

Truthful Mobile Crowdsensing for Strategic Users with Private Qualities

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Abstract—Mobile crowdsensing has found a variety of applications (e.g., spectrum sensing, environmental monitoring) by leveraging the “wisdom” of a potentially large crowd of mobile users. An important metric of a crowdsensing task is data accuracy, which relies on the qualities of the participating users’ data (e.g., users’ received SNRs for measuring a transmitter’s transmit signal strength). However, the quality of a user can be its private information (which, e.g., may depend on the user’s location) that it can manipulate to its own advantage, which can mislead the crowdsensing requester about the knowledge of the data’s accuracy. This issue is exacerbated by the fact that the user can also manipulate its effort made in the crowdsensing task, which is a hidden action that could result in the requester having incorrect knowledge of the data’s accuracy. In this paper, we devise truthful crowdsensing mechanisms for Quality and Effort Elicitation (QEE), which incentivize strategic users to truthfully reveal their private qualities and truthfully make efforts as desired by the requester. The QEE mechanisms achieve the truthful design by overcoming the intricate dependency of a user’s data on its private quality and hidden effort. Under the QEE mechanisms, we show that the crowdsensing requester’s optimal (CO) effort assignment assigns effort only to the best user that has the smallest “virtual valuation”, which depends on the user’s quality and the quality’s distribution. We also show that, as the number of users increases, the performance gap between the CO effort assignment and the socially optimal effort assignment decreases, and converges to 0 asymptotically. We further show that while the requester’s payoff and the social welfare attained by the CO effort assignment both increase as the number of users increases, interestingly, the corresponding users’ payoffs can decrease. Simulation results demonstrate the truthfulness of the QEE mechanisms and the system efficiency of the CO effort assignment.

I. INTRODUCTION

Mobile crowdsensing has found a variety of applications, such as spectrum sensing [1], and environmental monitoring (e.g., air quality [2], noise level [3], weather conditions [4] like temperature, humidity, and wind speed). In principle, crowdsensing leverages the “wisdom” of a potentially large crowd of mobile users for a crowdsensing task. The primary advantage of crowdsensing lies in that it exploits the diversity of inherently inaccurate data from many users by aggregating the data sensed by the crowd, such that the data accuracy after

aggregation can be substantially enhanced. With enormous opportunities brought by big data, crowdsensing serves as an important foundation for big data learning tools to harness the power of big data in a wide range of application domains.

To fully exploit the potential of crowdsensing, it is important to assign crowdsensing tasks to users based on the quality of their data. The quality of a user’s data captures the accuracy of the data relative to the actual ground truth of the event of interest, and it generally varies for different users depending on a user’s specific situation (e.g., location, surrounding). For example, if the crowdsensing task is to measure the transmit signal strength of a transmitter, then the SNR received by a user from the transmitter determines the quality of the user’s data, and users generally can receive distinct SNR values depending on their locations. A user can learn the quality of its data by estimation, based on its specific situation or using some history data. For example, a user can estimate the SNR received from a transmitter based on its distance from the transmitter. However, the quality of a user’s data can be its private information, which is unknown to and cannot be verified by the crowdsensing requester. For example, as a user’s received SNR from a transmitter depends on its location which is its private information, the requester cannot verify what is the actual received SNR of that user. As a result, a strategic user may have incentive to manipulate its quality revealed to the requester so as to gain an advantage. For example, a user with a low quality may pretend to have a high quality in the hope of receiving a high reward for contributing high quality data to the task. To the best of our knowledge, this paper is the first to design truthful mechanisms to elicit private qualities from strategic users.

In addition to the quality, the effort exerted by a user in the crowdsensing task also affects the accuracy of the user’s data. A user can improve its data’s accuracy by making a greater effort to complete the task. For example, to measure the signal strength of a transmitter, a user can take the average of more samples of the received signal in order to combat noise. However, a user’s effort can also be its hidden action that cannot be observed by the requester. Due to the inaccurate nature of the data, a strategic user may report some arbitrary data to the requester without making any effort in the task, while the requester is not able to verify how much effort was actually made.

In the presence of strategic users with private qualities and

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The work of X. Gong and N. B. Shroff was supported in part by the US Army grant W911NF-15-0277 and US NSF grant CNS-1421576. The work of X. Gong was also supported in part by the start-up fund by Auburn University.

hidden efforts, our goal is to incentivize users to truthfully reveal their qualities, and make efforts as desired by the crowdsensing requester. Such a truthful mechanism is desirable as it eliminates the possibility of manipulation, which would encourage users to participate in crowdsensing. More importantly, the truthful elicitation of quality and effort ensures that the requester can obtain the correct knowledge of the data's accuracy after aggregating the requested data, which is a critical metric of the crowdsensing task. This is in contrast to the situation of private cost, where manipulating the cost cannot mislead the requester about the data accuracy.

The jointly truthful elicitation of quality and effort calls for new designs that are significantly different from existing mechanisms. First, a user's payoff as a function of its private quality has a structure essentially different from that of its private cost. As a result, existing designs for cost elicitation cannot work for quality elicitation. Second, due to the intricate dependency of a user's data on its private quality and hidden effort, the joint elicitation of quality and effort needs to overcome the intricate coupling between the elicitation of quality and the elicitation of effort.

Given a truthful mechanism that can elicit qualities and efforts from users, an important question for the requester is to determine how much effort to assign to the users based on their qualities, in order to maximize the requester's payoff. This involves the tradeoff between assigning more effort to improve the data's accuracy, and assigning less effort to reduce the reward paid to the users to compensate their costs.

The main contributions of this paper can be summarized as follows.

- We devise truthful crowdsensing mechanisms for Quality and Effort Elicitation (QEE), with general effort assignment functions, which incentivize strategic users to truthfully reveal their private qualities and truthfully make efforts as desired by the crowdsensing requester. The QEE mechanisms achieve the truthful design by overcoming the intricate dependency of a user's data on its private quality and hidden effort.
- Under the QEE mechanisms, we characterize the crowdsensing requester's optimal (CO) effort assignment (under some condition) that maximizes the requester's expected payoff based on the distribution information of users' qualities. We show that the CO effort assignment assigns effort only to the best user that has the smallest virtual valuation, which depends on the user's quality and the quality's distribution.
- For the CO effort assignment, we show that the expected requester's payoff and the social welfare both increase as the number of users increases, or the cost decreases. We also show that the performance gap of the CO effort assignment from the SO social welfare decreases as the number of users increases, and converges to 0 asymptotically. We show via numerical results that the users' payoffs attained by the CO effort assignment can decrease when the number of users increases.

The rest of this paper is organized as follows. Section II discusses related work. In Section III, we describe the system model of crowdsensing with private data quality and formulate

the problems of truthful mechanism design. In Section IV, we devise truthful mechanisms for Quality and Effort Elicitation (QEE) for continuous-valued data. In Section V, we characterize the optimal effort assignment under the QEE mechanisms and devise truthful mechanism, and analyze their performance and system efficiency. Simulation results are presented in Section VI. Section VII concludes this paper and discusses future work.

II. RELATED WORK

Truthful crowdsensing with private cost. Crowdsensing has recently attracted a lot of research interests [5]–[8]. There have been many mechanisms to incentivize users to truthfully reveal their costs in crowdsensing [9]–[12]. The cost is considered to be a strategic user's private information that it would not be willing to reveal truthfully to the user's advantage without appropriate incentive. Departing from these works, we study the setting where the quality of a user's data contributed to the crowdsensing task is the user's private information that it can manipulate. A user's payoff as a function of its private quality has an essentially different structure as that of its private cost. As a result, existing designs for cost elicitation (such as the classical VCG auction and the characterization of truthful mechanisms [13, Theorem 9.36]) cannot work for quality elicitation, so that new designs are needed. Furthermore, this paper aims at joint elicitation of quality and effort. The intricate dependency of a user's data on its private quality and hidden effort results in the intricate coupling between the elicitation of quality and the elicitation of effort, which needs to be overcome.

Mechanism design for hidden actions. Mechanism design for hidden actions has been well studied in the economics literature [14], which is concerned with strategic agents that can take hidden actions that are not desired by a principal who employs the agents to work on a task. There are a few recent studies that have investigated this problem in the context of crowdsourcing [12], [15]. Cai *et al.* [15] have proposed truthful mechanisms to incentivize users to make efforts as desired in statistical estimation. However, most of the work on truthful elicitation of effort do not take into consideration agents' other possible private information (e.g., quality, cost). In a recent work [12], Luo *et al.* have made progress in this direction by providing mechanisms that not only elicit desired efforts from users but also truthful revelation of their private costs and data. This paper is different from these works as we aim to jointly elicit users' desired efforts and true qualities. Due to the intricate coupling between the elicitation of quality and the elicitation of effort, existing mechanism designs cannot handle the problem studied in this paper.

Quality-aware crowdsensing. The quality information of users is important for allocating crowdsensing tasks to the users, and has been studied in a few works [6], [16]–[19]. One interesting line of work in this direction has focused on learning the quality of users, e.g., by exploiting the correlation of their data for the same tasks [16], [17], or allocating tasks on the fly [18]. This paper focuses on the setting where quality is a user's private information that is unknown to the requester. To the best of our knowledge, this paper is the first to design

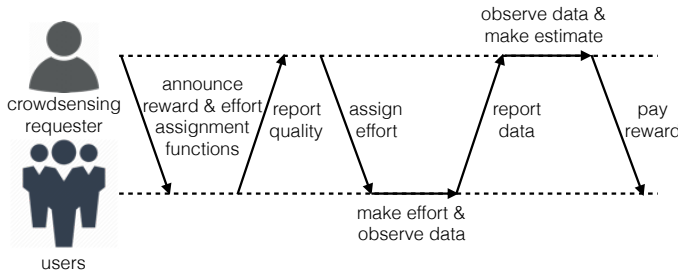


Fig. 1. Structure and procedure of the crowdsensing system.

truthful mechanisms to elicit private qualities from strategic users.

III. SYSTEM MODEL AND PROBLEM FORMULATION

We consider a crowdsensing requester (also referred to as user 0) recruiting a set of users $\mathcal{N} \triangleq \{1, \dots, N\}$ to work on a crowdsensing task. For convenience, let $\mathcal{N}^+ \triangleq \mathcal{N} \cup \{0\}$. The structure and procedure of the crowdsensing system is illustrated in Fig. 1 and described in detail as follows.

A. Crowdsensing with private user quality

1) *Data observation, user quality, and work effort:* The crowdsensing task aims to observe and estimate an unknown and random event of interest X . We consider continuous-valued data such that $X \in \mathbb{R}$ (e.g., the signal strength of a transmitter). The interested event X follows an arbitrary prior distribution which is known to the requester. Each user $i \in \mathcal{N}^+$ (i.e., including the requester) obtains random data D_i after working on the task, which is equal to X corrupted by an independent additive Gaussian noise W_i , i.e.,

$$D_i \triangleq X + W_i \quad (1)$$

where

$$W_i \sim \mathcal{N}\left(0, \frac{q_i}{e_i}\right). \quad (2)$$

Here the mean of W_i is assumed to be 0 without loss of generality (WLOG). Note that the Gaussian noise model is commonly used in many applications including crowdsensing (e.g., [1], [2]). The accuracy of D_i is quantified by the variance of W_i , which is equal to the ratio of the quality q_i of user i and the effort e_i exerted by user i in the task. For ease of exposition, we assume that users' qualities are within the range of $[q, \bar{q}]$, which is known to the requester.

Given the effort e_i , the quality $q_i > 0$ determines the variance $\frac{q_i}{e_i}$ of the difference $D_i - X$ (i.e., the noise W_i) which quantifies how accurate D_i is. The quality q_i is an intrinsic coefficient that captures user i 's capability for the task. Note that a smaller q_i means a higher quality. The quality generally varies for different users (e.g., users can receive distinct SNRs from a transmitter based on their locations). We assume that each user $i \in \mathcal{N}^+$ knows its quality q_i (e.g., by estimating the received SNR based on the user's distance from a transmitter). However, the quality of each user $i \in \mathcal{N}$ is unknown to the requester (e.g., the received SNR from a transmitter depends on the user's location which is its private information).

The effort $e_i \geq 0$ represents how much work user i devotes to the task. For example, the effort can be (approximately) the

number of samples of the received signal from a transmitter taken by the user. Given the quality q_i , a higher effort e_i means a smaller variance $\frac{q_i}{e_i}$ and thus a higher accuracy of D_i . We should note that it is reasonable to model the variance of noise W_i as the function $\frac{q_i}{e_i}$ which is inversely proportional to the effort e_i (e.g., as in [12]): if each unit of user i 's effort e_i is a sample of the observed event taken by user i , then when user i makes k units effort (i.e., ke_i) by taking k i.i.d. samples, it is clear that the variance of the average of the k samples is exactly $\frac{q_i}{ke_i}$. We assume that each user i can fully control its effort e_i , but it cannot be observed by the requester.

2) *Quality reporting, effort assignment, and data reporting:* The requester allocates the crowdsensing task to the users by assigning an effort e_i' that it desires each user i to exert in the task, based on the qualities of the users. To this end, each user i reports its quality q_i' to the requester. Since the true quality q_i is user i 's private information, it may manipulate the reported quality q_i' to its own advantage such that $q_i' \neq q_i$. Based on the qualities reported by all the users, the requester determines the effort e_i' assigned to each user i according to some effort assignment function

$$e_i'(q') \quad (3)$$

and notifies user i of its assigned effort e_i' . The effort assignment function $e_i'(q')$ is pre-defined by the requester and announced to all the users before they report their qualities. The effort assigned to a user generally varies for different users due to the diversity of their qualities. Intuitively, a user with a higher quality would be assigned a larger effort. Note that in general the assigned effort e_i' is not only dependent on the quality q_i' reported by user i but also on the qualities q_{-i}' reported by the other users. After being assigned effort e_i' to, each user i works on the task by making actual effort e_i . Since e_i is a hidden action of user i , it may manipulate it against the assigned effort e_i' to its own advantage such that $e_i \neq e_i'$. After obtaining data d_i from the task, which is a sample realization of the random data D_i , each user i reports data d_i' to the requester. We assume that each user i truthfully reports its data d_i (we will discuss in Remark 3 that this is a reasonable assumption).

3) *Data estimation and reward payment:* After collecting all the data \mathbf{d} reported by the users, the requester makes an estimate x^* of the interested event X based on \mathbf{d} . It uses the estimator that achieves the minimum mean squared error (MMSE), which is a common metric for statistical estimation [21], i.e.,

$$x^* \triangleq \arg \min_{x'} E_{X|\mathbf{d}(q', e')} [(x' - X)^2]. \quad (4)$$

Here the estimation is based on the posteriori distribution $X|\mathbf{d}$ of X , which depends on the qualities q' and efforts e' of the users. Then the utility of crowdsensing is represented by the estimation loss l , which is quantified by the MMSE:

$$l(\mathbf{d}, q', e') \triangleq E_{X|\mathbf{d}(q', e')} [(x^* - X)^2]. \quad (5)$$

On the other hand, the requester pays a reward r_i to each user i for its contribution to the task, according to a certain reward function:

$$r_i(d_0, d_i, q', e_i'). \quad (6)$$

Note that the reward r_i depends on the data d_0 observed by the requester itself. The reward function is also pre-defined by the requester, and announced to all the users before they report

their qualities (together with the effort assignment function $e'_i(\mathbf{q}')$). Note that the reward function can only depend on the information that the requester knows, i.e., d_0 , \mathbf{d} , \mathbf{q}' , and \mathbf{e}' .

B. Mechanism Design Objective

Based on the crowdsensing system described above, each user i 's payoff u_i is the reward r_i paid by the requester minus its cost in the task, given by,

$$u_i(d_0, d_i, \mathbf{q}', e_i) \triangleq r_i(d_0, d_i, \mathbf{q}', e_i) - c_i e_i. \quad (7)$$

Here the cost c_i represents how much resource (e.g., sensing time, energy) is consumed by user i for each unit of effort e_i devoted to the crowdsensing task. Therefore, as a linear function of e_i , the total cost $c_i e_i$ represents the total amount of resource consumed by user i in the task. Note that the weight of the total cost $c_i e_i$ relative to the reward r_i in (7) can be integrated into the cost c_i . We assume that all users have the same cost c (i.e., $c_i = c, \forall i$) and it is known to the requester. This assumption is reasonable when users' mobile devices have uniform (or similar) capabilities so that the resource consumption for making a unit of effort (e.g., taking a sample) is common knowledge to the requester and users.

The requester's payoff u_0 is the crowdsensing's utility (i.e., the negative of the estimation loss l) minus the total reward paid to the users, i.e.,

$$u_0(x, \mathbf{d}, \mathbf{q}', \mathbf{e}') \triangleq -l(\mathbf{d}, \mathbf{q}', \mathbf{e}') - \sum_{i \in \mathcal{N}} r_i(d_0, d_i, \mathbf{q}', e'_i) \quad (8)$$

As the users have private qualities and make hidden efforts, if any user manipulates its reported quality or actual effort, then the estimator found by (4) would be different from the correct estimator, i.e.,

$$x^* \neq \arg \min_{x'} E_{X|d(q,e)} [(x' - X)^2].$$

More importantly, the estimation loss found by (5) would be different from the correct one, i.e.,

$$l(\mathbf{d}, \mathbf{q}', \mathbf{e}') \neq \min_{x'} E_{X|d(q,e)} [(x' - X)^2].$$

This means that manipulation would lead to incorrect knowledge of the requester about the estimation loss! This is undesirable since the data's accuracy is a critical performance metric that needs to be ensured to meet some requirement (e.g., a tolerance threshold for acceptable data accuracy). Note that this issue does not arise in the setting where users have private costs only, since manipulating the costs can affect only the crowdsensing's utility and the reward payment but cannot affect the requester's knowledge of the data accuracy. Furthermore, the possibility of manipulation could result in concerns that discourage users to participate in crowdsensing. Thus motivated, we aim to design a mechanism, which is a pair of an effort assignment function $e'_i(\mathbf{q}')$ and a reward function $r_i(d_0, d_i, \mathbf{q}', e'_i)$, that can achieve the property of incentive compatibility as stated below.

Definition 1: A mechanism is *dominant incentive-compatible* (DIC) if, given any set of qualities reported by the other users, the optimal strategy of each user i for maximizing its expected payoff is to truthfully report its quality and make the effort desired by the requester, i.e.,

$$E_{D_0, D_i(q_i, e_i)} [u_i(D_0, D_i, q_i, \mathbf{q}'_{-i}, e'_i)] \geq E_{D_0, D_i(q_i, e_i)} [u_i(D_0, D_i, q'_i, \mathbf{q}'_{-i}, e_i)], \forall (q'_i, e_i), \forall \mathbf{q}'_{-i}.$$

Another natural and desirable property we aim to achieve is that each user's expected reward should at least compensate its cost (i.e., its expected payoff is nonnegative), since otherwise the user would not participate in crowdsensing for a payoff of 0. This property of individual rationality is stated as follows.

Definition 2: A mechanism is *individually rational* (IR) if for each user i , given that it truthfully reports its quality and makes the effort desired by the requester, its expected payoff is nonnegative, i.e.,

$$E_{D_0, D_i(q_i, e_i)} [u_i(D_0, D_i, q_i, \mathbf{q}'_{-i}, e_i)] \geq 0, \forall \mathbf{q}'_{-i}.$$

IV. TRUTHFUL QUALITY AND EFFORT ELICITATION FOR CROWDSENSING

In this section, we design truthful crowdsensing mechanisms that achieve the DIC and IR properties.

We first present the QEE mechanisms as follows.

Definition 3: A Quality and Effort Elicitation (QEE) mechanism is a pair of any effort assignment function $e'_i(\mathbf{q}')$ that satisfies the condition in (9) and the reward function $r_i(d_0, d_i, \mathbf{q}', e'_i)$ given by (10) based on that $e'_i(\mathbf{q}')$:

$$e'_i(q'_i, \mathbf{q}'_{-i}) \geq e'_i(q''_i, \mathbf{q}'_{-i}), \forall q'_i \leq q''_i, \forall \mathbf{q}'_{-i} \quad (9)$$

$$r_i(d_0, d_i, \mathbf{q}', e'_i) = c \int_{q'_i}^{\bar{q}} \frac{e'_i(q, \mathbf{q}'_{-i})}{q} dq + 2ce'_i(\mathbf{q}') - \frac{ce_i'^2(\mathbf{q}')}{q'_i} \left[(d_0 - d_i)^2 - \frac{q_0}{e_0} \right]. \quad (10)$$

The condition in (9) captures general effort assignment functions where the effort assigned to each user increases as its quality improves, given any qualities of the other users. Intuitively, these effort assignment functions are natural and desirable for system efficiency. In the following, we will show the main ideas of the design of the QEE mechanisms (9) and (10). The rationale behind the design will be explained in Remark 1.

We show how the QEE mechanisms achieve the DIC property in the following three steps. We first show how each user's expected payoff depends on its true quality and actual effort (Lemma 1). Then we show that if the elicitation of quality is achieved, the elicitation of effort is also achieved (Lemma 2). Last, given that the actual effort is optimized, we show that the elicitation of quality is achieved (Lemma 3). As a result, the DIC property is achieved (Theorem 1). Due to space limitation, the proofs of this paper are available in our online technical report [22].

We first show that each user's expected payoff can be expressed as a function of its true quality and actual effort using (10).

Lemma 1: Under the QEE mechanisms, given that any user i reports quality q'_i and its data d_i and makes effort e_i , its expected payoff is given by

$$E_{D_0, D_i(q_i, e_i)} [u_i(D_0, D_i, \mathbf{q}', e_i)] = c \int_{q'_i}^{\bar{q}} \frac{e'_i(q, \mathbf{q}'_{-i})}{q} dq + 2ce'_i(\mathbf{q}') - \frac{ce_i'^2(\mathbf{q}')q_i}{e_i q'_i} - ce_i. \quad (11)$$

Then we show that, as user i can only affect its payoff in (11) via its reported quality q'_i and actual effort e_i , its optimal actual effort can be found as a function of q'_i using (11).

Lemma 2: Under the QEE mechanisms, given that any user i reports quality q'_i and its data d_i , its optimal actual effort is given by

$$e_i = \sqrt{\frac{q_i}{q'_i}} e'_i(\mathbf{q}'). \quad (12)$$

Note that the optimal actual effort e_i in (12) is equal to the desired effort e'_i when the reported quality q'_i is equal to the true quality q_i . It means that if the elicitation of quality is achieved, then the elicitation of effort is also achieved. This is a key property we need to overcome the intricate coupling between the elicitation of quality and the elicitation of effort, and achieve the elicitation of effort. Using Lemma 2, given that user i reports its data d_i and makes the optimal effort as in (12), we can express its payoff in (11) as

$$c \int_{q'_i}^{\bar{q}} \frac{e'_i(q, \mathbf{q}'_{-i})}{q} dq + 2c e'_i(\mathbf{q}') - 2c \sqrt{\frac{q_i}{q'_i}} e'_i(\mathbf{q}'), \quad (13)$$

by substituting (12) into (11).

Next we show that, since user i can only affect its own payoff in (13) via its reported quality q'_i , its optimal q'_i is its true quality q_i , under the general condition (9) on the effort assignment function $e'_i(\mathbf{q}')$.

Lemma 3: Under the QEE mechanisms, given that any user i reports its data d_i and makes its optimal actual effort as (12), its optimal reported quality is its true quality $q'_i = q_i$.

Note that the optimal reported quality q'_i is always equal to the true quality q_i and is independent of e'_i . Therefore, this property achieves the elicitation of quality.

Using Lemmas 1, 2, and 3, we can show that the QEE mechanisms achieve the DIC property as in the next theorem. Given that user i reports its data d_i , makes the optimal effort $e_i = e'_i$, and reports the optimal quality $q'_i = q_i$, its payoff in (13) is given by

$$c \int_{q_i}^{\bar{q}} \frac{e'_i(q, \mathbf{q}'_{-i})}{q} dq. \quad (14)$$

It follows that the IR property is also achieved since (14) is no less than 0 due to the fact that $e'_i(\mathbf{q}') \geq 0, \forall \mathbf{q}'$.

Theorem 1: The QEE mechanisms are DIC and IR.

Remark 1: We explain the rationale behind the truthful design of the QEE mechanisms as follows. To incentivize each user i to report the true quality $q'_i = q_i$ and make the desired effort $e_i = e'_i$, the reward function r_i must depend on the true quality q_i and the actual effort e_i , since otherwise user i can manipulate q'_i and e_i without regard to q_i and e'_i . Since r_i can only be defined using the information known to the requester (i.e., d_0, d_i, \mathbf{q}' , and e'_i), and the variance of the noise W_i in data d_i is determined by the true quality q_i and the actual effort e_i , we can design r_i as a function of the squared error $(d_0 - d_i)^2$ such that the expected reward is a function of the variance and thus depends on q_i and e_i (as in Lemma 1 and (11)). Therefore, the expected reward depends only on q'_i, e'_i, q_i , and e_i (as in (11)). Then we can design the reward function such that the optimal actual effort e_i that maximizes user i 's expected payoff is equal to e'_i when $q'_i = q_i$ (as in Lemma 2 and (12)). Given that the actual effort is optimized, the payoff only depends on q'_i, e'_i , and q_i (as in (13)). Next we further design the reward function such that, under the general condition on e'_i (as in (9)), the optimal reported quality q'_i that maximizes the payoff is always equal to q_i and independent

of e'_i (as in Lemma 3).

Remark 2: We can see from (14) that, given the effort assignment function $e'_i(\mathbf{q}')$ and the users' qualities q_i and q'_{-i} , the user's payoff increases as the upper bound \bar{q} of users' qualities increases, and thus the requester's payoff decreases as \bar{q} increases. This means that the requester can pay less "information rent" [23] by knowing more information (i.e., having less uncertainty) about users' qualities with a smaller upper bound \bar{q} . In the extreme case where the requester knows that all users have the same quality (i.e., $q_i = \bar{q}, \forall i$), all users have 0 payoffs while the requester receives all the surplus of users' efforts, which means that the mechanism is fully "efficient" for the requester's interest.

Remark 3: We should note that, without any truthful design, it is difficult for a user to manipulate its reported data to its own advantage. This is because the user needs the private information of the requester's quality q_0 and effort e_0 , which it would not know, in order to find out how to manipulate its data to improve its payoff. Therefore, it is reasonable to assume that users truthfully report their data, as we do in this paper.

V. OPTIMAL EFFORT ASSIGNMENT FOR TRUTHFUL CROWDSENSING

We have shown that the DIC and IR properties can be achieved by all the QEE mechanisms which have general effort assignment functions that satisfy condition (9). We will now show how the requester can find the optimal effort assignment that maximizes its payoff, based on the distribution information of users' qualities. Because of the DIC property, we assume that $\mathbf{q}' = \mathbf{q}$ and $e = e'$ in this section, and thus, for brevity, we use \mathbf{q} and e instead of \mathbf{q}' and e' , respectively. For ease of analysis, we assume that the interested event X follows a normal prior distribution $\mathcal{N}(0, 1)$ (i.e., with mean 0 and variance 1). We further assume that users' qualities follow independent and identical uniform distributions over an interval $[q, \bar{q}]$, which is known to the requester.

Definition 4: The *crowdsensing requester's optimal (CO) effort assignment* $e^*(\mathbf{q})$ is the effort assignment function $e(\mathbf{q})$ that maximizes the requester's expected payoff (8) among all the QEE mechanisms, i.e.,

$$\{e^*(\mathbf{q}), \forall \mathbf{q}\} \triangleq \arg \max_{\{e(\mathbf{q}), \forall \mathbf{q}\}} E_{X, D(\mathbf{Q}, e)}[u_0(X, \mathbf{D}, \mathbf{Q}, e)]. \quad (15)$$

Then the optimal effort assignment can be characterized as follows.

Theorem 2: When $c \geq 1/(9\bar{q})$, the requester's optimal effort assignment (15) is given by

$$e_i^*(\mathbf{q}) = \begin{cases} \max \left\{ q_i \left(\frac{1}{\sqrt{\alpha(q_i)}} - 1 \right), 0 \right\}, & i = \arg \min_j \alpha(q_j) \\ 0, & \text{otherwise} \end{cases}, \quad (16)$$

$\forall \mathbf{q}$, where

$$\alpha(q_i) \triangleq c \left(\frac{F(q_i)}{f(q_i)} + q_i \right), \quad \forall i \quad (17)$$

and $f(q)$ and $F(q)$ denote the probability density function (PDF) and cumulative density function (CDF) of each user's quality, respectively.

In the rest of this section, we will assume that the condition $c \geq 1/(9\bar{q})$ in Theorem 2 is satisfied so that the CO effort

assignment is given in (16). This is because the characterization of the CO effort assignment under this condition and the corresponding performance analysis provide useful insights on the impact of system parameters on the performance and system efficiency. Furthermore, the performance under this condition also serves as an upper bound on the performance when the condition is not satisfied.

Remark 4: Theorem 2 shows that the optimal effort assignment assigns effort to only one user, and furthermore, this effort depends only on that user's quality (and its distribution) but is independent of the other users' qualities. Therefore, the optimal effort assignment appears to be "single-sensing" rather than "crowdsensing". However, we should note that in fact it exploits the diversity gain of multiple users' qualities, since only the "best"¹ user i that has the smallest $\alpha(q_i)$ is assigned to effort. This "single-sensing" observation is essentially because the cost functions are linear, so that the marginal gain of the requester's payoff by increasing the best user's effort is always greater than by increasing any other user's effort. It is in contrast to data estimation with no data cost [24], for which it is usually optimal to use data from multiple sources rather than only from the one source with the best quality. One attractive implication of this "single-sensing" observation is that it simplifies the implementation of crowdsensing: the requester needs to collect data only from the best user rather than a potentially large number of users.

For convenience, let q_1^* denote the quality of the best user for the CO effort assignment and $e_1^*(\mathbf{q})$ the CO effort assigned to the best user.

Remark 5: Theorem 2 shows that the best user is the user i with the smallest "virtual valuation" $\alpha(q_i)$ rather than the highest quality q_i , where each user i 's virtual valuation depends on not only its quality q_i but also the quality's distribution $F(q_i)$ and $f(q_i)$. This implies that the range of a user's possible qualities, represented by $\Delta q \triangleq \bar{q} - \underline{q}$, affects its effort assignment: given users' qualities, when users have a smaller quality range, more effort is assigned to the best user due to a smaller virtual valuation. This is intuitive because a larger quality range incurs a higher payment to the user in order to truthfully elicit quality. In the special case of $\Delta q = 0$, a user's virtual valuation is equal to its quality. The concept of virtual valuation was introduced by Myerson [13] and is in the same spirit as the result here.

Remark 6: According to condition (9), the CO effort $e_1^*(\mathbf{q})$ assigned to the best user in (16) increases when its quality q_1^* improves. Note that no effort is assigned if its quality is too low (i.e., $\alpha(q_1^*) \geq 1$). This is because a higher quality improves the marginal utility of crowdsensing by making more effort, and thus assigns more effort to the best user. On the other hand, we can observe from (16) and (17) that $e_1^*(\mathbf{q})$ decreases as the cost c increases. This is due to that a larger c incurs a larger payment to compensate the higher marginal cost, which results in less effort assigned.

Next we analyze the impact of system parameters on the performance of the CO effort assignment and its system

efficiency.

Proposition 1: The expected CO payoff $E_{\mathbf{Q}}[u_0(e^*(\mathbf{Q}))]$ attained by the CO effort assignment increases as the number of users N increases, or the cost c decreases.

Remark 7: Proposition 1 shows that the requester benefits from a greater diversity gain in users' qualities. This is because when there are more users, the quality of the best user is likely to be higher, which improves the crowdsensing's utility. On the other hand, a larger cost c increases the total cost and thus reduces the payoff.

The system efficiency of an effort assignment function $e(\mathbf{q})$ is quantified by the social welfare v it attains, which is the crowdsensing's utility (i.e., the expected estimation loss l) minus the total cost of all users, i.e.,

$$v(e(\mathbf{q})) \triangleq -E_{D(\mathbf{q}, e)}[l(\mathbf{D}, \mathbf{q}, e)] - \sum_{i \in \mathcal{N}} c_i e_i. \quad (18)$$

For the interest of system efficiency, it is desirable to achieve the optimal social welfare.

Definition 5: The socially optimal (SO) effort assignment $e^{so}(\mathbf{q})$ is the effort assignment function $e(\mathbf{q})$ that maximizes the social welfare, i.e.,

$$e^{so}(\mathbf{q}) \triangleq \max_{e(\mathbf{q})} v(e(\mathbf{q})). \quad (19)$$

The socially optimal effort assignment can be characterized as follows.

Proposition 2: The socially optimal effort assignment is given by

$$e_i^{so}(\mathbf{q}) = \begin{cases} \max \left\{ q_i \left(\frac{1}{\sqrt{cq_i}} - 1 \right), 0 \right\}, & i = \arg \min_j q_j \\ 0, & \text{otherwise} \end{cases}. \quad (20)$$

Remark 8: Proposition 2 shows that the SO effort assignment assigns effort only to the "best" user i that has the highest quality q_i . Comparing (16) and (20), we can see that the SO effort assignment is only different from the CO effort assignment in that it selects the best user and assigns the effort to it based on the highest quality rather than the smallest virtual valuation among the users. Since it can be easily seen that each user i 's virtual valuation $\alpha(q_i)$ is no less than its quality q_i , the CO effort assigned to the best user is less than the SO effort assigned. This is because, although assigning more effort can improve the social welfare, it would result in a too higher payment. As a result, the CO effort assignment is not socially optimal, and the gap is essentially due to the asymmetry of users' quality information between the users and the requester.

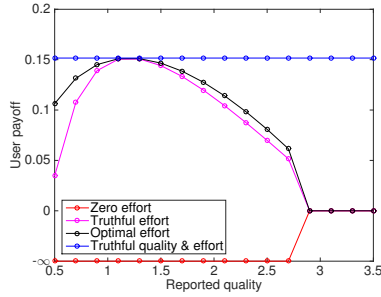
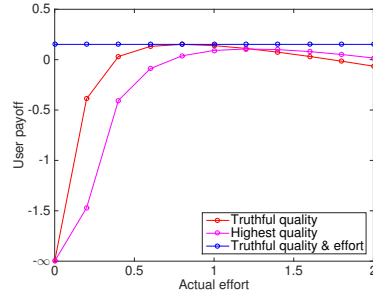
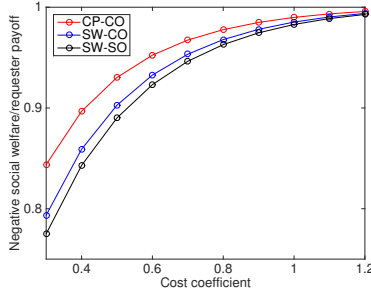
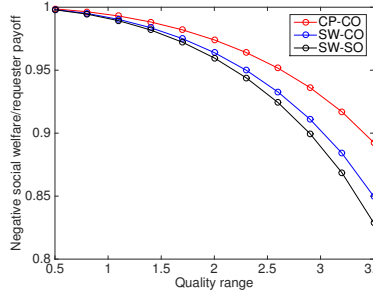
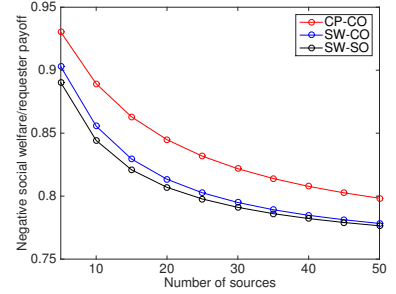
For convenience, let q_1^{so} denote the quality of the best user for the SO effort assignment and $e_1^{so}(\mathbf{q})$ the SO effort assigned to the best user.

Proposition 3: The expected SO social welfare $E_{\mathbf{Q}}[v(e_1^{so}(\mathbf{Q}))]$ and social welfare $E_{\mathbf{Q}}[v(e_1^*(\mathbf{q}))]$ attained by the CO effort assignment increases as the number of users N increases, or the cost c decreases.

Similar to Proposition 1, Proposition 3 shows that the social welfare also benefits from a greater diversity gain in users' qualities: when there are more users, the quality of the best user is likely to improve.

Proposition 4: The gap between the expected social welfare of the CO effort assignment and the SO effort assignment

¹If there are multiple "best" users, only one of them is selected by breaking the tie randomly.


 Fig. 2. Impact of reported quality q'_1 .

 Fig. 3. Impact of actual effort e_1 .

 Fig. 4. Impact of cost c .

 Fig. 5. Impact of quality range Δq .

 Fig. 6. Impact of the number of users N .

$E_Q[v(e_1^{so}(\mathbf{Q}))] - E_Q[v(e_1^*(\mathbf{Q}))]$ decreases as the number of users N increases, and converges to 0 as N goes to infinity.

Remark 9: Proposition 4 shows that the performance gap between the CO effort assignment and the SO effort assignment decreases to 0 asymptotically as the number of users increases. This is because the gap between the CO effort and the SO effort assigned to the best user decreases when its quality improves, and that the crowdsensing's utility and thus the social welfare is a concave function of the effort from the best user.

VI. SIMULATION RESULTS

In this section, we evaluate the properties of the QEE mechanisms and its performance with the CO effort assignment using simulation results.

A. User's payoff

To illustrate the DIC and IR properties of the QEE mechanisms, we compare a user's expected payoff when it truthfully reports its quality and makes its effort with that when it untruthfully reports its quality and/or makes its effort. We use the CO effort assignment $e_i^*(q)$ in (16) for the QEE mechanism. We set the default parameters as follows²: $n = 2$, $c = 0.3$, $\mu_q \triangleq (\bar{q} + q)/2 = 2$, $\Delta q = 3$, $q_1 = 1.2$, $q_2 = 2.75$.

Fig. 2 illustrates user 1's expected payoff as it reports varying quality q'_1 and makes no effort, or truthful effort $e_1^*(q'_1, q_2)$, or optimal effort $\sqrt{\frac{q_1}{q'_1}} e_1^*(q'_1, q_2)$ (as in (12)), compared to when it truthfully reports its quality and makes its effort. Fig. 2 illustrates user 1's expected payoff as it makes

²It is WLOG to consider 2 users only as the CO effort assignment assigns effort to the best user only based on the best user's quality.

varying effort e_1 and reports its actual quality q_1 , or the highest quality q , compared to when it truthfully reports its quality and makes its effort. We can see that the user's payoff when its behavior is untruthful is always no greater than when truthful. Furthermore, the user's payoff gap due to untruthfulness increases when it is more untruthful (i.e., the gap between the reported quality and actual quality, or the desired effort and the actual effort is larger). This confirms that the DIC property is achieved by the QEE mechanism so that users have incentive to behave truthfully. We also observe from Figs. 2-3 that the user's payoff is always greater than 0. This confirms that the IR property is achieved by the QEE mechanism.

B. Requester's payoff

To illustrate the system efficiency of the CO effort assignment, we compare the expected requester's payoff (CP) and total users' payoff (SP) attained by the CO effort assignment (CP-CO, SP-CO) with the expected social welfare (SW) attained by the SO effort assignment (SW-SO), and the expected SW attained by the CO effort assignment (SW-CO). Note that SP-CO is represented by the gap between CP-CO and SW-CO curves in figures. We set the default parameters as follows: $N = 5$, $c = 0.5$, $\mu_q \triangleq (\bar{q} + q)/2 = 2$, $\Delta q = 3$. It can be verified that all the data points presented in the figures of this section satisfy the optimality condition $c \geq 1/(9q)$ in Theorem 2 for the CO effort assignment. For convenience, we illustrate the negative of social welfare or the requester's payoff in all figures.

Fig. 4 illustrates the impact of the cost c on the performance of CP-CO, SW-CO, and SW-SO. We observe that all the three curves and SP-CO increase as c increases, which is because

higher cost results in less effort and low performance. We also observe that the gap between SW-CO and SW-SO is small when c is large. This is because a large c results in little effort so that the social welfare is close to the lower bound in which no effort is made, and thus the gap in the social welfare is also small.

Fig. 5 illustrates the impact of the quality range Δq on the performance. We observe that all the three curves are decreasing in Δq . This shows that CP and SW are concave functions of the qualities, so that the increase of CP or SW at high qualities is larger than the decrease of CP or SW at low qualities when Δq is large. We also observe that SP-CO increases as Δq increases. This is partly due to that a larger range of possible qualities would require a higher truth-eliciting reward according to (14). We further observe that the gap between SW-CO and SW-SO is small when Δq is small. This is partly because the gap between the CO and SO effort assignments is decreasing in Δq according to (16) and (20).

Fig. 6 illustrates the impact of the number of users N on the performance. We observe that all the three curves are decreasing in N , which is because they benefit from a greater diversity gain in users' qualities when there are more users. We also observe that the gap between SW-CO and SW-SO is decreasing and converging to 0 when N increases, which confirms our result in Proposition 4. It is interesting to observe that, while all of CP-CO, SW-CO, and SW-SO increases as N increases, SP-CO can decrease when N increases (e.g., as SP-CO is smaller at $N = 50$ than at $N = 20$). This can be understood by examining the best user's payoff given by

$$c \int_{q_1^*}^q \frac{e_1^*(q, \mathbf{q}_{-i})}{q} dq$$

according to (14). We can see that when N increases, q_1^* is likely to decrease which would increase the above integral. However, \mathbf{q}_{-i} is also likely to increase as N increases, which decreases $e_1^*(q, \mathbf{q}_{-i})$, and this effect can outweigh the increase of q_1^* such that the integral decreases. This means that while the requester benefits from more users, the users can experience a loss due to the "competition" among the users.

VII. CONCLUSION AND FUTURE WORK

In this paper, we have devised the QEE mechanisms for crowdsensing, to incentivize strategic users to truthfully reveal their private qualities and make efforts as desired by the crowdsensing requester. The QEE mechanisms have achieved the truthful design by overcoming the intricate coupling between the elicitation of quality and the elicitation of effort. Under the QEE mechanisms, we have analyzed the performance and system efficiency of the requester's optimal effort assignment.

For future work, one interesting direction is to consider users that have no knowledge of their qualities. In this case, the requester needs to learn the qualities of strategic users which may not truthfully provide data to the requester for the purpose of learning. In this paper, we have focused on the truthful quality and effort elicitation under the assumptions that users truthfully report their data and their cost is known to the requester. The truthful mechanism design when users'

data and/or costs are also private information is still an open problem and will be studied in our future work.

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