...	not used
x	summary.normaliw object
digits	digit option to print

**Details**

From Minnesota prior, set of coefficient matrices and residual covariance matrix have matrix Normal Inverse-Wishart distribution.

BVAR:

$$(A, \Sigma_e) \sim MNIW(\hat{A}, \hat{V}^{-1}, \hat{\Sigma}_e, \alpha_0 + n)$$

where  $\hat{V} = X_*^T X_*$  is the posterior precision of MN.

BVHAR:

$$(\Phi, \Sigma_e) \sim MNIW(\hat{\Phi}, \hat{V}_H^{-1}, \hat{\Sigma}_e, \nu + n)$$

where  $\hat{V}_H = X_+^T X_+$  is the posterior precision of MN.

**Value**

summary.normaliw [class](#) has the following components:

- names** Variable names
- totobs** Total number of the observation
- obs** Sample size used when training = totobs - p
- p** Lag of VAR
- m** Dimension of the data
- call** Matched call
- spec** Model specification (bvhar-spec)
- mn\_mean** MN Mean of posterior distribution (MN-IW)
- mn\_prec** MN Precision of posterior distribution (MN-IW)
- iw\_scale** IW scale of posterior distribution (MN-IW)
- iw\_shape** IW df of posterior distribution (MN-IW)

**iter** Number of MCMC iterations  
**burn** Number of MCMC burn-in  
**thin** MCMC thinning  
**alpha\_record (BVAR) and phi\_record (BVHAR)** MCMC record of coefficients vector  
**psi\_record** MCMC record of upper cholesky factor  
**omega\_record** MCMC record of diagonal of cholesky factor  
**eta\_record** MCMC record of upper part of cholesky factor  
**param** MCMC record of every parameter  
**coefficients** Posterior mean of coefficients  
**covmat** Posterior mean of covariance

## References

Litterman, R. B. (1986). *Forecasting with Bayesian Vector Autoregressions: Five Years of Experience*. Journal of Business & Economic Statistics, 4(1), 25.

Bańbura, M., Giannone, D., & Reichlin, L. (2010). *Large Bayesian vector auto regressions*. Journal of Applied Econometrics, 25(1).

---

summary.varlse

*Summarizing Vector Autoregressive Model*

---

## Description

summary method for varlse class.

## Usage

```
## S3 method for class 'varlse'
summary(object, ...)

## S3 method for class 'summary.varlse'
print(x, digits = max(3L, getOption("digits") - 3L), signif_code = TRUE, ...)

## S3 method for class 'summary.varlse'
knit_print(x, ...)
```

## Arguments

object	A varlse object
...	not used
x	summary.varlse object
digits	digit option to print
signif_code	Check significant rows (Default: TRUE)

**Value**

summary.varlse [class](#) additionally computes the following

names	Variable names
totobs	Total number of the observation
obs	Sample size used when training = totobs - p
p	Lag of VAR
coefficients	Coefficient Matrix
call	Matched call
process	Process: VAR
covmat	Covariance matrix of the residuals
corrmat	Correlation matrix of the residuals
roots	Roots of characteristic polynomials
is_stable	Whether the process is stable or not based on roots
log_lik	log-likelihood
ic	Information criteria vector

- AIC - AIC
- BIC - BIC
- HQ - HQ
- FPE - FPE

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

summary.vharlse	<i>Summarizing Vector HAR Model</i>
-----------------	-------------------------------------

---

**Description**

summary method for vharlse class.

**Usage**

```
## S3 method for class 'vharlse'
summary(object, ...)

## S3 method for class 'summary.vharlse'
print(x, digits = max(3L, getOption("digits") - 3L), signif_code = TRUE, ...)

## S3 method for class 'summary.vharlse'
knit_print(x, ...)
```

**Arguments**

object	A vharlse object
...	not used
x	summary.vharlse object
digits	digit option to print
signif_code	Check significant rows (Default: TRUE)

**Value**

summary.vharlse [class](#) additionally computes the following

names	Variable names
totobs	Total number of the observation
obs	Sample size used when training = totobs - p
p	3
week	Order for weekly term
month	Order for monthly term
coefficients	Coefficient Matrix
call	Matched call
process	Process: VAR
covmat	Covariance matrix of the residuals
corrmat	Correlation matrix of the residuals
roots	Roots of characteristic polynomials
is_stable	Whether the process is stable or not based on roots
log_lik	log-likelihood
ic	Information criteria vector

- AIC - AIC
- BIC - BIC
- HQ - HQ
- FPE - FPE

**References**

- Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.
- Corsi, F. (2008). *A Simple Approximate Long-Memory Model of Realized Volatility*. *Journal of Financial Econometrics*, 7(2), 174-196.
- Baek, C. and Park, M. (2021). *Sparse vector heterogeneous autoregressive modeling for realized volatility*. *J. Korean Stat. Soc.* 50, 495-510.

---

VARtoVMA	<i>Convert VAR to VMA(infinite)</i>
----------	-------------------------------------

---

**Description**

Convert VAR process to infinite vector MA process

**Usage**

VARtoVMA(object, lag\_max)

**Arguments**

object	A var1se object
lag_max	Maximum lag for VMA

**Details**

Let VAR(p) be stable.

$$Y_t = c + \sum_{j=0} W_j Z_{t-j}$$

For VAR coefficient  $B_1, B_2, \dots, B_p$ ,

$$I = (W_0 + W_1L + W_2L^2 + \dots +)(I - B_1L - B_2L^2 - \dots - B_pL^p)$$

Recursively,

$$W_0 = I$$

$$W_1 = W_0B_1(W_1^T = B_1^TW_0^T)$$

$$W_2 = W_1B_1 + W_0B_2(W_2^T = B_1^TW_1^T + B_2^TW_0^T)$$

$$W_j = \sum_{j=1}^k W_{k-j}B_j(W_j^T = \sum_{j=1}^k B_j^TW_{k-j}^T)$$

**Value**

VMA coefficient of  $k(\text{lag-max} + 1) \times k$  dimension

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

var\_bayes

*Fitting Bayesian VAR with Coefficient and Covariance Prior***Description**

**[Maturing]** This function fits BVAR. Covariance term can be homoskedastic or heteroskedastic (stochastic volatility). It can have Minnesota, SSVS, and Horseshoe prior.

**Usage**

```
var_bayes(
  y,
  p,
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvar(),
  cov_spec = set_ldlt(),
  intercept = set_intercept(),
  include_mean = TRUE,
  minnesota = TRUE,
  save_init = FALSE,
  convergence = NULL,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvarldlt'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvarldlt'
knit_print(x, ...)
```

**Arguments**

y	Time series data of which columns indicate the variables
p	VAR lag
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A BVAR model specification by <a href="#">set_bvar()</a> , <a href="#">set_ssvs()</a> , or <a href="#">set_horseshoe()</a> .
cov_spec	<b>[Experimental]</b> SV specification by <a href="#">set_sv()</a> .
intercept	<b>[Experimental]</b> Prior for the constant term by <a href="#">set_intercept()</a> .

include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). By default, TRUE.
save_init	Save every record starting from the initial values (TRUE). By default, exclude the initial values in the record (FALSE), even when num_burn = 0 and thinning = 1. If num_burn > 0 or thinning != 1, this option is ignored.
convergence	Convergence threshold for rhat < convergence. By default, NULL which means no warning.
verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvarldlt object
digits	digit option to print
...	not used

### Details

Cholesky stochastic volatility modeling for VAR based on

$$\Sigma_t^{-1} = L^T D_t^{-1} L$$

, and implements corrected triangular algorithm for Gibbs sampler.

### Value

var\_bayes() returns an object named bvarsv [class](#).

**coefficients** Posterior mean of coefficients.

**chol\_posterior** Posterior mean of contemporaneous effects.

**param** Every set of MCMC trace.

**param\_names** Name of every parameter.

**group** Indicators for group.

**num\_group** Number of groups.

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**p** VAR lag

**m** Dimension of the data

**obs** Sample size used when training = totobs - p

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. VHAR\_SSVS\_SV, VHAR\_Horseshoe\_SV, or VHAR\_minnesota-part\_SV

**type** include constant term (const) or not (none)

**spec** Coefficients prior specification

**sv** log volatility prior specification

**intercept** Intercept prior specification

**init** Initial values  
**chain** The numer of chains  
**iter** Total iterations  
**burn** Burn-in  
**thin** Thinning  
**y0**  $Y_0$   
**design**  $X_0$   
**y** Raw input

If it is SSVS or Horseshoe:

**pip** Posterior inclusion probabilities.

## References

- Carriero, A., Chan, J., Clark, T. E., & Marcellino, M. (2022). *Corrigendum to “Large Bayesian vector autoregressions with stochastic volatility and non-conjugate priors” [J. Econometrics 212 (1)(2019) 137-154]*. *Journal of Econometrics*, 227(2), 506-512.
- Chan, J., Koop, G., Poirier, D., & Tobias, J. (2019). *Bayesian Econometric Methods (2nd ed., Econometric Exercises)*. Cambridge: Cambridge University Press.
- Cogley, T., & Sargent, T. J. (2005). *Drifts and volatilities: monetary policies and outcomes in the post WWII US*. *Review of Economic Dynamics*, 8(2), 262-302.
- Gruber, L., & Kastner, G. (2022). *Forecasting macroeconomic data with Bayesian VARs: Sparse or dense? It depends! arXiv*.
- Huber, F., Koop, G., & Onorante, L. (2021). *Inducing Sparsity and Shrinkage in Time-Varying Parameter Models*. *Journal of Business & Economic Statistics*, 39(3), 669-683.
- Korobilis, D., & Shimizu, K. (2022). *Bayesian Approaches to Shrinkage and Sparse Estimation*. *Foundations and Trends® in Econometrics*, 11(4), 230-354.
- Ray, P., & Bhattacharya, A. (2018). *Signal Adaptive Variable Selector for the Horseshoe Prior*. arXiv.

---

var\_lm

*Fitting Vector Autoregressive Model of Order p Model*

---

## Description

This function fits VAR(p) using OLS method.

**Usage**

```

var_lm(y, p = 1, include_mean = TRUE, method = c("nor", "chol", "qr"))

## S3 method for class 'varlse'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'varlse'
logLik(object, ...)

## S3 method for class 'varlse'
AIC(object, ...)

## S3 method for class 'varlse'
BIC(object, ...)

is.varlse(x)

is.bvharmon(x)

## S3 method for class 'varlse'
knit_print(x, ...)

```

**Arguments**

y	Time series data of which columns indicate the variables
p	Lag of VAR (Default: 1)
include_mean	Add constant term (Default: TRUE) or not (FALSE)
method	Method to solve linear equation system. (nor: normal equation (default), chol: Cholesky, and qr: HouseholderQR)
x	A varlse object
digits	digit option to print
...	not used
object	A varlse object

**Details**

This package specifies VAR(p) model as

$$Y_t = A_1 Y_{t-1} + \dots + A_p Y_{t-p} + c + \epsilon_t$$

If include\_type = TRUE, there is constant term. The function estimates every coefficient matrix.

Consider the response matrix  $Y_0$ . Let  $T$  be the total number of sample, let  $m$  be the dimension of the time series, let  $p$  be the order of the model, and let  $n = T - p$ . Likelihood of VAR(p) has

$$Y_0 | B, \Sigma_e \sim MN(X_0 B, I_s, \Sigma_e)$$

where  $X_0$  is the design matrix, and MN is **matrix normal distribution**.

Then log-likelihood of vector autoregressive model family is specified by

$$\log p(Y_0 | B, \Sigma_e) = -\frac{nm}{2} \log 2\pi - \frac{n}{2} \log \det \Sigma_e - \frac{1}{2} \text{tr}((Y_0 - X_0 B) \Sigma_e^{-1} (Y_0 - X_0 B)^T)$$

In addition, recall that the OLS estimator for the matrix coefficient matrix is the same as MLE under the Gaussian assumption. MLE for  $\Sigma_e$  has different denominator,  $n$ .

$$\begin{aligned} \hat{B} &= \hat{B}^{LS} = \hat{B}^{ML} = (X_0^T X_0)^{-1} X_0^T Y_0 \\ \hat{\Sigma}_e &= \frac{1}{s-k} (Y_0 - X_0 \hat{B})^T (Y_0 - X_0 \hat{B}) \\ \tilde{\Sigma}_e &= \frac{1}{s} (Y_0 - X_0 \hat{B})^T (Y_0 - X_0 \hat{B}) = \frac{s-k}{s} \hat{\Sigma}_e \end{aligned}$$

Let  $\tilde{\Sigma}_e$  be the MLE and let  $\hat{\Sigma}_e$  be the unbiased estimator (covmat) for  $\Sigma_e$ . Note that

$$\tilde{\Sigma}_e = \frac{n-k}{n} \hat{\Sigma}_e$$

Then

$$AIC(p) = \log \det \Sigma_e + \frac{2}{n} (\text{number of freely estimated parameters})$$

where the number of freely estimated parameters is  $mk$ , i.e.  $pm^2$  or  $pm^2 + m$ .

Let  $\tilde{\Sigma}_e$  be the MLE and let  $\hat{\Sigma}_e$  be the unbiased estimator (covmat) for  $\Sigma_e$ . Note that

$$\tilde{\Sigma}_e = \frac{n-k}{T} \hat{\Sigma}_e$$

Then

$$BIC(p) = \log \det \Sigma_e + \frac{\log n}{n} (\text{number of freely estimated parameters})$$

where the number of freely estimated parameters is  $pm^2$ .

## Value

`var_lm()` returns an object named `varlse` [class](#). It is a list with the following components:

- coefficients** Coefficient Matrix
- fitted.values** Fitted response values
- residuals** Residuals
- covmat** LS estimate for covariance matrix
- df** Numer of Coefficients

**p** Lag of VAR  
**m** Dimension of the data  
**obs** Sample size used when training = totobs - p  
**totobs** Total number of the observation  
**call** Matched call  
**process** Process: VAR  
**type** include constant term (const) or not (none)  
**design** Design matrix  
**y** Raw input  
**y0** Multivariate response matrix  
**method** Solving method  
**call** Matched call

It is also a bvharmod class.

## References

- Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.
- Akaike, H. (1969). *Fitting autoregressive models for prediction*. Ann Inst Stat Math 21, 243-247.
- Akaike, H. (1971). *Autoregressive model fitting for control*. Ann Inst Stat Math 23, 163-180.
- Akaike H. (1974). *A new look at the statistical model identification*. IEEE Transactions on Automatic Control, vol. 19, no. 6, pp. 716-723.
- Akaike H. (1998). *Information Theory and an Extension of the Maximum Likelihood Principle*. In: Parzen E., Tanabe K., Kitagawa G. (eds) Selected Papers of Hirotugu Akaike. Springer Series in Statistics (Perspectives in Statistics). Springer, New York, NY.
- Gideon Schwarz. (1978). *Estimating the Dimension of a Model*. Ann. Statist. 6 (2) 461 - 464.

## See Also

- [summary.varlse\(\)](#) to summarize VAR model

## Examples

```
# Perform the function using etf_vix dataset
fit <- var_lm(y = etf_vix, p = 2)
class(fit)
str(fit)

# Extract coef, fitted values, and residuals
coef(fit)
head(residuals(fit))
head(fitted(fit))
```

---

VHARtoVMA	<i>Convert VHAR to VMA(infinite)</i>
-----------	--------------------------------------

---

**Description**

Convert VHAR process to infinite vector MA process

**Usage**

VHARtoVMA(object, lag\_max)

**Arguments**

object	A vharlse object
lag_max	Maximum lag for VMA

**Details**

Let VAR(p) be stable and let VAR(p) be  $Y_0 = X_0 B + Z$

VHAR is VAR(22) with

$$Y_0 = X_1 B + Z = ((X_0 \tilde{T}^T)) \Phi + Z$$

Observe that

$$B = \tilde{T}^T \Phi$$

**Value**

VMA coefficient of  $k(\text{lag-max} + 1) \times k$  dimension

**References**

Lütkepohl, H. (2007). *New Introduction to Multiple Time Series Analysis*. Springer Publishing.

---

vhar_bayes	<i>Fitting Bayesian VHAR with Coefficient and Covariance Prior</i>
------------	--

---

**Description**

**[Maturing]** This function fits BVHAR. Covariance term can be homoskedastic or heteroskedastic (stochastic volatility). It can have Minnesota, SSVS, and Horseshoe prior.

**Usage**

```
vhar_bayes(
  y,
  har = c(5, 22),
  num_chains = 1,
  num_iter = 1000,
  num_burn = floor(num_iter/2),
  thinning = 1,
  bayes_spec = set_bvhar(),
  cov_spec = set_ldlt(),
  intercept = set_intercept(),
  include_mean = TRUE,
  minnesota = c("longrun", "short", "no"),
  save_init = FALSE,
  convergence = NULL,
  verbose = FALSE,
  num_thread = 1
)

## S3 method for class 'bvharldlt'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'bvharldlt'
knit_print(x, ...)
```

**Arguments**

y	Time series data of which columns indicate the variables
har	Numeric vector for weekly and monthly order. By default, c(5, 22).
num_chains	Number of MCMC chains
num_iter	MCMC iteration number
num_burn	Number of burn-in (warm-up). Half of the iteration is the default choice.
thinning	Thinning every thinning-th iteration
bayes_spec	A BVHAR model specification by <a href="#">set_bvhar()</a> (default) <a href="#">set_weight_bvhar()</a> , <a href="#">set_ssvs()</a> , or <a href="#">set_horseshoe()</a> .
cov_spec	<b>[Experimental]</b> SV specification by <a href="#">set_sv()</a> .
intercept	<b>[Experimental]</b> Prior for the constant term by <a href="#">set_intercept()</a> .
include_mean	Add constant term (Default: TRUE) or not (FALSE)
minnesota	Apply cross-variable shrinkage structure (Minnesota-way). Two type: short type and longrun (default) type. You can also set no.
save_init	Save every record starting from the initial values (TRUE). By default, exclude the initial values in the record (FALSE), even when num_burn = 0 and thinning = 1. If num_burn > 0 or thinning != 1, this option is ignored.
convergence	Convergence threshold for $\hat{r} < \text{convergence}$ . By default, NULL which means no warning.

verbose	Print the progress bar in the console. By default, FALSE.
num_thread	Number of threads
x	bvhar1d1t object
digits	digit option to print
...	not used

### Details

Cholesky stochastic volatility modeling for VHAR based on

$$\Sigma_t^{-1} = L^T D_t^{-1} L$$

### Value

vhar\_bayes() returns an object named bvhar1d1t [class](#). It is a list with the following components:

**coefficients** Posterior mean of coefficients.

**chol\_posterior** Posterior mean of contemporaneous effects.

**param** Every set of MCMC trace.

**param\_names** Name of every parameter.

**group** Indicators for group.

**num\_group** Number of groups.

**df** Numer of Coefficients:  $3m + 1$  or  $3m$

**p** 3 (The number of terms. It contains this element for usage in other functions.)

**week** Order for weekly term

**month** Order for monthly term

**m** Dimension of the data

**obs** Sample size used when training = totobs - p

**totobs** Total number of the observation

**call** Matched call

**process** Description of the model, e.g. VHAR\_SSVS\_SV, VHAR\_Horseshoe\_SV, or VHAR\_minnesota-part\_SV

**type** include constant term (const) or not (none)

**spec** Coefficients prior specification

**sv** log volatility prior specification

**init** Initial values

**intercept** Intercept prior specification

**chain** The numer of chains

**iter** Total iterations

**burn** Burn-in

**thin** Thinning

**HARtrans** VHAR linear transformation matrix

**y0**  $Y_0$

**design**  $X_0$

**y** Raw input

If it is SSVS or Horseshoe:

**pip** Posterior inclusion probabilities.

## References

Kim, Y. G., and Baek, C. (2024). *Bayesian vector heterogeneous autoregressive modeling*. *Journal of Statistical Computation and Simulation*, 94(6), 1139-1157.

Kim, Y. G., and Baek, C. (n.d.). Working paper.

---

vhar\_lm

*Fitting Vector Heterogeneous Autoregressive Model*


---

## Description

This function fits VHAR using OLS method.

## Usage

```
vhar_lm(
  y,
  har = c(5, 22),
  include_mean = TRUE,
  method = c("nor", "chol", "qr")
)

## S3 method for class 'vharlse'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

## S3 method for class 'vharlse'
logLik(object, ...)

## S3 method for class 'vharlse'
AIC(object, ...)

## S3 method for class 'vharlse'
BIC(object, ...)

is.vharlse(x)

## S3 method for class 'vharlse'
knit_print(x, ...)
```

**Arguments**

<code>y</code>	Time series data of which columns indicate the variables
<code>har</code>	Numeric vector for weekly and monthly order. By default, <code>c(5, 22)</code> .
<code>include_mean</code>	Add constant term (Default: TRUE) or not (FALSE)
<code>method</code>	Method to solve linear equation system. ( <code>nor</code> : normal equation (default), <code>chol</code> : Cholesky, and <code>qr</code> : HouseholderQR)
<code>x</code>	A <code>vharlse</code> object
<code>digits</code>	digit option to print
<code>...</code>	not used
<code>object</code>	A <code>vharlse</code> object

**Details**

For VHAR model

$$Y_t = \Phi^{(d)} Y_{t-1} + \Phi^{(w)} Y_{t-1}^{(w)} + \Phi^{(m)} Y_{t-1}^{(m)} + \epsilon_t$$

the function gives basic values.

**Value**

`vhar_lm()` returns an object named `vharlse` class. It is a list with the following components:

<b>coefficients</b>	Coefficient Matrix
<b>fitted.values</b>	Fitted response values
<b>residuals</b>	Residuals
<b>covmat</b>	LS estimate for covariance matrix
<b>df</b>	Numer of Coefficients
<b>m</b>	Dimension of the data
<b>obs</b>	Sample size used when training = <code>totobs - month</code>
<b>y0</b>	Multivariate response matrix
<b>p</b>	3 (The number of terms. <code>vharlse</code> contains this element for usage in other functions.)
<b>week</b>	Order for weekly term
<b>month</b>	Order for monthly term
<b>totobs</b>	Total number of the observation
<b>process</b>	Process: VHAR
<b>type</b>	include constant term ( <code>const</code> ) or not ( <code>none</code> )
<b>HARtrans</b>	VHAR linear transformation matrix
<b>design</b>	Design matrix of VAR( <code>month</code> )
<b>y</b>	Raw input
<b>method</b>	Solving method
<b>call</b>	Matched call

It is also a `bvharmod` class.

## References

- Baek, C. and Park, M. (2021). *Sparse vector heterogeneous autoregressive modeling for realized volatility*. J. Korean Stat. Soc. 50, 495-510.
- Bubák, V., Kočenda, E., & Žikeš, F. (2011). *Volatility transmission in emerging European foreign exchange markets*. Journal of Banking & Finance, 35(11), 2829-2841.
- Corsi, F. (2008). *A Simple Approximate Long-Memory Model of Realized Volatility*. Journal of Financial Econometrics, 7(2), 174-196.

## See Also

- `coef.vharlse()`, `residuals.vharlse()`, and `fitted.vharlse()`
- `summary.vharlse()` to summarize VHAR model

## Examples

```
# Perform the function using etf_vix dataset
fit <- vhar_lm(y = etf_vix)
class(fit)
str(fit)

# Extract coef, fitted values, and residuals
coef(fit)
head(residuals(fit))
head(fitted(fit))
```

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