

# EDAS Method for Multiple Attribute Group Decision Making with Probabilistic Uncertain Linguistic Information and Its Application to Green Supplier Selection

Yan He<sup>1</sup>, Fan Lei<sup>1</sup>, Guiwu Wei<sup>2\*</sup>, Rui Wang<sup>2</sup>, Jiang Wu<sup>3</sup>, Cun Wei<sup>3</sup>

<sup>1</sup> School of Mathematical Sciences, Sichuan Normal University, Chengdu, 610101, P.R. China

<sup>2</sup> School of Business, Sichuan Normal University, Chengdu, 610101, P.R. China

<sup>3</sup> School of Statistics, Southwestern University of Finance and Economics, Chengdu, 611130, P.R. China

## ARTICLE INFO

### Article History

Received 28 Sep 2019

Accepted 18 Oct 2019

### Keywords

Multiple attribute group decision making (MAGDM)

Probabilistic uncertain linguistic term sets (PULTSs)

Information entropy

EDAS method

Green supplier selection

## ABSTRACT

In order to adapt to the development of the new times, enterprises should not only care for the economic benefits, but also properly cope with environmental and social problems to achieve the integration of environmental, economic and social performance of sustainable development, so as to maximize the efficiency of resource use and minimize the negative effects of environmental pollution. Hence, in order to select a proper green supplier, integration of the information entropy and Evaluation based on Distance from Average Solution (EDAS) under probabilistic uncertain linguistic sets (PULTSs) offered a novel integrated model, in which information entropy is used for deriving priority weights of each attribute and EDAS with PULTSs is employed to obtain the final ranking of green supplier. Furthermore, in order to show the applicability of the proposed method, it is validated by a case study for green supplier selection along with some comparative analysis. Thus, the advantage of this proposed method is that it is simple to understand and easy to compute. The proposed method can also contribute to the selection of suitable alternative successfully in other selection issues.

© 2019 The Authors. Published by Atlantis Press SARL.

This is an open access article distributed under the CC BY-NC 4.0 license (<http://creativecommons.org/licenses/by-nc/4.0/>).

## 1. INTRODUCTION

The Evaluation based on Distance from Average Solution (EDAS) method was initially designed by Keshavarz Ghorabae, Zavadskas, Olfat and Turskis [1] to tackle the multi-criteria inventory classification (MCIC) problems which can also be employed for Multiple attribute decision making (MADM) or Multiple attribute group decision making (MAGDM) issues. The main advantage of the EDAS method has high efficiency and needs less computation in comparison with other decision making and classification methods. Stevic, Vasiljevic, Zavadskas, Sremac and Turskis [2] proposed fuzzy EDAS method to select the carpenter manufacturer. Keshavarz Ghorabae, Zavadskas, Amiri and Turskis [3] presented the EDAS method to cope with the MADM problems under the fuzzy environment for supplier selection. Keshavarz Ghorabae, Amiri, Zavadskas and Turskis [4] gave the extended EDAS method for dealing with MAGDM with interval type-2 fuzzy sets. Kahraman, Keshavarz Ghorabae, Zavadskas, Onar, Yazdani and Oztaysi [5] employed the interval-valued intuitionistic fuzzy EDAS method based on the membership, hesitance degrees and non-membership. Keshavarz Ghorabae, Amiri, Zavadskas, Turskis and Antucheviciene [6] proposed the stochastic EDAS method for MADM with normally distributed data. Keshavarz-Ghorabae, Amiri, Zavadskas, Turskis and Antucheviciene [7] analyzed the

rank reversal (RR) phenomenon in EDAS method which is compared with TOPSIS method by using a simulation-based analysis. Peng and Dai [8] designed the algorithms for interval neutrosophic EDAS method for MADM based on the MABAC and similarity measure. Zhang, Gao, Wei, Wei and Wei [9] developed the EDAS method for MAGDM with picture 2-tuple linguistic information. Feng, Wei and Liu [10] defined the EDAS method to solve the Hesitant Fuzzy Linguistic MADM. Mi and Liao [11] utilized the hesitant fuzzy BWM and hesitant fuzzy EDAS method for choosing commercial endowment insurance products. Zhang, Wei, Gao, Wei and Wei [12] proposed the EDAS method for multiple criteria group decision making with picture fuzzy information for green suppliers selections.

In many decision-making problems [13], it has been traditionally supposed that all information is depicted in the form of crisp numbers. However, most of decision makers' assessment information is imprecise or uncertain [14–18]. For example, the DMs may utilize the linguistic terms such as “bad,” “medium” and “good” when the satisficing degree of a car is appraised [19]. In order to assess the qualitative information easily, Herrera and Martinez [20] defined the linguistic term sets (2TLTSs) for computing with words. Furthermore, Rodriguez, Martinez and Herrera [21] proposed the hesitant fuzzy linguistic term sets (HFLTSSs) on the basis of hesitant fuzzy sets [22] and LTSs [23] which allow DMs to provide several possible linguistic variable. Liao, Yang and Xu [24]

\* Corresponding author. Email: weiguiwu@163.com

proposed the ELECTRE II method under HFLTS environment and developed two novel methods named score-deviation-based ELECTRE II model and positive and negative ideal-based ELECTRE II model. Zhang, Liang and Zhang [25] provided a new consensus reaching process in multiple attribute group decision making (MAGDM) with HFLTSs. Wei [26] gave the generalized dice similarity measures for MADDM with hesitant fuzzy linguistic information. However, in most existing researches on HFLTSs, all possible values are treated by the DMs have same weight or importance. Clearly, it is inconsistent with the real life. In both personal MADDM and MAGDM issues, the DMs may give possible linguistic terms so that these offered information may have not equal probability distributions. Thus, Pang, Wang and Xu [27] proposed the probabilistic linguistic term sets (PLTSs) to overcome this limits and defined a framework for ranking PLTSs with the score or deviation degree of each PLTS. Gou and Xu [28] formed the operational laws for HFLEs and PLTSs based on two equivalent transformation functions. Zhang, Xu and Liao [29] developed a consensus algorithm to analyze the GDM with probabilistic linguistic preference relations. Kobina, Liang and He [30] constructed some Probabilistic linguistic power operators for MAGDM with classical power aggregation operators [31-33]. Liao, Jiang, Xu, Xu and Herrera [34] came up with linear programming method to deal with the MADDM with probabilistic linguistic information. Chen, Wang and Wang [35] proposed probabilistic linguistic MULTIMOORA for cloud-based Enterprise Resource Planning (ERP) system selection. Liang, Kobina and Quan [36] proposed the probabilistic linguistic gray relational analysis (PL-GRA) for MAGDM based on geometric Bonferroni mean [37,38]. Bai, Zhang, Qian and Wu [39] used more appropriate comparison method and proposed a more efficient way to handle PLTSs. Cheng, Gu and Xu [40] investigated the venture capital group decision-making with interaction under probabilistic linguistic environment. Lu, Wei, Wu and Wei [41] designed the TOPSIS method for probabilistic linguistic MAGDM for supplier selection of new agricultural machinery products.

In some practical situations, a set of DMs may have their preferences to express their assessment information by using uncertain linguistic terms [42] in the GDM processes because of lack of sufficient knowledge and the fuzziness of human's thinking. However, these uncertain linguistic terms are different from each other and also the number of occurrences of each uncertain linguistic term is different. Inspired by the idea based on PLTSs [27] and uncertain linguistic term [42], Lin, Xu, Zhai and Yao [43] came up with a new concept of probabilistic uncertain linguistic term set (PULTS) in order to model and operate the uncertain linguistic information in the GDM issues. Xie, Ren, Xu and Wang [44] built the probabilistic uncertain linguistic preference relation (PULPR) and the normalized PULPR and designed the distance measure and similarity degree measure the consensus degree. But there are no studies on the EDAS method for MAGDM under PULTSs in the existing literature. Therefore, it is necessary to pay attention to this issue. The goal of such paper is to design the EDAS method to tackle the MAGDM with the PULTSs. The originality of the paper can be highlighted as follows: (1) the EDAS method is modified by PULTSs; (2) the probabilistic uncertain linguistic EDAS (PUL-EDAS) method is designed to tackle the MAGDM issues with PULTSs; (3) a case study for green supplier selection is designed

to proof the developed method; (4) some comparative studies are given with the PULWA operator, PUL-TOPSIS method and uncertain linguistic weighted average (ULWA) operator to verify the rationality of PUL-EDAS method.

The remainder section of such paper is designed as follows. Section 2 reviews some basic concepts related to PULTSs. In Section 3, the EDAS method is designed for MAGDM issues under PULTSs. In Section 4, a detailed case study for green supplier selection is designed and some comparative analysis is investigated. The study ends with some meaningful conclusions in Section 5.

## 2. PRELIMINARIES

Firstly, Xu [45] defined the additive linguistic evaluation scale and Gou, Xu and Liao [46] defined the corresponding transformation function between the linguistic terms and  $[0, 1]$ .

**Definition 1.** [45,46] Let  $L = \{l_\alpha | \alpha = -\theta, \dots, -2, -1, 0, 1, 2, \dots, \theta\}$  be an LTS [45], the linguistic terms  $l_\alpha$  can express the equivalent information to  $\beta$  is derived by the transformation function  $g$  [46]:

$$g: [L_{-\theta}, l_\theta] \rightarrow [0, 1], g(l_\alpha) = \frac{\alpha + \theta}{2\theta} = \beta \tag{1}$$

At the same time,  $\beta$  can be expressed the equivalent information to the linguistic terms  $l_\alpha, \beta$  which is derived by the transformation function  $g^{-1}$ :

$$g^{-1}: [0, 1] \rightarrow [L_{-\theta}, l_\theta], g^{-1}(\beta) = l_{(2\beta-1)\theta} = l_\alpha \tag{2}$$

In order to strengthen the modeling capability of HFLTSs, Pang, Wang and Xu [27] proposed the definition of PLTSs to link each linguistic term with a probability value.

**Definition 2.** [27] Given an LTS  $L = \{l_j | j = -\theta, \dots, -2, -1, 0, 1, 2, \dots, \theta\}$ , a PLTS is defined as:

$$L(p) = \left\{ l^{(\phi)}(p^{(\phi)}) \mid l^{(\phi)} \in L, p^{(\phi)} \geq 0, \phi = 1, 2, \dots, \#L(p), \sum_{\phi=1}^{\#L(p)} p^{(\phi)} \leq 1 \right\} \tag{3}$$

where  $l^{(\phi)}(p^{(\phi)})$  is the  $\phi$ th linguistic term  $l^{(\phi)}$  associated with the probability value  $p^{(\phi)}$ , and  $\#L(p)$  is the length of linguistic terms in  $L(p)$ . The linguistic term  $l^{(\phi)}$  in  $L(p)$  are arranged in ascending order.

In order to depict the DMs' uncertainty accurately, Lin, Xu, Zhai and Yao [43] put forward a novel concept called PULTS based on uncertain linguistic term [42] and PLTSs.

**Definition 3.** [43] A PULTS could be defined as follows:

$$PULTS(p) = \left\{ [L^\phi, U^\phi](p^\phi) \mid p^\phi \geq 0, \phi = 1, 2, \dots, \#PULTS(p), \sum_{\phi=1}^{\#PULTS(p)} p^\phi \leq 1 \right\} \tag{4}$$

where  $[L^\phi, U^\phi](p^\phi)$  represents the uncertain linguistic term  $[L^\phi, U^\phi]$  associated with the probability  $p^\phi$ ,  $L^\phi, U^\phi$  are LTSs,  $L^\phi \leq U^\phi$ , and  $\#PULT(p)$  is the cardinality of  $PULTS(p)$ .

In order to easy computation, Pang, Wang and Xu [27] normalized the PLTS  $L(p)$  as  $\tilde{L}(p) = \left\{ l^{(\phi)}(\tilde{p}^{(\phi)}) \mid l^{(\phi)} \in L, \tilde{p}^{(\phi)} \geq 0, \phi = 1, 2, \dots, \#L(\tilde{p}), \sum_{\phi=1}^{\#L(\tilde{p})} \tilde{p}^{(\phi)} = 1 \right\}$ , where  $\tilde{p}^{(\phi)} = p^{(\phi)} / \sum_{\phi=1}^{\#L(p)} p^{(\phi)}$  for all  $\phi = 1, 2, \dots, \#L(\tilde{p})$ .

**Definition 4.** [43] Let  $PULTS_1(p) = \left\{ [L_1^\phi, U_1^\phi](p_1^\phi) \mid \phi = 1, 2, \dots, \#PULTS_1(p) \right\}$  and  $PULTS_2(p) = \left\{ [L_2^\phi, U_2^\phi](p_2^\phi) \mid \phi = 1, 2, \dots, \#PULTS_2(p) \right\}$  be two PULTSs, where  $\#PULTS_1(p)$  and  $\#PULTS_2(p)$  are the numbers of PULTSs  $PULTS_1(p)$  and  $PULTS_2(p)$ , respectively. If  $\#PULTS_1(p) > \#PULTS_2(p)$ , then add  $\#PULTS_1(p) - \#PULTS_2(p)$  linguistic terms to  $PULTS_2(p)$ . Moreover, the added uncertain linguistic terms should be the smallest linguistic term in  $PULTS_2(p)$  and the probabilities of added linguistic terms should be zero.

**Definition 5.** [43] For a PULTS  $PULTS(p) = \{[L^\phi, U^\phi](p^\phi) \mid \phi = 1, 2, \dots, \#PULTS(p)\}$ , the expected value  $E(PULTS(p))$  and deviation degree  $\sigma(PULTS(p))$  of  $PULTS(p)$  is defined:

$$E(PULTS(p)) = \frac{\sum_{\phi=1}^{\#PULTS(p)} \left( \frac{g(L^\phi)p^\phi + g(U^\phi)p^\phi}{2} \right)}{\sum_{\phi=1}^{\#PULTS(p)} p^\phi} \tag{5}$$

$$\sigma(PULTS(p)) = \frac{\sqrt{\sum_{\phi=1}^{\#PULTS(p)} \left( \frac{g(L^\phi)p^\phi + g(U^\phi)p^\phi}{2} - E(PULTS(p)) \right)^2}}{\sum_{\phi=1}^{\#PULTS(p)} p^\phi} \tag{6}$$

By using the Eqs. (4) and (5), the order relation between two PULTSs is defined as: (1) if  $E(PULTS_1(p)) > E(PULTS_2(p))$ , then  $PULTS_1(p) > PULTS_2(p)$ ; (2) if  $E(PULTS_1(p)) = E(PULTS_2(p))$ , then if  $\sigma(PULTS_1(p)) = \sigma(PULTS_1(p))$ , then  $PULTS_1(p) = PULTS_2(p)$ ; if  $\sigma(PULTS_1(p)) < \sigma(PULTS_1(p))$ , then,  $PULTS_1(p) > PULTS_2(p)$ .

**Definition 6.** Let  $PULTS_1(p) = \left\{ [L_1^\phi, U_1^\phi](p_1^\phi) \mid \phi = 1, 2, \dots, \#PULTS_1(p) \right\}$  and  $PULTS_2(p) = \left\{ [L_2^\phi, U_2^\phi](p_2^\phi) \mid \phi = 1, 2, \dots, \#PULTS_2(p) \right\}$  be two PULTSs with  $\#PULTS_1(p) = \#PULTS_2(p) = \#PULTS(p)$ , then Hamming distance  $d(PULTS_1(p), PULTS_2(p))$

between  $PULTS_1(p)$  and  $PULTS_2(p)$  is defined as follows:

$$d(PULTS_1(p), PULTS_2(p)) = \frac{\sum_{\phi=1}^{\#L_1(\tilde{p})} \left( \left( g(L_1^\phi)p^\phi - g(L_2^\phi)p^\phi \right) + \left( g(U_1^\phi)p^\phi - g(U_2^\phi)p^\phi \right) \right)}{2\#PULTS(p)} \tag{7}$$

### 3. EDAS METHOD FOR PROBABILISTIC UNCERTAIN LINGUISTIC MAGDM PROBLEMS

In such section, we design a new probabilistic uncertain linguistic EDAS (PUL-EDAS) method for MAGDM issues. The following mathematical notations are employed to cope with the probabilistic uncertain linguistic MAGDM problems. Let  $A = \{A_1, A_2, \dots, A_m\}$  be a discrete set of chosen alternatives, and  $G = \{G_1, G_2, \dots, G_n\}$  with weight vector  $w = (w_1, w_2, \dots, w_n)$ , where  $w_j \in [0, 1], j = 1, 2, \dots, n, \sum_{j=1}^n w_j = 1$ , and a set of experts  $E = \{E_1, E_2, \dots, E_q\}$ . Suppose that  $G_j$  are assessed by expert  $E_k$  for  $A_i$  and depicted as uncertain linguistic expressions  $[L_{ij}^k, U_{ij}^k]$  ( $i = 1, 2, \dots, m, j = 1, 2, \dots, n, k = 1, 2, \dots, q$ ).

Then, PUL-EDAS method is proposed to solve the MAGDM problems. The designed calculating steps are involved as follows:

**Step 1.** Shift cost attribute into beneficial attribute. If the cost attribute value is  $[l_\alpha, l_\beta]$ , then the corresponding beneficial attribute value is  $[l_\beta, l_\alpha]$ .

**Step 2.** Transform the uncertain linguistic information  $[L_{ij}^k, U_{ij}^k]$  ( $i = 1, 2, \dots, m, j = 1, 2, \dots, n, k = 1, 2, \dots, q$ ) into probabilistic uncertain linguistic decision matrix (PULDM)  $PULDM = (PULDM_{ij}(p))_{m \times n}$ ,  $PULDM_{ij}(p) = \left\{ [L_{ij}^\phi, U_{ij}^\phi](p_{ij}^\phi) \mid \phi = 1, 2, \dots, \#PULDM_{ij}(p) \right\}$  ( $i = 1, 2, \dots, m, j = 1, 2, \dots, n$ ).

**Step 3.** Calculate the normalized PULDM  $NPULDM = (NPULDM_{ij}(p))_{m \times n}$ .

**Step 4.** Compute the weight values for attributes.

Entropy [47] is a conventional term from information theory which is also famous as the average amount of information contained in each attribute. The larger the value of entropy in a given attribute is, the smaller the differences in the ratings of alternatives with respect to this attribute. In turn, this means that this kind of attribute supplies less information and has a smaller weight. Firstly, the normalized decision matrix  $NPULNDM_{ij}(p)$  is derived as follows:

$$NPULNDM_{ij}(p) = \frac{\sum_{\phi=1}^{\#NPULDM_{ij}(p)} \left( \frac{g(L_{ij}^\phi)p_{ij}^\phi + g(U_{ij}^\phi)p_{ij}^\phi}{2} \right)}{\sum_{i=1}^m \sum_{\phi=1}^{\#NPULDM_{ij}(p)} \left( \frac{g(L_{ij}^\phi)p_{ij}^\phi + g(U_{ij}^\phi)p_{ij}^\phi}{2} \right)} \tag{8}$$

$j = 1, 2, \dots, n$

Then, the vector of Shannon entropy  $E = (E_1, E_2, \dots, E_n)$  is computed:

$$E_j = -\frac{1}{\ln m} \sum_{i=1}^m NPULNDM_{ij}(p) \ln NPULNDM_{ij}(p) \quad (9)$$

and  $NPULNDM_{ij}(p) \ln NPULNDM_{ij}(p)$  is defined as 0, if  $NPULNDM_{ij}(p) = 0$ .

Finally, the vector of attribute weights  $w = (w_1, w_2, \dots, w_n)$  is computed:

$$w_j = \frac{1 - E_j}{\sum_{j=1}^n (1 - E_j)}, j = 1, 2, \dots, n \quad (10)$$

**Step 5.** Determine the probabilistic uncertain linguistic average values in accordance with all attributes, shown as follows:

$$PULAV = (PULAV_j)_{1 \times n} \quad (11)$$

$$PULAV_j = \left\{ [L_j^\phi, U_j^\phi] (p_j^\phi) \mid \phi = 1, 2, \dots, \#NPULDM_{ij}(p) \right\} \quad (12)$$

$$[L_j^\phi, U_j^\phi] (p_j^\phi) = \left[ \frac{\sum_{i=1}^m L_{ij}^\phi}{m}, \frac{\sum_{i=1}^m U_{ij}^\phi}{m} \right] \left[ \frac{\sum_{i=1}^m p_{ij}^\phi}{m} \right] \quad (13)$$

**Step 6.** The probabilistic uncertain linguistic positive distance from average (PULPDA) and probabilistic uncertain linguistic negative distance from average (PULNDA) matrix can be got by Eqs. (14-19) on the basis of attribute type (benefit or cost).

$$PULPDA = [PULPDA_{ij}]_{m \times n} \quad (14)$$

$$PULNDA = [PULNDA_{ij}]_{m \times n} \quad (15)$$

If  $j$ th attribute is beneficial type,

$$PULPDA_{ij} = \frac{\max(0, d(NPULDM_{ij}(p), PULAV_j))}{E(PULAV_j)} \quad (16)$$

$$PULNDA_{ij} = \frac{\max(0, d(PULAV_j, NPULDM_{ij}(p)))}{E(PULAV_j)} \quad (17)$$

If  $j$ th attribute is cost type,

$$PULPDA_{ij} = \frac{\max(0, d(PULAV_j, NPULDM_{ij}(p)))}{E(PULAV_j)} \quad (18)$$

$$PULNDA_{ij} = \frac{\max(0, d(NPULDM_{ij}(p), PULAV_j))}{E(PULAV_j)} \quad (19)$$

**Step 7.** The weighted sum of PULPDA and PULNDA can be calculated by Eqs. (20) and (21), respectively.

$$PULSP_i = \sum_{j=1}^m w_j PULPDA_{ij} \quad (20)$$

$$PULSN_i = \sum_{j=1}^m w_j PULNDA_{ij} \quad (21)$$

**Step 8.** The value of probabilistic uncertain linguistic weighted sum of PULPDA (PULSP) and probabilistic uncertain linguistic weighted sum of PULNDA (PULSN) for each alternative can be normalized by Eqs. (22) and (23), respectively:

$$PULNSP_i = \frac{PULSP_i}{\max_i(PULSP_i)} \quad (22)$$

$$PULNSN_i = 1 - \frac{PULSN_i}{\max_i(PULSN_i)} \quad (23)$$

**Step 9.** The probabilistic uncertain linguistic appraisal score (PULAS) for all alternatives can be got by Eq. (24).

$$PULAS_i = \frac{PULNSP_i + PULNSN_i}{2} \quad (24)$$

where  $0 \leq PULAS_i \leq 1$ .

**Step 10.** Rank the alternatives according to the decreasing values of assessment score  $PULAS_i$ , the alternative with maximum value is the best choice.

As aforementioned, firstly, the uncertain linguistic information is transformed into PULDM. Then, normalized PULDM is derived from the PULDM. In order to select optimal alternative, integration of the information entropy and EDAS method under probabilistic uncertain linguistic sets (PULTSs) offered a novel integrated model, in which information entropy is used for deriving priority weights of each attribute and EDAS with PULTSs is employed to obtain the final ranking of all alternatives.

## 4. A CASE STUDY AND COMPARATIVE ANALYSIS

### 4.1. A Case Study

The choice of long-term stable suppliers is the most important problem to build a green supply chain under the green supply chain management mode, which directly affects the competitiveness of enterprises in the market. How can enterprises grasp the changeable internal and external environment, determine reasonable evaluation indicators according to their own needs, and choose suitable green suppliers becomes an urgent problem to be solved. The selection process of green suppliers should not place too much emphasis on environmental protection factors or economic benefits. Only by coordinating the development of the two can the long-term cooperation between enterprises and suppliers be promoted. Green supplier selection is a very complex decision problem [48-53]. Due to the complexity of the green supply chain system and the uncertainty and hesitation of human thinking, the evaluation of green suppliers will be affected by many uncertain factors, which makes it difficult to describe the evaluation index with exact values. In order to better conform to the thinking mode and cognitive mode of decision makers, this paper adopts language expression to describe attribute values. With the rapid development of science and technology, many decision-making problems in life have become more



and more complex. It is difficult to solve these problems simply by one decision-maker. Multiple decision makers making decisions together can not only reduce errors, but also improve the accuracy of decisions [54–59]. Therefore, it is of great significance to apply the MAGDM method of PULTS to green supplier selection. Thus, in this section we present a numerical example for green supplier selection to illustrate the proposed method in this paper. There is a panel with five possible green suppliers  $A_i$  ( $i = 1, 2, 3, 4, 5$ ) to select. The experts selects four beneficial attribute to evaluate the five possible green suppliers: ① $G_1$  is environmental improvement quality; ② $G_2$  is transportation cost of suppliers; ③ $G_3$  is green image and financial conditions; ④ $G_4$  is environmental competencies. The transportation cost ( $G_2$ ) is cost attribute, others are beneficial attributes. The five possible green suppliers  $A_i$  ( $i = 1, 2, 3, 4, 5$ ) are to be evaluated by using the LTS

$$S = \{s_{-3} = \textit{extremely poor (EP)}, s_{-2} = \textit{verypoor (VP)}, s_{-1} = \textit{poor (P)}, s_0 = \textit{medium (M)}, s_1 = \textit{good (G)}, s_2 = \textit{verygood (VG)}, s_3 = \textit{extremelygood (EG)}\}$$

by the five decision makers under the above four attributes, as listed in the Tables 1–5.

In the following, we utilize the PUL-EDAS method developed for green supplier selection.

**Step 1.** Shift cost attribute  $G_2$  into beneficial attribute. If the cost attribute value is  $[s_\alpha, s_\beta]$  ( $-3 \leq \alpha, \beta \leq 3$ ), then the corresponding beneficial attribute value is  $[s_{-\beta}, s_{-\alpha}]$  (See Tables 6–10).

**Step 2.** Transform the uncertain linguistic variables into PULDM (Table 11).

**Table 1** | Uncertain linguistic decision matrix by the first DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[VG, EG]	[M, G]	[VP, P]
$A_2$	[P, G]	[G, VG]	[M, G]	[G, VG]
$A_3$	[G, VG]	[P, M]	[G, VG]	[EP, VP]
$A_4$	[M, G]	[M, VG]	[G, VG]	[M, G]
$A_5$	[M, G]	[P, M]	[M, VG]	[G, VG]

DM = decision maker.

**Table 2** | Uncertain linguistic decision matrix by the second DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[M, G]	[G, VG]	[P, G]
$A_2$	[M, G]	[G, VG]	[M, G]	[VG, EG]
$A_3$	[VP, P]	[P, M]	[G, VG]	[P, M]
$A_4$	[G, VG]	[M, G]	[G, EG]	[M, G]
$A_5$	[M, G]	[P, M]	[M, G]	[P, M]

DM = decision maker.

**Table 3** | Uncertain linguistic decision matrix by the third DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[G, VG]	[VG, EG]	[P, G]
$A_2$	[G, VG]	[P, M]	[G, VG]	[G, VG]
$A_3$	[M, G]	[P, M]	[VG, EG]	[P, M]
$A_4$	[G, VG]	[M, G]	[VP, P]	[G, VG]
$A_5$	[P, M]	[VP, P]	[M, VG]	[M, VG]

DM = decision maker.

**Table 4** | Uncertain linguistic decision matrix by the fourth DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, VG]	[M, G]	[VG, EG]	[M, G]
$A_2$	[M, G]	[G, VG]	[P, M]	[VG, EG]
$A_3$	[M, G]	[M, G]	[VG, EG]	[G, VG]
$A_4$	[G, VG]	[G, VG]	[G, EG]	[VG, EG]
$A_5$	[G, VG]	[VP, P]	[M, VG]	[M, VG]

DM = decision maker.

**Table 5** | Uncertain linguistic decision matrix by the fifth DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[G, VG]	[VG, EG]	[P, G]
$A_2$	[G, VG]	[M, G]	[M, G]	[VG, EG]
$A_3$	[VP, P]	[M, G]	[VG, EG]	[P, M]
$A_4$	[VG, EG]	[M, G]	[G, EG]	[VG, EG]
$A_5$	[P, M]	[VP, P]	[VG, EG]	[M, VG]

DM = decision maker.

**Table 6** | Uncertain linguistic decision matrix by the first DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[EP, VP]	[M, G]	[VP, P]
$A_2$	[P, G]	[VP, P]	[M, G]	[G, VG]
$A_3$	[G, VG]	[M, G]	[G, VG]	[EP, VP]
$A_4$	[M, G]	[VP, M]	[G, VG]	[M, G]
$A_5$	[M, G]	[M, G]	[M, VG]	[G, VG]

DM = decision maker.

**Table 7** | Uncertain linguistic decision matrix by the second DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[P, M]	[G, VG]	[P, G]
$A_2$	[M, G]	[VP, P]	[M, G]	[VG, EG]
$A_3$	[VP, P]	[M, G]	[G, VG]	[P, M]
$A_4$	[G, VG]	[P, M]	[G, EG]	[M, G]
$A_5$	[M, G]	[M, G]	[M, G]	[P, M]

DM = decision maker.

**Table 8** | Uncertain linguistic decision matrix by the third DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, G]	[VP, P]	[VG, EG]	[P, G]
$A_2$	[G, VG]	[M, G]	[G, VG]	[G, VG]
$A_3$	[M, G]	[M, G]	[VG, EG]	[P, M]
$A_4$	[G, VG]	[P, M]	[VP, P]	[G, VG]
$A_5$	[P, M]	[G, VG]	[M, VG]	[M, VG]

DM = decision maker.

**Table 9** | Uncertain linguistic decision matrix by the fourth DM.

Alternatives	$G_1$	$G_2$	$G_3$	$G_4$
$A_1$	[M, VG]	[P, M]	[VG, EG]	[M, G]
$A_2$	[M, G]	[VP, P]	[P, M]	[VG, EG]
$A_3$	[M, G]	[P, M]	[VG, EG]	[G, VG]
$A_4$	[G, VG]	[VP, P]	[G, EG]	[VG, EG]
$A_5$	[G, VG]	[G, VG]	[M, VG]	[M, VG]

DM = decision maker.

**Table 10** | Uncertain linguistic decision matrix by the fifth DM.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	[M, G]	[VP, P]	[VG, EG]	[P, G]
A <sub>2</sub>	[G, VG]	[P, M]	[M, G]	[VG, EG]
A <sub>3</sub>	[VP, P]	[P, M]	[VG, EG]	[P, M]
A <sub>4</sub>	[VG, EG]	[P, M]	[G, EG]	[VG, EG]
A <sub>5</sub>	[P, M]	[G, VG]	[VG, EG]	[M, VG]

DM = decision maker.

**Table 11** | Probabilistic uncertain linguistic decision matrix.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.8⟩, ⟨[l <sub>0</sub> , l <sub>2</sub> ], 0.2⟩}	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.4⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.2⟩}	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.6⟩}	{⟨[l <sub>-2</sub> , l <sub>-1</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>-1</sub> , l <sub>1</sub> ], 0.6⟩}
A <sub>2</sub>	{⟨[l <sub>-1</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.4⟩}	{⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.6⟩}	{⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.6⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩}	{⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.4⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.6⟩}
A <sub>3</sub>	{⟨[l <sub>-2</sub> , l <sub>-1</sub> ], 0.4⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩}	{⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.6⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩}	{⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.4⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.6⟩}	{⟨[l <sub>-3</sub> , l <sub>-2</sub> ], 0.2⟩, ⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.6⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩}
A <sub>4</sub>	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.6⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.2⟩}	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.6⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>2</sub> ], 0.2⟩}	{⟨[l <sub>-2</sub> , l <sub>-1</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>3</sub> ], 0.6⟩}	{⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.4⟩}
A <sub>5</sub>	{⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.4⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.4⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩}	{⟨[l <sub>-2</sub> , l <sub>-1</sub> ], 0.6⟩, ⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.4⟩}	{⟨[l <sub>0</sub> , l <sub>2</sub> ], 0.6⟩, ⟨[l <sub>0</sub> , l <sub>1</sub> ], 0.2⟩, ⟨[l <sub>2</sub> , l <sub>3</sub> ], 0.2⟩}	{⟨[l <sub>-1</sub> , l <sub>0</sub> ], 0.2⟩, ⟨[l <sub>1</sub> , l <sub>2</sub> ], 0.2⟩, ⟨[l <sub>0</sub> , l <sub>2</sub> ], 0.6⟩}

**Step 3.** Calculate the normalized PULDM (Table 12).

**Step 4.** Compute the weight values for attributes from Eqs. (8–10):  $w_1 = 0.1195, w_2 = 0.3955, w_3 = 0.0954, w_4 = 0.3896$ .

**Step 5.** Determine the  $PULAV_i (i = 1, 2, 3, 4, 5)$  for all attributes (Table 13).

**Step 6.** Compute the PULPDA and PULNDA matrix by Eqs. (14–19), which are listed in Tables 14 and 15.

**Step 7.** Calculate the  $PULSP_i, PULSN_i (i = 1, 2, 3, 4, 5)$  by using Eqs. (20) and (21). The calculating results are derived in Table 16.

**Step 8.** Calculate the  $PULNSP_i, PULNSN_i (i = 1, 2, 3, 4, 5)$  by using Eqs. (22) and (23). The calculating results are derived in Table 17.

**Step 9.** Calculate the  $PULAS_i (i = 1, 2, 3, 4, 5)$  by using Eq. (24) which is depicted in Table 18.

**Step 10.** According to the  $PULAS_i (i = 1, 2, 3, 4, 5)$ , we can rank all the green suppliers. Obviously, the rank is:  $A_2 > A_4 > A_1 > A_5 > A_3$  and the best green supplier is  $A_2$ .

### 4.2. Comparative Analysis

In such subsection, we shall compare our proposed method with PULWA operator[43], probabilistic uncertain linguistic TOPSIS method (PUL-TOPSIS method) [43] and ULWA operator [42].

#### 4.2.1. Compared with PULWA operator

Firstly, we compare our proposed method with probabilistic uncertain linguistic weighted average (PULWA) operator [43], the weight

vector of attributes is derived as:  $w_1 = 0.1195, w_2 = 0.3955, w_3 = 0.0954, w_4 = 0.3896$ , then the overall attribute value of each alternative  $Z_i(w) (i = 1, 2, 3, 4, 5)$  is obtained by employing PULWA operator.

$$Z_1(w) = \{[l_{-0.1558}, l_{0.0994}], [l_{0.0604}, l_{0.4621}], [l_{0.2846}, l_{0.6277}]\}$$

$$Z_2(w) = \{[l_{-0.1101}, l_{0.0000}], [l_{0.1558}, l_{0.5078}], [l_{0.7717}, l_{1.3097}]\}$$

$$Z_3(w) = \{[l_{-0.3294}, l_{-0.2036}], [l_{-0.4329}, l_{0.1241}], [l_{0.2163}, l_{0.5335}]\}$$

$$Z_4(w) = \{[l_{-0.0381}, l_{0.1607}], [l_{0.1973}, l_{0.6715}], [l_{0.5354}, l_{0.8624}]\}$$

$$Z_5(w) = \{[l_{-0.1257}, l_{0.0477}], [l_{-0.4460}, l_{-0.0154}], [l_{0.0986}, l_{0.4946}]\}$$

Then, the score values of these five overall attribute values of each alternative  $Z_i(w) (i = 1, 2, 3, 4, 5)$  are obtained by Definition 9 [43] as follows:

$$E(Z_1(w)) = l_{0.2297}, E(Z_2(w)) = l_{0.4391}, E(Z_3(w)) = l_{-0.0154}$$

$$E(Z_4(w)) = l_{0.3982}, E(Z_5(w)) = l_{0.0090}$$

Furthermore, we can derive the ranking result:  $A_2 > A_4 > A_1 > A_5 > A_3$ . Thus, we have the same optimal green supplier of coal enterprises  $A_2$ .

#### 4.2.2. Compared with PUL-TOPSIS method

Then, we compare our proposed method with probabilistic uncertain linguistic TOPSIS method (PUL-TOPSIS method) [43], then we can acquire the calculating results and sorting results (Table 19). Thus, we have the same optimal green supplier of coal enterprises  $A_4$ .

**Table 12** | Normalized probabilistic uncertain linguistic decision matrix.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	$\left\{ \langle [l_0, l_1], 0 \rangle, \langle [l_0, l_1], 0.9 \rangle, \langle [l_1, l_2], 0.1 \rangle \right\}$	$\left\{ \langle [l_0, l_1], 0.4 \rangle, \langle [l_1, l_2], 0.4 \rangle, \langle [l_2, l_3], 0.2 \rangle \right\}$	$\left\{ \langle [l_0, l_1], 0.2 \rangle, \langle [l_1, l_2], 0.2 \rangle, \langle [l_2, l_3], 0.6 \rangle \right\}$	$\left\{ \langle [l_{-2}, l_{-1}], 0.2 \rangle, \langle [l_{-1}, l_0], 0.3 \rangle, \langle [l_0, l_1], 0.5 \rangle \right\}$
A <sub>2</sub>	$\left\{ \langle [l_{-1}, l_0], 0.1 \rangle, \langle [l_0, l_1], 0.5 \rangle, \langle [l_1, l_2], 0.4 \rangle \right\}$	$\left\{ \langle [l_{-1}, l_0], 0.2 \rangle, \langle [l_0, l_1], 0.2 \rangle, \langle [l_1, l_2], 0.6 \rangle \right\}$	$\left\{ \langle [l_{-1}, l_0], 0.2 \rangle, \langle [l_0, l_1], 0.6 \rangle, \langle [l_1, l_2], 0.2 \rangle \right\}$	$\left\{ \langle [l_1, l_2], 0 \rangle, \langle [l_1, l_2], 0.4 \rangle, \langle [l_2, l_3], 0.6 \rangle \right\}$
A <sub>3</sub>	$\left\{ \langle [l_{-2}, l_{-1}], 0.4 \rangle, \langle [l_0, l_1], 0.4 \rangle, \langle [l_1, l_2], 0.2 \rangle \right\}$	$\left\{ \langle [l_{-1}, l_0], 0 \rangle, \langle [l_{-1}, l_0], 0.6 \rangle, \langle [l_0, l_1], 0.4 \rangle \right\}$	$\left\{ \langle [l_1, l_2], 0 \rangle, \langle [l_1, l_2], 0.4 \rangle, \langle [l_2, l_3], 0.6 \rangle \right\}$	$\left\{ \langle [l_{-3}, l_{-2}], 0.2 \rangle, \langle [l_{-1}, l_0], 0.6 \rangle, \langle [l_1, l_2], 0.2 \rangle \right\}$
A <sub>4</sub>	$\left\{ \langle [l_0, l_1], 0.2 \rangle, \langle [l_1, l_2], 0.6 \rangle, \langle [l_2, l_3], 0.2 \rangle \right\}$	$\left\{ \langle [l_0, l_1], 0 \rangle, \langle [l_0, l_1], 0.7 \rangle, \langle [l_1, l_2], 0.3 \rangle \right\}$	$\left\{ \langle [l_{-2}, l_{-1}], 0.2 \rangle, \langle [l_1, l_2], 0.5 \rangle, \langle [l_2, l_3], 0.3 \rangle \right\}$	$\left\{ \langle [l_0, l_1], 0.4 \rangle, \langle [l_1, l_2], 0.2 \rangle, \langle [l_2, l_3], 0.4 \rangle \right\}$
A <sub>5</sub>	$\left\{ \langle [l_{-1}, l_0], 0.4 \rangle, \langle [l_0, l_1], 0.4 \rangle, \langle [l_1, l_2], 0.2 \rangle \right\}$	$\left\{ \langle [l_{-2}, l_{-1}], 0.0 \rangle, \langle [l_{-2}, l_{-1}], 0.6 \rangle, \langle [l_{-1}, l_0], 0.4 \rangle \right\}$	$\left\{ \langle [l_0, l_1], 0.5 \rangle, \langle [l_1, l_2], 0.3 \rangle, \langle [l_2, l_3], 0.2 \rangle \right\}$	$\left\{ \langle [l_{-1}, l_0], 0.2 \rangle, \langle [l_0, l_1], 0.3 \rangle, \langle [l_1, l_2], 0.5 \rangle \right\}$

**Table 13** | PULAV in accordance with all attributes.

	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
PULAV	$\left\{ \langle [l_{-0.80}, l_{0.20}], 0.22 \rangle, \langle [l_{0.20}, l_{1.20}], 0.56 \rangle, \langle [l_{1.20}, l_{2.20}], 0.22 \rangle \right\}$	$\left\{ \langle [l_{-0.80}, l_{0.20}], 0.12 \rangle, \langle [l_{-0.40}, l_{0.60}], 0.50 \rangle, \langle [l_{0.60}, l_{1.60}], 0.38 \rangle \right\}$	$\left\{ \langle [l_{-0.40}, l_{0.60}], 0.22 \rangle, \langle [l_{0.80}, l_{1.80}], 0.40 \rangle, \langle [l_{1.80}, l_{2.80}], 0.38 \rangle \right\}$	$\left\{ \langle [l_{-1.00}, l_{0.00}], 0.20 \rangle, \langle [l_{0.00}, l_{1.00}], 0.36 \rangle, \langle [l_{1.20}, l_{2.20}], 0.44 \rangle \right\}$

PULAV = probabilistic uncertain linguistic average value.

**Table 14** | PULPDA matrix.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	0.0000	0.0843	0.0365	0.0000
A <sub>2</sub>	0.0090	0.0455	0.0000	0.1108
A <sub>3</sub>	0.0000	0.0000	0.0516	0.0000
A <sub>4</sub>	0.0721	0.0357	0.0000	0.0585
A <sub>5</sub>	0.0000	0.0000	0.0000	0.0000

PULPDA = probabilistic uncertain linguistic positive distance from average.

**Table 15** | PULNDA matrix.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	0.0090	0.0000	0.0000	0.0895
A <sub>2</sub>	0.0000	0.0000	0.0691	0.0000
A <sub>3</sub>	0.0721	0.0517	0.0000	0.1156
A <sub>4</sub>	0.0000	0.0000	0.0163	0.0000
A <sub>5</sub>	0.0360	0.1488	0.0163	0.0024

PULNDA = probabilistic uncertain linguistic negative distance from average.

**Table 16** | PULSP and PULSN values.

Alternatives	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>	A <sub>5</sub>
PULSP	0.0386	0.0622	0.0049	0.0455	0.0000
PULSN	0.0360	0.0066	0.0741	0.0016	0.0657

**Table 17** | PULNSP and PULNSN values.

Alternatives	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>	A <sub>5</sub>
PULNSP	0.5920	1.0000	0.0791	0.7322	0.0000
PULNSN	0.5148	0.9110	0.0000	0.9790	0.1139

PULNSP = probabilistic uncertain linguistic normalized PULSP; PULNSN = probabilistic uncertain linguistic normalized PULSN.

**Table 18** | PULAS value.

Alternatives	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>	A <sub>5</sub>
PULAS	0.5534	0.9555	0.0396	0.8556	0.0569

PULAS = probabilistic uncertain linguistic appraisal score.

### 4.2.3. Compared with ULWA operator

In this subsection, we further analysis the above example under the uncertain linguistic environment. Use the ULWA operator [42] with equal weight information to fuse all the uncertain linguistic decision matrices provided by the DMs into a group uncertain linguistic decision matrix (See Table 20).

The weight vector of attributes is derived as:  $w_1 = 0.1195, w_2 = 0.3955, w_3 = 0.0954, w_4 = 0.3896$ , then the overall attribute value of each alternative  $Z_i(w)$  ( $i = 1, 2, 3, 4, 5$ ) is obtained by employing ULWA operator [42].

$$Z_1(w) = [l_{0.0603}, l_{1.6492}], Z_2(w) = [l_{0.8055}, l_{2.1379}],$$

$$Z_3(w) = [l_{-0.5461}, l_{0.5453}] Z_4(w) = [l_{0.6264}, l_{2.3147}],$$

$$Z_5(w) = [l_{-0.6186}, l_{0.8932}]$$

Then, the score values of these five overall attribute values of each alternative  $Z_i(w)$  ( $i = 1, 2, 3, 4, 5$ ) are obtained by Definition 9 [43] as follows:

$$E(Z_1(w)) = l_{0.8548}, E(Z_2(w)) = l_{1.5106}, E(Z_3(w)) = l_{0.0092}$$

$$E(Z_4(w)) = l_{1.4705}, E(Z_5(w)) = l_{0.1373}$$

Furthermore, we can derive the ranking result:  $A_2 > A_4 > A_1 > A_5 > A_3$ . Thus, we have the same optimal green supplier of coal enterprises  $A_2$ .

**Table 19** | The calculating results and sorting results by using PUL-TOPSIS method.

TOPSIS Method	Calculating Results and Sorting Results
The distances of each alternative from PULPIS	$d_1^+ = 0.5882, d_2^+ = 0.2384, d_3^+ = 0.6912, d_4^+ = 0.3386, d_5^+ = 0.6864$
The distances of each alternative from PULNIS	$d_1^- = 0.6597, d_2^- = 0.8499, d_3^- = 0.4622, d_4^- = 0.7921, d_5^- = 0.5294$
Closeness coefficients	$CI_1 = -1.6944, CI_2 = -0.0000, CI_3 = -2.3555, CI_4 = -0.4882, CI_5 = -2.2564$
Ordering	$A_2 > A_4 > A_1 > A_5 > A_3$

PUL-TOPSIS = probabilistic uncertain linguistic TOPSIS; PULPIS = probabilistic uncertain linguistic positive ideal solution; PULNIS = probabilistic uncertain linguistic negative ideal solution.

**Table 20** | Group uncertain linguistic decision matrix.

Alternatives	G <sub>1</sub>	G <sub>2</sub>	G <sub>3</sub>	G <sub>4</sub>
A <sub>1</sub>	[l <sub>0.0</sub> , l <sub>1.2</sub> ]	[l <sub>0.8</sub> , l <sub>1.8</sub> ]	[l <sub>1.4</sub> , l <sub>2.4</sub> ]	[l <sub>-1</sub> , l <sub>0.6</sub> ]
A <sub>2</sub>	[l <sub>0.2</sub> , l <sub>1.4</sub> ]	[l <sub>0.4</sub> , l <sub>1.4</sub> ]	[l <sub>0</sub> , l <sub>1</sub> ]	[l <sub>1.6</sub> , l <sub>2.6</sub> ]
A <sub>3</sub>	[l <sub>-0.6</sub> , l <sub>0.4</sub> ]	[l <sub>-0.6</sub> , l <sub>0.4</sub> ]	[l <sub>1.6</sub> , l <sub>2.6</sub> ]	[l <sub>-1</sub> , l <sub>0</sub> ]
A <sub>4</sub>	[l <sub>1</sub> , l <sub>2</sub> ]	[l <sub>0.2</sub> , l <sub>1.4</sub> ]	[l <sub>0.4</sub> , l <sub>2</sub> ]	[l <sub>1</sub> , l <sub>2</sub> ]
A <sub>5</sub>	[l <sub>-0.2</sub> , l <sub>0.8</sub> ]	[l <sub>-1.6</sub> , l <sub>-0.6</sub> ]	[l <sub>0.4</sub> , l <sub>2</sub> ]	[l <sub>0</sub> , l <sub>1.6</sub> ]

From the above analysis, it can be seen that the ordering results obtained from the PUL-EDAS method, PUL-TOPSIS method, the PULWA operator are the same as that is obtained by the ULWA operator method under the uncertain linguistic setting. It implies that the PULTS is feasible and meaningful. However, their values of the score function are different when the aggregation-based method is used. The PULTS can not only consider the uncertain linguistic assessment information, but also contain the probabilities of each uncertain linguistic term. Therefore, it could take full advantage of the uncertain linguistic assessment information and their score values are more reasonable and interpretable than those obtained under the uncertain linguistic setting where the probabilities of uncertain linguistic terms are not taken in consideration and partial information is heavily lost. But, these four methods have their advantages: (1) PUL-TOPSIS method emphasizes the distance closeness degree from the positive and negative ideal solution; (2) PULWA operator can not only consider the uncertain linguistic assessment information, but also contain the probabilities of each uncertain linguistic term; (3) ULWA operator emphasis group influences degree and can't consider the probabilities of uncertain linguistic terms and partial information is heavily lost; (4) our proposed PUL-EDAS method only emphasizes the distance closeness degree from average solution for all attributes.

### 5. CONCLUSION

In this paper, we designed the EDAS method to tackle MAGDM issues with PULTSs. Firstly, the basic definition, comparative formula and Hamming distance of PULTSs are briefly reviewed. Then, on the basis of the conventional EDAS method, the EDAS method is proposed to deal with MAGDM problems with PULTSs and its significant characteristic is that it only highlights the distance closeness degree from average solution for all attributes. Finally, a practical case study for green supplier selection is used to illustrate the

developed method and some comparative analysis is also designed to show the applicability in MAGDM issues. In such research, the EDAS method, which is also an efficient MADM or MAGDM method, has been designed to deal with other uncertain decision-making problems. In the future, PULTSs could be expanded to derive the weight information of each DM. Moreover, the basic idea behind PULTSs can be used to extend other fuzzy sets by associating each membership degree with its probability [60–66]. Furthermore, the application of the proposed methods with PULTSs needs to be investigated along with the other uncertain decision making and many other uncertain and fuzzy environments [67–71].

### CONFLICT OF INTEREST

The authors declare that they have no conflict of interest.

### ACKNOWLEDGMENT

The work was supported by the National Natural Science Foundation of China under Grant No. 71571128 and the Humanities and Social Sciences Foundation of Ministry of Education of the People's Republic of China (No. 17XJA630003).

### REFERENCES

- [1] M. Keshavarz Ghorabae, E.K. Zavadskas, L. Olfat, Z. Turskis, Multi-criteria inventory classification using a new method of evaluation based on distance from average solution (EDAS), Informatica. 26 (2015), 435– 451.
- [2] Z. Stevic, M. Vasiljevic, E.K. Zavadskas, S. Sremac, Z. Turskis, Selection of carpenter manufacturer using fuzzy EDAS method, Inz. Ekon. Eng. Econ. 29 (2018), 281–290.
- [3] M. Keshavarz Ghorabae, E.K. Zavadskas, M. Amiri, Z. Turskis, Extended EDAS method for fuzzy multi-criteria decision-making: an application to supplier selection, Int. J. Comput. Commun. Control. 11 (2016), 358–371.
- [4] M. Keshavarz Ghorabae, M. Amiri, E.K. Zavadskas, Z. Turskis, Multi-criteria group decision-making using an extended edas method with interval type-2 fuzzy sets, E & M Ekon. Manag. 20 (2017), 48–68.
- [5] C. Kahraman, M. Keshavarz Ghorabae, E.K. Zavadskas, S.C. Onar, M. Yazdani, B. Oztaysi, Intuitionistic fuzzy EDAS method: an application to solid waste disposal site selection, J. Environ. Eng. Landsc. Manag. 25 (2017), 1– 12.



- [6] M. Keshavarz Ghorabae, M. Amiri, E.K. Zavadskas, Z. Turskis, J. Antucheviciene, Stochastic EDAS method for multi-criteria decision-making with normally distributed data, *J. Intell. Fuzzy Syst.* 33 (2017), 1627–1638.
- [7] M. Keshavarz-Ghorabae, M. Amiri, E.K. Zavadskas, Z. Turskis, J. Antucheviciene, A comparative analysis of the rank reversal phenomenon in the EDAS and TOPSIS methods, *Econ. Comput. Econ. Cybern. Stud. Res.* 52 (2018), 121–134.
- [8] X.D. Peng, J.G. Dai, Algorithms for interval neutrosophic multiple attribute decision-making based on MABAC, similarity measure, and EDAS, *Int. J. Uncertain. Quan.* 7 (2017), 395–421.
- [9] S.Q. Zhang, H. Gao, G.W. Wei, Y. Wei, C. Wei, Evaluation based on distance from average solution method for multiple criteria group decision making under picture 2-tuple linguistic environment, *Mathematics.* 7 (2019), 243.
- [10] X.Q. Feng, C.P. Wei, Q. Liu, EDAS method for extended hesitant fuzzy linguistic multi-criteria decision making, *Int. J. Fuzzy Syst.* 20 (2018), 2470–2483.
- [11] X.M. Mi, H.C. Liao, An integrated approach to multiple criteria decision making based on the average solution and normalized weights of criteria deduced by the hesitant fuzzy best worst method, *Comput. Ind. Eng.* 133 (2019), 83–94.
- [12] S.Q. Zhang, G.W. Wei, H. Gao, C. Wei, Y. Wei, EDAS method for multiple criteria group decision making with picture fuzzy information and its application to green suppliers selections, *Technol. Econ. Dev. Econ.* 26 (2019), 1123–1138.
- [13] J. Roy, H.K. Sharma, S. Kar, E.K. Zavadskas, J. Saparauskas, An extended COPRAS model for multi-criteria decision-making problems and its application in web-based hotel evaluation and selection, *Econ. Res-Ekon. Istraz.* 32 (2019), 219–253.
- [14] Z.X. Li, M. Lu, Some novel similarity and distance and measures of pythagorean fuzzy sets and their applications, *J. Intell. Fuzzy Syst.* 37 (2019), 1781–1799.
- [15] J.P. Lu, C. Wei, TODIM method for performance appraisal on social-integration-based rural reconstruction with interval-valued intuitionistic fuzzy information, *J. Intell. Fuzzy Syst.* 37 (2019), 1731–1740.
- [16] R. Wang, Research on the application of the financial investment risk appraisal models with some interval number muirhead mean operators, *J. Intell. Fuzzy Syst.* 37 (2019), 1741–1752.
- [17] L.P. Wu, H. Gao, C. Wei, VIKOR method for financing risk assessment of rural tourism projects under interval-valued intuitionistic fuzzy environment, *J. Intell. Fuzzy Syst.* 37 (2019), 2001–2008.
- [18] L.P. Wu, J. Wang, H. Gao, Models for competitiveness evaluation of tourist destination with some interval-valued intuitionistic fuzzy hamy mean operators, *J. Intell. Fuzzy Syst.* 36 (2019), 5693–5709.
- [19] F. Herrera, L. Martinez, An approach for combining linguistic and numerical information based on the 2-tuple fuzzy linguistic representation model in decision-making, *Int. J. Uncertain. Fuzz. Knowl-Bas. Syst.* 8 (2000), 539–562.
- [20] F. Herrera, L. Martinez, A 2-tuple fuzzy linguistic representation model for computing with words, *IEEE Trans. Fuzzy Syst.* 8 (2000), 746–752.
- [21] R.M. Rodriguez, L. Martinez, F. Herrera, Hesitant fuzzy linguistic term sets for decision making, *IEEE Trans. Fuzzy Syst.* 20 (2012), 109–119.
- [22] V. Torra, Hesitant fuzzy sets, *Int. J. Intell. Syst.* 25 (2010), 529–539.
- [23] L.A. Zadeh, The concept of a linguistic variable and its application to approximate reasoning, *Inf. Sci.* 8 (1975), 301–357.
- [24] H.C.C. Liao, L.Y.Y. Yang, Z.S.S. Xu, Two new approaches based on ELECTRE II to solve the multiple criteria decision making problems with hesitant fuzzy linguistic term sets, *App. Soft Comput.* 63 (2018), 223–234.
- [25] B.W. Zhang, H.M. Liang, G.Q. Zhang, Reaching a consensus with minimum adjustment in MAGDM with hesitant fuzzy linguistic term sets, *Inform. Fusion.* 42 (2018), 12– 23.
- [26] G.W. Wei, The generalized dice similarity measures for multiple attribute decision making with hesitant fuzzy linguistic information, *Econ. Res-Ekon. Istraz.* 32 (2019), 1498–1520.
- [27] Q. Pang, H. Wang, Z.S. Xu, Probabilistic linguistic linguistic term sets in multi-attribute group decision making, *Inf. Sci.* 369 (2016), 128–143.
- [28] X.J. Gou, Z.S. Xu, Novel basic operational laws for linguistic terms, hesitant fuzzy linguistic term sets and probabilistic linguistic term sets, *Inf. Sci.* 372 (2016), 407–427.
- [29] Y.X. Zhang, Z.S. Xu, H.C. Liao, A consensus process for group decision making with probabilistic linguistic preference relations, *Inf. Sci.* 414 (2017), 260–275.
- [30] A. Kobina, D.C. Liang, X. He, Probabilistic linguistic power aggregation operators for multi-criteria group decision making, *Symmetry Basel.* 9 (2017), 320.
- [31] G.W. Wei, Pythagorean fuzzy hamacher power aggregation operators in multiple attribute decision making, *Fundam. Inform.* 166 (2019), 57–85 .
- [32] R.R. Yager, The power average operator, *IEEE Trans. Syst. Man Cybern. Part A.* 31 (2001), 724–731.
- [33] Z.S. Xu, R.R. Yager, Power-Geometric operators and their use in group decision making, *IEEE Trans. Fuzzy Syst.* 18 (2010), 94–105.
- [34] H.C. Liao, L.S. Jiang, Z.H. Xu, J.P. Xu, F. Herrera, A linear programming method for multiple criteria decision making with probabilistic linguistic information, *Inf. Sci.* 415 (2017), 341–355.
- [35] S.X. Chen, J.Q. Wang, T.L. Wang, Cloud-based ERP system selection based on extended probabilistic linguistic MULTIMOORA method and Choquet integral operator, *Comput. Appl. Math.* 38 (2019), 88.
- [36] D.C. Liang, A. Kobina, W. Quan, Grey relational analysis method for probabilistic linguistic multi-Criteria group decision-Making based on geometric bonferroni mean, *Int. J. Fuzzy Syst.* 20 (2018), 2234–2244.
- [37] J. Wang, G.W. Wei, Y. Wei, Models for green supplier selection with some 2-tuple linguistic neutrosophic number bonferroni mean operators, *Symmetry Basel.* 10 (2018), 131.
- [38] G.W. Wei, R. Wang, J. Wang, C. Wei, Y. Zhang, Methods for evaluating the technological innovation capability for the high-Tech enterprises with generalized interval neutrosophic number bonferroni mean operators, *IEEE Access.* 7 (2019), 86473–86492.
- [39] C.Z. Bai, R. Zhang, L.X. Qian, Y.N. Wu, Comparisons of probabilistic linguistic term sets for multi-criteria decision making, *Knowl. Based Syst.* 119 (2017), 284–291.
- [40] X. Cheng, J. Gu, Z.S. Xu, Venture capital group decision-making with interaction under probabilistic linguistic environment, *Knowl. Based Syst.* 140 (2018), 82–91.
- [41] J.P. Lu, C. Wei, J. Wu, G.W. Wei, TOPSIS method for probabilistic linguistic MAGDM with entropy weight and its application

- to supplier selection of new agricultural machinery products, *Entropy*. 21 (2019), 953.
- [42] Z.S. Xu, Uncertain linguistic aggregation operators based approach to multiple attribute group decision making under uncertain linguistic environment, *Inf. Sci.* 168 (2004), 171–184.
- [43] M.W. Lin, Z.S. Xu, Y.L. Zhai, Z.Q. Yao, Multi-attribute group decision-making under probabilistic uncertain linguistic environment, *J. Oper. Res. Soc.* 69 (2018), 157–170.
- [44] W.Y. Xie, Z.L. Ren, Z.S. Xu, H. Wang, The consensus of probabilistic uncertain linguistic preference relations and the application on the virtual reality industry, *Knowl. Based Syst.* 162 (2018), 14–28.
- [45] Z.S. Xu, Deviation measures of linguistic preference relations in group decision making, *Omega-Int. J. Manage. Sci.* 33 (2005), 249–254.
- [46] X.J. Gou, Z.S. Xu, H.C. Liao, Multiple criteria decision making based on Bonferroni means with hesitant fuzzy linguistic information, *Soft Comput.* 21 (2017), 6515–6529.
- [47] S. Ding, Z. Shi, Studies on incident pattern recognition based on information entropy, *J. Inf. Sci.* 31 (2005), 497–502.
- [48] H. Gao, Pythagorean fuzzy hamacher prioritized aggregation operators in multiple attribute decision making, *J. Intell. Fuzzy Syst.* 35 (2018), 2229–2245.
- [49] J.P. Lu, X.Y. Tang, G.W. Wei, C. Wei, Y. Wei, Bidirectional project method for dual hesitant Pythagorean fuzzy multiple attribute decision-making and their application to performance assessment of new rural construction, *Int. J. Intell. Syst.* 34 (2019), 1920–1934.
- [50] M. Tang, J. Wang, J.P. Lu, G.W. Wei, C. Wei, Y. Wei, Dual hesitant pythagorean fuzzy heronian mean operators in multiple attribute decision making, *Mathematics*. 7 (2019), 344.
- [51] J. Wang, H. Gao, G.W. Wei, Some 2-tuple linguistic neutrosophic number muirhead mean operators and their applications to multiple attribute decision making, *J. Exp. Theor. Artif. Intell.* 31 (2019), 409–439.
- [52] E.K. Zavadskas, Z. Turskis, J. Tamosaitiene, V. Marina, Multicriteria selection of project managers by applying grey criteria, *Technol. Econ. Dev Econ.* 14 (2008), 462–477.
- [53] M. Yazdani, P. Chatterjee, E.K. Zavadskas, S. Hashemkhani Zolfani, Integrated QFD-MCDM framework for green supplier selection, *J. Clean. Prod.* 142 (2017), 3728–3740.
- [54] E.K. Zavadskas, Z. Turskis, T. Vilutiene, N. Lepkova, Integrated group fuzzy multi-criteria model: case of facilities management strategy selection, *Expert Syst. Appl.* 82 (2017), 317–331.
- [55] H. Hashemi, S.M. Mousavi, E.K. Zavadskas, A. Chalekaee, Z. Turskis, A new group decision model based on grey-Intuitionistic fuzzy-ELECTRE and VIKOR for contractor assessment problem, *Sustainability*. 10 (2018), 1635.
- [56] R. Davoudabadi, S.M. Mousavi, J. Saparauskas, H. Gitinavard, Solving construction project selection problem by a new uncertain weighting and ranking based on compromise solution with linear assignment approach, *J. Civ. Eng. Manag.* 25 (2019), 241–251.
- [57] J. Wang, G.W. Wei, J.P. Lu, F.E. Alsaadi, T. Hayat, C. Wei, Y. Zhang, Some q-Rung orthopair fuzzy hamy mean operators in multiple attribute decision making and their application to enterprise resource planning systems selection, *Int. J. Intell. Syst.* 34 (2019), 2429–2458.
- [58] Z.X. Li, H. Gao, G.W. Wei, Methods for multiple attribute group decision making based on intuitionistic fuzzy dombi hamy mean operators, *Symmetry Basel*. 10 (2018), 574.
- [59] J. Wang, G.W. Wei, M. Lu, An extended VIKOR method for multiple criteria group decision making with triangular fuzzy neutrosophic numbers, *Symmetry Basel*. 10 (2018), 497.
- [60] P. Wang, J. Wang, G.W. Wei, C. Wei, Similarity measures of q-rung orthopair fuzzy sets based on cosine function and their applications, *Mathematics*. 7 (2019), 340.
- [61] P. Wang, G.W. Wei, J. Wang, R. Lin, Y. Wei, Dual hesitant q-Rung orthopair fuzzy hamacher aggregation operators and their applications in scheme selection of construction project, *Symmetry Basel*. 11 (2019), 771.
- [62] A. Biswas, B. Sarkar, Interval-valued pythagorean fuzzy TODIM approach through point operator-based similarity measures for multicriteria group decision making, *Kybernetes*. 48 (2019), 496–519.
- [63] T.Y. Chen, Novel generalized distance measure of pythagorean fuzzy sets and a compromise approach for multiple criteria decision analysis under uncertainty, *IEEE Access*. 7 (2019), 58168–58185.
- [64] S.Z. Zeng, X.M. Peng, T. Balezentis, D. Streimikiene, Prioritization of low-carbon suppliers based on pythagorean fuzzy group decision making with self-confidence level, *Econ. Res. Ekon. Istraz.* 32 (2019), 1073–1087.
- [65] G.F. Yu, W. Fei, D.F. Li, A compromise-Typed variable weight decision method for hybrid multiattribute decision making, *IEEE Trans. Fuzzy Syst.* 27 (2019), 861–872.
- [66] H. Gao, J. Wu, C. Wei, G.W. Wei, MADM method with interval-valued bipolar uncertain linguistic information for evaluating the computer network security, *IEEE Access*. 7 (2019), 151506–151524.
- [67] S.A. Erdogan, J. Saparauskas, Z. Turskis, Decision making in construction management: AHP and expert choice approach, in: A. Juozapaitis, A. Daniunas, E.K. Zavadskas (Eds.), *Modern Building Materials, Structures and Techniques*, Vilnius Gediminas Technical University, Faculty of Civil Engineering, Vilnius, (2017), pp. 270–276.
- [68] J. Wang, H. Gao, G.W. Wei, The generalized dice similarity measures for Pythagorean fuzzy multiple attribute group decision making, *Int. J. Intell. Syst.* 34 (2019), 1158–1183.
- [69] A. Jahan, E.K. Zavadskas, ELECTRE-IDAT for design decision-making problems with interval data and target-based criteria, *Soft Comput.* 23 (2019), 129–143.
- [70] G.F. Yu, D.F. Li, W. Fei, A novel method for heterogeneous multi-attribute group decision making with preference deviation, *Comput. Ind. Eng.* 124 (2018), 58–64.
- [71] D.F. Li, G.H. Chen, Z.G. Huang, Linear programming method for multiattribute group decision making using IF sets, *Inf. Sci.* 180 (2010), 1591–1609.