

Distributed Learning for Proportional-Fair Resource Allocation in Coexisting WiFi Networks

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Abstract—WiFi networks suffer from severe network utility degradation due to the usage of diverse modulation and coding schemes. The proportional-fair allocation, that has been shown to be a good remedy, can be enforced through the proper selection of contention window values. This has been achieved so far for centralized systems by an explicit solution of an optimization problem or, as proposed recently, by following a learning-based approach. In this paper, we present the first fully distributed solution in which each of the WiFi nodes independently tunes its contention window to achieve proportional fairness. Our solution is therefore applicable also for a set of collocated, unconnected WiFi networks. We compare the throughput and air-time allocation that this algorithm achieves to the values achieved by standard WiFi binary exponential back-off and values achieved by known centralized algorithms.

Index Terms—WiFi, Contention Window, Distributed Optimization

I. INTRODUCTION

The widely deployed WiFi stations employ various modulation and coding schemes (MCSs) to preserve transmission robustness in response to the quality of the radio link they experience, which in turn depends on their communication distance, mobility, and other factors. The lower MCSs offer increased robustness against errors at the cost of a slower data rate. Under the frame-level fairness implied by the standard WiFi contention window (CW) adaptation, a station with poor transmission conditions captures extensive air-time share and reduces the air time available to other (possibly faster) stations, and hence the station *slows down* all stations. This pathological behavior was first identified in 802.11b networks [1]. Then, Patras *et al.* [2] demonstrated that the effect is dramatically exacerbated in today’s high throughput networks (i.e., 802.11n/ac), where the data rates among stations may vary by orders of magnitude, e.g., the throughput of a station using the data rate of 780 Mbps becomes similar to that of a co-existing station with the data rate of 6 Mbps.

The proportional-fair allocation, introduced by Kelly *et al.* [3], was shown to address the performance anomaly problem appropriately [4]. By definition, it maximizes the network utility (defined as the sum of the logarithms of individual throughputs) subject to the constraints that the communication conditions impose on the individual stations. In [5], the proportional fairness allocation in WiFi networks was formulated as a convex optimization problem that is solved by selecting optimal contention window values for the stations. The existing approaches to solve this problem

are deployed in a central node (e.g., AP or a controller node) and require knowledge of individual MAC parameters (e.g., packet duration) and/or throughput of each transmitting station. Such centralized operation cannot be assumed in the case of overlapping but separately managed WiFi networks – the typical case for an apartment complex or office building occupied by multiple companies. In fact, the standard does not envision the possibility of communication between nodes belonging to different networks eliminating any attempt for centralized control (e.g., by the elected leader).

Therefore, we have started working on a distributed learning-based approach where each of the WiFi nodes, based on local observation of the traffic, independently tunes its own contention window to achieve global proportional fairness. Our approach follows the mindset of a distributed stochastic convex optimization framework. Unfortunately, we have found no theoretical results which might be applied to our case. Motivated by this real technical problem, one of the authors succeeded to deliver rigorous proof of the convergence of the Kiefer-Wolfowitz algorithm [6] in a distributed and asynchronous setting. The results, published in [7], [8], have been very encouraging but, unfortunately, obtained under mathematical assumptions that are not strictly satisfied by our technical problem.

In this work, we explore the usability of the distributed and asynchronous Kiefer-Wolfowitz (DA-KW) algorithm under realistic assumptions in a practical use-case of wireless optimization. Specifically, the contributions of this work are as follow:

- We propose a simple approach for distributed contention window tuning that achieves proportional fairness in coexisting WiFi scenarios. To this end, we apply the DA-KW algorithm to the WiFi domain with slight modifications to address the practical issues.
- Using simulations, we evaluate the proposed approach in terms of convergence speed and achieved performance in multiple scenarios. Moreover, we compare its performance with the standard WiFi.
- We investigate the impact of the level of coordination (i.e., synchronized execution and information exchange). It appears that there is no significant gain of the coordination in the case of a single collision domain. However, coordination and information exchange allow achieving optimal channel allocation in the case of overlapping collision domains.

II. RELATED WORK

Proportional fairness in WiFi networks has been extensively studied, e.g., [9]–[11]. Checco *et al.* [4] provided an analysis of proportional fairness in WiFi networks. The authors proved that a unique proportional fair rate allocation exists and assigns equal total (i.e., spent on both colliding and successful transmission) air-time to nodes. Patras *et al.* [2] extended this analysis to multi-rate networks, and confirmed that under proportional fair solution all the stations get an equal share of the air-time, which is inversely proportional to the number of active stations. The authors formulated network utility maximization as a convex optimization problem and provided a closed-form solution that can be solved explicitly. To this end, an AP estimates the average duration of successful transmissions for each station and pass it as an input to the optimization tool. The computed CW values are distributed to nodes in a beacon frame. The optimization is executed periodically (i.e., every beacon interval) to react to changes in the network (e.g., traffic or wireless conditions).

An alternative approach was proposed by Famitafreshi *et al.* [12]. The authors use a stochastic gradient descent (SGD) algorithm, which can iteratively learn the optimal contention window only by monitoring the network's throughput. Specifically, the learning agent resides in the WiFi access point (AP), where it can measure the uplink throughput of each connected station and send the CW value updates to all the stations in a beacon frame. The algorithm combines two throughputs measured under different CW values to compute the gradient and update the CW following the SGD algorithm.

Both proposed algorithms use global knowledge and centralized operation (i.e., deployed in AP). However, in typical scenarios, multiple networks under separate management domains are co-located and have to coexist, and there is no central entity with the full knowledge to perform the optimization or learning.

III. RELEVANT WiFi BACKGROUND

In this section, we briefly describe the CSMA operation, present its analytical models, and summarize the throughput optimization in WiFi networks.

A. WiFi Random Back-off Operation

WiFi nodes use the Distributed Coordination Function (DCF) mechanism to access the channel. The DCF is based on the Carrier Sense Multiple Access/Collision Avoidance (CSMA/CA) method and employs binary exponential back-off (BEB) to control the contention window. Specifically, in DCF, before a frame transmission, a WiFi station has to perform a random back-off procedure. To this end, it initializes its back-off counter with a random number drawn uniformly from $\{0, \dots, CW-1\}$, where CW is the contention window. Then, the station observes the wireless channel and decrements the counter whenever it is sensed idle during a DCF inter-frame space (DIFS) and freezes the back-off counter otherwise. Finally, when the back-off counter reaches zero, the station transmits a frame. If the transmission is successful (as

indicated by the reception of an acknowledgment), the station sets CW to the minimal value, i.e., CW_{min} , for the next transmission. Otherwise, it doubles the previous contention window and performs the frame retransmission. The CW is increased until it reaches the maximal value defined by CW_{max} .

B. Analytical Model of Contention-based Medium Access

Here, we briefly describe the analytical model derived in [2] which allows computing the total throughput achieved by WiFi nodes. We assume that all nodes are in a single collision domain (i.e., each node overhears transmissions of all other nodes). For the sake of clarity of presentation, in this section, we consider the case where all stations are saturated (i.e., they always have packets to transmit), but in Section VI, we also evaluate our algorithm in scenarios with non-saturated traffic. Note that the model allows for arbitrary packet sizes and selection of MCS.

Let us consider a set of N wireless stations, where each active station i accesses the channel with slot transmission probability λ_i . The relation between channel access probability to a constant contention window is $CW_i = \frac{2-\lambda_i}{\lambda_i}$ [13]. The transmission failure probability experienced by a station i equals $p_{f,i} = 1 - (1 - p_{n,i})(1 - p_i)$, where $p_{n,i}$ is the probability that the transmission fails due to channel errors (e.g., noise or interference), while $p_i = 1 - \prod_{j=1, j \neq i}^N (1 - \lambda_j)$ denotes the collision probability experienced by a packet transmitted by this station. Then, the throughput of station i equals S_i :

$$S_i = \frac{p_{s,i} D_i}{P_e T_e + P_s T_s + P_u T_u} \quad (1)$$

where, $p_{s,i} = \lambda_i(1 - p_{f,i})$ is the probability of a successful transmission performed by station i , while D_i denotes its frame payload size in bits. $P_e = \prod_{i=1}^N (1 - \lambda_i)$ is the probability that the channel is idle during a slot of duration T_e (e.g., $9\mu s$ in 802.11n). $P_s = \sum_{i=1}^N p_{s,i}$ and $P_u = 1 - P_e - P_s$ are the expected probabilities of successful and unsuccessful transmission with the expected durations $T_s = \prod_{i=1}^N \frac{p_{s,i}}{P_s} T_{s,i}$ and $T_u = \prod_{i=1}^N \frac{p_{u,i}}{P_u} T_{u,i}$, respectively. Here, $T_{s,i}$ and $T_{u,i}$ are the durations of successful and a failed transmissions of each station that depend on the fixed preamble duration, the variable duration of a header, the size of a payload transmitted with the PHY rate C_i , and whether an acknowledgment is sent (success) or not (failure). Finally, $p_{u,i} = \tau_i p_{n,i} \prod_{j=1, j \neq i}^N (1 - \tau_j) + \tau_i \left(1 - \prod_{j=1}^{i-1} (1 - \tau_j)\right) \prod_{j=i+1}^N (1 - \tau_j)$ is the probability of an unsuccessful transmission (either due to collision or channel errors) of stations of highest index i (when labeling stations according to their transmission durations). Note that the proper labeling is needed as the duration of a collision is dominated by the frame with the longest duration involved in that collision, and collisions should only be counted once.

Using the transformed variable $y_i = \frac{\lambda_i}{1-\lambda_i}$, the expression of a station's throughput (1) can be rewritten as:

$$S_i = (1 - p_{n,i}) \frac{y_i}{Y} D_i \quad (2)$$

where $Y = T_e + \sum_{i=1}^N \left(y_i T_{s,i} \prod_{k=1}^{i-1} (1 + y_k) \right)$. We refer to [2] for the details of the model and the transition from identity (1) to (2).

C. Proportional-fair Allocation

Following [4], we formulate the proportional-fair allocation problem as a convex optimization problem. The global utility function is defined as the sum of the logarithms of individual throughputs, i.e., $U = \sum_{i=1}^N \tilde{S}_i$, where $\tilde{S}_i = \log(S_i)$. The utility maximization problem is as follows:

$$\begin{aligned} & \text{maximize} && \sum_{i=1}^N \tilde{S}_i \\ & \text{s.t.} && \tilde{S}_i \leq \log \left(z_i \frac{y_i}{Y} D_i \right), \quad i = 1, 2, \dots, N \\ & && \text{and } 0 \leq y_i, \quad i = 1, 2, \dots, N \quad (0 \leq \lambda_i \leq 1) \end{aligned}$$

where $z_i = 1 - p_{n,i}$. The constraints ensure that the optimal solution is feasible, i.e., it is within the log-transformed rate region \tilde{R} . The rate region R is a set of achievable throughput vectors $S(\lambda) = [S_1, S_2, \dots, S_N]$ as the vector λ of attempt probabilities ranges over domain $[0, 1]^N$. The set R is known to be non-convex in 802.11 networks, but the log-transformed rate region \tilde{R} is strictly convex [5]. Moreover, as the strong duality and the KKT (Karush-Kuhn-Tucker) conditions are satisfied, a global and unique solution exists.

IV. DISTRIBUTED STOCHASTIC OPTIMIZATION PRIMER

Here, we briefly introduce the stochastic convex optimization techniques in centralized (i.e., single agent) and distributed (i.e., multiple agents) settings.

A. Stochastic Convex Optimization

A Stochastic Convex Optimization deals with minimizing of the expected value of a function $F(\mathbf{x}, \xi)$ that is convex in $\mathbf{x} \in \mathbb{R}^d$ where ξ is random vector:

$$\text{Find } \mathbf{x}^* = \underset{\mathbf{x} \in \mathcal{K}}{\text{argmin}} f(\mathbf{x}) := E(F(\mathbf{x}, \xi)). \quad (3)$$

The setup is that one has access to sample values of $F(\mathbf{x}, \xi)$.

If one could measure the gradient $\nabla f(\mathbf{x})$ of the function, one could use a gradient descent algorithm where the parameters at the t -th iteration, \mathbf{x}_t , are updated according to $\mathbf{x}_{t+1} = \mathbf{x}_t - \eta_t \nabla f(\mathbf{x})$, where η_t is the step size at iteration t . However, in practical scenarios there is no access to the actual gradient $\nabla f(\mathbf{x})$. Accordingly, the stochastic gradient descent algorithms rely on constructing noisy gradient estimates \tilde{g}_t , which are then used to adjust the parameters according to $\mathbf{x}_{t+1} = \mathbf{x}_t - \eta_t \tilde{g}_t$.

The Kiefer-Wolfowitz (KW) algorithm [6] is a gradient estimation method that combines two function evaluations with perturbed values of its variable to compute the estimate. The simultaneous perturbation stochastic approximation (SPSA) algorithm [14] is an extension of the KW algorithm towards multivariate problems. In SPSA, the partial derivatives with

respect to the different variables are estimated by simultaneously perturbing each variable by an independent and zero-mean amount, instead of perturbing the variables one at a time.

The optimization procedure can be performed in a centralized or distributed setting. In the former case, a single agent knows and controls all the variables in vector \mathbf{x} and has the exclusive right to query the function (we refer to it as *environment*), while in the latter case, those assumptions do not hold.

B. Distributed Convex Optimization

In the distributed settings, a set of N distributed agents try to optimize a global objective function. The critical challenge is that agents make individual decisions simultaneously, and the value of the function depends on all agents' actions. Moreover, we assume that the agents are not synchronized (i.e., they query the function and update their variable asynchronously at a random point in time) and cannot communicate. Specifically, each agent adjusts his own variable x_i without knowing the values of the other variables, i.e., x_{-i} . Fig. 1 shows the interaction between agents and the environment.

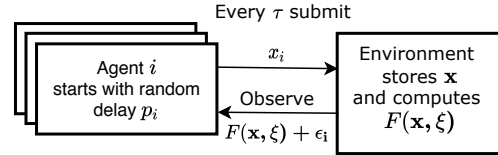


Fig. 1. The interaction between distributed agents and the environment – agents asynchronously submit their individual variables to the environment and get noisy observations of its value.

Following a naive application of the KW algorithm, each agent estimates the gradient by perturbing its own variable by a zero-mean change and querying the global function every time interval τ . Then, it uses those measurements to determine the gradient and updates its variable in proportion to the computed estimate. Note that agents perform such experiments without any coordination. Thus, when an agent attempts to get

Algorithm 1: DA-KW (executed by each agent i)

- 1 **Input:** Non-increasing sequences $(\delta_k), (\eta_k)$
 - 2 **Input:** Function sample interval $\tau \geq 1$
 - 3 **Input:** Phase offset $p_i \in \{1, \dots, \tau - 1\}$
 - 4 **Initialization:** Choose arbitrary $y_0 \in \mathbb{R}$
 - 5 **for** $k = 0, 1, \dots$, **do**
 - 6 Draw ε_k uniformly from $\{-1, 1\}$
 - 7 Let $t = k \times 2\tau + p_i$
 - 8 At t set $x_t = y_k + \varepsilon_k \delta_k$
 - 9 Observe $g_k^+ = f(\mathbf{x}_t)$.
 - 10 At $t + \tau$ set $x_{t+\tau} = y_k - \varepsilon_k \delta_k$
 - 11 Observe $g_k^- = f(\mathbf{x}_{t+\tau})$
 - 12 Compute gradient estimate $\tilde{g}_k = \frac{g_k^+ - g_k^-}{2\varepsilon_k \delta_k}$
 - 13 Update $y_{k+1} = y_k - \eta_k \tilde{g}_k$
 - 14 **if** $\|x_t - x^*\| < \varepsilon^*$ **break**
 - 15 **end**
-

a second evaluation of the function, the function may have already changed due to another agent's query. Intuitively, each agent gets gradient estimates corrupted due to the actions of other agents. However, we have recently proved that the KW algorithm can converge to the optimal solution in a distributed and asynchronous (DA) setting if the size of perturbation is bounded [7]. The algorithm executed by each agent is presented as Algorithm 1.

V. DISTRIBUTED CONTENTION WINDOW LEARNING

Based on a distributed and asynchronous Kiefer-Wolfowitz algorithm, we propose a simple collaborative learning scheme for WiFi nodes, which allows them to learn the optimal contention window values without coordination and information exchange.

A. Practical Issues

There are several practical issues that have to be considered. First, the utility function evaluation is not immediate, as an agent cannot measure the instantaneous throughput. Instead, it has to count an amount of successfully transmitted data by overhearing frames and compute the mean throughput of neighboring nodes over the measurement time slot τ . As agents follow this procedure simultaneously with random phase offsets, the utility that each agent observes is an average of multiple function evaluations during τ that correspond to changing CW of agents. Second, in contrast to the formal proof where the function is globally defined, the congestion window takes values in a discrete set between CW_{min} and CW_{max} . Finally, to make an algorithm responsive to changes (e.g., used data rates), we use constant exploration and learning parameters and remove the termination condition. Therefore, the algorithm cannot converge to the optimum value but only to its neighborhood.

B. Proposed Approach

We apply a modified version of the DA-KW algorithm to learn the IEEE 802.11's CW cooperatively. More specifically, as illustrated in Algorithm 2, we introduce modifications to match the discussed practical issues.

From the point of view of a single agent, our proposed technique works as follows. During initialization, a WiFi node selects a contention window value within the range of $[CW_{min}, CW_{max}]$. The integer CW value is converted to log-transformed variable y using function L . Specifically, L computes channel access probability as $\lambda = \frac{2}{CW+1}$, and then transformed variable as $y = \log(\frac{\lambda}{1-\lambda})$. By L^{-1} , we designate the operation inverse to L .

At a random time point t , node i perturbs its log-transformed variable by a fixed exploration parameter δ_k , i.e., it replaces y_k by $y_k + \varepsilon_k \delta_k$ and converts that value back to the discrete CW_t value. Next, for the duration of a single measurement slot τ (e.g., 100 ms), it transmits all its frames applying the CW_t value to the back-off procedure. Simultaneously, the node observes the environment formed by all WiFi nodes. That is, by overhearing frames, it counts the amount of data transmitted

Algorithm 2: Proposed Algorithm (executed by each agent i)

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1 Input:  $L$  converts  $CW$  to log-transformed value  $y$ 
2 Input: Constant parameters  $\delta_k = \delta, \eta_k = \eta$ 
3 Input: Function sample interval  $\tau$ 
4 Input: Random phase offset  $p_i \in [0, \tau]$ 
5 Initialization: Choose  $y_0 \in [L(CW_{min}), L(CW_{max})]$ 
6 for  $k = 0, 1, \dots$ , do
7   Draw  $\varepsilon_k$  uniformly from  $\{-1, 1\}$ 
8   Let  $t = k \times 2\tau + p_i$ 
9   At  $t$  set  $CW_t = \lceil L^{-1}(y_k + \varepsilon_k \delta_k) \rceil$ 
10  Observe transmissions of neighbors for  $\tau$  and
    compute  $g_k^+ = \sum_{i=1}^N \tilde{S}_i$ .
11  At  $t + \tau$  set  $CW_{t+\tau} = \lceil L^{-1}(y_k - \varepsilon_k \delta_k) \rceil$ 
12  Observe transmissions of neighbors for  $\tau$  and
    compute  $g_k^- = \sum_{i=1}^N \tilde{S}_i$ .
13  Compute gradient estimate  $\tilde{g}_k = \frac{g_k^+ - g_k^-}{2\varepsilon_k \delta_k}$ 
14  Update  $y_{k+1} = \Pi_k(y_k - \eta_k \tilde{g}_k)$ , where  $\Pi_k$  is the
    projection operator onto  $\mathcal{K}_{\delta_k}$ 
15 end

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by each neighbor. At the end of the measurement slot, it computes the value of the network utility function, i.e., the sum of the logarithms of the observed throughputs of the different nodes and the known own throughput. Then at $t + \tau$, the node again perturbs its log-transformed variable, i.e., it replaces y_k by $y_k - \varepsilon_k \delta_k$, and repeats the measurement procedure. Finally, at $t + 2\tau$, it combines both measurements to compute the gradient estimate and updates its log-transformed variable y_{k+1} accordingly. The value is projected to the decision set defined as $\mathcal{K}_\alpha = [A + \alpha, B - \alpha]$, where $\alpha \leq \frac{B-A}{2}$. The projection of x to the nonempty interval $[a, b]$ is defined as $\Pi_{[a,b]} = \max\{\min\{b, x\}, a\}$. Note that the gradient descent is performed in a continuous domain using log-transformed variable y , which is then converted and discretized into an integer CW value.

C. Impact of Diverse Coordination Levels

To evaluate the impact of action synchronization among the distributed nodes, we target the scenario with a two-step approach that gradually removes the coordination:

Coordinated Learning: In the case of full coordination, the measurement slots of agents are synchronized, i.e., $p_i = 0$ for $i \in \{1, \dots, N\}$. Specifically, agents perform the gradient estimation procedure and update the CW at the same time. Therefore, the utility function is evaluated with constant variables in each time slot.

Uncoordinated Learning: In the general case, the actions of distributed agents are not synchronized, and at any point in time t each agent is at a different stage of the algorithm. Note that from each agent's perspective, the environment state could change $N - 1$ times within a single measurement period.

VI. PERFORMANCE EVALUATION

We evaluate the distributed contention window tuning algorithm by means of simulations using the ns3-gym framework [15]. Specifically, we use the model for IEEE 802.11n in infrastructure-based mode and create multiple overlapping WiFi networks. Note that nodes belonging to separate networks cannot communicate. If not stated otherwise, we create a fully-connected topology (i.e., single collision domain), where nodes are uniformly spread in the area of 10-by-10 m; hence, every transmitter can sense ongoing transmissions. In order to change network contention conditions, we vary the number of transmitting nodes. Moreover, we change the data rates and frame sizes to influence the solution of the proportional-fairness problem. To turn off the BEB procedure and enable simple uniform back-off, i.e., we assign the same value of CW to CW_{min} and CW_{max} . We bound the CW value to the range used in WiFi, i.e., $CW \in \{15, 1023\}$, hence the log-transformed CW operates in $y \in \{-6.23, -1.94\}$. We show the convergence of the algorithm using the evolution of the contention window, air-time share, and throughput.

A. Selection of Measurement Slot Duration

First, we evaluate the impact of the measurement slot duration on the quality of the network utility estimates and the algorithm's convergence. To this end, we consider a scenario with five transmitting stations with homogeneous traffic, i.e., each station is backlogged with 1000B UDP packets and transmits to its own AP with a data rate equal to 26 Mbps.

Fig. 2 shows the evolution of the contention window value (we show $c = \log_2(CW)$) for each of transmitting nodes with four slot durations, $\tau \in \{25, 50, 100, 200\}$ ms. We observe higher variability for smaller values of τ , which is expected due to the random nature of the frame transmissions. Specifically, with smaller values of τ , the nodes cannot collect enough statistics to accurately estimate the network utility. These effects are alleviated by increasing the duration of τ so that the throughput estimates become more accurate, but at the cost of longer convergence time as updates are less

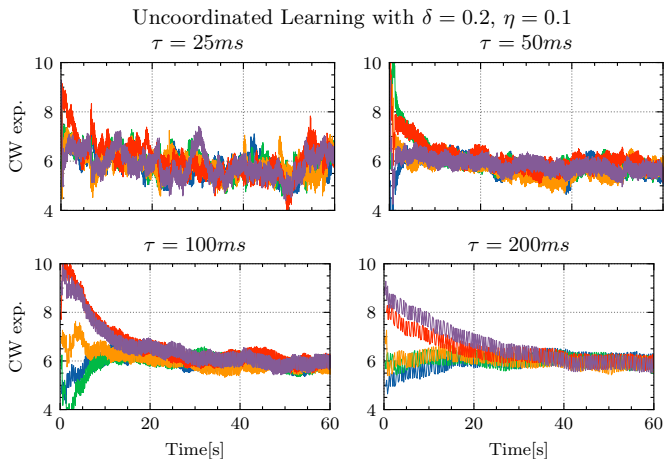


Fig. 2. Convergence of individual CW under various measurement slot duration $\tau \in \{25, 50, 100, 200\}$ ms.

frequent. For further evaluation, we select $\tau = 200$ ms, and leave its optimization as future work.

B. Homogeneous Traffic

Here, we examine the sensitivity of the proposed distributed algorithm to the type of coordination and learning parameters. We vary the number of active nodes with $N \in \{2, 10\}$. We use the same homogeneous traffic parameters as in section VI-A. Note that the exploration parameter δ and the learning rate η were adequately selected to provide good performance.

We compare the performance of our technique to the original IEEE 802.11 BEB technique and to the centralized learning approach. In centralized learning, there is only a single agent (e.g., residing in a cloud server) that collects individual throughput data from each transmitting node, performs gradient search and sends new CW values to the nodes. Therefore, in contrast to the distributed learning where agents have to estimate each others' throughputs, in centralized learning, the single-agent gets exact throughput values as measured by each transmitting node. Note that we do not model the communication delay between the nodes and the cloud server, which might be in the order of tens of milliseconds.

Fig. 3 and Fig. 4 show a representative evolution of individual contention windows, total network throughput, as well as allocation of air-time in the scenario with two and ten nodes, respectively. In each setting, the nodes start with the same CW value selected from $\{15, 1023\}$. First, we observe that nodes converge to similar CW values, as expected because of the homogeneous traffic, and the algorithm converges to equal air-time allocation and optimal total network throughput. Note that in the case of ten active nodes, the total throughput is around 20% higher than that achieved by WiFi. The algorithm converges faster in the case of ten nodes, as the utility function becomes steeper with an increased number of nodes [12]. The variability of CW is higher for ten nodes, as the node estimates become noisier. Nevertheless, the network operates with approximately optimal utility. Moreover, in the case of two nodes, we observe an interesting cooperative behavior where the initially more aggressive node slows down to free more air-time for its peer, then both nodes increase their aggressiveness to maximize the network utility. Note that the convergence speed is rather slow (i.e., in order of tens of seconds), so the learning-based schemes are useful in scenarios with long-lasting flows (e.g., video streaming).

Our results also show that the distributed algorithm provides similar performance as the centralized algorithm. Specifically, in a single collision domain and thanks to CSMA/CA channel access mechanism the throughput estimates computed by each learning agent are very accurate (i.e., close to the real values). Therefore, the exchange of those values is not needed and would only introduce additional delay slowing down the convergence even further. Moreover, the distributed algorithm behaves similarly with and without learning coordination, i.e., there is no significant advantage to coordination.

Finally, the three right-most columns in Fig. 3 and Fig. 4 show the convergence behavior with different learning rates

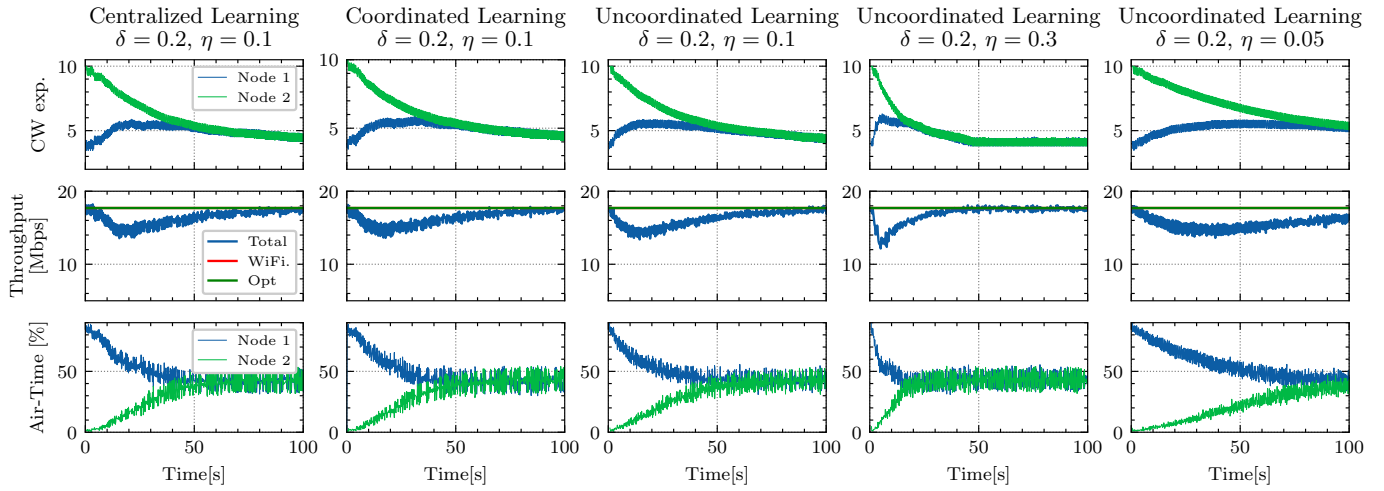


Fig. 3. Convergence of the proposed algorithm with two transmitting nodes.

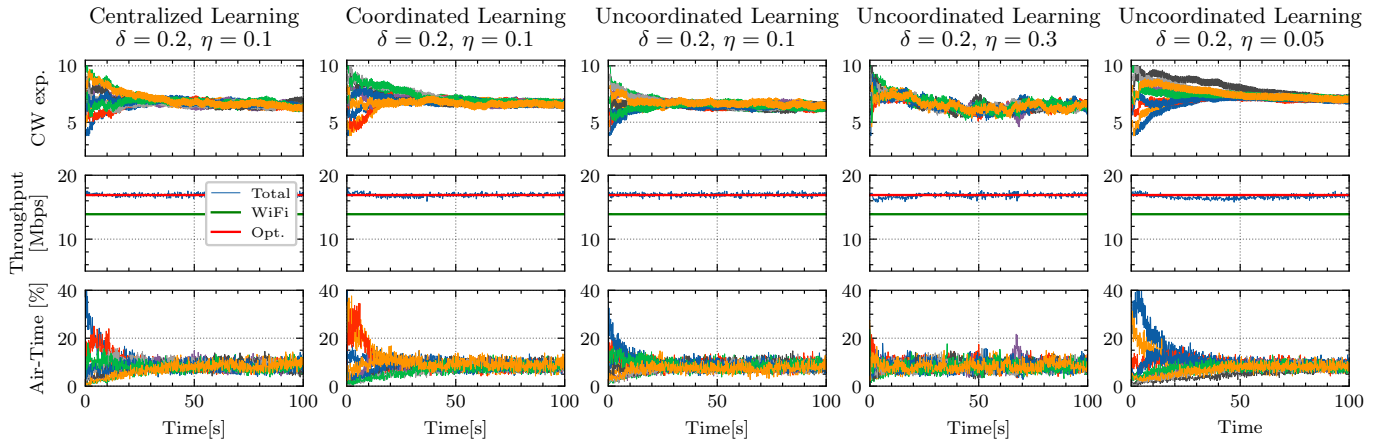


Fig. 4. Convergence of the proposed algorithm with ten transmitting nodes.

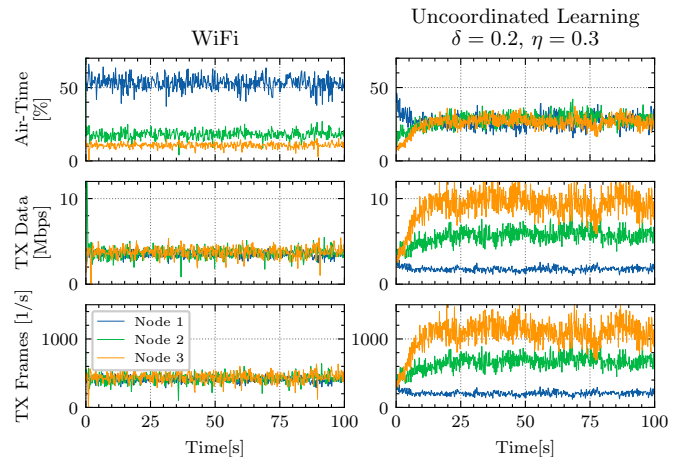
$\eta \in \{0.05, 0.1, 0.3\}$. Increasing the value of η allow the algorithm to take bigger steps and to converge faster in case of two nodes. But, when $N = 10$, the higher learning rate brings more fluctuations due to increased noise in the utility estimates. The evaluation with varying exploration parameters was skipped due to the space limit.

C. Heterogeneous Traffic

Here, we evaluate the performance of the algorithm under heterogeneous traffic, where the optimal CW values are not identical for all transmitting nodes. We consider two scenarios, where three nodes use diverse transmission parameters: *i*) the same data rate (MCS3, 26 Mbps), but diverse packet sizes $D_i \in \{250, 500, 1000\}$ B; *ii*) the same packet size (1500 B), but diverse data rates $M_i \in \{6.5, 26, 65\}$ Mbps.

In Fig. 5 and Fig. 6, we compare the performance of our distributed approach with standard WiFi operation. Specifically, we are interested in air-time allocation, individual throughputs and packets data rate. Due to the symmetric contention process, WiFi assures an equal number of transmission opportunities to all nodes, i.e., frame-fairness. Our results show the *performance anomaly* problem in WiFi, i.e., despite using

the higher data rate, the performance of the faster nodes is capped at that of the slowest station. In contrast, the proposed algorithm allows nodes to successfully and quickly converge to equal air-time allocation (i.e., proportional-fair allocation).


 Fig. 5. Air-time allocation, individual throughput and packet rate in case of heterogeneous traffic, i.e., all nodes use the same packet size of 1500 B, but different data rates $M_i \in \{6.5, 26, 65\}$ Mbps.

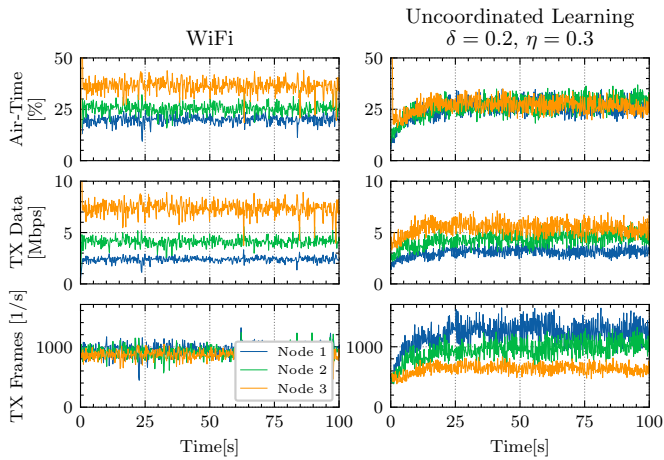


Fig. 6. Air-time allocation, individual throughput and packet rate in case of heterogenous traffic, i.e., all nodes use the same data rate of 26 Mbps (MCS3), but different packet sizes $D_i \in \{250, 500, 1000\}$ B.

D. Dynamic Scenario

Using a setup similar as in the previous sections, we evaluate the adaptability of the proposed algorithm to network dynamics. Specifically, we consider a dynamic scenario with three transmitters that change data rates (e.g., due to the change of wireless propagation condition). Fig. 7 shows the individual air-time allocation and throughput. The traffic is saturated, and nodes use a packet size of 1000 B. The nodes start with the same data rate of 13 Mbps (MCS2), then at time $t = 20$ s, nodes change the data rates (e.g., due to changing shadowing conditions): Node-1 switches to 6.5 Mbps (MCS0) and Node-2 switches to 65 Mbps (MCS7). At $t = 60$ s, nodes change data rates again, i.e., Node-1 switches to 65 Mbps (MCS7) and Node-2 switches to 6.5 Mbps (MCS0). Node-3 never changes its data rate.

We observe in Fig. 7 that the algorithm can adapt to the changes in data rates. The convergence takes around 10 s after the change occurs.

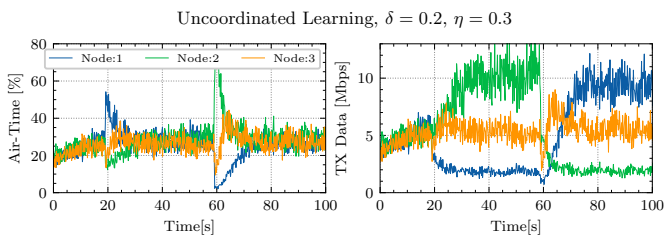


Fig. 7. Air-time allocation and individual throughput in dynamic scenario. Nodes start with the same data rate. At $t = 20$ s and $t = 60$ s, node 1 and 2 change the used data rate.

E. Unsaturated traffic

Here, we evaluate the behavior of the proposed algorithm under unsaturated traffic conditions. Specifically, we simulate two scenarios with three transmitting nodes, in which: *i*) the total offered load does not saturate the wireless channel, i.e., $r_i \in \{200, 400, 600\}$ pkts/s; *ii*) the total offered load saturates the wireless channel as one node operates with

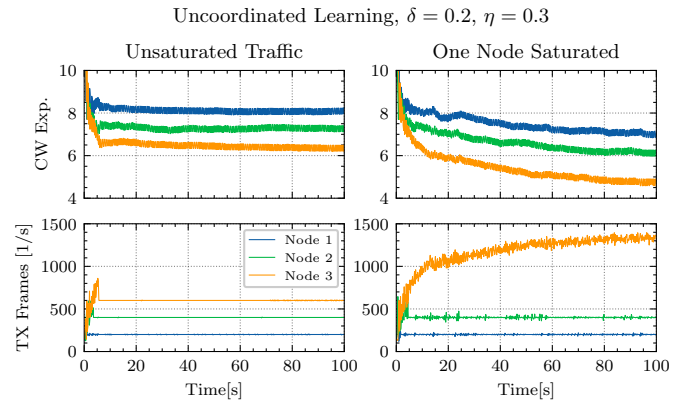


Fig. 8. Individual contention window and packet rate in unsaturated scenario (left) with offered load of $r_i \in \{200, 400, 600\}$ pkts/s and with one node saturated (right), i.e., $r_i \in \{200, 400, 2000\}$ pkts/s.

saturated traffic, i.e., $r_i \in \{200, 400, 2000\}$ pkts/s. The nodes use homogeneous transmission parameters, namely a data rate of 26 Mbps (MCS3), and a packet size of 1000 B.

Fig. 8 shows the evolution of individual contention window and packet rate in both scenarios. We observe that in the case of unsaturated traffic the nodes increase their aggressiveness until the offered load is satisfied. Next, they operate with a stable CW as the perturbation of the CW does not change the value of the network utility, and hence the estimated gradient equals zero. In the second scenario, the node with a high traffic load increases its aggressiveness until it saturates the wireless channel, but without negatively affecting the slower nodes, i.e., they also adapt their CW properly to get enough transmission opportunities and satisfy their own traffic.

F. Flow-In-the-Middle Topology

Finally, we evaluate the behavior of the proposed scheme in a flow-in-the-middle (FIM) topology – Fig. 9. The FIM topology is a simple multi-collision domain scenario, where nodes have asymmetric contention information. Specifically, the central transmitter can carrier sense transmissions of both its neighbors, while the edge transmitters cannot carrier sense each other. Therefore, the middle transmitter defers its transmissions whenever at least one of its neighbors transmits a frame, while concurrent transmissions of the edge nodes can occur. Note that the transmissions of the edge nodes may interleave, leaving no silent periods for the middle node. As a result, the throughput of the middle node is lowered due to the lack of transmission opportunities. In the worst case, the middle node suffers from complete starvation [16].

We simulate a scenario where all three transmitters use the same data rate of 26 Mbps (MCS3), and packet size

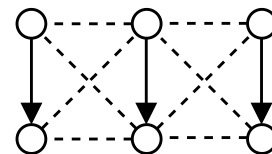


Fig. 9. Flow-In-the-Middle (FIM) Topology. In the network graph, vertices, dotted lines, and arrows represent nodes, connectivity, and flows, respectively.

of 1000B. The traffic is saturated. We disable the frame capture effect to simplify our simulation model. In the FIM topology, only the middle transmitter can estimate the global utility function, however only if frame transmissions of its neighbors are not colliding (i.e., the quality of estimation decreases when the edge nodes become more aggressive). The edge nodes can estimate the utility function only in their local collision domains. We consider two cases of CW learning, namely uncoordinated distributed learning, where nodes locally estimate the utility function, and centralized learning, where nodes perform gradient estimation procedure synchronously and they exchange (e.g., over a control channel) their own throughput values with all nodes to compute the value of the global function.

Fig. 10 shows the evolution of the individual CW and the air-time allocation, while the Fig. 11 shows the air-time allocation averaged over the simulation duration (i.e., 100 s). Our results confirm the problem of starvation of the middle node in the case of standard WiFi BEB operation. Specifically, the middle node gets only 5% of the channel air-time, while the edge nodes around 80%. We also show the optimal air-time allocation found with extensive simulations. The proposed algorithm improves the fairness among nodes, i.e., the middle node gets assigned more air-time while the edge nodes get less. In the case of centralized learning, the nodes can find the CW values leading to the optimal solution. However, in the case of uncoordinated learning, the distributed algorithm cannot converge. Instead, we can observe oscillations in the CW evolution caused by inconsistent goals, i.e., the middle node wants to achieve proportional fairness for three nodes, while the edge nodes optimize its operation for two nodes.

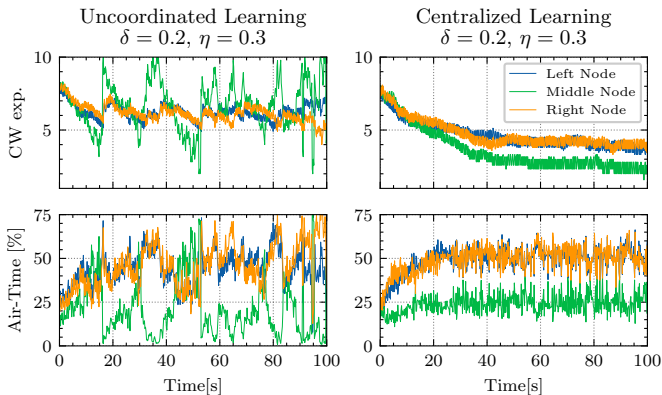


Fig. 10. The individual contention window and air-time allocation in FIM topology for uncoordinated learning with locally estimated utility (left) and centralized learning with global utility (right).

VII. CONCLUSIONS

In this paper, we apply a distributed Kiefer-Wolfowitz algorithm to a wireless network optimization problem. We address the distributed tuning of contention windows in WiFi networks and show that nodes can learn the proper contention windows values yielding proportional fair resource allocation even without explicit communication. Specifically, in the case of fully-connected topologies, they can individually estimate

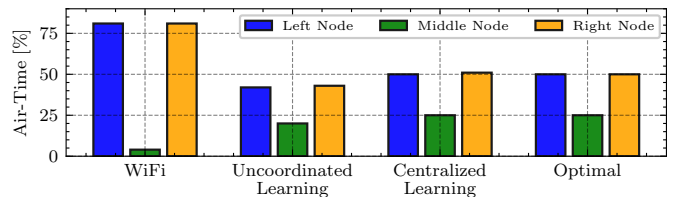


Fig. 11. The averaged air-time allocation attained by 802.11 WiFi and using the proposed learning-based approach in the FIM topology. Optimal air-time allocation is presented for comparison.

the global utility function by overhearing each others' transmissions and use it to maximize the log-convex optimization problem collaboratively. We have shown that the distributed algorithm converges albeit the strict mathematical assumptions used for the analytical proof of DA-KW do not hold. The convergence time (in order of tens of seconds) makes the learning-based algorithm suitable for long-lasting connections, such as video streaming or conference. In the topologies without full-connectivity nodes cannot estimate the global utility, therefore the exchange of individual throughput values is needed to make the distributed algorithm converge. The automatic tuning of the learning parameters, which might speed up the convergence, is left for further study.

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