

# Package ‘RQEntangle’

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**Type** Package

**Title** Quantum Entanglement of Bipartite System

**Version** 0.1.3

## Description

It computes the Schmidt decomposition of bipartite quantum systems, discrete or continuous, and their respective entanglement metrics. See Artur Ekert, Peter L. Knight (1995) <[doi:10.1119/1.17904](https://doi.org/10.1119/1.17904)> for more details.

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**Encoding** UTF-8

**LazyData** true

**Depends** R(>= 2.15.1), itertools(>= 0.1-3), iterators

**Suggests** knitr, rmarkdown, dplyr, ggplot2, roxygen2

**RoxygenNote** 6.1.0

**URL** <https://github.com/stephenhky/RQEntangle>

**BugReports** <https://github.com/stephenhky/RQEntangle/issues>

**VignetteBuilder** knitr

**NeedsCompilation** no

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**Repository** CRAN

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continuous.function.interpolate  
*Interpolate values of functions.*

---

### Description

Interpolate values of functions.

### Usage

continuous.function.interpolate(xarr, yarr, x)

### Arguments

|      |                        |
|------|------------------------|
| xarr | a vector of x (sorted) |
| yarr | a vector of y          |
| x    | given value of x       |

### Value

interpolated value of y

---

continuous.schmidt.decompose  
*Perform a continuous Schmidt decomposition*

---

### Description

Perform a continuous Schmidt decomposition

### Usage

continuous.schmidt.decompose(bifunc, x1lo, x1hi, x2lo, x2hi, nbx1 = 100,  
nbx2 = 100, keep = min(10, nbx1, nbx2))

**Arguments**

|        |  |
|--------|--|
| bifunc | bipartite continuous wavefunction  |
| x1lo   | lower limit of x1  |
| x1hi   | upper limit of x1  |
| x2lo   | lower limit of x2  |
| x2hi   | upper limit of x2  |
| nbx1   | number of discretized x1 (default: 100)                                  |
| nbx2   | number of discretized x2 (default: 100)                                  |
| keep   | number of Schmidt modes to keep (default: minimum of 10, nbx1, and nbx2) |

**Value**

Schmidt modes, including the eigenvalues, and the lambda interpolated function of the Schmidt modes

**Examples**

```
coupled.harm.fcn<- function(x1,x2) exp(-((0.5*(x1+x2))**2))*exp(-(x1-x2)**2)*sqrt(2./pi)
continuous.schmidt.decompose(coupled.harm.fcn, -10, 10, -10, 10)
```

---

discretize.continuous.bipartitefunc

*Making a discretized tensor for a continuous function*

---

**Description**

Making a discretized tensor for a continuous function

**Usage**

```
discretize.continuous.bipartitefunc(bifunc, x1lo, x1hi, x2lo, x2hi,
  nbx1 = 100, nbx2 = 100)
```

**Arguments**

|        |   |
|--------|---|
| bifunc | bipartite continuous wavefunction       |
| x1lo   | lower limit of x1                       |
| x1hi   | upper limit of x1                       |
| x2lo   | lower limit of x2                       |
| x2hi   | upper limit of x2                       |
| nbx1   | number of discretized x1 (default: 100) |
| nbx2   | number of discretized x2 (default: 100) |

**Value**

discretized tensor for Schmidt decomposition

---

entanglement.entropy *Calculate the entanglement entropy given the calculate Schmidt modes.*

---

**Description**

Calculate the entanglement entropy given the calculate Schmidt modes.

**Usage**

```
entanglement.entropy(modes)
```

**Arguments**

modes                Schmidt modes

**Value**

entanglement entropy

**Examples**

```
singlet<- matrix(c(0, sqrt(0.7), sqrt(0.3), 0), byrow = TRUE, nrow = 2)
modes<- schmidt.decompose(singlet)
entanglement.entropy(modes)
```

---

interpolated.continuous.function  
*Lambda function of the interpolated continous function.*

---

**Description**

Lambda function of the interpolated continous function.

**Usage**

```
interpolated.continuous.function(xarr, yarr)
```

**Arguments**

xarr                a vector of x (sorted)  
yarr                a vector of y

**Value**

interpolated lambda function

---

negativity                      *Calculate the negativity given the calculate Schmidt modes.*

---

**Description**

Calculate the negativity given the calculate Schmidt modes.

**Usage**

```
negativity(modes)
```

**Arguments**

modes                      Schmidt modes

**Value**

negativity

**Examples**

```
singlet<- matrix(c(0, sqrt(0.7), sqrt(0.3), 0), byrow = TRUE, nrow = 2)
modes<- schmidt.decompose(singlet)
negativity(modes)
```

---

participation.ratio            *Calculate the participation ratio given the calculate Schmidt modes.*

---

**Description**

Calculate the participation ratio given the calculate Schmidt modes.

**Usage**

```
participation.ratio(modes)
```

**Arguments**

modes                      Schmidt modes

**Value**

participation ratio

**Examples**

```
singlet<- matrix(c(0, sqrt(0.7), sqrt(0.3), 0), byrow = TRUE, nrow = 2)
modes<- schmidt.decompose(singlet)
participation.ratio(modes)
```

---

|                |                                   |
|----------------|-----------------------------------|
| reduced.denmat | <i>Get reduced density matrix</i> |
|----------------|-----------------------------------|

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**Description**

Get reduced density matrix

**Usage**

```
reduced.denmat(bipartite.qubits, keep.dim = 1)
```

**Arguments**

|                  |                                |
|------------------|--------------------------------|
| bipartite.qubits | tensor of bipartite systems    |
| keep.dim         | dimension to keep (default: 1) |

**Value**

reduced density matrix

**Examples**

```
singlet<- matrix(c(0, sqrt(0.7), sqrt(0.3), 0), byrow = TRUE, nrow = 2)
reduced.denmat(singlet)
```

---

|                   |                                      |
|-------------------|--------------------------------------|
| schmidt.decompose | <i>Perform Schmidt decomposition</i> |
|-------------------|--------------------------------------|

---

**Description**

Perform Schmidt decomposition

**Usage**

```
schmidt.decompose(bipartite.qubits)
```

**Arguments**

bipartite.qubits  
tensor of bipartite systems

**Value**

Schmidt modes, including the eigenvalues, and eigenvectors of both subsystems of the modes

**Examples**

```
singlet<- matrix(c(0, sqrt(0.7), sqrt(0.3), 0), byrow = TRUE, nrow = 2)  
schmidt.decompose(singlet)
```

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