Linear Hull Attack on Round-Reduced Simeck with Dynamic Key-guessing Techniques

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Abstract. Simeck is a new family of lightweight block cipher proposed by Yang *et al.* in CHES'15, which performs efficiently in hardware implementation. In this paper, we search out Simeck's differentials with low Hamming weight and high probability using Kölbl's tool, then exploit the links between differentials and linear characteristics to construct linear hulls for Simeck. We give improved linear hull attack with dynamic key-guessing techniques on Simeck on the basis of round function's property. Our results cover Simeck 32/64 reduced to 23 rounds, Simeck 48/96 reduced to 30 rounds, Simeck 64/128 reduced to 37 rounds, which are the best known results so far for any variant of Simeck.

Keywords: Simeck, Linear Cryptanalysis, Differential Cryptanalysis, Linear Hull, Dynamic Key-guessing

1 Introduction

Simeck [19] is a new family of lightweight block cipher proposed in CHES'15 by Yang, Zhu, Suder, Aagaard and Gongbased. They combined the Simon and Speck block ciphers designed by NSA in [8], using a different set of rotation constants of Simon's round function and the key schedule of Speck. The round function of Simeck only contains the AND operation, left rotation and the XOR operation, leading to a more compact and efficient implementation in hardware. The Simeck family has three variants with different block size and key size, including Simeck32/64, Simeck48/96, Simeck64/128.

Related Works. Many cryptanalysis techniques of Simon can be used to attack Simeck due to their similarity, including differential [3, 5, 9], linear [2, 4] cryptanalysis and so on. For Simon, wang *et al.* [18] improved the differential

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attack results by dynamic key-guessing techniques. Then basing on the dynamic key-guessing techniques in the linear hull cryptanalysis, Chen $et\ al.\ [10]$ applied the Guess, Split and Combine technique to reduce the time complexity in the calculation of the empirical correlations. They can attack one or two more rounds for all versions of Simon than Wang $et\ al.$'s results.

For Simeck, there are only a few cryptanalysis results so far. Kölbl et al. [12] compared Simon and Simeck on the lower bound of differential and linear characteristic and presented some differentials to attack 19/26/33 rounds of Simeck32/48/64. Bagheri et al. [7] analyzed Simeck's security against linear cryptanalysis. With Matsui's algorithm 2, they can attack 18/23/27 rounds for Simeck32/48/64. Zhang et al. evaluated the security of 20/24/27 rounds of Simeck32/48/64 against zero correlation linear cryptanalysis [20]. Qiao et al. [15] used differential cryptanalysis with dynamic key-guessing techniques to attack Simeck and improved the previously best results on all versions by 2 rounds.

cipher	round	Data Complexity	Time Complexity	Reference
	18	2^{31}	$2^{63.5}$	[7]
C: 1.90/C4	19	2^{31}	2^{36}	[12]
Simeck32/64	20	2^{32}	$2^{56.65}$	[20]
	22	2^{32}	$2^{57.9}$	[15]
	23	$2^{31.91}$	$2^{61.78}A^{a} + 2^{56.41}E^{b}$	section 4.1
	24	2^{45}	2^{94}	[7]
C:1- 40 /0C	24	2^{48}	$2^{91.6}$	[20]
Simeck48/96	26	2^{47}	2^{62}	[12]
	28	2^{46}	$2^{68.3}$	[15]
	30	$2^{47.66}$	$2^{92.2}A + 2^{88.04}E$	section 4.2
	27	2^{61}	$2^{120.5}$	[7]
Simeck64/128	27	2^{64}	$2^{112.79}$	[20]
	33	2^{63}	2^{96}	[12]
	35	2^{63}	$2^{116.3}$	[15]
	37	$2^{63.09}$	$2^{111.44}A + 2^{121.25}E$	section 4.3

Table 1. Summary of cryptanalysis results on Simeck

Our contributions. This paper analyzes the security of Simeck against improved linear hull cryptanalysis with dynamic key-guessing techniques. At first using Kölbl's tool, we search out better differentials than the previous results. The probability of Simeck32/64 is more accurate with searching more differential characteristics. For Simeck48/96 and Simeck64/128, the differentials with less active bits are preferred so we can extend the trails for more rounds and attack more rounds. Then we take advantage of the links between linear characteristic and differential characteristic to construct linear hull distinguishers for

^a additions.

^b encryption of attacked rounds.

the Simeck family. After getting the boolean expressions for the parity bits of the distinguishers, we use the Guess, Split and Combine technique to calculate the empirical correlations, which reduces the time complexity greatly. As a result, 23/30/37 rounds of Simeck32/48/64 can be attacked (Table 1), which are the best results so far. We also do some experiments to verify our results. The experiment on the bias of the linear hull for Simeck32/64 meets our expectation and 48.4% of the results have a bias higher than we expect. Due to the time limitation, we implement the attack on 21-round Simeck32/64 to recover 8-bit information of 32-bit subkeys. The success rate is 45.6% corresponding to our estimated value, which proves our algorithm is effective.

Outline. This paper is organized as follows. Section 2 gives a brief description of the Simeck family and dynamic key-guessing techniques in the linear hull cryptanalysis. In section 3, we introduce some new differentials and linear hulls from the differentials. Then linear hull cryptanalysis with the dynamic key-guessing techniques are applied to attack all versions of Simeck in section 4. Finally we conclude in section 5.

2 Preliminaries

2.1 The Simeck family

The Simeck family with Feistel structure is proposed in CHES'15. The cipher with 2n-bit block and mn-bit key will be referred to as Simeck2n/mn. There are three versions of Simeck, including Simeck32/64 (32 rounds), Simeck48/96 (36 rounds) and Simeck64/128 (44 rounds). In this paper, we use the notations as follows.

 X^r 2n-bit output of round r (input of round r+1)

 X_L^r left *n*-bit of X^r

 X_R^r right *n*-bit of X^r

 K^r n-bit subkey of round r+1

 $X \ll i$ cycle shift of X to the left by i bits

⊕ bitwise XOR

& bitwise AND

Round function. The round function is described in Figure 1. The (r+1) round's input is $(X_L^r||X_R^r)$ and output is $(X_L^{r+1}||X_R^{r+1})$. The round function is

$$X_L^{r+1} = F(X_L^r) \oplus X_R^r \oplus K^r, \quad X_R^{r+1} = X_L^r,$$

where function $F(X)=((X \ll 5)\&X)\oplus (X \ll 1)$. We can also present the round function for single bit, which we will use in the rest of the paper. Let $X_L^r=\{X_{L,n-1}^r,X_{L,n-2}^r,...,X_{L,0}^r\}$, $X_R^r=\{X_{R,n-1}^r,X_{R,n-2}^r,...,X_{R,0}^r\}$, and the round function can be denoted as

$$\begin{split} X_{L,i}^{r+1} &= (X_{L,(i-5+n)\%n}^r \& X_{L,i}) \oplus X_{L,(i-1+n)\%n}^r \oplus X_{R,i}^r \oplus K_i^r, \quad X_{R,i}^{r+1} = X_{L,i}^r, \\ \text{where } i = 0,1,...,n-1, \text{ and } X_{L,0}^r, \ X_{R,0}^r \text{ is the LSB of } X_L^r \text{ and } X_R^r. \end{split}$$

4

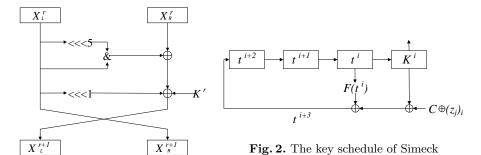


Fig. 1. The round function of Simeck

Key Schedule. The key schedule of Simeck (Figure 2) is similar with Speck. We describe it briefly. To generate a sequence of round keys $\{K^0, ..., K^{n_r-1}\}$ from the master key, the states $\{t^2, t^1, t^0, K^0\}$ are initialized with the master key at first. Then the registers are updated to generate the round keys used in all n_r -round encryption. The updating process is

$$K^{i+1} = t^i$$
, $t^{i+3} = F(t^i) \oplus K^i \oplus C \oplus (z_i)_i$,

where $0 \le i \le n_r - 1$, $C = 2^n - 4$ (n is the word size), $(z_j)_i$ is the i-th bit of z_j . For Simeck32/64 and Simeck48/96, the sequence z_j is generated by the primitive polynomial $X^5 + X^2 + 1$ with the initial states (1, 1, 1, 1, 1). And for Simeck64/128, the z_j is generated by the primitive polynomial $X^6 + X + 1$ with the initial states (1, 1, 1, 1, 1, 1).

2.2 Linear cryptanalysis

We first give the calculation formula of the correlation for boolean function. Let $g(x): F_2^n \to F_2$ is a boolean function and $B(g) = \sum_{x \in F_2^n} (-1)^{g(x)}$, so the correlation c(g) is

$$c(g) = \frac{1}{2^n} B(g) = \frac{1}{2^n} \sum\nolimits_{x \in F_2^n} {{{(- 1)}^{g(x)}}}.$$

Then the bias of g(x) is $\epsilon(g) = \frac{1}{2}c(g)$. In the rest of the paper, we use the B(g) as correlation for simplicity of description in some situations.

Linear cryptanalysis [13] is an important known plaintext cryptanalytic technique, and it tries to find a highly probable expression with plaintexts P, ciphertexts C and key bits K as

$$\alpha \cdot P \oplus \beta \cdot C = \gamma \cdot K$$
,

where α, β, γ are masks. The bias of the expression is $\varepsilon(\alpha \cdot P \oplus \beta \cdot C \oplus \gamma \cdot K)$, so at least $O(\frac{1}{\varepsilon^2})$ plaintexts are needed in the key recovery attack.

The linear hull [14] is a set of linear approximations with the same input mask and output mask, and the potential of a linear hull with mask α and β is

$$ALH(\alpha,\beta) = \sum\nolimits_{\gamma} \epsilon^2 (\alpha \cdot P \oplus \beta \cdot C \oplus \gamma \cdot K) = \bar{\epsilon}^2.$$

Notice the $\bar{\epsilon}^2$ may be higher than ϵ^2 in most situations, so there needs less plaintexts in the linear hull cryptanalysis than linear cryptanalysis.

2.3 Linear compression and Dynamic key-guessing techniques

To reduce the time complexity of calculating the correlation in the linear hull cryptanalysis, the linear part of the function can be compressed at first. Let y = f(x, k) is a boolean function, and x is l_1 -bit plaintext, k is l_2 -bit key, the counter vector V[x] denotes the number of x. If $y = f(x, k) = x_0 \oplus k_0 \oplus f'(x', k')$, we can generate a new counter vector $V'[x'] = \sum_{x_0 \in F_2} (-1)^{x_0} V[x_0||x']$, so the correlation of y under some k guess is

$$B^k(y) = \sum\nolimits_x {(- 1)^{f(x,k)} V[x]} \Rightarrow B^k(y) = (- 1)^{k_0} {\sum\nolimits_{x'} {(- 1)^{f'(x',k')} V'[x']} }.$$

Since the k_0 value doesn't affect the absolute value of $B^k(y)$, k_0 is called related bit and doesn't need to be guessed. So there needs $2^{l_1+l_2-2}$ computations, less than $2^{l_1+l_2}$. If y=f(x,k) has multiple linear bits of x,k, we can also compress them using above method.

Besides, Chen et al. in [10] introduced the Guess, Split and Combine technique to reduce the time complexity based on the dynamic key-guessing techniques. In the calculation of $B^k(y) = \sum_x (-1)^{f(x,k)} V[x]$, let $k = k_G ||k_A|| k_B ||k_C|| ((k_G, k_A, k_B, k_C)$ are $l_2^G, l_2^A, l_2^B, l_2^C$ -bit) and guess the k_G at first. Then all the x values are split into two sets S_A and S_B . For N_A values of $x \in S_A$, f(x) = $f_A(x, k_A | | k_C)$, and for N_B values of $x \in S_B, f(x) = f_B(x, k_B | | k_C)$,

$$B^k(y) = \sum\nolimits_{x \in S_A} {(- 1)^{f_A(x,k_A||k_C)} V_A[x]} + \sum\nolimits_{x \in S_B} {(- 1)^{f_B(x,k_B||k_C)} V_B[x]}.$$

One needs $N_A 2^{l_2^G + l_2^A + l_2^C} + N_B 2^{l_2^G + l_2^B + l_2^C} + 2^{l_2}$ additions in the Guess, Split and Combine process, which takes less time than the general method with $2^{l_1+l_2}$

For example, we use the Guess, Split and Combine technique to calculate the correlation $\hat{B}^{k_1,k_2}(y)$ of $f_1 = (x_1 \oplus k_1) \& (x_2 \oplus k_2)$ with the counter $V[x_1,x_2]$.

- 1. Guess k_1 at first.
- 2. Split the $x = x_1 | |x_2|$ into two cases according the value of $(x_1 \oplus k_1)$.
 - (a) For x_1 that satisfies $x_1 \oplus k_1 = 0$, $f_1 = 0$. It is necessary to generate a
 - new counter $V_1 = \sum_{x_2 \in F_2} V[x_1 = k_1, x_2]$. (b) For x_1 that satisfies $x_1 \oplus k_1 = 1$, $f_1(x, k) = (x_2 \oplus k_2)$. It is necessary to generate a new counter $V_2 = \sum_{x_2 \in F_2} (-1)^{x_2} V[x_1 = k_1 \oplus 1, x_2]$, and k_2 is related bit.
- 3. Combine the two cases, $B^{k_1,k_2}(y) = V_1 + (-1)^{k_2}V_2$.

Step 2.(a)/2.(b) needs 1 addition, and step 3 needs 2 additions. So in total there needs $2 \times (1+1+2) = 2^3$ additions to compress x_1, x_2 , less than the general method.

3 The Linear Hull distinguishers of Simeck

This section first gives some good differentials searched by Kölbl's tool, then derives equivalent linear hulls from the differentials. We also do an experiment on the 13-round linear hull for Simeck32/64 to verify the bias in section 3.2.

3.1 Differential distinguishers of Simeck

Differential cryptanalysis is a chosen plaintext/ciphertext cryptanalytic technique. In the round function of Simeck, the only non-linear operation is the AND operation. For the single bit x and y, the probability of (x & y) = 0 is 0.75. We can extract highly probable differential expressions of the function F(X) as

```
Differential Characteristic 1 : \Pr[(\Delta X))_i \to (\Delta F(X))_{i+1}] = 0.5,
Differential Characteristic 2 : \Pr[(\Delta X))_i \to (\Delta F(X))_{i+1,i}] = 0.5,
Differential Characteristic 3 : \Pr[(\Delta X))_i \to (\Delta F(X))_{i+1,i+5}] = 0.5,
Differential Characteristic 4 : \Pr[(\Delta X))_i \to (\Delta F(X))_{i+1,i,i+5}] = 0.5,
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where the $(\Delta F(X))_{i+1}$ denotes the (i+1)-th bit is 1 and the others are 0.

In [11], Kölbl introduced a tool for cryptanalysis of symmetric primitives based on SMT/SAT solvers. We use the tool to search the differentials which have a balance between low Hamming weight and high probability to attack more rounds using less plaintexts. The differentials we choose are listed in Table 2.

cipher round Δ_{in} Δ_{out} log_2 diff Reference Simeck32/64 13 (0x0, 0x2)(0x2, 0x0)-29.64[15] Simeck32/64 13 (0x0, 0x2)(0x2, 0x0)-28.91 this paper Simeck48/96 (0x400000, 0xE00000) (0x400000, 0x200000) -43.6520 [12]Simeck48/96 20 (0x400000, 0xA00000) (0x400000, 0x200000) -43.66 this paper Simeck64/128 26 (0x0, 0x4400000)(0x8800000, 0x400000) -60.02Simeck64/128 26 (0x0, 0x4400000)(0x800000, 0x400000)-60.09 this paper

Table 2. The differentials of Simeck

For Simeck32/64, by searching all the characteristics with probability higher than 2^{-52} , we get more accurate result than [15]. For Simeck48/96 and Simeck64/128, the differentials with less active bits in the input difference and output difference are preferred, since less key bits are involved in the attack. At the same time, the probability of the differentials must be higher than 2^{-45} or 2^{-61} , to ensure the data complexity and success rate can be achieved (If we search more time, the probability will be equivalent to the result in [12]).

Linear Hull distinguishers of Simeck

In [4], Alizadeh et al. noticed each differential characteristic can be mapped into a linear approximation for Simon. The property is based on the round function of Simon, so we can use the similar property for Simeck to construct an equivalent linear characteristic from a differential characteristic. The relation between the probability p of a differential and the potential $\bar{\epsilon}^2$ of a linear hull is $\bar{\epsilon}^2 = 2^{-2}p$. The linear approximation expressions of the function F(X) for Simeck are

```
Linear Approximation 1: Pr[(F(X))_i = (X)_{i-1}] = 0.75,
Linear Approximation 2: \Pr[(F(X))_i = (X)_{i-1} \oplus (X)_i] = 0.75,
Linear Approximation 3: \Pr[(F(X))_i = (X)_{i-1} \oplus (X)_{i-5}] = 0.75,
Linear Approximation 4: \Pr[(F(X))_i = (X)_{i-1} \oplus (X)_i \oplus (X)_{i-5}] = 0.25.
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[1,6,17] gave some other methods to find linear hulls for Simon, including correlation matrix, Mixed Integer Programming (MIP) and so on. In this paper, we use the differential characteristics to get linear characteristics. The used linear

Table 3. Linear hull based on the differential for Simeck32/64

r	Diffe	rential			Line	ar
	Λ	Λ	l v	-	v	Hand Ann

r	Dif	ferential	Linear					
•	Δ_L	Δ_R	X_L	X_R	Used App			
0	_	1	1	_	_			
1	1	_	_	1	1			
2	2	1	1	0	1			
3	1, 3	2	0	1, 15	1:1			
4	4	1, 3	1,15	14	1			
5	1, 3, 5	4	14	1,13,15	3:1:2			
6	2,3	1, 3, 5	1, 13, 15	0, 15	1:1			
7	1, 4, 5	2,3	0, 15	1,13,14	3:2:2			
8	3, 4	1, 4, 5	1, 13, 14	14, 15	1:2			
9	1, 3	3, 4	14, 15	1, 15	1:2			
10	2	1, 3	1,15	0	1			
11	1	2	0	1	1			
12	_	1	1	_	_			
13	1	_	_	1	_			
		$g_2 pr = -38$	$\log_2 \varepsilon^2 = -40$					
	$\log_2 p_{di}$	$_{ff} = -28.91$	$\log_2 \bar{\varepsilon}^2 = -30.91$					
	#trail.	s = 1846518	#chara	cteristics	s = 1846518			

approximations (Used App) can be found above. The details for Simeck32/64 are listed in Table 3. For Simeck48/96 and Simeck64/128, the details of the calculation process are similar with Simeck32/64 that we omit them in this paper. The linear hulls for all versions of Simeck can be seen in Table 4.

Table 4. The linear hulls for Simeck

cipher	round	Input Active bits	Output Active bits	ALH
Simeck32/64	13	$X_{L,1}^r$	$X_{R,1}^{r+13}$	-30.91
Simeck48/96	20	$X_{L,19}^r, X_{L,21}^r, X_{R,20}^r$	$X_{L,21}^{r+20}, X_{R,20}^{r+20}$	-45.66
Simeck64/128	26	$X_{L,18}^r, X_{L,22}^r$	$\begin{array}{c} X_{R,1}^{r+13} \\ X_{L,21}^{r+20}, X_{R,20}^{r+26} \\ X_{L,22}^{r+26}, X_{R,21}^{r+26} \end{array}$	-62.09

Experiments for Simeck32/64. Since the block of Simeck32/64 only contains 32 bits, we can iterate over the 2^{32} possible plaintexts to validate the bias $(\bar{\varepsilon}^2)$ of the 13-round linear hull. Randomly select 1000 keys and the experimental results are listed in Table 5. In the experiments, 48.4% of the keys have a bias higher than $2^{-30.91}$, which is corresponding to the linear hull's $ALH = 2^{-30.91}$.

Table 5. Bias of the 13-round linear hull

$log_2(ararepsilon^2)$	Num	Probability	$log_2(ararepsilon^2)$	Num	Probability
$ \begin{array}{c} [-27.91, 0) \\ [-28.91, -27.91) \end{array} $		$0.056 \\ 0.123$	[-30.91, -29.91) [-31.91, -30.91)	151 144	$0.151 \\ 0.144$
[-28.91, -27.91) [-29.91, -28.91)		0.123	$(-\infty, -31.91)$	372	0.144 0.372

4 Key Recovery Attack on Simeck

In this section, we discuss key recovery attack on all three versions of Simeck, and implement the 21-round attack for Simeck32/64 to verify our algorithm.

4.1 Key Recovery Attack on Simeck32/64

We use the 13-round linear hull

$$X_{L,1}^r \to X_{R,1}^{r+13}$$

obtained in section 3.2 to attack Simeck32/64. At first four more rounds before and four more rounds after the linear hull are added to get a 21-round distinguisher. Take some plaintexts or subkeys as a whole, we can get the expression for $X_{L,1}^r$ as $f(x,k) = x_0 \oplus k_0 \oplus f'(x',k')$, where

$$f'(x',k') = ((x_1 \oplus k_1)\&(x_2 \oplus k_2)) \oplus ((x_3 \oplus k_3)\&(x_4 \oplus k_4)) \oplus$$

$$[(x_5 \oplus k_5 \oplus (x_6 \oplus k_6)\&(x_7 \oplus k_7))\&(x_8 \oplus k_8 \oplus (x_7 \oplus k_7)\&(x_9 \oplus k_9))]$$

$$\oplus \{\{(x_{10} \oplus k_{10} \oplus (x_6 \oplus k_6)\&(x_7 \oplus k_7)) \oplus$$

$$[(x_{11} \oplus k_{11} \oplus (x_{12} \oplus k_{12})\&(x_{13} \oplus k_{13}))\&(x_{14} \oplus k_{14} \oplus (x_3 \oplus k_3)\&(x_{13} \oplus k_{13}))]\}$$

$$\&\{(x_{15} \oplus k_{15} \oplus (x_7 \oplus k_7)\&(x_9 \oplus k_9)) \oplus$$

$$[(x_{14} \oplus k_{14} \oplus (x_{13} \oplus k_{13})\&(x_3 \oplus k_3))\&(x_{16} \oplus k_{16} \oplus (x_3 \oplus k_3)\&(x_4 \oplus k_4))]\}\}.$$

In the expression, $x' = \{x_1, ..., x_{16}\}$ and $k' = \{k_1, ..., k_{16}\}$. The details of $\{x_0, x_1, ..., x_{16}\}$, $\{k_0, k_1, ..., k_{16}\}$ are given in Table 6. Notice $x_{10} = x_3 \oplus x_5$ and $x_{15} = x_4 \oplus x_8$, so there are 15 independent bits of x and 17 independent bits of k. The $X_{R,1}^{r+13}$ also can be represented as f(x, k) where x, k have similar expressions as that in Table 6. (The expressions of x, x for x

\overline{x}	Expression of x	$\mid k$	Expression of k
x_0	$X_{L,1}^{r-4} \oplus X_{L,15}^{r-4} \\ \oplus (X_{L,9}^{r-4} \& \oplus X_{L,14}^{r-4}) \oplus X_{L,13}^{r-4} \oplus X_{R,14}^{r-4}$	k_0	$K_1^{r-1} \oplus K_0^{r-2} \oplus K_1^{r-3} \\ \oplus K_{15}^{r-3} \oplus K_{14}^{r-4}$
x_1	$(X_{L,10}^{r-4} \& \oplus X_{L,14}^{r-4}) \oplus X_{L,13}^{r-4} \oplus X_{R,14}^{r-4} (X_{L,5}^{r-4} \& \oplus X_{L,10}^{r-4}) \oplus X_{L,9}^{r-4} \oplus X_{R,10}^{r-4} (X_{L,10}^{r-4} \& \oplus X_{L,15}^{r-4}) \oplus X_{L,14}^{r-4} \oplus X_{R,15}^{r-4} (X_{L,7}^{r-4} \& \oplus X_{L,12}^{r-4}) \oplus X_{L,14}^{r-4} \oplus X_{R,12}^{r-4} (X_{L,12}^{r-4} \& \oplus X_{L,1}^{r-4}) \oplus X_{L,04}^{r-4} \oplus X_{R,1}^{r-4} $	k_1	K_{10}^{r-4}
x_2	$(X_{L,10}^{r-4}\&\oplus X_{L,15}^{r-4})\oplus X_{L,14}^{r-4}\oplus X_{R,15}^{r-4}$	k_2	$K_{15}^{r-4} \ K_{12}^{r-4}$
x_3	$(X_{L,7}^{r-4}\&\oplus X_{L,12}^{r-4})\oplus X_{L,11}^{r-4}\oplus X_{R,12}^{r-4}$	k_3	K_{12}^{r-4}
x_4	$(X_{L,12}^{r-4}\&\oplus X_{L,1}^{r-4})\oplus X_{L,0}^{r-4}\oplus X_{R,1}^{r-4}$	k_4	K_1^{r-4}
x_5	$(X_{L,5}^{r-4} \& \oplus X_{L,10}^{r-4}) \oplus X_{L,9}^{r-4} \oplus X_{R,10}^{r-4} \oplus X_{L,11}^{r-4}$	k_5	$K_{10}^{r-4} \oplus K_{11}^{r-3}$
x_6	$(X_{L,1}^{r-4}\& \oplus X_{L,6}^{r-4}) \oplus X_{L,5}^{r-4} \oplus X_{R,6}^{r-4}$	k_6	K_6^{r-4}
x_7	$(X_{L,6}^{r-4}\&\oplus X_{L,11}^{r-4})\oplus X_{L,10}^{r-4}\oplus X_{R,11}^{r-4}$	k_7	K_{11}^{r-4}
x_8	$(X_{L,10}^{r-4}\& \oplus X_{L,15}^{r-4}) \oplus X_{L,14}^{r-4} \oplus X_{R,15}^{r-4} \oplus X_{L,0}^{r-4}$	k_8	$K_{15}^{r-4} \overset{\oplus}{\oplus} K_0^{r-3} \ K_0^{r-4}$
x_9	$(X_{L,11}^{r-4}\& \oplus X_{L,0}^{r-4}) \oplus X_{L,15}^{r-4} \oplus X_{R,0}^{r-4}$	k_9	
x_{10}	$x_3 \oplus x_5$	$ k_{10} $	$k_3 \oplus k_5 \oplus K_{12}^{r-2}$
x_{11}		$ k_{11} $	$K_6^{r-4} \oplus K_7^{r-3}$
x_{12}	$(X_{L,13}^{r-4} \& \oplus X_{L,2}^{r-4}) \oplus X_{L,1}^{r-4} \oplus X_{R,2}^{r-4}$	$ k_{12} $	
x_{13}		k_{13}	
x_{14}	$(X_{L,6}^{r-4}\& \oplus X_{L,11}^{r-4}) \oplus X_{L,10}^{r-4} \oplus X_{R,11}^{r-4} \oplus X_{L,12}^{r-4}$	$ k_{14} $	$K_{11}^{r-4} \oplus K_{12}^{r-3}$
x_{15}	$x_4 \oplus x_8$	$ k_{15} $	$k_4 \oplus k_8 \oplus K_1^{r-2}$
x_{16}	$(X_{L,11}^{r-4}\& \oplus X_{L,0}^{r-4}) \oplus X_{L,15}^{r-4} \oplus X_{R,0}^{r-4} \oplus X_{L,1}^{r-4}$	$ k_{16} $	$K_0^{r-4} \oplus K_1^{r-3}$

Table 6. The expressions for $X_{L,1}^r$

The x denotes the plaintexts or ciphertexts and the k denotes the subkey bits. We use $x_p = \{x_{p,0},...,x_{p,16}\}$ and $k_p = \{k_{p,0},...,k_{p,16}\}$ to represent the x,k for $X_{L,1}^r$. For $X_{R,1}^{r+13}$, we use x_c and k_c . Then the $X_{L,1}^r$ can be denoted by $f(x_p,k_p)$ and the $X_{R,1}^{r+13}$ can be denoted by $f(x_c,k_c)$.

Let the plaintexts $P = X^{r-4}$ and the ciphertexts $C = X^{r+17}$. We can compress the N pairs (P,C) into a counter vector $V[x_p,x_c]$ of size $2^{15+15}=2^{30}$. Then the empirical correlation under some subkey k_p and k_c is

$$\overline{c}_{k_p,k_c} = \frac{1}{N} \sum\nolimits_{x_p,x_c} {(-1)^{f(x_p,k_p) \oplus f(x_c,k_c)} V[x_p,x_c]}. \label{eq:constraint}$$

As we can see, $f(x,k) = x_0 \oplus k_0 \oplus f'(x',k')$ is linear with $x_0 \oplus k_0$. So the $x_{p,0}$ and $x_{c,0}$ can be compressed at first as following

$$V_1[x_p', x_c'] = \sum_{x_{p,0}, x_{c,0} \in F_2} (-1)^{x_{p,0} \oplus x_{x,0}} V[x_p, x_c].$$

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The target correlation becomes

$$\overline{c}_{k_p',k_c'} = \frac{1}{N} \sum\nolimits_{x_c'} {{{(- 1)}^{f'(x_c',k_c')}}} \sum\nolimits_{x_p'} {{{(- 1)}^{f'(x_p',k_p')}}} V_1[x_p',x_c'],$$

and the $k_{p,0}$, $k_{c,0}$ can be regarded as related bits and omitted in the calculation. We introduce how to calculate the $B^{k'}(y) = \sum_{x'} (-1)^{f'(x',k')} V'[x']$ efficiently using dynamic key-guessing techniques in the following Procedure A, where y = f'(x',k') and V'[x'] is the num of x'. The calculation of $B^{k'_p}(y) = \sum_{x'_p} (-1)^{f'(x'_p,k'_p)} V_1[x'_p,x'_c]$ for constant x'_c is same with $B^{k'}(y)$, so calculating the $\overline{c}_{k'_p,k'_c}$ needs to call Procedure A twice.

Procedure A. The expression of f'(x', k') is the same with the expression for Simon32/64, so the calculation process is similar. The details can be seen in the section 4.2 of [10], and we gives the basic ideas in the following. There are only 14 independent bits for $\{x_1, \ldots, x_{16}\}$ and 16 independent bits for $\{k_1, \ldots, k_{16}\}$. We introduces the procedure briefly.

- 1. Guess k_1, k_3, k_7 at first.
- 2. Split the f'(x', k') into 8 cases according to the values of $\{x_1 \oplus k_1, x_3 \oplus k_3, x_7 \oplus k_7\}$. For each case, there needs $2^8 \times 7$ additions to generate a new counter vector. Then also apply the Guess, Split and Combine technique to calculate the partial correlation of each case, and the time complexity is $2^{11.19}$ additions each.
- 3. Combine the 8 cases to get the final correlation, there needs $2^{13} \times 7$ additions.

The total time of Procedure A is

$$T = 2^3 \times (8 \times (2^8 \times 7 + 2^{11.19}) + 2^{13} \times 7) = 2^{19.46}$$
.

Attack on 23 rounds. We add one more round before and one more round after the 21-round distinguisher. According the plaintexts and ciphertexts involved in the 21-round distinguisher, there needs to guess 13-bit keys in (r-5)-th round and 13-bit keys in (r+17)-th round. The estimated potential $\bar{\varepsilon}^2$ of the linear hull is $2^{-30.91}$. Set the advantage a=8 and data complexity $N=2\times 2^{30.19}=2^{31.19}=c_N\cdot\bar{\varepsilon}^2$. According to the experiments on the bias of the 13-round linear hull in the section 3.2 and the theory of success rate in [16], we can get the range of the success rate (0.411,0.532) of the attack in Table 7.

The details of the attack are as follows.

- 1. Guess 13 bits $\{K_0^{r-5} K_2^{r-5}, K_5^{r-5} K_7^{r-5}, K_9^{r-5} K_{15}^{r-5}\}$ and 13 bits $\{K_0^{r+17} K_2^{r+17}, K_5^{r+17} K_7^{r+17}, K_9^{r+17} K_{15}^{r+17}\}$. For each of the 2^{26} values.
 - a. Encrypt the plaintexts by one round and decrypt the ciphertexts by one round to get the X^{r-4} and X^{r+17} . Then compress the N pairs (X^{r-4}, X^{r+17}) into a counter vector $V_1[x_p', x_c']$ of size $2^{14+14} = 2^{28}$. This step takes $N = 2^{31.91}$ times two-round encryptions and compressions.

$log_2(ararepsilon^2)$	Prob.(p)	c_N	Lower success-rate(s_l)	Upper success-rate (s_u)
[-27.91, 0)	0.056	$c_N \ge 16$	1	1
[-28.91, -27.91)	0.123	$8 \le c_N < 16$	0.997	1
[-29.91, -28.91)	0.154	$4 \le c_N < 8$	0.867	0.997
[-30.91, -29.91)	0.151	$2 \le c_N < 4$	0.477	0.867
[-31.91, -30.91)	0.144	$1 \le c_N < 2$	0.188	0.477
			$\sum p \cdot s_l = 0.411$	$\sum p \cdot s_u = 0.532$

Table 7. Experimental results for the 13-round linear hull of Simeck32/64

- b. For each of 2¹⁴ x'_c, call Procedure A to calculate the correlation for different k'_p and constant x'_c. Now we have 2¹⁶⁺¹⁴ counters of 14 bits x'_c and 16 bits k'_p. This step needs 2¹⁴ × 2^{19.46} times additions.
 c. For each of 2¹⁶ k'_p, call Procedure A to calculate the correlation for different k'_c. Now we have 2¹⁶⁺¹⁶ counters of 16 bits k'_p and 16 bits k'_c.
- This step needs $2^{16} \times 2^{19.46}$ additions.

In total, there needs $2^{26} \times 2^{31.91}$ times two-round encryptions and $2^{26} \times$ $(2^{33.46} + 2^{35.46}) = 2^{61.78}$ additions.

2. We have $2^{26+32} = 2^{58}$ counters now. Since the advantage is 8, so the key ranked in the largest 2^{58-8} counters can be the right key. Get 2^{56} candidates of the master key according to the the key schedule and do exhaustive search to find the right key. There needs 2^{56} times 23-round encryptions.

Attack complexity: $2^{61.78}$ additions and $2^{56.41}$ 23-round encryptions.

Implementation of the 21-round attack If we don't consider the (r-5)-th round and (r+17)-th round in the 23-round attack, the 21-round attack needs $2^{35.78}$ additions to get 2^{24} possible values of 32 subkey bits. (Due to the time limitation, we don't do the exhaustive search to recover the whole master key).

We randomly select the master key to do experiments on the recovery of 8-bit key information for the 32 bits subkey involved in the 21-round attack. If the correct subkey bits are in the first 2^{24} counters of all the 2^{32} counters in descending order, we believe the attack is successful and can recover the correct key bits. There are 1000 master keys tested and the success rate is 0.456, which meets our expectation (0.411, 0.531) and our attack algorithm is effective.

Key Recovery Attack on Simeck48/96

We use the 20-round linear hull

$$X_{L,19}^r \oplus X_{L,21}^r \oplus X_{R,20}^r \to X_{L,21}^{r+20} \oplus X_{R,20}^{r+20}$$

obtained in section 3.2 to attack Simeck48/96. Add 4 rounds before r-th round, we get the expression $f_B(x_B,k_B)$ for $X_{L,19}^r \oplus X_{L,21}^r \oplus X_{R,20}^r$. Add 4 rounds after (r+20)-th round, we get the expression $f_C(x_C,k_C)$ for $X_{L,21}^{r+20} \oplus X_{R,20}^{r+20}$. (We give expressions of $f_B(x_B, k_B)$ and $f_C(x_C, k_C)$ and details of $\{x_B, k_B\}$ and $\{x_C, k_C\}$ are similar with Table 6 that we omit them in this paper.). Then we can get a 28-round distinguisher for Simeck48/96.

Table 8. Time complexity for some functions

Case	Expression	Time
f_1	$(x_1 \oplus k_1 \oplus (x_2 \oplus k_2) \& (x_3 \oplus k_3)) \& (x_4 \oplus k_4 \oplus (x_2 \oplus k_2) \& (x_5 \oplus k_5))$	$2^{6.46}$
f_2		$2^{15.99}$
f_3	$f_2 \oplus ((x_8 \oplus k_8) \& (x_{12} \oplus k_{12}))$	$2^{15.99}$
f_4	$f_2 \oplus ((x_{13} \oplus k_{13})\&(x_{14} \oplus k_{14})) \oplus ((x_8 \oplus k_8)\&(x_{12} \oplus k_{12})) \oplus (x_{15} \oplus k_{15} \oplus (x_2 \oplus k_2)\&(x_3 \oplus k_3))\&(x_{16} \oplus k_{16} \oplus (x_{10} \oplus k_{10})\&(x_3 \oplus k_3))$ $Notice: x_1 = x_8 \oplus x_{15}, x_9 = x_{12} \oplus x_{16}$	
f_5	$f_4 \oplus ((x_8 \oplus k_8) \& (x_{12} \oplus k_{12}))$	$2^{19.46}$

For simplicity, we give the time complexity of calculating the correlation for some common boolean functions in Table 8. Case f_1 and f_2 can be found in [10] and the time complexity is $2^{6.46}$ and $2^{15.99}$. There is little difference between case f_2 and f_3 , where $f_3 = f_2 \oplus ((x_8 \oplus k_8) \& (x_{12} \oplus k_{12}))$. Because the x_8, x_{12} and k_8, k_{12} are also involved in f_2 and compressed at first, so in the calculation the only change is the method of generating the new counter vector, and the time complexity is equal for the two cases. The case f_4 is same with the Procedure A in section 4.1 and the time complexity is $2^{19.46}$. For the similar reason like f_2 and f_3 , the f_5 have a time complexity of $2^{19.46}$ as f_4 .

Procedure B. Here we discuss how to calculate $B^{k_B}(y) = \sum_{x_B} (-1)^{f_B(x_B,k_B)}$

```
f_B(x_B, k_B) = x_0 \oplus k_0 \oplus (x_1 \oplus k_1) \& (x_2 \oplus k_2)
\oplus (x_3 \oplus k_3) \& (x_4 \oplus k_4) \oplus (x_5 \oplus k_5) \& (x_6 \oplus k_6)
\oplus [(x_7 \oplus k_7 \oplus (x_8 \oplus k_8) \& (x_9 \oplus k_9)) \& (x_{10} \oplus k_{10} \oplus (x_9 \oplus k_9) \& (x_{11} \oplus k_{11}))]
\oplus \{ [x_{12} \oplus k_{12} \oplus (x_8 \oplus k_8) \& (x_9 \oplus k_9) \oplus
(x_{13} \oplus k_{13} \oplus (x_{14} \oplus k_{14}) \& (x_{15} \oplus k_{15})) \& (x_{16} \oplus k_{16} \oplus (x_3 \oplus k_3) \& (x_{15} \oplus k_{15}))]
\& [x_{17} \oplus k_{17} \oplus ((x_9 \oplus k_9) \& (x_{11} \oplus k_{11})) \oplus
(x_{16} \oplus k_{16} \oplus (x_3 \oplus k_3) \& (x_{15} \oplus k_{15})) \& (x_{18} \oplus k_{18} \oplus (x_3 \oplus k_3) \& (x_4 \oplus k_4))]\}
\oplus \{ [x_{19} \oplus k_{19} \oplus (x_{20} \oplus k_{20}) \& (x_{21} \oplus k_{21}) \oplus
(x_{22} \oplus k_{22} \oplus (x_{23} \oplus k_{23}) \& (x_{24} \oplus k_{24})) \& (x_{25} \oplus k_{25} \oplus (x_5 \oplus k_5) \& (x_{24} \oplus k_{24}))]
\& [x_{26} \oplus k_{26} \oplus (x_{21} \oplus k_{21}) \& (x_{27} \oplus k_{27}) \oplus
(x_{25} \oplus k_{25} \oplus (x_5 \oplus k_5) \& (x_{24} \oplus k_{24})) \& (x_{28} \oplus k_{28} \oplus (x_5 \oplus k_5) \& (x_6 \oplus k_6))]\}
```

 $V_B[x]$ efficiently using dynamic key-guessing techniques. Compress the plaintexts of r-th round into a counter $V_B[x_1,...,x_{28}]$. Since $x_{12}=x_3\oplus x_7, x_{17}=x_4\oplus x_{10}$, there are only 26 independent x bits.

- 1. Compress $\{x_1-x_4,x_7-x_{18}\}$ as case f_4 for each $\{x_5,x_6,x_{19}-x_{28}\}$, the time complexity is $2^{19.46}$ each. This step needs $2^{12} \cdot 2^{19.46} = 2^{31.46}$ additions in total. Now we have a counter vector for 16 bits keys and 12 bits x.
- 2. Compress $\{x_5, x_6, x_{19} x_{28}\}$ as case f_3 for each $\{k_1 k_4, x_7 x_{18}\}$, the time complexity is $2^{15.99}$ each. This step needs $2^{16} \cdot 2^{15.99} = 2^{31.99}$ additions in total. Now we have a counter vector for 28 bits keys.

In total, the time complexity of procedure B is $2^{31.46} + 2^{31.99} = 2^{32.75}$ additions.

Procedure C. Here we discuss how to calculate $B^{k_C}(y) = \sum_{x_C} (-1)^{f_C(x_C, k_C)} V_C[x]$ efficiently using dynamic key-guessing techniques. Compress the ciphertexts of (r+20)-th round into a counter $V_C[x_1, ..., x_{21}]$, since $x_{13} = x_8 \oplus x_{18}, x_{19} = x_{11} \oplus x_{21}$, there are only 19 independent x bits.

```
f_{C}(x_{C}, k_{C}) = x_{0} \oplus k_{0} \oplus ((x_{1} \oplus k_{1}) \& (x_{2} \oplus k_{2}))
\oplus [(x_{3} \oplus k_{3} \oplus (x_{4} \oplus k_{4}) \& (x_{5} \oplus k_{5})) \& (x_{6} \oplus k_{6} \oplus (x_{5} \oplus k_{5}) \& (x_{7} \oplus k_{7}))]
\oplus [(x_{8} \oplus k_{8} \oplus (x_{9} \oplus k_{9}) \& (x_{10} \oplus k_{10})) \& (x_{11} \oplus k_{11} \oplus (x_{10} \oplus k_{10}) \& (x_{12} \oplus k_{12}))]
\oplus \{[x_{13} \oplus k_{13} \oplus ((x_{9} \oplus k_{9}) \& (x_{10} \oplus k_{10})) \oplus (x_{14} \oplus k_{14} \oplus (x_{15} \oplus k_{15}) \& (x_{16} \oplus k_{16})) \& (x_{17} \oplus k_{17} \oplus (x_{16} \oplus k_{16}) \& (x_{18} \oplus k_{18}))]
\&[x_{19} \oplus k_{19} \oplus ((x_{10} \oplus k_{10}) \& (x_{12} \oplus k_{12})) \oplus (x_{17} \oplus k_{17} \oplus (x_{16} \oplus k_{16}) \& (x_{18} \oplus k_{18})) \& (x_{20} \oplus k_{20} \oplus (x_{18} \oplus k_{18}) \& (x_{21} \oplus k_{21}))]\}
```

- 1. Compress $\{x_3-x_7\}$ as case f_1 for each $\{x_1, x_2, x_8-x_{21}\}$, the time complexity is $2^{6.46}$ each. This step needs $2^{14} \cdot 2^{6.46} = 2^{20.46}$ additions in total. Now we have a counter vector for 5 bits keys and 14 bits x.
- 2. Compress $\{x_1, x_2, x_8 x_{21}\}$ as case f_5 for each $\{k_3 k_7\}$, the time complexity is $2^{19.46}$ each, and this step needs $2^5 \cdot 2^{19.46} = 2^{24.46}$ additions. Now we have a counter vector for 21 bits keys.

In total, the time complexity of procedure C is $2^{20.46} + 2^{24.46} = 2^{24.55}$ additions.

Attack on 30 rounds. We add one more round before and one more round after the 28-round distinguisher. According the plaintexts and ciphertexts involved in the 28-round distinguisher, there needs to guess 21-bit keys in (r-5)-th round and 18-bit keys in (r+24)-th round. The estimated potential of this linear hull is $2^{-45.66}$. Set the advantage a=8 and data complexity $N=4\times 2^{45.66}=2^{47.66}$, the success rate is 0.867.

1. Guess 21 bits $\{K_1^{r-5}, K_3^{r-5} - K_{21}^{r-5}, K_{23}^{r-5}\}$ and 18 bits $\{K_0^{r+24}, K_4^{r+24} - K_6^{r+24}, K_8^{r+24} - K_{21}^{r+24}\}$. For each of 2^{39} values,

- 14
- a. Encrypt the plaintexts by one round and decrypt the ciphertexts by one round to get the X^{r-4} and X^{r+24} . Then compress the N pairs (X^{r-4}, X^{r+24}) into a counter vector of size 2^{45} . This step takes $N = 2^{47.66}$ times two-round encryptions and compressions.
- b. For each of 2^{19} x_C in f_C , call Procedure B. Now we have 2^{19+28} counters of 19 bits x_C and 28 bits k_B . This step needs $2^{19} \times 2^{32.75}$ additions.
- c. For each of 2^{28} k_B , call Procedure C. Now we have 2^{28+21} counters of 28 bits k_B and 21 bits k_C . This step needs $2^{28} \times 2^{24.55}$ additions.

In total, this step needs $2^{39}\times 2^{47.66}$ times two-round encryptions and $2^{39}\times 2^{53.2}$ additions.

2. We have $2^{39+49} = 2^{88}$ counters in total and the key ranked in the largest 2^{88-8} counters can be the right key. Get 2^{88} candidates of the master key according to the the key schedule and do exhaustive search to find the right key.

Attack complexity: $2^{92.2}$ additions and $2^{88.04}$ 30-round encryptions.

4.3 Key Recovery Attack on Simeck64/128

We use the 26-round linear hull

$$X_{L,18}^r \oplus X_{L,22}^r \to X_{L,22}^{r+26} \oplus X_{R,21}^{r+26}$$

obtained in section 3.2 to attack Simeck64/128. Add four more rounds on the top and four more rounds on the bottom to get a 34-round distinguisher. The expression for the parity bits $X_{L,18}^r \oplus X_{L,22}^r$ and $X_{L,22}^{r+26} \oplus X_{R,21}^{r+26}$ are also similar with the other two situations that we omit the details in this paper.

Then adding two more rounds before and one more round after the 34-round distinguisher we can attack the 37-round Simeck64/128. The procedure is similar with the attack on Simeck32/64 and Simeck48/96, and due to the space limitation we will not repeat it. The estimated potential of this linear hull is $2^{-62.09}$. Set the advantage a=8 and data complexity $N=2\times 2^{62.09}=2^{63.09}$, the success rate is 0.477. The time complexity of the 37-round attack is $2^{111.44}$ additions and $2^{121.25}$ 37-round encryptions.

5 Conclusion

In this paper, we analyzed the security of Simeck against improved linear hull cryptanalysis with dynamic key-guessing techniques. We searched out better differentials using Kölbl's tool, then got linear hulls for all versions of Simeck. With Chen et al.'s Guess, Split, Combine technique to reduce the time complexity in the calculation of empirical correlations, we made the improved linear hull attack on Simeck. As a result, we can attack 23-round Simeck32/64, 30-round Simeck48/96 and 37-round Simeck64/128, which are the best results so far from the point of rounds attacked. The experiments on the bias of the linear hull for Simeck32/64 met our expectation and 48.4% of the results have a bias higher

than we expected. We also implemented the attack on 21-round Simeck32/64, and the success rate is 45.6% corresponding to our estimated value, which proves our algorithm is effective.

In the future, we will try to search better linear hulls for Simeck using other methods like correlation matrix, Mixed Integer Programming (MIP) and so on. Then we will apply the improved linear hull attack with dynamic key-guessing techniques to other bit-oriented block ciphers.

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