

# On the Anonymity of One Authentication and Key Agreement Scheme for Peer-to-Peer Cloud

Zhengjun Cao, Lihua Liu

**Abstract.** Peer-to-peer communication systems can provide many functions, including anonymized routing of network traffic, massive parallel computing environments, and distributed storage. Anonymity refers to the state of being completely nameless, with no attached identifiers. Pseudonymity involves the use of a fictitious name that can be consistently linked to a particular user, though not necessarily to the real identity. Both provide a layer of privacy, shielding the user's true identity from public view. But we find their significations are often misunderstood. In this note, we clarify the differences between anonymity and pseudonymity. We also find the Zhong et al.'s key agreement scheme [IEEE TCC, 2022, 10(3), 1592-1603] fails to keep anonymity, not as claimed.

**Keywords:** Key agreement; Anonymity; Pseudonymity; Mutual authentication; Peer-to-peer cloud.

## 1 Introduction

In peer-to-peer (P2P) communication systems, each party has the same capabilities and either party can initiate a communication session. P2P systems can provide anonymized routing of network traffic, massive parallel computing environments, distributed storage, and so on. In 2018, Nguyen and Chang [8] designed a biometric-based three-party authenticated key exchange for dynamic P2P systems. Parne et al. [10] proposed a security enhanced authentication key agreement protocol for P2P networks. Tahavori et al. [2, 13–15] presented some authenticated key agreement schemes for smart grid. In 2023, Chen et al. [3, 9] discussed two provably-secure authenticated key agreement protocols for healthcare systems. Das et al. [4] presented a non-linear multi-objective technique for hybrid P2P communication. Khodoomi et al. [5, 7, 11, 12] discussed P2P energy trading case. Alfaverh et al. [1] investigated a dynamic P2P electricity market model.

In 2022, Zhong et al. [16] have also presented a mutual authentication and key agreement scheme based on elliptic curve certificate-free cryptography for peer-to-peer cloud. It is designed to meet many security requirements, such as mutual authentication, session key establishment, identity anonymity, identity traceability, perfect forward secrecy, resistance to replay attack, man-in-the-middle attack, impersonation attack, etc. In this note, we show that the scheme fails to keep anonymity, not as claimed. We also clarify the signification of true anonymity. To the best of our knowledge, it is the first time to clarify the explicit signification and the differences between anonymity and pseudonymity.

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## 2 Review of the Zhong et al.'s scheme

In the proposed scenario, there are three entities: cell phone user  $U$ , request data cloud server  $C_i$ , and source data cloud server  $U_j$ . It consists of three phases: initialization, login, and cloud handshake.

Let  $E(F_p)$  be an elliptic curve,  $G_q$  be an additive cyclic group over the curve with a base point  $P$ , where  $p, q$  are two large prime numbers. Let  $E_k()$  be a symmetric key encryption with the key  $k$ . The user  $U$  picks  $\omega \in Z_q^*$  and sets it as the private key, corresponding to the public key  $P_{pub} = \omega P$ . Choose four one-way secure hash functions:

$$\begin{aligned} H_1 &: \{0, 1\}^* \times G_q \rightarrow Z_q^*, & H_2 &: \{0, 1\}^* \times G_q \times G_q \times \{0, 1\}^* \rightarrow Z_q^* \\ H_3 &: \{0, 1\}^* \times \{0, 1\}^* \times G_q \times G_q \times \{0, 1\}^* \times G_q \times G_q \rightarrow Z_q^* \\ H_4 &: \{0, 1\}^* \times \{0, 1\}^* \times G_q \times G_q \times G_q \times G_q \times \{0, 1\}^* \rightarrow Z_q^* \end{aligned}$$

Finally, the user  $U$  publishes system arguments as,

$$argums = \{E(F_p), p, q, P, P_{pub}, H_1, H_2, H_3, H_4\}$$

and saves  $\omega$  secretly. The other phases can be depicted as follows (see Table 1).

## 3 Anonymity versus pseudonymity

Anonymity refers to the state of being completely nameless, with no attached identifiers. Pseudonymity involves the use of a fictitious name that can be consistently linked to a particular user, though not necessarily to the real identity [6]. Both provide a layer of privacy, shielding the user's true identity from public view. However, the key difference lies in traceability. While anonymous actions are designed to be unlinkable to any one individual, pseudonymous actions can be traced back to a certain entity.

We want to stress that the true anonymity means that the adversary cannot attribute different sessions to users. In other words, it relates to entity-distinguishable, not just identity-revealable. To illustrate the signification, we refer to Fig.1.

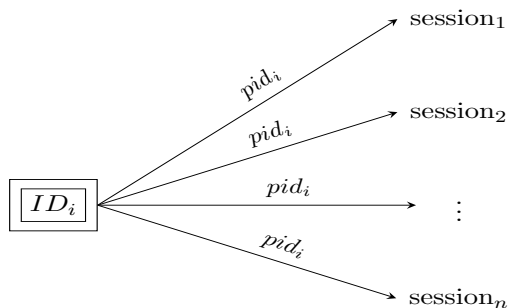


Fig.a: Pseudonymity  
(with the same identifier  $pid_i$ )

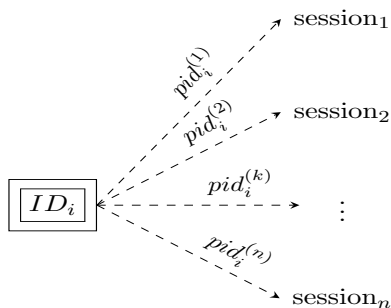


Fig.b: Anonymity  
(with different and irregular identifiers  $pid_i^{(k)}$ )

Figure 1: Pseudonymity versus anonymity

In Fig.a, the server's identity  $ID_i$  uniquely corresponds to the pseudo-identity  $pid_i$ . Thus, different sessions launched by this entity can be attributed to the entity by checking the consistency of  $pid_i$ .

Table 1: The Zhong *et al.*'s authentication and key agreement scheme

Cloud server: $C_i$	Cell phone user: $U$	Login phase	Cloud server: $C_j$
Send the identity $ID_i$ . $\xrightarrow{\substack{ID_i \\ \text{[secure channel]}}}$	Pick $r_i, r_j \in Z_q^*$ , compute $R_i = r_i \cdot P, R_j = r_j \cdot P$ $S_i = \omega^{-1} R_i, S_j = \omega^{-1} R_j$ , $pid_i = E_\omega(r_i, ID_i)$ , $pid_j = E_\omega(r_j, ID_j)$ , $\alpha_i = H_1(pid_i, R_i)$ , $\alpha_j = H_1(pid_j, R_j)$ , $y_i = \omega^{-1} \cdot r_i + \omega \cdot \alpha_i$ , $y_j = \omega^{-1} \cdot r_j + \omega \cdot \alpha_j$ . $\xleftarrow{\substack{pid_i, R_i, y_i, S_i \\ pid_j, R_j, y_j, S_j}}$	Send the identity $ID_j$ . $\xleftarrow{ID_j}$	Check $y_j \cdot P = S_j + \alpha_j \cdot P_{pub}$ . If so, pick $x_j \in Z_q^*$ . Set $X_j = x_j \cdot P$ . Save $\{x_j, y_j, pid_j, R_j, S_j, X_j\}$ . Publish the public key $\{R_j, S_j, X_j\}$ .
Check $y_i \cdot P = S_i + \alpha_i \cdot P_{pub}$ . If so, pick $x_i \in Z_q^*$ . Set $X_i = x_i \cdot P$ . Save $\{x_i, y_i, pid_i, R_i, S_i, X_i\}$ . Publish the public key $\{R_i, S_i, X_i\}$ .	Cloud handshake phase $\xleftarrow{pid_j}$ [open channel] $\xrightarrow{pid_i}$ $\xrightarrow{\gamma_i, A_i, V_i, T_i^1}$ $\xleftarrow{\gamma_j, A_j, V_j, T_j^1}$	Cloud server: $C_j$	Set the timestamp $T_j^1$ . Check the timestamp $T_i^1$ . Compute $\alpha_i = H_1(pid_i, R_i)$ , $\beta_i = H_2(pid_i, A_i, S_i, T_i^1)$ , $R'_i = A_i + \beta_i \cdot X_i + \alpha_i \cdot P_{pub} + S_i, X'_i = \gamma_i \cdot R'_i$ . Check $V_i = H_3(pid_i, pid_j, R_i, R_j, \gamma_i, A_i, X'_i)$ . If so, pick $a_j \in Z_q^*$ , compute $A_j = a_j \cdot P, \beta_j = H_2(pid_j, A_j, S_j, T_j^1)$ , $\gamma_j = x_j \cdot (a_j + x_j \cdot \beta_j + y_j)^{-1} \bmod q$ , $V_j = H_3(pid_i, pid_j, R_i, R_j, \gamma_j, A_j, X_j)$ , $sk_j = H_4(pid_i, pid_j, R_i, R_j, V_i, V_j, x_j \cdot X'_i, T_j^1)$ .
Pick $a_i \in Z_q^*$ . Set the timestamp $T_i^1$ . Compute $A_i = a_i \cdot P$ , $\beta_i = H_2(pid_i, A_i, S_i, T_i^1)$ , $\gamma_i = x_i \cdot (a_i + x_i \cdot \beta_i + y_i)^{-1} \bmod q$ , $V_i = H_3(pid_i, pid_j, R_i, R_j, \gamma_i, A_i, X_i)$ . Check the timestamp $T_j^1$ . Compute $\alpha_j = H_1(pid_j, R_j), \beta_j = H_2(pid_j, A_j, S_j, T_j^1)$ , $R'_j = A_j + \beta_j \cdot X_j + \alpha_j \cdot P_{pub} + S_j, X'_j = \gamma_j \cdot R'_j$ . Check $V_j = H_3(pid_i, pid_j, R_i, R_j, \gamma_j, A_j, X'_j)$ . If so, compute the session key $sk_i = H_4(pid_i, pid_j, R_i, R_j, V_i, V_j, x_i \cdot X'_i, T_j^1)$ .	Cloud server: $C_i$	Cloud server: $C_j$	Set the timestamp $T_j^1$ . Check the timestamp $T_i^1$ . Compute $\alpha_i = H_1(pid_i, R_i)$ , $\beta_i = H_2(pid_i, A_i, S_i, T_i^1)$ , $R'_i = A_i + \beta_i \cdot X_i + \alpha_i \cdot P_{pub} + S_i, X'_i = \gamma_i \cdot R'_i$ . Check $V_i = H_3(pid_i, pid_j, R_i, R_j, \gamma_i, A_i, X'_i)$ . If so, pick $a_j \in Z_q^*$ , compute $A_j = a_j \cdot P, \beta_j = H_2(pid_j, A_j, S_j, T_j^1)$ , $\gamma_j = x_j \cdot (a_j + x_j \cdot \beta_j + y_j)^{-1} \bmod q$ , $V_j = H_3(pid_i, pid_j, R_i, R_j, \gamma_j, A_j, X_j)$ , $sk_j = H_4(pid_i, pid_j, R_i, R_j, V_i, V_j, x_j \cdot X'_i, T_j^1)$ .

In this case, the unique pseudo-identity  $pid_i$  can be eventually used to recognize this entity. But in Fig.b,  $ID_i$  only corresponds to different temporary identities  $pid_i^{(1)}, \dots, pid_i^{(n)}$ . Therefore, the adversary cannot attribute different sessions to the entity, even though these sessions are launched by this entity.

## 4 The Loss of anonymity in Zhong et al.’s scheme

The original argument says that (page 1599, Ref.[16]):

*The two parties participating in the cloud handshakes and interacts with anonymous identities  $pid_i = E_\omega(r_i, ID_i)$  and  $pid_j = E_\omega(r_j, ID_j)$  in the PCAKA protocol. For them, anonymity protects the privacy of their identities when interacting with data on public channels. The adversary can not extract the  $ID_i(ID_j)$  from the  $pid_i(pid_j)$ . Thus, the proposed PCAKA protocol supports cloud anonymity.*

We find the argument is not sound. It simply thinks that anonymity equals to protecting the original identity.

As we see, the identity of a person or thing is the characteristics that distinguish it from others. In the scheme, the real identity  $ID_i$  could be a regular string of some meanings, while the pseudo identity  $pid_i$  is a random string, i.e.,  $pid_i = E_\omega(r_i, ID_i)$ , issued by the cell phone user  $U$  for long-term use. Since a real identity uniquely corresponds to a pseudo-identity, one should prevent both identifiers  $ID_i$  and  $pid_i$  from exposure. But in the scheme the adversary can capture  $pid_i$  via the open channel and attribute sessions to the entity by checking the consistency of the pseudo identifier.

The scheme simply thinks that anonymity is equivalent to protecting the real identity. But the true anonymity means that the adversary cannot attribute different sessions to target entities, which relates to entity-distinguishable, not just identity-revealable.

## 5 Further discussions

The cloud server  $C_i$  needs to publish the public parameters  $R_i, S_i, X_i$ . These parameters will be invoked by other parties. For example, the cloud server  $C_j$  will invoke these public parameters to compute

$$\alpha_i = H_1(pid_i, R_i), \beta_i = H_2(pid_i, A_i, S_i, T_i^1)$$

The parameters are published for long-term use, not just for a single session. So, they can be used to recognize the target entity. To keep anonymity, these parameters should be updated in each session.

The scheme uses four hash functions  $H_1, H_2, H_3, H_4$  with a same codomain  $Z_q^*$ . It suffices to specify a hash function  $H : \{0, 1\}^* \rightarrow Z_q^*$ , in which all input strings are concatenated by the operator “||”. Hence, we have

$$\begin{aligned} \alpha_i &= H(pid_i || R_i), \quad \beta_i = H(pid_i || A_i || S_i || T_i^1) \\ V_i &= H(pid_i || pid_j || R_i || R_j || \gamma_i || A_i || X_i) \\ sk_i &= H(pid_i || pid_j || R_i || R_j || V_i || V_j || x_i \cdot X_j' || T_j^1) \\ sk_j &= H(pid_i || pid_j || R_i || R_j || V_i || V_j || x_j \cdot X_i' || T_j^1) \end{aligned}$$

The simplification can save much cost. Note that in the original computation of  $\beta_i = H_2(pid_i, A_i, S_i, T_i^1)$ , one needs to check  $A_i \in G_q$  and  $S_i \in G_q$ , i.e., both two points belong to the elliptic curve group  $G_q$ . The subtle difference between  $H_2$  and  $H$  is neglected by some researchers.

## 6 Conclusion

We show that the Zhong et al.'s key agreement scheme fails to keep anonymity. We also clarify the signification of anonymity and pseudonymity. The findings in this note could be helpful for the future work on designing such schemes.

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