



# AnQL: SPARQLing Up Annotated RDFS

**Nuno Lopes**   Axel Polleres   Umberto Straccia  
Antoine Zimmermann

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NUI Galway  
OÉ Gaillimh



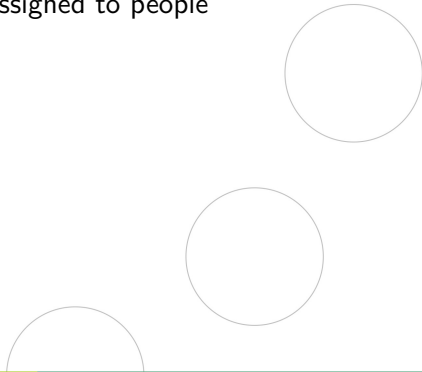
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# Usecase: Exposing Sensor data as RDF



*sensor tags* are assigned to people





# Usecase: Exposing Sensor data as RDF



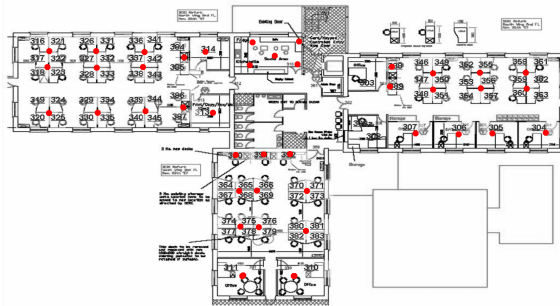
*sensor tags* are assigned to people

tag proximity is registered by *base stations*





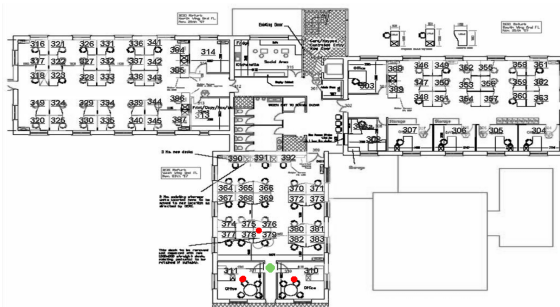
# Usecase: Exposing Sensor data as RDF



*base stations* are deployed throughout a building



# Usecase: Exposing Sensor data as RDF

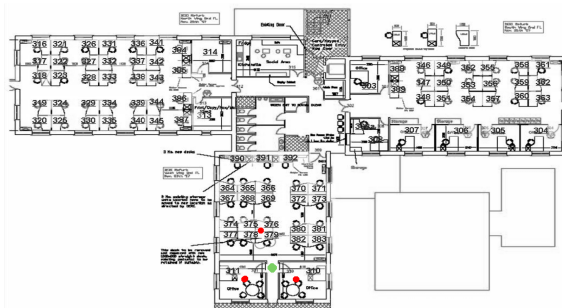


sensor data readings:

timestamp	ip	tag	ssi
2010-11-09 14:57:51	10.254.2.15	4302	83
2010-11-09 14:57:51	10.254.3.1	4302	83
2010-11-09 14:57:51	10.254.2.6	4302	83



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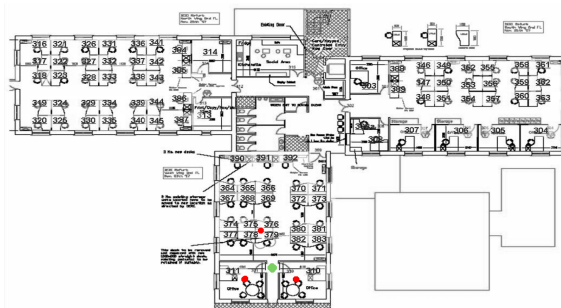
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- RDF triples

```
:tag4302 :locatedIn :room311 .
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:tag4302 :locatedIn :room311 .  
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:tag4302 :locatedIn :room310 .
```

Not enough info!



# How to represent sensor data as RDF?

- RDF triples

```
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room310 .
```

Not enough info!

- Domain vocabulary/ontology

```
:record1 a          :SensorRecord;  
          :tag       :tag4302;  
          :locatedIn :room311;  
          :timestamp "2010-11-09 14:57:51" .
```



# How to represent sensor data as RDF?

- RDF triples

```
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room310 .
```

Not enough info!

- Reification

```
:record1 rdf:type rdf:Statement  
rdf:subject :tag4302;  
rdf:predicate :locatedIn ;  
rdf:object :room311 ;  
:timestamp "2010-11-09 14:57:51" .
```



# How to represent sensor data as RDF?

- RDF triples

```
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room311 .  
:tag4302 :locatedIn :room310 .
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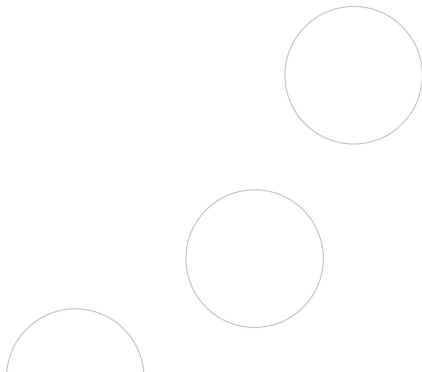
```
:record1 rdf:type rdf:Statement  
          rdf:subject :tag4302;  
          rdf:predicate :locatedIn ;  
          rdf:object :room311 ;  
          :timestamp "2010-11-09 14:57:51" .
```

No defined semantics!



# Use Annotated RDF(S)!

Annotations refer to a specific **domain**





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Temporal:

```
:tag4302 :locatedIn :room311 . "2010-11-09 14:57:51"
```





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Annotations refer to a specific **domain**

Temporal:

```
:tag4302 :locatedIn :room311 . "2010-11-09 14:57:51"
```

Fuzzy:

```
:tag4302 :locatedIn :room311 . "0.9"
```



# Use Annotated RDF(S)!

Annotations refer to a specific **domain**

## Temporal:

```
:tag4302 :locatedIn :room311 . "2010-11-09 14:57:51"
```

## Fuzzy:

```
:tag4302 :locatedIn :room311 . "0.9"
```

## Queries:

*"When were two people in the same room?"*

*"Who is closer to room 311?"*



# Overview

## Annotated RDF(S) (Straccia et al. [2010])

- Based on previous work on Annotated RDF (Udrea et al. [2010])
- Encompasses other proposals for domain-specific RDF: Temporal, Fuzzy, Trust, Provenance, . . .
- Deductive system as extension of RDFS



# Overview

## Annotated RDF(S) (Straccia et al. [2010])

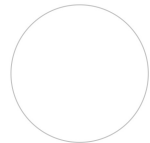
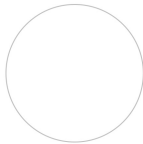
- Based on previous work on Annotated RDF (Udrea et al. [2010])
- Encompasses other proposals for domain-specific RDF: Temporal, Fuzzy, Trust, Provenance, ...
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## AnQL: Annotated SPARQL

- Annotation-aware SPARQL
- Extension of the semantics presented in Pérez et al. [2009]
- Includes features from SPARQL 1.1
  - subqueries, aggregates and assignment



# Annotated RDF(S)





# Annotation Domain Example

## Temporal domain example

```
:tag4302 :locatedIn :room311 . ["09:25", "11:49"]
```

```
:tag4302 :locatedIn :room311 . ["10:35", "12:57"]
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To define a **new domain** you need to specify:

- the *representation* of the annotations



# Annotation Domain Example

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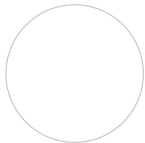
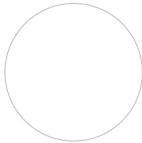
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- an *order* between the elements:







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*universal* ( $\top$ ) and *empty* ( $\perp$ ) annotations



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["09:25", "11:49"]  $\otimes$  ["10:35", "12:57"] = ["10:35", "11:49"]



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["09:25", "11:49"]  $\oplus$  ["14:35", "15:57"] = ["09:25", "11:49"],  
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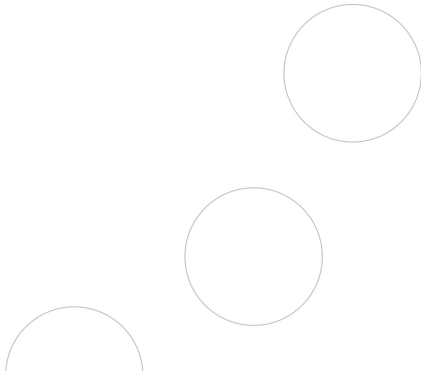
$$["09:25", "11:49"] \oplus ["14:35", "15:57"] = \{["09:25", "11:49"], ["14:35", "15:57"]\}$$





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Consider a non-empty set  $L$ : **annotation values**





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An **annotation domain** is an idempotent, commutative semi-ring

$$D = \langle L, \oplus, \otimes, \perp, \top \rangle$$

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For  $\lambda, \lambda_i \in L$

- 1  $\oplus$  and  $\otimes$  are commutative and associative;
- 2  $\oplus$  is idempotent;
- 3  $\perp \oplus \lambda = \lambda$ ,  $\top \oplus \lambda = \top$ ,  $\top \otimes \lambda = \lambda$  and  $\perp \otimes \lambda = \perp$ ;
- 4  $\otimes$  is distributive over  $\oplus$ , i.e.  
$$\lambda_1 \otimes (\lambda_2 \oplus \lambda_3) = (\lambda_1 \otimes \lambda_2) \oplus (\lambda_1 \otimes \lambda_3);$$



# Annotated RDF(S)

Consider the alphabets **U** (*URI references*), **B** (*blank nodes or variables*) and **L** (*Literals*).

## Annotated triple and graph

An “extended” **RDF triple** is  $\tau = (s, p, o) \in \mathbf{UBL} \times \mathbf{U} \times \mathbf{UBL}$ .



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An **annotated graph**  $G$  is a finite set of *annotated triples*.

## $\rho$ df vocabulary

$(p, sp, q)$  property  $p$  is a **subproperty** of property  $q$

$(c, sc, d)$  class  $c$  is a **subclass** of class  $d$

$(a, \text{type}, b)$   $a$  is of **type**  $b$

$(p, \text{dom}, c)$  the **domain** of property  $p$  is  $c$

$(p, \text{range}, c)$  the **range** of property  $p$  is  $c$





# Annotated RDF(S) Semantics

## Interpretation

An **interpretation**  $\mathcal{I}$  assigns to a triple  $\tau$  an element  $\lambda \in L$



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An interpretation  $\mathcal{I}$  is a **model** of  $G$  if it assigns to the triples of  $G$  a value that is greater or equal (i.e.,  $\succeq$ ) to the annotation and satisfies the schema axioms constraints (sp, sc, type, dom, range).



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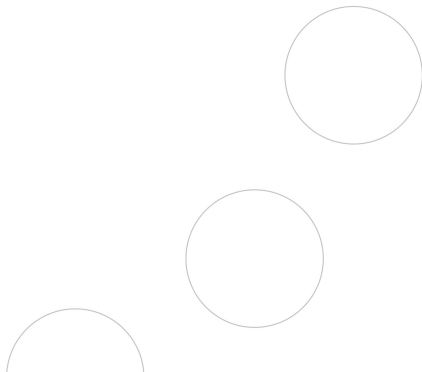
## Graph entailment

$G$  **entails**  $H$  under  $\rho$ df ( $G \models H$ ) iff every model under  $\rho$ df of  $G$  is also a model under  $\rho$ df of  $H$ .



# Annotated RDF(S) Inference example

Inference rules are **independent** of the annotation domain





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## RDFS "sp" rule:

```
?Prop1 sp ?Prop2 .  
?x ?Prop1 ?y .  
⇒ ?x ?Prop2 ?y .
```

```
:locatedIn sp :basedNear .  
:tag4302 :locatedIn :room311 .  
⇒ :tag4302 :basedNear :room311 .
```



# Annotated RDF(S) Inference example

Inference rules are **independent** of the annotation domain

## Annotated RDFS “sp” rule:

```
?Prop1 sp ?Prop2 .   ?v1
?x ?Prop1 ?y .       ?v2
⇒ ?x ?Prop2 ?y .     ?v1 ⊗ ?v2
```

```
:locatedIn sp :basedNear .           [−∞, +∞]
:tag4302 :locatedIn :room311 .       ["14:25", "14:57"]
⇒ :tag4302 :basedNear :room311 .    ["14:25", "14:57"]
```



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```

```

:locatedIn sp :basedNear .   [−∞, +∞]
:tag4302 :locatedIn :room311 . ["14:25", "14:57"]
⇒ :tag4302 :basedNear :room311 . ["14:25", "14:57"]

```

## Extra rule to group annotations triples ( $\oplus$ ):

```

:tag4302 :locatedIn :room311 .   ["14:25", "14:57"]
:tag4302 :locatedIn :room311 .   ["14:43", "15:20"]

```



# Annotated RDF(S) Inference example

Inference rules are **independent** of the annotation domain

## Annotated RDFS “sp” rule:

```
?Prop1 sp ?Prop2 . ?v1
?x ?Prop1 ?y . ?v2
⇒ ?x ?Prop2 ?y . ?v1 ⊗ ?v2
```

```
:locatedIn sp :basedNear . [-∞, +∞]
:tag4302 :locatedIn :room311 . ["14:25", "14:57"]
⇒ :tag4302 :basedNear :room311 . ["14:25", "14:57"]
```

## Extra rule to group annotations triples (⊕):

```
:tag4302 :locatedIn :room311 . ["14:25", "14:57"]
:tag4302 :locatedIn :room311 . ["14:43", "15:20"]
⇒ :tag4302 :locatedIn :room311 . ["14:25", "15:20"]
```





# Annotated RDF(S) Inference example

Inference rules are **independent** of the annotation domain

## Annotated RDFS “sp” rule:

```

?Prop1 sp ?Prop2 .   ?v1
?x ?Prop1 ?y .       ?v2
⇒ ?x ?Prop2 ?y .    ?v1 ⊗ ?v2

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```

:locatedIn sp :basedNear .           [−∞, +∞]
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```

## Extra rule to group annotations triples ( $\oplus$ ):

```

⇒ :tag4302 :locatedIn :room311 .    ["14:25", "15:20"]

```



# Integration with RDF

## Transparent integration of annotated and classical RDF

```
:nuno foaf:name "Nuno Lopes" .  
:tag4302 :assignedTo :nuno .  
:tag4302 :locatedIn :room311 .      ["14:25", "14:57"]
```



# Integration with RDF

## Transparent integration of annotated and classical RDF

```
:nuno foaf:name "Nuno Lopes" .      [-∞, +∞]  
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```

### Possible approaches:

- use **T** as annotation



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### Possible approaches:

- use  $\top$  as annotation
- triple is valid at a time interval common throughout the graph  
requires **blank nodes** in annotations



# Integration with RDF

## Transparent integration of annotated and classical RDF

```
:nuno foaf:name "Nuno Lopes" .      [−∞, now]  
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```

### Possible approaches:

- use  $\top$  as annotation
- triple is valid at a time interval common throughout the graph  
requires blank nodes in annotations
- triple is valid until “now” (Gutiérrez et al. [2005])  
represents **current time**



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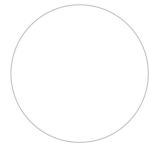
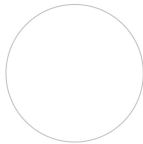
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```

### Possible approaches:

- use  $\top$  as annotation **“compatible with classical RDF”**
- triple is valid at a time interval common throughout the graph  
requires blank nodes in annotations
- triple is valid until “now” (Gutiérrez et al. [2005])  
represents current time



# AnQL: Annotated SPARQL





# AnQL: Annotated SPARQL

Consider the alphabets **U**, **B**, **L** as before

## SPARQL

- $\tau = (s, p, o)$  where  $s, o \in \mathbf{UBL}$  and  $p \in \mathbf{UB}$  is a **triple pattern**.

## triple pattern example

```
?tag :assignedTo :nuno .
```





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## Annotated SPARQL

- $\tau = (s, p, o)$  where  $s, o \in \mathbf{UBL}$  and  $p \in \mathbf{UB}$  is a **triple pattern**.
- $\tau: \lambda$  is an **annotated triple pattern** if  $\tau$  is a triple pattern and  $\lambda \in L$  (annotation term)

## annotated triple pattern example

```
?tag :assignedTo :nuno .  $[-\infty, +\infty]$ 
```



# AnQL: Annotated SPARQL

Consider the alphabets **U**, **B**, **L** as before, and **V** as the alphabet for *Annotation variables*.

## Annotated SPARQL

- $\tau = (s, p, o)$  where  $s, o \in \mathbf{UBL}$  and  $p \in \mathbf{UB}$  is a **triple pattern**.
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## annotated triple pattern example

```
?tag :locatedIn ?room . ?l
```



# AnQL: Annotated SPARQL

Consider the alphabets **U**, **B**, **L** as before, and **V** as the alphabet for *Annotation variables*.

## Annotated SPARQL

- $\tau = (s, p, o)$  where  $s, o \in \mathbf{UBL}$  and  $p \in \mathbf{UB}$  is a **triple pattern**.
- $\tau: \lambda$  is an **annotated triple pattern** if  $\tau$  is a triple pattern and  $\lambda \in L$  (annotation term) or  $\lambda \in \mathbf{V}$  (annotation variable)
- **Basic Annotated Patterns** (BAP) are sets of annotated triple patterns

## BAP example

```
{ ?tag :assignedTo :nuno . [-∞, +∞]  
  ?tag :locatedIn ?room . ?1 }
```



# AnQL definitions

An **annotated graph pattern (AGP)** is:

- 1 any BAP
- 2  $P, P'$  are annotated graph patterns,  $R$  a filter expression:
  - $(P \text{ AND } P')$
  - $(P \text{ OPTIONAL } P')$
  - $(P \text{ UNION } P')$
  - $(P \text{ FILTER } R)$



# AnQL definitions

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  - $(P \text{ OPTIONAL } P')$
  - $(P \text{ UNION } P')$
  - $(P \text{ FILTER } R)$

Filter expressions

- any SPARQL filter ( $=, \vee, \wedge, \text{isBOUND}, \dots$ )
- Domain  $\preceq$  for comparing annotations
- Domain specific built-in functions



# Compatible substitutions

## SPARQL

```
SELECT *  
WHERE { ?tag :assignedTo :nuno .  
        ?tag :locatedIn ?room . }
```

## Substitutions

$\theta_1$  = { ?tag  $\rightarrow$  :tag4302 }

$\theta_2$  = { ?tag  $\rightarrow$  :tag4304 }

$\mu_1$  = { ?tag  $\rightarrow$  :tag4302, ?room  $\rightarrow$  :room311 }

$\mu_2$  = { ?tag  $\rightarrow$  :tag4302, ?room  $\rightarrow$  :room312 }



# Compatible substitutions

## SPARQL

```
SELECT *  
WHERE { ?tag :assignedTo :nuno .  
        ?tag :locatedIn ?room . }
```

## Substitutions

$\theta_1 = \{?tag \rightarrow :tag4302\}$   
 $\theta_2 = \{?tag \rightarrow :tag4304\}$   
 $\mu_1 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room311\}$   
 $\mu_2 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room312\}$

## Union of compatible substitutions

$\theta_1 \cup \mu_1 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room311\}$   
 $\theta_1 \cup \mu_2 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room312\}$



# Compatible substitutions

## AnQL

```
SELECT *  
WHERE { ?tag :assignedTo :nuno . ?l  
        ?tag :locatedIn ?room . ?l }
```

## Substitutions

$\theta_1 = \{?tag \rightarrow :tag4302, ?l \rightarrow ["13:00", "15:00"]\}$   
 $\theta_2 = \{?tag \rightarrow :tag4304, ?l \rightarrow ["12:00", "13:00"]\}$   
 $\mu_1 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room311, ?l \rightarrow ["14:00", "16:00"]\}$   
 $\mu_2 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room312, ?l \rightarrow ["16:00", "18:00"]\}$

## Union of compatible substitutions

$\theta_1 \cup \mu_1 = \{?tag \rightarrow :tag4302, ?room \rightarrow :room311, ?l \rightarrow ["14:00", "15:00"]\}$





# AnQL query evaluation

- for a BAP  $P$  a **substitution** is a mapping  $\theta : var(P) \rightarrow term(G)$ .
- $\theta(P)$  represents the triples obtained by replacing the variables in  $P$  according to  $\theta$ .
- $G \models \theta(P)$  denotes  $\theta(P)$  is entailed by  $G$ .
- $\llbracket P \rrbracket_G = \{ \theta \mid dom(\theta) = var(P) \text{ and } G \models \theta(P) \}$



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- $\llbracket P \rrbracket_G = \{\theta \mid dom(\theta) = var(P) \text{ and } G \models \theta(P)\}$

Extension of the semantics presented in Pérez et al. [2009]

## compatible substitutions (extension)

- Two substitutions  $\theta_1, \theta_2$  are **compatible** if the value for all shared annotation variables  $v$  is not “disjoint”:  $\theta_1(v) \otimes \theta_2(v) \neq \perp$
- The **union** of compatible substitutions  $\theta_1, \theta_2$ , the value of a shared annotation variable  $v$  is:  $\theta_1(v) \otimes \theta_2(v)$



# OPTIONALS

“When was :nuno located in room 311 optionally with another person.”

```
SELECT  ?1 ?person
WHERE   { ?tag1 :assignedTo :nuno .
          ?tag1 :locatedIn :room311 . ?1
          OPTIONAL { ?tag2 :assignedTo ?person .
                     ?tag2 :locatedIn :room311 . ?1 } }
```

Sample input:

```
:tag4302 :assignedTo :nuno .
:tag4302 :locatedIn  :room311 . ["13:48", "14:34"]
:tag4304 :assignedTo :axel
:tag4304 :locatedIn  :room311 . ["14:26", "15:17"]
:tag4301 :assignedTo :antoine
:tag4301 :locatedIn  :room311 . ["13:31", "13:53"]
```



# OPTIONALS

“When was :nuno located in room 311 optionally with another person.”

```
SELECT  ?l ?person
WHERE  { ?tag1 :assignedTo :nuno .
        ?tag1 :locatedIn :room311 . ?l
        OPTIONAL { ?tag2 :assignedTo ?person .
                   ?tag2 :locatedIn :room311 . ?l } }
```

Sample input:

```
:tag4302 :assignedTo :nuno .
:tag4302 :locatedIn :room311 . ["13:48", "14:34"]
:tag4304 :assignedTo :axel
:tag4304 :locatedIn :room311 . ["14:26", "15:17"]
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:tag4301 :locatedIn :room311 . ["13:31", "13:53"]
```

$$\theta_1 = \{ ?l \rightarrow ["13:48", "14:34"] \}$$

Answers:



# OPTIONALS

“When was :nuno located in room 311 optionally with another person.”

```

SELECT  ?l ?person
WHERE   { ?tag1 :assignedTo :nuno .
          ?tag1 :locatedIn :room311 . ?l
          OPTIONAL { ?tag2 :assignedTo ?person .
                     ?tag2 :locatedIn :room311 . ?l } }

```

Sample input:

```

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:tag4304 :locatedIn :room311 . ["14:26", "15:17"]
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```

Answers:

$$\theta_1 = \{ ?l \rightarrow ["13:48", "14:34"] \}$$

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# OPTIONALS

“When was :nuno located in room 311 optionally with another person.”

```

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Sample input:

```

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:tag4301 :locatedIn  :room311 . ["13:31", "13:53"]

```

Answers:

$$\theta_1 = \{ ?l \rightarrow ["13:48", "14:34"] \}$$

$$\theta_2 = \{ ?l \rightarrow ["14:26", "14:34"], ?person \rightarrow :axel \}$$

$$\theta_3 = \{ ?l \rightarrow ["13:48", "13:53"], ?person \rightarrow :antoine \}$$



# OPTIONALS

“When was :nuno located in room 311 optionally with another person.”

```

SELECT  ?l ?person
WHERE   { ?tag1 :assignedTo :nuno .
          ?tag1 :locatedIn :room311 . ?l
          OPTIONAL { ?tag2 :assignedTo ?person .
                     ?tag2 :locatedIn :room311 . ?l } }

```

Sample input:

```

:tag4302 :assignedTo :nuno .
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:tag4304 :locatedIn  :room311 . ["14:26", "15:17"]
:tag4301 :assignedTo :antoine
:tag4301 :locatedIn  :room311 . ["13:31", "13:53"]

```

Answers:

$$\theta_1 = \{ ?l \rightarrow ["13:48", "14:34"] \}$$

$$\theta_2 = \{ ?l \rightarrow ["14:26", "14:34"], ?person \rightarrow :axel \}$$

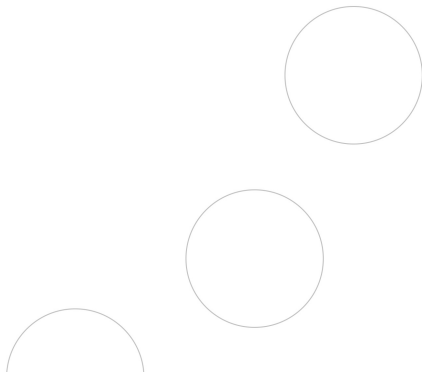
$$\theta_3 = \{ ?l \rightarrow ["13:48", "13:53"], ?person \rightarrow :antoine \}$$

OPTIONAL provide more information maybe restricting annotation values



# Further extensions

## Features under discussion in SPARQL 1.1







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## Features under discussion in SPARQL 1.1

“During how long was a tag located in a room?”

### Variable assignment & domain built-in functions

```
SELECT ?tag ?room ?dur
WHERE { ?tag :locatedIn ?room . ?1
        ASSIGN length(?1) AS ?dur }
```



# Further extensions

## Features under discussion in SPARQL 1.1

“During how long was a tag located in a room?”

### Variable assignment & domain built-in functions

```
SELECT ?tag ?room ?dur
WHERE { ?tag :locatedIn ?room . ?1
        ASSIGN length(?1) AS ?dur }
```

“What was the average length a tag was located in a room?”

### Aggregators

```
SELECT ?tag ?avgL
WHERE { ?tag :locatedIn ?room . ?1
        GROUPBY(?tag) AVG(length(?1)) AS ?avgL }
```



# Uniform Evaluation of Queries

## Uniform Evaluation of annotated and classical triple patterns

```
SELECT   ?l ?person
WHERE    { ?tag1 :assignedTo :nuno .
          ?tag1 :locatedIn :room311 . ?l
          OPTIONAL { ?tag2 :assignedTo ?person .
                    ?tag2 :locatedIn :room311 . ?l } }
```



# Uniform Evaluation of Queries

## Uniform Evaluation of annotated and classical triple patterns

```
SELECT ?l ?person
WHERE { ?tag1 :assignedTo :nuno . ?g1
        ?tag1 :locatedIn :room311 . ?l
        OPTIONAL { ?tag2 :assignedTo ?person . ?g1
                   ?tag2 :locatedIn :room311 . ?l } }
```

### Possible approaches:

- 1 adding the same annotation variable for each non-annotated triple



# Uniform Evaluation of Queries

## Uniform Evaluation of annotated and classical triple patterns

```
SELECT   ?l ?person
WHERE    { ?tag1 :assignedTo :nuno . ?g1
          ?tag1 :locatedIn :room311 . ?l
          OPTIONAL { ?tag2 :assignedTo ?person . ?g2
                    ?tag2 :locatedIn :room311 . ?l } }
```

### Possible approaches:

- 1 adding the same annotation variable for each non-annotated triple
- 2 adding a different annotation variable for each non-annotated triple



# Uniform Evaluation of Queries

## Uniform Evaluation of annotated and classical triple patterns

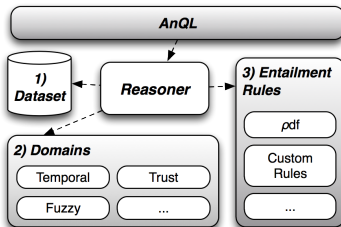
```
SELECT   ?l ?person
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          ?tag1 :locatedIn :room311 . ?l
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                    ?tag2 :locatedIn :room311 . ?l } }
```

### Possible approaches:

- 1 adding the same annotation variable for each non-annotated triple
- 2 adding a different annotation variable for each non-annotated triple
- 3 adding the  $\top$  element from the domain



# Implementation



- Prototype implementation of Annotated RDF(S) and AnQL
- Based on SWI-Prolog's semweb library
- Modular system: can use different domains and rulesets

More info and downloads available at:

<http://anql.deri.org>



# Conclusions

## Presented

- General framework for annotating RDF triples.
- Deductive system as extension of RDFS
- SPARQL extension for Annotated RDF(S)
- Includes the most salient SPARQL 1.1 features





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- General framework for annotating RDF triples.
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## Future work

- Refine combination of domains
- Uniform evaluation of queries
- Define interchangeable format for representing annotations



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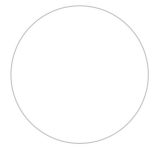
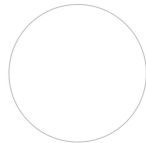
## Future work

- Refine combination of domains
- Uniform evaluation of queries
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Thank you! Questions?



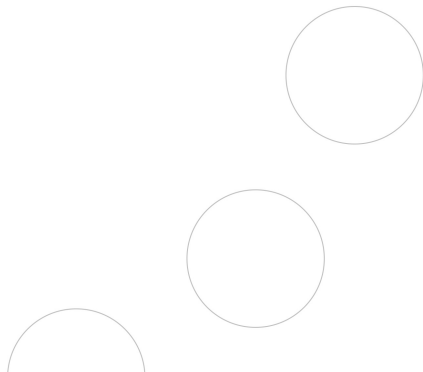
# Extra Slides





# AnQL query evaluation

Extension of the semantics presented in Pérez et al. [2009]





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- for a BAP  $P$  a **substitution** is a mapping  $\theta : var(P) \rightarrow term(G)$ .  
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- two substitutions  $\theta_1$  and  $\theta_2$  are  **$\otimes$ -compatible** iff:
  - ① The mappings agree on all non-annotated shared variables:  
 $\theta_1(x) = \theta_2(x), \quad x \text{ non-annot var} \in dom(\theta_1) \cap dom(\theta_2);$



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  - 2 All the shared annotation variables must not be “disjoint”:  
 $\theta_1(\lambda) \otimes \theta_2(\lambda) \neq \perp$ ,  $\lambda$  annot var  $\in dom(\theta_1) \cap dom(\theta_2)$ .





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 $\theta_1(\lambda) \otimes \theta_2(\lambda) \neq \perp$ ,  $\lambda$  annot var  $\in dom(\theta_1) \cap dom(\theta_2)$ .
- $\theta_1, \theta_2$   **$\otimes$ -compatible**,  $\theta_1 \otimes \theta_2 = \theta_1 \cup \theta_2$ , except any annotation variable  $\lambda \in dom(\theta_1) \cap dom(\theta_2)$ ,  $(\theta_1 \otimes \theta_2)(\lambda) = \theta_1(\lambda) \otimes \theta_2(\lambda)$ .



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$

Answers of a BAP  $P$  are the substitutions *entailed* by  $G$



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
- $\llbracket P_1 \text{ AND } P_2 \rrbracket_G = \{\theta_1 \otimes \theta_2 \mid \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1 \text{ and } \theta_2 \text{ } \otimes\text{-compatible}\}$

Answers of two AGPs are the substitutions that are  $\otimes$ -compatible



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
- $\llbracket P_1 \text{ AND } P_2 \rrbracket_G = \{\theta_1 \otimes \theta_2 \mid \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1 \text{ and } \theta_2 \text{ } \otimes\text{-compatible}\}$
- $\llbracket P_1 \text{ UNION } P_2 \rrbracket_G = \llbracket P_1 \rrbracket_G \cup \llbracket P_2 \rrbracket_G$

Answers for the UNION of two AGPs is the *union* of the substitutions



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
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- $\llbracket P_1 \text{ UNION } P_2 \rrbracket_G = \llbracket P_1 \rrbracket_G \cup \llbracket P_2 \rrbracket_G$
- $\llbracket P_1 \text{ FILTER } R \rrbracket_G = \{\theta \mid \theta \in \llbracket P_1 \rrbracket_G \text{ and } R\theta \text{ is true}\}$

$R\theta$  is true iff: ...

- (9)  $R = (x \preceq y)$  with  $x, y \in \text{dom}(\theta) \cup L$  and  $\theta(x) \preceq \theta(y)$ ;
- (10)  $R = p(\vec{z})$  with  $p(\vec{z})\theta = \text{true}$  iff  $p(\theta(\vec{z})) = \text{true}$ ,  $p$  built-in predicate.



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
- $\llbracket P_1 \text{ AND } P_2 \rrbracket_G = \{\theta_1 \otimes \theta_2 \mid \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1 \text{ and } \theta_2 \text{ } \otimes\text{-compatible}\}$
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- $\llbracket P_1 \text{ OPTIONAL } P_2[R] \rrbracket_G = \{\theta \mid \text{and } \theta \text{ meets one of the following conditions:}$

}

Answers for an OPTIONAL where the  $P_2$  may contain a FILTER expression are:



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
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- $\llbracket P_1 \text{ OPTIONAL } P_2[R] \rrbracket_G = \{\theta \mid \text{and } \theta \text{ meets one of the following conditions:}$ 
  - ①  $\theta = \theta_1 \otimes \theta_2, \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G \text{ are } \otimes\text{-compatible, and } R\theta \text{ is true}$

}

Keep compatible substitutions that make the FILTER  $R$  true



# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
  - $\llbracket P_1 \text{ AND } P_2 \rrbracket_G = \{\theta_1 \otimes \theta_2 \mid \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1 \text{ and } \theta_2 \text{ } \otimes\text{-compatible}\}$
  - $\llbracket P_1 \text{ UNION } P_2 \rrbracket_G = \llbracket P_1 \rrbracket_G \cup \llbracket P_2 \rrbracket_G$
  - $\llbracket P_1 \text{ FILTER } R \rrbracket_G = \{\theta \mid \theta \in \llbracket P_1 \rrbracket_G \text{ and } R\theta \text{ is true}\}$
  - $\llbracket P_1 \text{ OPTIONAL } P_2[R] \rrbracket_G = \{\theta \mid \text{and } \theta \text{ meets one of the following conditions:}$ 
    - ①  $\theta = \theta_1 \otimes \theta_2, \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G$  are  $\otimes$ -compatible, and  $R\theta$  is true
    - ②  $\theta = \theta_1 \in \llbracket P_1 \rrbracket_G$  and  $\forall \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1, \theta_2 \otimes\text{-compatible}, R(\theta_1 \otimes \theta_2)$  is true, and all annotation variables  $\lambda \in \text{dom}(\theta_1) \cap \text{dom}(\theta_2) \theta_2(\lambda) \prec \theta_1(\lambda)$
- }

Keep substitutions  $\theta_1$  if, for all  $\theta_2$  such that  $\theta_1$  and  $\theta_2$  are  $\otimes$ -compatible and for all the shared annotation variables between those substitutions,  $\theta_1$  has a “better” annotation





# AnQL query evaluation (cont.)

Let  $P$  be a BAP,  $P_i$  AGPs,  $G$  an annotated graph and  $R$  a filter expression:

- $\llbracket P \rrbracket_G = \{\theta \mid \text{dom}(\theta) = \text{var}(P) \text{ and } G \models \theta(P)\}$
- $\llbracket P_1 \text{ AND } P_2 \rrbracket_G = \{\theta_1 \otimes \theta_2 \mid \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1 \text{ and } \theta_2 \text{ } \otimes\text{-compatible}\}$
- $\llbracket P_1 \text{ UNION } P_2 \rrbracket_G = \llbracket P_1 \rrbracket_G \cup \llbracket P_2 \rrbracket_G$
- $\llbracket P_1 \text{ FILTER } R \rrbracket_G = \{\theta \mid \theta \in \llbracket P_1 \rrbracket_G \text{ and } R\theta \text{ is true}\}$
- $\llbracket P_1 \text{ OPTIONAL } P_2[R] \rrbracket_G = \{\theta \mid \text{and } \theta \text{ meets one of the following conditions:}$ 
  - ①  $\theta = \theta_1 \otimes \theta_2, \theta_1 \in \llbracket P_1 \rrbracket_G, \theta_2 \in \llbracket P_2 \rrbracket_G$  are  $\otimes$ -compatible, and  $R\theta$  is true
  - ②  $\theta = \theta_1 \in \llbracket P_1 \rrbracket_G$  and  $\forall \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1, \theta_2 \otimes\text{-compatible}, R(\theta_1 \otimes \theta_2)$  is true, and all annotation variables  $\lambda \in \text{dom}(\theta_1) \cap \text{dom}(\theta_2) \theta_2(\lambda) \prec \theta_1(\lambda)$
  - ③  $\theta = \theta_1 \in \llbracket P_1 \rrbracket_G$  and  $\forall \theta_2 \in \llbracket P_2 \rrbracket_G, \theta_1, \theta_2 \otimes\text{-compatible } R(\theta_1 \otimes \theta_2)$  is false

Keep substitutions  $\theta_1$  if, for all  $\theta_2$  such that  $\theta_1$  and  $\theta_2$  are  $\otimes$ -compatible, the FILTER expression is false



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