



Using Earthquake Clustering for Short-Term Forecasting

Dr. Lucile Jones

Standing in for Andy Michael, USGS Seismologist

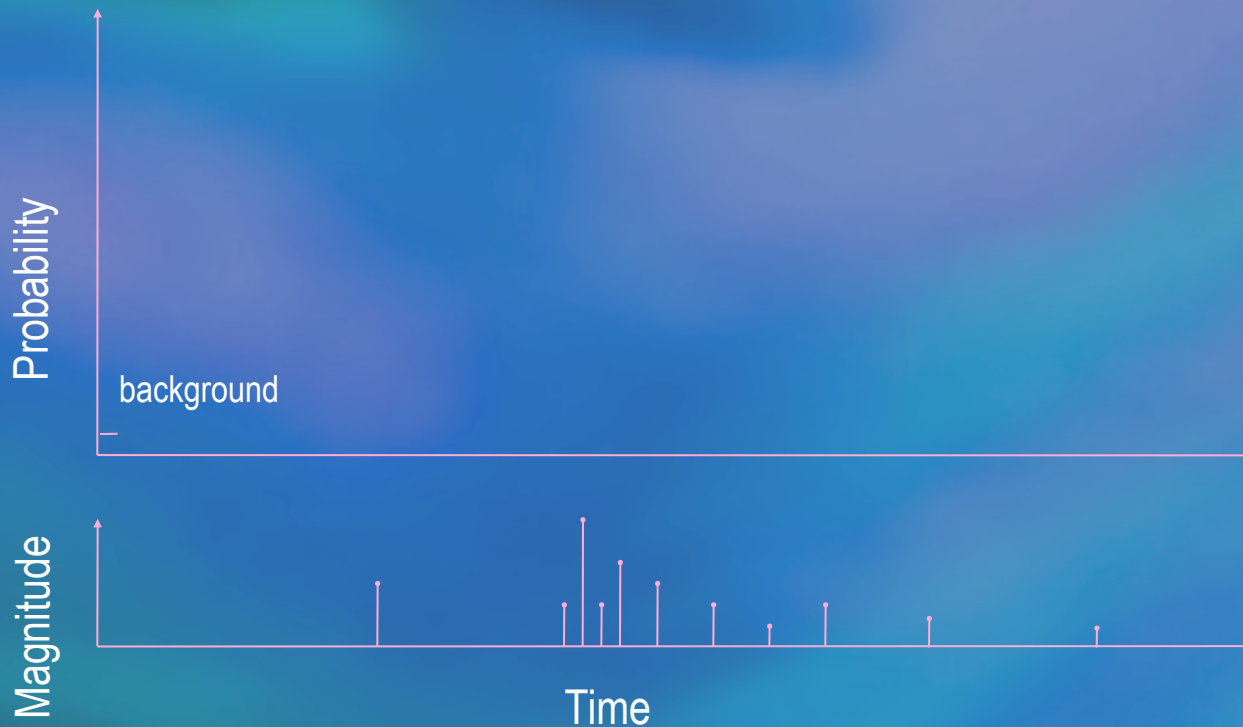
Chief Scientist, Multi Hazards Demonstration Project

U. S. Geological Survey

What is Operational in California?

- Aftershock statistics based on Reasenberg & Jones (1989)
- Automatic updates of STEP aftershock model – probability of earthquake shaking
- Foreshock model (based on Agnew and Jones, 1992) used with discussion after possible foreshocks
- STEP is being tested in CSEP

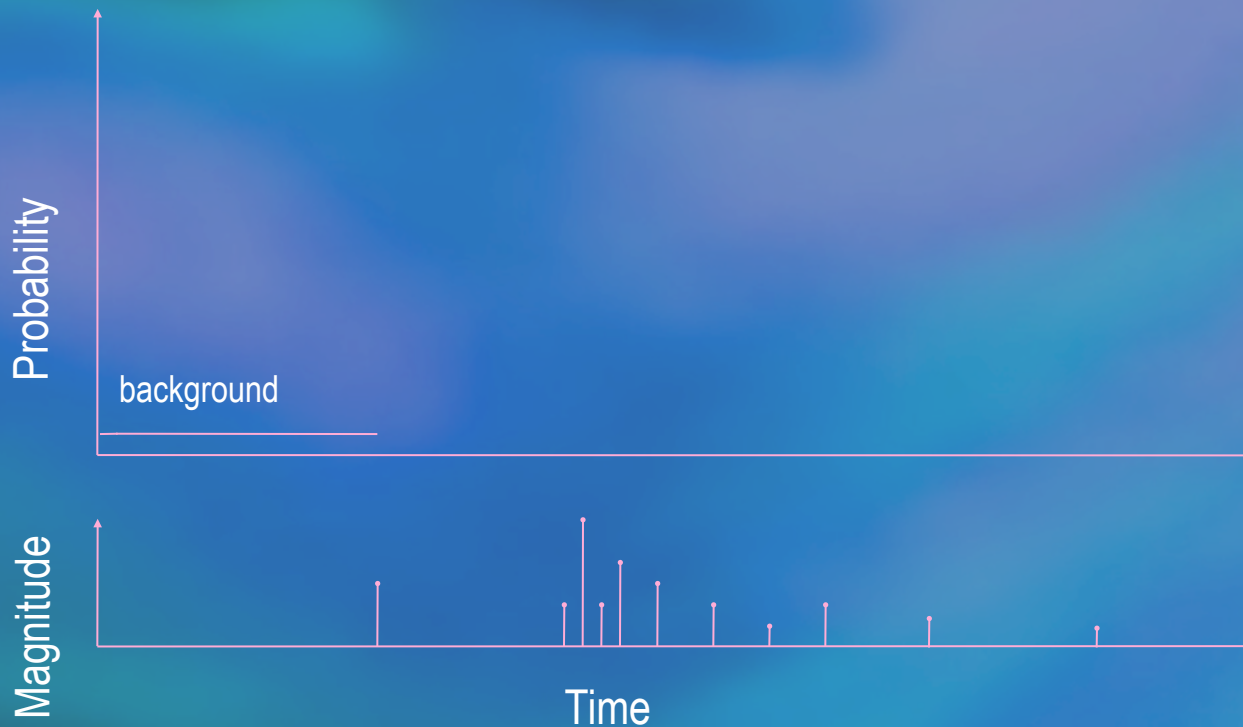
Earthquake Clustering



Aftershocks/Foreshocks > 50% of all events in California



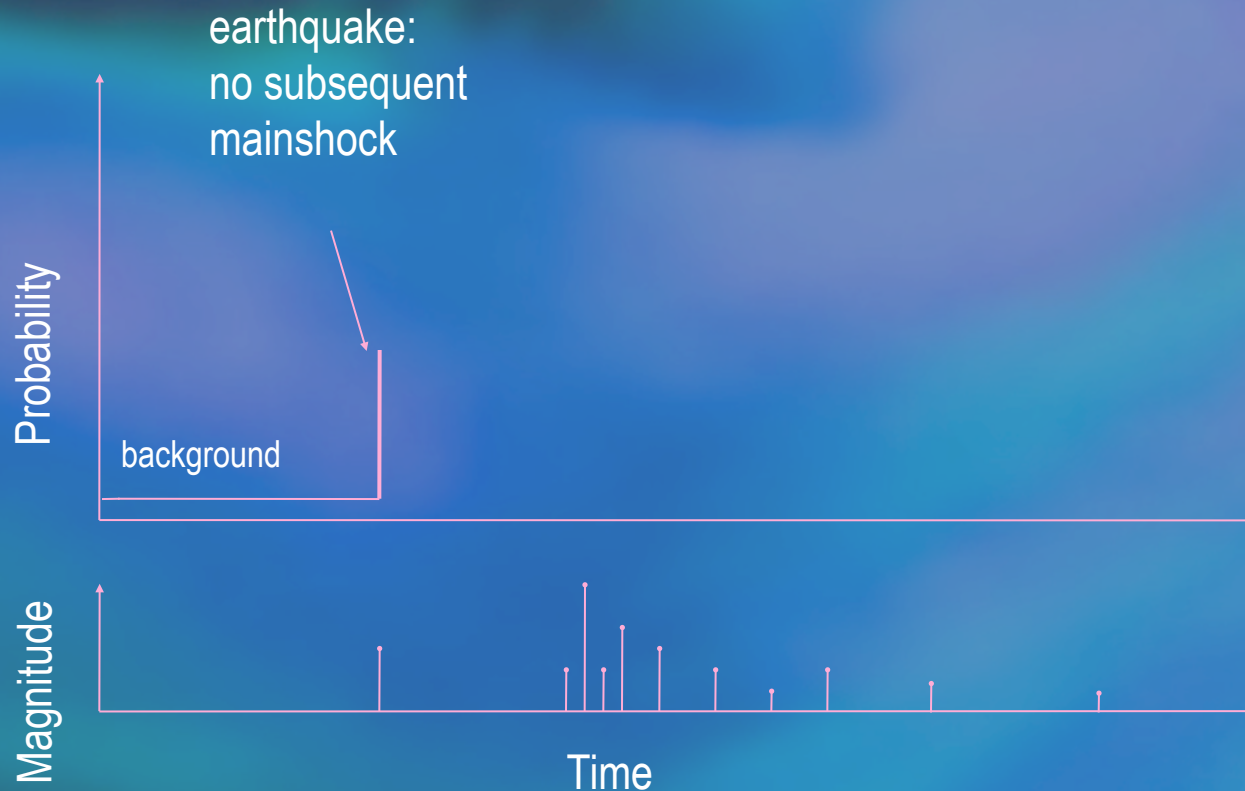
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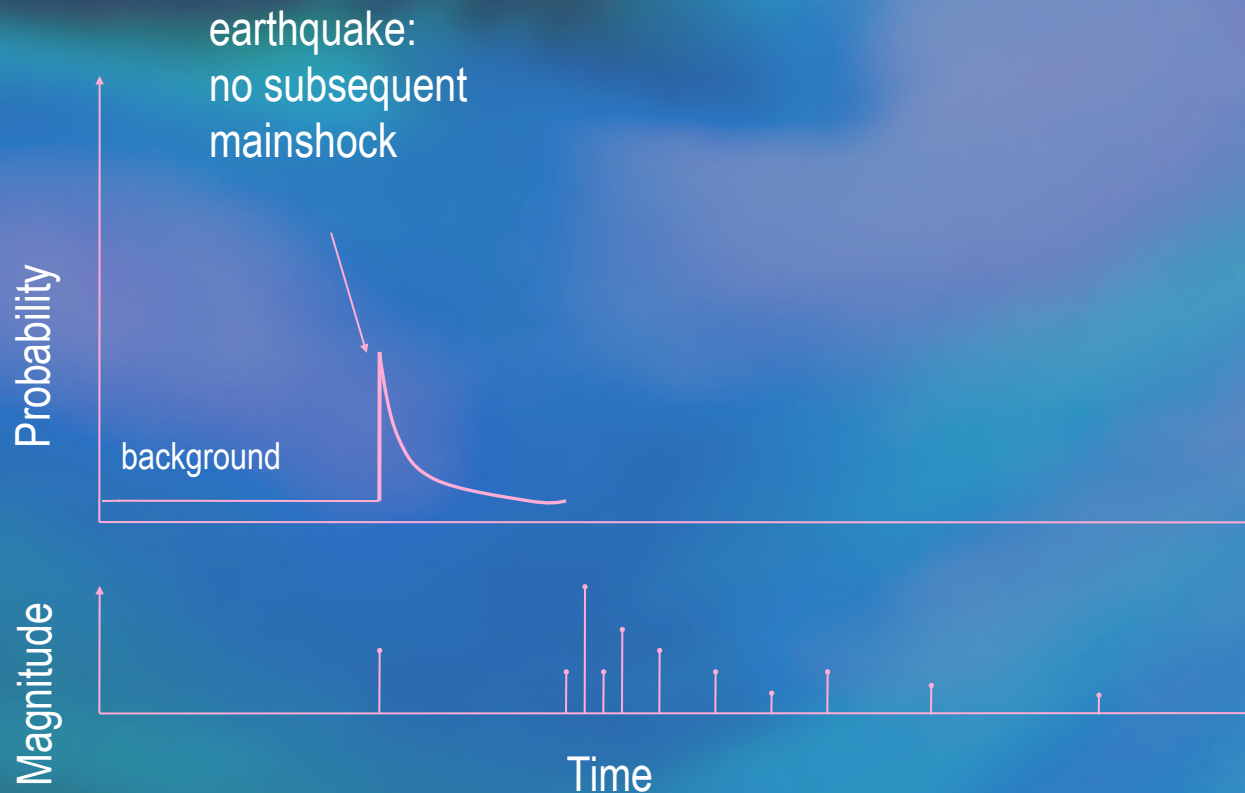
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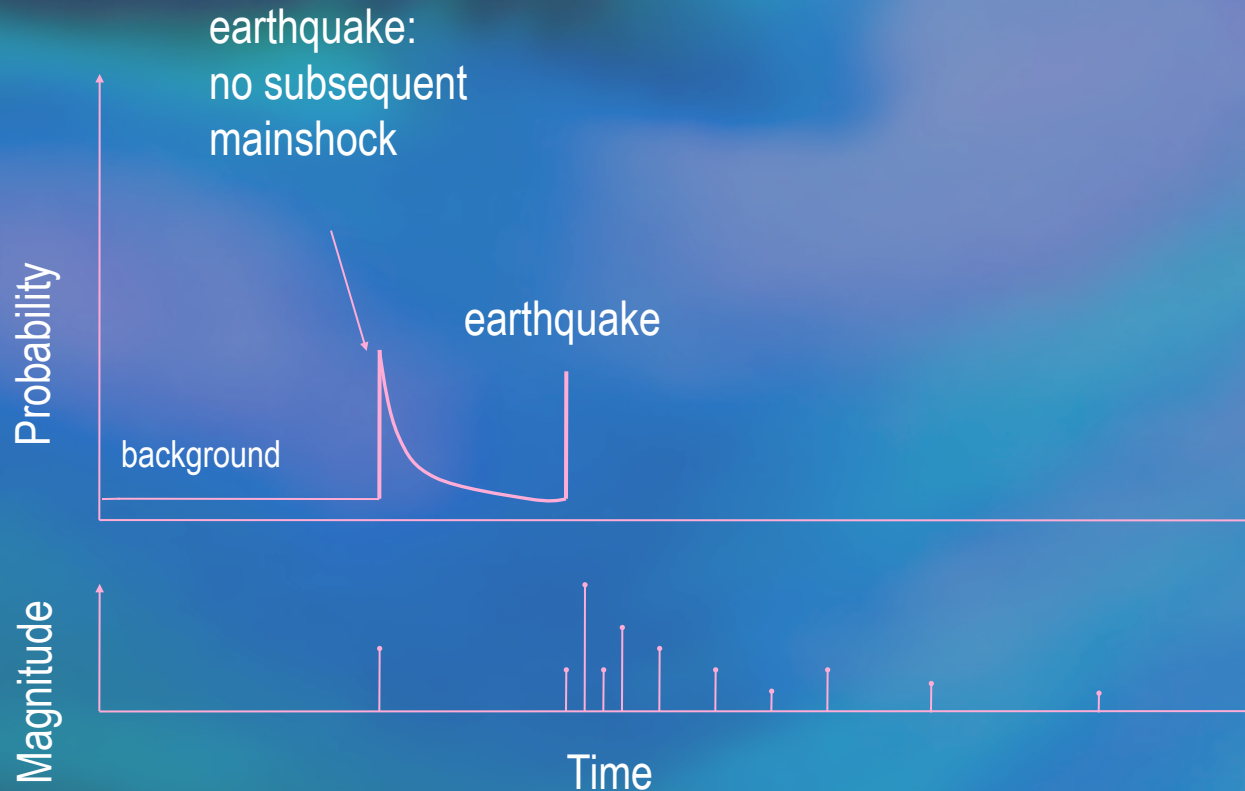
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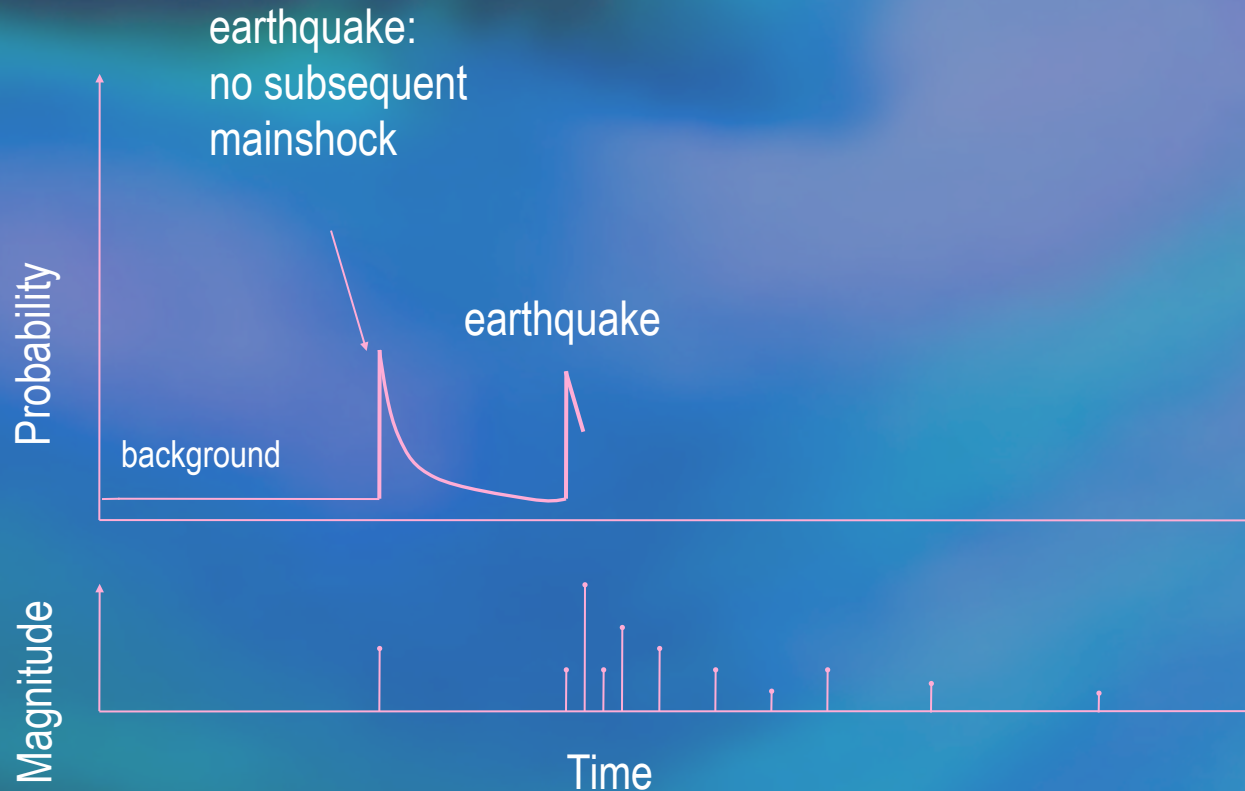
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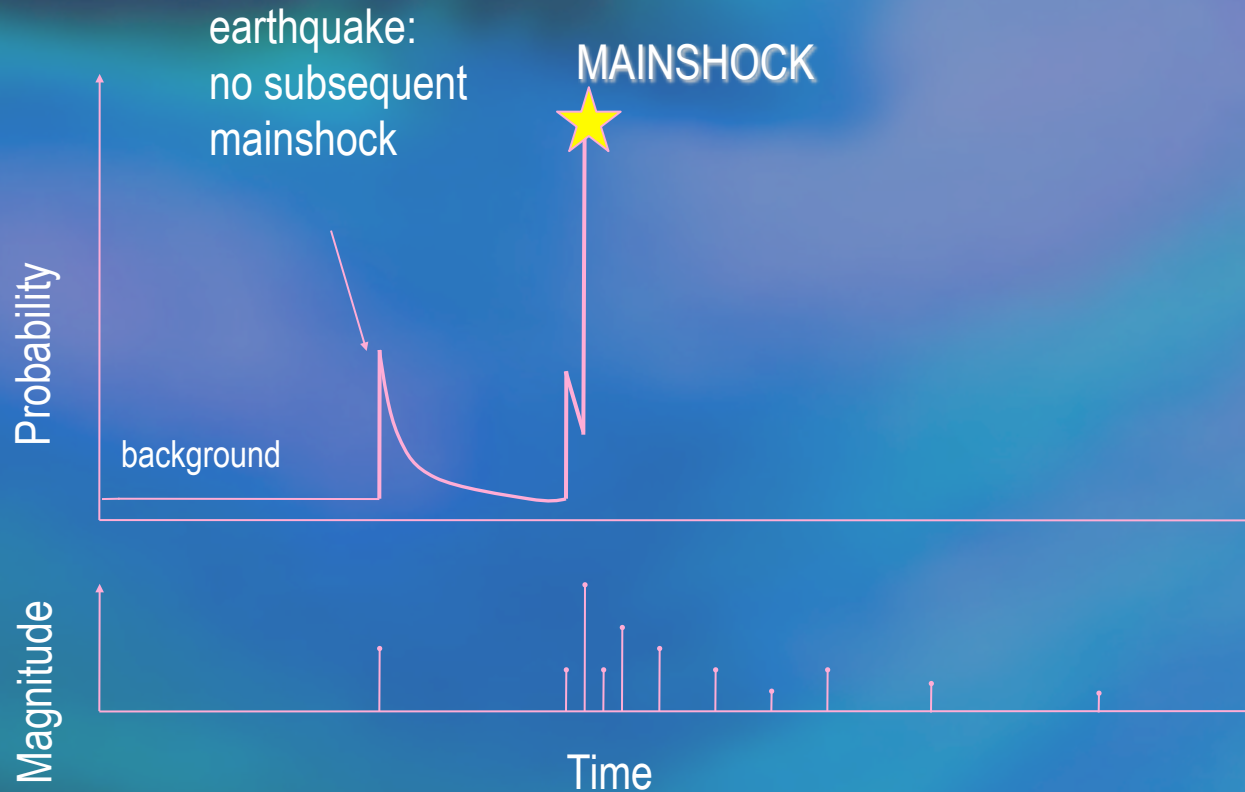
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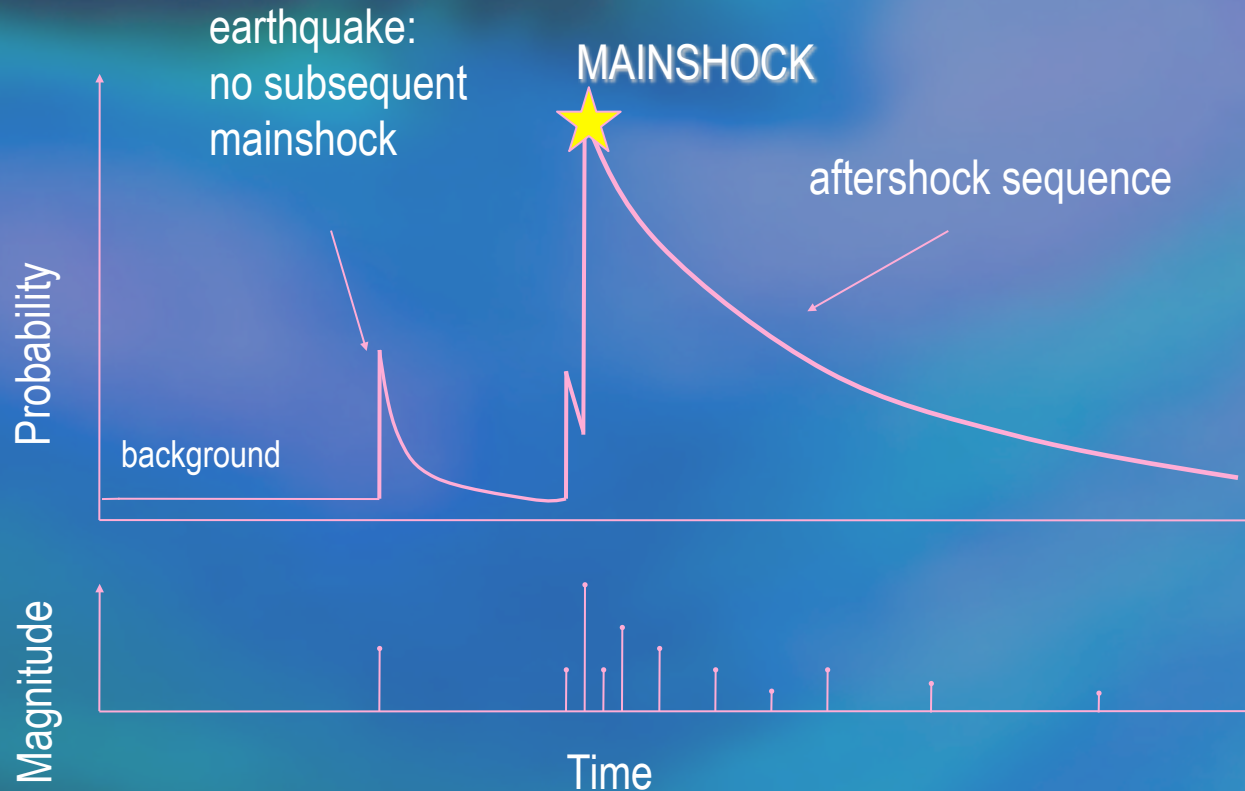
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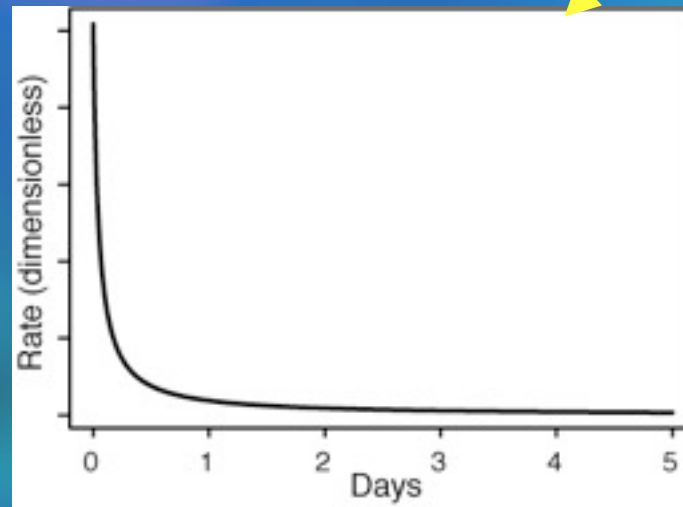
Aftershock probabilities

- Probability determined from Omori's Law and Gutenberg-Richter relation
 - Reasenberg and Jones, 1989
- Rupture forecast, not shaking
- First issued as public statements in 1989

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$$N = f(1/t)$$

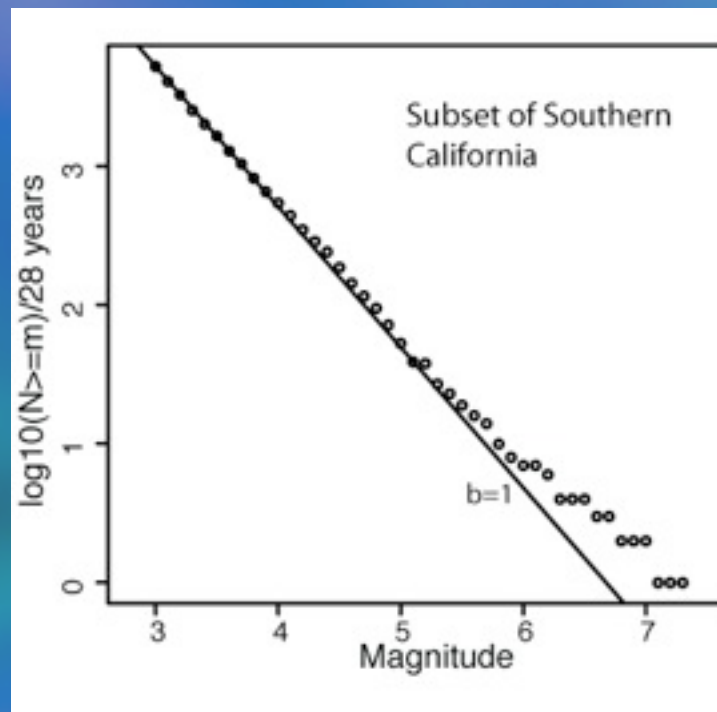


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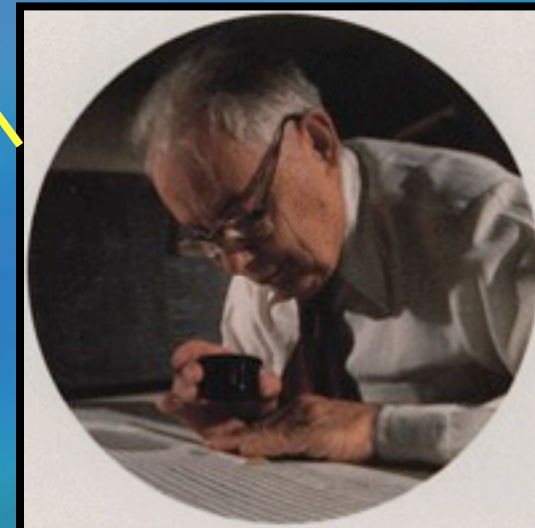
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$$N = f(1/t)$$



$$N = f(10^{-bM})$$



Reasenberg and Jones (1989)

$$\lambda(t, M) = 10^{a' + b(M_i - M)} (t + c)^{-p}$$

$$\lambda(t, M) = k 10^{bM_i} 10^{-bM} (t + c)^{-p}$$

Rate

Overall
Productivity

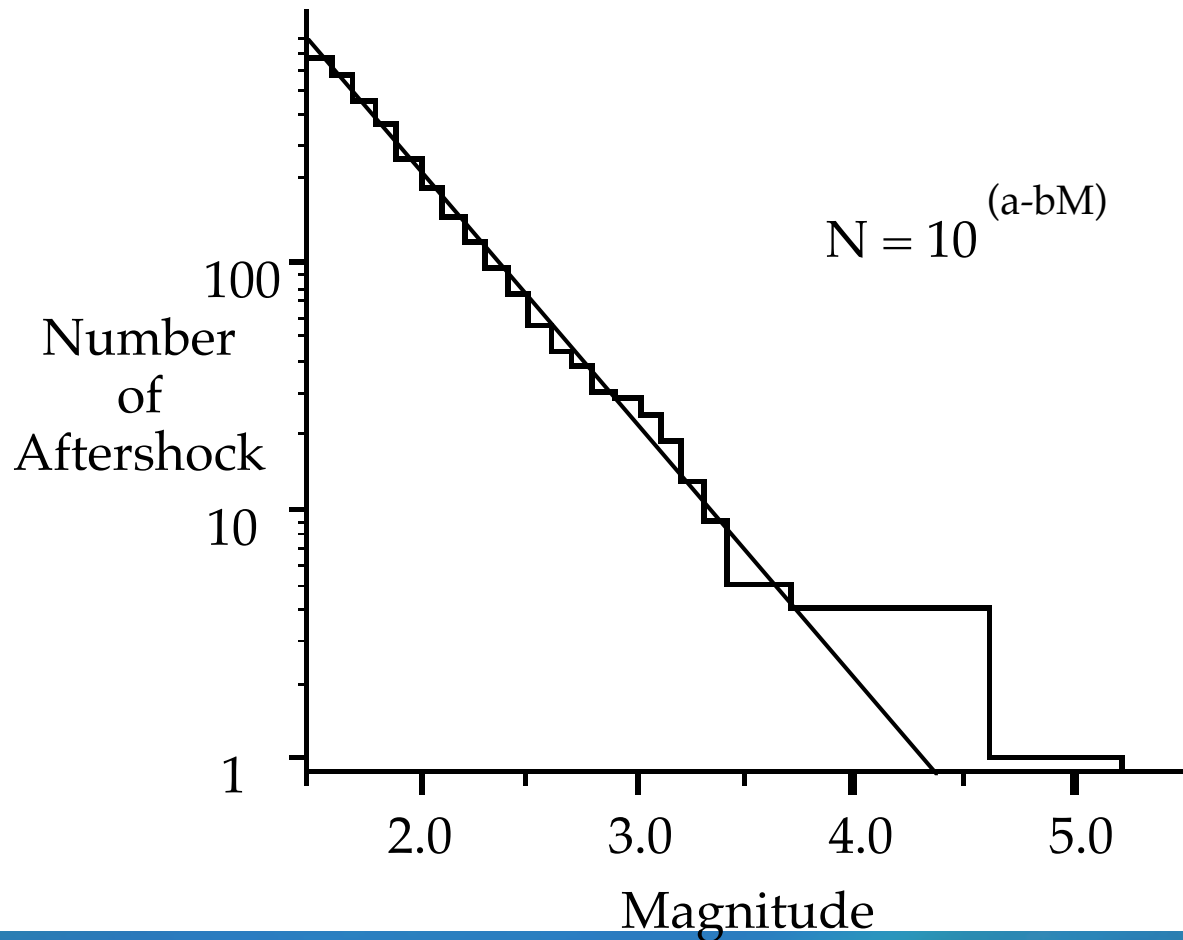
Productivity vs.
Initiating Event
Magnitude

Probability of $m \geq M$
given an Earthquake
 $P(m \geq M | E)$
($M_{min} = 0$)

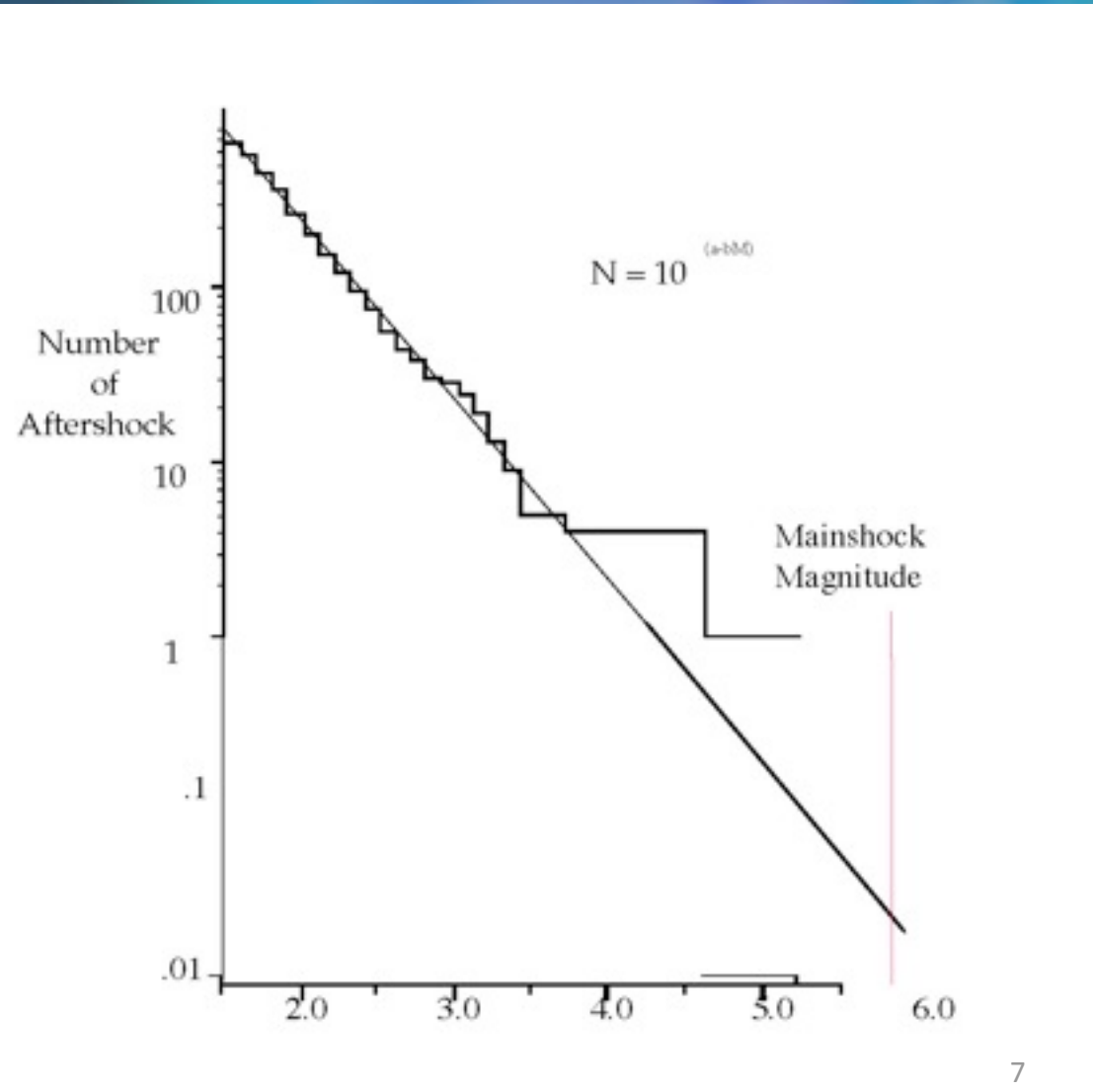
modified-Omori
Decay

Small earthquakes are more common

Each unit smaller
has 10 times
more earthquakes

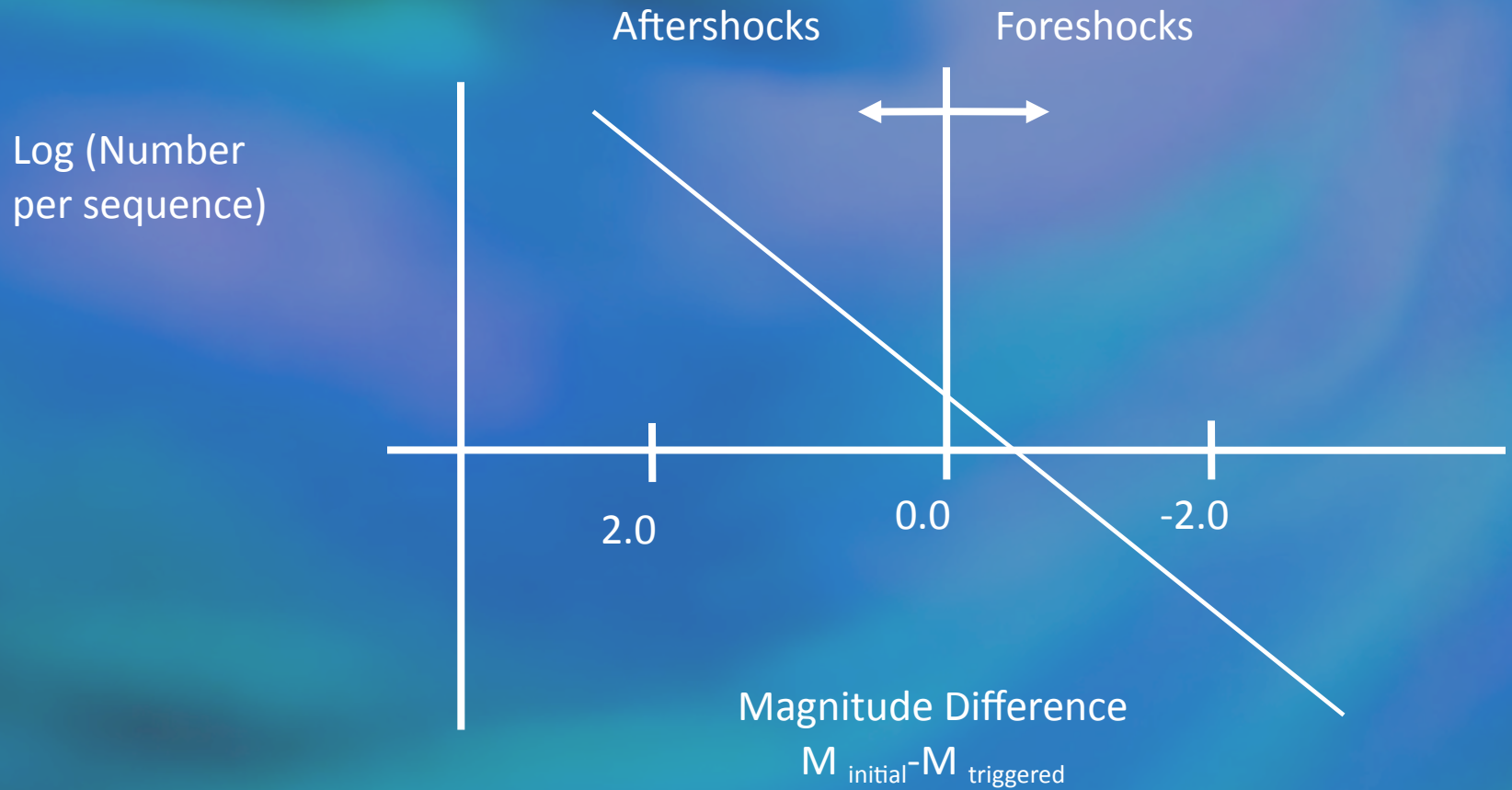


But what if
we look
below $N=1$?



Self-similar Model

Foreshocks as
mainshocks with
large aftershocks

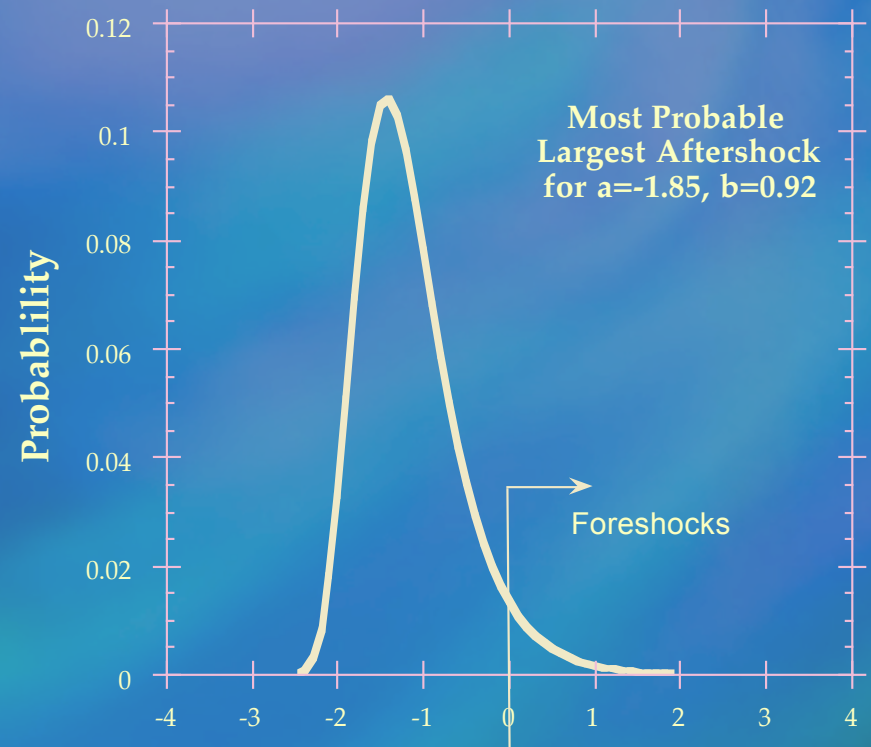


Evidence for Self-similar Model

- Decay of foreshocks
- Magnitude distribution

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- Magnitude distribution

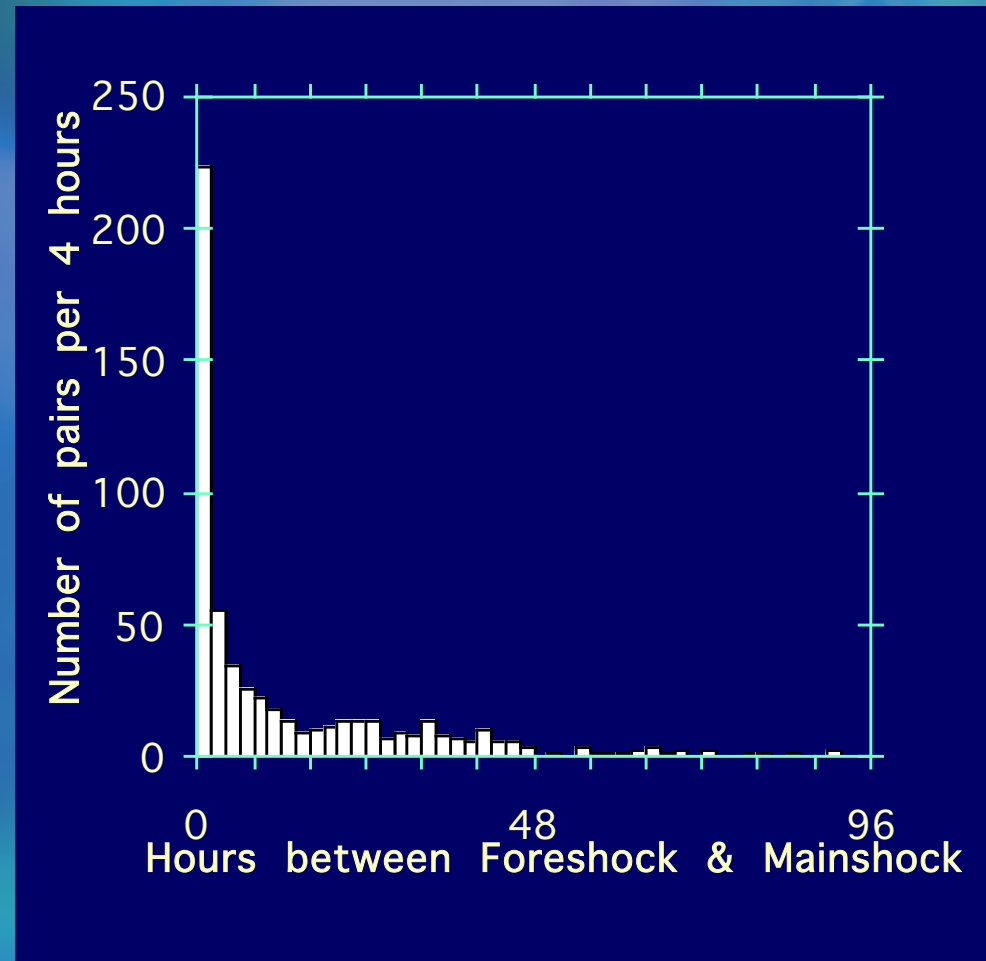


This is exactly what happens

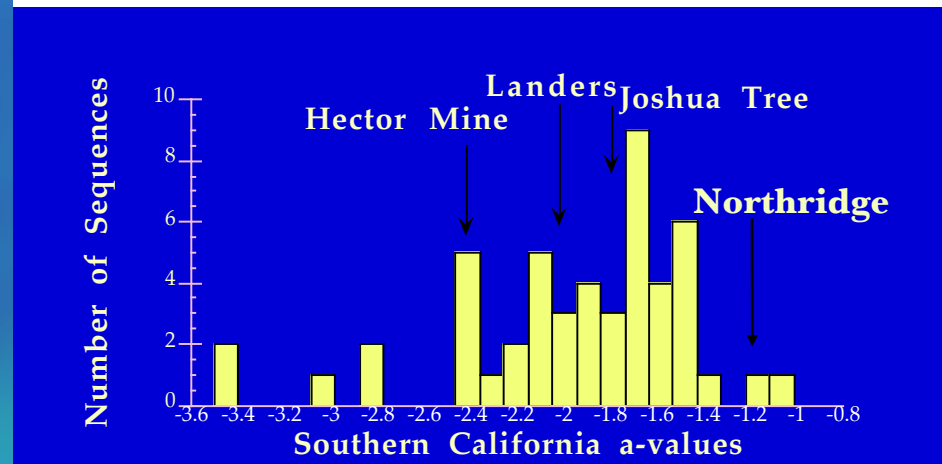
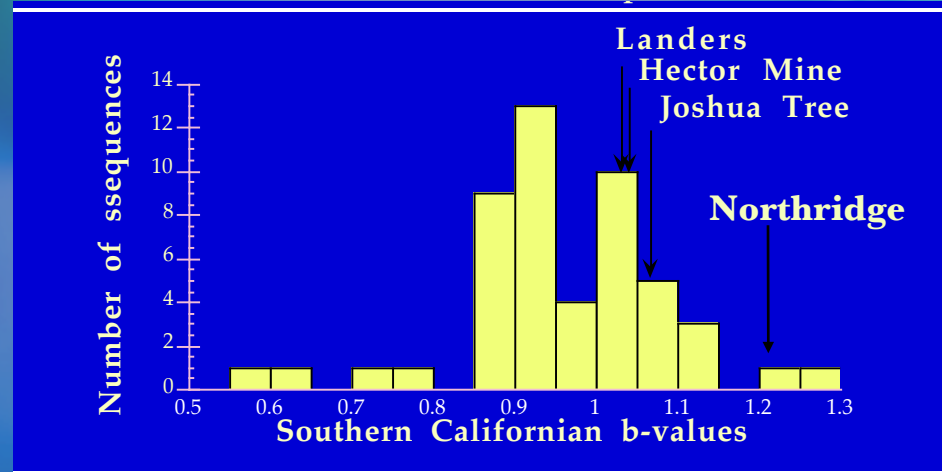
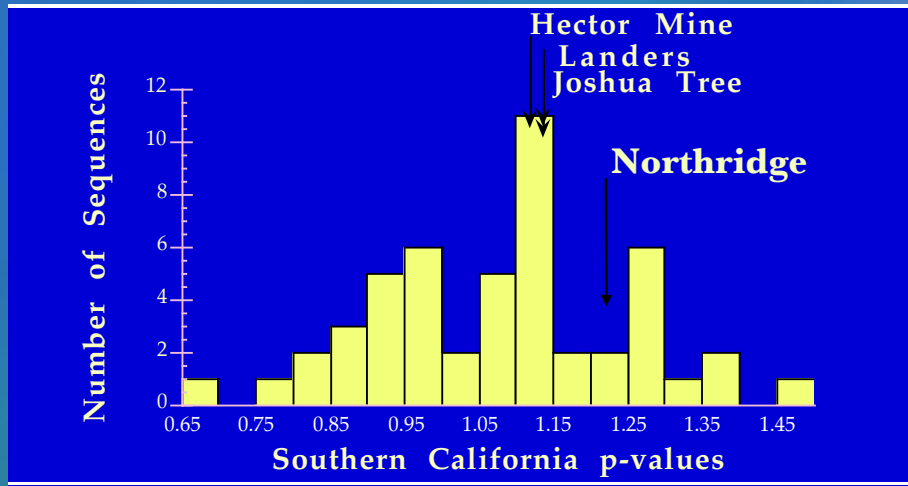
- Rate of mainshocks after foreshocks

=

- Rate of aftershocks after mainshocks



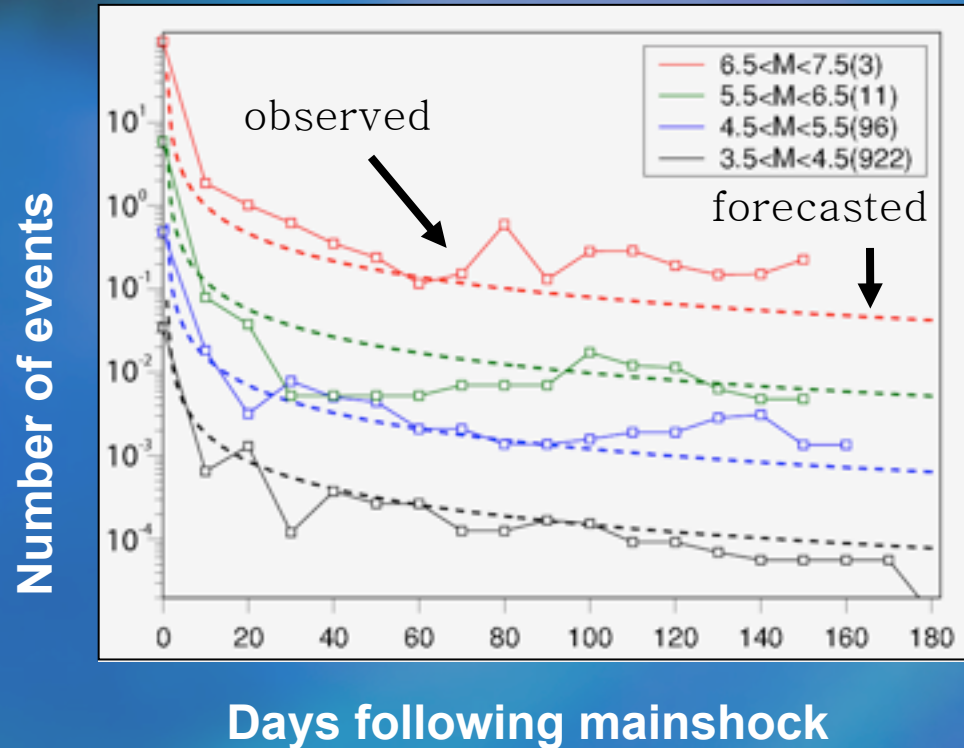
The parameters vary



Generic Aftershock Model

Generic parameters calculated using California aftershock sequences (1932-1987)

Only requires mainshock magnitude as input



California aftershock rates (1988-2003) vs. Generic model



Issued as probability statement

- Predicting events without spatial information
- Time decay not communicated
 - Message on Internet can be days out of date

The screenshot shows a web page from the California Integrated Seismic Network (CISN). At the top, there are logos for CISN, USGS, OES, Caltech, and UC Berkeley. The main heading is "09/29/2004 AFTERSHOCK PROBABILITIES". On the left side, there is a navigation menu with links for Home, Earthquake Info, News & Updates, Products & Services, Who We Are, Calendar, Links & Resources, and Contact Us. The main content area includes the following information:

Published on Thu Sep 30 11:45:10 2004 PDT

Southern California Seismic Network: a cooperative project of U.S. Geological Survey, Pasadena, California
Caltech Seismological Laboratory, Pasadena, California

Version 1: This report supersedes any earlier probability reports about this event.

MAINSHOCK

Magnitude	: 5.0 M1
Time	: 29 Sep 2004 03:54:53 PM PDT
	: 29 Sep 2004 22:54:53 UTC
Coordinates	: 35 deg. 23.31 min. N, 118 deg. 37.24 min. W
	: 17 mi. (27 km) NE of Arvin, CA
	: 21 mi. (34 km) E of Bakersfield, CA
Event ID	: 14095628

STRONG AFTERSHOCKS (Magnitude 5 and larger) -

At this time (17 hours after the mainshock) the probability of a strong and possibly damaging aftershock IN THE NEXT 7 DAYS is less than 10 PERCENT.

EARTHQUAKES LARGER THAN THE MAINSHOCK -

Most likely, the recent mainshock will be the largest in the sequence. However, there is a small chance (APPROXIMATELY 5 TO 10 PERCENT) of an earthquake equal to or larger than this mainshock in the next 7 days.

WEAK AFTERSHOCKS (Magnitude 3 to 5) -

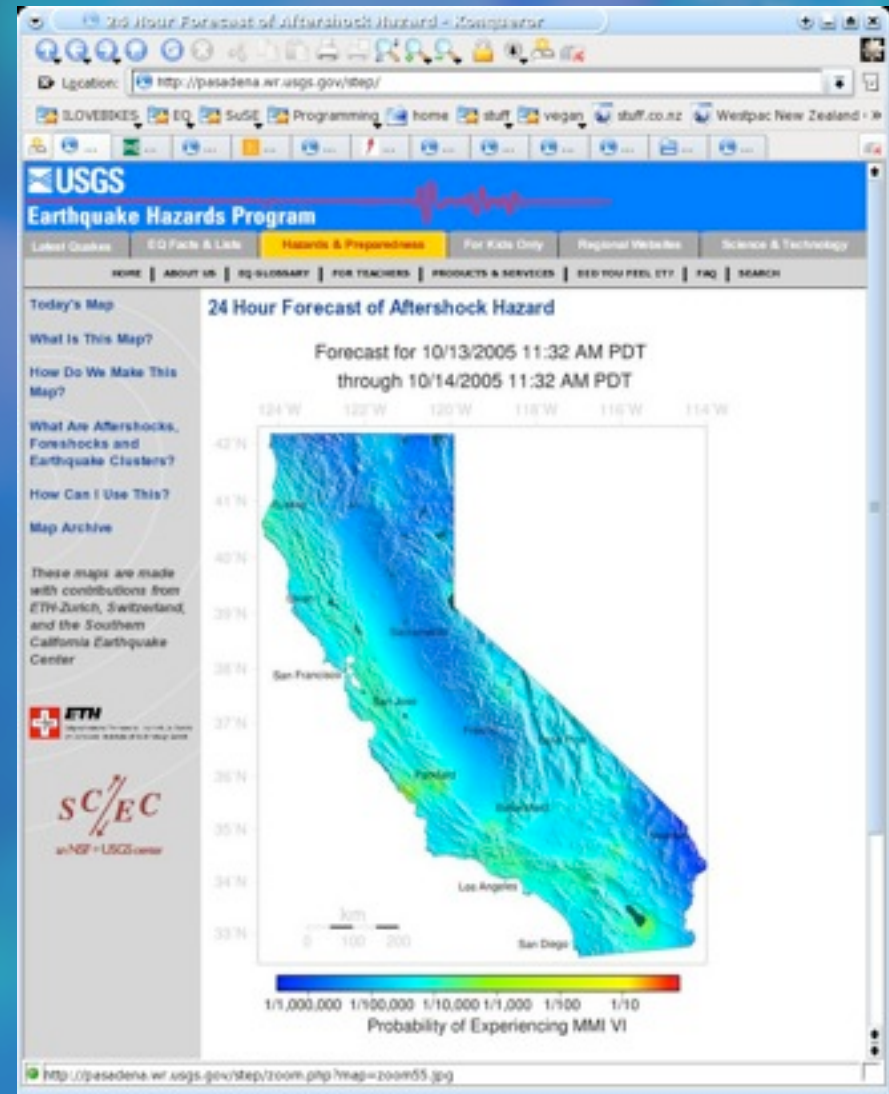
In addition, up to approximately 10 SMALL AFTERSHOCKS are expected in the same 7-DAY PERIOD and may be felt locally.

This probability report is based on the statistics of aftershocks typical for California. This is not an exact prediction, but only a rough guide to expected aftershock activity. This probability report may be revised as more information becomes available.



Short Term Earthquake Probabilities (STEP)

- 24 hour forecast
- probability of exceeding MMI VI
- automatic calculations
- online
- real-time
- updated every half-hour

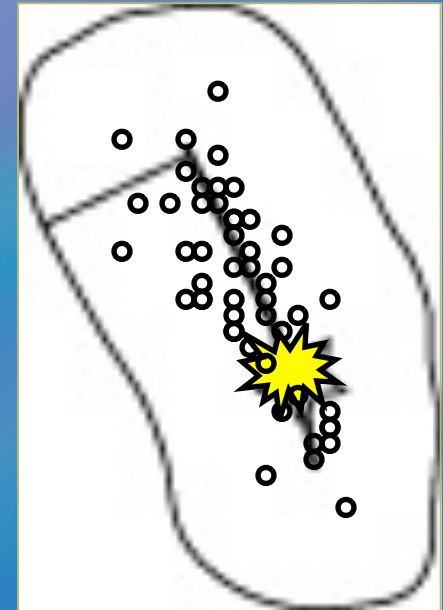
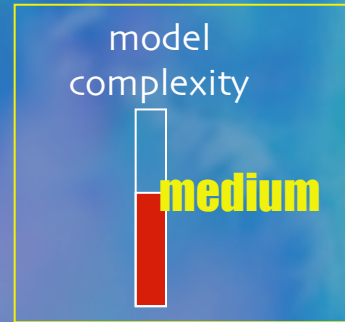


The Aftershock Models

Sequence Specific Model

**needs minimum of 100 aftershocks
before estimating parameters**

**One set of model parameters
(Gutenberg-Richter and modified Omori
laws) calculated for the entire
aftershock sequence**



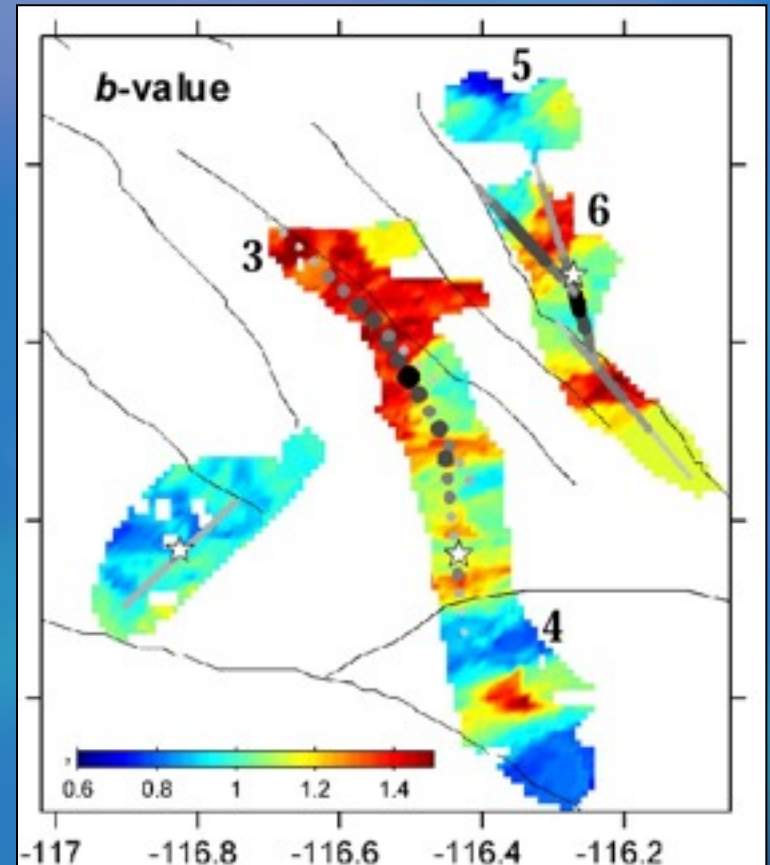
The aftershock zone

The Aftershock Models

Spatially Varying Model



Gutenberg-Richter and modified Omori law parameters are mapped at 5km spacing

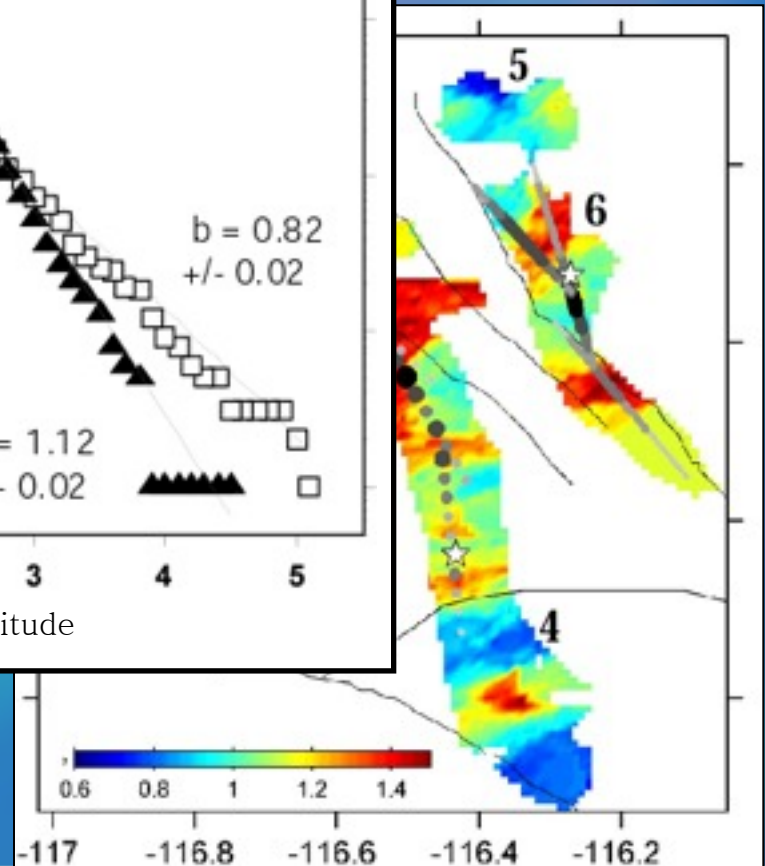
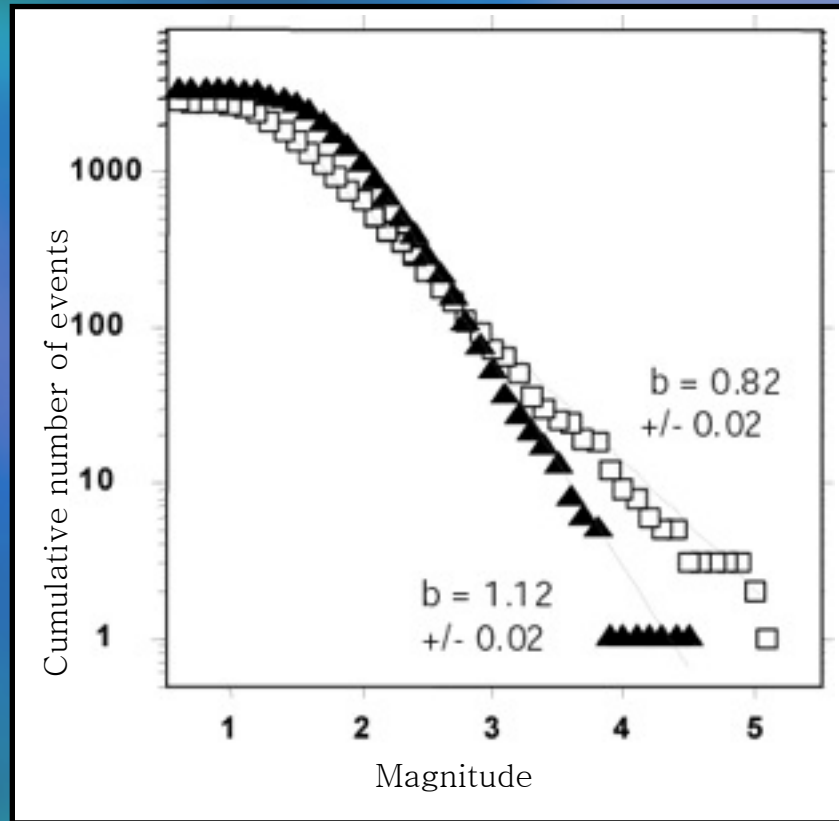


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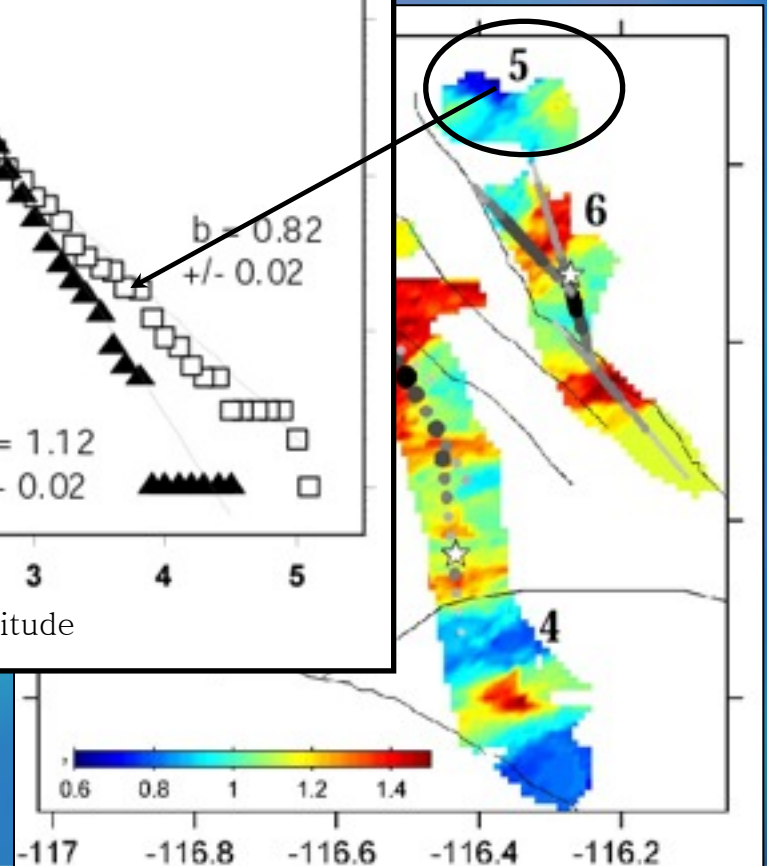
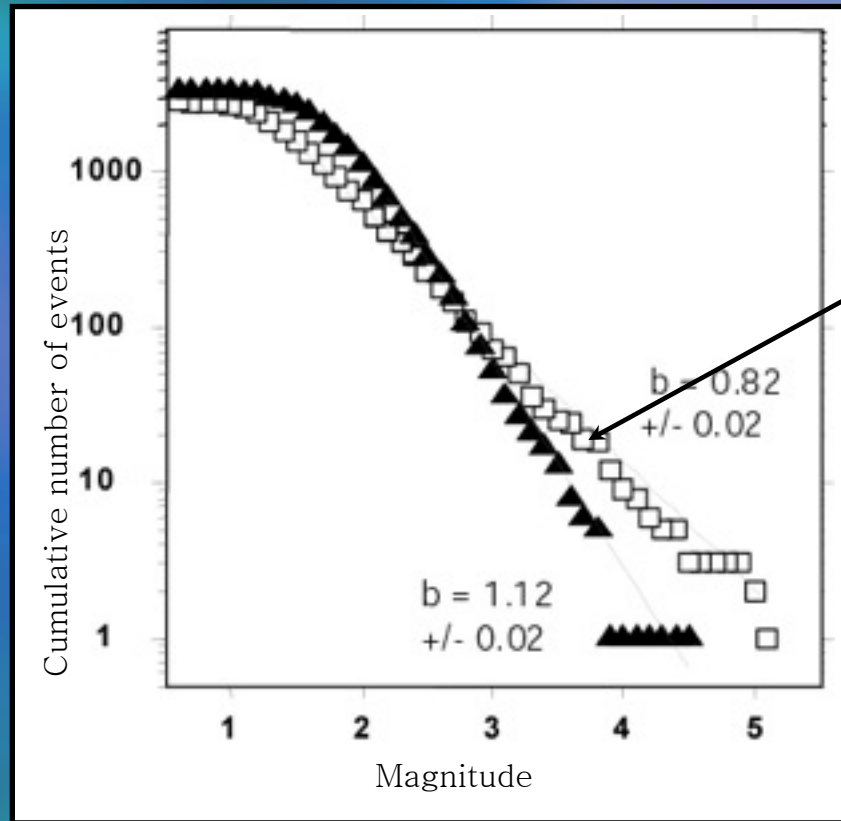
model complexity
highest



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Spatially Varying Model

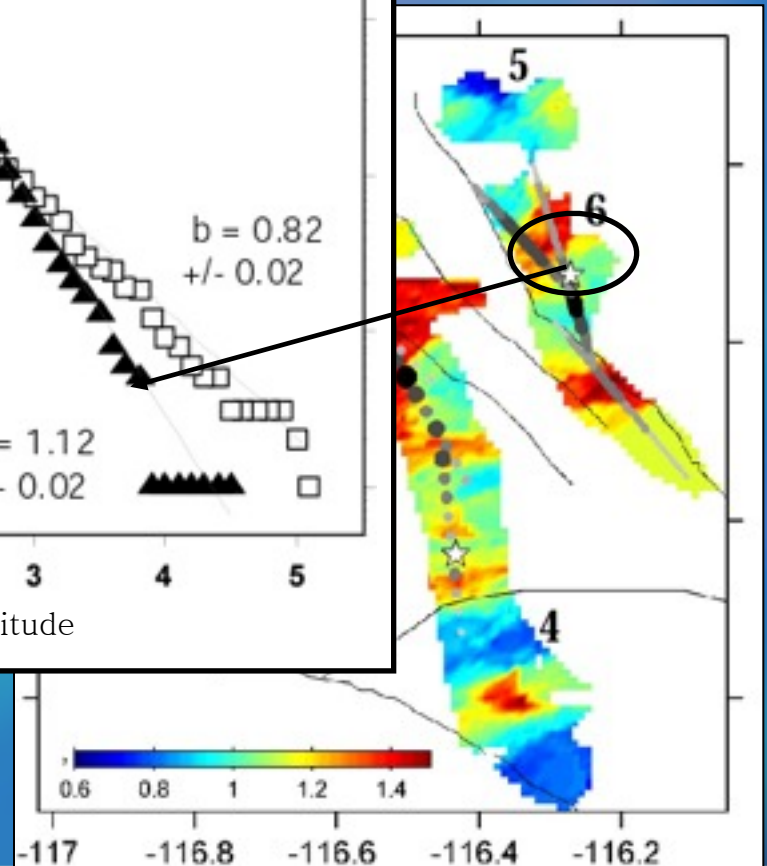
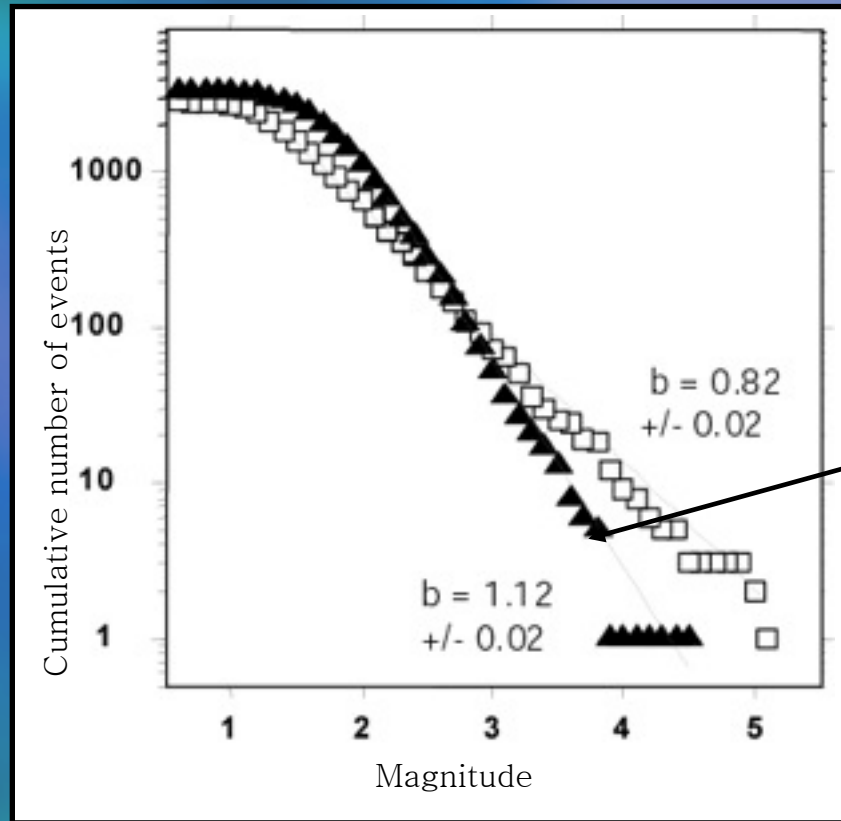
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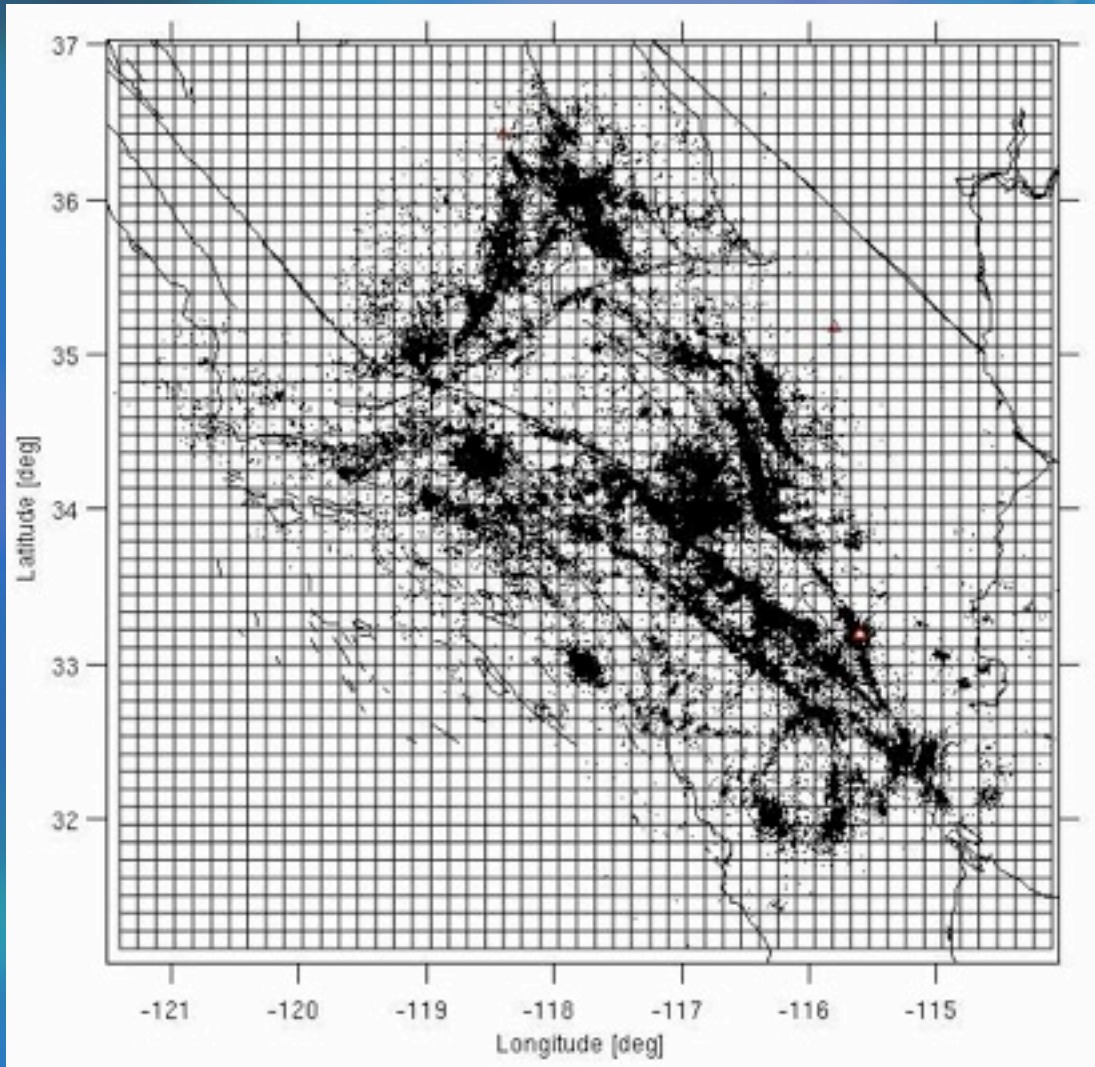
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Our forecasts are consistent with actual earthquakes



Should we say the same thing after every event?

Agnew and Jones, JGR, 1991:

“But it ought to be possible to do better:

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“But it ought to be possible to do better:

the probability of a very large earthquake should be higher if the candidate foreshock were to occur near a fault capable of producing that mainshock than if it were located in an area where we believe such a mainshock to be unlikely.

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“But it ought to be possible to do better:

the probability of a very large earthquake should be higher if the candidate foreshock were to occur near a fault capable of producing that mainshock than if it were located in an area where we believe such a mainshock to be unlikely.

Moreover, the chance of a candidate earthquake actually being a foreshock should be higher if the rate of background (nonforeshock) activity were low.”

After discarding aftershocks,
earthquakes are divided into three categories for statistical purposes:

Mainshocks: which we want to forecast

Foreshocks: which are always followed by mainshocks

Background Events: which are never followed by mainshocks

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$$PF = \frac{\text{Rate of } \mathbf{Foreshocks}}{\text{Rate of } \mathbf{Foreshocks} + \text{Rate of } \mathbf{Background Events}}$$

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$$\text{Rate of } \mathbf{Foreshocks} = \text{Rate of } \mathbf{Mainshocks} * \text{Probability of } \mathbf{Foreshocks} \text{ Before } \mathbf{Mainshocks}$$



Seemingly good behavior

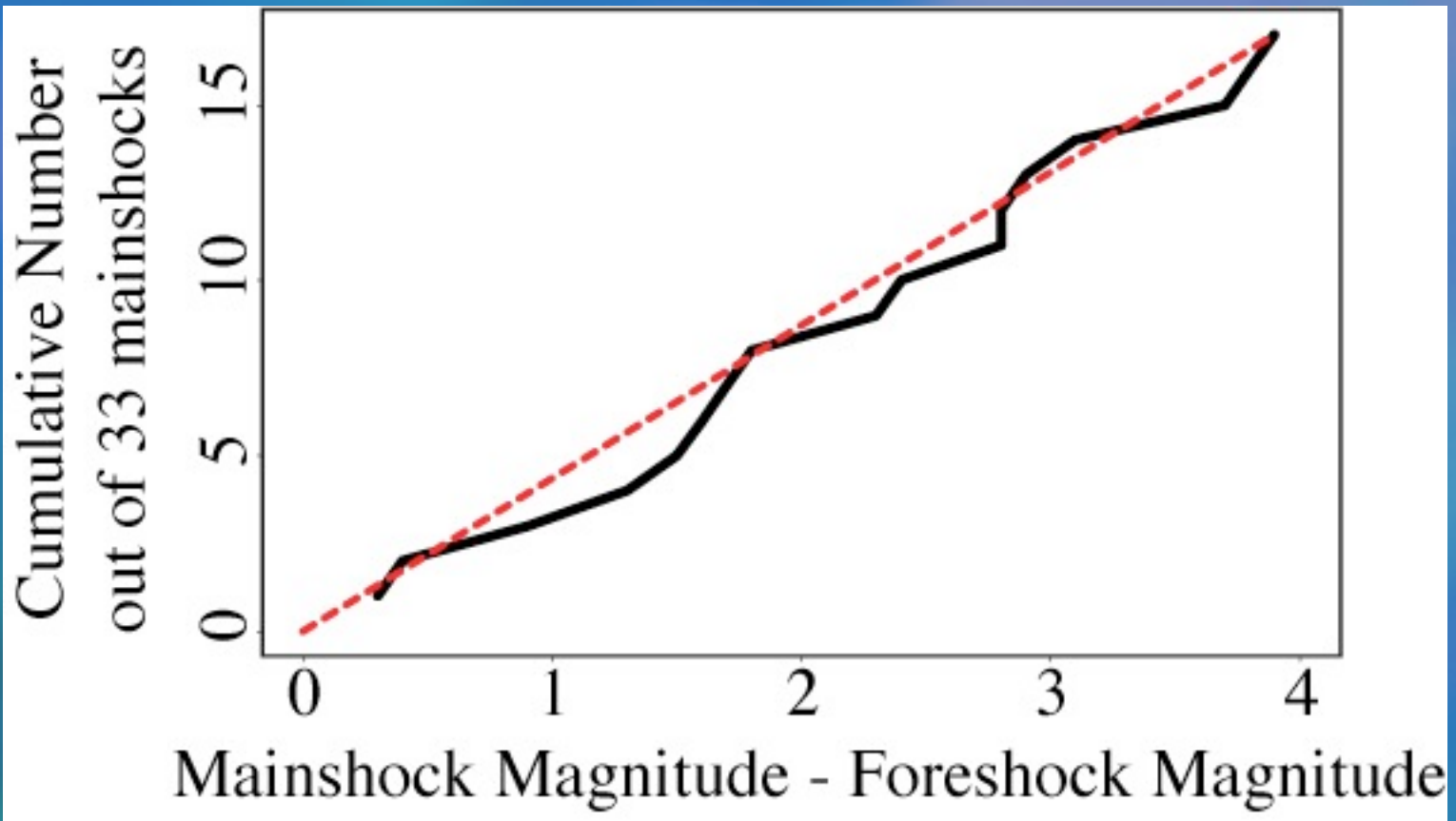
$$PF = \frac{\text{Rate of Mainshocks} * \text{Prob of Foreshocks} | \text{Mainshock}}{(\text{Rate of Mainshocks} * \text{Prob of Foreshocks} | \text{Mainshock} + \text{Rate of Background Events})}$$

The resulting probability goes

- up with higher mainshock rate and
- down with higher background rate.

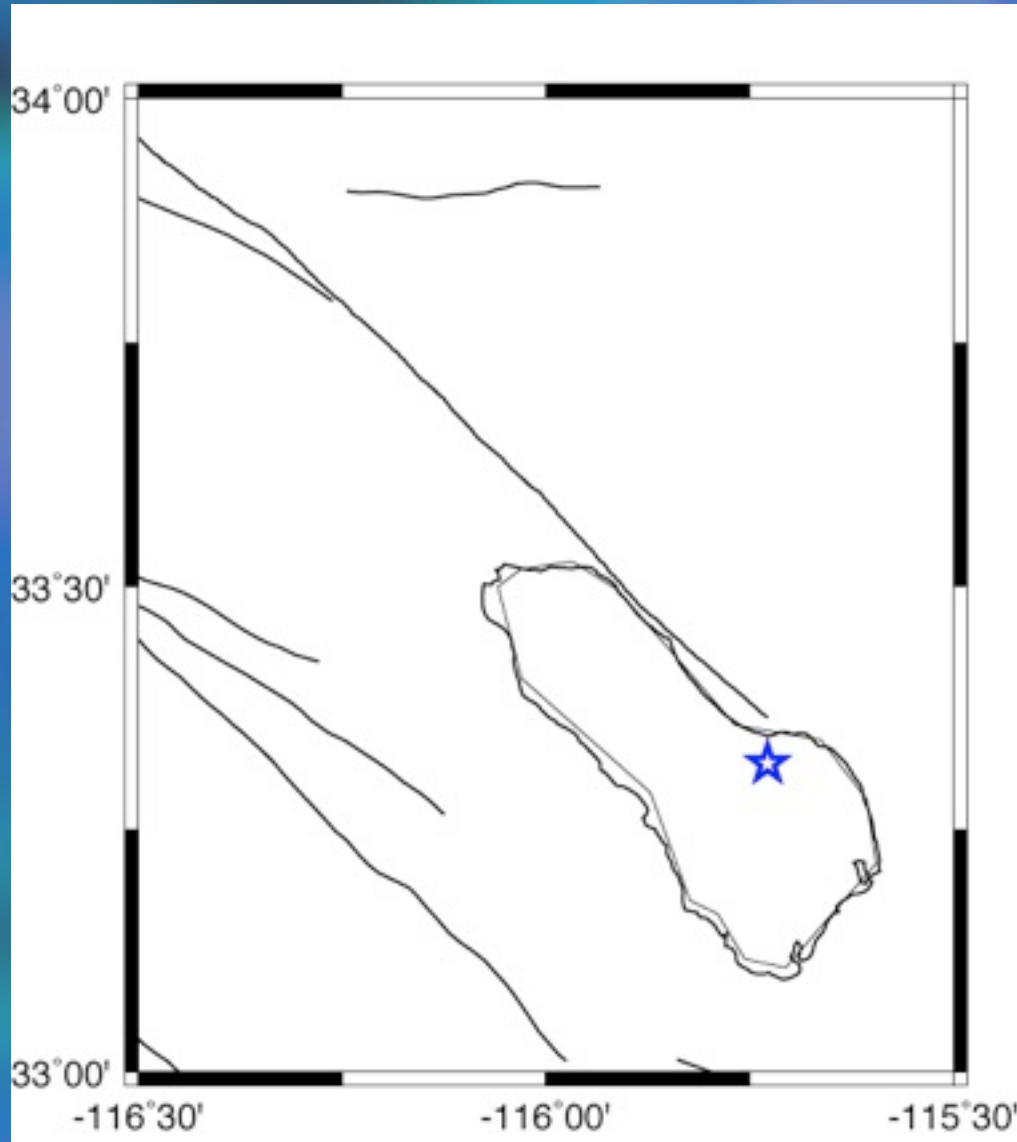
The rate at which mainshocks are preceded by foreshocks:
50% of San Andreas stress province $M \geq 5$ mainshocks
have an $M \geq 2$ foreshock within 3 days, and 10 km.

(Jones, 1984; Michael & Jones, 1998).



M4.8 Event At Bombay Beach On March 24, 2009

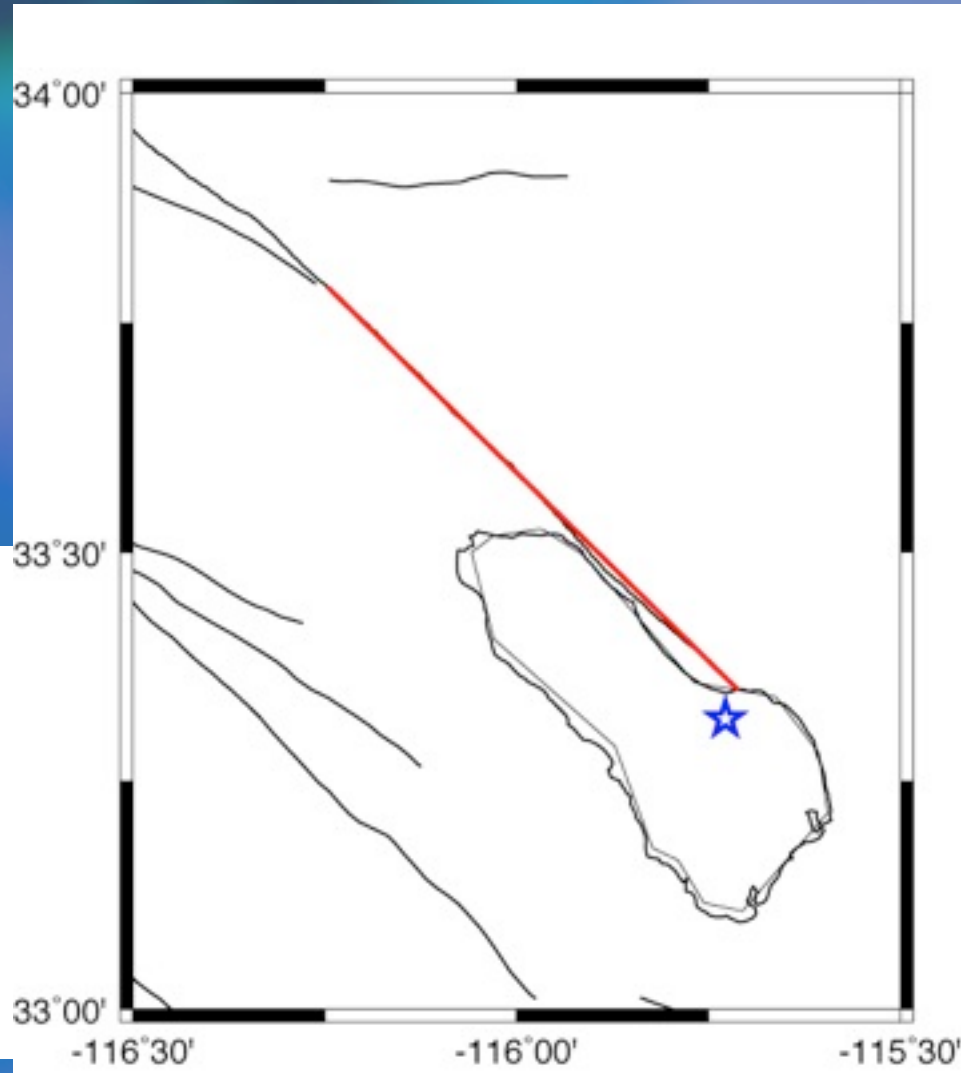
Could It Be A Foreshock To A Larger Earthquake In The Next 3 Days?



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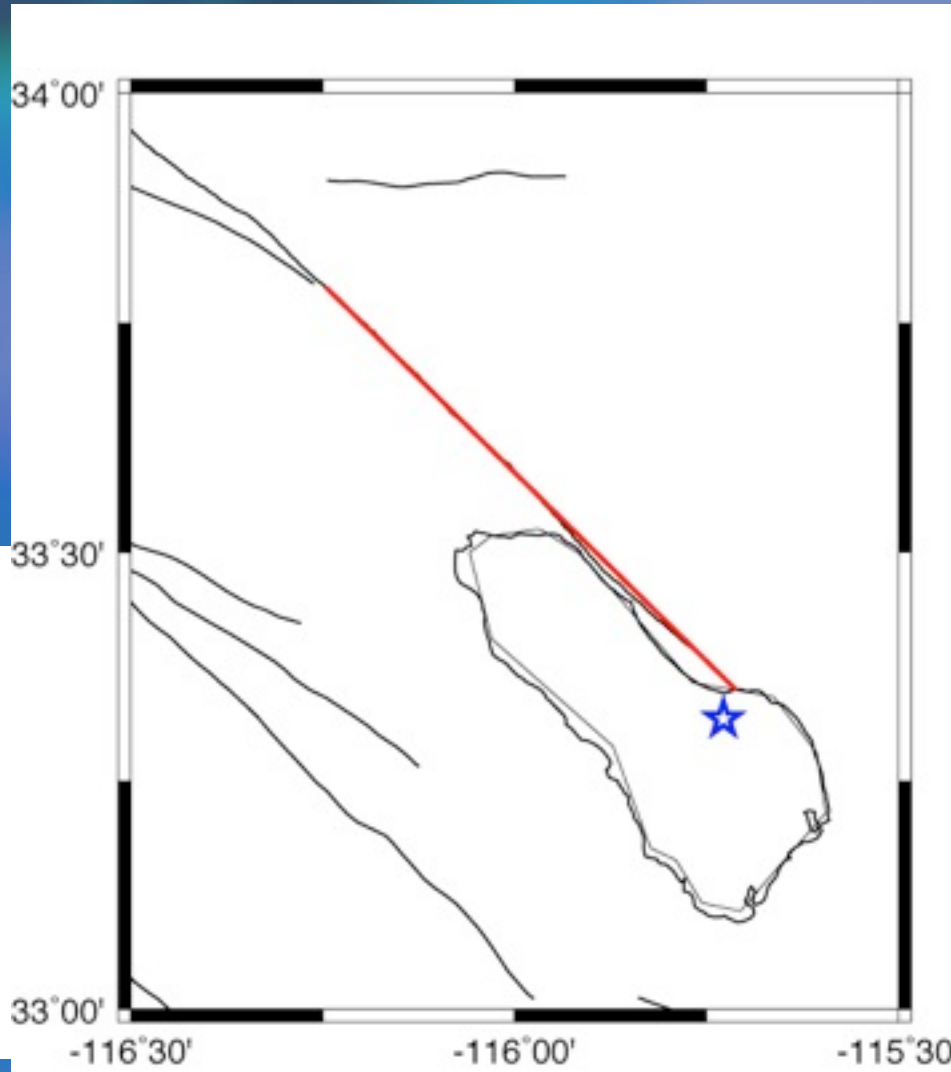
Mainshock:
SAF, Coachella Seg.
UCERF2:
Length = 69 km
M 7
5-yr Prob. = 5%
3-day Prob. = 0.009%



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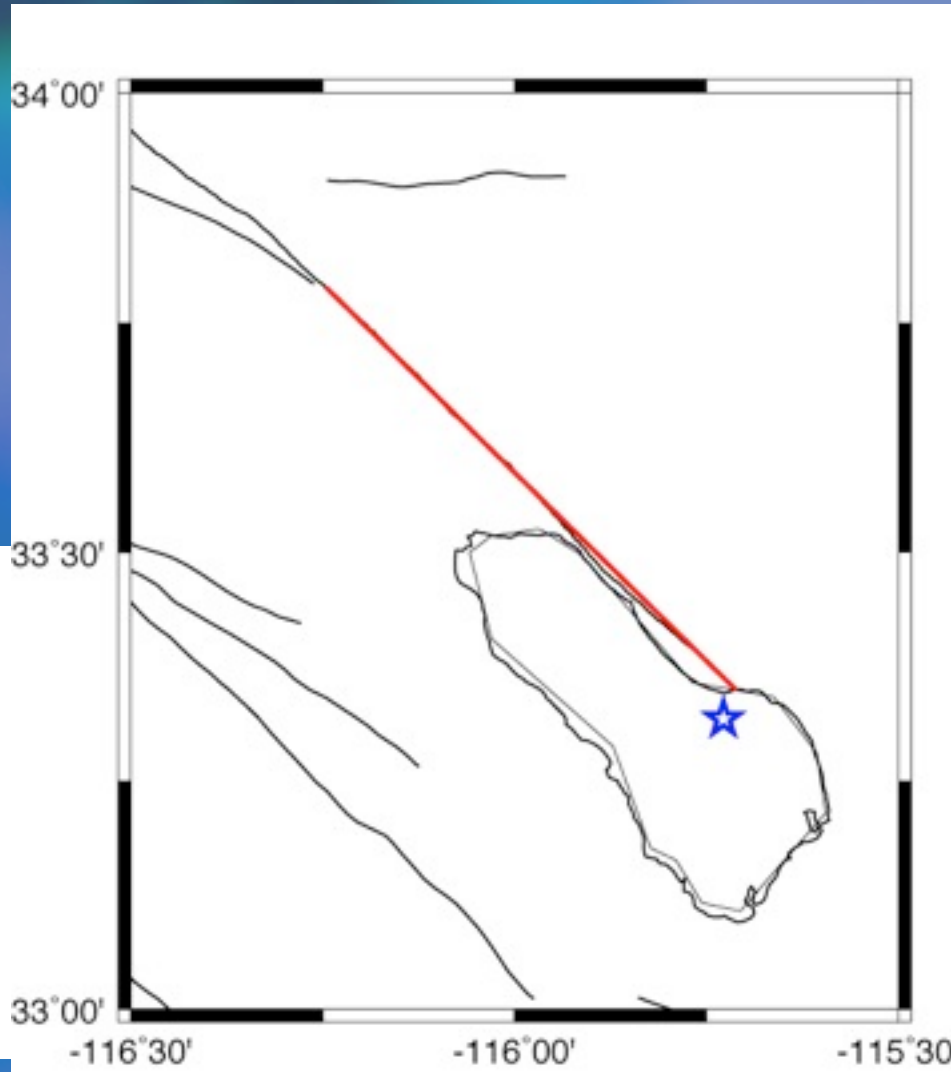
Reasenber &
Jones, 1989:
Probability
of M4.8 being
followed by
an $M \geq 7$ event
PF = 0.05%



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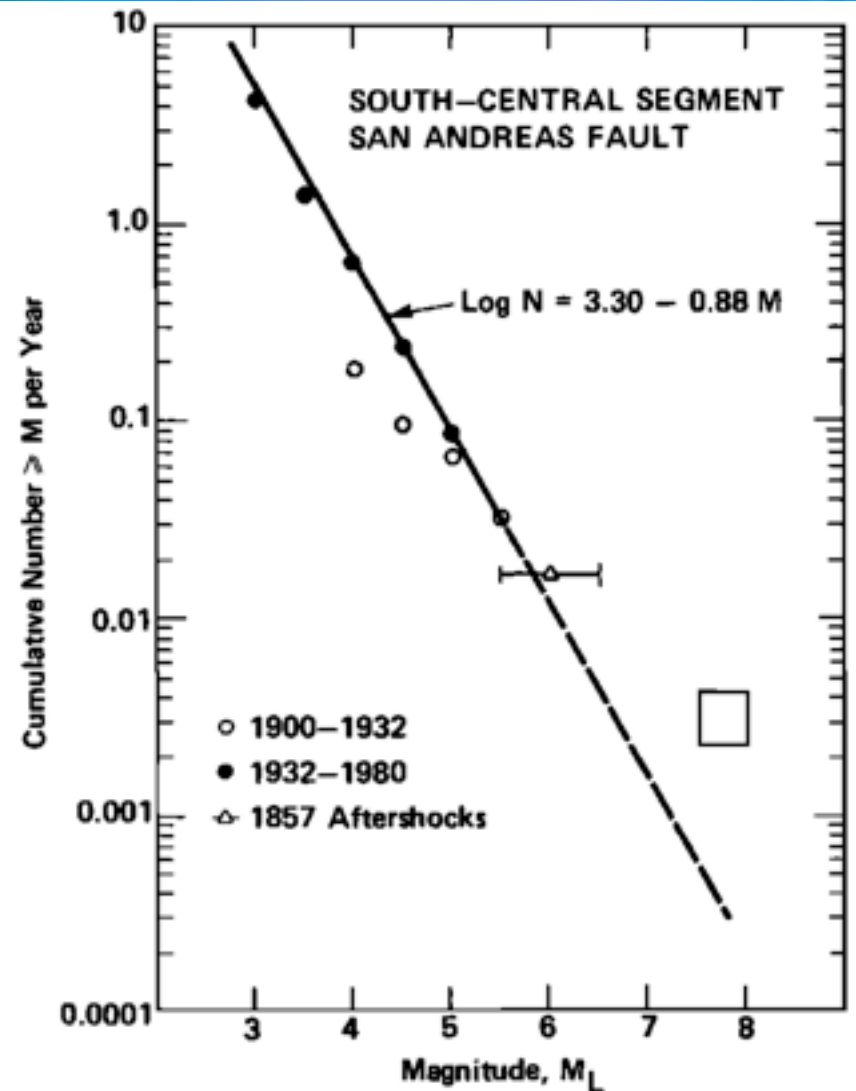
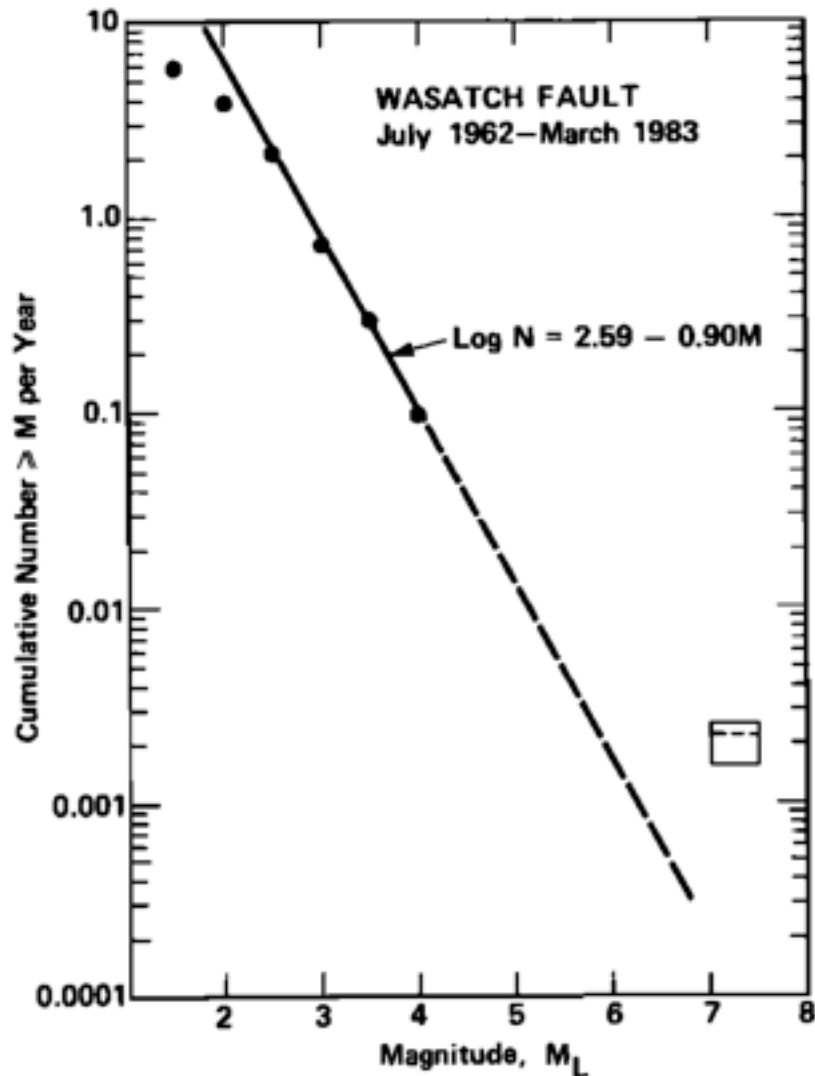


Reasenberg &
Jones, 1989:
Probability
of M4.8 being
followed by
an $M \geq 7$ event
PF = 0.05%

Agnew and
Jones, 1991:
PF = 4%

Fault Behavior and Characteristic Earthquakes: Examples From the Wasatch and San Andreas Fault Zones

DAVID P. SCHWARTZ AND KEVIN J. COPPERSMITH



Gutenberg-Richter + Characteristic Earthquake Relationships – Michael 2010

$$N(m \geq M) = 10^{a-bM} + DH(M_c - M)$$

Rate of
Characteristic
Earthquake

Heaviside
Function

Magnitude of
Characteristic
Earthquake

Gutenberg-Richter + Characteristic Earthquake Relationships – Michael 2010

$$N(m \geq M) = 10^{a-bM} + DH(M_c - M)$$

Rate of
Characteristic
Earthquake

Heaviside
Function

Magnitude of
Characteristic
Earthquake

$$P(m \geq M | E) = \frac{10^{a-bM} + DH(M_c - M)}{10^{a-bM_{\min}} + D}$$



Approximate the Probability of an $M \geq M_c$ event
following an $M = M_i$ event

assuming:

rate of $M=0$ events $10^a \gg D$ the rate of M_c events

rate of M_i events $10^{a-bM_i} \gg D$ the rate of M_c events

$D \gg 10^{a-bM_c}$ the Gutenberg-Richter rate of $M \geq M_c$

small probabilities so $P \approx \lambda$

Characteristic Reasenberg & Jones Approximate Model

$$P(M \geq M_c) \approx kI_t \frac{D}{10^{a-bM_i}}$$

Agnew & Jones Approximate Model

$$P(C | F \cup B) \approx \frac{2N_m}{(10^{b\mu} - 10^{-b\mu})} \frac{D}{10^{a-bM_i}}$$

Both models are

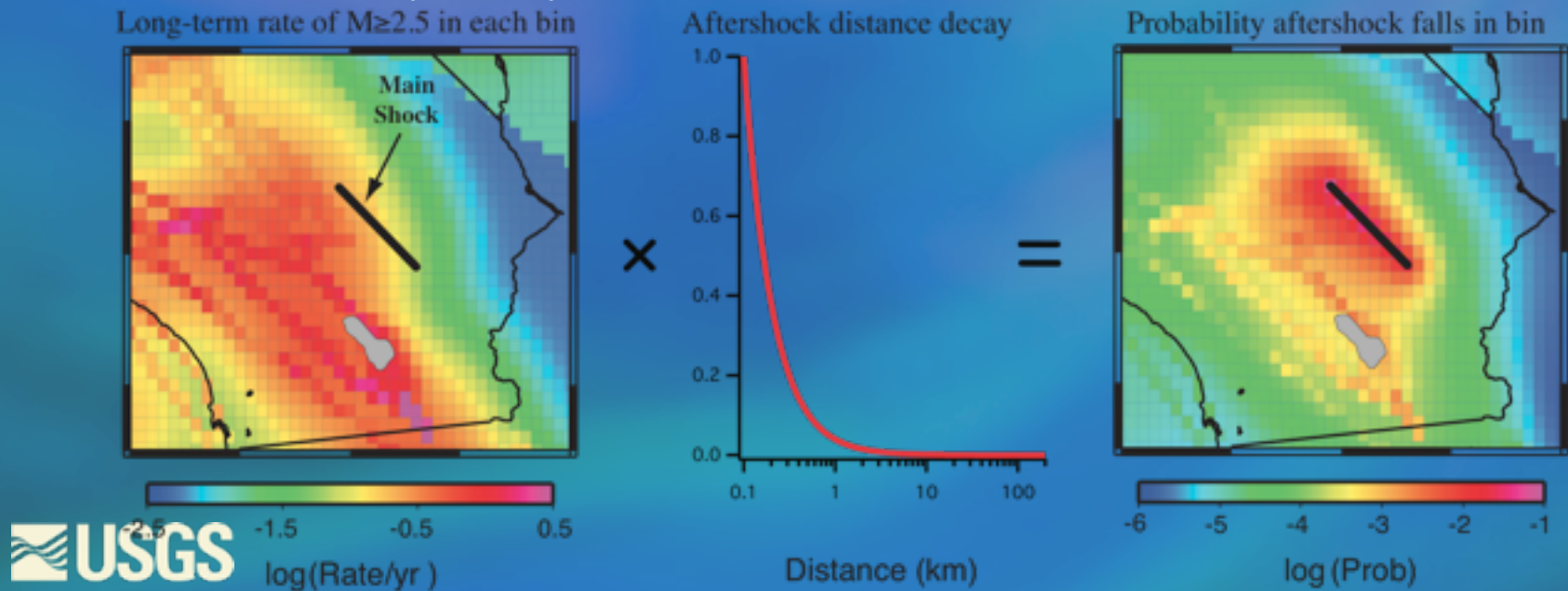
proportional to the rate of characteristic events

inversely proportional to the rate of initiating events



ETAS-based simulations for UCERF3?

- For given start time and forecast duration, collect all observed $M \geq 2.5$ events, plus randomly sample spontaneous (non-triggered) events from the model.
- For each main shock in (a), randomly sample times of occurrence of **Primary** aftershocks from modified Omori law.
- Use the long-term nucleation rate of $M > 2.5$ events throughout the region, plus a spatial decay of R^{-n} from the main shock surface, to sample a grid-cell location for each primary aftershock.



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