Revisiting Query Variation Robustness of Transformer Models

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Abstract

The most commonly used transformers for retrieval at present, BERT and T5, have been shown not to be robust to query variations such as typos or paraphrases. Although this is an important prerequisite for their practicality, this problem has hardly been investigated. More recent large language models (LLMs), including instruction-tuned LLMs, have not been analyzed yet, and only one study looks beyond typos. We close this gap by reproducing this study and extending it with a systematic analysis of more recent models, including Sentence-BERT, CharacterBERT, E5-Mistral, AnglE, and Ada v2. We further investigate if instruct-LLMs can be prompted for robustness. Our results are mixed in that the previously observed robustness issues for cross-encoders also apply to bi-encoders that use much larger LLMs, albeit to a lesser extent. While further LLM scaling may improve their embeddings, their cost-effective use for all but large deployments is limited. Training data that includes query variations allows LLMs to be finetuned for more robustness, but focusing on a single category of query variation may even degrade the effectiveness on others.¹

1 Introduction

Despite their proficiency with natural language, transformer-based large language models (LLMs) trained for document ranking, like BERT or T5, are not robust to ill-formed queries, including queries with typos and queries that omit less important words (Penha et al., 2022; Sidiropoulos and Kanoulas, 2022; Zhuang et al., 2022). Zhuang et al. (2023) reason that these variations are hardly represented in the LLMs' training data. However, query variations are the norm in practice: about 70% of information-seeking queries to web search engines are keyword queries (White et al., 2015) instead of fully formed questions, and up to 26% of queries contain typos (Wang et al., 2003). However, due to their superior effectiveness, current information retrieval (IR) systems use these 'embedding models'² despite their lack of robustness.

To our knowledge, this phenomenon has hardly been investigated with respect to information retrieval (Section 2). Penha et al. (2022) contributed the most exhaustive study to date. They measure the changes in ranking effectiveness of various models for an originally intended, well-formed query from TREC DL'19 (Craswell et al., 2020) and ANTIQUE (Hashemi et al., 2020) compared to randomly generated but semantically equivalent variations. However, no study yet investigated the ranking robustness of LLM-based embedding models more recent than BERT (Devlin et al., 2019) and T5 (Raffel et al., 2020) with respect to query variations. Given the fast pace at which LLMs have been scaled, it is unclear whether scaling alone suffices to solve the problem.

In this paper, we investigate the robustness of recent large language models against purely syntactic, query variants which preserve semantics. We reproduce Penha et al.'s experiment on the robustness of cross encoders to different query variants from well-formed queries. In addition to comparing the ranking effectiveness of query variations to well-formed queries, we measure the anisotropy adjusted cosine similarity of the variations' embeddings compared to their respective original's to quantify the robustness of the embeddings, i.e., how much input variations affect the models' outputs. Doing so, we also extend Penha et al.'s study, to the state-of-the-art embedding models Sentence-BERT, CharacterBERT, E5-Mistral, AnglE, and Ada v2.

¹Our code, results, and artifacts can be found at github.com /webis-de/EMNLP-24.

²Although there is a wide range of models and architectures, we focus on the representations they compute and therefore refer to them collectively as 'embedding models'.

Our reproduction results are consistent with previous work, showing that existing dense retrieval models are not robust to semantically identical illformed query variants. We also find LLM-based embedding models to suffer from the same problem, but to a lesser extent. Our experiments show that robustness to typos can be improved substantially using character-level transformers and typo aware pre-training, but this does not generalize to other query variations. We observe that focusing on a single category of query variation may even degrade effectiveness on other categories of variations. Moreover, some models were less robust to keyword queries than to typos, presumably because transformer models use stop words to aggregate the context (Clark et al., 2019; Ethayarajh, 2019).

2 Related Work

Though LLMs are effective at information retrieval and natural language processing tasks (Kocoń et al., 2023), they are not robust to language variations like typos or keywording (Zhuang and Zuccon, 2021; Penha et al., 2022; Zhuang et al., 2022; Sidiropoulos and Kanoulas, 2022). Previous research identified two key contributing factors to this lack of robustness: (1) LLMs and ranking models are mostly trained on clean data, rendering variations like typos and keywords out of domain (Zhuang et al., 2023), and (2) character-level information is lost during tokenization (Almagro et al., 2023; Zhuang and Zuccon, 2022). For example, 'weird' and its misspelling 'wierd' are tokenized by BERT as weird and wi ##er ##d.

Typo awareness Solutions to improve robustness of transformer-based models for information retrieval can be categorized into improving robustness using typo aware (pre-)training strategies (Tasawong et al., 2023; Zhuang et al., 2023, 2022), using datasets with input variations (Penha et al., 2022; Bailey et al., 2016), and developing models using character-level tokenization schemes (Zhuang and Zuccon, 2022; Almagro et al., 2023).

Zhuang et al. (2023) propose pre-training using a typo aware masked language modeling strategy to strengthen a model's robustness to typos. Previous studies improved typo robustness by finetuning models on datasets augmented with misspellings (Zhuang et al., 2022; Tasawong et al., 2023). Sidiropoulos and Kanoulas (2022, 2024) train dual encoders using a contrastive loss to learn closer representations for words and their typos while keeping other words' representations apart. Sidiropoulos and Kanoulas find that typos in less prevalent words degrade effectiveness more than typos in common words and identify BERT's Word-Piece tokenizer as a limiting factor in this respect.

To address the tokenizer's shortcomings, Zhuang and Zuccon (2022) use CharacterBERT (Boukkouri et al., 2020), a BERT variant that creates characterlevel token representations instead of word pieces. They fine-tune it on a typo-augmented dataset, minimizing two loss components: the KL-divergence of the relevance label distributions of a query and its typo variant, and contrastive cross entropy loss to retain effectiveness. Tasawong et al. (2023) call these components 'robustness' and 'effectiveness' and additionally propose 'alignment' to learn similar representations for queries and their variants. CharacterBERT's character-level tokenizer is crucial for more typo robustness as it can better recognize small input variations. Almagro et al. (2023) propose the LExical-aware Attention module (LEA), which adds a learnable bias to the attention scores based on text similarity.

Beyond typos The research mentioned above only focuses on typos. Penha et al. (2022) take the robustness analysis further by creating a test collection covering three more classes of query variations that retain semantics. To our knowledge, the only other test collection for query variations beyond typos is UQV100 (Bailey et al., 2016). However, it does not guarantee identical semantics across query variations, nor does it specify the category of the variation. We make extensive use of Penha et al.'s collection to study the query robustness of a spectrum of transformer-based retrieval models, ranging from the cross-encoders used to supplement the collection, to typo aware embedding models, to embedding models based on LLMs.

Robustness issues are also not confined to IR. Ravichander et al. (2021), Sidiropoulos et al. (2022), and Qiang et al. (2024) observe a significant drop in effectiveness introduced by synonyms, paraphrasing, and errors induced by automatic speech recognition when providing a voice interface for language models. Zheng and Saparov (2023) analyze the accuracy degradation due to typos, synonyms, repetition, and 'shortcuts' (providing part of the answer together with the prompt) observed with prompted embedding models on natural language tasks. By adding perturbed examples in fewshot prompts, they improved robustness to all variations except typos.

| Query variation | | Example | Valid variants | | | |
|-----------------|--|--|--|--|--|--|
| Category | Transform. heuristic | | TREC DL'19 | ANTIQUE | | |
| Original | | what is durable medical equipment consist of | | | | |
| Misspelling | NeighbCharSwap RandomCharSub QWERTYCharSub | what is durable mdeical equipment consist of what is durable medycal equipment consist of what is durable medical equipment xonsist of | 43 (100.00%) 42 (97.67%) 42 (97.67%) | 199 (99.50%) 197 (98.00%) 182 (91.50%) | | |
| Naturality | RemoveStopWords T5DescToTitle | what is durable medical equipment consist of what is durable medical equipment consist of | 37 (86.05%) 35 (81.40%) | 199 (99.50%) 136 (68.00%) | | |
| Ordering | RandomOrderSwap | medical is durable what equipment consist of | 43 (100.00%) | 200 (100.00%) | | |
| Paraphrasing | BackTranslation T5QQP WordEmbedSynSwap WordNetSynSwap | what is sustainable medical equipment consist of what is durable medical equipment consist of what is durable medicinal equipment consist of what is long lasting medical equipment consist of | 23 (53.49%) 26 (60.47%) 27 (62.79%) 16 (37.21%) | 93 (46.50%) 105 (52.50%) 124 (62.00%) 71 (35.50%) | | |

Table 1: Examples of query variations when applying transformation heuristics to the query '*what is durable medical equipment consists of*', and the number of valid (i.e., semantically identical) variations generated. Not all variations exemplified may be valid. This table is reproduced from Penha et al. (2022, Table 3).

3 Methods and Experimental Setup

This section describes the experimental setup consisting of the datasets with query variations, the embedding models used for the experiments and the experiments performed.

3.1 Query Variation Dataset

We use the query variation dataset by Penha et al.³ They define four types of query variations that preserve semantics and suggest transformation heuristics to create them automatically: Misspelling, naturality (which refers to turning a fully formed query into a keyword query), word ordering, and paraphrasing. To create the dataset, the transformations were applied independently to each of the test queries in TREC DL'19 and each of the validation queries in ANTIQUE.⁴ The resulting queries were manually filtered to keep only semantically identical query variations. Table 1 shows examples for each transformation prior to filtering.

3.2 Embedding Models

In addition to BERT and T5 used in the experiments of Penha et al., we include newer embedding models in our experiments: SBERT (Reimers and Gurevych, 2019) often serves as a new baseline for BERT-based embedding models. CharacterBERT-DR-ST (Zhuang and Zuccon, 2022), or CBERT for brevity, represents models specifically designed to be robust to typos. E5 (Wang et al., 2024) (the E5-mistral-7b-instruct variant), AnglE (Li and Li, 2023) (the UAE-Large-v1 variant), and Ada v2 (Greene et al., 2022) (OpenAI's embedding model

⁴Penha et al. used ANTIQUE's validation queries instead of the text queries as stated in their paper (see Section 4.1)

the test queries as stated in their paper (see Section 4.1).

text-embedding-ada-002), represent the state of the art in embedding models: E5-mistral-7b-instruct and UAE-Large-v1 were the leading models on the MTEB ranking list at the time of the experiment, and text-embedding-ada-002 is a leading commercial model.⁵ The MTEB dataset was created specifically for the comparison of embedding models for various natural language processing and information retrieval tasks (Muennighoff et al., 2023). Further information on the models and their training can be found in the Appendix A.1.

3.3 Experimental Setup

The experiment reproduces the setup of Penha et al. (2022), which examines the impact of each query variation category on ranking effectiveness, to investigate the *ranking robustness* of a model. Furthermore, we introduce a second experiment to investigate the *embedding robustness* of a model by measuring how similar the embedding of a query variation is to that of the original query.

To assess ranking robustness, we evaluate an embedding model in the second step of a reranking retrieval pipeline, using it as a dual encoder, and computing the difference in nDCG@10 (' Δ nDCG@10') when ranking on the original query and its variants. Ideally, Δ nDCG@10 should be 0, as semantically identical queries should result in the same rankings. A positive value indicates that the model is more effective for the query variant than for the original query, a negative value indicates less effectiveness. For the initial retrieval in the first step of our pipeline, we use the official top 1000 test set of TREC DL'19, and the top 1000 documents returned by BM25 for ANTIQUE.

³github.com/Guzpenha/query_variation_generators/

⁵huggingface.co/spaces/mteb/leaderboard

The evaluation of ANTIQUE is zero-shot for all models. We have not fine-tuned the models for ANTIQUE and, to our knowledge, neither have the authors of the models.

Our experimental setup differs slightly from the main experiment of Penha et al. in that we always perform the initial retrieval with BM25 on the original query. We are only interested in the robustness of the dual encoders and not that of the entire retrieval pipeline. However, our results are comparable to their results, since Penha et al. have shown that the robustness of the re-ranker is similar to that of the entire pipeline.

To assess embedding robustness, we compute the embeddings of a query and a query variant and measure the anisotropy adjusted cosine similarity between them. We define the anisotropy adjusted cosine similarity as

$$\operatorname{adjcossim}(v, v') = \frac{\operatorname{cossim}(v, v') - \mu}{1 - \mu}, \quad (1)$$

where μ is the expected cosine similarity when embedding two randomly selected inputs (see Table 5 for the values we used). Embedding models often embed into localized subspaces instead of the entire embedding space (Mu and Viswanath, 2018; Ethayarajh, 2019), which makes it difficult to compare cosine similarities across models without renormalization by the adjusted cosine similarity (see Appendix A.2 for details). Note that embeddings with a cosine similarity of 1 also have an adjusted cosine similarity of 1, while the expected adjusted similarity of any two strings is 0. Since the embeddings are semantic representations and since Penha et al. has ensured that each variant is semantically identical to its original query, their similarity should ideally be 1.

4 Results and Discussion

First, we present the similarities and differences in our reproduction of Penha et al.'s experiments. Then, we compare these results with various other models from the literature to see how they generalize. Finally, we evaluate the impact that typo awareness can have by comparing the robustness of different architectures and fine-tuning CBERT and prompt-tuning E5 using a training set created from the query variations of Penha et al.'s dataset.

4.1 Reproduction

To reproduce the robustness results by Penha et al. for BERT and T5, we reran their code with slight modifications: 6 (1) We updated the versions in the requirements.txt since previous versions were not supported anymore, (2) we fixed minor runtime errors which presumably occurred due to the version updates, and (3) we resolved an error in the evaluation routine for BERT on ANTIQUE. As previously noted, Penha et al. did not evaluate on ANTIQUE's test set but on the validation split defined by ir_datasets (MacAvaney et al., 2021), antique/train/split200-valid, which is a split of ANTIQUE's official training set, since ANTIQUE officially does not have a validation set. However, Penha et al. fine-tune BERT on ANTIQUE's official training set (antique/train) instead of ir_datasets' training set (antique/ train/split200-train), thus training on part of their test data. We also remap ANTIQUE's graded relevance labels to the range 0-3 as described by Hashemi et al. in its README.⁷

As we use the same test set, the same pre-trained T5 model and their code, we expect the results for T5 to be nearly identical to those reported by Penha et al., apart from what can reasonably be attributed to rounding differences during inference. For BERT on TREC DL'19 we expect similar results to the original paper, but discrepancies beyond rounding errors are expected due to the stochastic nature of fine-tuning. On ANTIQUE, we expect that our results for BERT are dramatically worse regarding each query variant with the largest expected drop for the original queries.

Table 2a presents our reproduction results. The results are generally as expected—including the large drop in BERT's effectiveness on ANTIQUE as compared to the original paper's results. However, we see four instances of our reproduction deviating stronger than explained by the reasoning above. We most notably observe large deviations in both paraphrasing variants that replace a word with its synonym (WordEmbedSynSwap and WordNetSynSwap), which yield better results on TREC DL'19 in our reproduction.

4.2 Model Robustness

Table 2b presents the mean nDCG@10 scores achieved when re-ranking with each model on TREC DL'19 and ANTIQUE while applying a single query transformation (the query 'variant' in the table). Figure 1 shows the Δ nDCG@10 resulting from each transformation category. Like

⁶github.com/Guzpenha/query_variation_generators

⁷ciir.cs.umass.edu/downloads/Antique/readme.txt

| | | (a) Reproduction | | | | (b) (| Gene | raliz | ation | n | | | | | |
|-----------------|--|--|--|--|--|---------------------------------|--------------------------|---------------------------------|---------------------------|--------------------------|--------------------------|--------------------------|--|---------------------------|----------------------------|
| Query variation | | TREC DL '19 | | ANTIQUE | | TREC DL '19 | | | ANTIQUE | | | | | | |
| Category | Transform. heuristic | BERT | Т5 | BERT | T5 | SBERT | CBERT | ES 3 | A_{nglE} | A_{da}_{V2} | SBERT | CBERT | ES 21 | A_{nglE} | A_{da}_{V2} |
| Original | | .65 /.66 | .70 /.70 | .42 / .29 | .33 /.33 | .70 | .64 | .69 | .70 | .69 | .25 | .29 | .41 | .36 | .37 |
| Misspelling | NeighbCharSwap RandomCharSub QWERTYCharSub | .42*/.42* .33*/.34* .39*/.38* | .50*/.50* .40*/.39* .45*/.44* | .29*/ .19 * .28*/ .19 * .30*/ .18 * | ² .25*/.25* ² .25*/.24* ² .27*/.26* | .52* .56* .60* | .59* .60 .56* | <u>.66</u> .60 .62 | .55* .57 .55* | .61* .58* .59* | .18* .20* .20* | .26* .26* .26* | <u>.37</u> * <u>.37</u> * <u>.38</u> * | .29* .30* .32* | .31* .31* .31* |
| Naturality | RemoveStopWords T5DescToTitle | .64 /.64 .54*/.55* | .69 /.70 .57*/.59 | .38*/ .26 * .27*/ .25 * | .32*/.32 .24*/ .29 * | .69 .62 | .62 .58 | <u>.69</u> .62 | .68 .61 | .68 .62 | .22* .20* | .24* .22* | <u>.36</u> * <u>.31</u> * | .32* .29* | .28* .23* |
| Ordering | RandomOrderSwap | .64 /.65 | .70 /.70 | .41*/ .28 | .33*/.33 | .67 | .58 | .66 | .65 | .62* | .25 | .27 | <u>.39</u> * | .35 | .34* |
| Paraphrasing | BackTranslation T5QQP WordEmbedSynSwap WordNetSynSwap | .55*/.58 .64 /.64 .47*/ .59 .45*/ .62 | .61*/.61 .71 /.71 .56*/ .65 .55*/ .71 | .31*/ .26 .39*/ .26 .33*/ .23 * .32*/ .22 * | .26*/ .32 .32*/.30 :.28*/.28* :.27*/.28* | .60 .67 <u>.66</u> .58 | .57 .61 .59 .62 | <u>.64</u> .65 .61 .64 | .63 . <u>69</u> .66 | .62 .68 .64 .61 | .25 .23 .23 .19 | .28 .25 .26 .24 | <u>.40</u> <u>.37</u> * <u>.40</u> * <u>.34</u> | .36 .34 .36 .30* | .36 .33 .35* .29* |

* significant difference (Bonferroni corrected two-sided paired Student's T-Test at p < 5%) to ranking on the original query

Table 2: (a) Reproduction results. Cells indicate [theirs]/[ours], where 'theirs' is the nDCG@10 reported by Penha et al. (2022) and 'ours' the score we achieved when repeating their experiment as described. Values in bold indicate large differences we discussed in Section 4.1. The models re-rank the top 100 passages initially retrieved by BM25. (b) nDCG@10 of embedding models on TREC DL '19 and ANTIQUE. The most effective model per variant and dataset is underlined. The models re-rank the top 1000 passages initially retrieved by BM25.



Figure 1: Robustness per model, variation category, and dataset. Embedding-robustness (top) is the adjusted cosine similarity of the original query's embedding to its variant's. Ranking-robustness (bottom) is the difference in effectiveness from ranking on the query variant. For clarity, 1981 outliers out of 18400 data points are not shown.

Penha et al., we observe that, while these transformations can improve effectiveness on some queries (positive Δ nDCG@10), the mean effectiveness is not improved statistically significantly. Table 2b shows that only effectiveness degradation is statistically significant. Similar to Penha et al., we can observe that the embedding models we tested are most robust to transformations from the 'ordering' category (i.e., median close to 0 and spread the least in Figure 1). We also observe that the misspelling category has a considerably smaller effect on ANTIQUE than on TREC DL'19. Penha et al. hypothesize that this occurs since queries in TREC DL'19 are shorter. However, concrete comparisons, e.g., about query length, cannot be made using nDCG across datasets due to differences in query, document, and relevance assessments distributions. The experiments on ANTIQUE also have a vastly larger sample size as ANTIQUE's training set contains more queries (Table 1).

Figure 1 presents the embedding robustness in terms of adjusted cosine similarity between each model's embedding of the original query and its variants. A similarity closer to 0 indicates unrelated semantic representations, while a similarity of 1 indicates semantic identity. Like with embedding robustness, we can observe similar trends on both datasets. The ordering category is the easiest, then paraphrasing. All models are least robust to transformations from the naturality and the misspelling category, except CBERT, which is considerably more embedding robust to the misspelling category than other models. AnglE is the most embedding robust model overall (median adjusted cosine similarity close to 1 and least spread) except for robustness to misspelling, which it is the second least robust to. The largest model we tested, E5, is generally similarly robust to the most robust model per category. This is especially interesting on the misspelling category, where its median embedding robustness is only slightly worse than CBERT's, but the spread is larger, i.e., E5 is similarly robust for the median query but in some worst cases the misspelling can have a larger negative effect on embedding robustness. Note, however, that in practice E5 and CBERT are similarly ranking robust while E5 is considerably more effective on misspellings despite missing a character-level tokenizer and specific fine-tuning for typo robustness. Thus, E5 presents an interesting proof of concept for the application of LLM-based embedding models to information retrieval. In short, we find that, though contemporary large embedding models can be a lot more ranking-robust to semantics retaining query transformations than BERT-based embedding models, they still are not robust. Further, their robustness (though not their effectiveness) can be closely matched by far more efficient BERT-based embedding models (CBERT on misspellings and AnglE on all other categories).

Finally, CBERT demonstrates that character tokenization paired with typo-aware training improves robustness to typos. However, comparing SBERT's and CBERT's ranking-robustness (Figure 1), shows that this robustness does not translate to other variation categories as CBERT consistently exhibits slightly worse robustness across all other variants. We leave comparing character level architectures and typo-aware training strategies for future work.

4.3 Robustness Across Architectures

Figure 2 presents the ranking robustness of various models on TREC DL'19 and ANTIQUE. Specifically, we compare the BERT-based dual encoder SBERT with the BERT-based cross-encoder monoBERT (denoted by 'BERT'), the most robust ranking model from the original work, monoT5 ('T5'), and the most robust model from our experi-



Figure 2: Ranking-robustness of cross-encoders compared to the most robust model from Table 2 (b). O denotes retrieval on the original query and re-ranking using the variant. V denotes retrieval and re-ranking using the query variant. 1731 outliers hidden for clarity.

ments, E5. Models with the V subscript evaluate the entire ranking pipeline's robustness when reranking BM25's top 1000 passages. That is, the query *variant* is used for both initial retrieval and re-ranking, whereas models denoted by O, use the *original* query for initial retrieval.

Interestingly, neither architecture, cross-encoder or dual encoder, appears more robust than the other. Both architectures further display similar trends: all models and the pipelines based on these are least robust to typos, then paraphrasing and naturality, and all are most robust to ordering. For the pipelines' robustness, we observe that, while BM25 does not meaningfully impact the robustness to naturality and ordering, since it itself filters stop words and is a bag-of-word model such that ordering does not matter, it heavily degrades robustness in response to typos, especially on TREC DL'19. We hypothesize two causes to explain the robustness of $BERT_O$ and $T5_O$ over $BERT_V$ and $T5_V$ respectively: (1) the number of initially retrieved documents using the original query influences robustness of the output rankings of the re-ranker, and (2) errors propagate in the pipeline and if initial retrieval on the typo-induced query does not contain relevant documents, the pipeline's effectiveness as whole worsens regardless of the re-ranker. Note that (1) describes an advantage for BERT_O and $T5_O$ over $BERT_V$ and $T5_V$ respectively, while (2) gives a disadvantage of $BERT_V$ and $T5_V$ over $BERT_O$

| Category | Transform. heuristic | Valid variants |
|-------------|--|---|
| Misspelling | NeighbCharSwap RandomCharSub QWERTYCharSub | 502K (99.83%) 492K (97.92%) 503K (99.98%) |
| Naturality | RemoveStopWords | 448K (89.16%) |
| Ordering | RandomOrderSwap | 502K (99.73%) |

Table 3: The number of query variations generated for TREC DL'19's training set.

and T5₀. In practice, these findings show that, to evaluate only the re-ranking stage and mitigate (1), the number of initially retrieved documents should be sufficiently large (we chose 1000 but believe values between 100 and 1000 are sufficient). We leave investigating (2) for future research.

4.4 Training Robust Models

Lastly, we investigated if CBERT could be finetuned or E5 be prompted differently to produce more robust embeddings. To generate a training set, we applied the misspelling, ordering and RemoveStopWords transformations from Penha et al. to every query in the TREC DL'19 training set and applied automatic labeling: variants identical to the original query or variants that are empty strings are invalid and valid otherwise. Table 3 shows statistics of the new dataset. For training, we fine-tuned CBERT on the same loss objective it was trained with but using the new dataset. Since Mistral-7B-instruct, the model used by E5, is designed to follow instructions, we performed prompt-tuning (Lester et al., 2021). That is, we froze all the model's parameters and learned a prefix for the input embeddings. This fixed prefix replaces the instruction. E5 was trained using the same loss objective as CBERT and, for efficiency, we trained it 4bit-quantized. Appendix A.3 further presents an experiment on manually prompting E5 to be more typo-robust.

Table 4 and Figure 3 present the robustness and effectiveness of the tuned models when re-ranking the top 1000 passages returned by BM25, respectively. If the fine-tuning using noisy input behaved similar to Zheng and Saparov's few-shot prompting experiments with noisy examples, we would expect robustness and mean effectiveness on all variations except typos to improve. Table 4 shows that this is not the case: there are only negligible differences in mean effectiveness between CBERT's and E5's tuned and untuned variant.⁸ Both models still

| Que | ery variation | | ANTIQUE | | | | | |
|--------------|--|--------------------------|---------------------------|-------------------------------|---------------------------|--|--|--|
| Category | Transform. heuristic | CBERT | CBERT | ES ^{1 uned} | $ES_{T_{uned}}$ | | | |
| Original | | .29 | .27 | .41 | .41 | | | |
| Misspelling | NeighbCharSwap RandomCharSub QWERTYCharSub | .26* .26* .26* | .23* .24* .25 | .37* . 37 * .38* | .38* .37* .38* | | | |
| Naturality | RemoveStopWords T5DescToTitle | .24* .22* | .24* .23* | .36* .31* | .36* .33* | | | |
| Ordering | RandomOrderSwap | .27 | .27 | .39* | .39* | | | |
| Paraphrasing | BackTranslation T5QQP WordEmbedSynSwap WordNetSynSwap | .28 .25 .26 .24 | .27 .25 .24* .22 | .40 .37* .40* .34 | .39 .37 .40* .35 | | | |

* significant difference (Bonferroni corrected two-sided paired Student's T-Test at p < 5%) to ranking on the original query

Table 4: nDCG@10 of CBERT and E5 on ANTIQUE before and after fine-tuning on our training set. The models re-rank the top 1000 passages initially retrieved by BM25. The most effective model per variant is highlighted bold. See Table 8 in the appendix for details.



Figure 3: Robustness of CBERT and E5 before and after fine-tuning on our training set. Each model re-ranks the top 1000 passages retrieved by BM25.

exhibit statistically significant effectiveness degradation due to variations, yet Figure 3 highlights considerable improvements across both models in embedding robustness and ranking robustness in terms of the median and spread. The only exceptions are (1) CBERT's ranking robustness to misspellings, which can be expected since CBERT was previously fine-tuned specifically for this case, and (2) both models' ranking robustness to naturality which may be explained by Ethayarajh's finding that transformer based language models use stop

⁸This occurs irrespective the initial retriever (Appendix A.4).

words to aggregate their contexts, or Clark et al. who observe some of BERT's attention heads to have learned syntactic structures around stop words (e.g., prepositions attending to their objects).

Altogether, we find that our experiment shows promise in the feasibility of robustness to naturally occurring language phenomena; either by fine-tuning BERT-based models or solely by (soft-) prompting large language models differently. The models' problems with keyword queries indicate that embedding models may have to be trained (or even be pre-trained) on incomplete sentences more.

4.5 Summary

Reproducing Penha et al. (2022)'s work, we found a fault in their experimental setup but, ultimately, reaffirmed all their key findings. We generalized their experiments to a wider range of model architectures by investigating the robustness of SBERT, CharacterBERT-DR-ST ('CBERT'), E5 Mistral ('E5'), AnglE, and Ada v2 regarding typos, naturality, ordering and paraphrasing. Our results show that all these embedding models, like the transformer models tested by Penha et al., are most robust to paraphrasing and ordering, except for CBERT, which is slightly more robust to typos than to ordering. While not robust, the largest model we tested, E5, is the most effective and most robust model overall, but not always the most robust. We could further improve CBERT's and E5's robustness via fine-tuning and prompt-tuning respectively. Yet, this robustness did not entail improved effectiveness.

Though E5 is too large for efficient ad-hoc retrieval, its improved robustness through prompttuning promises interesting opportunities for instruct-LLMs in IR research beyond the context of this paper: For example, allowing users to specify instructions containing what aspects are most important in their query or designers of retrieval systems specifying additional preprocessing steps, e.g., 'Fix typos and retrieve the most relevant passages'. Other contemporary work began investigating these ideas: Zhuang et al. (2024) explore prompting LLMs for retrieval and Weller et al. (2024a,b) let users add an instruction to concretize the information need expressed in the query.

5 Conclusion

We investigated the robustness of transformerbased retrieval models to query variations using a test collection with syntactic query variations that keep semantics. We reproduced Penha et al.'s baseline results and extended them by assessing the robustness of (1) much larger models and (2) a model designed to be typo-robust.

While we were not able to completely replicate the results by Penha et al., we obtained similar results and reaffirmed their conclusions. We show that, while the typo-aware CharacterBERT model was the most robust to typos, this did not lead to robustness to other types of query variations. Finally, we observed that the largest model we tested, while dramatically less efficient than other models, was generally more robust or competitive with all the other tested models regarding all query variations. However, none of the models were robust to the query variations and all were the least robust to typos or keyword queries. Our results indicate that focusing on typo robustness alone is not enough and highlight the need for datasets like Penha et al.'s such that typos and keyword queries no longer are out-of-distribution for IR models.

Ethical Considerations

We do not see any particular ethical ramifications of our work.

Third Party Artifacts Beyond the third party artifacts previously mentioned and cited in the paper, we used the following frameworks: HuggingFace Transformers (Wolf et al., 2020), PyTorch Lightning (Falcon and The PyTorch Lightning team, 2019), NumPy (Harris et al., 2020), pandas (The pandas development team), PEFT (Mangrulkar et al., 2022), PyTorch (Ansel et al., 2024), and pytrec_eval (Van Gysel and de Rijke, 2018).

Limitations

The scope of our experiments was constrained by the number of models per model architecture category that could be sensibly evaluated and by the availability of suitable datasets. Nevertheless, our experiments align with the scope of similar studies and focus on evaluating representative models within each category. Further, note that the sample size for variations from Penha et al.'s TREC DL'19 dataset is limited, particularly for the WordNet-SynSwap transformation, which produced only 16 valid instances.

Due to memory constraints, both inference and training on E5 Mistral were performed using 4-bit

quantization. Precomputing all document representations for the TREC DL'19 training split would have been time-prohibitive, such that we prompttuned E5 Mistral on approximately half the data that CharacterBERT-DR-ST was fine-tuned on. Despite this, the observed improvements across both models suggest the main conclusions drawn from the experiment remain valid.

Finally, this study evaluates the robustness of the re-ranking stage and not the entire retrieval pipeline. As such, the observed effectiveness results may vary if the initial retrieval stage lacks robustness (see Section 4.3).

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A Appendix

A.1 Model Descriptions

Table 6 presents the number of parameters and embedding dimensionality of each model we tested.

SBERT (Reimers and Gurevych, 2019) SBERT uses BERT's mean-pooled final hidden representation as a sentence embedding. We use the msmarcodistilbert-cos-v5 checkpoint, which fine-tuned DistilBERT (Sanh et al., 2019) on MS MARCO Passage (Nguyen et al., 2016).

CBERT (Zhuang and Zuccon, 2022) CBERT replaces BERT's WordPiece Tokenizer with character level tokenization and is trained on a typoinduced version of MS MARCO Passage (Nguyen et al., 2016) using a proposed 'Self-Teaching' objective: The model's output on the original queries is used as a target for the output on the typoed queries. To achieve this, the loss has two components: 1) using KL-divergence to learn similar relevance-score distributions for original and typoed queries and 2) using supervised contrastive cross-entropy-loss to learn an effective ranker on the original queries.

E5 (Wang et al., 2024) To fine-tune Mistral-7B (Jiang et al., 2023) for the generation of embeddings, Wang et al. prompt GPT-4 to generate text retrieval tasks together with synthetic training data and fine-tune the official Mistral-7B checkpoint on this data using contrastive cross entropy loss. While the generated training data contains training samples in 93 different languages, the authors point out that, due to Mistral-7B's pre-training on predominantly English texts and since over 40% of training samples of the synthetic dataset are in English, $E5_{mistral-7b}$, which we call E5 for brevity, is not a multilingual model. E5 is by far the largest model we tested and represents the class of stateof-the-art LLM-based embedding models.

AnglE (Li and Li, 2023) Training objectives for embedding models often aim to learn a cosine similarity of 1 for two similar inputs and 0 otherwise. Since the cosine function is quite flat around these values, the gradient vanishes close to the targets, and it gets harder to improve the model further. To mitigate this Li and Li propose the 'Angle Objective' which interprets the *d*-dimensional real-valued embedding vectors as $\frac{d}{2}$ -dimensional complex-valued vectors to compute the angular distance between two vectors while avoiding vanishing gradients. For our experiments, we use the

| Model | Expected cosine similarity | | | | | | |
|------------------------|----------------------------|---------|--|--|--|--|--|
| | TREC DL'19 | ANTIQUE | | | | | |
| SBERT | 0.036 | 0.050 | | | | | |
| CBERT | 0.731 | 0.732 | | | | | |
| CBERT _{Tuned} | 0.737 | 0.741 | | | | | |
| E5 | 0.555 | 0.568 | | | | | |
| $E5_{Tuned}$ | 0.243 | 0.243 | | | | | |
| AnglE | 0.377 | 0.373 | | | | | |
| Ada v2 | 0.654 | 0.688 | | | | | |

Table 5: The expected cosine similarity for each of the embedding models we tested.

| Model | # Params | Embed. Dim. |
|--------|----------|-------------|
| SBERT | 66M | 768 |
| CBERT | 104M | 768 |
| E5 | 7110M | 4096 |
| AnglE | 335M | 1024 |
| Adā v2 | N/A | 1536 |

Table 6: Number of parameters and embedding dimensionality of the tested models.

UAE-Large-V1 variant, which is a fine-tuned version of BERT_{LARGE} (Devlin et al., 2019).

Ada v2 (Greene et al., 2022) OpenAI's text embedding model text-embedding-ada-002, which we call Ada v2 for ease of reading, was OpenAI's latest text embedding model at the time of our experiments. Although the training regime and model architecture are undisclosed, we include Ada v2 since it represents an interesting category: the stateof-the-art commercial embedding models.

A.2 Anisotropy in Embedding Models

Table 5 presents the expected cosine similarity if two random queries were embedded using each of the embedding models we tested. Intuitively, one would expect a similarity of 0 for unrelated embeddings. However, as Table 5 shows and Mu and Viswanath (2018); Ethayarajh (2019) observed for static and contextualized embeddings respectively, this does not hold since embedding models' outputs often are not uniformly distributed around the origin (the embeddings are 'anisotropic') but directionally localized (Ethayarajh, 2019). Thus, cosine similarity is difficult to compare across embedding models: As seen in Figure 4, a cosine similarity of 0.73 is quite high for SBERT but indicates unrelated semantics for CBERT.

Ethayarajh (2019) observed similar anisotropy of embeddings with LLMs and most notably found that embeddings generated by GPT2 for any two randomly chosen words have a near perfect expected cosine similarity. To compare embedding similarity across models, Ethayarajh subtract μ , the expected cosine similarity given two random



Figure 4: Cosine similarity between the embeddings of each query and every query variation in the dataset.

words. To keep these values within the 0-1 range, we additionally normalize cosine similarity for *anisotropy adjusted cosine similarity* (as defined in Equation (1)), where we calculate μ as the mean cosine similarity of any two queries in the variation dataset. Our values for μ are given in Table 5.

Note that anisotropy may not result in poor ranking robustness or worse effectiveness – E5 maps embeddings to a similarly small range as CBERT and Ada v2 but its ranking-robustness and effectiveness is the highest among all tested models. Anisotropy is, however, suboptimal, as Mu and Viswanath (2018) discovered that making embeddings more isotropic by simply subtracting a common mean vector improved effectiveness on general natural language processing tasks. We could not observe any improvements when applying their algorithm (Mu and Viswanath, 2018, Algorithm 1) to retrieval, likely because they study static embeddings and all models we tested are contextualized.

A.3 Promptable Embedding Models

Mistral's instructable nature teases a novel concept: promptable embedding models. Embeddings generated for retrieval should be asymmetric, i.e., the same text should not be mapped to the same embedding when embedded as a query and as a document. Otherwise, when the most relevant documents are retrieved by similarity, the query would rank the highest though it does not fulfill the information need. To mitigate this, Li and Li (2023) and Wang et al. (2024) recommend prompting the queries' generation for AnglE and E5 respectively.

Since Mistral, like other LLMs, shows unprecedented zero-shot effectiveness in general natural language tasks, we investigated if we could generate robust embeddings solely by prompting the Mistral-based embedding model E5 differently. Wang et al. (2024) recommend prompts of the form

| Instruction | nD | CG@ | 10 |
|---|-------|------|----------|
| | Orig. | Туро | Δ |
| Given a web search query, retrieve relevant passages that answer the query | .71 | .66 | .050 |
| Given a web search query, fix typos and retrieve relevant passages that answer the query | .70 | .65 | .056 |
| Synthesize the ideal query to express the given informationneed and retrieve relevant passages for it | .72 | .66 | .067 |
| Do what you want | .55 | .44 | .112 |

Table 7: A selection of the instructions we used to instruct E5's query embedding generation. The first instruction is the one recommended by Wang et al. (2024).

Instruct: {instuction}\nQuery: {query}, where {instruction} and {query} are replaced with the instruction and query respectively and \n marks a line break. To assess the instruction's impact on ranking effectiveness and robustness, we evaluated different instructions on the typo-induced dataset by Zhuang and Zuccon (2022). We focus on typos since E5 is least robust to these on TREC DL'19, and we avoid using the Penha et al. (2022) dataset as not to fit a prompt on a test-set.

A subset of the instructions we tested is shown in Table 7 and every instruction and their effectiveness on the original queries and typo-induced queries are plotted in Figure 5. The figure shows that the original instruction by the authors is already quite robust, and more effective rankings on the original queries are more robust to typos as well (instructions further to the right on the x-axis are brighter, i.e., closer to the ideal line). This shows that the zero-shot effectiveness observed with stateof-the-art LLMs may not translate to promptable embedding models based on these LLMs but choosing the right instruction can improve effectiveness and robustness. We have not found an instruction that improves ranking robustness considerably beyond what the author's instruction achieves, yet we can not rule out that such a prompt may exist. On the contrary, we observe the positive trend that more effective prompts improve robustness.

A.4 Different Initial Retrieval

To investigate effects induced by the initial retrieval, we further evaluated CBERT, E5 and their tuned variants with ColBERT v2 for initial retrieval. Both effectiveness and robustness behave similarly however, irrespective the initial retrieval model, as seen in Figure 6 and Table 8. This probably stems from the large number of initially retrieved passages.

| | | | AN'I | IQUE | | | | | |
|-----------------|--|------------------------------|-------------------------------|--------------------------------|--------------------------------|-------------------------------|-------------------------------|--------------------------------|---|
| Query variation | | BM25 + | | | | ColBERT v2 + \dots | | | |
| Category | Transform. heuristic | CBERT | CBERT _{Tuned} | E5 | $E5_{Tuned}$ | CBERT | CBERT _{Tuned} | E5 | E5 _{Tuned} |
| Original | | 0.29 | 0.27 | 0.41 | 0.41 | 0.28 | 0.26 | 0.44 | 0.43 |
| Misspelling | NeighbCharSwap RandomCharSub QWERTYCharSub | 0.26* 0.26* 0.26* | 0.23* 0.24* 0.25 | 0.37* 0.37* 0.38* | 0.38* 0.37* 0.38* | 0.24* 0.25* 0.25* | 0.22* 0.23* 0.24 | 0.40* 0.39* 0.40* | $\begin{array}{r} 0.40^{*} \\ 0.40^{*} \\ 0.40^{*} \end{array}$ |
| Naturality | RemoveStopWords T5DescToTitle | 0.24* 0.22* | 0.24* 0.23* | 0.36* 0.31* | 0.36* 0.33* | 0.24* 0.23* | 0.23* 0.22* | 0.37* 0.33* | 0.39* 0.35* |
| Ordering | RandomOrderSwap | 0.27 | 0.27 | 0.39* | 0.39* | 0.26 | 0.25 | 0.41* | 0.41* |
| Paraphrasing | BackTranslation T5QQP WordEmbedSynSwap WordNetSynSwap | 0.28 0.25 0.26 0.24 | 0.27 0.25 0.24* 0.22 | 0.40 0.37* 0.40* 0.34 | 0.39 0.37 0.40* 0.35* | 0.28 0.24 0.25* 0.23 | 0.25 0.24 0.22* 0.20 | 0.44 0.40* 0.42* 0.36 | 0.42 0.39 0.42* 0.38 |

* significant difference (Bonferroni corrected two-sided paired Student's T-Test at p < 5%) to ranking on the original query

Table 8: Mean nDCG@10 on ANTIQUE of CBERT and E5 before and after fine-tuning on our training set. The models re-rank the top 1000 passages initially retrieved by BM25 and ColBERT v2.



 $\begin{array}{c} 0.2 \\$

Figure 5: Prompt tuning results. Each point marks a prompt's effectiveness in face and absence of typos. The cross marks the prompt used by E5's authors. Points further from the ideal line (same effectiveness regardless of typos) are darker.

Figure 6: Ranking-robustness of CBERT and E5 before and after fine-tuning on our training set. Each model re-ranks the top 1000 passages retrieved by BM25 (top) and ColBERT v2 (bottom).