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## Stochastic structural modelling in sparse data situations

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#### Abstract

This paper introduces a stochastic structural modelling method which honours interpretations of both faults and stratigraphic horizons on maps and cross-sections in conjunction with ancillary prior information such as fault orientation and statistical size-displacement relationships. The generated stochastic models sample not only geometric uncertainty but also topological uncertainty about the fault network. Faults are simulated sequentially; at each step, fault traces are randomly chosen to constrain a fault surface so as to obtain consistent fault geometry and displacement profile. For each simulated fault network, stratigraphic modelling is performed to honour interpreted horizons using an implicit approach. Geometrical uncertainty on stratigraphic horizons can then be simulated by adding a correlated random noise to the stratigraphic scalar field. This strategy automatically maintains the continuity between faults and horizons.

The method is applied to a Middle East field where stochastic structural models are generated from interpreted 2D seismic lines, first by representing only stratigraphic uncertainty and then by adding uncertainty about the fault network. These two scenarios are compared in terms of gross rock volume uncertainty (GRV) and show a significant increase of GRV uncertainty when fault uncertainties are considered. This underlines the key role of faults on resource estimation uncertainties and advocates a more systematic fault uncertainty consideration in subsurface studies, especially in settings in which data are sparse.

#### Introduction

Structural uncertainty is often a major but neglected factor in subsurface studies. Structural uncertainty typically stems from the lack of observations or ambiguities of measurement and associated processing (e.g. limited resolution, lack of impedance contrasts, velocity uncertainty in seismic reflection data). In such a context, geological interpretation is very important and relies on regional knowledge about the tectonic and sedimentary evolution of the area through time, in addition to physical laws describing rock behaviour. However, the interpretation of seismic data may lead to various interpretations by experts (Bond et al. 2007). Consequently, a given subsurface model should not be considered as the truth but as a possible representation of the subsurface honouring available information at a given stage. Additional data may then be used to update or even falsify the model in case of inconsistency with new data (Tarantola 2006).

To address this challenge, several authors have proposed generating a set of possible structural models honouring subsurface data, then to use inverse methods to reduce uncertainty based on potential field or reservoir production data (Guillen *et al.* 2008; Suzuki *et al.* 2008; Seiler *et al.* 2010; Jessell *et al.* 2010; Wellmann *et al.* 2010; Aydin *et al.* (2014); Irving *et al.* 2014; Lindsay *et al.* 2014). The first stage in such approaches is to appropriately sample prior structural uncertainty. Most techniques (Lecour *et al.* 2001; Thore *et al.* 2002; Caumon *et al.* 2007; Mallet & Tertois 2010) start from an initial interpretation and perturb the geometry of the structures, but keep the topology frozen, *i.e.*, do not change fault network connectivity. More recently, it has been proposed to perturb orientation data, which may have some impact

on the model topology (Jessell *et al.* 2010; Wellmann *et al.* 2010; Lindsay *et al.* 2014; Wellmann *et al.* 2014). In this paper, we propose a method which does not rely on an initial fault network interpretation, which removes possible interpretation bias carried by the initial model. In addition, it allows, in principle, to observe a larger variability in the simulated models because extrapolation away from the data is not constrained by some initial 3D model.

The Havana modelling tool introduced by Hollund et al. (2002) and Holden et al. (2003) similarly enables to generate fault networks which may have different topologies. Originally, it simulated relatively small faults and the associated displacement along the pillars of a reference reservoir grid (Rivenæs et al. 2005). More recently, Georgsen et al. (2012) and Røe et al. (2014) have proposed a more flexible data model based on tilted 2D grids and Gaussian random fields; faults are defined within fixed fault envelopes and intersections are managed by a cookie cutter strategy, which allows for topological changes in areas where fault envelopes overlap. These approaches are suitable to represent uncertainty about fault locations on good 3D seismic data sets, but tend to only explore the uncertainty around a given structural scenario.

In this paper, we focus on fault uncertainties in settings where the number and overall topology of faults is poorly constrained. This may typically occur in onshore exploration settings, or when 3D seismic acquisition or imaging is challenging, for example in deep and subsalt reservoirs and in high-relief onshore areas. In these contexts, many different scenarios can be envisioned about the 3D fault network and the associated reservoir geometry and

connectivity. Exploring these scenarios with classical interpretation methods is demanding, costly, and subject to interpretive bias (Bond et al. 2007). Therefore, the goal of our method is to help interpretation tasks by automatically generating alternative models of field geometry and compartmentalization compatible with observations. The primary input of our method is a set of interpretation lines corresponding to horizons and fault lines picked on 2D sections, together with ancillary information (fault families and associated statistics based on regional knowledge and fault displacement for each fault line). As in Cherpeau et al. (2010 a), the method stochastically regroups fault sticks based on prior knowledge, but new rules are introduced to generate more consistent fault displacement profiles. The resulting stochastic fault networks may have variable fault connections, reflecting uncertainties about the correlation of faults between sections. For each fault network realization, one or several 3D structural models are generated by computing and possibly perturbing the stratigraphy.

The whole methodology is implemented in a plugin of the SKUA-GOCAD geomodelling software. It is applied on a Middle East field in order to illustrate its potential on an exploration play. Stochastic structural models are generated from interpreted seismic lines and are used to estimate gross rock volume uncertainty. The results are compared to those obtained by only perturbing the stratigraphy of the reference model built from 3D seismic data in order to highlight the influence of fault-related uncertainties.

## Stochastic structural modelling method

This section presents the stochastic modelling method and in particular the fault object simulation. In our current implementation, we represent faults as zerothickness slip surfaces. Faults may be a few hundred meters to kilometres long. The first step in the stochastic modelling workflow consists in characterizing faults features from the various input data (*e.g.* seismic profiles, geological cross-sections, wells).

Cherpeau *et al.* (2010b) present a framework for stochastic fault modelling which is based on an implicit 3D fault representation (also known as level set) and a binary tree which defines how faults intersect to define 3D regions. This representation has the required flexibility and computational robustness to handle changes of fault connections during simulation. In Cherpeau *et al.* (2010a), this method is extended to the conditional simulation case, *e.g.* to honour fault traces interpreted from seismic sections. These methods are briefly reviewed and extended in the following, in particular to generate 3D stratigraphy.

Faults are simulated sequentially in the input chronological order (*i.e.*, the oldest fault family is simulated first). This allows for truncating younger faults by older ones, thereby reproducing the arrest of fracture growth when abutting on a pre-existing discontinuity. This will determine whether a younger fault surface crosses or stops at an older fault. More complex configurations such as splay faults and faults being displaced by younger faults are currently not handled in our simulation method.

From the input data, the overall stochastic structural modelling strategy first simulates fault surfaces to generate a fault array, then generates possible stratigraphic models. This process is summarized in Figure 1 and further described below:

1. Prepare the data:

- 1.1. Interpret fault data to create fault sticks (e.g., by picking likely faults traces on seismic sections).
- 1.2. Attach information about displacement and location uncertainty to these fault sticks.
- 1.3. Associate fault sticks to fault families based on orientation and, when relevant, displacement information. By default, a fault stick may correspond to a fault of any family.
- 1.4. Interpret horizon data to create horizon lines and points.
- 2. Start the iterative fault simulation: For each fault family by decreasing age,

**Do:** Simulate a current a fault *F* 

- 2.1. If fault sticks not yet associated to the fault exist in the current family, randomly select a fault stick and generate an initial geometry for fault *F*, honouring the data points *S* and the fault orientation and center.
- 2.2. Try to cluster some fault sticks with *S*, so that *F* honours several fault sticks.
- 2.3. Perturb the initial fault geometry accounting for data and interpolation uncertainty.
- 2.4. Work out the lateral and vertical terminations of fault F and its branching onto other faults.

While: Fault sticks remain to be processed and target number of faults is not reached.

- 3. Build the stratigraphy:
  - 3.1. Generate a reference 3D stratigraphy honouring horizon data.
  - 3.2. Perturb the 3D stratigraphy to reflect data and interpolation-related uncertainties.

## Input data and ancillary information

#### Location information

The fault and horizon traces picked on seismic sections, interpretive paper cross-sections or maps make up the



**Fig. 1.** Flow chart showing the general simulation process.

primary input of our method. Point data may also be taken as input, but we will mainly discuss lines in the following because they correspond to the common output of seismic interpretation and provide useful information such as apparent dip. Owing to picking approximations, limited resolution of subsurface data and georeferencing and time-to-depth conversion errors, the exact location of these traces may be uncertain. Therefore, an uncertainty is attached to traces using a radial probability distribution around line points (Fig. 2), similarly as in Lecour *et al.* (2001), Wellmann *et al.* (2010). The more general model of  $Røe\ et\ al.$  (2014) for point uncertainty could also be used. During fault simulation, each fault trace (also named fault stick) will be associated to a fault surface. To avoid inconsistencies in these surfaces, we now describe additional geometric information which can be associated to each fault trace.



**Fig. 2.** Example of interpretation data on a vertical seismic section. Two seismic reflectors have been picked and are shown as green and orange lines. A fault trace is represented as a set of points (white squares); red spheres (in red) around each point represent the uncertainty about these fault picks. The maximum fault throw associated to the fault trace (in black, 60m in this example) is estimated and attached to the fault trace.



**Fig. 3.** Ambiguity about fault trace information. Many faults may honour a fault trace interpreted on a 2D section. Example of two fault surfaces representing two different faulting events honouring the same fault trace.

#### Orientation information from fault traces

As a fault trace is a 2D interpretation on a seismic section or map, the dip of a fault trace does not represent the true dip of the fault. Indeed, the apparent dip on a crosssection is smaller than the true fault dip, unless the seismic section is strictly perpendicular to the fault strike:

$$\tan(dip_{apparent}) = \tan(dip_{true}) \times \sin(\alpha), \qquad (1)$$

where  $\alpha$  is the angle between the cross-section and the fault strike

Equation (1) basically tells that the uncertainty about the true dip is small only when the cross-section is almost orthogonal to the fault strike. In practice, the angle  $\alpha$  is unknown so little information can be deduced from ap-

parent orientation alone (Fig. 3), but this information may be used to assign a fault to a fault family.

#### Slip information

Geological maps and cross-sections do not only provide location and orientation information about faults but also indications about the fault slip (Fig. 2). In seismic data interpretation, semi-automatic methods may also estimate such information. For instance, Liang *et al.* (2010) proposed the computation of throw vectors based on cross-correlation of adjacent seismic traces.

In this work, we associate to each fault trace a positive value representing the maximum vertical slip component. This information is used to constrain the fault size and obtain coherent displacement profiles on the simulated faults. The discrimination between fault types (normal or inverse) is made when assigning each fault trace to a given fault family characterized by a type and a strike and dip distributions. A signed slip value could also be relevant in tectonically complex domains where strikeslip is dominant or when fault throw may have been reversed owing to fault reactivations.

#### Size/Slip model

In the field, faults are never observed entirely. Uncertainties about lateral fault extent also exist in the presence of 3D seismic data because faults are not easily identified when the displacement is below seismic resolution. Through several systematic studies, it has been shown that the maximum displacement  $d_{max}$  and fault size L are generally related by a power law (Yielding *et al.* 1996; Kim & Sanderson 2005):

$$d_{max} = cL^n$$
, with  $n \in [0.5, 2]$ . (2)

This information is very interesting in the context of stochastic fault simulation because it provides a constraint on fault size based on the observed displacement. The exponent n is often assumed to be equal to 1 (Kim & Sanderson 2005). The factor c corresponds to the displacement at unit length and may be estimated from analogues.

On a cross-section, the maximum observed vertical displacement (fault throw) is only an approximation of the true one owing to several factors:

- The maximum throw may not be observed, so the fault size may be under-estimated.
- Some faults may be missed or misinterpreted during interpretation, *e.g.* two close faults may be interpreted as one single fault leading to an over-estimation of the fault size.

Therefore, a possible perspective could be to use random variables to sample parameters c and n in order to account for uncertainty about the maximum observed throw and the approximate nature of this type of statistical model.



Fig. 4. Flow chart showing the fault simulation steps. See text for details.



Fig. 5. Fault represented as an implicit surface. The fault is defined by the equipotential f of a volumetric scalar field  $D_F(x,y,z)$ .

## Fault families

Characteristic fault shape parameters can be summarized through statistical distributions of size, orientation and sinuosity. Similar faults are grouped into fault families, each family relating to a given faulting event characterized from regional tectonic knowledge, *e.g.* a NW-SE extension or a W-E transtension. Fault families are ranked chronologically to represent the time sequence of the fault events and to model observed fault truncations: a fault terminates on or crosses existing faults.

Fault traces are assigned to specific fault families when possible:

- If the global fault orientation is believed to be almost perpendicular to seismic sections (*e.g.* from regional context), fault traces can be restricted to some fault families based on apparent orientation, *e.g.*, to distinguish opposed-dipping faults.
- If the throw information is sufficient to discriminate the fault type for a given fault trace, the fault trace can be restricted to belong to specific fault families corresponding to this particular fault type.

When fault traces are assigned to several fault families, only the simulated faults of these families can honour these fault traces.

Additionally, families contain information about the target number of fault surfaces to be simulated. The actual number of faults in a realization may be equal to that target if it is sufficient to honour all fault sticks, or larger otherwise.

## Stratigraphic information

The stratigraphic data corresponds to points or lines representing stratigraphic horizons interpreted on seismic sections, either manually or using horizon tracking tools. As compared to fault data which are associated to families, horizon points or lines are associated with layering information in the form of a stratigraphic column. This piece of information is essential to generate layer geometries, especially in the presence of unconformities. Additionally, stratigraphic orientation as observed on wells may be used as input, both on main stratigraphic horizons and within layers (see Caumon *et al.* (2013) for details).

## Fault network simulation

The method proceeds iteratively by fault family (Fig. 1). We now describe the elementary steps for simulating one fault of a given family, see also Figure 4. For the sake of simplicity, we assume below that each fault to simulate contains at least one fault pick (otherwise, the fault parameters are simply drawn randomly from the statistical information associated to the current fault family).

## Step 2.1: Initial fault geometry computation

A fault trace S is first randomly drawn from the input fault data (Fig. 4a). If the average plane of the fault trace is inconsistent with the orientation distribution of the associated fault family, the dip and the strike are randomly drawn from that distribution. Then, a fault centre is randomly drawn in the neighbourhood of S (Fig. 4b). This fault centre is drawn in a volumetric probability distribution function, which is uniform if no input information is provided. This distribution may also account for the distance to other faults, *e.g.* to simulate secondary faults occurring in the vicinity of existing major faults (conditional distribution law), or conversely to emulate screening effects (Ackermann & Schlische 1997).

At this point, fault parameters (fault trace *S*, orientation and centre) are used to define the initial fault geometry (Fig. 4c). In our implementation, a fault is an implicit surface defined as the equipotential *f* of a volumetric scalar field  $D_F(x,y,z)$  within a given volumetric domain *A* meshed with tetrahedra (Frank *et al.* 2007; Caumon *et al.* 2013):

$$D_F(x, y, z) = f, \quad \forall (x, y, z) \in A.$$
(3)

Each simulated fault is defined by its own scalar field (Fig. 5). The interpolation is performed in a tetrahedral mesh and scalar field values are stored on the mesh vertices. This scalar field is computed by numerical optimization as described by Frank *et al.* (2007) and Caumon *et al.* (2013), which makes it convenient to rapidly update the fault geometry in further steps.

## Step 2.2: Data clustering

Once an initial fault surface has been computed, available fault traces are considered as candidates for possible inclusion in the fault surface being built. Therefore, the algorithm first performs a three-step filtering in order to ensure plausible fault geometry and slip profile. All available fault traces from the same family are considered as candidates by the set of filtering rules below.



**Fig. 6.** Fault trace filtering based on orientation. The closest and furthest points of each trace  $S_1$  and  $S_2$  from fault F are projected onto F. Angle  $\alpha'_1$  is too large so F cannot honour  $S_1$  whereas  $\alpha'_2$  is small which enables F to possibly honour  $S_2$ . The filtering ensures reasonable dip or strike changes in case the fault trace is sub horizontal.



#### Data filtering based on size information (Fig. 4, d)

Depending on the target fault size as defined in the current fault family, fault traces that are too far away from the current fault centre are discarded. Indeed, their inclusion in the fault would lead to a fault too long as compared to the input size distribution for the family. Additionally, fault sticks which are not in the same fault block as the fault centre may be ignored to avoid crossing contacts between faults. With our current representation of fault blocks based on extrapolated faults, this option is generally irrelevant because it tends to generate smaller and smaller faults as simulation proceeds

#### Data filtering based on data orientation(Fig. 4, e)

In general, fault traces with opposed dip should not be clustered, because it would imply significant changes in fault dip and unrealistic stratigraphic geometry. For a given fault trace S, we propose to compute the distance between the furthest point  $p_f$  and the closest point  $p_c$ projected onto the fault surface, respectively  $p_f^{impact}$  and  $p_c^{impact}$ . The angle  $\alpha'$  between the vectors  $v_S(p_f, p_c)$  and  $v_S^{impact}(p_f^{impact}, p_c^{impact})$  is then computed. Clustering is not allowed if  $\alpha'$  is deemed too large, which ensures an acceptable dip change in case of clustering (Fig. 6). In case S is sub-horizontal, this strategy avoids clustering data points that would entail a too large strike change for the fault being built. In practice,  $\alpha'$  should not be chosen greater than 30° to ensure realistic orientation changes. This strategy could be modified to allow for listric fault geometries.

#### Data filtering based on throw information (Fig. 4, f)

The maximum throw attached to fault traces provides useful information that can help clustering fault traces in a consistent way. Indeed, the slip amplitude is often assumed to be sub-maximum to maximum at the fault centre and null at fault tip-line (Barnett *et al.* 1987; Walsh *et al.* 2003) (Fig. 7).

Therefore, a fault honouring a trace *S* with maximum displacement  $d_S$  may or may not be clustered with a trace *S'* with maximum displacement  $d_{S'}$  depending on the following configurations:

- If S and S' are on both sides of the fault centre, no rule applies, so clustering is possible (trace S<sub>0</sub>' in Figure 8);
- (2) If S' is between S and the fault tip-line,  $d_{S'}$  should be smaller than  $d_S$  (trace  $S_2$ ' in Figure 8);
- (3) If S' is between S and the fault centre,  $d_{S'}$  should be larger than  $d_S$  (trace  $S_1$ ' in Figure 8).

These rules must be strictly applied in the case of isolated faults but are not appropriate when faults are close and interact because the displacement profile may then be more complex. They do not apply either if faults have grown by segment linkage (Walsh *et al.* 2003). Consequently, a tolerance  $\varepsilon$  is introduced for more general fault displacement profiles, which yields the following updated rules in cases 2 and 3:



**Fig. 8.** Fault trace filtering based on displacement information. The fault honours the fault trace S with attached displacement  $d_s$  and three other fault traces  $S'_0$ ,  $S'_1$ ,  $S'_2$  (with respectively displacement  $d_{S'_1}$ ,  $d_{S'_2}$  and  $d_{S'_3}$ ) are candidates for clustering. Fault trace  $S'_0$  is not on the same side of the fault centre than S; therefore  $S'_0$  is not filtered out because no rule applies. Fault trace  $S'_1$  is between S and the fault centre, so  $d_{S'_1}$  should be larger than  $d_S$  (Eq. (3)) for considering  $S'_1$  as candidate for clustering. Fault trace  $S'_2$  is between S and the fault trace  $S'_2$  is between S and the fault centre S and the fault tipline, so  $d_{S'_2}$  should be smaller than  $d_S$  (Eq. (2)) to consider  $S'_2$  as candidate for clustering.

• If S' is between S and the fault tip-line,  $d_{S'}$  must satisfy:

$$d_{S'} \le d_S(1+\varepsilon). \tag{4}$$

• If S' is between S and the fault centre,  $d_{S'}$  must satisfy:

$$d_{S'} \ge d_S(1-\varepsilon). \tag{5}$$

If these relations are not honoured, S' is not associated with S. Other rules could also be considered to constrain data clustering. Indeed, if the difference of displacement observed at two relatively close fault sticks is large, these two fault sticks are unlikely to belong to the same fault because it would imply the stratigraphy to be highly curved along the fault strike. This may also be the sign of a branching fault occurring between the fault sticks.

#### Data clustering based on angle criterion (Fig. 4, g)

The three previous processing steps aim at filtering kinematically inconsistent fault sticks. Then, remaining fault sticks are considered as candidates for possible clustering with the fault being built. The data clustering probability of each candidate relies on the angle  $\alpha$  it forms with the initial fault surface (Fig. 9) (Cherpeau *et al.* 2010a). Small  $\alpha$  angles entail small fault surface changes as compared to large  $\alpha$  angles, hence are considered more likely, *i.e.* the smaller  $\alpha$ , the higher the probability of clustering. The algorithm first defines a Gaussian cumulative distribution function  $CDFc(\alpha)$ : the distribution is centred (mean 0) and its standard deviation is arbitrarily chosen to 20 degrees. For a fault stick with angle  $\alpha$ , the algorithm computes the probability of clustering  $pc(\alpha)$  as follows (Fig. 10):

$$pc(\alpha) = 1 - |0.5 - CDFc(\alpha)| \times 2$$

Therefore, a fault stick with  $\alpha$  equal to zero is systematically considered for clustering and the probability of clustering is equal to 0.32 for  $\alpha$ =20°, which limits high curvature changes. The mean *m* of *CDFc*( $\alpha$ ) is updated to be the mean of  $\alpha$  angles of accepted fault sticks in order to only draw coherent fault sticks. From a computational point of view, this methodology avoids updating the fault geometry and  $\alpha$  angles each time a fault stick is drawn.

#### Steps 2.3 and 2.4: final fault geometry computation

#### Fault sinuosity (Fig. 4,h)

Once data clustering has been performed, the fault scalar field is updated so that the fault equipotential surface passes through the retained fault traces. This is achieved by using all traces in the optimization of the scalar field  $D_F$  (Eq. (3)). Then, the fault scalar field is stochastically perturbed to obtain the final fault geometry. The perturbation consists in adding a correlated random field generated by a conditional Sequential Gaussian Simulation whose parameters are determined from the input sinuosity parameters. The value of the random field is set to zero at conditional fault trace locations if no uncertainty exists. If a perturbation range is attached to fault traces, the value of the perturbation is drawn from a triangular law whose mode is the current location. As in Lecour et al. (2001), a probability field simulation (Srivastava 1992) is used to provide the random numbers in order to ensure a correlated geometry between data points.

#### Fault extension (Fig. 4,i)

The next simulation step consists in modelling the extension of the fault. For that, we represent the fault existence domain A (Eq. (2)) by thresholding a 3D scalar field (Cherpeau *et al.* 2011). This scalar field is initialized analytically with a 3D ellipsoid around the fault centre. Without any further information and based on previous studies (Barnett *et al.* 1987; Walsh *et al.* 2003), the 3D ellipsoid is built from size parameters simulated from the input statistical distributions given by the users. It is also possible to use displacement/size statistical relationships to randomly draw the fault size, see Eq. (2).

#### Fault intersection (Fig. 4,j)

The simulated fault may intersect previously simulated faults, hence the final step consists in honouring fault intersections. The algorithm first tests the intersection with neighbour faults using a Binary Partition Tree that describes the fault spatial layout (Fuchs *et al.* 1980).

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**Fig. 9.** Data clustering based on angle criterion (map view). (a) The angles  $\alpha_i$  between data points and the initial fault surface are computed (map view). The probability of clustering increases when  $\alpha_i$  decreases. (b) Example of different fault surfaces corresponding to different data clustering. From Cherpeau *et al.* (2010a).



**Fig. 10.** Probability law of data clustering. The probability pc(a) depends on the angle  $\alpha$  between data points and the initial fault surface (Fig. 9). If  $\alpha$  equals zero, it means the data points are already on the fault surface, thus the clustering probability is 1. The probability  $pc(\alpha)$  is symmetrical about the zero angle and quickly decreases towards large angles to avoid sinuous faults.



Fig. 11. Partial branching between two faults. In the case of partial branching, the algorithm may consider it as a crossing contact (in which the two faults are conjugate, a) or branching contact (in which the fault assumed youngest is truncated by the other fault, b).

Then, it propagates to further faults only if needed so as to limit computational time.

In some cases, the outline of the simulated fault intersects another fault in only one point (partial branching, see Figure 11). To our knowledge, this type of configuration has received little attention in the literature, either because it is never observed on outcrop or simply because it does not exist in nature. In such a case, we propose the fault contact to be considered either as crossing (Fig. 11a) or branching (Fig. 11b).

#### Stopping criterion

A target number of faults is given as input for each fault family. It can be estimated by the supposed number of fault traces per fault, regional analogues, other prior information or modelling constraint. The simulation process continues as long as the number of simulated faults is smaller than the input number of faults or some fault traces are still available, *i.e.* fault traces not included in any simulated fault. The number of faults may also be randomized so that the algorithm generates fault network realizations with varying numbers of faults (Cherpeau *et al.* 2012).

## Stratigraphic modelling

#### Computing the stratigraphy

The method uses implicit surfaces to represent fault surfaces. Consequently, the tetrahedral mesh supporting the fault simulation is not conformable to the simulated faults. However, these discontinuities need to be introduced into the mesh to be able to compute the stratigraphic field with displacement along fault surfaces (Caumon et al. 2013). This work uses a resampling and point insertion Delaunay method implemented in the SKUA software to compute fault blocks from fault surfaces (Lepage 2003; Jayr et al. 2008). Then, one or several stratigraphic fields  $D_{S}(x,y,z)$ , depending on the number of stratigraphic unconformities, are interpolated through the faulted model with horizon data guiding and constraining the process in a deterministic manner (for more details, see Frank et al. (2007); Jayr et al. (2008) and Caumon et al. (2013)).

#### Stratigraphy-related uncertainty

Stratigraphic horizon uncertainties can be divided into two terms:

- A continuous uncertainty about the horizon depth away from the boreholes and cross-sections. In sparse data settings, it mainly consists of interpolation and interpretation uncertainties. In seismic data settings, it relates to time-to-depth conversion and hence to the uncertainty about the velocity field in the overburden (Abrahamsen 1992; Thore *et al.* 2002). This term can be sampled by perturbing horizon geometry while preserving the fault displacement fields. It generally represents the first order uncertainty.
- A discontinuous uncertainty reflecting the uncertainty about the fault displacement field (Suzuki *et al.* 2008). This uncertainty can be significant away from cross-sections in 2D data settings. In the presence of 3D seismic data, this uncertainty may also be large in poorly imaged areas such as in subsalt structures.

These two uncertainties are handled by adding two correlated random fields (Fig. 12, middle) to the initial stratigraphic scalar field (Fig. 12, top) to obtain the final geometry (Fig. 12, bottom) (Caumon et al. 2007, Caumon 2010). This correlated noise is computed in the depositional space (Mallet, 2014) for the continuous term  $(R_1(x,y,z))$  (Fig. 12, middle left), which ensures a coherent layer perturbation across faults. A second random field  $R_2(x,y,z)$  is computed in the xyz Cartesian space to model the discontinuous term (Fig. 12, middle right) with locally varying anisotropy aligned on the stratigraphic orientation. This second random field is discontinuous across faults to account for fault throw uncertainty. As such it is computed directly on the tetrahedral mesh through an extension of the GsTL algorithms (Remy et al. 2002) to the tetrahedral SKUA data structure. In both cases, the random field is set to zero at data location to guarantee data conditioning.

Specific care is needed to ensure a homogeneous perturbation of the stratigraphic scalar field  $D_S(x,y,z)$ . Indeed, the random noise has to be scaled by the local norm of the gradient of  $D_S(x,y,z)$  so that the amplitude of perturbation in meters can be considered even if the layer thickness varies over the domain of interest (Caumon 2010). The perturbed stratigraphic field  $D'_S(x,y,z)$  is obtained as follows (figure 12, bottom):

$$D'_{S}(x, y, z) = D_{S}(x, y, z) + R_{1}(x, y, z) \times$$
$$|\nabla D_{S}(x, y, z)| + R_{2}(x, y, z) \times |\nabla D_{S}(x, y, z)|$$
(6)

Consequently, several stochastic stratigraphic fields can be generated for a given fault network realization. Mallet & Tertois (2010) similarly account for geometric uncertainty about faults and horizons but their methodology relies on a preferred deterministic geometric model (Mallet, 2014). Here, this uncertainty compounds with that which is sampled by the stochastic fault network realizations.

#### Simulation choices: discussion

The simulation process presented above generates stochastic structural models to account for possibly large structural uncertainties. The various parameters describing a fault surface (choice of fault traces, orientation, centre, sinuosity, and dimension) are simulated sequentially for each fault. The relative order of these steps is arbitrary and could be changed; for instance, the fault extension could be simulated before the data clustering step. In this case, the clustering rules would be stricter as the method actually takes the maximum fault size from input distribution. The fault centre could also be drawn after the data clustering to allow for more fault trace inclusion possibilities. However, we consider the fault centre as being a crucial parameter because it determines the neighbourhood of the future fault. This choice is also motivated by the perspective of including more input information during the fault nucleation step, e.g. to favour nucleation in high displacement areas and avoid nucleation in low displacement areas.

In general, the simulation steps should first randomly draw the fault characteristics which are most constrained by observations. Then, these well constrained fault parameters should help constraining the simulation of the less informed fault characteristics, along with geological rules, physical laws or prior geological knowledge.

In some geodynamic contexts, recent faults may also displace older ones; this is not presently allowed in the current workflow. This may be emulated by simulated older faults as independent surfaces on the more recent fault surface. Several strategies need to be considered to add such poly-phased tectonics in the proposed algorithm; some recent related works such as vector-field based deformations open interesting avenues to address this problem (Bouziat 2012; Laurent *et al.* 2013).



**Fig. 12.** Method for modelling stratigraphic uncertainty. Top: initial geometry. Middle: the uncertainty is composed of a stratigraphic and a Cartesian correlated random fields. Bottom: updated horizon geometry which corresponds to the sum of the initial geometry with the perturbations fields.

## Application to a Middle East field case

In this section, we propose to illustrate the methodology on a Middle East field to show the impact of both fault and horizon uncertainties on gross rock volume (GRV) estimations in a sparse data situation such as encountered from exploration to development phases. One of our main objectives here is to consider how much fault uncertainty affects the GRV as compared to considering deterministic fault network and solely assessing reservoir depth and thickness uncertainty. The studied area is a horst with normal faults and three main horizons overlying three stratigraphic reservoir units.

#### Input data

Both horizons and faults are interpreted on five fictive seismic lines orthogonal to the regional horst direction. These five lines and the associated 2D structural interpretations are generated from a 3D seismic dataset and the corresponding reference interpretation (Fig. 13). For each fault trace S, the maximum vertical offset of horizons on



**Fig. 13.** The reference interpretation has been built from a full 3D seismic survey. Faults and horizons have been interpreted on five fictive seismic lines. Fault traces have been grouped according to their orientation. SW dipping traces (green colour) are set to belong to *family*<sub>1</sub>. NE dipping traces (yellow colour) are set to belong to *family*<sub>2</sub>. Other fault traces (pink colour) are not classified hence can correspond to a fault from any fault family. Scale is not given and orientation has been modified for confidentiality reasons.

both sides of the fault is measured and associated to *S* in the data base. Interpreted data are composed of twentyfive fault traces and data points corresponding to stratigraphic horizons. Uncertainty about fault location is set to 10m for each fault trace to reflect picking and migration uncertainty, with a triangular radial probability function centred on the reference location. In this scenario, uncertainty in time-to-depth conversion is assumed negligible as compared to the uncertainty due to the lack of data between the sections, so horizon picks are considered deterministic. For confidentiality reasons, orientation has been changed from original data, GRV unit is arbitrary, the stratigraphic ages and scale are not given.

## Fault network characterization

## Fault families

From the interpreted fault traces and regional context, faults are grouped into two normal fault families corresponding to an east/west extension:

(1) *family*<sup>1</sup> strikes [N80-N100] and dipping [60-70]. Most traces seem oriented along that direction (green data points in Figure 13) and the minimum number of faults in the area is set to 5.

 (2) family<sub>2</sub> corresponds to opposed-dipping faults, hence is oriented [N260-N280], dips [60-70] (yellow data points in Figure 13) and the minimum number of faults in the area is set to 3.

For both families, the maximum number of faults is at most equal to the number of fault sticks in that family. In this particular study, we choose to keep the models as simple as possible by stopping the fault simulation as soon as all fault sticks belonging to a given family have been associated to a fault surface. Therefore, the actual number of faults in each realization only depends on the outcome of the fault stick clustering procedure described above.

From regional reservoir analogues, a third fault family, *family*<sub>3</sub>, oriented [N160-N180] with dip uniformly distributed in [60-70] is also expected. The number of faults for *family*<sub>3</sub> is set to 2. The relative age of the two first fault families cannot be deduced from the available data and tectonic history, so families are considered cogenetic, i.e. there is no systematic truncation rule between faults from different fault families. The third fault family, *family*<sub>3</sub>, is considered branching on the two first families, so the algorithm simulates first *family*<sub>1</sub> and *family*<sub>2</sub>.

## Fault size

The size/slip model (Eq. (2)) introduced previously is used to estimate the fault size. In the absence of regional analogue data, we use the coefficient c = 0.02 provided by Kim & Sanderson (2005) for normal faults.

The throws observed on the seismic sections range from 20 to 260m, which corresponds to a maximum fault elongation of 13km. As discussed above, this can be considered as a lower bound of the actual throw because largest throw amplitude may occur between sections.

## Stratigraphic uncertainty

The layer geometry is perturbed by adding random field realizations to the implicit stratigraphic model in SKUA. These perturbation fields are simulated using a Sequential Gaussian Simulation conditioned to be zero at horizon picks. The perturbation amplitude is considered centred Gaussian in both cases, with zero mean and standard deviations  $\sigma_1 = 17$ m for the continuous uncertainty and  $\sigma_2 = 8$ m for the discontinuous uncertainty and  $\sigma_2 = 8$ m for the discontinuous uncertain smooth perturbations. Variogram ranges are equal to 2,500m horizontally and 600m vertically for the continuous term  $R_I$ . The discontinuous term  $R_2$  is modelled with a variogram having ranges equal to 1,000m horizontally and 300m vertically.

## Results

## Fault networks

190 fault networks have been simulated using interpreted fault traces and input fault families. All realizations have



**Fig. 14.** Gross rock volumes (GRV) distributions for units  $U_1$ ,  $U_2$ ,  $U_3$  and total volume (unit is arbitrary for confidentiality reasons) for case A (topological uncertainties about both faults and stratigraphy, in blue) and case B (uncertainty in the stratigraphy only, in yellow). P10, P90 and interquartile range (IQR) are represented for both cases. The reference model (red arrows) corresponds to a medium case for all units, but case A entails much larger GRV uncertainty than case B.

a larger number of faults than the reference one (Fig. 13) because most simulated faults contain less fault traces than the reference model. This may be explained by:

- Clustering rules (displacement profile, orientation deviation) that are too restrictive.
- Fault size underestimation, due to an approximated maximum slip or inappropriate parameters c and n in Equation (2). Indeed, if we consider the largest fault in the reference model and assume n equal to one, the parameter c is equal to 0.013 whereas we used 0.02 in the simulation. This may suggest that some faults have been merged in the reference interpretation or that some have grown by segment linkage.

In a real situation, no reference model would be available so we chose to proceed with the stratigraphic and gross rock volume uncertainty assessment using all the 190 stochastic fault networks.

## **Gross Rock Volumes (GRV)**

For each stochastic fault network, five stratigraphic fields have been computed by adding the stratigraphic field obtained by interpolating horizon data through the fault blocks with a random noise composed of the first and second order perturbation  $R_1$  and  $R_2$ . Consequently, 950 structural models have been generated using the method presented above. These models, referred to as case A, were then used to study the uncertainty on the gross rock volumes above a deterministic planar water-oil contact with no transition zone located at 2800m depth in the three distinct stratigraphic units.

To compare the GRV uncertainty accounting for topological fault uncertainty method with classical uncertainty models which consider fixed fault networks, we also generated a case *B* comprised of 950 models obtained by perturbing only the stratigraphy of the reference fault model. The chosen stratigraphic uncertainty parameters were the same as in case *A*. Results for cases A and B are presented in Figure 14.

The GRV values for case B are close to the GRV values of the reference model, the difference between the mean GRV estimation being only 0.02%. In case A, the total GRV mean is about 1% greater than in the reference



Fig. 15. Example of stochastic models (top reservoir surfaces). Top horizon is painted by the depth and contour lines for: (a.) the reference model, (b.) a pessimistic scenario, (c.) a medium scenario and (d.) an optimistic scenario. The black lines represent crosssections of Figure 16. Black points correspond to horizon data of the top reservoir. Red points correspond to the locations of the reference faults at the top reservoir (fault data are not visible because they are below the top reservoir). The difference in GRV estimation may be explained by a deeper top reservoir in the southern part of the studied area for the pessimistic scenario and a higher top reservoir in the eastern part for the optimistic scenario. These zones contain few data, leading to a relatively large variability in the simulated models.

estimation but 4% greater for unit  $U_1$  (volumes in units  $U_2$  and  $U_3$  are correlatively lower). For all three units, the GRV interquartile range is about five times larger in case *A* than in case *B*. This highlights the large impact of uncertainty about fault definition and connectivity on the output volumetric uncertainty.

Top reservoir surfaces of a pessimistic scenario (small gross rock volume), a medium scenario (volume similar to the reference) and an optimistic scenario (volume larger than the reference) are presented in Figure 15 and cross-sections of these scenarios are shown in Figure 16. Thanks to the prior definition of fault families and the fault trace clustering rules, the generated fault networks

and the associated displacements seem globally consistent and plausible in three dimensions.

These results show that considering fault geometry and connectivity uncertainty may be crucial for assessing accumulation uncertainty when only sparse data are available. Indeed, whereas the reference model corresponds to a medium scenario both with and without fault uncertainty, the low case (P10) and high-case (P90) cover a much larger range when uncertainties about faults are accounted for. This confirms that considering significantly varying interpretations and scenarios in poorly constrained reservoir studies is necessary to appropriately address uncertainties and to support field appraisal and development decisions.



**Fig. 16.** Example of stochastic models (cross-sections). Cross-sections AB (location shown in Figure 15) correspond to: (*a.*) the reference model, (*b.*) a pessimistic scenario, (*c.*) a medium scenario and (*d.*) an optimistic scenario. Some faults may be interpreted on all cross-sections owing to the proximity of fault traces (*e.g.*, faults  $F_1$  and  $F_3$  from family<sub>1</sub> and fault  $F_2$  from family<sub>2</sub>). The slip of fault  $F_1$  is larger for the pessimistic scenario so that the hanging wall is below the water-oil contact. The optimistic scenario seems to contain more faults of family<sub>2</sub> than other scenarios, which entails the uplift of tilted foot walls.

## Conclusions

The presented work sets the basis for a full stochastic structural modelling workflow. The method starts by the characterization of faults using hard data, geological concepts and physical laws to help determining fault parameters that cannot be directly measured. Then, the stochastic fault model samples both geometrical and topological fault uncertainties. During the next step, one or several stratigraphic fields, depending on the number of unconformities, are computed and stratigraphic uncertainties are considered by adding a correlated random perturbation in both depositional and present-day spaces. Consequently, the method generates structural models with various fault connections, number of faults, fault slips and stratigraphic units without limiting assumptions about fault and horizon geometry. This set of models can then be used for making predictions such as gross rock volumes as presented on a Middle East field case study,

which enables to better evaluate risks and be more confident for decision-making in exploration and development settings. Such a stochastic approach is most relevant in sparse data situations, because of the large uncertainties and broad range of possible models that cannot be sampled by geometrical perturbations of a single deterministic model.

In the presented workflow, the algorithm first generates fault surfaces, using fault displacement information at the data clustering step. Then, the fault displacement is computed using horizon data. Whereas faults can be seeded so as to reproduce interactions, some of the generated fault networks are not fully consistent. In particular, no check is made during fault simulation to ensure that the simulated faults have a globally consistent displacement field compatible with horizon data. One solution could consist in adding an extra step at the end of a fault object simulation to directly simulate a fault displacement field according to the fault size. Then, the algorithm could

compare the global measured displacement to the current simulated displacement field and use this information to: (1) nucleate new faults where observed displacement is still greater than the simulated one; (2) avoid nucleation where no displacement has been observed and (3) stop the fault simulation when all displacement is honoured given a tolerance threshold. Instead of interpolating a stratigraphic field constrained to horizon data, the displacement of geological layers could also be modelled accounting for the rock behaviours, *e.g.* to model drag folds, directly in the vicinity of faults (Røe *et al.* 2010, Laurent *et al.* 2013).

These improvements would constrain the simulation process to obtain more realistic results, in particular for the location and slip profile of faults. The geomechanical restoration of the simulated models could also be used to falsify inconsistent models, as done by section balancing.

In this study, we have focused on structural uncertainties in sparse data contexts and we only assessed the impact of these uncertainties in terms of hydrocarbon accumulations. In exploration studies, the proposed workflow could be connected with seal integrity studies. In appraisal and development studies, this method also has potential to be integrated in the rest of the modelling workflow to assess the impact of structural uncertainties on reservoir production. This would be relevant also in the presence of 3D seismic data, where fault connectivity may also be uncertain at the fault segment scale (Julio *et al.* 2014). In all cases, structural uncertainty should be considered jointly with other uncertain parameters such as well correlations (Lallier *et al.* 2012), fault conductivity, petrophysics and fluid properties.

In practice, the computational time required for such an approach does not allow to consider all possible models but only a subset of models. These models should be carefully selected and ranked, for instance using reservoir simulation proxies. An avenue for further research is to increase the level of input information directly in the simulation model, for instance by formulating mass balance computations as stochastic simulation constraints. Another avenue is to falsify or update some of the models by computing their likelihood and solving an inverse problem. This can be done by introducing some structural concepts not accounted for during the simulation process, as done by Wellman et al. (2014). Confronting the stochastic models to other types of data (e.g., reservoir production curves) is also interesting to reduce uncertainties. For example, Cherpeau et al. (2012) propose a parameterization of faults integrated in a stochastic inverse method and use dynamic information to infer fault characteristics and reduce fault-related uncertainties. A future challenge is therefore to include this full stochastic structural method in such inverse problem to consider geological features all together and not only faults separately.

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