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On the bindings in AB M phases

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Abstract

A decisive stability argument for borides is afforded by the influence of the spatial correlation of the electrons on the bonding. The analysis of the relations between electron numbers and stability suggests that more electrons take part in the bonding than merely the electrons outside the peripheral closed shell. Furthermore, it may be assumed that electrons belonging to different bands may accommodate to one and the same correlation lattice (collective binding). These assumptions and the earlier rules of the plural correlations model allow to assign to most borides simple bonding types (bindings) which express intrastructural and quasihomologic numero—metrical relations providing useful interpretations of the stability. These relations are empirical rules being valid in the field of numerical data of crystal structures and conveying intermediary results of the systematic crystal chemistry.

Introduction

The crystal data of AB_M phases (borides) have been reviewed by 54Kie, 63Now, 64Ada, 64Sch, 65Aro, 67Gol, 67Hoa, 69Tho, 71Eck, 72Now, 72Pea, 73Gre, 75Wel, 76Spe, 77Lun, 77Now, 77Spe, 85Vil, 86Mas. With respect to these reviews, in the present study the references to structural communications are replaced by Structure Reports references for the sake of brevity. These reviews also permit the restriction of lattice—constant data to two decimals of an $\rm \AA$.

The assignment of bonding types (bindings) to the phases is not yet in an advanced state. It is well known that boron very rarely forms an anion, so that Lewis' rule of octet completion applies only where B is a cation. In the remaining borides various special rules

have been reported, for instance the formation of characteristic simple partial structures of B (54Kie), or the rule that the CaB₆ type occurs for $A^{1...3}$ but not for $A^{4...10}$. Such special rules may be formulated as relations between the structure of a phase and its electron numbers. They have not yet been appreciated much because the two-electron bond concept of molecular chemistry as applied in crystal chemistry tends to obscure the energetical cause of the rules, namely the lattice like property of the electron spatial correlations (64,83, 86Sch). Furthermore, this bond concept hampers the recognition that electrons below the valence bands have some influence on the bonding. These views have been applied in recent discussions of bindings in AB_M phases (79,82Sch). However, continued binding analyses uncovered additional valence rules suggesting various changes of binding proposals. For example one of these rules proposes that the correlation b of the valence electrons, and the correlation c of the peripheral core electrons may obey the same correlation lattice $q=b_{-}e$ (collective correlation). This phenomenon simplifies the binding analysis and the reading of binding formulae. If d electrons take part in b it may be written $b' = b \cdot e$, and if d or f electrons take part in c it may be written c' = c - f. Therefore q may also be equal to b'-c'. The collective correlations do not necessarily cause a highly uniform electron density as may be inferred from the example 83Sch Fig.1.

In the following the present state of the interpretation of borides is described. However, there is no doubt that additional valence rules will be found later on and make necessary a further revision of the binding proposals. In the subsequent text the brackets behind the crystal cell a contain the numbers of electrons per a for the various bands; the earlier added "N=" is omitted for brevity. Behind the prototype of a phase name, a previous quasihomologic isotype may be added to refer to additional structural remarks. For further abbreviations and formal conventions see 86,87,88Sch. Since the search for a binding interpretation is a search for hypotheses explaining observations, each proposal must be considered as a possibility. However, in order to simplify the presentation it is frequently described here as a fact. While a binding proposal for a crystal with a small cell is frequently quite plausible, a proposal for a crystal with a large cell is necessarily less certain. The assingment of bindings to the borides is now examined.

Analysis

It may be appropriate to consider briefly the structures of B before inquiring for bindings of borides. The B structures should be seen in conjunction with the structures of Be and C.

Be.r(Mg,H2,SR1.40,23.46), the room temperature phase of Be, may have the binding (see 82Sch1) $a[4+4=8]=H2.29;3.58\mathring{A}=b_{\text{CH}}\times(1;3.8/3)=c_{\text{CH}}\times(2;3.8/2)$, where a is the cell matrix of Be.r, [4+4=8] contains the numbers of electrons per a in the valence band b and in the core electron band c and also their sum, H... \mathring{A} is the abbreviated notation (86Sch) of the numerical value of a, b_{CH} is the cell of the b correlation, being cubic primitive (C), in hexagonal aspect (H), c_{CH} is the tetragonal bodycentered isometric correlation (U) in H-aspect and somewhat contracted along the quasihexagonal axis (*), (1;3.8/3) and (2;3.8/2) are commensurability matrices in abbreviated notation; the multiplication crosses x will be omitted below, and [] will be replaced by (). The observation that the number of b sites per a is 3.8, instead of 4, indicates that the b and c correlations form a collective correlation, $b \sim c = g$, obeying $a = g_{\text{CH}}(2;3.8/2)$ and thus yielding the number of g sites per atom $N_{\text{S}}^{\text{A}}(g) = 7.6$. The \tilde{U}_{H} type is no longer isometric like U_{H} , but provides an improved spin compensation. However, another interpretation is $a = g_{\text{H}}(\sqrt{3};3)$ yielding $N_{\text{S}}^{\text{A}}(g) = 4.5$. With respect to the spins, g_{H}^{A} must be twinned in a.

Be.h(W,SR23.45) yields $a(4,4)=2.55\text{\AA}=b_F(1)=c_C(2)$ or $a=g_B(2)$ with $N_{S(g)}^{/\Lambda t}=8$, being greater than 7.6 of r, conforming to the rule of site numbers (86Sch). It might be suspected that a correlation $a=g_B(2)$ would cause a uniform electron density. That this is not the case may be seen, as noted above, from Fig.1 in 83Sch or Fig.1 in 86Sch. An alternative pro-posal is $a=g_F(\sqrt{2};1.4)$ with $N_{S(g)}^{/\Lambda t}=5.5$.

C.r(H4,SR1.28,drw64Sch.180) is composed of close packed a layers in which every third atom is missing. $a(16,8) = H2.46;6.71 \text{Å} = b_{\tilde{F}H}(\sqrt{3};6/3) = c_{\tilde{C}H}(\sqrt{3}.12/3)$ (82Sch1) or $a = g_{\tilde{C}H}(\sqrt{3};12/3)$ with $N_{S(g)}^{/At} = 9$. The contraction of b and c to $g_{\tilde{C}H}$ instead of to $g_{\tilde{B}H}$ as in Be.h becomes possible by the loose packing. The high b electron number causes the lacunae in the a layers and the support number 1 of the a layer stacking. Because of the low occupation of g its cell is compressed, while a is strained in a_3 direction. For C.hp₂(F2,SR1.46) comes $a(32,16)=3.57 \text{Å} = b_{\tilde{F}}(2)=c(4)$ (82Sch1), or $a=g_{\tilde{C}}(4)$ with $N_{S(g)}^{/At}=8$

being smaller than 9 of r because of the high pressure. The reason why also here $g_{\mathbb{C}}$ occurs instead of $g_{\mathbb{R}}$ in Be lies in the higher b concentration.

B.h₁(R12,SR23.270,drw 64Sch.178) is formed at 800...1200°C and is composed of close packed layers parallel to a_1, a_2 in which every forth atom is missing. While in C.r there are layers parallel to a_1, a_2 with weakly occupied g sites, in this structure there are strings parallel to a_3 with weakly occupied g sites. Just as in C.r foreign atoms may enter the empty layers, here the empty strings may be filled by foreign atoms (B₄C). Just as in C.r the atom layers keep distant from the empty layers, here the atoms recede from the empty strings to form B₁₂ icosehedra. This must be understood as a first step towards molecule formation as in N₂O₂ etc. In the weakly occupied regions no e electrons may be found, only e electrons. In the strongly occupied regions the e electrons are an essential stabilizing factor. To be sure the empty strings are not infinitely extended but the B₁₂ are in a F_H packing, e a(108,72)=H4.91;12.57Å=e b_H(e12;9)=e c c H(e12;24/3) or e15.e16 are in a F_H e26. Another probable binding is e26. e3. Another probable binding is e4.

B.r(R105,SR35.127,38.37,43.34,drw67Hoa,73Gre.677) is said to be stable at room temperature (73Gre). $a(945,630) = H10.94;23.81 \text{Å} = g_{CH}(\sqrt{49};37/3), N_{S(g)}^{/At} = 5.7$. Because of the high number of atoms per cell the binding must remain tentative.

B.h₂(T190,SR44.34,45.41,drwSR43.6) was obtained by decomposition of purified BBr₃+H₂ on Ta filament at 1200°C (79Vla). It is closely httpc to AlB₁₂.r. a(570,380) = 10.14,14.17Å= $g_C(9;13)$, $N_{S(a)}^{/At}$ =5.5.

"B(T50,SR15.137,22.211,drwSR22.212)" is in reality $^{\mathrm{B}}_{50}\mathrm{C}_2$ or $^{\mathrm{B}}_{50}\mathrm{N}_2$ (SR38.39,40.38, 42.52).

It is well known that the B phases belong to the most complicated structures of the chemical elements. The bindings proposed can therefore only be a first attempt to find the energetical reason for their structure. We now consider the borides.

In A^1B_M mixtures Lewis-phases are not expected since the compositions A_5^1B or A_3^1B do not provide a good Coulomb interaction. Therefore all stable phases are superborides. Furthermore, the low b electron contribution of A^1 causes that the A^1 cores are close together and do not give much room for B atoms. Only when the mole fraction of B is $N_B \ge 0.75$ compounds are formed.

Li(W,SR1.32), $u(2,4) = 3.51\tilde{\Lambda} = h_{B}(1) = g_{C}(2)$.

LiB₃(T4.12.84Mai) is a read semiconductor, filling-homeotypic to CaB₆ since the atomic volume fulfils $V_{\text{Ca}} = 2V_{\text{Li}}$. It is isodesmic to CaB₆, $a(4+36.32) = 5.98;4.19\text{Å} = g_{\text{B}}(\sqrt{18};3)$. The number of g sites per atom is $N_{\text{S}}(g) = 6.75$.

 $\text{Li}_6\text{B}_{19}(\text{H}6.19,84\text{Mai})$ contains B_6 octahedra bonded through corners. w(6+57,50) $\text{H}8.23;4.16\text{Å} = y_{\text{B}}(6;10;3), N_{\text{S}}^{/\text{At}} = 7,2$.

Li₃B₁₄(U12.56,84Mai) contains B₈ and B₁₀ polyhedra. a(24+336,272)=10.77;8.95Å= a(4+336,272)=10.77;8.95Å= a(4+336,272)=10.77;8.95Å=

NaB₆(73Gre, 77Mat).

NaB $_{15}$ (P2.30,SR35.39) is homeotypic to MgB $_{7}$ and contains B $_{12}$ icosahedra in H1 packing. Because of $V_{\mathrm{Na}} = V_{\mathrm{Mg}} + V_{\mathrm{AI}}$ the phase is homeotypic to MgAlB $_{14}$ (P2.2.28, SR35.4,drw ibid.). $a(4,212,128) = 5.85;8.42;10.30 \hat{A} = g_{\mathrm{R}}(4;6;7)$.

KB₆(CaB₆,71Eck) is a CsCl structure of K and B₆: $a(1,26,20)=4.23\text{Å}=g_{\text{B}}(3)$ where g=b-e-c-f. The assumption that there is not only a binding $a=(b-e)_{\text{C}}(3)$ (82Sch2) is supported by the stability of the isotypes CaB₆ and YB₆ having more electrons.

The bindings of Be.r and Be.h have been considered above. The phase "Be₅B"(SR 24.58) is in fact Be₄B(SR27.65).

Be₄B(T8.2,SR27.65,drw ibid.) is htpc to Be.h(W) with a=aBe.h($\sqrt{2}$:3). The lacunae caused by the higher electron contribution of B are neighbouring the B atoms. Since every B causes one lacuna the electron content as compared to Be is decreased. a(22,20)=3.37; $7.05\text{Å}=b_{\tilde{F}U}(2;5.5/2)=c_{\tilde{C}}(\sqrt{8};5.5)$ or $a=g_{\tilde{C}}(\sqrt{8};5.5)$. The little strain of the binding causes full occupancy of b and a small contraction of a in a_3 direction.

 $Be_2B.h(CaF_2,SR26.57)$, $a(28,24)=4.66\text{\AA}=g_C(4)$. The high g site number 5.4 seems to be the reason for instability at room temperature.

Be₂B₃(T24.36;73Ste), $u(156,120) = 7.25;8.46\text{Å} = b_{FU}(\sqrt{20};7.5/2) = g_{C}(\sqrt{40};7.5)$. The binding is tentative since the cell content is not yet certain; $N_{S}/At = 5$.

BeB₃(H27.82,SR39.27) contains icosahedra and other polyhedra, a(300,218) = H9.80; $9.53\text{Å} = b_{FH}(6;7/3) = c_{CH}(6;14/3) \text{ or } = g_{CH}(\sqrt{39};15/3) \text{ with } N_{S}^{/At} = 5.4.$

BeB₆(T28.168,SR26.57) is htpc to AIB₁₂, $a(560,392) = 10.16;14.28\text{Å} = b_{FU}(\sqrt{40};12) = g_{C}(9;12)$.

BeB $_{12}$ (T4.48.SR24.59), a(152;104) =8.80;5.08Å=gC(8:4.5). This phase is httpc to B $_{50}$ C $_2$ and B $_{50}$ N $_2$ (drwSR22.212) and displays a B $_{12}$ packing of the U type.

Mg(H2,SR1.40), a(4,16) =H3.21;5.21Å = $g_{\tilde{H}}(3;5)$. The high site number comes from the neighbourhood to Na.

MgB₂(AlB₂,SR17.71,drw64Sch.270) decomposes at 1600°C (77Spe). It contains B-layers parallel to a_1, a_2 of the graphite type, and displays an unusual axial ratio. a(2,14.6) = H3.08;3.52Å= $b_{CH}(1;2.75/3)$ = $c_{CH}(2;5.5/3)$ or simplified $a=g_{CH}(2;5.5/3)$. The g correlation is highly occupied and causes therefore the unusual axial ratio of a. Surprisingly AlB₂(H1.2,SR20.5) has a lower axial ratio, a(3,14,6)=H3.01;3.26Å= $g_{CH}(\sqrt{(13/3);5.5/3)}$ might be an interpretation for it. The commensurability in the basal plane has been changed from $2=\sqrt{(12/3)}$ to $2.08=\sqrt{(13/3)}$, see 86Sch.

MgB₄(O4.16,SR38.50,drw ibid.) decomposes at 1800°C (77Spe), it contains B_{2+4/2} pyramids forming chains in a₂ direction. $a(8,80,40)=5.46;4.43;7.47\text{Å}=b_F(1.25;1;1.75)=$ $g_C(5;4;7)$. The number of g sites per atom is 7 while it was 7.3 in MgB₂.

 $\label{eq:mgB7} {\rm MgB_7(P4.28,SR48.34,drw~ibid.)~contains~B}_{12}~{\rm icosahedra~in~H1~packing~and~six~B}_{12}~{\rm surrounding~one~Mg.~a(16,232,128)=5.97;8.13;10.48Å=$$g_C(5.5;7.5;9.5).}$

 ${
m MgB}_{12}$ (65Ell, but see 69Shu). The explanation of the constitution needs further work.

$$\label{eq:CaB4} \begin{split} \text{CaB}_4(\text{ThB}_4,\text{T4}.16,\text{SR26}.74,\text{drw64Sch}.273) \ \text{is htpc to CaB}_6 \ \text{with } a=a_{\text{CaB}_6}(2;1), \ \text{every second Ca cube is filled by a B}_2 \ \text{dumpbell.} \ a(8,80,64)=7.11;4.11\text{Å}=g_{\text{B}}(\sqrt{26};3). \ \text{The } g_{\text{C}} \ \text{of MgB}_M \ \text{becomes } g_{\text{B}} \ \text{because of higher number of } f \ \text{electrons involved.} \end{split}$$

 ${\rm CaB_6(C1.6,SR2.37,drw64Sch.273)}$ decomposes near to 2500°C (77Spe). a(2,26,20)= $4.15{\rm \AA}=b_{\rm B}(1)=g_{\rm B}(3)$. Below, it is found why ${\rm LaB_6(C1.6)}$ is stable but "HfB $_6({\rm C1.6})$ " not. Comparing the electron distance d_g with $d_b({\rm B.h})$ =1.4 ${\rm \AA}$ reveals that a strong compression of $d_b({\rm B.h})$ is caused by the core electrons of Ca. Since at lower B content the boron electrons tend to increase their distance, the g correlation is there not possible and intermediate phases are not longer stable.

 $SrB_6(CaB_6, SR17.63), \ a(2,26,22) = 4.20\text{Å} = g_B(3).$ $BaB_6(CaB_6, SR17.63), \ a(2,26,22) = 4.27\text{Å} = g_B(3).$

 $ScB_2(AlB_2,SR22.65,44.108)$ has a congruent melting point at 2250°C (cmp). $a(3,14,12)=H3.15;3.52 \hat{A}=b_{CH}(1;2.75/3)=g_{BH}(2;11/3)$. The phase is isodesmic to MgB_2 if the

participation of the Sc2sp electrons is disregarded. The influence of these celectrons can only be weak in the sense of 83SchFig.1. For the η_C part of the binding the site number is $\sqrt{\frac{\lambda_L}{SC}}$ -8. The less perfect commensurability element 11/3 has no influence since there is no possibility of stacking homeotypism.

ScB₄(73Gre).

 $ScB_6(CaB_6, 85Vil), u=4.44A=g_R(3).$

ScB₁₂(U1.12,SR30.116,44.100) is a Sc_{F1} structure with B₁₂ cubooctahedra in octahedral interstices. a(6,88,64)=5.22;7.35Å= $g_{\hat{\mathbf{B}}}(4;5)$. This binding is not compatible with a cubic UB₁₂ structure (SR12.34).

YB₂(Δ IB₂,MgB₂,71Eck), a(3,14,10+4)=H3.30;3.84Å=b_C(1;2.75/3)=g_{BH}(2;11/3). The participation of the B1s² electrons in g becomes possible because of the weaker attraction by the nucleus as compared with C,N,O.

 $YB_4(ThB_4, CaB_4, SR.30.31, 46.41, drw64Sch.237)$ cmp (77Spe), u(12,80,40+32) = 7.09; $4.01 \text{Å} = y_B(\sqrt{29}; 3)$. The phase is only homeodesmic to $CaB_4(ThB_4)$ because of its higher electron contribution.

YB₆(CaB₆,SR17.63), $w(3,26,22)=4.11\text{Å}=g_{\text{B}}(3)$. The stability of the CaB₆ type with A¹,A²,A³, confirms the assumption of a collective binding. That the A²B₆ phases are semi-conductors while YB₆ is a metallic conductor (67Hoa) comes from the good fit of b in CaB₆.

YB₁₂(UB₁₂,F1.12,SR30.29,drw64Sch.273), $a(12,176,136)=7.50\text{\AA}=g_{\hat{\mathbf{B}}}(6;9/2)$. The commensurability to the structure in the basal plane is excellent and spin compensation is possible since $(g_{\hat{\mathbf{B}}})_3/(g_{\hat{\mathbf{B}}})_1 < \sqrt{2}$.

 ${
m YB}_{66}({
m F6.396,SR34.43;drw}$ ibid.) is an intermediate phase containing many ${
m B}_{12}$ icosahedra. a(72,4944,3408) =23.44Å = $g_{
m B}(16;17)$. Because of the high electron number the proposal is tentative.

LaB₂(73Gre).

 $LaB_4(ThB_4, CaB_4, SR6.75), \ n(12,80,72) = 7.32; 4.18 \hat{A} = g_B(\sqrt{29}; 3).$

 $LaB_6(CaB_6,SR26.74)$ cmp (77Spe), $a(3,26,22)=4.16 \text{\AA} = g_B(3)$. For "HfB₆" would come a(4,26,26), this phase cannot be stable therefore. A review of LnB_M phases is found in 76Spe. The crystal chemistry of these phases provides the possibility to analyse the

influence of the filling of the 4f shell. For instance ${\rm HoB_6(CaB_6,SR23.61)}$, u(3,26.22) is stable while "ErB₆(CaB₆)", u(3,26.23) could not be prepared (76Spe). Also "TuB₆" and "CpB₆" could not be prepared (76Spe). This shows that the limit of stability lies at $N_{b+\epsilon+c+f}^{/a}$ =51. Complete filling of the g sites is not possible, since for optimum position of the g lattice with respect to B₆ one g site coincides with the La nucleus.

In the mixture TiB $_M$ the intermediate phases are no longer restricted to the mole fractions $N_B'>0.66$, as in $A^{1...3}B_M$. This must be caused by the Ti3d⁴ electrons which more strongly separate the Ti cores so that B atoms may easier enter the structure. The intermediate phases thus occur in all parts of the mixture and the bindings must be compatible with the bindings assumed for Ti. For Ti.h(W,SR4.84,13.148) was proposed (82Sch1) $a(8, 16)=3.31\text{Å}=b_{\text{B}}(1)=e_{\text{C}}(2)=e_{\text{F}}(2)$. Here $e_{\text{F}}(2)$ appears questionable since it does not provide good spin compensation. A collective binding fitting to this proposal might be $a=g_{\text{C}}(\sqrt{8};2.8)$. However, this would suffer from slight overoccupation. Therefore it may be assumed $a=(8,16,16)=g_{\text{B}}(\sqrt{8};2.8)$ so that $N_{\text{S}}^{/\text{Al}}=22$ being appropriate up to Cr. For Ti.r(Mg, SR1.53) comes a(8,16,16)=H2.95; $4.68\text{Å}=g_{\tilde{\text{H}}}(3;5)$. This binding is nearly fully occupied, and the matrix element 5 favours the Mg type stacking.

 ${\rm Ti}_2 B ({\rm FhtpMg,SR12.34})$ is httpc and hdmc to Ti.r, see ${\rm Ti}_4 N, {\rm Ti}_6 O, {\rm Ti}_3 O$. $u(24,57.54) = {\rm H5.95;4.79 \AA} = g_{\tilde{\rm H}}(6;5)$. This favours the Mg type stacking of Ti layers following rules of 84Sch.

"Ti2B(T,SR18.67)" was doubted (65Ell).

TiB(FeB,O4.4,SR18.69,drw64Sch.265) displays parallel to a_1, a_2 a quadratic Ti-net, like as in TiC(NaCl), but pleated, so that it allows the formation of B-chains. The separate B-B bonding, earlier discussed by 54Kie, may be caused by the fact that the B2sp electrons do not fit as well into the Ti3sp electron correlation as the C2sp electrons. In ABe_M-phases the formation of Be₁₃ icosahedra may have a similar reason. However, the binding to be proposed now still reveals another cause: $a(16,44,40) = 6.12;3.06; 4.56\text{Å} = b'_{\hat{B}}(2\sqrt{2};\sqrt{2};1.88) = g_{\hat{B}}(4\sqrt{2};2\sqrt{2};3.75)$ with the site number $N_{\hat{S}}^{T\hat{I}}(g) = 30$ while in TiC(NaCl), $a = 4.33\text{Å} = g_{\hat{B}}(4), N_{\hat{S}}^{T\hat{I}}(g) = 32$. From this proposal may be seen that a sufficent occupation of b' = c' is more important than a full occupation of b'. The participation of f electrons makes possible the homeodesmism $g_{\hat{B}} = g_{\hat{B}}$ as $g_{\hat{C}} = g_{\hat{C}}$ is less favourable. The strain $\hat{B} = \hat{B}$ disturbs the com-

mensurability found in TiC. The generated dipole vectors in u_3 direction at Ti favour the pleating of the quadratic Ti-nets and hence the formation of B-chains,

Ti₃B₄(Ta₃B₄,P3.4,71Eck,drw64Sch.263) contains double chains of B or hexagon tapes, the quadratic Ti-nets are not pleated but slightly strained for structural reasons. $a(24.72.64) = 3.26;13.73;3.04 \hat{A} = b_B(\sqrt{2};6) = g_B(\sqrt{8};12)$. Like as in TiB, $g_{C^1}g_B$ is fully occupied by b-c. Since there are 6 Ti layers parallel to a_1,a_3 , dipole vectors are not formed and pleating is not possible. The strong decrease of d_g as compared with TiB presumably indicates that g has more the property g_C than the property g_B .

TiB₂(AlB₂,SR13.46) has a congruent melting point at 2790°C (cmp 2790°C), a(4,14,12)=H3.03;3.23Å= $g_{\tilde{\mathbf{B}}}(\sqrt{8};4.5)$ as written for $a_{\tilde{\mathbf{Q}}}$. It would be of interest whether at low temperatures a structural transformation occurs. Another probable interpretation is $a=g_{\tilde{\mathbf{B}}\mathbf{H}}(2;9/3)$. The striking strain of $\hat{\mathbf{B}}_{\mathbf{H}}$ must be caused by a special spin distribution.

$$\label{eq:tight} \begin{split} &\text{Ti}_2\text{B}_5(\text{W}_2\text{B}_5;\text{H4.10,SR16.33,drw64Sch.270}) \text{ is a filling htp of AlB}_2. \ \textit{a}(\text{16,62,52}) = \\ &\text{H2.98;13.98} \\ \mathring{\text{A}} = &g_{\text{BH}}(2;45/3). \end{split}$$
 The energetic advantage against TiB_2 is the integral value $(g^{-1}a)_{33} = 15$ whithout a strain $\hat{\text{B}}_{\text{H}}$.

 $Ti_2B_{50}(T2.50)$, SR41.40, drw ibid.), $a(8,166,116) = 8.83; 5.07 Å = g_B(\sqrt{45}; 3.9)$, see $B_{50}C_2$. ZrB.ih(NaCl, SR 16.34), $a(16,44,48) = 4.65 Å = g_B(4)$. Strikingly, the NaCl type is avoided in borides. If the impurity is N or O then the isodesmism to ZrC is favoured.

 ${\rm ZrB_2(AlB_2,SR16.34)},~a(4,14,10+4)={\rm H3.17;3.53}\mathring{A}=g_{\rm BH}(2;11/3).$ The low occupancy indicates that the f correlation is not very important. If here also $a=g_{\rm BH}(2;9/3)$ is assumed then the full occupation of $b^* \sim c$ is attained.

ZrB₆(73Gre).

 ZrB_{12} .h(UB₁₂,F1.12,SR16.35,drw64Sch.273), a(16,176,136) = 7.41Å= $g_{\hat{\mathbf{B}}}(6;9.2/2)$.

HfB.i(NaCl,SR17.70), $a(16,44,64) = 4.62\text{Å} = g_B(4)$.

HfB(FeB,71Eck), $a(16,44,64) = 6.50; 3.21; 4.83 \text{Å} = b_{\hat{\mathbf{B}}}(2\sqrt{2}; \sqrt{2}; 1.9) = g_{\hat{\mathbf{B}}}(4\sqrt{2}; 2\sqrt{2}; 3.75)$. Remarkably the g correlation is slightly overoccupied.

 $HfB_2(AlB_2,SR17.69), \ a(4,14,18) = H3.14; 3.47 \text{Å} = g_{\tilde{B}H}(2;9/3).$

HfB₁₂(UB₁₂,85ViI), $a(16,176,152) = 7.38\text{Å} = g_{R}(6;10/2)$.

V(W,SR1.56,26.275), $a(10,16,16) = 3.02\text{Å} = g_{\text{B}}(\sqrt{8};2.8)$.

V₂B(73Gre).

 $V_3B_2(U_3Si_2,T6.4,SR23.72,drw64Sch.252)$ contains W and AIB_2 elements, the B combine to pairs displaying thus a specific interaction of the light atoms which appears less developed in AC_M phases. u(30,60,56) –5.75;3.03Å – $y_B(\sqrt{29};2.8)$, the phase is closely homeodesmic to V. The tetragonal V_3B_2 suggests twinning of y_B in V.

VB(TII,O2.2,SR23.72,drw64Sch.263) is a shear htp of NaCI permitting all B to condense to chains. $u(20,44,40)=3.06;2.97;8.04\text{Å}=g_{\text{B}}(\sqrt{8};7.5)$. Remarkably the b-c correlation does not find place in the g_{C} part of the g_{B} correlation providing only 60 sites. This indicates that g_{C} does not accept all b electrons and that in slight deviation from Hunds rule only V3d⁴ electrons have a +spin while one V3d¹ electron has a -spin. It becomes clear that V2sp electrons weakly take part in g_{B} , because they make it possible that a g_{C} correlation of one spin direction is formed. The unoccupied sites of g_{B} are remote of the atom cores. In a there are 4 approximately equidistant V layers parallel to a_1,a_2 , and 15 g_{B} layers. It may easily be seen that this favours the shear since it causes two neighbouring V layers to have the same momentary electro dipole component in a_3 direction.

 $V_5B_6(QS.6.69Spe,drw\ ibid.)$ is closely htpe to VB, it contains 10 V-layers and 6 non-equidistant shear planes parallel to the smallest cell-face. Since a shear plane contains B zigzag chains, in the closely neighbouring shear planes a tape along a_3 of B-bexagons sharing edges is formed (see Ta_3B_4 in 64Sch.263). a(40+10.116.104)=3.06;21.25;2.97Å= $g_B(\sqrt{8};20)$. The correlation $g_C(g_B)$ is nearly filled by $b^+ c$ where $N_b^a = 40$ and the + sign refers to the spin.

 V_3B_4 (Ta₃B₄,P3.4,SR20.56,drw64Sch.263) contains 6 V-layers, 4 shear planes, and two B-hexagon tapes. $a(24+6,72,64)=3.03,2.99;13.18 \text{Å} = g_{\hat{B}}(\sqrt{8};12)$. The $g_{\hat{B}}$ correlation is strained to reach the good commensurability as in Ti₃B₄. The V_3B_4 phase is homeodesmic and heterotypic to TiC.

 $V_2B_3(Q4.6,69Spe,drw ibid.)$ contains 8 V-layers and 2 double tapes of B-hexagons. $a(32+8,100,88)=3.06;2.98;18.40\text{Å}=g_{\hat{\mathbf{B}}}(\sqrt{8};16)$. The B type is more strained to conserve the good commensurability.

VB₂(AlB₂:SR12.36) has a congruent melting point (cmp), u(5,14,12) =H3.00;3.06Å = $g_{\rm BH}(2;10/3)$ or $a_{\rm Q}(10,28,24)$ =3.00;3.06;5.20Å = $g_{\rm B}(\sqrt{8};5)$. The commensurability per V layer has jumped from 2 in V₂B₃ to 2.5 in VB₂.

Nb(W,SR1.56), $n(10,16,20) = 3.30 \text{Å} = q_D(\sqrt{8};2.8)$.

 $N_{53}B_{2}(U_{3}Si_{4},V_{3}B_{2},SR23.71)$, $s(24+6.60,68)=6.19(3.29A+g_{B}(\sqrt{29}(2.9))$. The g_{C} correction is filled by h^{+} .c.

NbB(TII,VB,SR23.71), $a(16+4.44.48) = 3.30(3.16(8.72A = y_B(\sqrt{8};7.5).$

 $\mathsf{Nb_3B_4}(\mathsf{Ta_3B_4},\mathsf{V_3B_4},\mathsf{SR\,13.42}),\ \omega(24+6,72,76) = 3.30; 3.14; 14.07 \text{Å} = q_{\hat{\mathbf{B}}}(\sqrt{8};12).$

 $NbB_2(AlB_2, VB_2, SR12.36), \ u(4+1, 14, 14) = 113.11; 3.27 \mathring{A} = g_{BH}(2; 9/3),$

Ta(W,SR1.57,15.121), $a(10,16,28) = 3.30\text{Å} = g_D(3)$.

 ${\rm Ta_2B.h(CuAl_2,U4.2,SR26.80,drw64Sch.299)},~~a(70,76,120)=5.78;4.86 \begin{align*} A=g_{\rm B}(\sqrt{26};4.3),~~g \end{align*}$ is here and in the next three phases somewhat overoccupied, perhaps the f band donates electrons to a lower band, or a separate b correlation is formed.

 $Ta_3B_2(U_3Si_2, V_3B_2, SR23.71), \ a(24+6,60,92) = 6.18;3.29 \mathring{A} = g_{12}(\sqrt{29};2.9).$

 $TaB(TII,VB,SR12.32)cmp,\ a(16+4,44,64)=3.28;3.16;8.67\tilde{A}=g_{\tilde{B}}(\sqrt{8};7.5).$

 ${\rm Ta_3B_4(P3.4,V_3B_4,SR12.32)},\ a(24+6,72,100)=3.28;3.13;13.98 \\ {\rm \mathring{A}}=g_{\rm \mathring{B}}(\sqrt{8};12).$

 $TaB_2(AIB_2, VB_2, SR12.32)$ emp, $u(4+1, 14, 18) = H3.10; 3.23 Å = <math>y_{BH}(2; 10/3)$.

Cr.h(W,SR1.61, 20.68), $a(12,16,16) = 2.89 \text{Å} = g_R(\sqrt{8};2.8)$.

Cr.r(T28,SR23.113), $a(168,224,224) = 2.88;40.30\text{Å} = g_{\hat{\mathbf{R}}}(\sqrt{8};39).$

CrB_{0.2}(FhtpMg,SR21.56), $a(12,17.5,16.5) = H2.58:4.45 \text{Å} = g_{BH}(\sqrt{3};15/3)$. The slight overfilling may be removed by a little change in the mole fraction N_R .

 ${\rm Cr_4B(Mn_4B, S8.2, SR\,17.67, drw64Sch.254)}$ contains parallel to the smallest cell face quasihexagonal layers as in ${\rm CuAl_2(110)}$. These layers are sheared against one another. a(192,280,272) =4.26;7.38;14.71Å. For the isotypic ${\rm Mn_2B_{0.98}}$ a tentative proposal is noted.

 ${\rm Cr_2B(CuAl_2, Ta_2B.h, U4.2, SR\,17.67, drw64Sch.299)}, \ u(48, 76, 72) = 5.19; 4.32 \text{\AA} = \ y_{\hat{\mathbf{B}}}(5; 4).$

 $\text{Cr}_5\text{B}_3(\text{U}10.6,\text{SR}17.67,\text{drw}64\text{Sch}.254)}$ appears intermediary between $\text{Cr}_2\text{B}(\text{CuAl}_2)$ and $\text{V}_3\text{B}_2(\text{U}_3\text{Si}_2)$ and contains 4 filled Cr layers, $a(120,196,184) = 5.46;10.64\text{Å} = g_{\text{B}}(\sqrt{26};10)$.

CrB.h(TII,VB,SR12.30), $a(24,44,40) = 2.97; 2.93; 7.86 \text{Å} = y_{\text{R}}(\sqrt{8}; 7.5).$

CrB.r(MoB,U4.4,SR39.107,drw64Sch.263), $a(48,88,80) = 2.94;15.72 \text{Å} = g_{\tilde{\mathbf{B}}}(\sqrt{8};14)$. The structure has 8 Cr layers parallel to a_1, a_2 and 4 shear planes as compared to the NaCl type. The proposal is not certain because of MoB.r and WB.r. Perhaps a separate b is precipitated.

 ${\rm Cr_3B_4(Ta_3B_4,V_3B_4,P3.4,SR26.71)},\ a(36,72,64) = 2.99; 2.95; 13.02 {\rm \mathring{A}} = g_{\rm \mathring{B}}(\sqrt{8};12).$

 ${\rm CrB_2(AlB_2,SR12.36)},~a=$ H2.97:3.07Å. With respect to the homeotypism of ${\rm CrB_2}$ with the earlier phases (${\rm Cr_3B_4}$ etc.) it is of interest to consider the pseudotetragonal cells $a_{\rm O}(12.28.24)=2.97:3.07:5.14Å=g_{\bar{\rm B}}(\sqrt{8}:5)$. Alternatively $a=g_{\bar{\rm BH}}(2:9/3)$.

 ${\rm CrB_4(P1.4,SR33.46,drw\ ibid.)}$ contains ${\rm B_4 squares\ parallel\ to\ u_1,u_2,\ surrounded\ by\ six}$ Cr. u(12,40,32) =4.74;5.48;2.87Å= $g_{\rm R}(4;5;2.5)$ is a tentative proposal.

 $CrB_{41}(R8.328,SR35.34)$ is htpc to B.h(R12). u(48,1048,720) = H10.96;23.85Å.

Mo(W, SR1.61,24.88), $a(12,16,20) = 3.15 \text{Å} = g_{\text{R}}(\sqrt{34/4});2.9)$.

 $Mo_2B(CuAl_2, Ta_2B, h, SR11.52)$, $a(48,76,88) = 5.54; 4.74 \mathring{A} = g_B(\sqrt{26}; 4.3)$. The axial ratio $|a_3|/|a_1|(Mo_2B) = 0.86 > |a_3|/|a_1|(Cr_2B) = 0.83$ is an indication for the influence of the Mo3d electrons on the stability.

 $Mo_3B_2(U_3Si_2,V_3B_2,71Eck)$, $a(36,60,68)=6.00;3.15Å=g_B(\sqrt{29};2.85)$. The non-integral commensurability element 2.85 might cause very distant shears with plane a_1,a_2 .

MoB.h(TII,VB,SR11.51), $u(24,44,48) = 3.16;3.08;8.61 = g_{\hat{R}}(\sqrt{8};7.5)$.

MoB.r(U4.4,CrB.r,SR16.31), $a(48,88,96) = 3.10;16.95\text{Å} = g_R(\sqrt{8};14.5)$.

 $MoB_2(AlB_2,SR16.32)$, $a(4+2,14,14) = H3.04; 3.06 Å = g_{BH}(2;9/3)$. The low occupation is only in the partial correlation occupied by the felectrons.

$$\label{eq:mo2B5} \begin{split} \text{Mo}_2\text{B}_5(\text{R2.5}, \text{SR11.49}, \text{drw64Sch.270}) \text{ is closely httpc to } \text{W}_2\text{B}_5 \text{ and } \text{Ti}_2\text{B}_5(\text{W}_2\text{B}_5), \ a(36.93,90) = \text{H3.01}; 20.93 \text{Å} = g_{\hat{\mathbf{R}}\mathbf{H}}(2;60/3). \end{split}$$

 ${
m Mo_{0.8}B_3(H(3.2).12,SR39.39)}$, has a filled B site set as in ${
m MoB_2}$ while the corresponding Mo site set is only partially occupied. a(19,62,56) =H5.20;6.35Å = $g_{\tilde{C}H}(\sqrt{12;12/3})$. The similarity of a to $a({
m WB_4})$ suggests that both structures need confirmation.

MoB₁₂(73Gre).

W(B1,SR1.61,24.88), $a(12,16,28)=3.17\text{Å}=b_{\text{B}}(1)=(e\circ e')_{\text{B}}(3)$. The slight overfilling of $a=g_{\text{R}}(3)$ suggests a separate b correlation.

 $\label{eq:W2BCuAl2T2Bh,SR11.52} W_2 B (\text{CuAl}_2, \text{Ta}_2 \text{B.h,SR11.52}), \quad \textit{a} (48,76,120) = 5.56; 4.74 \text{Å} = \textit{y}_{\tilde{\text{B}}} (\sqrt{2}9; 4.5). \quad \text{Just} \quad \text{as} \quad \text{in} \\ \text{TaB}_M \text{ the correlation appears overoccupied.}$

WB.h(TiI,VB,SR11.51), $a(24,44,64)=3.19;8.40;3.07\text{Å}=b_{\overline{B}}(\sqrt{2};3.75)=g_{\overline{B}}(\sqrt{8};7.5)$. It is remarkable that the structure contains a separate b correlation signalizing that the type will become unstable in A^7B phases.

WB.r(MoB.r,CrB.r,SR16.31), $u(48,88,128) = 3.12;16.93\text{Å} = b_{R}(\sqrt{2};7.25) = g_{R}(\sqrt{8};14.5)$. A

phase "WB₂(AlB₂)" is no longer stable because #t6,14,18) would not tolerate the commensurability element 9/3 since more free sites are required.

WB₂(H4.8,SR34.41) is a stacking htp of AlB₂ with 4 W layers. a(24,56,72) =H2.98; 13.88Å= $g_{\rm BH}(2:45/3)$. The cell is the same as that of W₂B₅,h so that both phases might be identical.

 W_2B_5 .h(H4.10,SR11.49,drw64Sch.270), $u(24,62,76) = H2.98;13.87 \mathring{A} = g_{RH}(2;45/3)$.

 W_2B_5 .r(Mo₂B₅,SR32.139), $a(36,93,114) = 3.01;20.93 \hat{A} = g_{BH}(2;69/3)$.

WB₄(H4.16,SR31.29) is htpc to Mo_{0.8}B₃. $u(24.80.88) = 5.20;6.34\text{Å} = g_{BH}(\sqrt{12;21/3})$.

The very low occupancy suggests that a g_{CH} correlation is locally filled to g_{RH} .

WB₁₂(H,71Eck).

 $Mn.h_3(W,SR18.210), u(14,16,16) = 3.08Å = g_D(\sqrt{8};2.8).$

 $Mn.h_2(Cu,SR18.210), \ a(28,32,(32)) = 3.86 \text{Å} = g_C(4).$

 $Mn.h_1(C20,SR1.757,2.3,20,149), \ a(140,160,160) = 6.31 \mathring{A} = b_R(3) = (e - e - f)_R(6).$

Mn.r(B29,SR2.2), a(406,464,464)=8.91Å.

Mn₄B(S8.2,SR13.38,drw64Sch.254) is L-htpc to Mn₂B_{0.98}.

 $Mn_2B_{0.98}(S8.4,SR48.35)$ is a shear htp of $CuAl_2$, $a(224,304,288) = 14.54;7.29;4.21Å = <math>g_{\tilde{B}}(11\sqrt{2};5\sqrt{2};4)$. The commensurability element 11 appears to introduce the shear following the mechanism described for Cu_3Au in 64Sch.

 $Mn_2B(CuAl_2.Ta_2B.h,SR13.40)$, $a(32+24,76,72) = 5.15;4.21\mathring{\Lambda} = g_{\tilde{B}}(\sqrt{26};4)$. The binding provides 104 sites for +spin so that Mn contributes only 4 +spins in slight contradiction to Hunds rule.

MnB(FeB,O4.4,SR4.101,drw64Sch.265) is httpc to CrB.h(TII), the B chains being in different manner distributed. $a(16+12,44,40)=5.56;2.98;4.15\text{Å}=g_B(3.75\sqrt{2};2\sqrt{2};4)$. In the electron contribution there are 62 +spins while the CrB.h type provides only 60 +spin sites. The type is found also in FeB and CoB but not in NiB.

 $Mn_3B_4(Ta_3B_4, P3.4, SR13.40), \ a(42,72,64) = 3.03; 12.86; 2.96 \text{Å} = g_R(\sqrt{8}; 12).$

 $MnB_2(AlB_2,SR24.79), a(7,14,12) = H3.01;3.04\text{Å} = g_{\hat{\mathbf{R}}\mathbf{H}}(2;9/3).$

MnB₄(N1.4,SR35.38) is deformation htpc to CrB₄. Analysis must be postponed.

 $\label{eq:Tc(Mg,SR11.183,26.254)} Tc(Mg,SR11.183,26.254), \ \textit{a}(14,16,20) = H2.74; \\ 4.40 \\ \text{Å} = g_{BH}(2;15/3). \ \text{The commensurability element } 15/3 = 5 \ \text{favours the Mg type (84Sch)}.$

Fc₃B(Re₃B,O6.2,SR29.104,drw65Ato.55) is httpc to CrB.h, so that the B are in trigomal prismatic Tc₆ coordination. However, the prisms do not share quadratic faces but trigomal faces, $w(84,108,128) = 2.89;9.16;7.25 \text{Å} = g_{\text{B}}(2\sqrt{2};9;5\sqrt{2})$. The commensurability elements 9 and $5\sqrt{2}$ cause shears that forbid common tetragonal faces of Tc₆ prisms and generate a 9-coordination of Tc around B.

 Te_7B_3 (Th₇Fe₃,H14.6,SR29.104,drw64Sch.266,SR23.58) is a more symmetrical homeotype of Cr_7C_3 . On a column of Te_6 -octahedra sharing faces, trigonal prisms centred by B are erected. n(98,130,152)=H7.42,4.78,= g_{RH} ($\sqrt{27}$;16/3).

TcB, Tc3B4(73Gre).

 ${
m TcB_2(ReB_2,H2.4,SR29.104)}$, a(14,28,28) = ${
m H2.89}$;7.45Å = $g_{
m BH}(2;24/3)$. In ${
m ReB_2}$ are on the B rich side 6B in the cell. Therefore $(b-e)_{
m CH}$ is nearly fully occupied. For a ${
m AlB_2}$ type too many electrons are in the cell.

Re(Mg,SR2.193,26.240), $u(14,16,28) = H2.76;4.46 \text{Å} = g_{RH}(2;15/3).$

 $Re_3B(Q6.2,Tc_3B,SR24.73)$, $a(84,108,176) = 2.89;9.31;7.26 Å = <math>g_B(2\sqrt{2};9;5\sqrt{2})$. Somehow the binding tolerates a little overoccupation as in TaB_{AF} and WB_{AF}

 $\text{Re}_7\text{B}_3(\text{Th}_7\text{Fe}_3,\text{Te}_7\text{B}_3,\text{SR}24.71), \ u(98,130,208) = 117.50;4.77\text{Å} \cdot u_{\text{BH}}(\sqrt{27};16/3).$ ReB(72Now).

 ${\rm ReB_2(H2.4,SR24.71,drw64Sch.270)}$ is homogeneous up to ${\rm ReB_3(77Mof)}$. $u(14,34,40)={\rm H2.90;7.48} \hat{\bf A}=g_{\hat{\bf BH}}(2;24/3)$. The underoccupation comes from the f part $({\rm Re4}f^{14})$ of the correlation.

 Re_2B_5 .h(W₂B₅,H4.10,71Eck), $u(28,62,76) = H2.97;13.80Å = <math>g_{BH}(2;45/3)$.

Fe.h₃(W,SR19.198), $u(16,16,16) = 2.93 \text{Å} = g_{\text{B}}(\sqrt{8}; 2.8)$, presumably h₃ contains lacunae.

Fe.h₂(Cu,SR19.198), $u(32,32,(32)) = 3.65 \text{Å} = (b' \circ c)_{\text{C}}(4)$. It appears that the Fe2sp electrons fall out of the g correlation, and there is not much spin correlation so that b' and c may be considered as having the F type. When the spin correlation sets in, a transition F- $\hat{\text{B}}$ must occur first in c. Because of a possible twinning of the binding the a correlation transforms from F1 (γ -Fe) immediately to B1 (β -Fe):

Fe.h₁(W,SR19.198), $a(16,16) = 2.90 \text{Å} = b \hat{B}(\sqrt{5};1.92) = c \hat{B}(\sqrt{5};1.92)$ (87Sch). Below 770°C the b correlation precipitates from b', leaving c.

Fe.r(W,SR19.198), $a(16,16) = 2.87 \text{Å} = b_{\hat{\mathbf{C}}}(\sqrt{1.25};0.96) = c_{\hat{\mathbf{B}}}(\sqrt{5};1.92) = c_{\hat{\mathbf{B}}}(\sqrt{5};1.92)$. The

magnetic data show that the binding in pure Fe is no longer collective (87Sch). However, the phenomenon of isotypism of FeB_M phases with MnB_M phases suggests to seek for intermediate phases a collective binding.

$$\text{Fe}_{23}\text{B}_6$$
.m(Cr_{23}C_6 :F23.6,SR44.107), $a(736,808) = 10.67\text{Å} = b_{\text{C}}(4.5) = (e - e)_{\text{B}}(9)$.

 $Fe_3B.h_2(U12.4,Fe_3P,78Wal,87Kne)$, is closely homeotypic to h_1 (SR27.99), u=8.63; 4.29Å.

$$\begin{split} &\text{Fe}_3\text{B.h}_1(\text{T}24.8,\text{Fe}_3\text{B}_{0.6}\text{P}_{0.4},\text{SR}44.107,87\text{Kne}), \quad a(192,216,208) = 8.75;4.36\text{\AA} = b_{\text{C}}(\sqrt{18};2) \\ = &g_{\hat{\text{B}}}(\sqrt{72};4). \text{ The strain of } g_{\text{B}} \text{ may indicate the existence of a separate } b \text{ correlation (87Sch)}. \end{split}$$

$$\text{Fe}_2\text{B}(\text{CuAl}_2, \text{Ta}_2\text{B.h.}, \text{SR}2.286), \ a(64, 76, 72) = 5.11; 4.25\text{Å} = h_{\hat{C}}(2.5; 2) = (e \circ e')_{\hat{\mathbf{R}}}(5; 4).$$

FeB(O4.4,MnB,SR2.241), $a(32,44,46) = 5.51;2.95;4.06\text{Å} = g_B(3.75\sqrt{2};2\sqrt{2};4)$. The Fe partial structure in Fe₂B is approximately of the C1 type. It might therefore be surprising that with a higher B content the Fe partial structure is closer packed in FeB. However, the commensurability of g_B to the quasiquadratic Fe meshes is different.

FeB2.m(AIB2,85Vil,77Mof).

 $FeB_{40}(R2.98, SR42.57), a=10.96;23.87Å.$

Ru(Mg,SR1.69,24.222), $a(16,16,20) = H2.71;4.28\text{Å} = g_{BH}(2;15/3)$. The commensurability element 15/3 = 5 is favourable for the Mg type stacking. The binding of Ru is closer packed than that of Fe. This may be caused by the influence of the Ru3d electrons which is stronger than the influence of the Fe2sp electrons.

 ${\rm Ru_7B_3(Th_7Fe_3,Tc_7B_3,SR23.57)},\ a(112,130,152) = H7.47; 4.71 \\ \mathring{\rm A} = g_{\mathring{\rm BH}}(\sqrt{27};15/3).$

 ${\rm Ru}_{11}{\rm B}_8({\rm U}22.16,{\rm SR}24.73,{\rm drw}72{\rm Pea.527})~{\rm is~homeotypic~to~Ni}_4{\rm B}_3,~{\rm all~B~have~a~trigonal~prismatic~Ru}_6~{\rm surrounding.}~a(176,224,252)=11.61;11.34;2.84 Å=g_{\bar{\rm R}}(10.5;8\sqrt{2};2\sqrt{2}).$

 ${\rm RuB}_{1.1}({\rm WC,SR27.93}), \ a(8,12,12)$ =H2.85;2.85Å = $g_{\rm BH}(2;9/3)$. The WC type replaces the AlB₂ type found still in MnB₂. The +spin offer is too high for a TII type.

 $Ru_2B_3(W_2B_5,H4.10,SR34.41)$, $a(32,50,52)=H2.89;12.81 Å=g_{\hat{B}\hat{H}}(2;39/3)$. The reason for the B defect becomes clear when it is assumed that B contributes only +spins. In this case the +spin offer in a "Ru₂B₅" phase would be 20+16+30+20+10=96.

 ${
m RuB_{2.1}(O2.4,SR27.94)}$ is an inhomogeneous deformation of ${
m AlB_2}$ with pleated Ru layers. $a(16,28,28)=4.65;2.84;4.05 {\rm \^{A}}=g_{\rm B}(3\sqrt{2};2\sqrt{2};4)$. An ${
m AlB_2}$ type would be impossible since the +spin offer would be 22 while ${
m AlB_2}$ admits only 18 +spin sites.

$$()_{8}(\text{Mg},\text{SR}1.70,5.35),\ n(16,16,28)=\text{H2.74};4.32\mathring{\text{A}}=g_{\text{BH}}(2;15/3)$$

$$(3)$$
8 $B_{1,2}$ 1 WC, SR27.43), $a(8,12,14) = H2.88; 2.87 \hat{A} = a_{BH}(2;9/3)$.

$$O_8B_{1.6}(W_2B_5,SR27.93), \ \alpha(32,50,68) = H2.91;12.91\text{Å} = g_{BH}(2;42/3).$$

$$O_8B_{2,2}(RuB_2,SR27.94), \ a(16,31,38) = 4.68;2.87;4.10\mathring{A} = g_R(3\sqrt{2};2\sqrt{2};4).$$

"Os₂B₅" (SR26.76) is not confirmed, SR27.93.

Co.h(Cu,SR18.118),
$$a(36,32,32) = 3.54\text{\AA} = b_{\hat{\mathbf{C}}}(\sqrt{2};1.25) = e_{\hat{\mathbf{B}}}(\sqrt{8};2.5) = e_{\hat{\mathbf{B}}}(\sqrt{8};2.5)$$
.

Co.r(Mg,SR22.101),
$$a(18,16,16) = H2.51;4.07\text{Å} = b_{H}(1;1.66) = c_{\tilde{U}H}(2;5/2).$$

 $\text{Co}_3\text{B}(\text{Fe}_3\text{C.m},\text{O}12.4,\text{SR}22.58,\text{drw}64\text{Sch}.253)}, \ a(108,108,104) = 4.41;5.22;6.63\text{Å} = g_{\text{B}}(4.5;5.5;7).$ The distance d_q does not fit very well to the distance of Co_2B .

$$\text{Co}_2\text{B}(\text{CuAl}_2,\text{Ta}_2\text{B.h.}\text{SR}3.619), \ a(72,76,72) = 5.02; 4.22\text{Å} = b_{\hat{\mathbf{B}}}(2.5;2) = g_{\hat{\mathbf{B}}}(5;4).$$

CoB(FeB,MnB,SR3.619), $a(36,44,40) = 5.25;3.04;3.96\text{Å} = g_{\widehat{\mathbf{B}}}(5;3;4)$. The phase is somewhat heterodesmic to FeB and a(CoB) is quite different from a(FeB).

Rh(Cu,SR1.69,24.223),
$$a(36,32,40) = 3.80 \text{Å} = y_{\text{R}}(4)$$
.

$$\mathsf{Rh}_7 \mathsf{B}_3 (\mathsf{Th}_7 \mathsf{Fe}_3, \mathsf{Tc}_7 \mathsf{B}_3, \mathsf{SR}23.57), \ a(126,130,152) = \mathsf{H}7.47; 4.78 \mathring{\mathsf{A}} = g_{\mathsf{BH}} (\sqrt{27}; 16/3).$$

 Rh_5B_4 (H10.8,SR48.37). The Rh form a close packing with stacking -++++++ and the B are in Rh_6 coordination. a(90,104,116)=H3.31;20.39Å= $g_{UH}(\sqrt{12;28/2})$. For a simple close packing a stacking would be +-+-++-+. However, the interference of the B atoms causes a stacking sequence which disregards the equal sign clustering prohibition (84Sch).

RhB_{1.1}(NiAs,SR27.71) has Rh in +- type packing while B form straight strings. a(18, 22,24) =H3.31;4.22Å = $g_{\tilde{\mathbf{U}}\mathbf{H}}(\sqrt{12;6/2})$. The commensurability element 6/2=3 favours the +- stacking.

Ir(Cu,SR1.70,3.182), $a(36,32,56) = 3.84\text{Å} = g_{\text{R}}(4)$.

IrB_{0.9}.h(WC,SR37.40),
$$a(9,11,16) = H2.82; 2.82 \text{Å} = g_{\hat{\mathbf{B}}\mathbf{H}}(2;9/3).$$

$${\rm IrB}_{0.9}, {\rm r}({\rm Q4.4,SR37.40}), \ a(72,88,128) = 2.71; 7.58; 7.31 \mathring{\rm A} = g_{\rm B}(2\sqrt{2};8;5\sqrt{2}).$$

 $IrB_{1.1}(ThSi_2,U2.4;SR24.71,drw64Sch.313) \ \, is \ \, htp \ \, to \ \, TII. \ \, a(36,56,72)=2.81;10.26\text{\AA}=9_{\rm R}(\sqrt{8};10.3).$

 $Ir_4B_{5/4}(N4.5,SR39.38)$ is quasiorthogonal.

Ni(Cu, SR1.68, 13.88),
$$a(40,32,32) = 3.52 \text{Å} = b_{\hat{\mathbf{C}}}(\sqrt{2};1.25) = e_{\hat{\mathbf{B}}}(\sqrt{8};2.5) = e_{\hat{\mathbf{B}}}(\sqrt{8};2.5)$$
.

$$Ni_3B(Fe_3C.m,Co_3B,SR32.32), \ a(120,108,104) = 4.39;5.21;6.62Å = g_B(4.5;5.5;7).$$

 $Ni_2B(CuAl_2, Ta_2B, h, SR23.64), n(80, 76, 72) = 4.99; 4.25 \acute{A} = g_{R}(\sqrt{26}; 4.4).$

 $Ni_4B_{2,9}(O16.12,SR32.32,drw64Sch.265)$ is httpc to FeB, but besides B chains there occur isolated B atoms, $a(160,164,152)=11.95;2.98;6.57 Å = g_B(12;3;6.7)$.

 $Ni_4B_2(N8.6,SR32.33), a=M103.306.43;4.88;7.82Å.$

NiB(TII, VB, SR16.32), $a(40,44,40) = 2.93;7.39;2.96\text{Å} = g_D(3;7.5)$.

NiB₂(73Gre).

NiB₁₂(F1.12,71Eck), $a(40,176,128)=7.53\text{Å}=g_{C}(7)$. Apparently the dilution of Ni makes possible a strong increase of d_{g} .

Pd(Cu,SR1.70), a(40,32,40) = 3.89Å= $g_B(4)$. Therefore Ni and Pd are hdmc isotypes.

 $Pd_{16}B_3$ (F8.(1.5),82Alq) is a superstructure of Pd (Cu type) with inserted B atoms. $\eta(320,274,332)=8.01 \text{Å}=g_{\hat{\mathbf{B}}}(8;8;7.5)$. The doubled lattice constant permits a more economical commensurability.

 $Pd_3B(Fe_3C.m, Co_3B, SR26.77),$ $a(120,108,128) = 4.85; 5.46; 7.57Å = b_B(2.3; 2.5; 3.5) = g_B(4.5; 5; 7).$

Pd₅B₂(Mn₅C₂,N10.4,SR26.76).

 $Pd_2B(CaCl_2,SR46.40,drw64Sch.257)$, $a(40,38,44)=4.69;5.13;3.11\mathring{A}=g_B(4.5;5;3)$. For the CuAl₂ type the electron numbers would have been (80,76,88) i.e. too large.

Pt(Cu, SR 1.71;11.174), $a(40,32,56) = 3.92\text{Å} = g_{\text{R}}(4)$.

 $Pt_AB(C24.6,79Has)$, $a(240,210,348) = 7.57 Å = <math>g_B(7.5)$, tentative.

 $Pt_3B(T2.(0.7),SR30.116), a=2.63;3.83Å.$

 $Pt_2B(H4.2,79Has), \ a(40,38,60) = H2.79;10.49Å = g_{BH}(2;36/3).$

 $Pt_2B_{1,3}(anti NiAs,RhB_{1,1}.85Vil)$, $a(20,20,31)=3.37;5.82;4.05Å=g_{UH}(\sqrt{12};6/2)$. The deformation of g might be caused by the participation of electrons below f in the binding. Also the orthorhombic deformation of a may depend on it.

CuB₂₃(B.h,R108,SR40.41,42.55), no intermediate phase (nip) (77Mof).

"AgB₂" (SR26.73) not confirmed, Hildebrands rule (50Hil) for miscibility gap is obeyed, (65Wal), nip(77Mof).

"AuB₂" (SR26.73) not confirmed (65Wal), nip(77Mof).

ZnB₂₅(64Pic).

 CdB_M nip(77Mof), HgB_M nip(77Mof).

 ${\rm MB}_{5}({\rm HL2,MgB}_{5},{\rm SR20.5}),\ v(3,14,6)={\rm H3.01;3.26A}=g_{\rm CH}(2:6/3),\ see {\rm MgB}_{5}.$

 ${\rm VB}_{10}({\rm O}5.52,{\rm SR}32.3)$ is mainly composed of ${\rm B}_{12}$ icosahedra. The phase probably contains C (SR32.4).

AIB₁₂.h(O348.29,SR26.5), a = 16.56;17.35;10,16Å.

 $\Delta \text{IB}_{12}.r(\text{T13.176,SR43.6,drw ibid.}), \ a(39,632,378) + 10.16;14.28 \\ \dot{\Delta} = g_{\text{B}}(\sqrt{52};10).$

GaB₁₂(T10.120,SR26.72), doubtful.

 $InB_{M}nip(77Mof)$, $TIB_{M}nip(77Mof)$.

 $B_{12}BC_2$ (R13.2,SR42.52,drw64Sch.179) was earlier named B_4 C. It is composed of B_{12} icosahedra and CBC strings. a(141,90)=H5.63;12.14 \hat{A} = g_{CH} (4;21/3). The commensurability explains why a_1 is very different from a_1 (B.h₁).

BoC(O348.48,85Vil).

 ${}^{B}{}_{50}C_{2}(T50.2,SR42.52,drwSR22.212), \qquad u(158,104) = 8.75;5.09 \\ \dot{\Lambda} = g_{B}(\sqrt{44};3.75), \qquad \sec B_{50}N_{2}.$

 $B_4Si(B_4C,R12.3,SR24.255)$, $a(36,180,90) = H6.35;12.69 Å = g_{BH}(\sqrt{10.5;30/3})$, tentative.

 $B_6Si.i(CaB_6,SR20.209)$, $u(4,26,14) = 4.13 \text{Å} = g_B(3)$. SiC and SiO₂ were in the samples.

 $B_6Si(O240.40,SR22.65,23.278), u(160,1040,560) = 14.39;18.27;9.89Å.$

B₁₄Si(B.r,R108,SR30.116) probably marginal.

 $B_{36}Si(R102.3,SR48.37)$ is httpc to B.r(R105). u=H11.01;23.90Å.

BGe Mnip(77Mof), BSn Mnip(77Mof), BPb Mnip(77Mof).

BN(H2.2,SR13.44,drw ibid.) is homeotypic to C.r(drw64Sch.180), its structure provides a better Coulomb interaction. However, it is isodesmic to C.r: $u(16,8) = H2.52;6.69\text{Å} = g_{\tilde{C}H}(\sqrt{3};12/3)$ displaying $N_{\tilde{S}(g)}^{At} = 9$.

BN.hp(ZnS,F1.1,SR21.194), $a(32,16) = 3.62 \text{Å} = b_F(2) = c_C(4)$ or $a = g_C(4)$. While BN has a site number $N_S^{/At}(g) = 9$, the phase BN.hp has $N_S^{/At}(g) = 8$ conforming to the site number rule.

BN.rp(ZnO,H2.2,67Hoa.147). $u(16.8) = 112.55;4.20\text{Å} = h_{\mathrm{BH}}(1;7/3) = g_{\mathrm{CH}}(2;7/3)$. The reason for the stability is presumably the decreased site number 7. The axial ratio of u needs not to express the strain of g because of an independent part of g.

 $B_{50}N_2$ (T50.2,SR42.52,drwSR22.212), $u(160,104) = 8.63;5.13 Å = g_{CH}(15/3;\sqrt{13})$. $B_{50}N_2$ is assumed to be homeodesmic to $B.h_1$ (R12). $N_S/At = 7.5$. However, see $B_{50}C_2$.

 $B_{12}B_{0.6}P_{1.4}(R12.2,SR40.43)$ is http://to/ $B_{13}C_{2^{-1}}(20,124,S4)=H5.98(11.85A=\sigma_{CH}(4;20/3))$. In σ_{CH} is contained $a=b_{EH}(2;5/3)$ determining the P content.

BP.h(ZnO,SR28.43,296) obeys Lewis' rule. $w(10,22.8) = H3.56; 5.90 \text{Å} = g_{\text{BH}}(2;15/3)$. The w cell needs confirmation. The strain of g_{BH} has the same reason as the strain in SiC.

BP.r(ZnS,SR28,43,296) is httpc to SiC.r. $e(20,44,16) = 4.53 \text{Å} = g_B(4)$. According to Lewis' rule there are 16+16+8=40 +spins and 4+16+12+8=40 -spins.

$$B_6P(R12.2,SR40.43), \ a(138,120) = H5.96;11.81\text{Å} = g_{CH}(4;20/3).$$

 $B_{12}B_{0.6}As_{1.4}(B_{12}B_{0.6}P_{1.4},SR26.79)$ changed according to SR40.43), a(20.185,108)= H6.14;11.89Å= $g_{CH}(4;20/3)$. The low As content enhances the expansion of As so that a g_{CH} correlation becomes possible.

BAs(ZnS,SR22.39), $a(20,40,44,(40)) = 4.78\text{Å} = g_B(4)$. Perhaps the As2sp electrons do not participate in the correlation.

 $BSb_M nip(77Mof)$, $BBi_M nip(77Mof)$. The formation of the Lewis phases of these mixtures is impossible because of the f electrons.

 $B_6O(H24.4,75Pie)$, $a(96,56) = H5.40;12.34Å = g_{UH}(\sqrt{13};12/3)$.

B₂O.hp(H36.18,75Pie), $a(216,108) = H7.98; 9.09 \text{Å} = g_{CH}(\sqrt{31}; 15/3).$

 $B_2O_3(H6.9,SR33.258,drwSR33.259)$, $a(72,30)=4.34;8.34Å=g_{CH}(3;14/3)$. Since the g correlation contains numerous lacunae a p—phase becomes stable.

 ${\rm B_2O_3.p(Q4.6,SR33.259,drwSR33.261)},\ a(96,40) = 4.61; 7.80; 4.13 \text{Å} = g_{\text{\textbf{B}}}(3.5;6;3.3).$

B₁₂S(htpB₄C,B₁₃P,SR26.79).

BS₂(M16.32,SR46.408).

B2Se3(M16.24, SR43.37).

B₂F₄.1(M4.8,SR22.230).

 $BCl_2(O8.16,SR19.314)$, $BCl_3.l(H2.6,SR19.317)$, a=H6.08;6.55Å.

 $BI_3(H2.6,SR27.438), a=H7.00;7.46Å.$

Discussion

Numerous metrical data on solid phases are excellently accumulated; sometimes they have been applied to derive atomic radius ratio criteria for stability. However, the relation of electron numbers with metrical data has remained unexploited. Some authors believe

that only extended computations can reveal these relations. The present study attenuted to show that the inductive chemical systematics can provide rules for these relations which are quite easily accessible. These rules are useful because of their influence on the systematics of chemical and physical properties as for instance the energy of formation. A systematics of these energies is a condition for the calculation of phase diagrams strongly condensing the knowledge on constitution. The inductive chemistry makes use of general theoretical concepts, but conversely the deductive chemistry will utilize results of inductive research. To be sure, the experimental chemist sometimes prefers to use inductive rules to find a promising direction for his work since they are easier accessible than the extended computations. Some examples of questions of the experimental chemists are the following:

Why is ${\rm LiB_3}$ homeotypic to ${\rm CaB_6}$? The volume of ${\rm Li_2}$ approximately equals the volume of Ca so that a homeotypic binding may develop.

Why is ${\rm SrB_6}$ a semiconductor and ${\rm YB_6}$ a metallic conductor? The $b_{\rm B}$ correlation is favourable in ${\rm SrB_6}$ but unfavourable in ${\rm YB_6}$.

Why is LaB_6 stable but "HfB6" not? In "HfB6" the binding of LaB_6 type would be overoccupied.

Why is TiB of the FeB type while TiC is of NaCl type? The y correlation tends to high occupancy so that in TiB the correlation is deformed and with it the structure, while in TiC it is not deformed.

Why are the closely neighbouring phases V_5B_6 , V_3B_4 , V_2B_3 stable? There is the g correlation in such a harmony that on each V layer parallel to the smallest cell face there come 4g layers.

Why is a phase " $WB_2(AlB_2)$ " not stable? The electron offer exceeds the electron site number of the AlB_2 type.

Why is MnB₂ of the AlB₂ type although "WB₂(AlB₂)" was not stable? There are less felectrons contributed by Mn.

Why is RuB of the WC type and not of the TII type like MoB,h? The +spin offer is too high.

Why is $IrB_{0.9}$ r not of the WC type? The Q4.4 structure has a better commensurability.

Why is NiB(TII) not of the FeB type like CoB? The η correlation has acquired a new favourable commensurability.

Why does CuB_M and ZnB_M not form intermediate phases? The h electrons press the metal atoms together and prevent insertion of B.

Why is BN.hp(ZnS,F1.1) and BN.rp(ZnO,H2.2) stable? At the lower temperature the site number is reduced and this is possible only in the hexagonal structure.

It is clear that a first attempt of binding analysis cannot answer all questions. The considerable frequency of deformed correlations suggests that details of spin correlations are still to be investigated. Also, the somewhat uneven fit of the bindings of Fe to those of Fe_2B , or the compatibility in CoB_M needs further attention.

Some of the arguments used above belong to a Madelung theory of the pair density, as for instance the dependence of the stacking sequence on the binding. Since this theory seems to be not yet worked out, the interpretative possibilities of the plural correlations model are not yet exhausted. The present interpretation provides numerous applications for a future Madelung theory of the pair density. A further missing support is a theory of the influence of electron correlation on conductivity. When such a theory exists, with conductivity measurements the binding can be examined.

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