



3D-Kernel Foveated Rendering for Light Fields

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¹University of Maryland, College Park

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Content

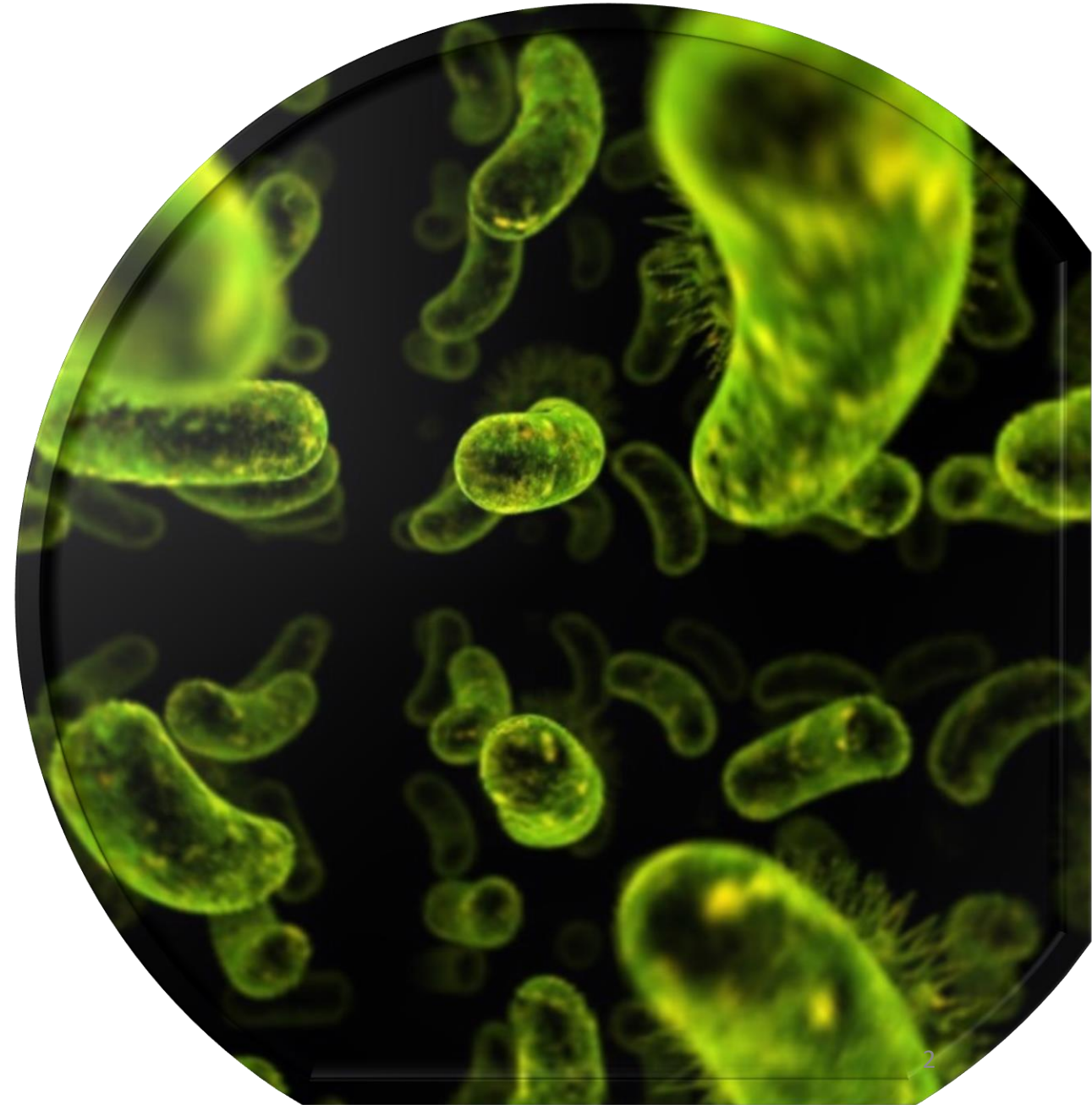
Motivation

Foveated Rendering

Our Approach

User Study

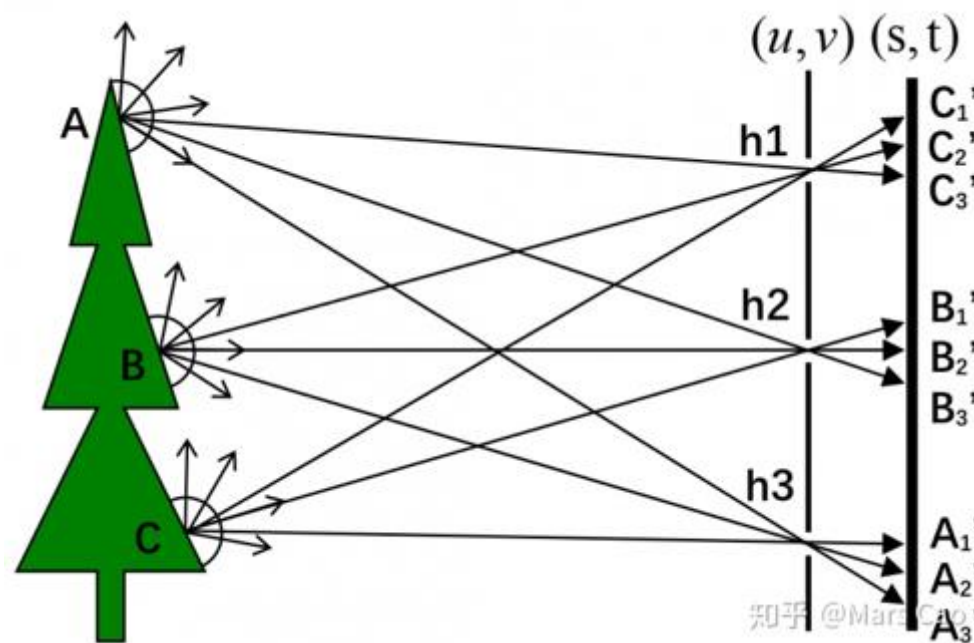
Rendering Acceleration



Light Field $L(u, v, s, t)$

uv - camera plane

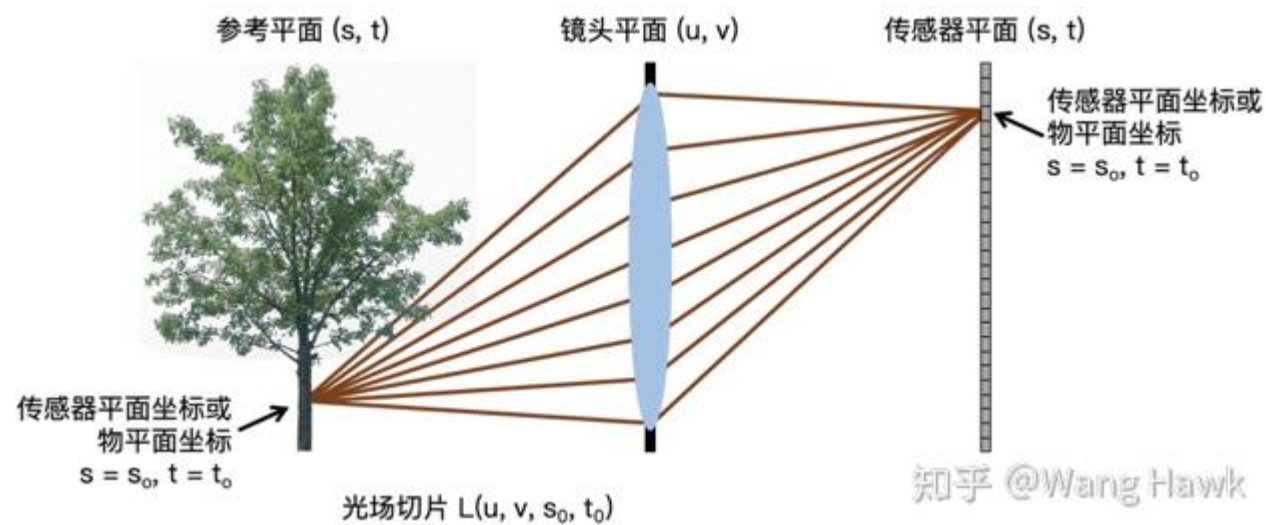
st - focal plane



Light Field $L(u, v, s, t)$

uv - camera plane

st - focal plane



view_match_v010.nk [modified] - NukeX

File Edit Workspace Viewer Render Cache Help Shotgun Lytro

Viewer1

rgba rgba.alpha sRGB

f/8 1 Y 1

square_2K 2048x2048 bbox: 0 | x=700 y=772 0.36792 0.36475 0.38232 1.00000 H:251 S:0.05 V:0.38 L: 0.36669

20 | 20 22

Global I 22 10

Node Graph Curve Editor Dope Sheet

Properties Lytro Rig Select (alpha)

Find Rig Highlight Refresh

Find:

Planar List

Wedge 1 (0 - 999)

Wedge 2 (1000 - 1999)

Wedge 3 (2000 - 2999)

Wedge 4 (3000 - 3999)

Wedge 5 (4000 - 4999)

00045 00001 00002 00003 00004 00005

00006 00007 00008 00009 00010 00011 00012

00013 00014 00015 00016 00017 00018 00019 00020

00021 00022 00023 00024 00025 00026 00027 00028 00029

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00040 00041 00042 00043 00044 00045 00046 00047 00048 00049 00050

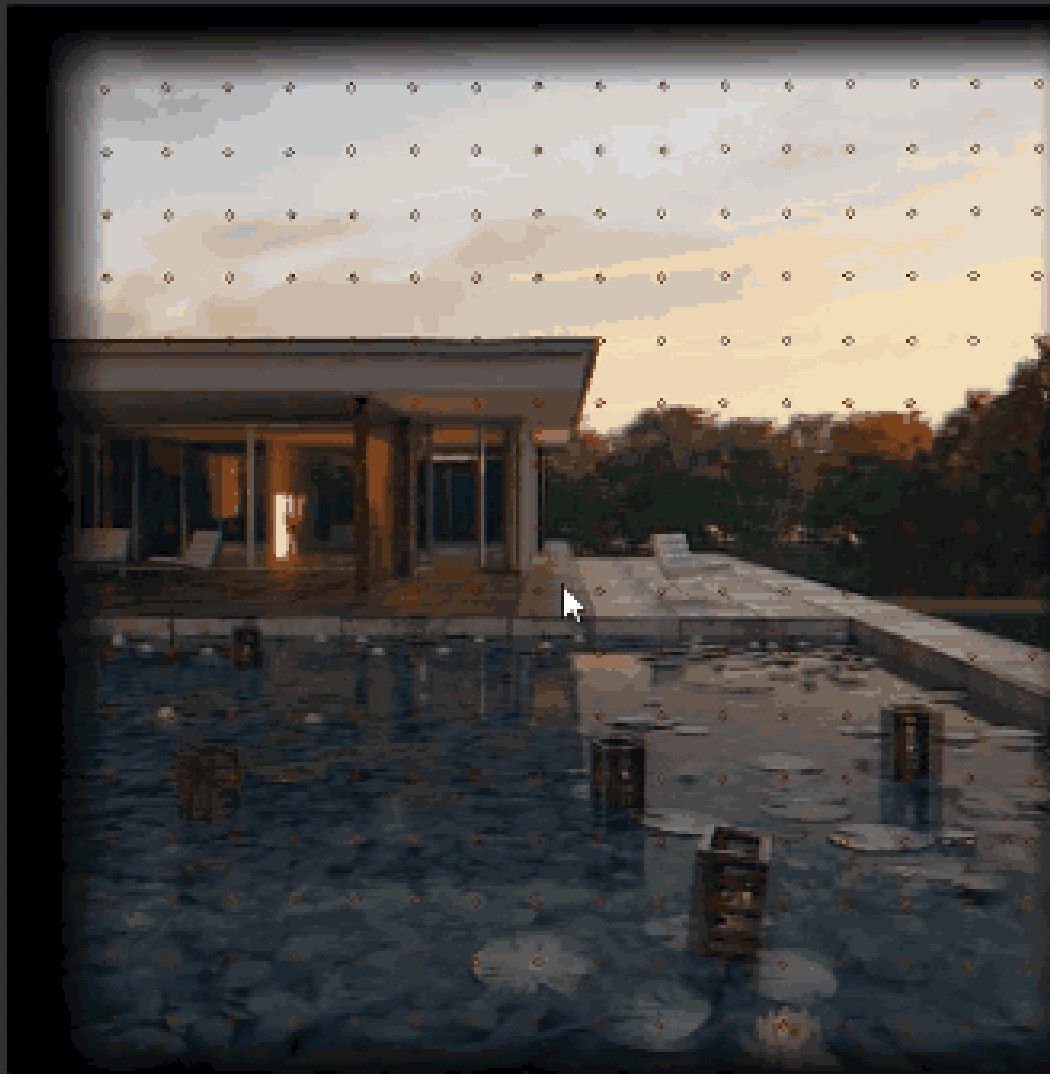
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00061 00062 00063 00064 00065 00066 00067 00068 00069

00070 00071 00072 00073 00074 00075 00076 00077

00078 00079 00080 00081 00082 00083 00084

00085 00086 00087 00088 00089 00090



Light field info

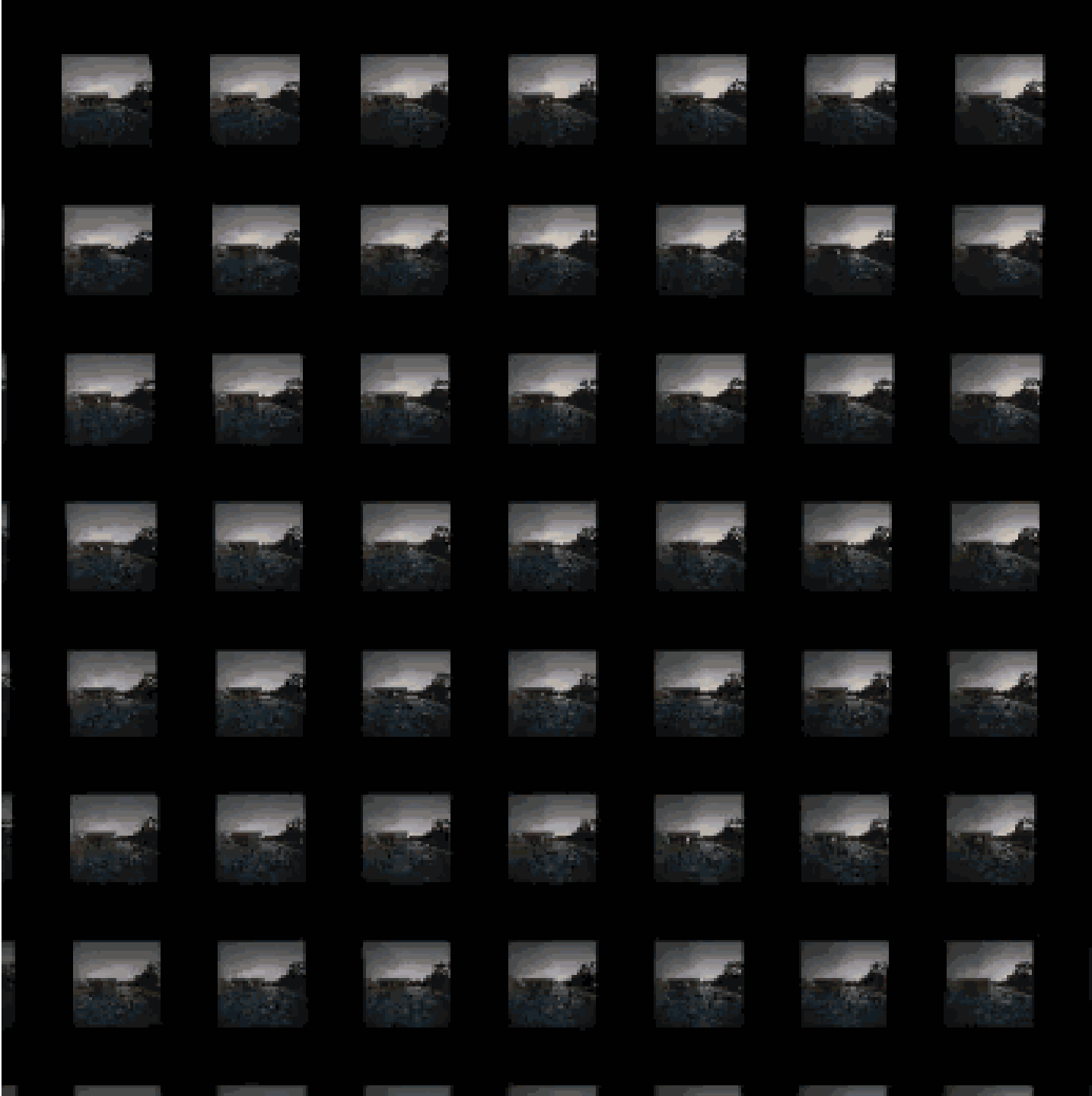
Camera plane: 16 x 16 Capture interval: 10 cm
Image plane: 1024 x 1024 Capture density: 100 cameras/m²
Ray count: 268,44 Megarays Fov: 90°

Viewpoint camera

Position (m): X: 0,296 Y: -0,740 Z: -1,936
Rotation: X: 0,000 Y: -0,138 Z: 0,000
Image size (px): 512 x 512
FOV (°): 47,000
Focusing plane (m): 15,000
Aperture (cm): 0,200 Bilinear

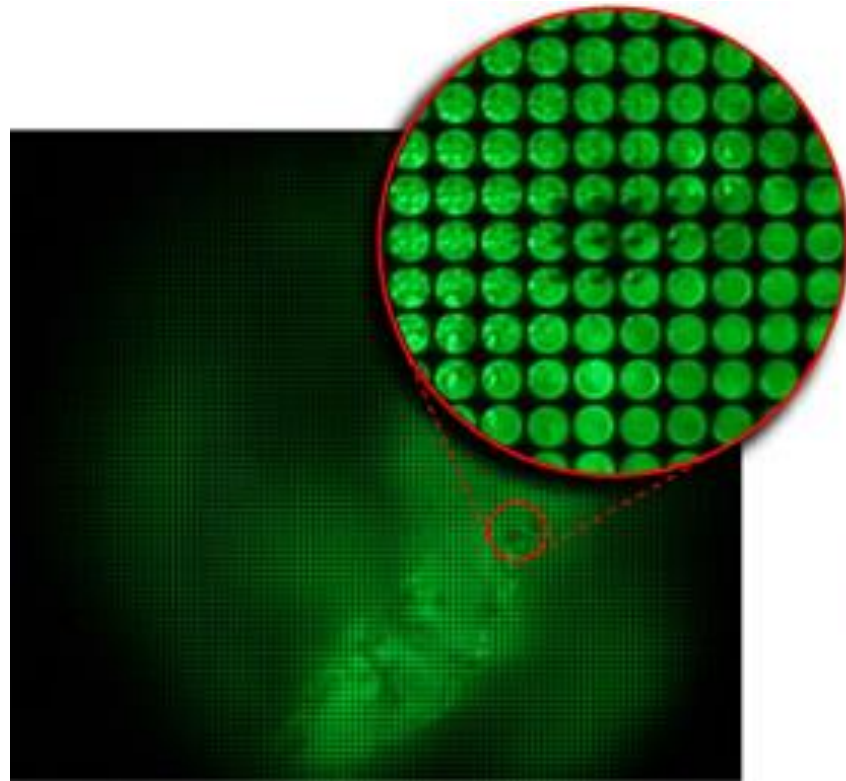
Geometry



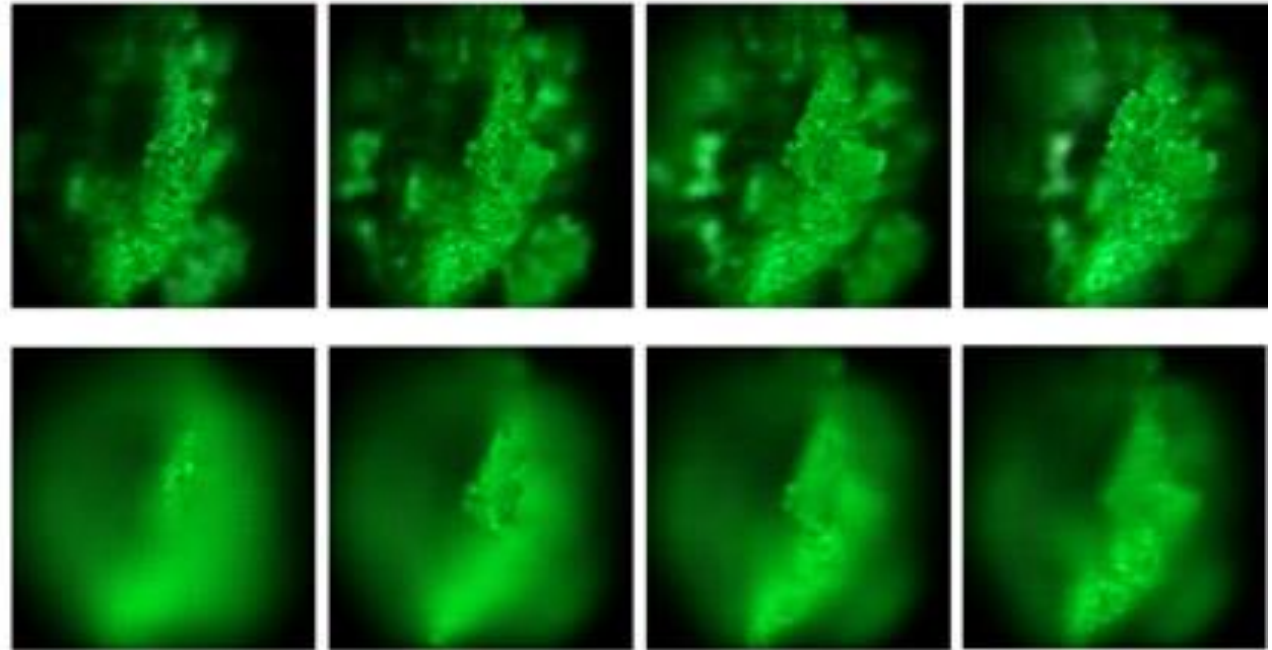




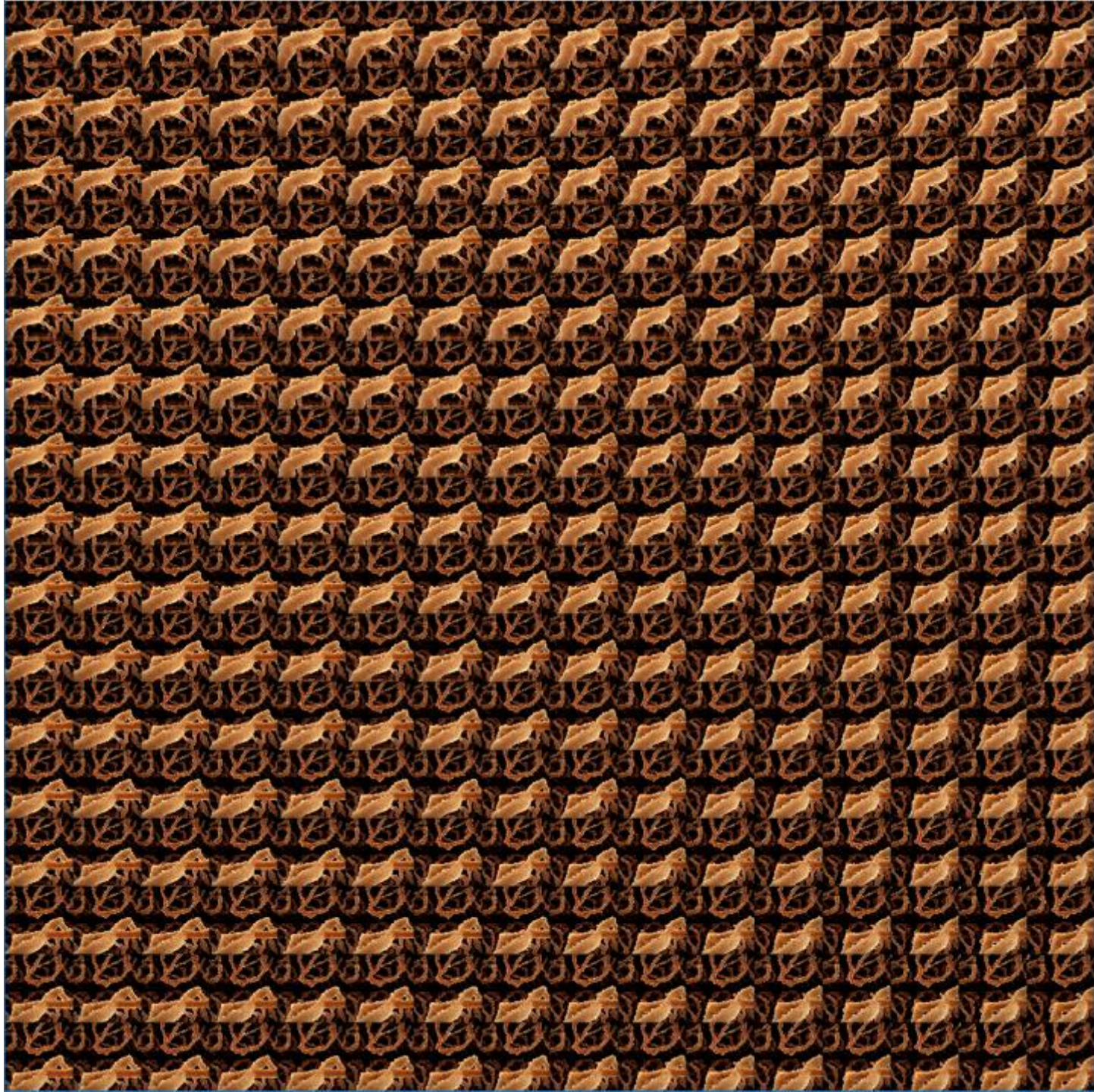
Light field “autostereoscopic”

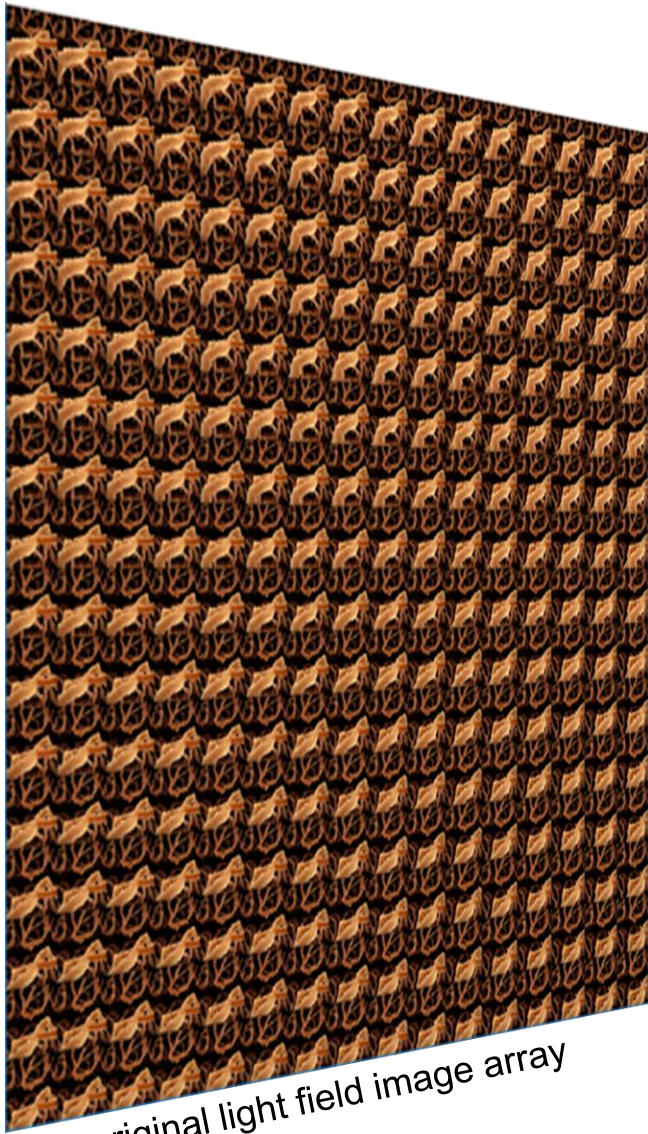


a light field captured by photographing a speck of fluorescent crayon wax through a microscope objective and microlens array



"Since microscopes are inherently orthographic devices,
perspective views represent a new way to look at microscopic specimens." [1]



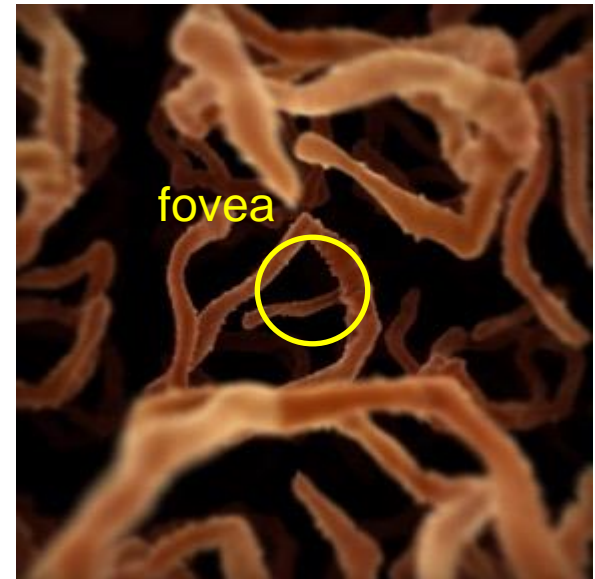


original light field image array

foveated rendering



Screen



Content

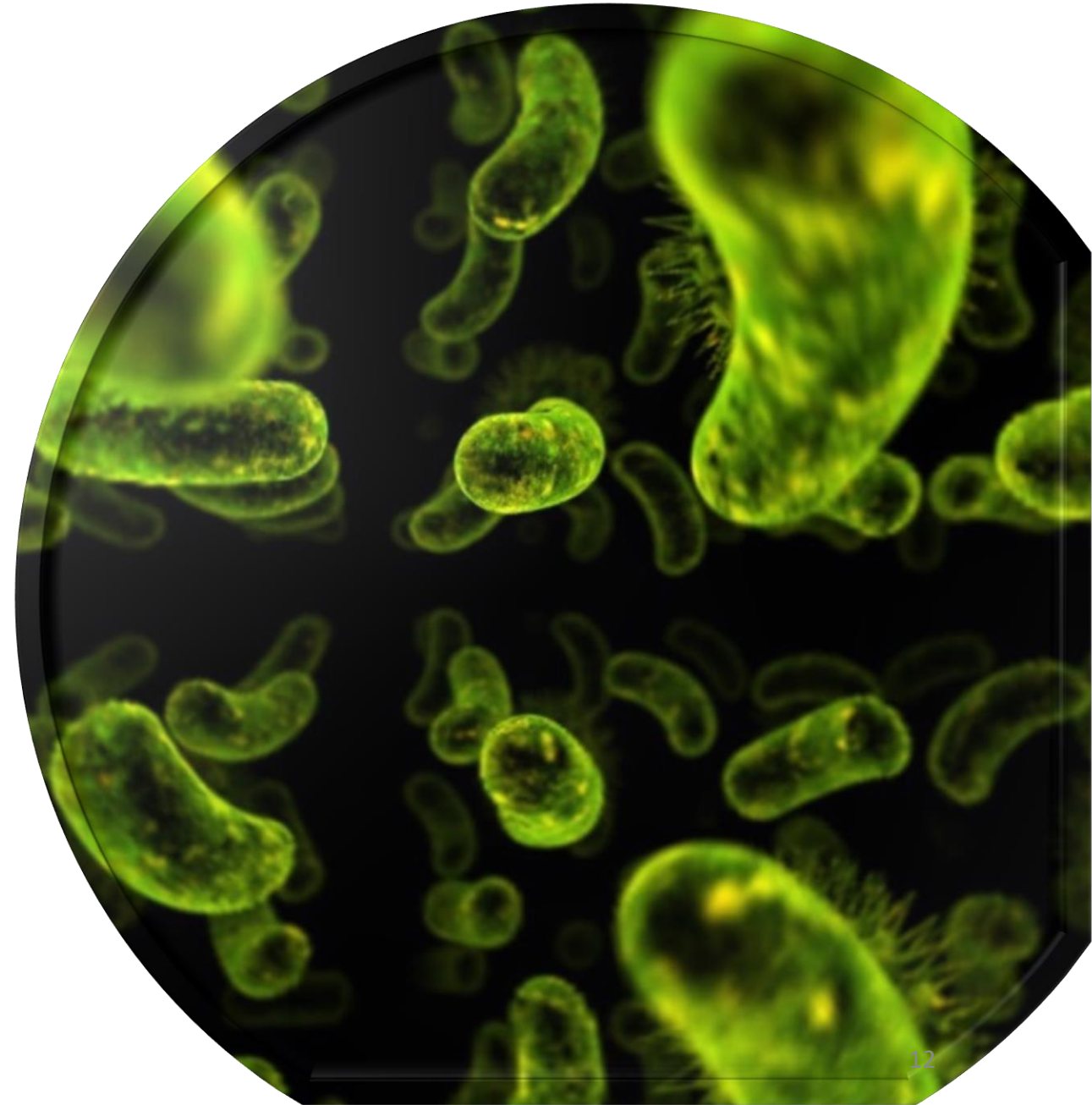
Motivation

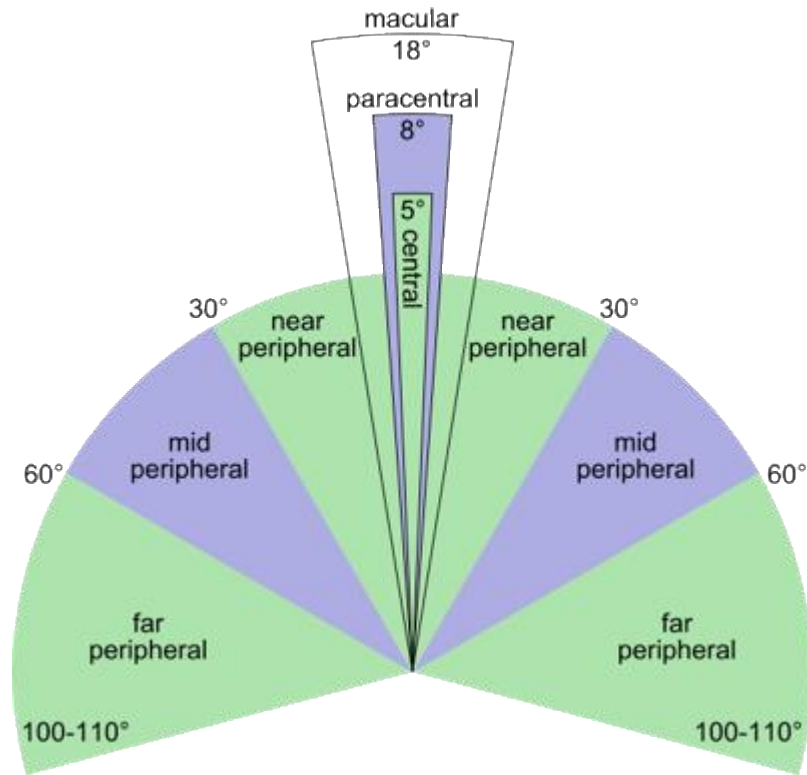
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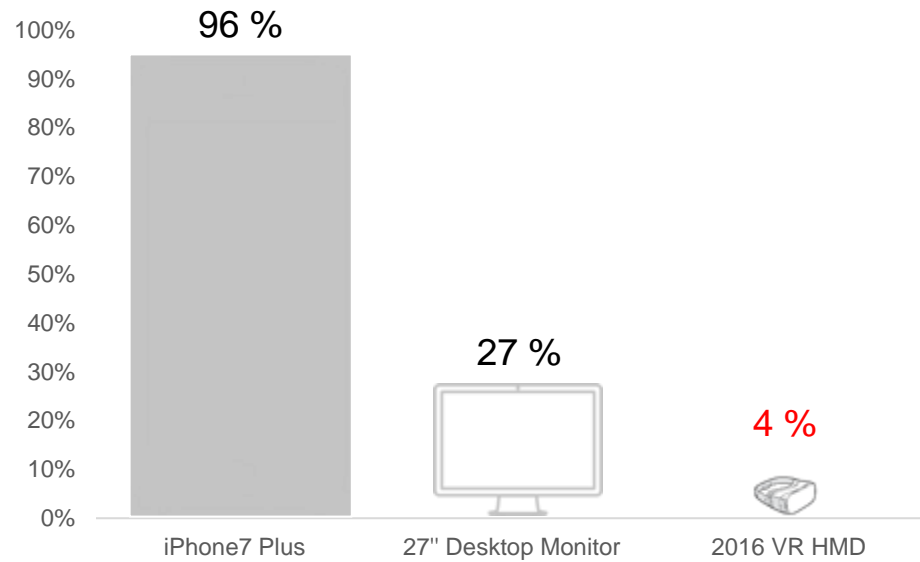




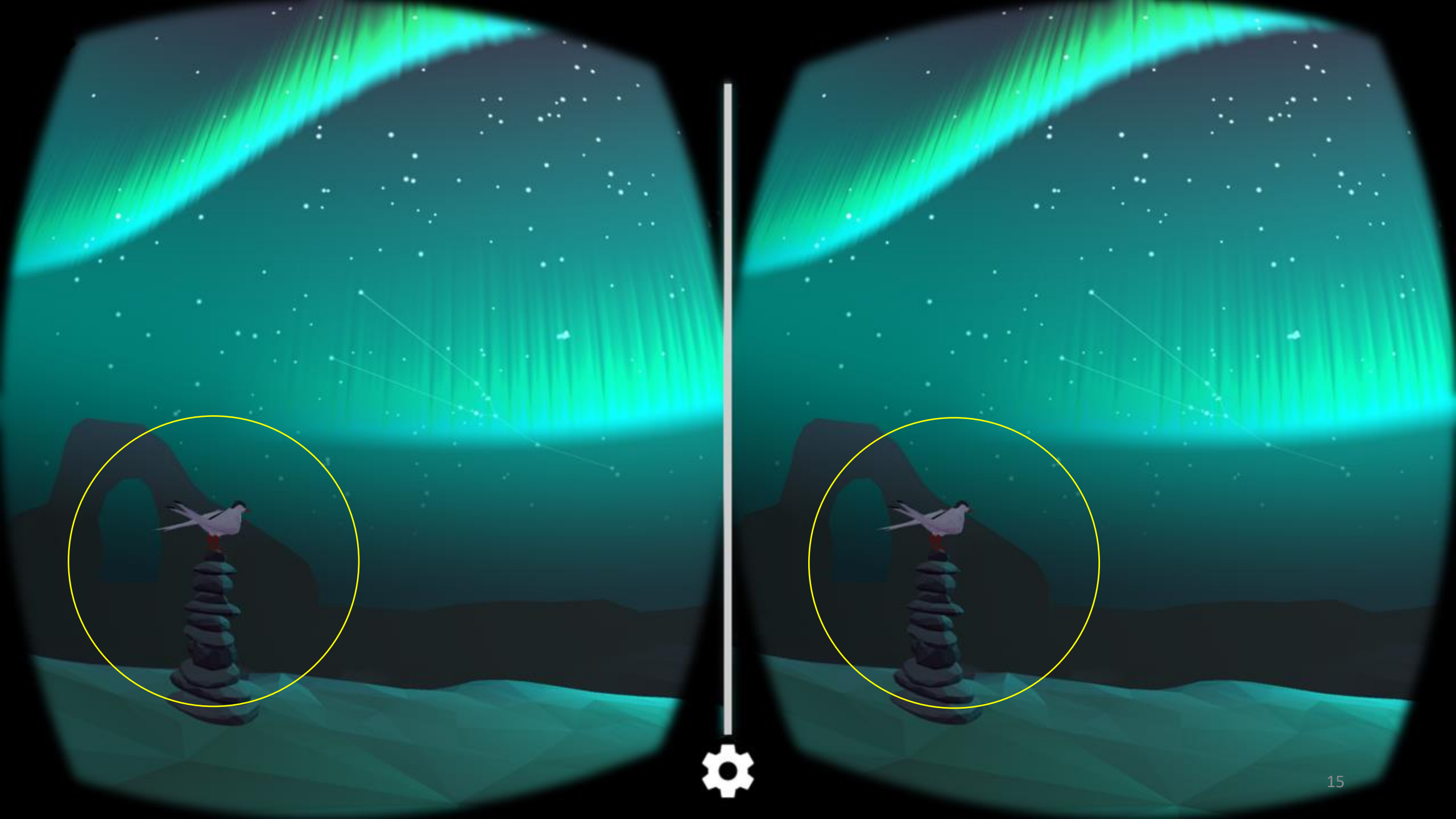
foveal region: the human eye detects significant high-fidelity detail
peripheral region: the human eye detects little high-fidelity detail

- Virtual reality is a challenging workload
- Most VR pixels are peripheral

Percentage of the Foveal Pixels



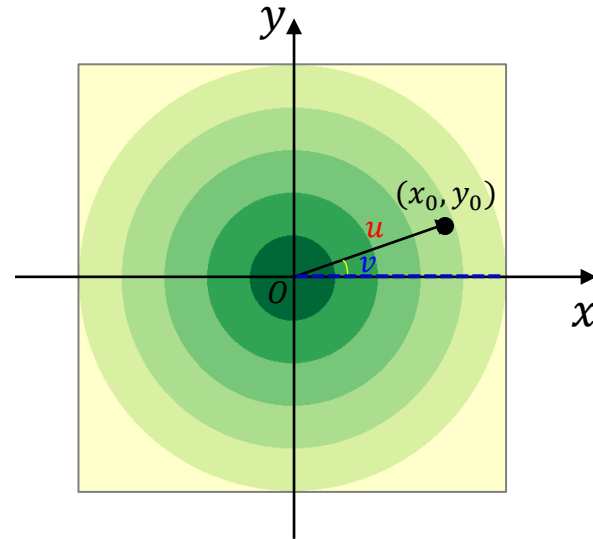
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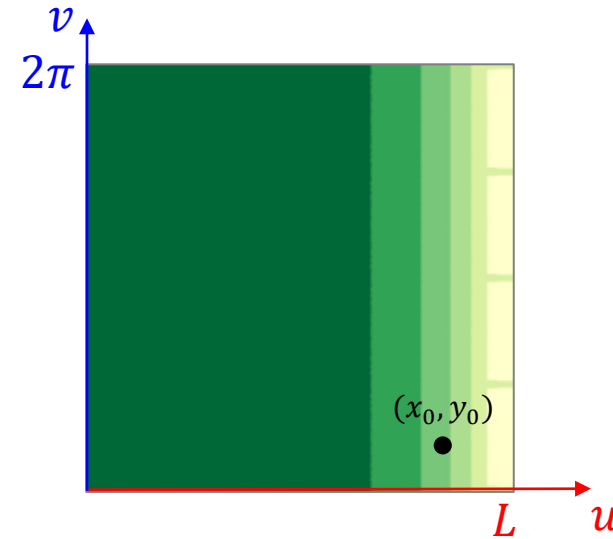
Foveated Rendering



Log-polar mapping [Araujo and Dias 1996]



Cartesian coordinates
(x, y)



Log-polar coordinates
(u, v)

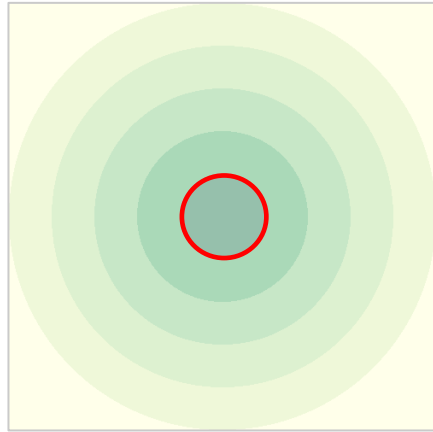
Log-polar Mapping

$$u = \frac{\log\sqrt{x^2 + y^2}}{L} \cdot w$$

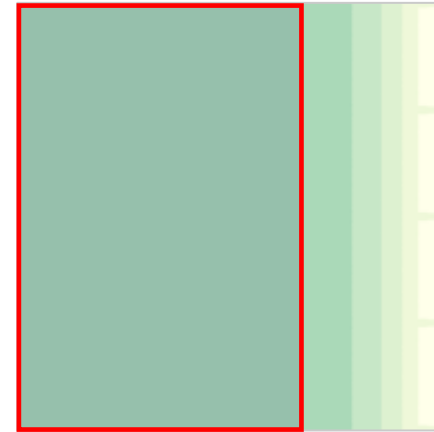
$$v = \frac{(\arctan\frac{y}{x} + \mathbf{1}[y < 0] \cdot 2\pi)}{2\pi} \cdot h$$

- W : screen width H : screen height w : buffer width h : buffer height
- $\mathbf{1}[y < 0] = \begin{cases} 1 & y < 0 \\ 0 & y > 0 \end{cases}$
- $L = \log\sqrt{W^2 + H^2}$

Log-polar mapping [Araujo and Dias 1996]



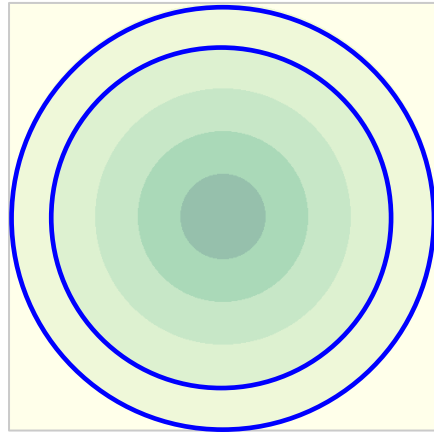
Cartesian coordinates
(x, y)



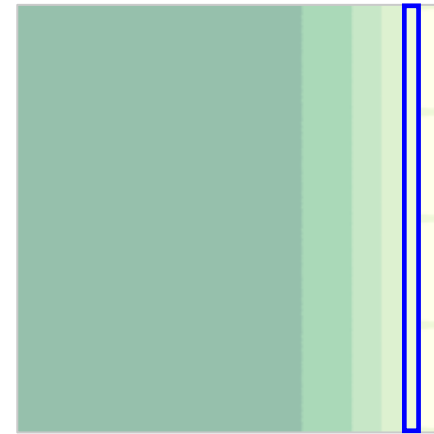
Log-polar coordinates
(u, v)

The closer the point is to the center, the higher pixel density it preserves.

Log-polar mapping [Araujo and Dias 1996]



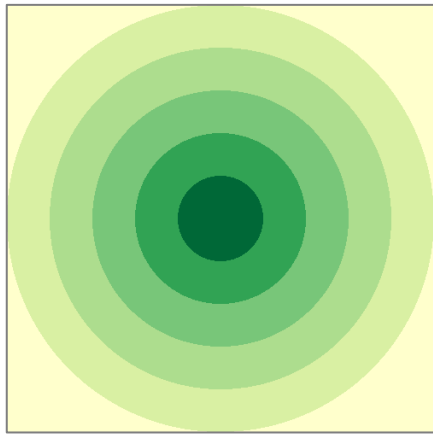
Cartesian coordinates
(x, y)



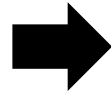
Log-polar coordinates
(u, v)

Points in the **peripheral regions** are naturally **compressed** in the log polar domain.

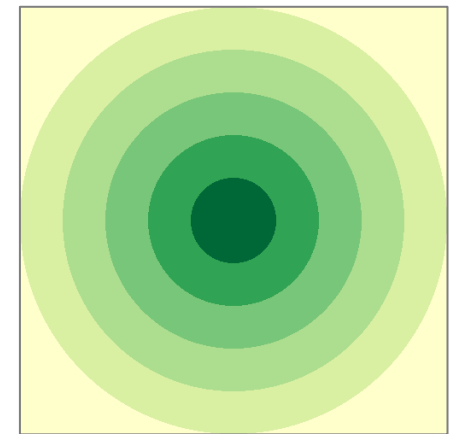
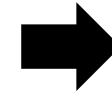
Log-polar mapping [Araujo and Dias 1996]



Cartesian coordinates
(x, y)



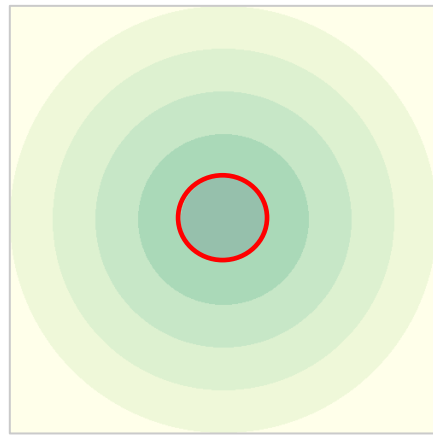
Log-polar coordinates
(u, v)



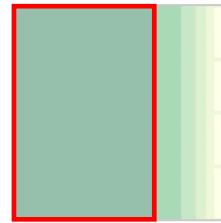
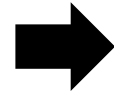
Cartesian coordinates
(x, y)

We can recover the image by performing the inverse transformation

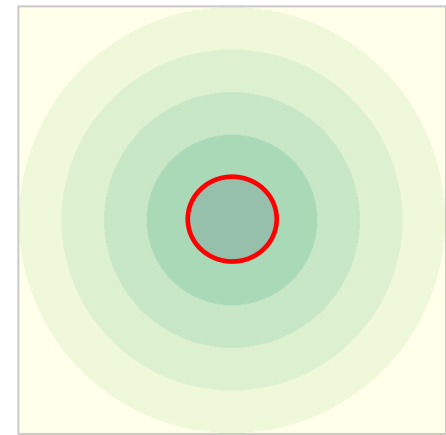
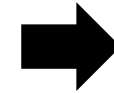
Log-polar mapping [Araujo and Dias 1996]



Cartesian coordinates
(x, y)



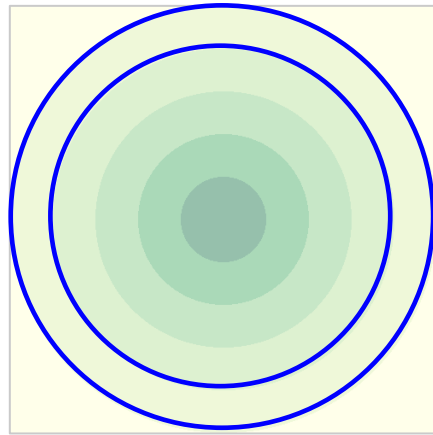
Log-polar coordinates
(u, v)



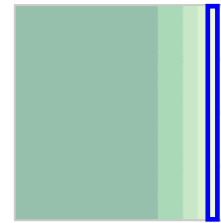
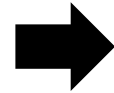
Cartesian coordinates
(x, y)

With smaller log-polar buffer, the **foveal** preserves the original pixel density while the **peripheral** regions are compressed.

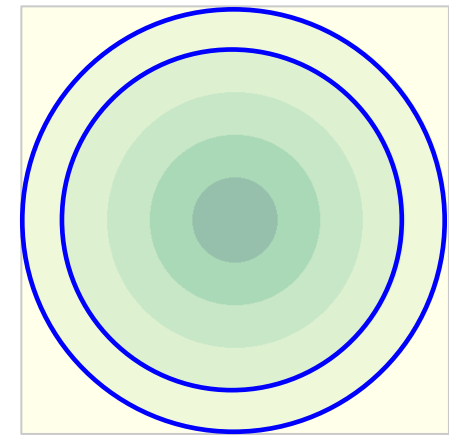
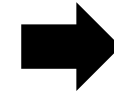
Log-polar mapping [Araujo and Dias 1996]



Cartesian coordinates
(x, y)



Log-polar coordinates
(u, v)



Cartesian coordinates
(x, y)

With smaller log-polar buffer, the **foveal** preserves the original pixel density while the **peripheral** regions are **compressed**.

Log-polar Mapping for 2D Image [Antonelli et al. 2015]



MxM cartesian image



RxS log-polar image




MxM reconstructed cartesian image

Log-polar Mapping for 2D Image



RxS log-polar image

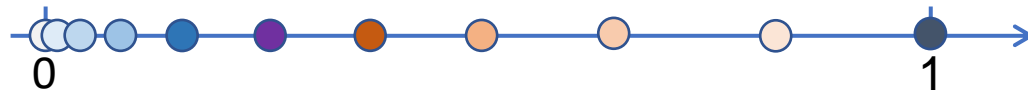
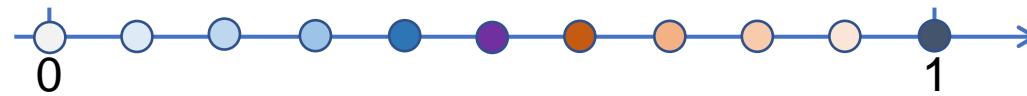
Inverse log-polar mapping



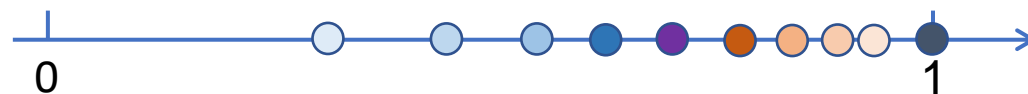
MxM reconstructed cartesian image

What if we directly render in the log-polar domain to reduce the rendering cost?
How to improve the quality in the peripheral regions?

Change the Distribution of Pixels (1D)



$$K(x) = x^2$$



$$K(x) = x^{\frac{1}{2}}$$

Kernel Log-polar Mapping

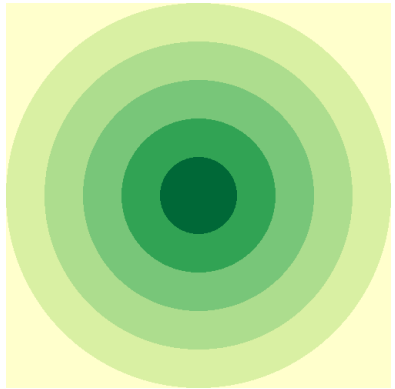
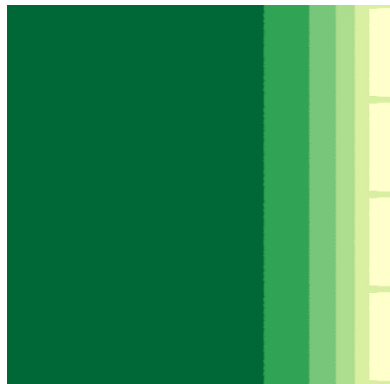


Image in Cartesian Coordinates



$$K(x) = x$$



$$K(x) = x^2$$



$$K(x) = x^3$$



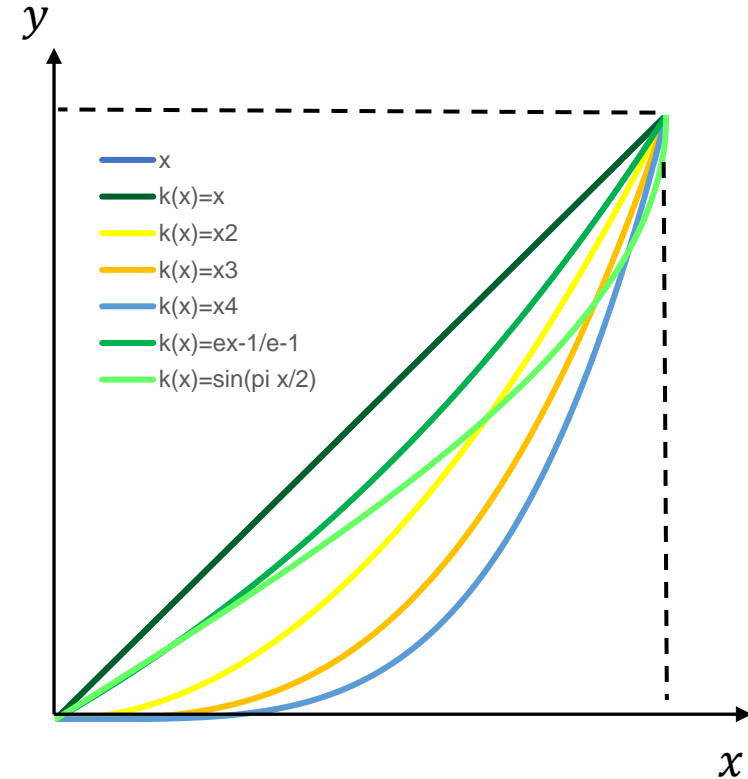
$$K(x) = x^4$$



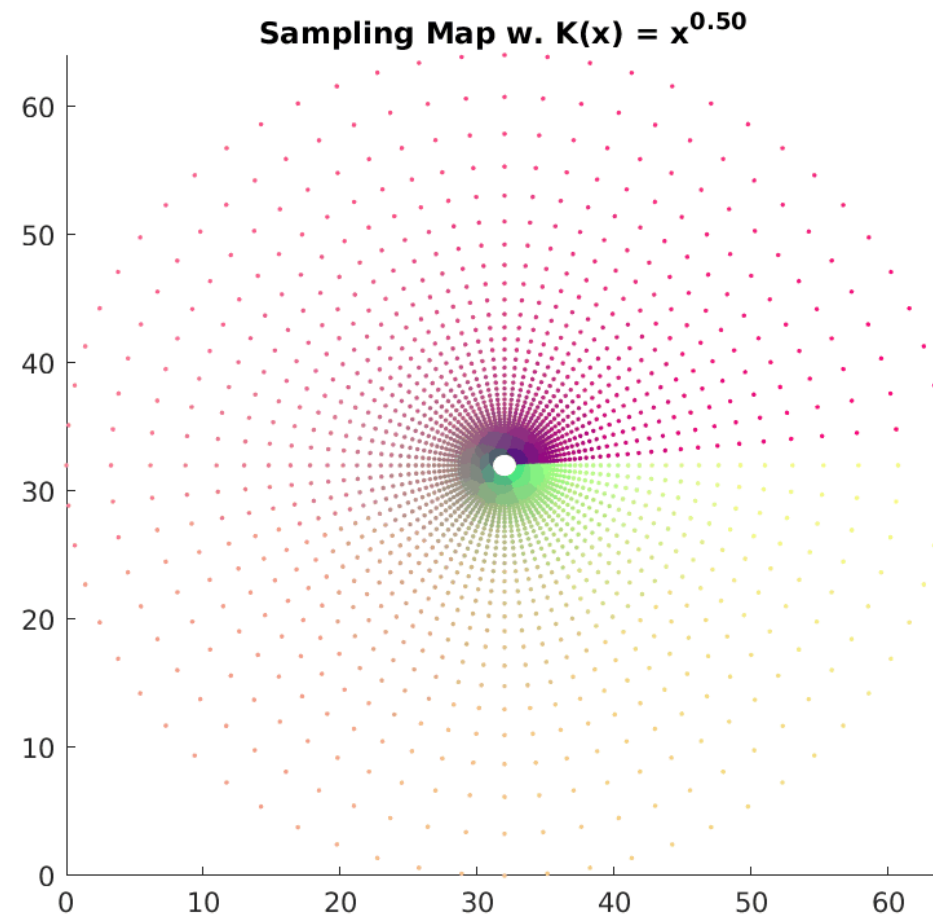
$$K(x) = \frac{e^x - 1}{e - 1}$$



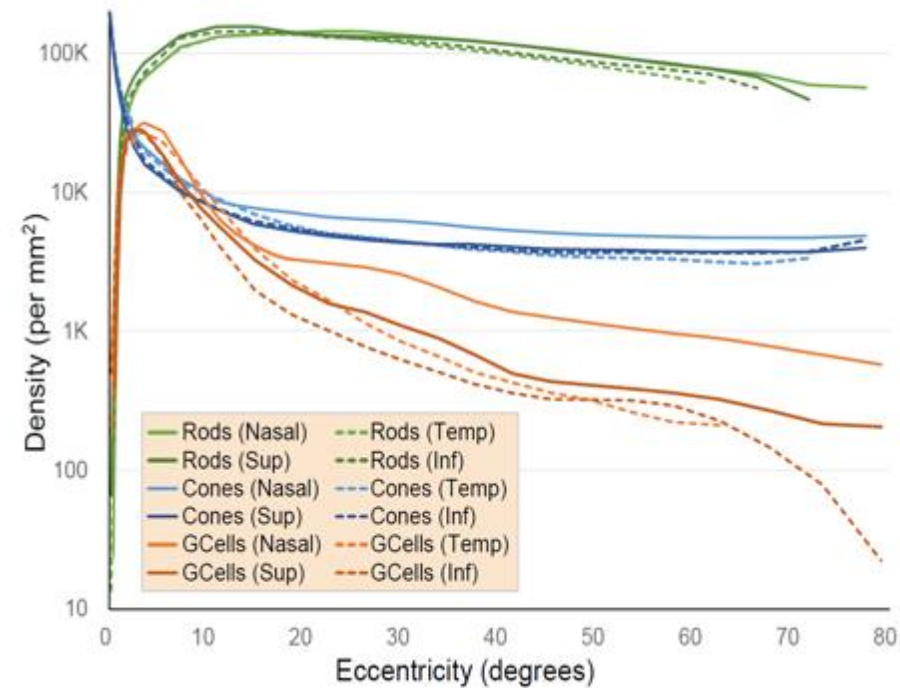
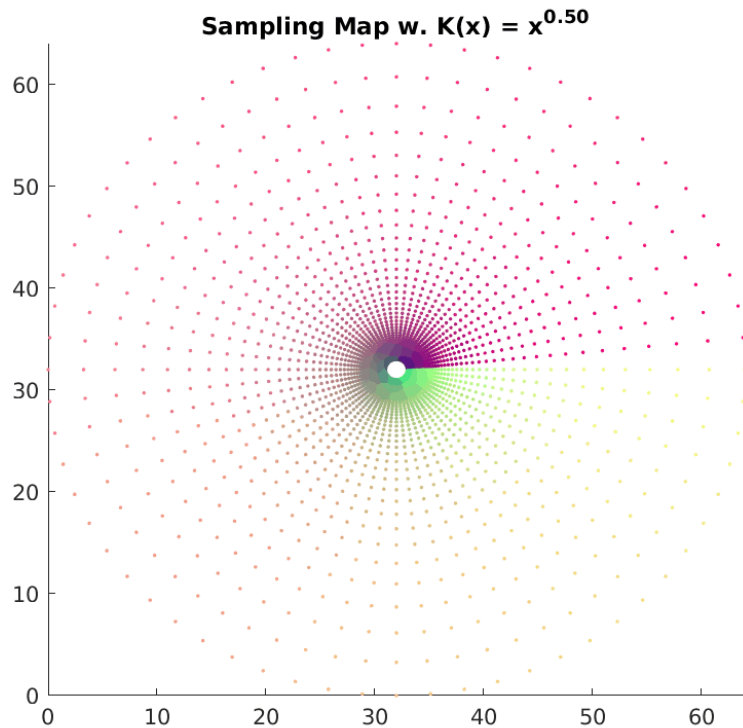
$$K(x) = \sin\left(\frac{\pi}{2}x\right)$$



Change the Distribution of Pixels (2D)



Kernel Foveated Rendering



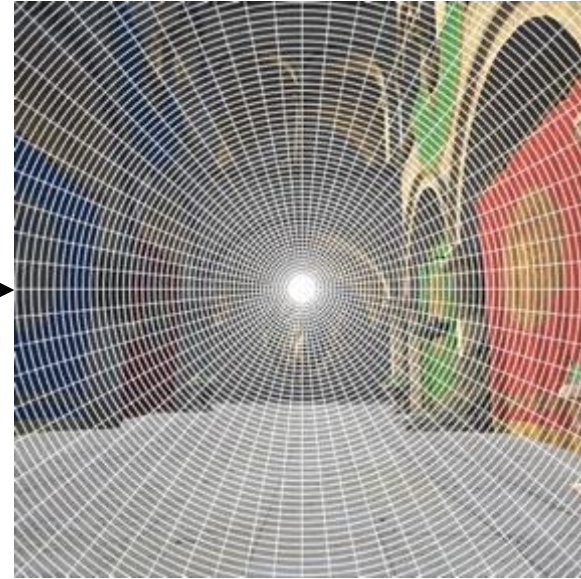
Distribution of pixels $\xrightarrow{\text{mimic}}$ *Distribution of photoreceptors in the human retina*



W



W

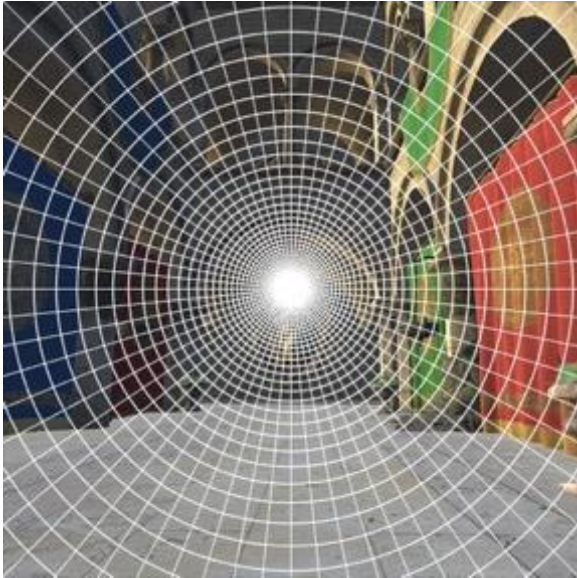


W

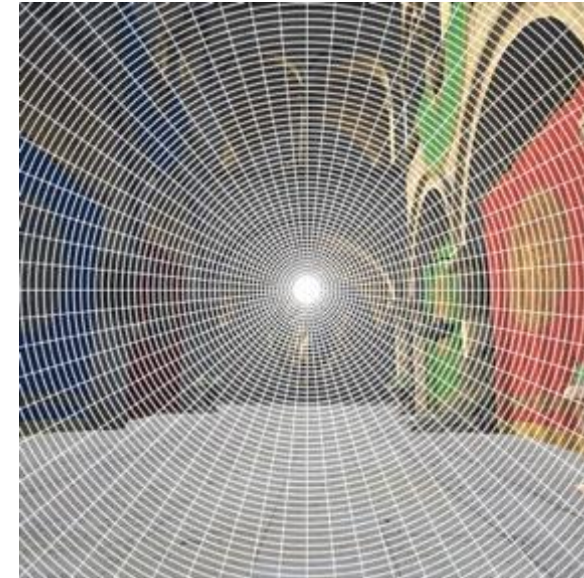
Kernel log-polar Mapping

- Define buffer parameter σ

$$\sigma = \frac{W}{w}$$



Result of log-polar
($K(x) = x$)



Result of kernel log-polar
($K(x) = x^4$)

Kernel log-polar Mapping

- *Define buffer parameter σ*

$$\sigma = \frac{W}{w}$$

- *Define kernel function parameter α*

$$K(x) = x^\alpha$$

Buffer parameter
 σ

Original Frame



Buffer



Screen



Sample Map

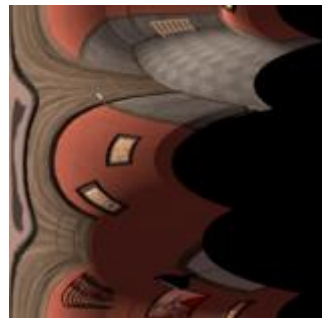


$\sigma = 1.2$

Original Frame



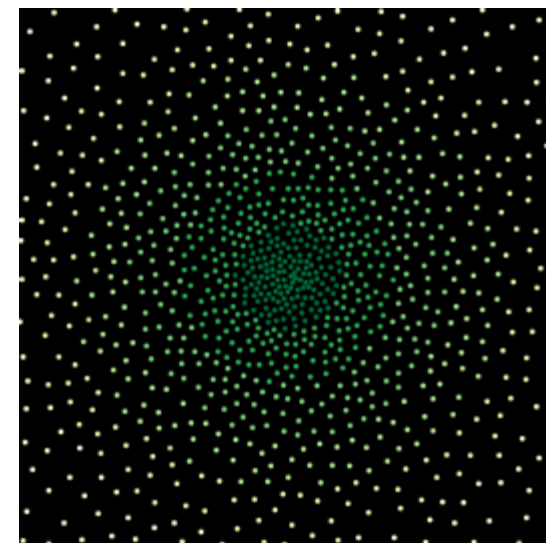
Buffer



Screen



Sample Map

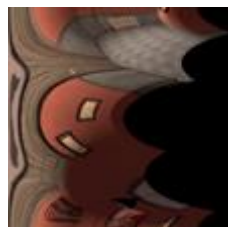


$$\sigma = 1.7$$

Original Frame



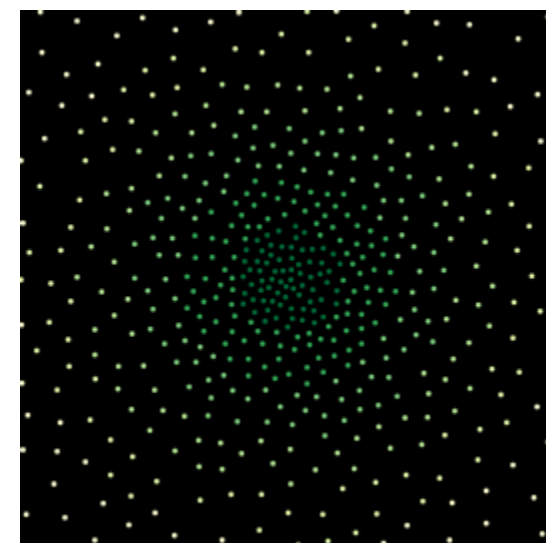
Buffer



Screen

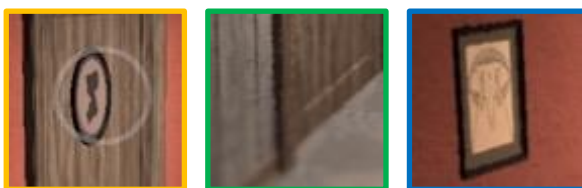
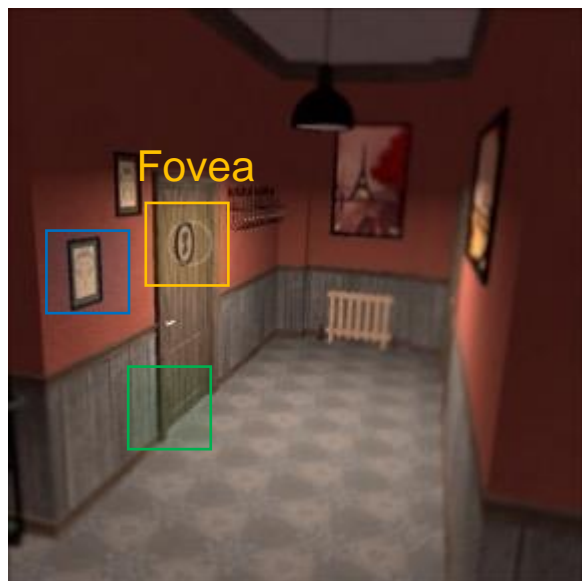


Sample Map

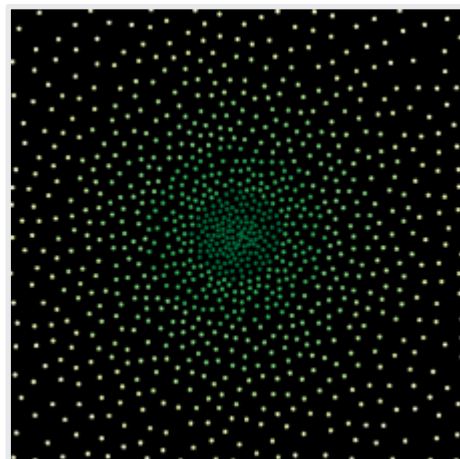
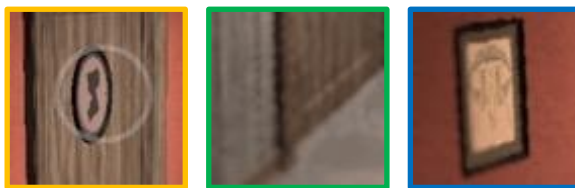
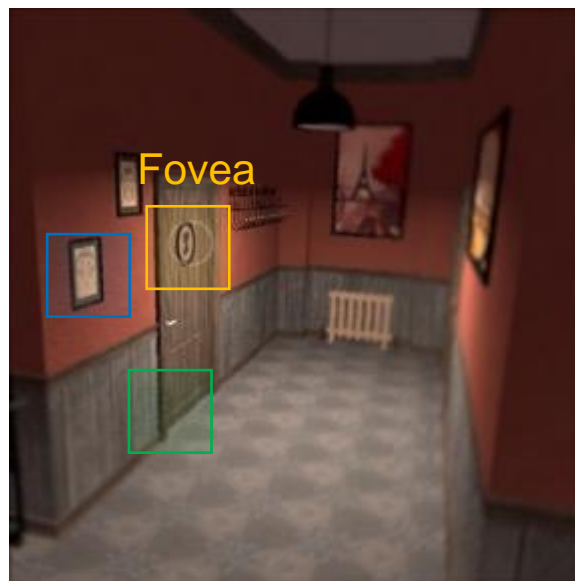


$$\sigma = 2.4$$

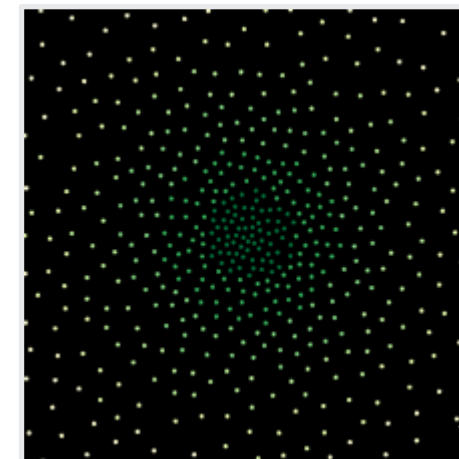
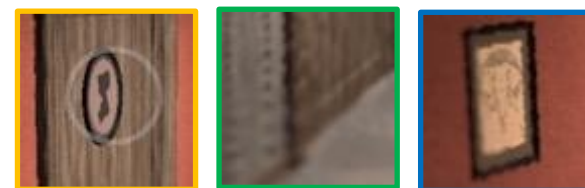
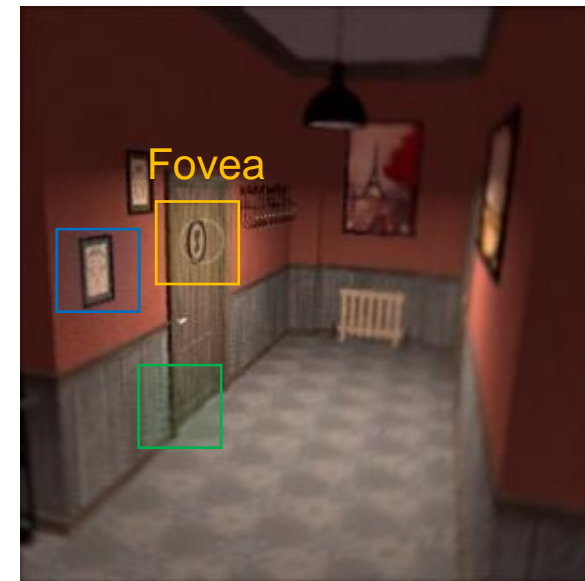
$\sigma = 1.2$



$\sigma = 1.7$



$\sigma = 2.4$



kernel function parameter
 α

Original Frame



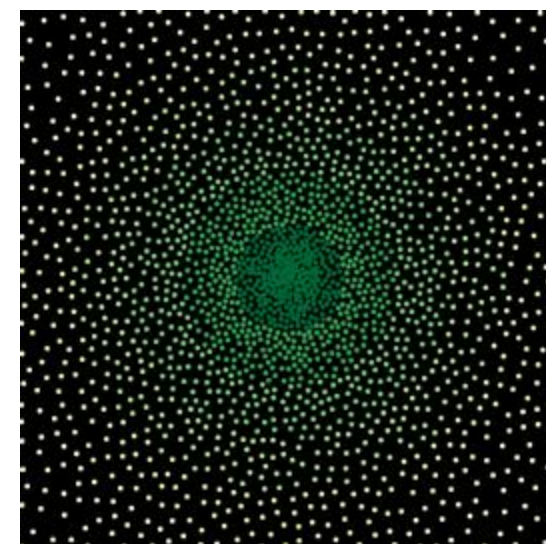
Buffer



Screen



Sample Map

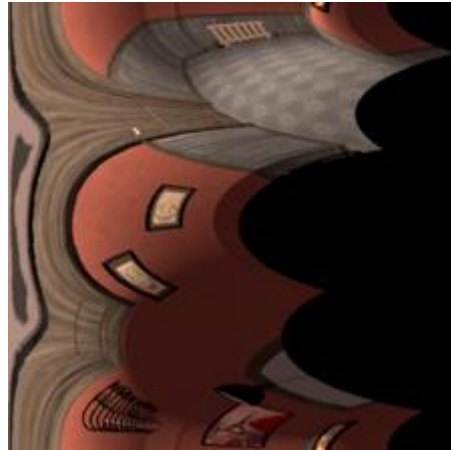


$$\alpha = 1$$

Original Frame



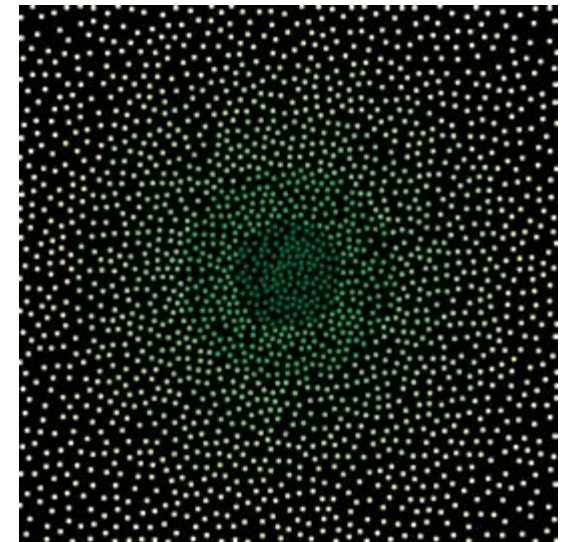
Buffer



Screen



Sample Map



$$\alpha = 4$$

Original Frame



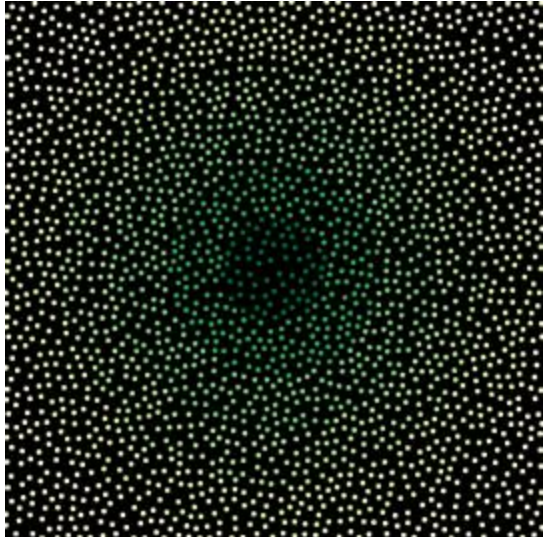
Buffer



Screen

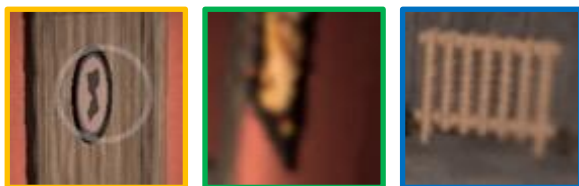


Sample Map

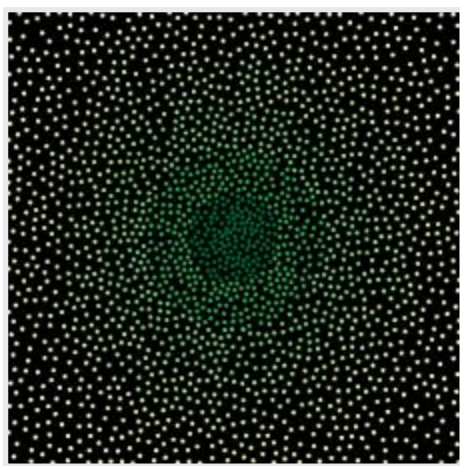
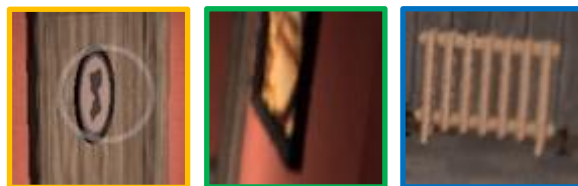


$\alpha = 6$

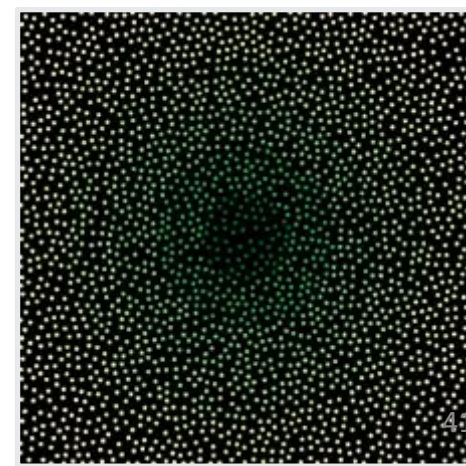
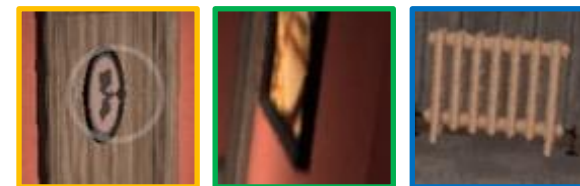
$\alpha = 1$



$\alpha = 4$



$\alpha = 6$



G-buffer



World position

Bit tangent

Normal

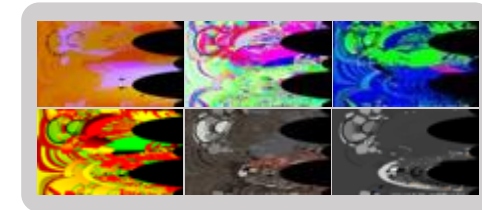


Texture coordinates

Albedo map

Roughness, ambient, and refraction maps

Kernel log-polar transformation



Shading & internal anti-aliasing



Inverse kernel log-polar transformation & post anti-aliasing



LP-buffer

($\sigma = 3.0$)

Screen

Sampling Rate Comparison between Different Rendering Approaches

# Samples	Original Light Field Rendering	KFR
Pass 1	-	$\frac{n^2}{\sigma_0^2}$
Pass 2	-	≈ 0
Total	n^2	$\frac{n^2}{\sigma_0^2}$

- Display resolution is $n \times n$

Content

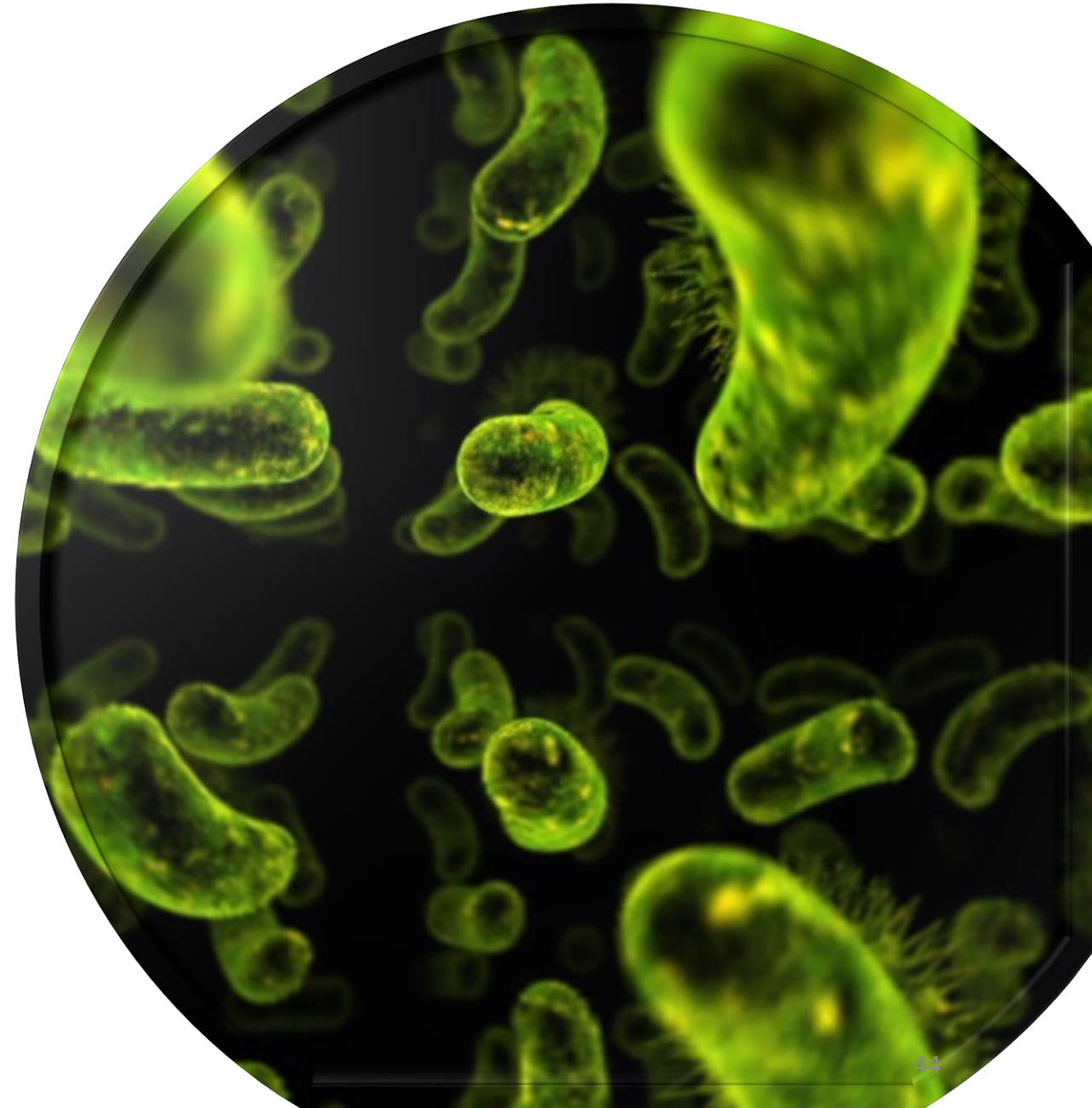
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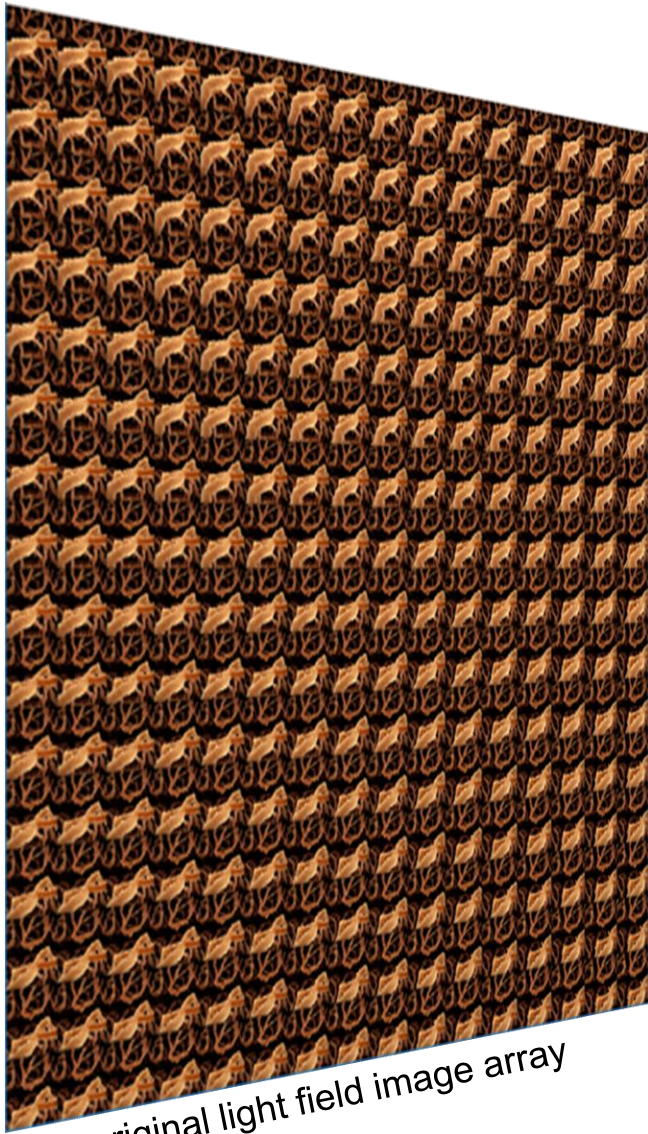
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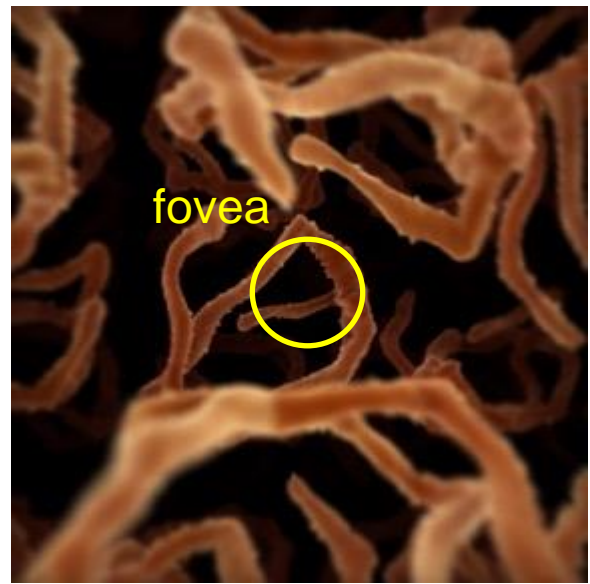


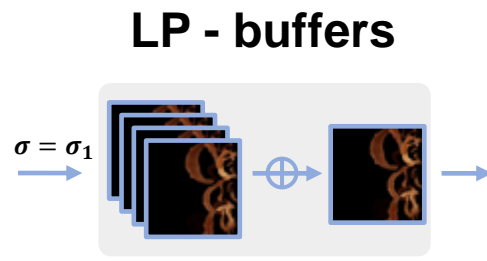
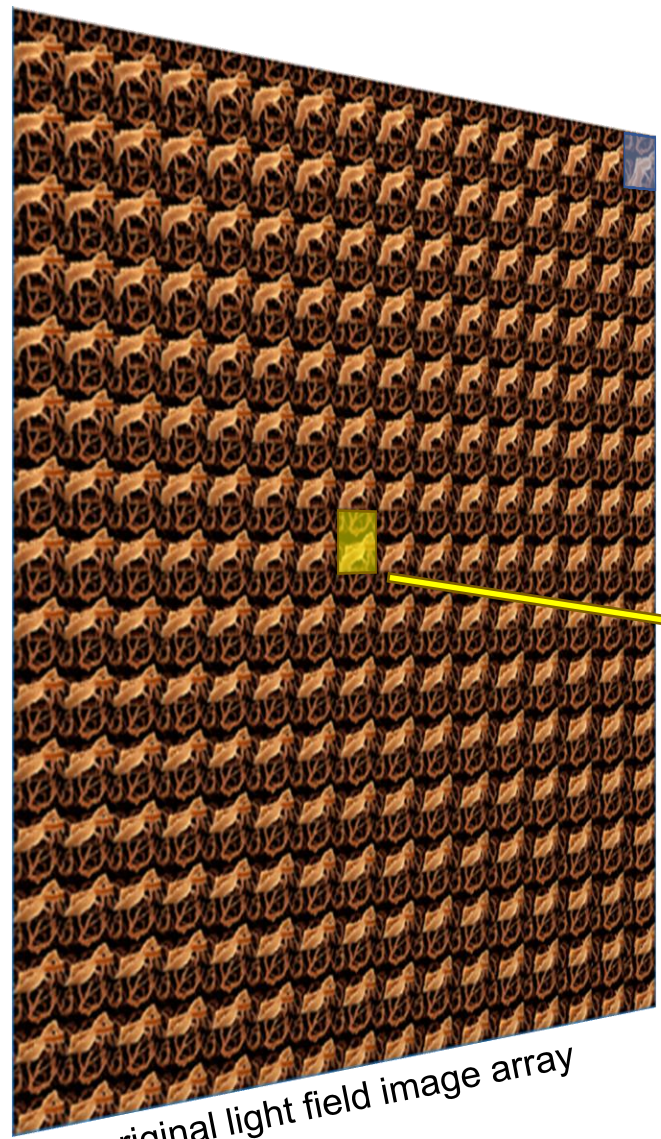
original light field image array

**Better
Than**
foveated rendering



Screen

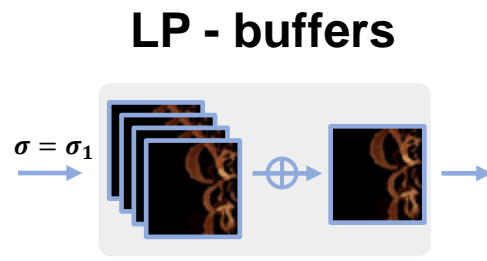
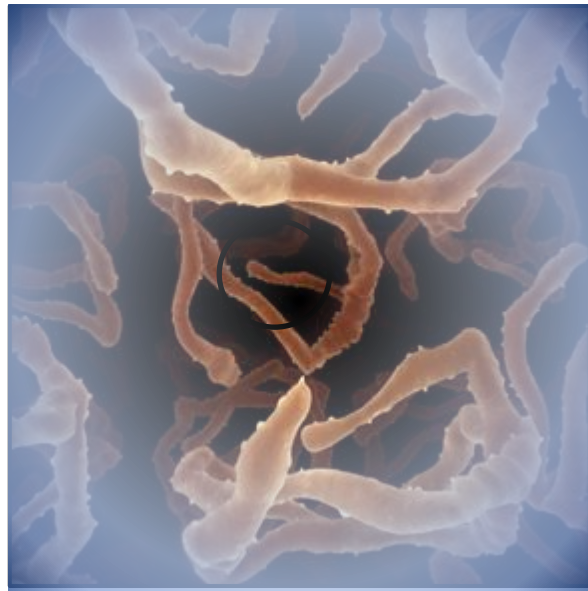
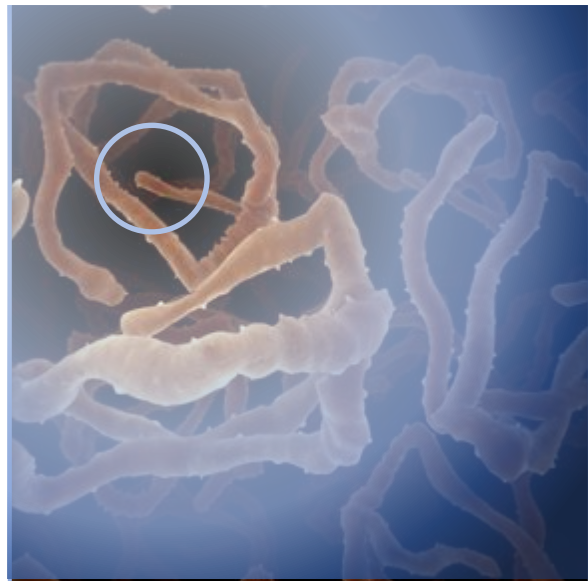
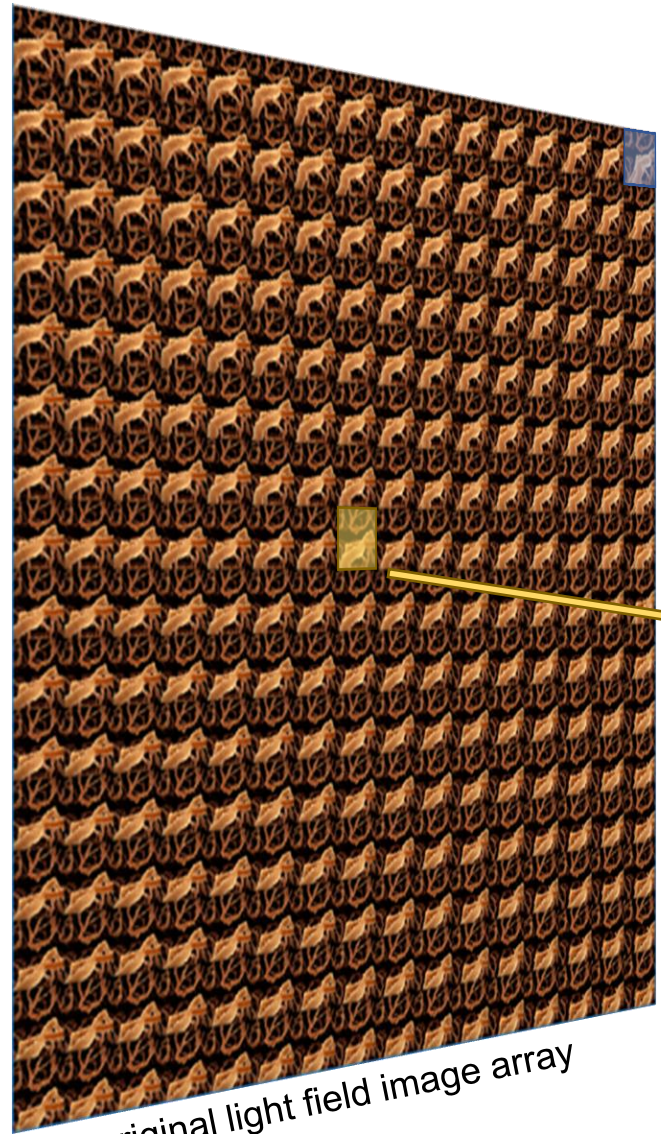




Screen



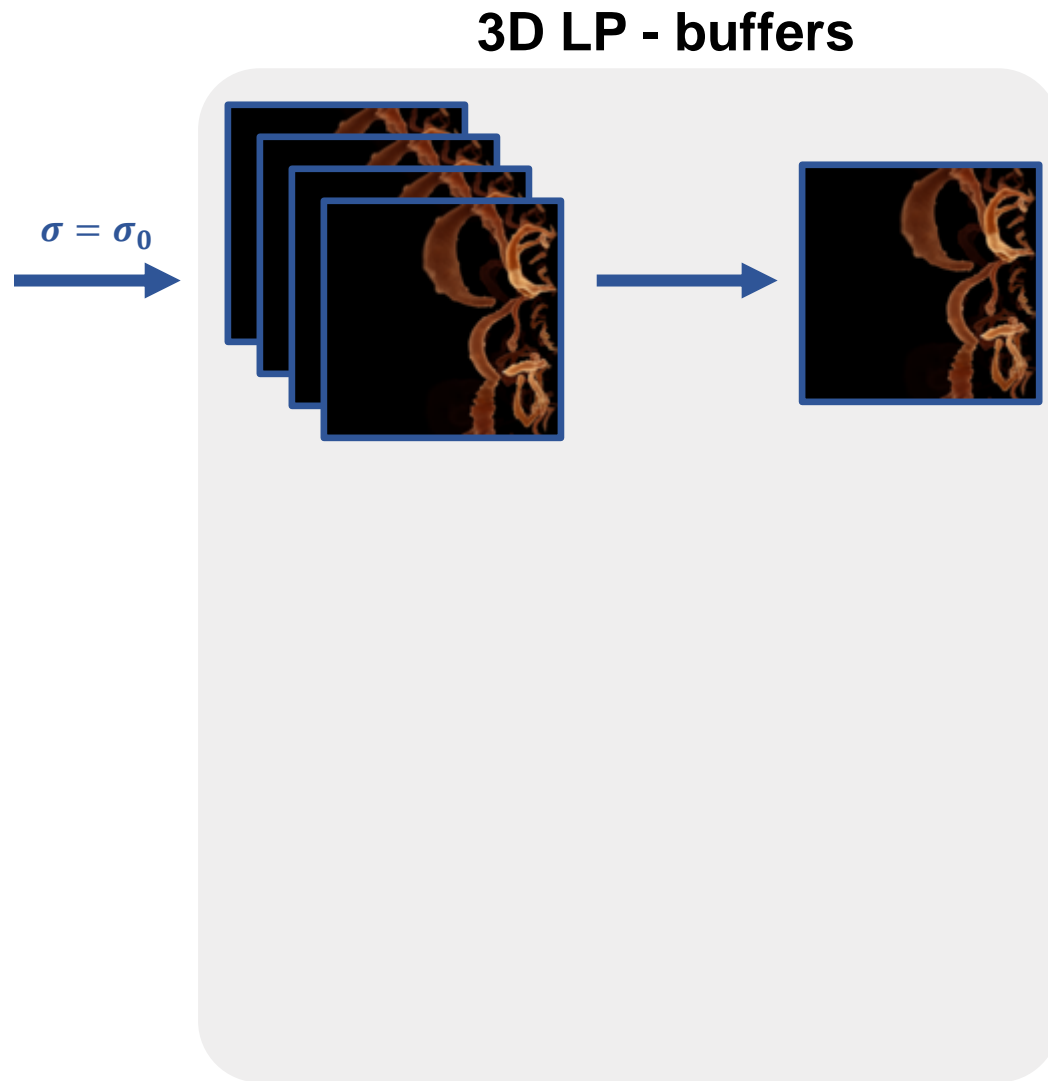
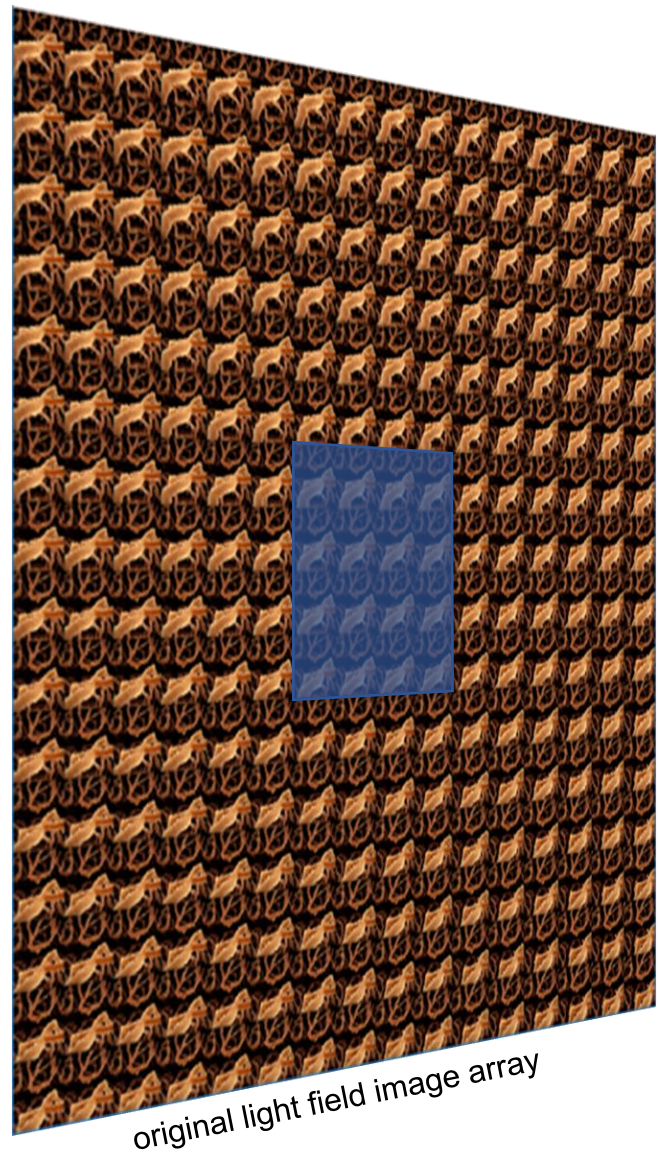
recovered visualization of the light field microscopy



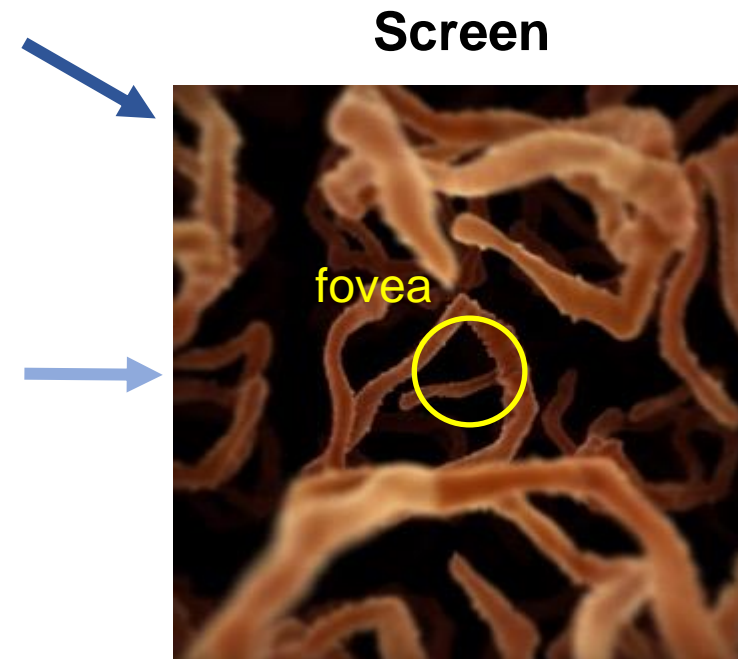
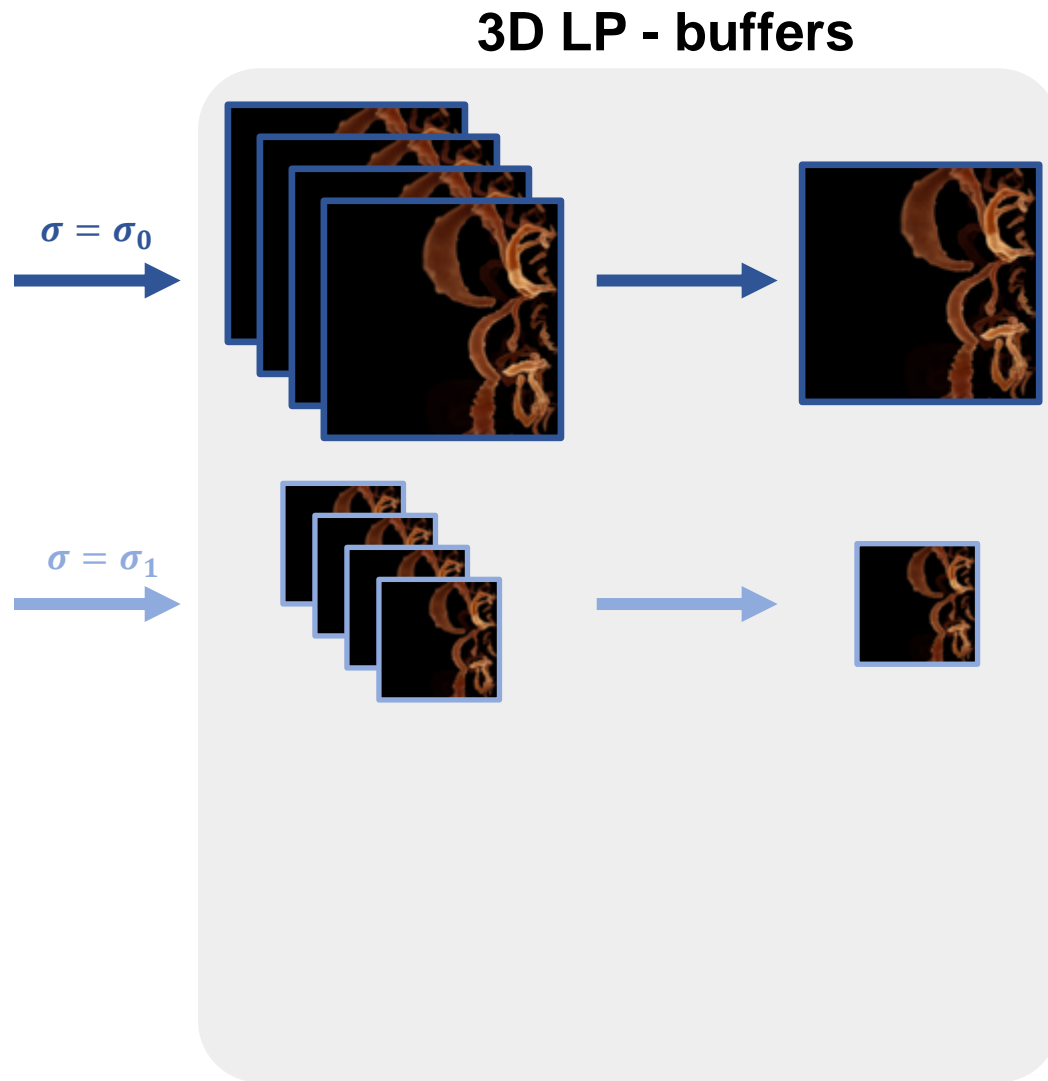
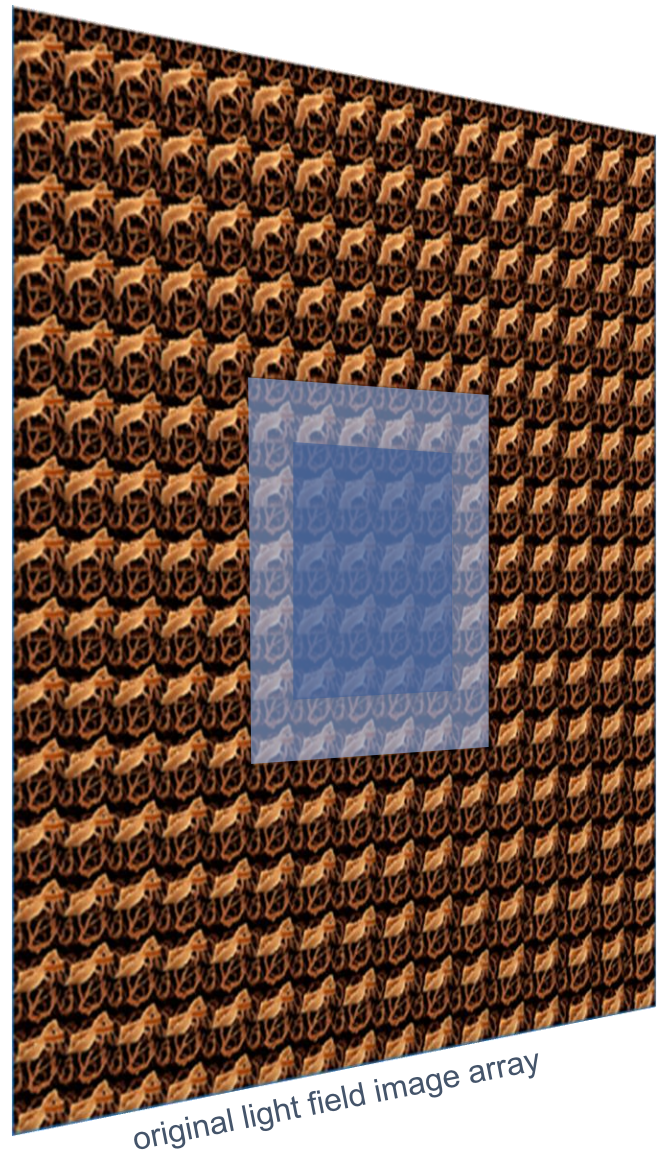
Screen



recovered visualization of the light field microscopy



recovered visualization of the light field microscopy

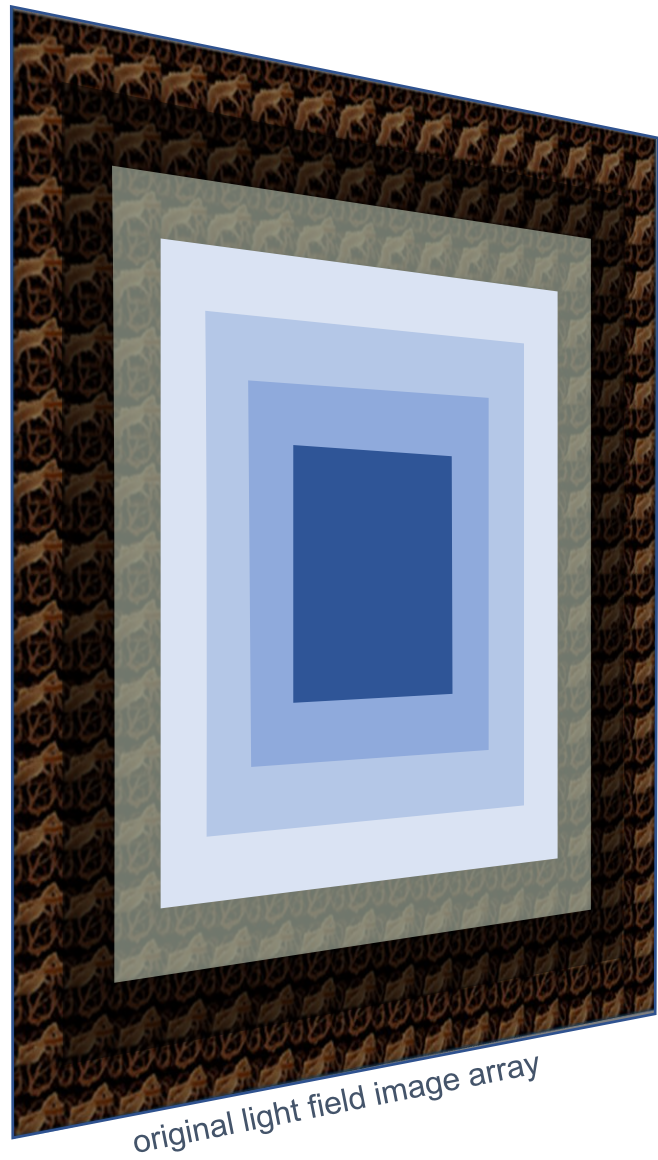


recovered visualization of the light field microscopy

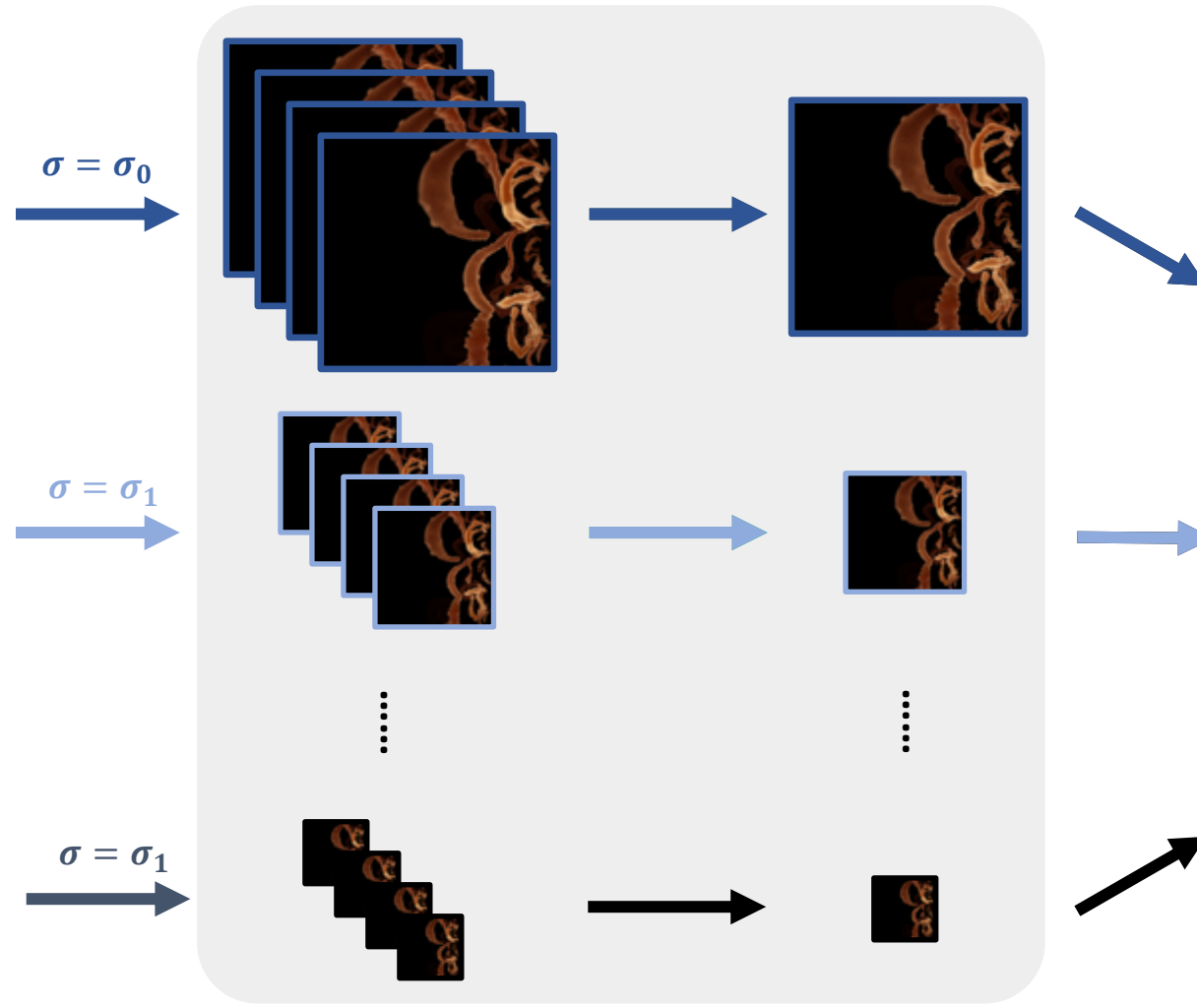
3D kernel log-polar transformation
with different σ for different frames

sum up the frames with the
same σ into one texture

inverse log-polar transformation
and post-anti-aliasing



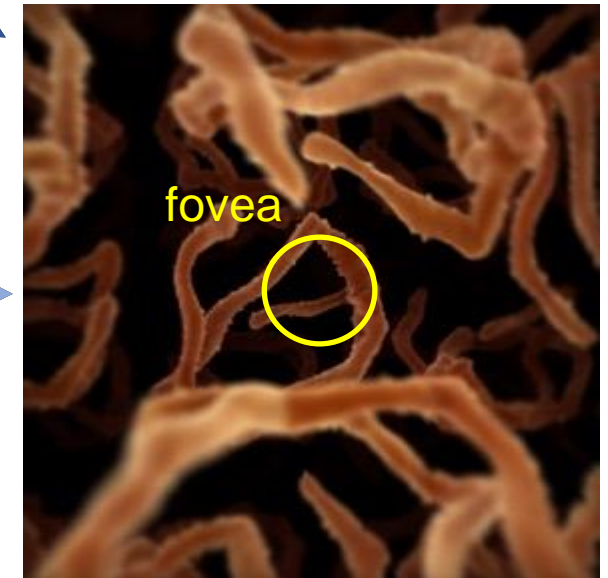
3D LP - buffers



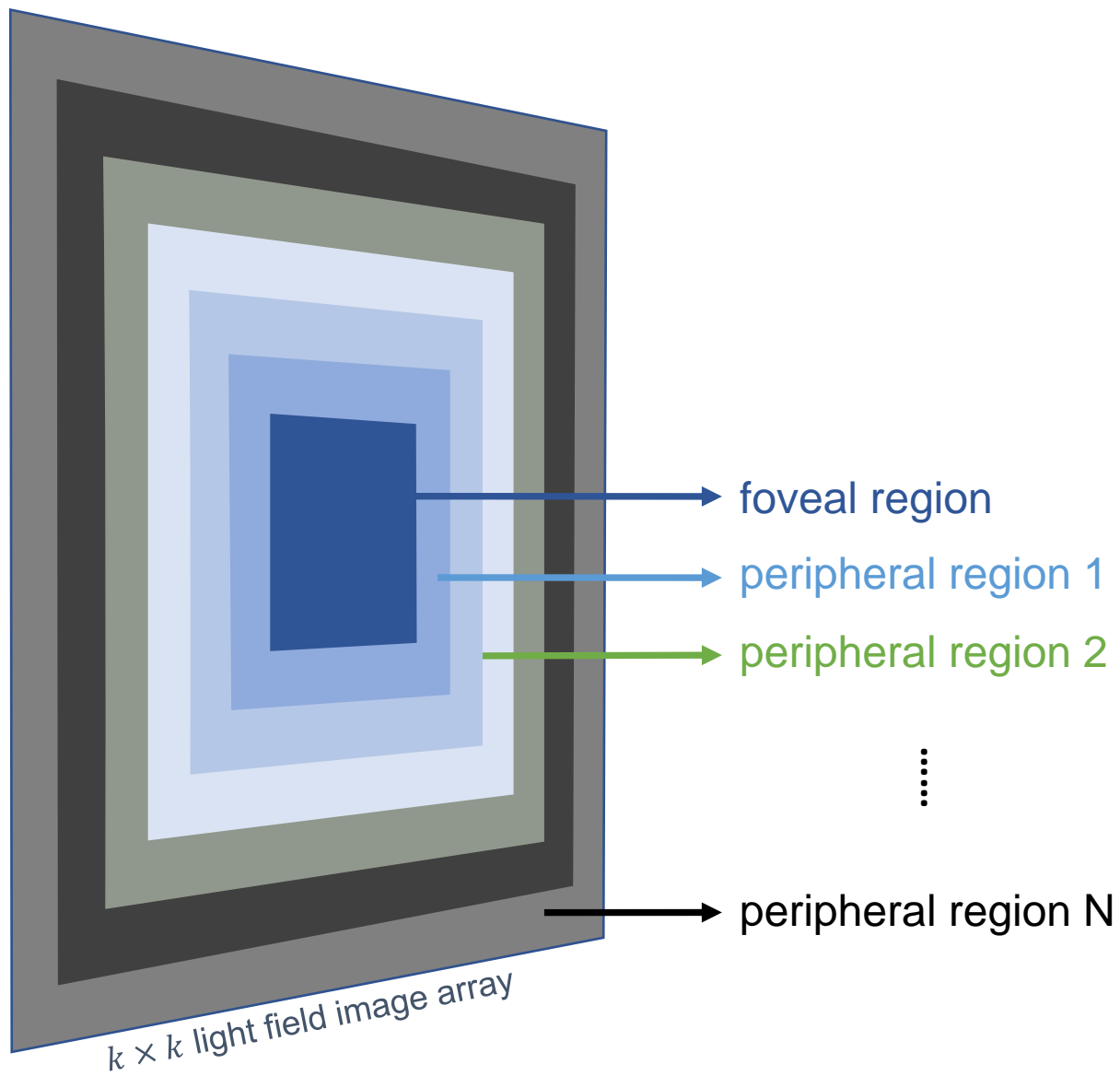
transformed image sub-
arrays in kernel log-polar
coordinates

transformed average image
in kernel log-polar coordinates

Screen



recovered visualization of
the light field microscopy
with speedup of 7.3x compared with
original light field microscopy



$d < r_0$	σ_0	k_0 frames
$r_0 \leq d < r_1$	σ_1	k_1 frames
$r_1 \leq d < r_2$	σ_2	k_2 frames
⋮	⋮	⋮
$r_{N-1} \leq d < r_N$	σ_N	k_N frames

$$k \times k = k_0 + k_1 + k_2 + k_N$$

Sampling Rate Comparison between Different Rendering Approaches

# Samples	Original Light Field Rendering	KFR	3D-KFR
Pass 1	-	$\frac{k^2}{\sigma_0^2} \times n^2$	$\left(\frac{k_0}{\sigma_0^2} + \frac{k_1}{\sigma_1^2} + \dots + \frac{k_N}{\sigma_N^2}\right) \times n^2$
Pass 2	-	n^2	$(1 + N) \times n^2$
Total	$k^2 \times n^2$	$\left(\frac{k^2}{\sigma_0^2} + 1\right) \times n^2 \approx \frac{k^2}{\sigma_0^2} \times n^2$	$\left(\frac{k_0}{\sigma_0^2} + \frac{k_1}{\sigma_1^2} + \dots + \frac{k_N}{\sigma_N^2} + 1 + N\right) \times n^2$

- For a $k \times k$ light field with image resolution of $n \times n$
- $k \times k = k_0 + k_1 + \dots + k_N$
- Display resolution is $n \times n$

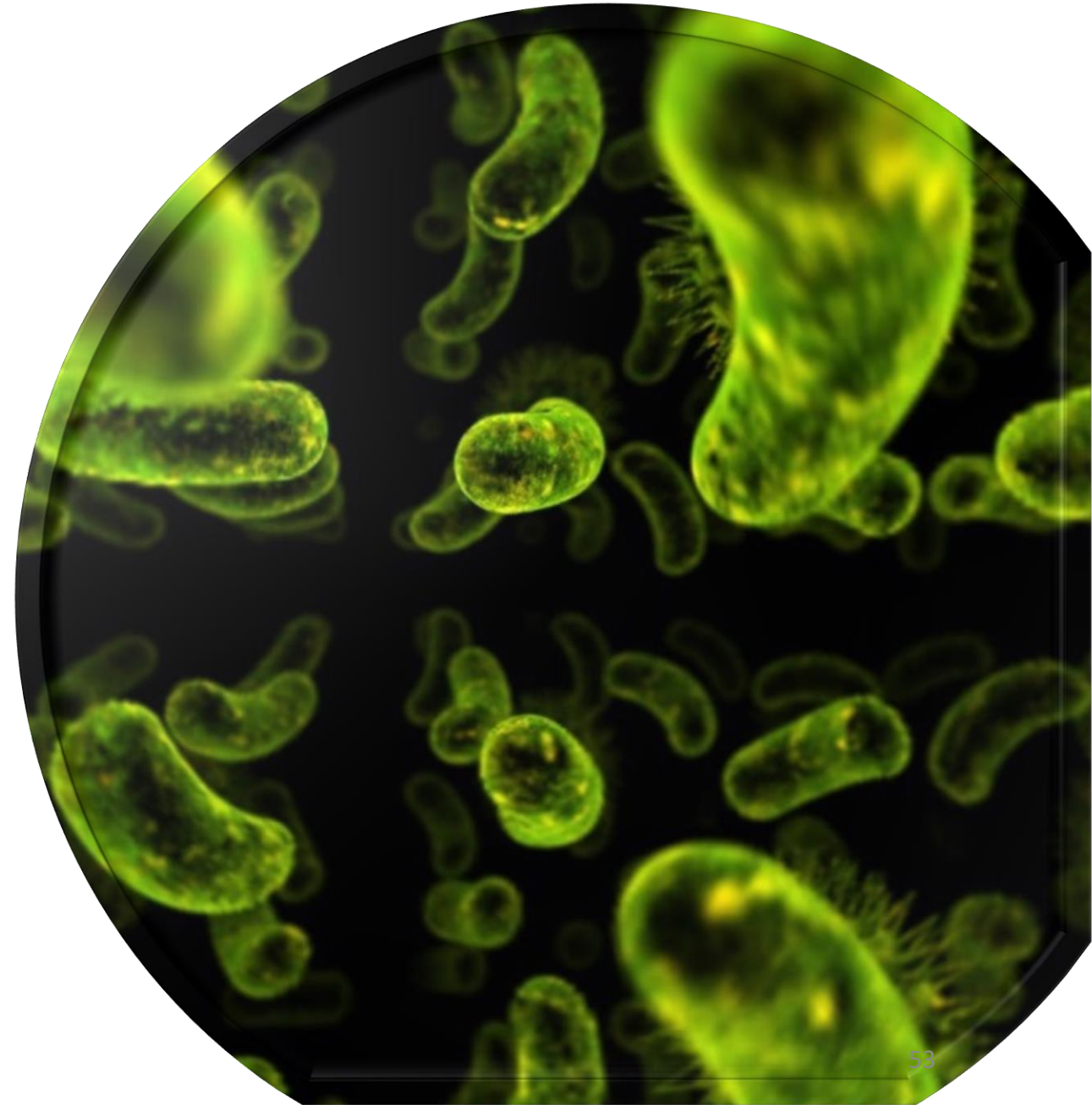
Content

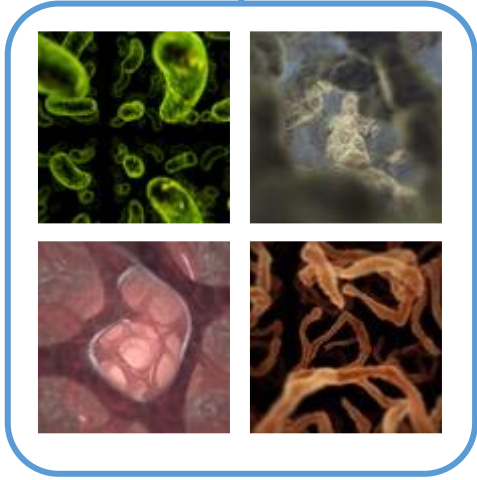
Motivation

Our Approach

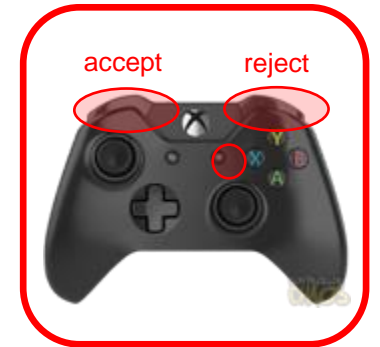
User Study

Rendering Acceleration





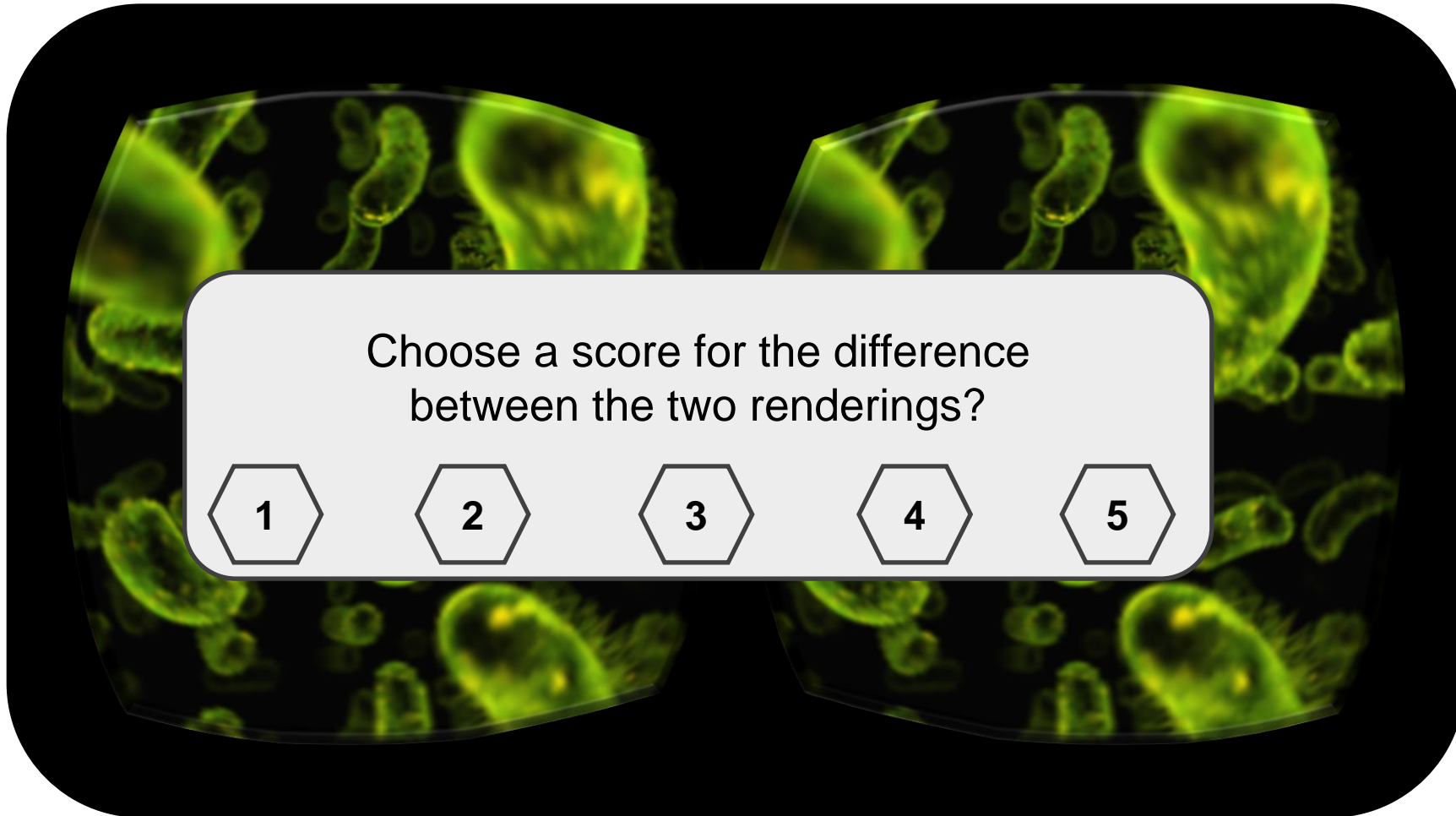
Resolution: 2560×1440
Field of view: up to 100 degrees



$\sigma \in [1.2, 3.6]$

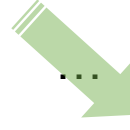
step size: 0.2

Pair Test



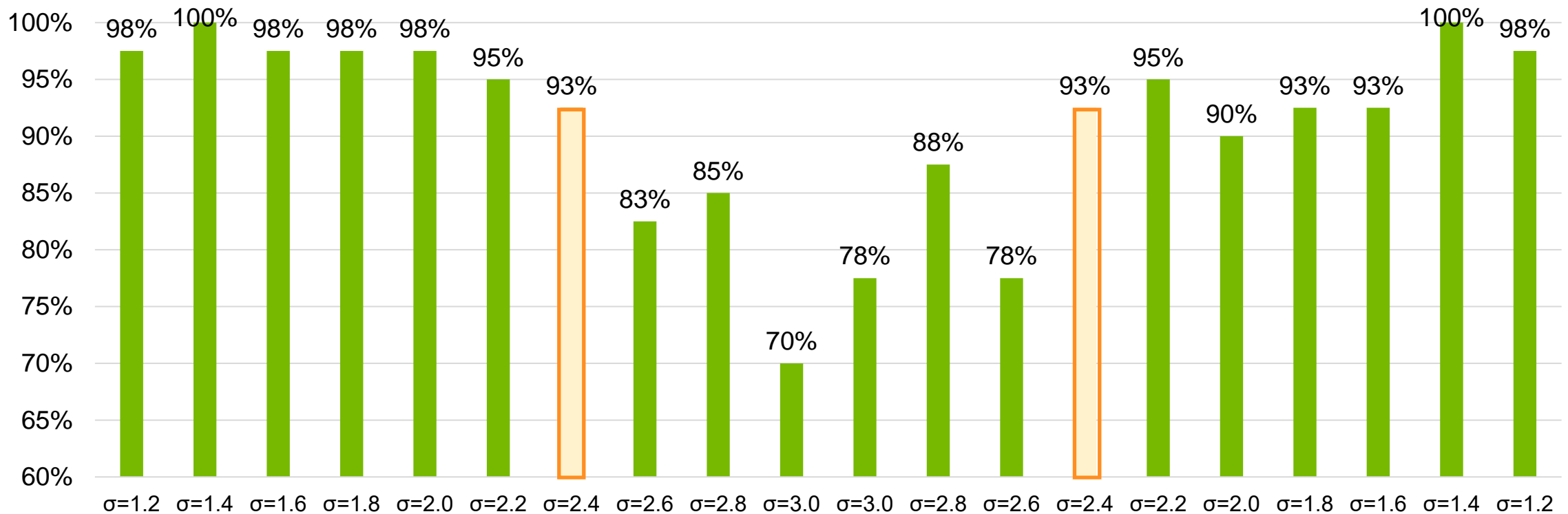
- 1 Ground Truth
- 2 Foveated Rendering
- 3 Evaluation

σ 1.2 1.4 ... 2.8 **3.0** 2.8 ... 1.4 1.2

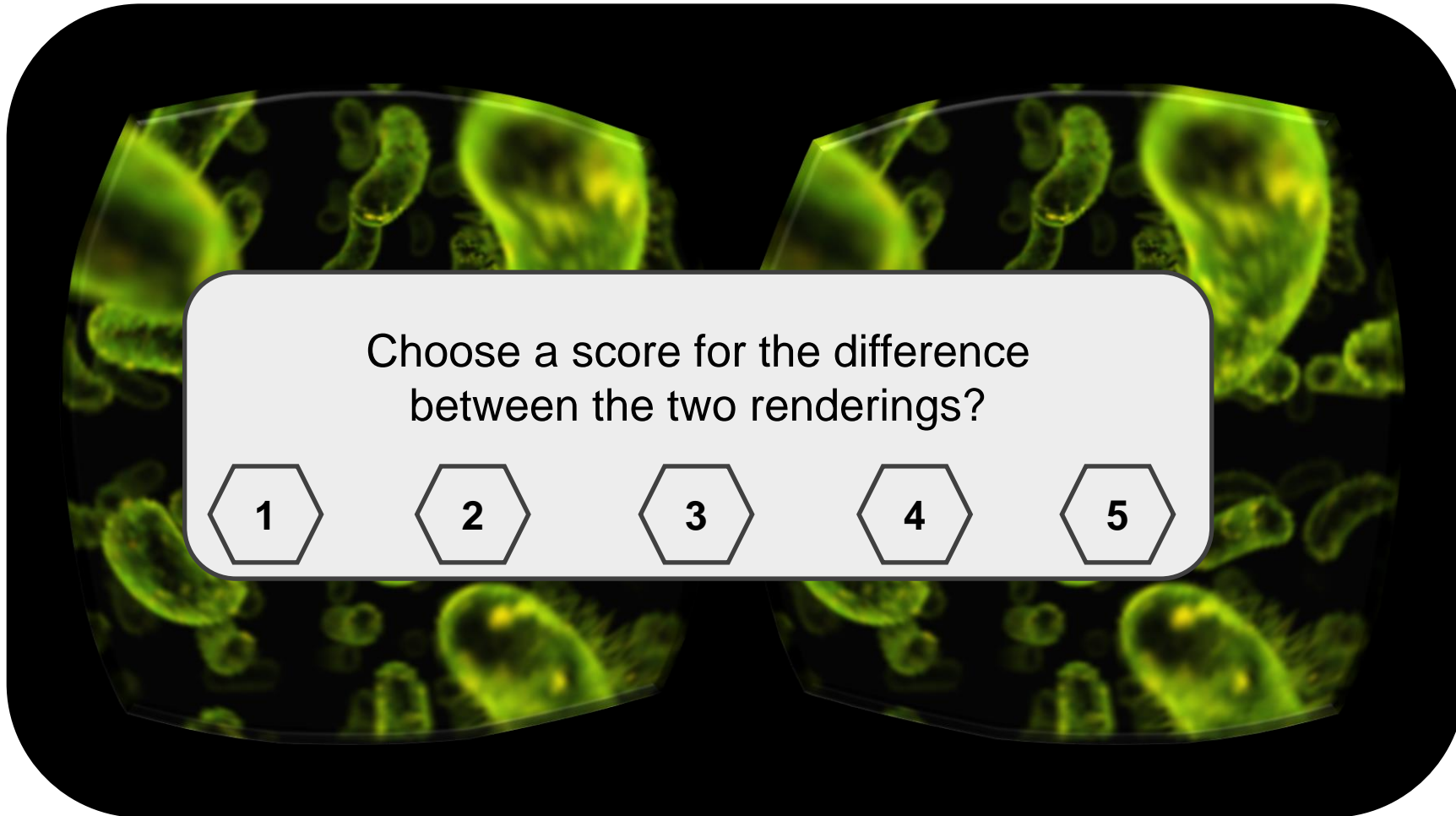


Result – Pair Test

Are the **regular rendering** and the **foveated rendering** identical?



Random Test



- 1 Ground Truth
- 2 Foveated Rendering
- 3 Evaluation

Shuffled σ

2.6

1.4

...

2.0

3.0

1.8

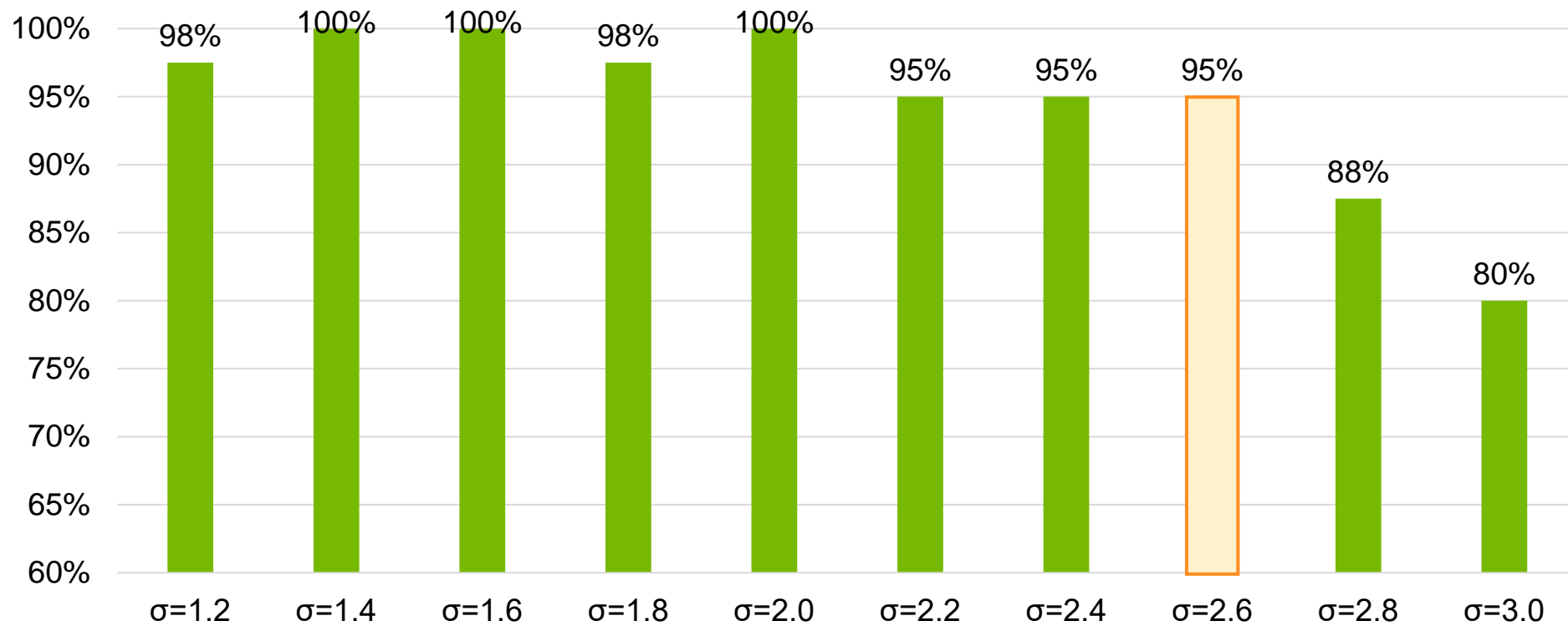
...

2.2

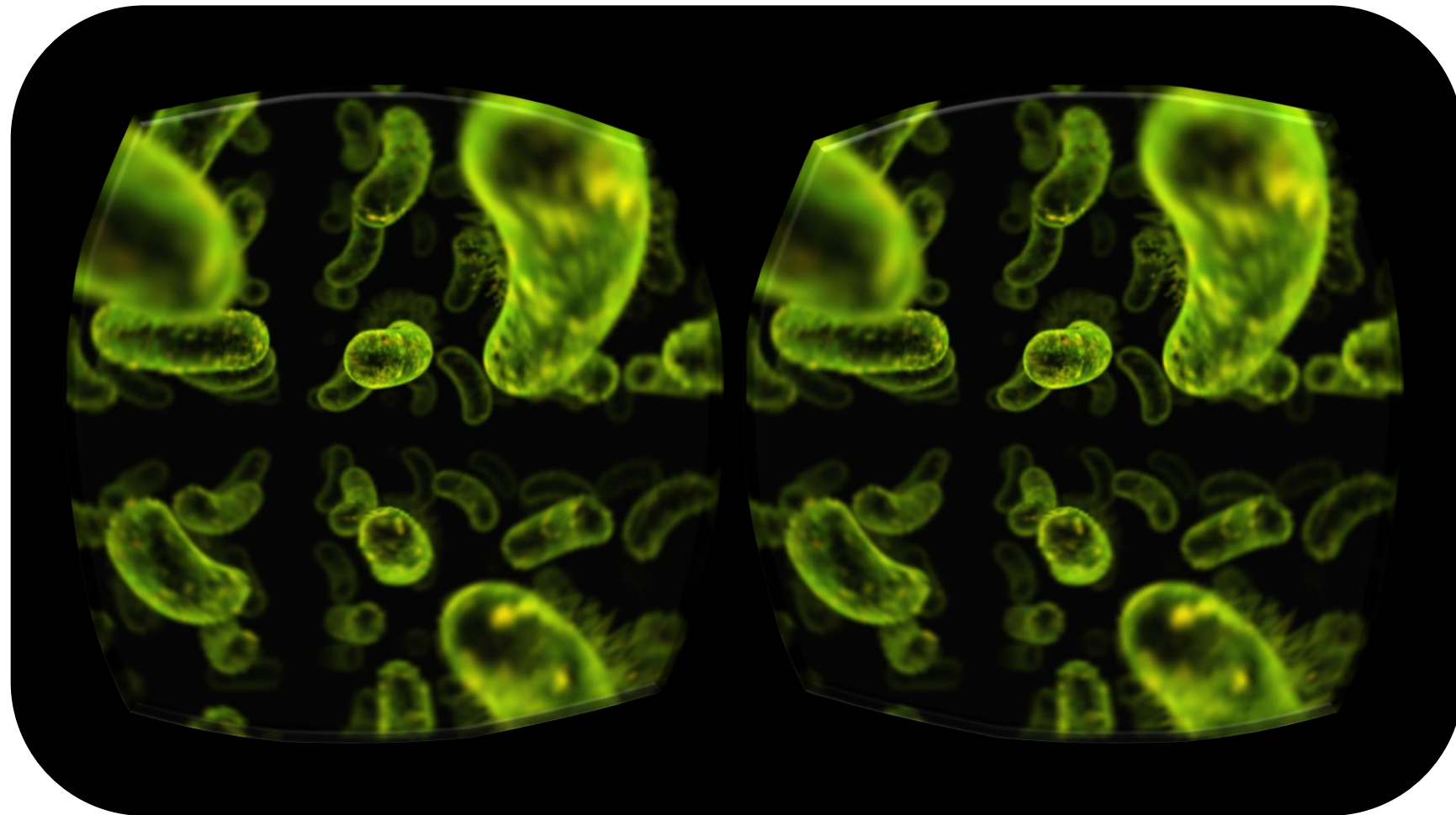
1.6

Result – Random Test

Are the **regular rendering** and the **foveated rendering** identical?



Slider Test

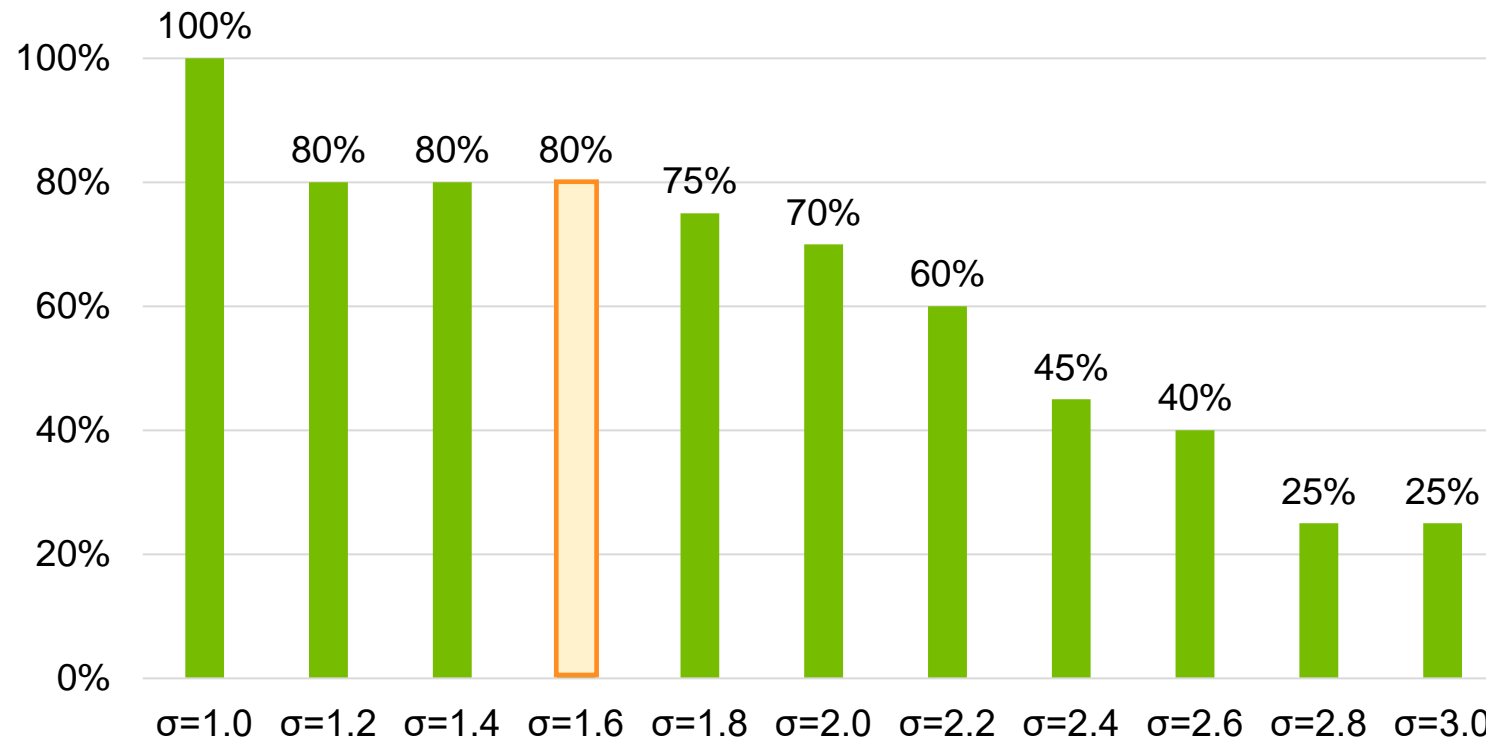


- 1 Ground Truth
- 2 Foveated Rendering



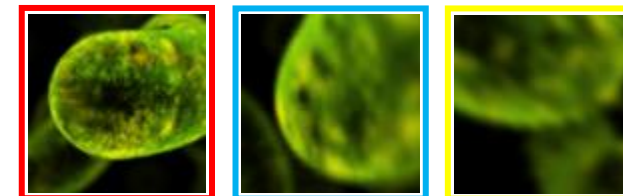
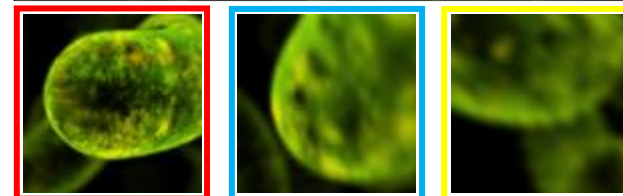
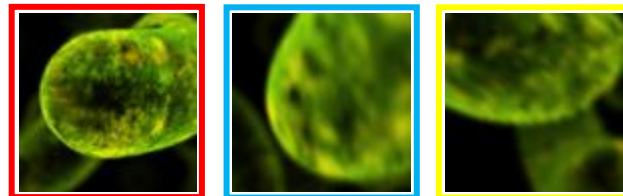
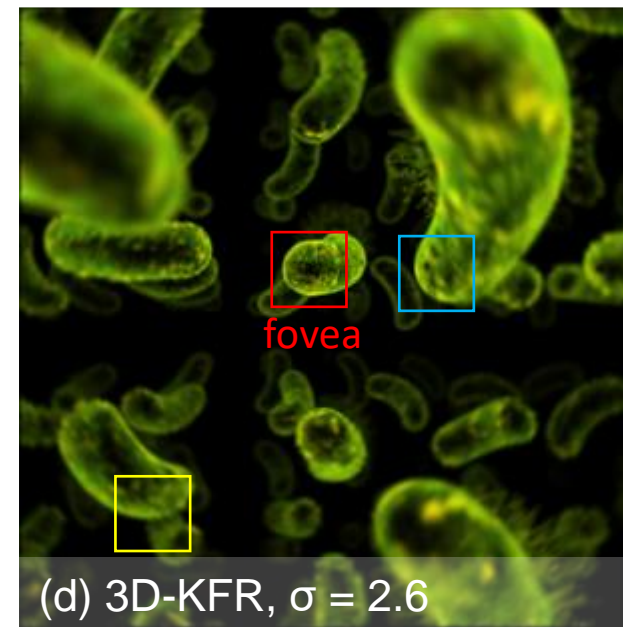
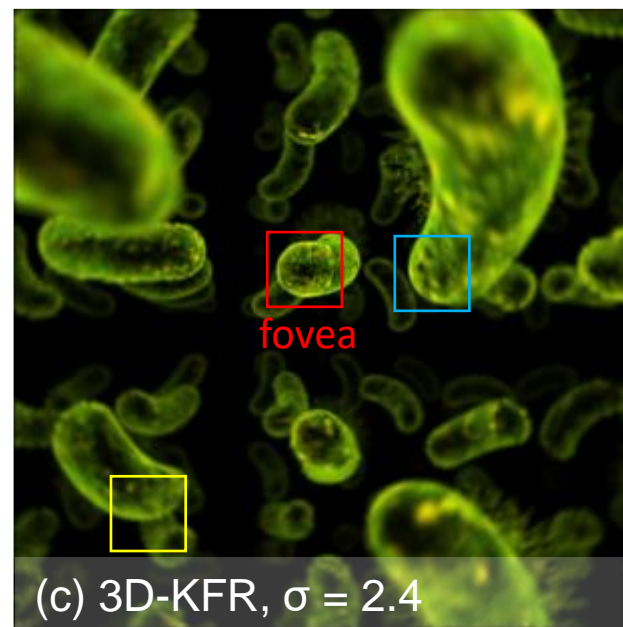
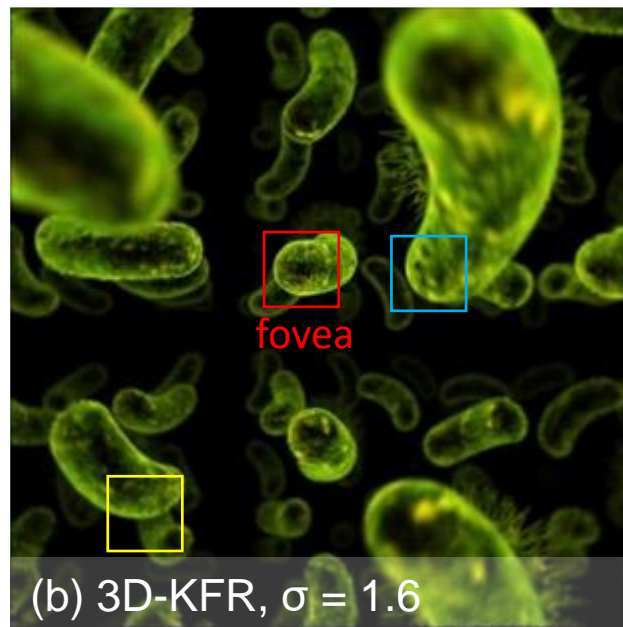
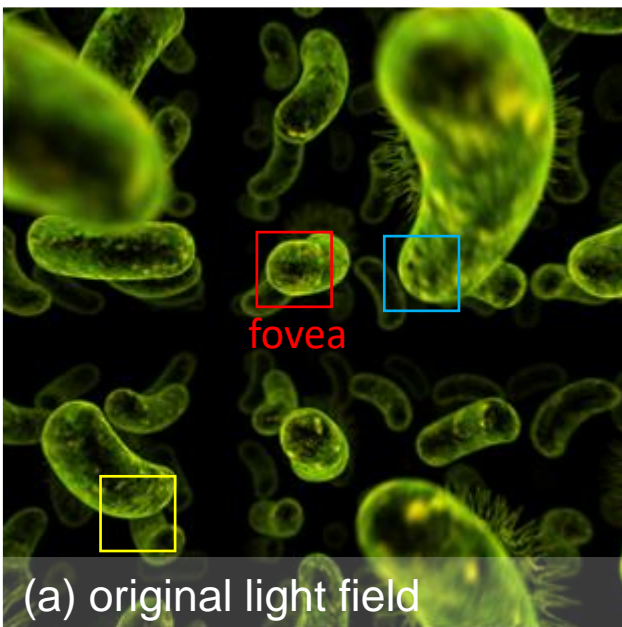
Result – Slider Test

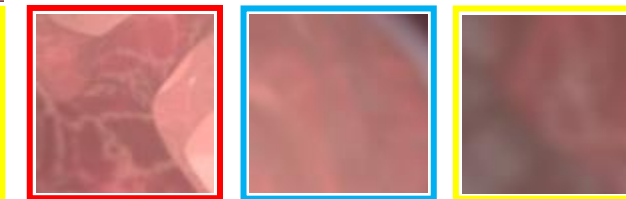
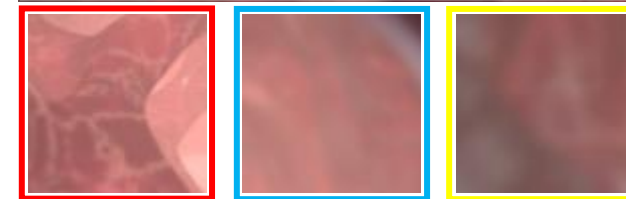
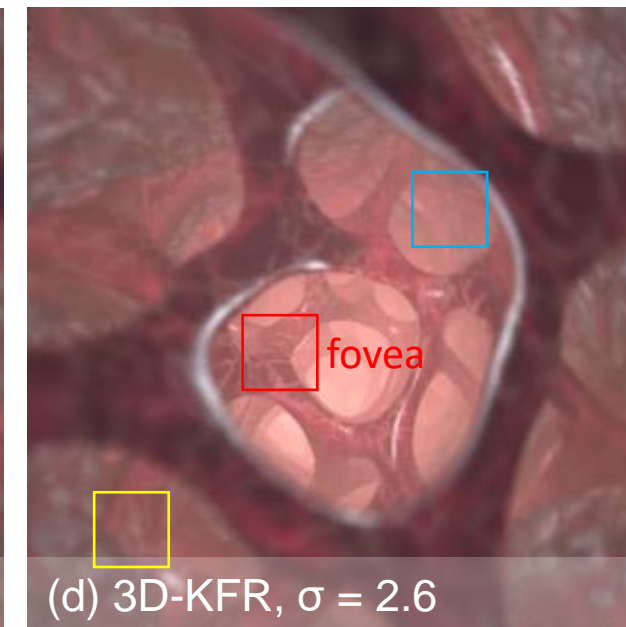
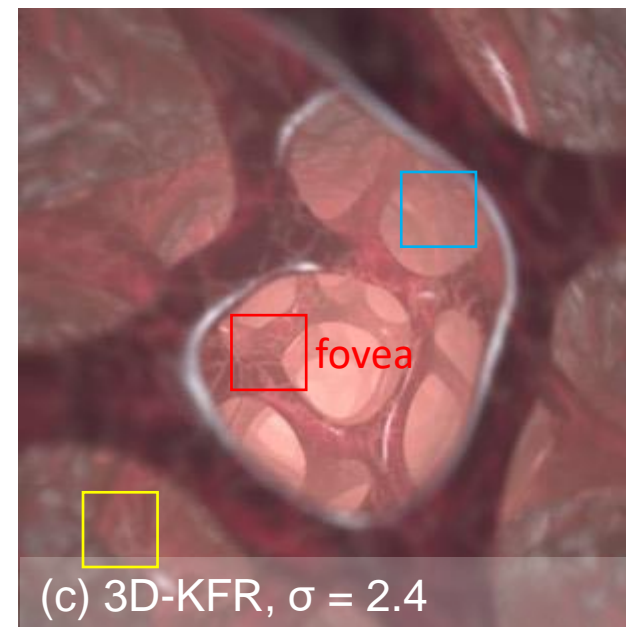
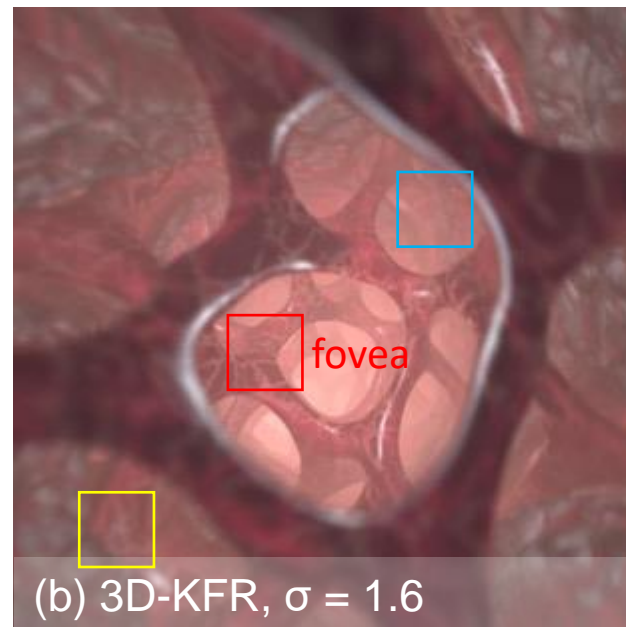
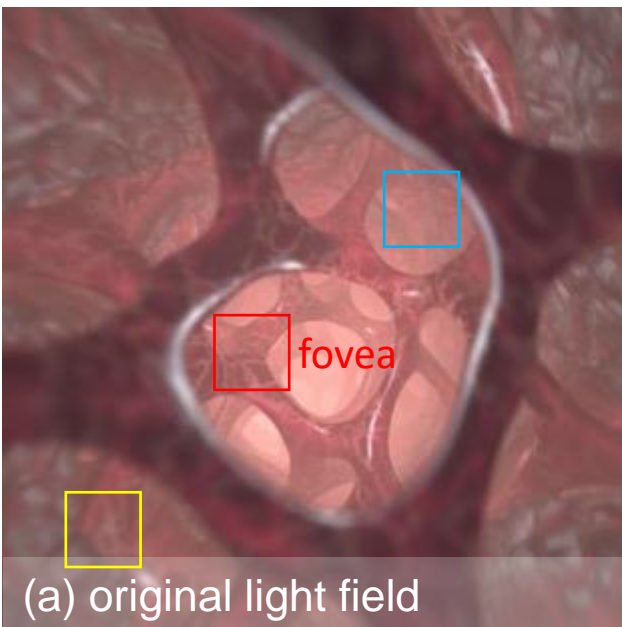
Are the **regular rendering** and the **foveated rendering** identical?

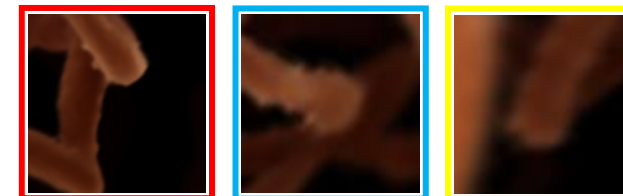
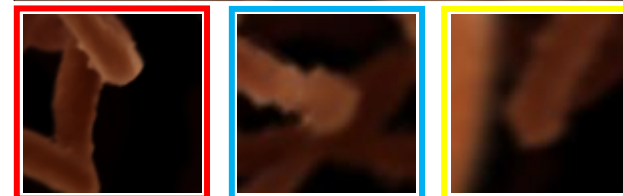
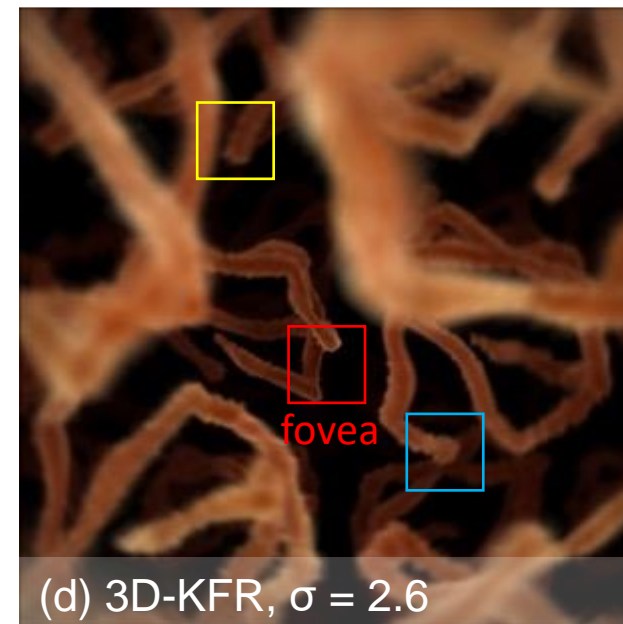
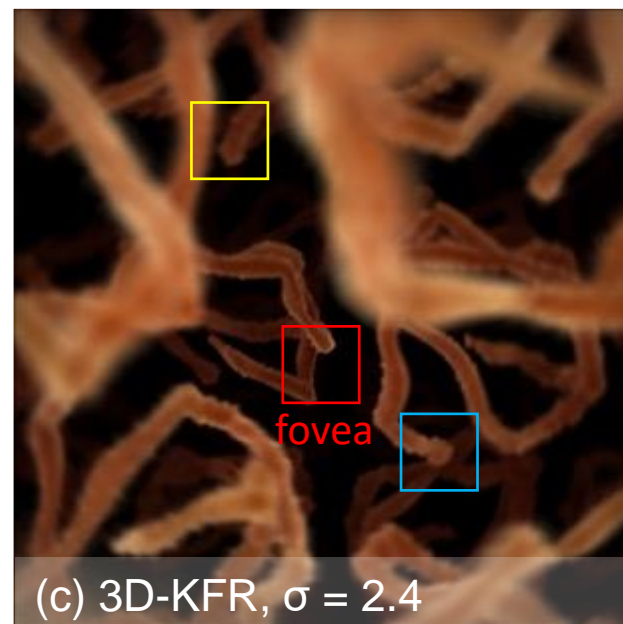
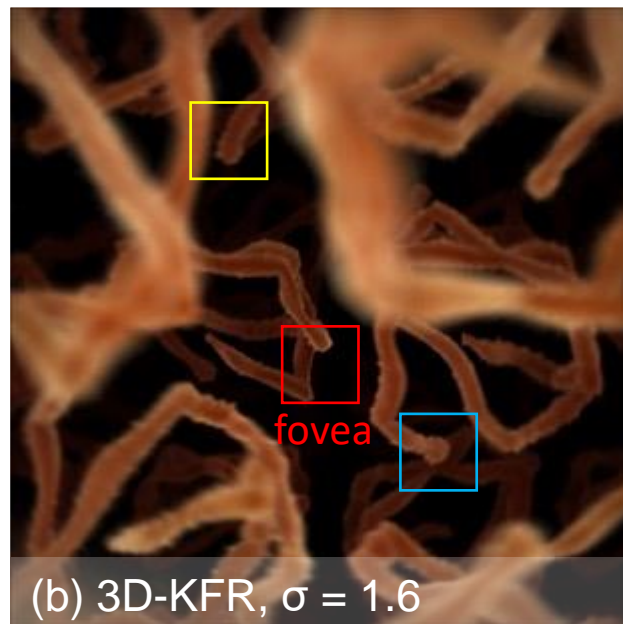
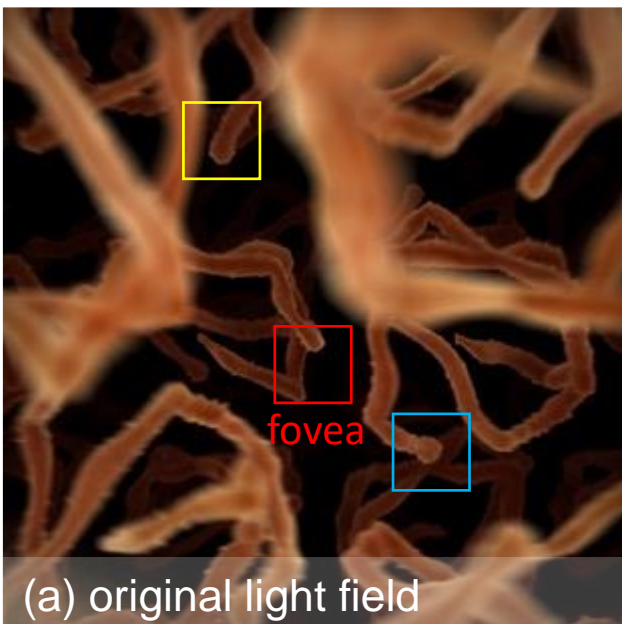


Rendering Acceleration

Resolution	Rendering Time of Ground Truth	$\sigma = 1.6$		$\sigma = 2.4$		$\sigma = 2.6$	
		Rendering Time of 3D KFR	Speedup	Rendering Time of 3D KFR	Speedup	Rendering Time of 3D KFR	Speedup
$20 \times 20 \times 1024 \times 1024$	66.83 <i>ms</i>	19.27 <i>ms</i>	3.47 ×	10.22 <i>ms</i>	6.54 ×	9.39 <i>ms</i>	7.11 ×
$21 \times 21 \times 1024 \times 1024$	74.17 <i>ms</i>	22.39 <i>ms</i>	3.31 ×	11.90 <i>ms</i>	6.24 ×	10.39 <i>ms</i>	7.14 ×
$22 \times 22 \times 1024 \times 1024$	92.33 <i>ms</i>	28.26 <i>ms</i>	3.27 ×	14.65 <i>ms</i>	6.30 ×	12.64 <i>ms</i>	7.30 ×
$23 \times 23 \times 1024 \times 1024$	100.26 <i>ms</i>	30.64 <i>ms</i>	3.27 ×	16.30 <i>ms</i>	6.15 ×	13.95 <i>ms</i>	7.18 ×
$24 \times 24 \times 1024 \times 1024$	122.29 <i>ms</i>	35.92 <i>ms</i>	3.40 ×	19.09 <i>ms</i>	6.41 ×	16.79 <i>ms</i>	7.28 ×
$25 \times 25 \times 1024 \times 1024$	138.93 <i>ms</i>	41.42 <i>ms</i>	3.35 ×	21.96 <i>ms</i>	6.33 ×	19.09 <i>ms</i>	7.28 ×

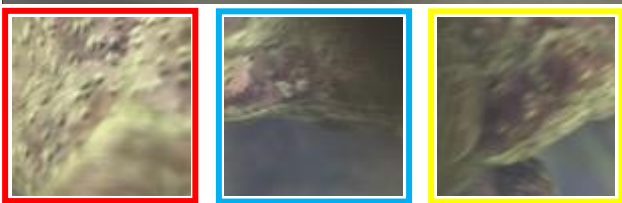




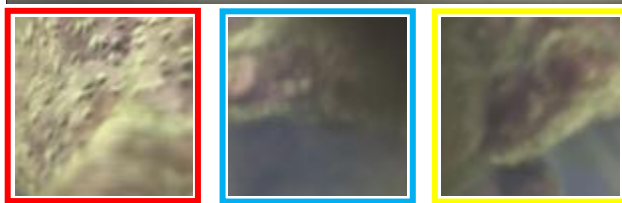




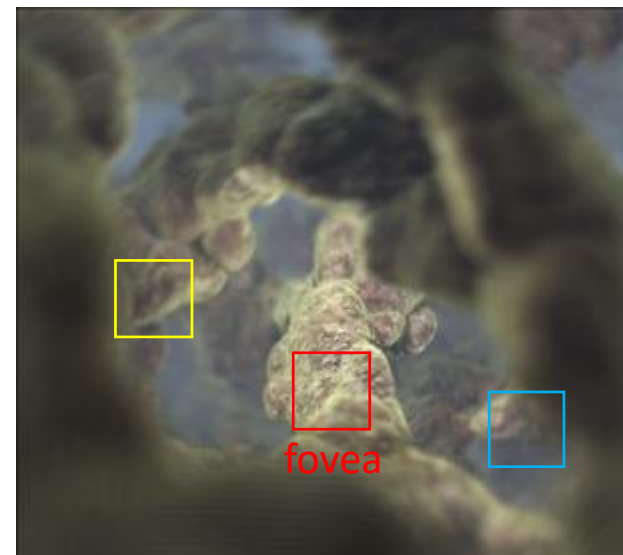
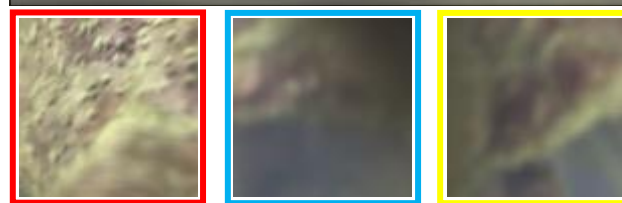
(a) original light field



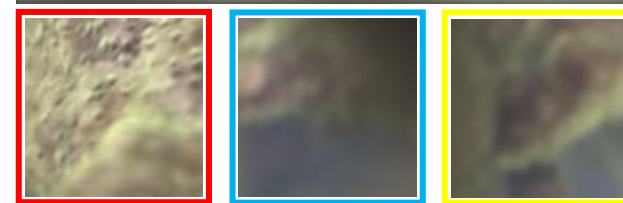
(b) 3D-KFR, $\sigma = 1.6$



(c) 3D-KFR, $\sigma = 2.4$

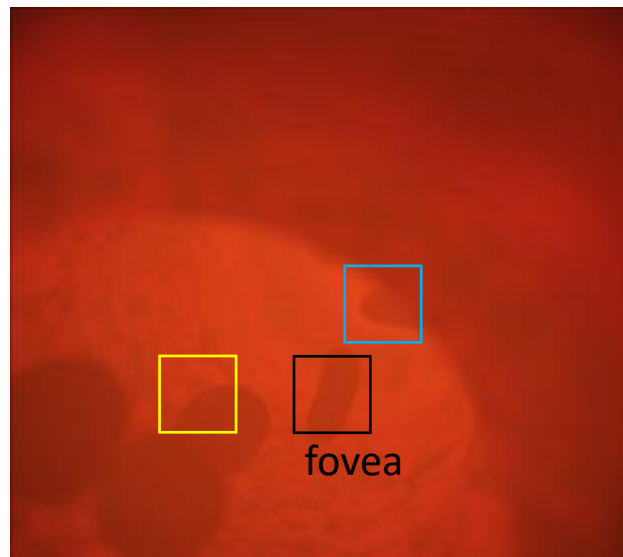


(d) 3D-KFR, $\sigma = 2.6$

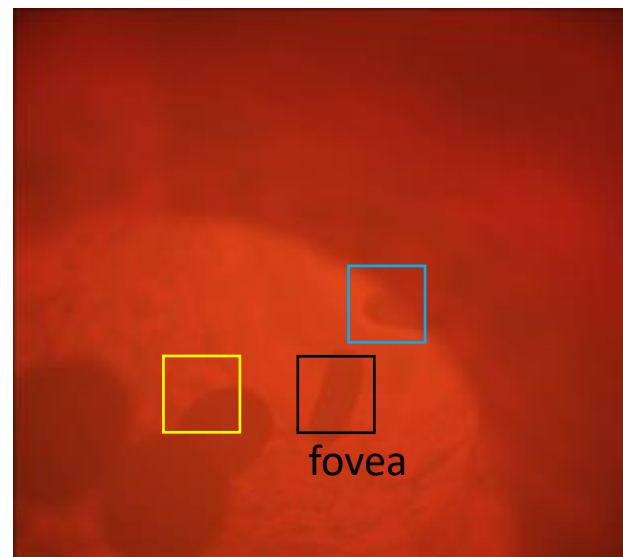




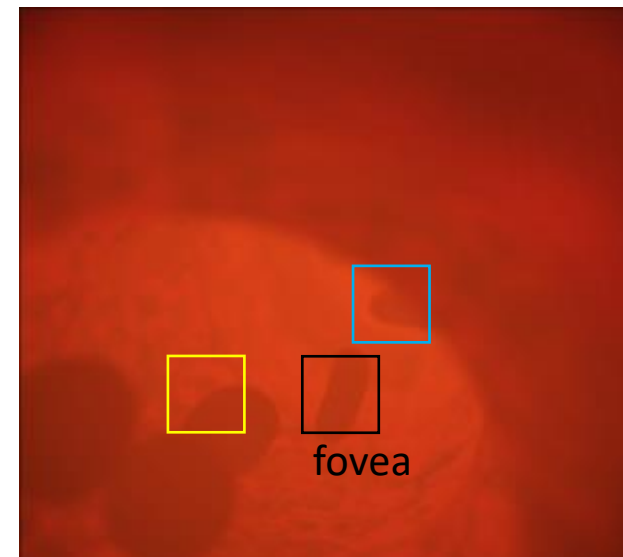
(a) original light field



(b) 3D-KFR, $\sigma = 1.6$

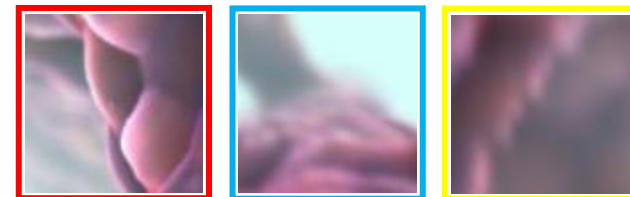
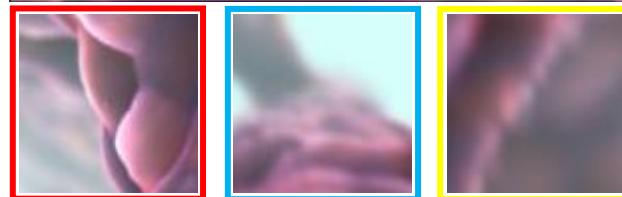
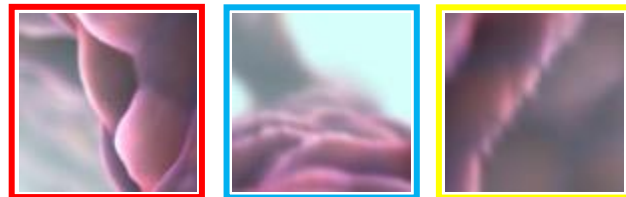
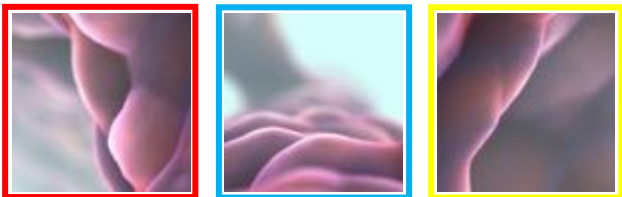
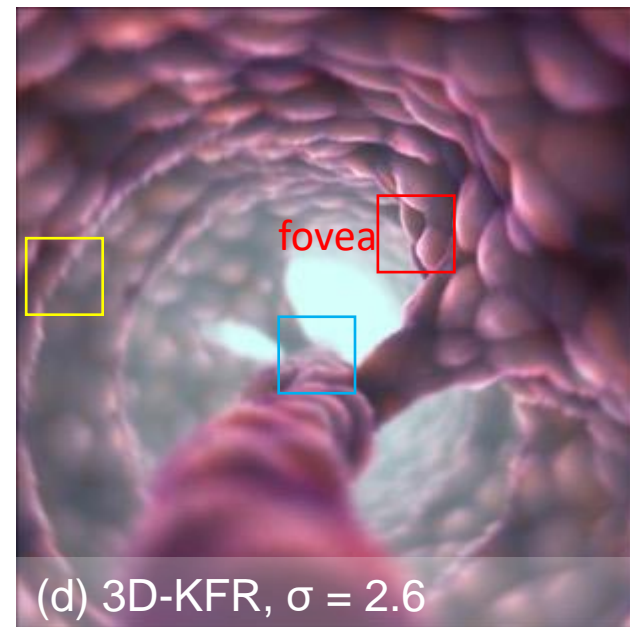
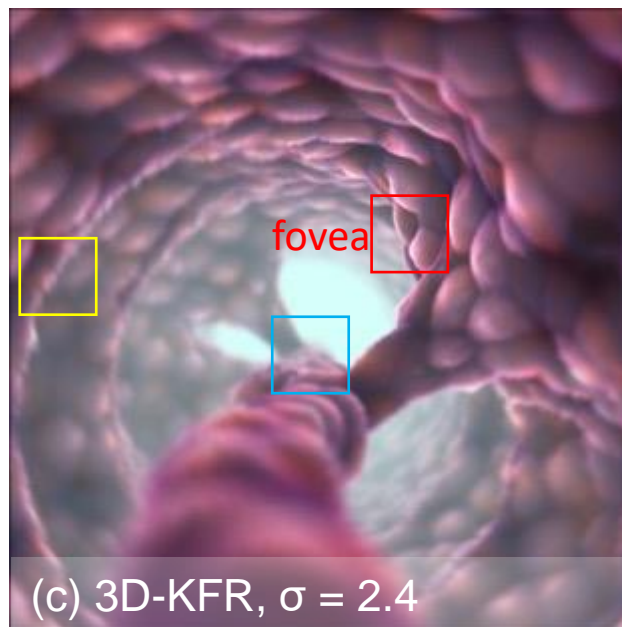
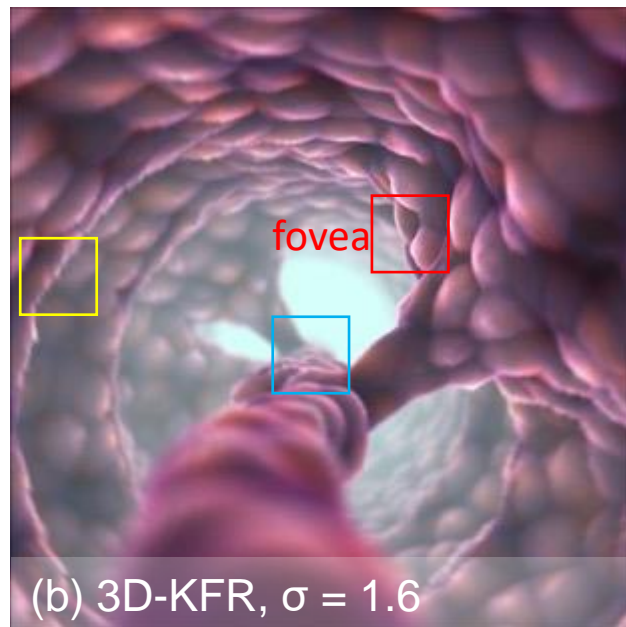
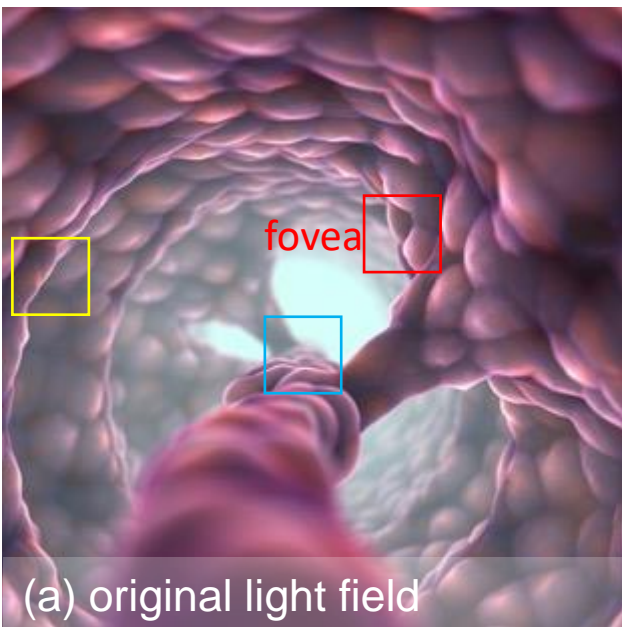


(c) 3D-KFR, $\sigma = 2.4$



(d) 3D-KFR, $\sigma = 2.6$





Summary

- 3D-Kernel log-polar transformation for light fields
 - 3.3X - 7.3X speedup
- User study
 - Determine parameters to maximize perceptual realism and minimize computation
- Light field dataset
 - Open Source: https://foveation.umiacs.umd.edu/3D_KFR