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LDMC design for low complexity MIMO detection and efficient decoding

Han Hai¹, Xue-Qin Jiang^{1*}, Poongundran Selvaprabhu², Sunil Chinnadurai³, Jia Hou⁴ and Moon Ho Lee⁵

Abstract

Low-density multiple-input multiple-output code (LDMC) can reduce the complexity of tree-search detection in MIMO systems. In this paper, we present a new modified progressive edge-growth (PEG) algorithm to construct large girth LDMCs, which are referred to as PEG-LDMCs. We analyze the complexity of the LDMC constrained sphere decoding (SD) and show that the LDMC constrained SD detection can be used for high reliability of the data transmission in MIMO systems. Furthermore, we propose two new efficient iterative decoding algorithms for LDMCs, which are high speed serial decoding and fast convergence shuffled decoding. Finally, we compare the bit error rate (BER) performance of PEG-LDMCs to that of the existing LDMCs. The simulation results show that the PEG-LDMCs can achieve better BER performance than that of the existing LDMCs.

Keywords: Low-density parity-check (LDPC) codes, Multiple-input multiple-output (MIMO), Sphere decoding (SD), Low-density MIMO codes (LDMCs)

1 Introduction

Multiple-input multiple-output (MIMO) techniques have been widely studied during the past decades as they can provide significant multiplexing and diversity gains in transmission. Therefore, MIMO techniques have been identified as one of the most practical methods to combat fading and to increase the capacity of wireless channels in the recent years [1–4].

In order to provide high reliability of the data transmission in MIMO systems, special attention has to be paid in the receiver design. Maximum-likelihood (ML) detection is the optimal detection for MIMO systems [5, 6]. However, the complexity of the exhaustive searching in ML detection is too high for practical use. Therefore, suboptimal but low complexity detections were proposed, which include linear detection, such as zero-forcing (ZF) [7, 8], minimum mean-square error (MMSE) [9], and non-linear detection, such as sphere decoding (SD) [10]. The performance of MMSE detection is better than that of ZF detection, due to the fact that the correlation between the noises in ZF detection is neglected in the projection operation. However, both the ZF detection and the MMSE

detection suffer from serious performance degradation with respect to the optimal ML detection. On the other hand, the SD detection draws attention of researchers as it can achieve a near-ML detection performance [11]. The main idea of the SD detection is that it only searches the ML candidate symbols which lie inside a specific sphere. For a given sphere size, the detection complexity of SD detection in MIMO systems becomes very high when the number of candidates is large.

Practically, error-correction codes are usually applied in MIMO systems. In particular, low-density parity-check (LDPC) codes have drawn attention of many researchers due to their Shannon limit approaching performance [12–14]. As a subclass of LDPC codes, low-density MIMO codes (LDMCs) were presented in [15, 16], which reduce the complexity of the ML detection by introducing constraints in each transmission vector. The transmission vector is defined as the set of symbols which are transmitted simultaneously via multiple antennas. In [17], LDMCs with low-encoding complexity are further presented.

Motivated by the near-ML detection performance of the SD detection and the complexity reduction property of the LDMCs, in this paper, we study the design of LDMCs and the concatenation strategy of LDMCs and SD detection in MIMO systems.

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Furthermore, we propose more efficient iterative decoding algorithms for LDMCs. It is well known that the iterative decoding converges to the optimal solution provided that the parity-check matrix of the code is of large girth [18]. Therefore, LDMCs of large girth are particularly desirable. Hence, we propose a modified progressive edge-growth (PEG) algorithm to construct LDMCs of large girth. The contributions of this paper are as follows:

- We propose a new modified PEG algorithm to construct large girth LDMCs for good performance.
- We analyze the complexity of SD detection in the LDMC-coded MIMO systems, which indicates that the LDMC-constrained SD detection can be used for MIMO systems with large number of transmit antennas.
- We propose two efficient iterative decoding algorithms for LDMCs for high speed and fast convergence decoding.

This paper is organized as follows. In Section 2, we review MIMO systems and LDMCs. In Section 3, we introduce a modified PEG algorithm to construct large girth LDMCs. In Section 4, we compare the complexity of LDMC-constrained SD detection with that of the MMSE and ZF detections. In Section 5, we introduce two new shuffled decoding algorithms for LDMCs. Examples of the LDMC-constrained SD detection in MIMO systems and the corresponding simulation results are given in Section 6. Finally, Section 7 concludes the paper.

Notation: bold lower case letters represent vectors, while bold upper case letters denote matrices. $(\cdot)^T$, $(\cdot)^H$, and $\|\cdot\|$ denote transpose, Hermitian, and norm operations, respectively. $\mathbb{C}^{m \times n}$ stands for the complex space of size $m \times n$.

2 Preliminaries

This section introduces some background concepts that will be used throughout the paper.

2.1 MIMO systems

Let M_t be the number of transmit antennas and M_r be the number of receive antennas. The source binary information bits $\mathbf{b} = [b_1, \dots, b_{nR}]$ are first encoded using an LDPC encoder to generate a codeword $\mathbf{w} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_{\frac{n}{M_t Q}}]$, where R is the code rate and n is the length of the codeword. Then, each group of $M_t Q$ coded bits $\mathbf{w}_i = [b_1, \dots, b_{M_t Q}]$ is mapped to a group of M_t transmission vector $\mathbf{x} = [x_1, \dots, x_{M_t}]^T$, where x_j is taken out of the constellations of size 2^Q . \mathbf{x} is then passed to the transmit filter and sent through the M_t transmit antennas. \mathbf{x} is denoted as the transmission vector in the following.

Without loss of generality, we express the system model as

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{z}. \quad (1)$$

Here, $\mathbf{y} \in \mathbb{C}^{M_r \times 1}$ is the complex received signal vector. $\mathbf{H} \in \mathbb{C}^{M_r \times M_t}$ is the Rayleigh fading channel matrix with independent entries that are complex Gaussian distributed with zero mean and unit variance. \mathbf{H} is assumed to be known to the receiver, but not to the transmitter, and the channel coefficient randomly varies in time. $\mathbf{z} \in \mathbb{C}^{M_r \times 1}$ is complex white Gaussian noise with variance σ^2 per dimension.

Referring to [22–24], the received signal is iteratively detected and decoded by mutually exchanging soft information between the detector and LDPC decoders. The detection computes the log-likelihood ratios (LLRs), L_i , for each coded bit by using

$$\begin{aligned} L_i &= \log \left(\frac{\Pr[w_i = 1 | \mathbf{y}, \mathbf{H}]}{\Pr[w_i = 0 | \mathbf{y}, \mathbf{H}]} \right), \\ &= \log \left(\frac{\sum_{\mathbf{x}: w_i = 1} e^{-\|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \sum_j \log \Pr[w_j]} }{\sum_{\mathbf{x}: w_i = 0} e^{-\|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 + \sum_j \log \Pr[w_j]} } \right), \end{aligned} \quad (2)$$

where $i = 1, 2, \dots, n$. Transforming (2) into a tree-search problem and using the SD detection allows efficient computation of the LLRs [22, 23].

Let (3) denote the distribution of the searching candidates in the searching space,

$$\eta_{\text{SD}} = (\underbrace{1, \dots, 1}_{\eta_P}, \underbrace{Q, \dots, Q}_{\eta_Q}), \quad (3)$$

each of whose elements is the number of constellation symbols to be searched at each antenna. Here, $\eta_P + \eta_Q = M_t$. η_Q denotes the number of candidates, which are considered to be fully searched, and η_P denotes the number of candidates are not required to be searched. It is clear that if $\eta_Q = M_t$, the SD detection becomes the ML detection.

The search over bit possibilities within \mathbf{x} scales exponentially with the number of antennas M_t and the constellation size Q . In addition, the complexity of SD detection is very high when the number of bits mapped to the transmission vector and the constellation are large. Then, the complexity of the SD detection is the major problem for applying SD detection to MIMO systems with large number of transmit antennas. In the next subsection, we will describe that the LDMC is a subclass of LDPC codes and can reduce the complexity of the SD detection for MIMO systems.

2.2 Low-density MIMO codes

LDMCs are linear block codes which can be described by $\mathbf{P}\mathbf{w}^T = \mathbf{0}$, where \mathbf{P} is a parity-check matrix of n columns and m rows. Therefore, the overall code rate is $R = 1 - m/n$. The LDMC parity-check matrix can be described by two layers as

$$\mathbf{P} = \begin{pmatrix} \mathbf{P}_g \\ \mathbf{P}_e \end{pmatrix} = \begin{pmatrix} \mathbf{P}_g & & \\ \mathbf{P}'_e & \cdots & 0 \\ 0 & \ddots & 0 \\ 0 & \cdots & \mathbf{P}'_e \end{pmatrix}. \quad (4)$$

The first layer \mathbf{P}_g is a sparse parity-check matrix, while the second layer \mathbf{P}_e is defined by multiple, unconnected sub-codes \mathbf{P}'_e . Each sub-code \mathbf{P}'_e corresponding to \mathbf{w}_i has a code length $N'_e \leq M_t Q$. Let $N_g = n/N'_e$ denote the number of sub-codes in an LDMC codeword. The size of \mathbf{P}'_e is $q \times M_t Q$ and the size of \mathbf{P}_g is $(m - N_g q) \times n$.

As mentioned before, each transmission vector \mathbf{x} carries $M_t Q$ bits. It has to be guaranteed that all bits of a sub-code \mathbf{P}'_e are transmitted within one transmission vector \mathbf{x} . Thus, each transmission vector \mathbf{x} carries an embedded code \mathbf{P}'_e , i.e., $\mathbf{P}'_e \mathbf{w}_i^T = 0$.

It has been shown that, the SD detection achieves near-ML performance if $\eta_Q \geq \sqrt{M_t} - 1$ [19]. Therefore, it requires at least $2^{Q(\sqrt{M_t}-1)}$ times searching to achieve near-ML performance. With q constraints in LDMC-constrained SD detection, the number of searching in LDMC-constrained SD will downscale to $2^{Q(\sqrt{M_t}-1)-q}$ [15, 16].

3 LDMC design based on PEG algorithm

It was stated in [18] that large girths facilitate iterative decoding and impose a respectable minimum distance bound that enhances decoding performance. Among the existing approaches for constructing LDPC codes, one of the most successful approaches is PEG algorithm [17]. Recently, several PEG algorithms have been proposed [25–27], which can be applied to construct \mathbf{P}_e . For a given symbol node s_j , define its neighborhood within depth l , $N_{s_j}^l$, as the set consisting of all check nodes reached by a subgraph (or a tree) spreading from symbol node s_j within depth l . Its complementary set, $\bar{N}_{s_j}^l$, is defined as $V_c \setminus N_{s_j}^l$, or equivalently $\bar{N}_{s_j}^l \cup N_{s_j}^l = V_c$. Denote the symbol-degree sequence by

$$\mathbf{D}_s = \{d_{s_0}, d_{s_1}, \dots, d_{s_{n-1}}\} \quad (5)$$

in which d_{s_j} is the degree of symbol node s_j , $0 \leq j \leq n - 1$ and $d_{s_0} \leq d_{s_1} \leq \dots \leq d_{s_{n-1}}$. The PEG algorithm constructs a Tanner graph by operating progressively on symbol nodes to establish edges required by \mathbf{D}_s . To establish an edge incident to s_j , the PEG algorithm first spreads a tree from s_j up to maximum depth l and then chooses a check node c_i at random from the check nodes of the lowest degree in $\bar{N}_{s_j}^l$. In this section, we introduce a modified PEG algorithm to construct large girth LDMCs, which is referred to as PEG-LDMC algorithm and the corresponding codes as PEG-LDMCs in this paper.

Let \mathbf{D}_g and \mathbf{D}_e denote the degree sequence associated with \mathbf{P}_g and \mathbf{P}_e , respectively. The parity-check matrix \mathbf{P} of

Algorithm 1 High-level description of PEG-LDMC algorithm

Input: code length n , sub-code length N_e , parity length n , sub-code parity length q , the symbol-degree sequence \mathbf{D}_g and \mathbf{D}_e

for $k = 1$ to N_g **do**

 Construct \mathbf{P}'_e with the \mathbf{P}'_e -PEG algorithm and symbol-degree sequence \mathbf{D}_e .

for $j = k \cdot N'_e$ to $(k + 1) \cdot N'_e$ **do**

 Construct the j th column of \mathbf{P}_g with the \mathbf{P}_g -PEG algorithm and symbol-degree sequence \mathbf{D}_g .

end for

end for

Output: parity-check matrix \mathbf{P}

Algorithm 2 \mathbf{P}'_e -PEG algorithm

Input: sub-code length N'_e , sub-code parity length q , symbol-degree sequence \mathbf{D}_e

for $j = 0$ to $N'_e - 1$ **do**

if $j \leq q$ **then**

 Establish the edge (c_i, s_j) .

else

 Establish the edge (c_i, s_j) with the PEG algorithm.

end if

end for

Output: parity-check matrix \mathbf{P}'_e

LDMC can be constructed by the PEG-LDMC algorithm with the following steps.

Preprocessing process :

From the optimized degree distribution for the code rate $1 - (m - N_g q)/n$ and code rate $1 - q/N'_e$, generate the symbol-degree sequences $\mathbf{D}_g = \{d_{s_0}, d_{s_1}, \dots, d_{s_{(N'_e-1)}}\}$ and $\mathbf{D}_e = \{d_{s_0}, d_{s_1}, \dots, d_{s_{(N'_e-1)}}\}$, respectively.

Constructing process :

Step 1. Construct $q \times N'_e$ submatrix \mathbf{P}'_e of the form $\mathbf{P}'_e = [\bar{\mathbf{P}}'_e \mathbf{I}]$ with the PEG algorithm and symbol-degree sequence \mathbf{D}_e , where \mathbf{I} denotes an identity matrix of size $q \times q$ and $\bar{\mathbf{P}}'_e$ is of size $q \times (N'_e - q)$.

Step 2. Construct the columns of \mathbf{P}_g , which are in the same columns as \mathbf{P}_e in \mathbf{P} . If the construction of \mathbf{P} is not finished, go back to **Step 1**. Otherwise, stop the construction.

It is worth pointing out that in the PEG-LDMC algorithm, the submatrices \mathbf{P}_e and \mathbf{P}_g of the parity-check

Algorithm 3 P_g -PEG algorithm

Input: d_{s_j}
for $k = 0$ to $d_{s_j} - 1$ **do**

Expand a subgraph from s_j up to depth l under the current graph setting such that the cardinality of $N_{s_j}^l$ stops increasing but is less than m , or $\bar{N}_{s_j}^l \neq \emptyset$ but $\bar{N}_{s_j}^{l+1} = \emptyset$, then $E_{s_j}^k \leftarrow \text{edge}(c_i, s_j)$, where $E_{s_j}^k$ is the k th edge incident on s_j and c_i is a check node picked from $\bar{N}_{s_j}^l$ having the lowest check-node degree.

end for

Output: the j th column of \mathbf{P}_g

matrix \mathbf{P} are constructed simultaneously. Therefore, the girth of \mathbf{P} is optimized. A high-level description of the PEG-LDMC algorithm is given in **Algorithm 1** and the algorithms for steps 1 and 2 are given in **Algorithm 2** and **Algorithm 3**, respectively.

4 Analysis of detection complexity

In this section, we compare the detection complexity of the LDMC-constrained SD detection in the LDMC coded MIMO system with that of ZF and MMSE detections. To estimate the computational complexity, we use the number of multiplications required in the detection. Rough computational complexity estimations are given in Table 1. The number of additions is relatively small, therefore, it is omitted in the analysis.

Generally, SD is a searching algorithm for detection. It performs an exhaustive search based on setting a radius constraint. This has been proved by Hassibi [11] that the expected total number of points visited by the sphere decoding is proportional to the total number of candidates inside spheres of dimension $k = 1 \dots m$:

$$\omega = \sum_{k=1}^m \frac{\pi^{\frac{k}{2}}}{\Gamma\left(\frac{k}{2} + 1\right)^k}, \quad (6)$$

where d is radius and $\Gamma(n) = (n-1)!$ represents the Gamma function. Clearly, ω depends on the radius d . Therefore, the channel state information (CSI) estimation does not impact the complexity in SD.

Table 1 Number of multiplications in LDMC-constrained SD, ZF, and MMSE detections

Detection technique	Computational complexity
LDMC-constrained SD	$2^{Q(\sqrt{M_t}-1)-q}(M_t+2)$
Zero forcing	$2M_t^3$
MMSE	$2M_t^3$

Specifically, if SD is performed in an LDMC coded MIMO system, the norm $\|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2$ in the LDMC-constrained SD detection in (2) needs $2(M_t+2)$ multiplications. Thus, the total number of multiplications in the LDMC-constrained SD detection is

$$C_{\text{LDMC}} = 2^{Q(\sqrt{M_t}-1)-q+1}(M_t+2). \quad (7)$$

On the other hand, the ZF detection is represented by

$$\bar{\mathbf{x}} = (\mathbf{H}^H \mathbf{H})^{-1} \mathbf{H}^H \mathbf{y}, \quad (8)$$

and the MMSE detection is represented by

$$\bar{\mathbf{x}} = (\mathbf{H}^H \mathbf{H} + \sigma^2 \mathbf{I})^{-1} \mathbf{H}^H \mathbf{y}. \quad (9)$$

From the (8) and (9), it is clear that the MMSE and ZF detections consist of a complex inversion of $M_t \times M_t$ matrix, and some matrix multiplications and additions. $M_t \times M_t$ matrix inverse and matrix multiplication operations are both known to need M_t^3 multiplications. Consequently, the total number of multiplications in MMSE and ZF detections are both

$$C_{\text{MMSE}} = C_{\text{ZF}} = 2M_t^3. \quad (10)$$

Note that the computational complexity of linear detector mainly depend on M_t while the computational complexity of LDMC-constrained SD detection depends on M_t , Q , and q . If q is large enough, it is possible that the computational complexity of LDMC-constrained SD detection is lower than that of ZF and MMSE detections. Let $M_t^3 \geq 2^{Q(\sqrt{M_t}-1)-q} 2(M_t+2)$, we have

$$q \geq Q(\sqrt{M_t}-1) + 1 - \log_2 \frac{M_t^3}{M_t+2}. \quad (11)$$

If q satisfies condition (11), the computational complexity of LDMC-constrained SD detection with near-ML performance can be lower than that of ZF and MMSE detections. From Fig. 1, we can see that the complexity of the LDMC-constrained SD detection is lower than that of the MMSE and ZF detections if we choose q properly. Note that a larger q reduces the size of P_g of the LDMC matrix, which is constructed by the PEG algorithm. Among the existing approaches for constructing LDPC codes, the most successful one is the PEG algorithm. The LDPC code constructed by the PEG algorithm is one of the best codes of good error-correcting performance. Therefore, a larger q not only leads to worse error-correcting performance, but also lower SD detection complexity. Hence, there is a trade-off between performance and detection complexity by choosing the value q .

5 Efficient decoding algorithm

In this section, we proposed two new decoding algorithms for LDMCs for high speed decoding and fast convergence

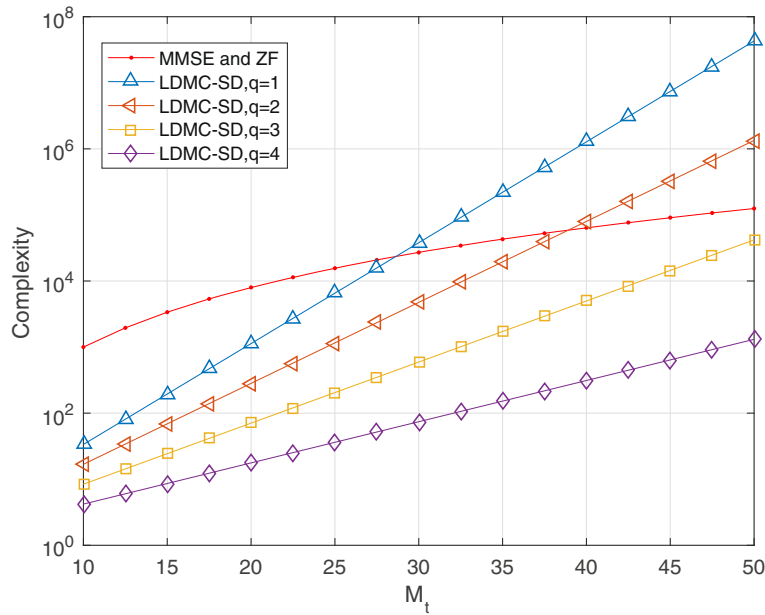


Fig. 1 Complexity comparison of MMSE, ZF, and LDMC-constrained SD detections for varying M_t and q

decoding. We denote the set of symbol nodes that participate in check node c_i by $N(i) = \{j : \mathbf{P}_{ij} = 1\}$, and the set of check nodes in which s_j participates as $M(j) = \{i : \mathbf{P}_{ij} = 1\}$.

The standard belief propagation (BP) decoding algorithm consists of initialization, check-node updating, symbol-node updating, stopping criterion test, and output steps [20]. In the proposed decoding algorithms, the initialization, stopping criterion test, and output steps remain the same as that in the standard BP algorithm, and therefore omitted here.

5.1 High-speed serial decoding

In LDMCs, the code length n can be divided into sub-codes \mathbf{P}'_e of length N'_e . In the high-speed shuffled decoding algorithm, the updating of sub-codes is processed sequential, but the updating of symbol nodes and check nodes corresponding to each sub-code \mathbf{P}'_e remain in parallel. Let r^l_{ij} and g^l_{ij} be the LLRs sent from check node c_i to symbol node s_j , and sent from the symbol node s_j to check node c_i , respectively, in the l th iteration.

In the standard BP algorithm, all value r^l_{ij} should be updated before updating all value g^l_{ij} . We observe that, since the sub-codes \mathbf{P}'_e in transmission vectors should not be connected to each other as shown by (4), all value r^l_{ij} for updating $g^{(l+1)}_{ij}$ of k th sub-code have already been updated before updating $r^{(l+1)}_{ij}$ of the $(k + 1)$ th sub-code, $1 \leq k \leq (N_g - 1)$. Therefore, the updating of $g^{(l+1)}_{ij}$ for k th sub-code can be computed in parallel with the

updating of r^l_{ij} for $(k + 1)$ th sub-code. In the high-speed serial decoding (HSSD), the check-node updating and the symbol-node updating of the HSSD are carried out alternately as follows.

Check-node updating corresponding to \mathbf{P}_g : for $1 \leq i \leq (m - N_g q)$ and each $j \in N(i)$, process

$$\tau_{ij}^l = \prod_{j' \in N(i) \setminus j} \tanh \left(\frac{g_{ij'}^{(l-1)}}{2} \right) \quad (12)$$

$$r_{ij}^l = \log \frac{1 + \tau_{ij}^l}{1 - \tau_{ij}^l}. \quad (13)$$

For $1 \leq k \leq N_g$, process jointly the following two steps.

- **Check-node updating:** for $k \cdot q \leq i \leq (k + 1) \cdot q$ and each $j \in N(i)$, process (12) and (13).
- **Symbol-node updating:** for $k \cdot N'_e \leq j \leq (k + 1) \cdot N'_e$ and each $i \in M(j)$, process

$$g^l_{ij} = L_j + \sum_{i' \in M(j) \setminus i} r^l_{i'j} \quad (14)$$

$$r^l_{ij} = L_j + \sum_{i \in M(j)} r^l_{ij}, \quad (15)$$

where L_j is the LLR of j th bit and initially set $L_j = (4/N_0)y_j$.

Note that compared to the serial BP algorithm, our algorithm has higher decoding speed without increasing the complexity.

5.2 Fast convergence shuffled decoding

In the HSSD algorithm, the check-node updating corresponding to \mathbf{P}_g should be done for only once in each iteration. To increase the convergence speed, we modified the HSSD and propose the fast convergence shuffled decoding (FCSD) algorithm in this subsection. In this decoding algorithm, the check-node updating corresponding to \mathbf{P}_g will be done at each time the check-node updating corresponding to sub-code is done. The check-node updating and the symbol-node updating of the FCSD are carried out as follows. For $1 \leq g \leq N_g$, process jointly the following two steps:

- **Check-node updating:** for $1 \leq i \leq (m - N_g q)$, $k \cdot q \leq i \leq (k + 1) \cdot q$ and each $j \in N(i)$, process (12) and (13).
- **Symbol-node updating:** for $k \cdot N'_e \leq j \leq (k + 1) \cdot N'_e$ and each $i \in M(j)$, process (14) and (15).

Note that compared to the high-speed serial decoding, this algorithm has faster convergence speed [21].

6 Simulation results

In this section, we compare the bit error rate (BER) performance of the PEG-LDMCs, LDMCs proposed in [17] and original LDMCs [16]. The PEG-LDMCs are constructed with the proposed PEG-LDMCs algorithm. The code rate is $R = 0.5$. The channel matrix \mathbf{H} is assumed to remain constant during the transmission of each codeword. We perform three outer-iterations between MIMO detector and LDPC decoder. In each outer-iteration, MIMO detection is performed followed by 40 inner-iterations inside LDPC decoder. The decoding process is halted if the decoder converges to a valid code or a maximum number of outer and inner iterations are reached. Note that in [16, 17], only the physical layer is considered. Therefore, for the sake of fairness, we have only considered the LDMCs of the same length as that of [16, 17], which are transmitted over the physical layer.

Figure 2 shows the BER performance of proposed PEG-LDMCs, LDMCs proposed in [17] and original LDMCs [16]. The transmission is over a 4×4 MIMO channel with 16-QAM and 64-QAM modulations. The first layer \mathbf{P}_g is of size 480×1920 and 480×2880 for each modulation, respectively. Therefore, the parity-check matrix \mathbf{P} of the corresponding LDMCs is of size 960×1920 and 1440×2880 for 16-QAM and 64-QAM. Thus, the code length is $n = 1920$ for 16-QAM and $n = 2880$ for 64-QAM, respectively. For the proposed PEG-LDMCs, the HSSD and FCSD algorithms are both applied for decoding. It can be seen that our proposed PEG-LDMCs with HSSD and FCSD algorithms have about 0.3 and 0.5 dB performance

gain compared to original LDMCs with 16-QAM modulation, and they have about 0.1 and 0.3 dB performance gain compared to LDMCs in [17] with 16-QAM modulation. The proposed PEG-LDMCs with HSSD and FCSD algorithms also have about 0.4dB and 0.6dB performance gain compared to original LDMCs with 64-QAM modulation, and they have about 0.15 and 0.35 dB performance gain compared to LDMCs in [17] with 64-QAM modulation. This is due to the reason that the girth of the PEG-LDMC is optimized globally by the PEG-LDMC algorithm and the FCSD has faster convergence speed. Therefore, the performance of PEG-LDMCs with FCSD algorithm is better than that of PEG-LDMCs with HSSD algorithm and original LDMCs in [16].

Figure 3 shows the BER performance of proposed PEG-LDMCs, LDMCs proposed in [17] and original LDMCs. The simulations are under 4×4 MIMO and 16×16 MIMO with 16-QAM modulations. For the proposed PEG-LDMCs, the proposed HSSD and FCSD algorithms are also applied for decoding. It can be seen from Fig. 3 that our proposed PEG-LDMCs with HSSD and FCSD algorithms have about 0.5 and 0.6 dB performance gain compared to original LDMCs over a 16×16 MIMO channel, and they have about 0.1 and 0.3 dB performance gain compared to LDMCs in [17] over a 16×16 MIMO channel. This is due to the reason that the performance of LDMCs depends on the girth, and our proposed new modified PEG algorithm can construct PEG-LDMCs with a girth of 8, which is larger than that of LDMCs proposed in [17].

7 Conclusions

In this paper, we have introduced the PEG-LDMC algorithm to construct LDMCs of large girth. In order to reduce the complexity of detection, SD detection has been adopted into LDMC coded MIMO systems. The complexity of LDMC-constrained SD detection has been analyzed and compared to that of MMSE and ZF detections. Two new decoding algorithms have also been proposed for high-speed decoding and fast convergence decoding. The simulation results have shown that the proposed PEG-LDMCs with new decoding algorithms achieved better BER performance than that of LDMCs proposed in [17] and original LDMCs in [16].

8 Methods/Experimental

The purpose of this work is to reduce the detection complexity in the MIMO systems and to achieve a good BER performance. For this purpose, we use the method which is referred to as LDMC-constrained SD detection. Since LDMCs with large girth have good performance, we propose a new modified PEG algorithm to construct large girth LDMCs. In this

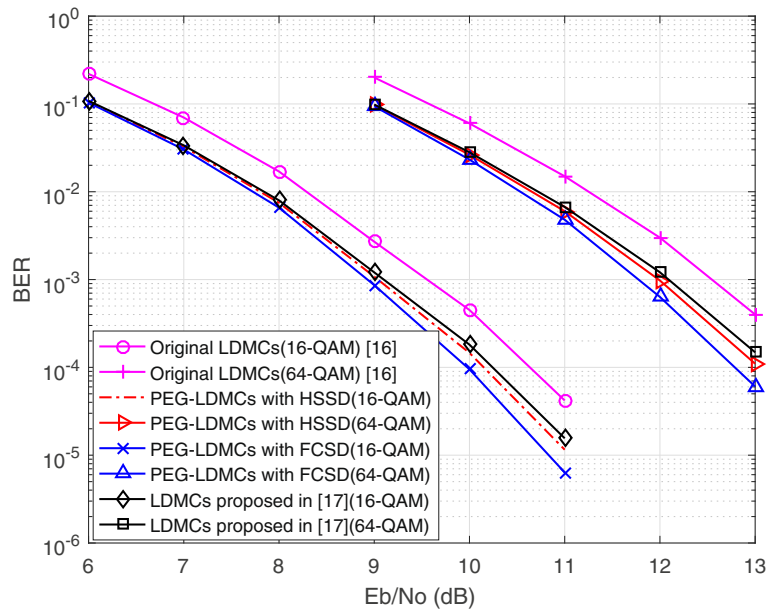


Fig. 2 BER performance comparison of PEG-LDMCs, LDMCs proposed in [17] and original LDMCs in [16] with 16-QAM and 64-QAM

paper, we analyze the complexity of SD detection in the LDMC coded MIMO systems, and compare it to ZF detection and MMSE detection. Furthermore, we propose high-speed serial decoding and fast convergence shuffled decoding in order to improve the BER performance.

In this paper, the comparison of BER performance among the PEG-LDMCs, original LDMCs

[16], and LDMCs proposed in [17] is presented. The PEG-LDMCs are constructed with the proposed PEG-LDMCs algorithm. The function to generate the LDMCs and proposed PEG-LDMCs algorithm for MIMO systems can be made by MATLAB code. Experimental results in this paper had performed by using MATLAB R2016a on Intel Core i7-4790 @ 3.60GHz platform.

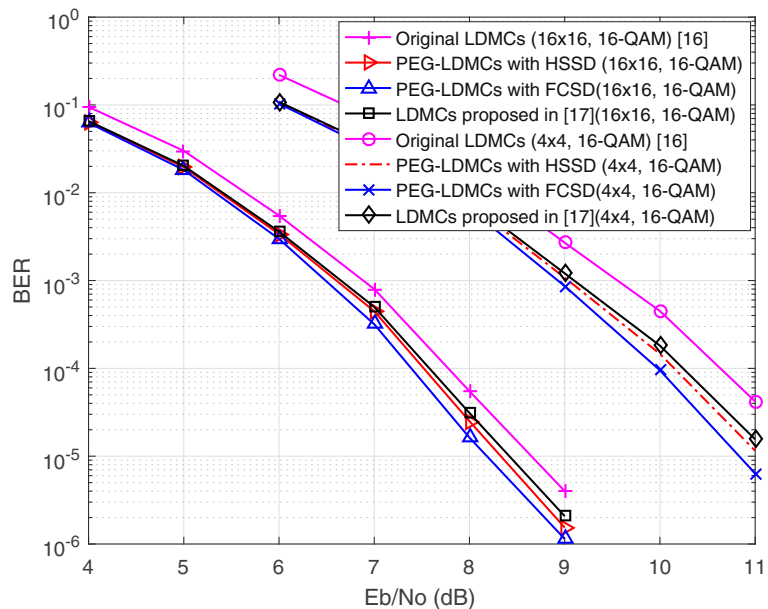


Fig. 3 BER performance comparison of PEG-LDMCs, LDMCs proposed in [17] and original LDMCs in [16] with 4 x 4 MIMO and 16 x 16 MIMO

Abbreviations

BER: Bit error rate; BP: Belief propagation; CSI: Channel state information ; FCSD: Fast convergence shuffled decoding; HSSS: High-speed serial decoding; LDMC: Low-density MIMO code ; LDPC: Low-density parity-check; LLR: Log-likelihood ration; MIMO: Multiple-input multiple-output; MMSE: Minimum mean-square error ; PEG: Progressive edge-growth ; SD: Sphere decoding ; ZF: Zero-forcing;

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Availability of data and materials

All data are fully available without restriction.

Authors' contributions

HH and XQJ contributed to the main idea, PEG based algorithms and wrote the manuscript. PS and SC designed and carried out the analysis and simulations. MHL and HJ reviewed and edited the manuscript. All authors read and approved the final manuscript.

Competing interests

The authors declare that they have no competing interests.

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