

# ReadE: Learning Relation-Dependent Entity Representation for Knowledge Graph Completion

Anonymous ACL submission

## Abstract

Conventional knowledge graph embedding methods learn semantic representations for entities considering their intrinsic interactions through powerful graph neural networks. However, previous methods represent each node solely with a coarse-grained unique representation, regardless of the variance of emphasis of entity semantics by different relations. To tackle this problem, we propose ReadE, a method to learn relation-dependent entity representations of which the semantic information is emphasized by varied relations types. First, we propose a relation-controlled gating mechanism targeting on utilizing the relation to control the information flow in the aggregation step of the graph neural network. Second, we propose a contrastive learning method with mixing both relation-level and entity-level negative samples to enhance semantics preserved in relation-dependent entity representations. Experiments on three benchmarks show that our proposed model outperforms all strong baselines. The code will be made open-sourced on Github.

## 1 Introduction

Knowledge graph (KG) is a semantic network and can be used to represent the relations of different entities in the real world. Due to the existence of huge amount of potential facts, existing KGs, like NELL (Carlson et al., 2010) and YAGO3 (Mahdisoltani et al., 2015), mostly face the problem of completing the missing relations, which is known as the knowledge graph completion (KGC) task. In this work, we mainly focus on the task of how to predict the missing entity in incomplete triplets like  $\langle \textit{entity}, \textit{relation}, ? \rangle$ .

To complete the KG, a fundamental task is to learn informative and meaningful representations for the entities and relations in KG, based on which the missing links can be predicted. Given a triplet  $\langle e_1, r, e_2 \rangle$ , TransE (Bordes et al., 2013) proposed to learn the representations that satisfy the

property of translation invariance  $e_1 + r \approx e_2$ . To increase the model’s representational ability, in ConvE (Dettmers et al., 2018), a multi-layer convolution network is used to predict missing entities. However, all these methods process each triplet independently, ignoring the neighborhood information of a given entity in the KG. To leverage the connection structure information of a graph, many methods have proposed to include the neighbor’s information into the entity representation by using various kinds of graph neural networks (GNNs), like using graph attention network (GAT) in Nathani et al. (2019), weighted graph convolutional network (WGCN) in Shang et al. (2019) and the heterogeneous relation attention network (HRAN) in Li et al. (2021).

Intuitively, an entity could contain information from many different aspects. For example, the entity *MichaelJordan*, who was born in Brooklyn in 1963, contains information about the date of birth and place of birth simultaneously. Therefore, when an incomplete triplet  $\langle \textit{MichaelJordan}, \textit{YearOfBirth}, ? \rangle$  is given, if the information related to the relation *YearOfBirth* among many different aspects of information in the entity *MichaelJordan* can be emphasized, it would be easier to predict the ground-truth missing entity *1963*. Therefore, it is important for every entity to have a representation that is dependent on the concrete relation. That is, when interacting with different relations, an entity need to show different representations. However, existing methods only learn a static representation for an entity, irrespective of different relations they may interact with. For relation-irrelevant representations, obviously, different aspects of information cannot be shown when interacting with different relations.

In this paper, we propose the representation learning method ReadE, a method to learn **Relation-dependent Entity** representations. In the proposed method, the representation of an entity

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can vary according to the relation that is interacted with. To this end, we first propose a relation-controlled gating mechanism that is used to control which and how much information can flow into the interested entity’s representation during the aggregation step. Since a good relation representation can make the relation-controlled gating mechanism work better, in contrast to previous methods, a similarity-preserving relation representation is learned for every relation through GCN, hoping that similar relations (e.g., *PlaceOfBorn* and *PlaceOfResidence*) in the graph can share similar representations, capturing the correlation among different relations. Moreover, we further propose to use contrastive learning to enhance the semantic information in our relation-dependent entity representation, in which a novel two-level generation process of negative samples are proposed. Extensive experiments are conducted on three benchmarks for the knowledge graph completion task. The experiments show that our ReadE outperforms all strong baselines and further analyses verify the validity of each proposed component.

## 2 Preliminary

Due to the strong ability to learn commonalities among adjacent nodes for graph-structured data, graph neural networks (GNN) have been widely used to learn the entity representations of knowledge graphs in recent years (Nathani et al., 2019; Shang et al., 2019; Li et al., 2021). The GNN-based models generally share the common architecture of using a GNN to learn the entity representation and then applying a score function to evaluate the matching degree of a triplet <head entity, relation, tail entity>. Because of the similarity among these methods, here we take the SACN (Shang et al., 2019) as an example to illustrate the basic principles behind the GNN-based entity representation learning methods.

By viewing the KG as an entity graph  $G_e$ , in which each node and edge represents an entity and relation, respectively, SACN applies a  $L$ -layer weighted graph convolutional network onto graph  $G_e$  to obtain entity representations

$$z_i^l = \sigma \left( \sum_{j \in \mathcal{N}_e(i)} \alpha_{i,j} z_j^{l-1} \mathbf{W}^{l-1} + z_i^{l-1} \mathbf{W}^{l-1} \right), \quad (1)$$

where  $\ell = 1, 2, \dots, L$  denotes the  $\ell$ -th layer of GNN;  $\mathcal{N}_e(i)$  represents the neighbors of entity  $i$

in graph  $G_e$ ;  $z_i^\ell$  denotes the embedding of  $i$ -th entity  $e_i$  obtained at the  $\ell$ -th layer, with the initial embedding  $z_i^0 \in \mathbb{R}^{d_e}$  initialized from random Gaussian noise;  $\mathbf{W}^l \in \mathbb{R}^{d_e \times d_e}$  is the network parameter at  $(\ell - 1)$ -th layer; the coefficient  $\alpha_{i,j}$  is used to control the interaction strength between node  $i$  and  $j$ ; and  $\sigma(\cdot)$  is the sigmoid activation function.  $z_i^L$  from the  $L$ -th layer is then used to represent the final embedding of the  $i$ -th entity  $e_i$ , that is,

$$z_i = z_i^L. \quad (2)$$

Besides the entity embedding  $z_i$ , SACN also learns an embedding for every relation  $r$ . For the  $k$ -th relation  $r_k$ , its embedding  $\mathbf{h}_k \in \mathbb{R}^{d_e}$  is directly initialized from a random Gaussian noise.

Using the entity embeddings  $z_i$  and relation embeddings  $\mathbf{h}$  obtained above, for a given triplet  $\langle e_i, r_k, e_j \rangle$ , the SACN evaluates a matching score for it with a scoring function of the form

$$\varphi(z_i, \mathbf{h}_k, z_j) = CNN([z_i; \mathbf{h}_k]) \mathbf{W}^c z_j^T, \quad (3)$$

where  $CNN(\cdot)$  denotes a convolutional network applied to a  $2 \times d_e$  matrix  $[z_i; \mathbf{h}_k]$ . The model will compute the probability that the given triplet  $\langle e_i, r_k, e_j \rangle$  is true as

$$p(e_i, r_k, e_j) = \sigma(\varphi(z_i, \mathbf{h}_k, z_j)). \quad (4)$$

Given a training dataset containing both of true and false triplets, the model parameters and initial embeddings can be optimized by minimizing the following cross-entropy loss

$$\mathcal{L}_c = \frac{-1}{N} \sum_{n=1}^N (y_n \log p_n + (1 - y_n) \log(1 - p_n)) \quad (5)$$

where  $p_n$  denotes the probability of truth for the  $n$ -th triplet computed according to (4); and  $y_n$  is the ground-truth label, which is 1 for true triplet and 0 otherwise.

## 3 Methodologies

In this section, we propose our ReadE. First, we present how to learn relation-dependent entity representations through a relation-controlled gating mechanism, then introduce a novel contrastive learning method with mixing both relation-level and entity-level negative samples to enhance the entities’ semantic information.

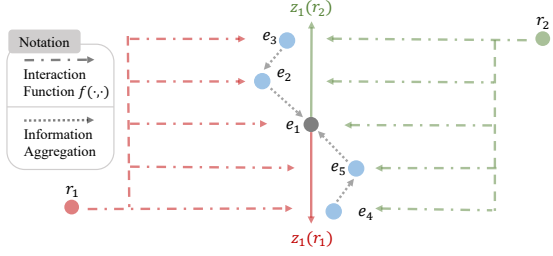


Figure 1: The overall framework of our designed relation-dependent entity representation learning method.

### 3.1 Relation-Dependent Entity Representation Learning

Existing methods mainly focus on how to learn good representations for the entities and relations so that the relevance among the entities and relations in true triplets can be retained as much as possible. However, in all of these existing methods, the learned representation of an entity is never dependent on the relations, that is, the representation maintains one appearance under different relations. However, no matter the problem is to predict the tail entity given the head entity and relation  $\langle e_i, r_k, ? \rangle$ , or to predict the head entity given the tail entity and relation  $\langle ?, r_k, e_j \rangle$ , the relation is always available. Thus, if we learn for every entity a collection of representations, with each corresponding to a relation, when facing the entity prediction task  $\langle e_i, r_k, ? \rangle$  or  $\langle ?, r_k, e_j \rangle$ , we can always choose to use the entity representation under the specific relation  $r_k$ . To the convenience of presentation, in the following, we denote the representation of  $i$ -th entity  $e_i$  under relation  $r$  as  $z_i(r)$ .

The relation-dependent entity representation under relation  $r$  can be learned with a GNN as

$$z_i^l(r) = \frac{1}{|\mathcal{N}_e(i)|} \sum_{j \in \mathcal{N}_e(i)} f(\mathbf{h}_r, z_j^{l-1}(r)) \mathbf{W}^{l-1} + f(\mathbf{h}_r, z_i^{l-1}(r)) \mathbf{W}^{l-1}. \quad (6)$$

Here,  $f(\cdot, \cdot)$  is the interaction function between the entity and relation and is designed as

$$f(\mathbf{h}_r, z_i^{l-1}(r)) = \sigma(\mathbf{W}^f \mathbf{h}_r + \mathbf{g}^f) \odot z_i^{l-1}(r), \quad (7)$$

where  $\mathbf{W}^f \in \mathbb{R}^{d_e \times d_r}$ ,  $\mathbf{g}^f \in \mathbb{R}^{d_e}$  are parameters to be learned,  $\odot$  is the feature-wise product. The final entity representation  $z_i(r)$  is obtained by applying the sigmoid function  $\sigma$  to the output at the last layer, i.e.,  $z_i(r) = \sigma(z_i^L(r))$ . The function

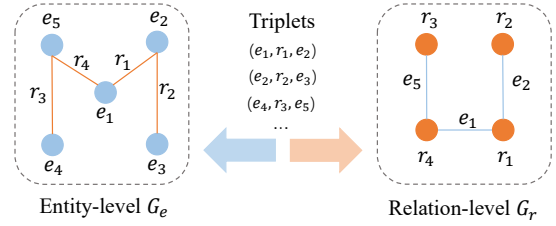


Figure 2: The illustration of our graph construction methods of  $G_r$  and  $G_e$ .

$f(\cdot, \cdot)$  plays a role of relation-controlled gate that can determine which dimension's information in the entity representation  $z_i^{l-1}$  can be flowed into neighboring nodes. If the relevance between the relation and an entity is weak, the  $\sigma(\cdot)$  function will output a value close to zero, cutting off the information flowing into to the entity's neighbors.

The reason why we design this relation-controlled gate function is that KGs are usually densely connected Lovelace et al. (2021), making a GCN-based encoder prone to aggregate from its neighbors the irrelevant information *w.r.t.* the considered relation. Thus, as illustrated in Fig 1, as aggregating the information from neighbors, we first let the relation control which and how much information can flow into the interested entity's representation, making the entity have different representations under different relations.

### Similarity-preserving Relation Representation Learning

The relation dependence in the proposed entity representations is achieved by incorporating the relation representations  $\mathbf{h}_k$  into the entities' representation updating process through a gating mechanism. However, the relation representations used in the gating function (7) do not contain any correlation information among different relations as they are directly obtained from their initial embeddings without going through any information exchanging process. In practice, different relations are related, rather than isolated, to each other. For example, in KG, the relation *PlaceOfBorn* and *PlaceOfResidence* are both related to the city entity, suggesting they should share some common semantic information in their representations. To have the relation representations to reflect this kind of similarities, we propose to construct a relational graph  $G_r$  from the KG by representing every relation as a node and adding an edge between two relations if they refer to a common entity, as illustrated in Fig 2. With the relation graph  $G_r$ , we can

now apply the graph neural networks (*e.g.*, GCN) on the graph to obtain relation representations

$$\mathbf{h}_r^l = \sigma \left( \sum_{j \in \mathcal{N}_r(r)} \mathbf{h}_j^{l-1} \mathbf{W}_r^{l-1} + \mathbf{h}_r^{l-1} \mathbf{W}_r^{l-1} \right), \quad (8)$$

where  $\ell = 1, 2, \dots, L'$  denotes the  $\ell$ -th layer of GCN; the initial embedding  $\mathbf{h}_r^0$  is initialized by random Gaussian noise;  $\mathcal{N}_r(\cdot)$  denotes the set of the neighbors of relation  $r$  in  $G_r$ ; and  $\mathbf{W}_r^l \in \mathbb{R}^{d_r \times d_r}$  is the GCN parameter. We set the output  $\mathbf{h}_r^{L'}$  from the last layer as the final relation representation, that is,

$$\mathbf{h}_r = \mathbf{h}_r^{L'}. \quad (9)$$

Thanks to the message-passing process during the learning, the representation of a relation is not isolated anymore, but is related to other relations that share common entities. In this way, the common information of different relations or their similarity information can be manifested in the learned representations. By substituting the similarity-preserved relation representation (9) into entity representation updating equation (6), the final relation-dependent entity representation updating method is obtained.

### 3.2 Enhancing Semantics of Entity Representation with Contrastive Learning

The link prediction task is to predict the missing head or tail entity given the other two components. Thus, similar to the classification tasks in images and texts, if more semantic information of entities are preserved in their representations, better prediction performance can be expected. Technically, contrastive learning can be understood as finding pairs of positive and negative instances and then trying to reducing the distance between positive pairs while enlarging that between negative ones under different contrast losses. Among them, the NT-Xent contrast loss below is used most widely

$$l = -\log \frac{\mathcal{D}(\mathbf{u}_i^{(1)}, \mathbf{u}_i^{(2)})}{\mathcal{D}(\mathbf{u}_i^{(1)}, \mathbf{u}_i^{(2)}) + \sum_{j \neq i, m=1,2} \mathcal{D}(\mathbf{u}_i^{(1)}, \mathbf{u}_j^{(m)})},$$

where  $\mathbf{u}_i^{(m)}$  represents the  $m$ -th view of the  $i$ -th instance. Different views from the same instances are generally treated as positive pairs, while views from different instances are considered as negative pairs. The key of using contrastive learning lies at how to find effective positive and negative pairs, which can determine whether semantic information

can be well preserved in the representations. For images, both of the positive and negative pairs can be easily obtained by applying transformations to the same or different images. However, for graphs, especially for knowledge graphs that contain the additional information of relation, generating effective positive and negative pairs is not that straightforward at all.

To generate positive pairs, inspired by the works that apply self-supervised learning on general graphs (Velickovic et al., 2019; Xia et al., 2021; Yu et al., 2021), we perturb the knowledge graph by randomly dropping some nodes and edges and then apply the aforementioned methods on the perturbed graph to obtain the entities' representations  $\mathbf{z}_i'$ . Then, the representations  $\mathbf{z}_i$  and  $\mathbf{z}_i'$  can be viewed as a positive pair. For convenience of presentation, the two representations  $\mathbf{z}_i$  and  $\mathbf{z}_i'$  are deemed as two views of entity  $i$ , and are denoted as  $\mathbf{z}_i^{(1)}$  and  $\mathbf{z}_i^{(2)}$ . The concrete steps to perturb the KG are described in the Appendix B.

As for the generation of negative pairs, a common method is to treat views of other entities as negative samples. However, in order to learn more meaningful semantic information in KG, we suggest to collect negative samples in two different levels, *i.e.*, the relation level and the entity level.

**Relation-Level Negative Samples** For a relation-dependent entity representation  $\mathbf{z}_i(r)$ , we hope it can retain discriminative semantic information of entity  $i$  under the specific relation of  $r$ . To strength the objective that the semantic information contained in  $\mathbf{z}_i(r)$  is exclusive to the relation  $r$ , we propose to generate negative samples under the same entity by using different relations  $r'$  with  $r' \neq r$ . Specifically, for the representation of entity  $e_i$  under the relation  $r$ , *i.e.*,  $\mathbf{z}_i(r)$ , its relation-level negative samples is defined to be from the following set

$$\mathcal{Z}_i^{neg}(r) = \left\{ \mathbf{z}_i^{(1)}(r'), \mathbf{z}_i^{(2)}(r') \mid r' \neq r \right\}. \quad (10)$$

**Entity-Level Negative Samples** For an entity representation  $\mathbf{z}_i(r)$ , in addition to include exclusive semantic information comparing to entity representations under other relations  $\mathbf{z}_i(r')$  with  $r' \neq r$ , it should also contain exclusive semantic information when comparing with other entities. Therefore, we define the entity-level negative samples of  $\mathbf{z}_i(r)$  as

$$\tilde{\mathcal{Z}}_i^{neg}(r) = \left\{ \mathbf{z}_j^{(1)}(r), \mathbf{z}_j^{(2)}(r) \mid j \neq i \right\}, \quad (11)$$

where we require the relation in other entities to be the same as the considered entity. In the implementation, the entity  $j$  can just be the other entities from the same mini-batch.

With the two negative sample sets, we can define the final contrastive learning loss as

$$\ell_i^{(1)} = -\log \frac{\mathcal{D}_{pos}}{\mathcal{D}_{pos} + \sum_{\mathbf{u} \in \mathcal{Z}_i(r)} \mathcal{D}(\mathbf{z}_i^{(1)}(r), \mathbf{u})}, \quad (12)$$

where  $\mathcal{Z}_i(r) \triangleq \mathcal{Z}_i^{neg}(r) \cup \tilde{\mathcal{Z}}_i^{neg}(r)$ ; and  $\mathcal{D}_{pos} \triangleq \mathcal{D}(\mathbf{z}_i^{(1)}(r), \mathbf{z}_i^{(2)}(r))$ . Here,  $\mathcal{D}(\mathbf{z}_i^{(1)}(k), \mathbf{z}_i^{(2)}(k))$  is calculated as

$$\mathcal{D}(\mathbf{z}_i^{(1)}(k), \mathbf{z}_i^{(2)}(k)) = e^{sim(\mathbf{z}_i^{(1)}(k), \mathbf{z}_i^{(2)}(k))/\tau}, \quad (13)$$

where  $sim(\cdot, \cdot)$  denotes the cosine similarity between vectors, and  $\tau$  is a temperature parameter controlling the concentration level of the distribution (Hinton et al., 2015). By averaging over a mini-batch of size  $N$ , the final contrastive loss  $\mathcal{L}_{cl}$  is

$$\mathcal{L}_{cl} = \frac{1}{2N} \sum_{i=1}^N (\ell_i^{(1)} + \ell_i^{(2)}). \quad (14)$$

By minimizing  $\mathcal{L}_{cl}$  with both the relation-level and entity-level negative samples, our ReadE can learn a entity representation preserving more meaningful semantics. Finally, we unify the objective of the KGC task and the contrastive learning as:

$$\mathcal{L} = \mathcal{L}_c + \lambda \mathcal{L}_{cl}, \quad (15)$$

where  $\lambda$  is a hyper-parameter used to control the trade-off between the loss function.

## 4 Experiments

### 4.1 Datasets, Evaluation and Baselines

**Datasets** We evaluate the proposed ReadE model on three benchmark datasets from different domains. 1) *FB15k-237* (Toutanova and Chen, 2015) contains the knowledge base relation triplets including real-world named entities and the relation. The FB15k-237 is the subset of the FB15K (Bordes et al., 2013), which is originally collected from Freebase. Different from the FB15K, the inverse relations are removed from FB15k-237. 2) *WN18RR* consists of English phrases and the corresponding semantic relations, which is derived from the WN18 (Bordes et al., 2013). Similar to FB15k-237, the inverse relations and the leaky data are removed

Dataset	FB15k-237	WN18RR	UMLS
Entities	14541	40943	135
Relations	237	11	46
Train Edges	272115	86835	5216
Dev Edges	17535	3034	652
Test Edges	20466	652	661

Table 1: The statistics of the three benchmark datasets.

from the WN18RR. 3) *UMLS* (Kok and Domingos, 2007), named Unified Medical Language System, is a medical KG dataset. It contains 135 medical entities and 46 semantic relations. Statistics of these three datasets are listed in Table 1.

**Evaluation Metrics** In this work, we evaluate the performance of our ReadE model on the link prediction task, *i.e.*, predicting the missing entity. In the inference phase, given an incomplete triplet, our model takes all the entities as the candidates and outputs the probabilities over all the candidates. Then each candidate is re-ranked according to their probabilities to calculate the Mean rank (MR), Mean reciprocal rank (MRR), and Hits@N. MR is the average of the rankings of entities predicted correctly over all triplets while MRR targets at the average of reciprocal rankings. Hits@N denotes the ratio of those predicted correctly entities which are ranked in top-N. Also, We follow Shang et al. (2019) to use the filtered setting Bordes et al. (2013), which will filter out all valid triplets before ranking.

In addition, we follow Sun et al. (2020) to adopt the ‘‘RANDOM’’ protocol to handle the situation that the ground-truth triplets have the same scores as the negative triplets, which is caused by the float precision problem. Namely, the rankings of triplets with the same scores will be randomly determined.

**Baselines** We compare our model with following strong baselines: TransE (Bordes et al., 2013), DistMult (Yang et al., 2015), ComplEx (Trouillon et al., 2016), ConvE (Dettmers et al., 2018), ConvKB (Nguyen et al., 2018), R-GCN (Schlichtkrull et al., 2018), RotatE (Sun et al., 2019), SACN (Shang et al., 2019), InteractE (Vashishth et al., 2020), TorusE (Ebisu and Ichise, 2020), PairRE (Chao et al., 2021), HRAN (Li et al., 2021).

Model	FB15k-237			WN18RR			UMLS	
	Hits			Hits			Hits	
	@10	@1	MRR	@10	@1	MRR	@10	MR
TransE	0.441	0.198	0.279	0.532	0.043	0.243	0.989	1.84
DistMult	0.446	0.199	0.281	0.504	0.412	0.444	0.846	5.52
ComplEx	0.450	0.194	0.278	0.530	0.409	0.449	0.967	2.59
ConvE	0.497	0.225	0.312	0.531	0.419	0.456	0.990*	<b>1.00*</b>
ConvKB	0.421	0.155	0.243	0.520	0.400	0.430	—	—
R-GCN	0.300	0.100	0.164	0.207	0.080	0.123	—	—
RotatE	0.533	0.241	0.338	0.571	0.428	0.476	—	—
SACN	0.536	0.261	0.352	0.535	0.427	0.470	—	—
InteractE	0.535	0.263	0.354	0.528	—	0.463	—	—
TorusE	0.484	0.217	0.316	0.512	0.422	0.452	—	—
PairRE	0.544	0.256	0.351	—	—	—	—	—
HRAN	0.541	0.263	0.355	0.542	0.450	0.479	—	—
<b>ReadE</b>	<b>0.562</b>	<b>0.275</b>	<b>0.371</b>	<b>0.555</b>	<b>0.460</b>	<b>0.490</b>	<b>0.993</b>	1.43
<b>Improvements</b>	<b>3.3%</b>	<b>4.6%</b>	<b>4.5%</b>	<b>2.4%</b>	<b>2.2%</b>	<b>2.3%</b>	—	—

Table 2: Performances on FB15k-237, WN18RR, and UMLS datasets. The performances of ConvE in the UMLS dataset are taken from the author’s Github and are marked with \*.

## 4.2 Experimental Results

The experimental results of our ReadE and the strong baselines on FB15k-237, WN18RR, and UMLS are shown in Table 2. From the table, the proposed ReadE outperforms the strongest baseline HRAN significantly, with relative MRR improvement of 4.5% and 2.3% on FB15K-237 and WN18RR, respectively. Among all the baselines, SACN is the most similar one to our model. SACN and our ReadE both utilize the Conv-TransE model to predict the missing entity, and the main difference is that SACN learns a unique representation for each entity while ReadE learns a relation-dependent entity representation instead. It can be seen that our model outperforms SACN by 5.4% and 4.3% in MRR on FB15K-237 and WN18RR respectively, showing the effectiveness of the relation-dependent entity representation.

On UMLS, ReadE shows comparable performance with baselines. However, it is undeniable that ConvE outperforms our model on UMLS under the MR criterion. This may be due to the small size of UMLS, which leads to the over-fitting issue when injecting the graph structure information into the entity representation. However, On FB15k-237 and WN18RR with the more complex graph structure, our ReadE outperforms ConvE by 18.9% and 7.5% under the MRR criterion.

## 4.3 Impacts of Different Components

In this section, we give a deep insight into how much improvement different components contribute to the model performance. To do this, we evaluate the performance of variants of ReadE that exclude one or more components that have a large impact on the performance.

Specifically, three components included in ReadE are considered, and we follow our model’s pipeline to describe the three components in turn: (1) Component *C*. It uses the relation to Control the neighborhood information aggregation during the GCN-based encoding stage to generate the relation-dependent entity representation. Without it, every entity will be assigned a unique representation instead. (2) Component *R*. It means the similarity-preserving Relation representation learning component which obtains the relation representation by applying GCN on  $G_r$ . Without it, the relation representation degenerates the one ignoring its similarity information. (3) Component *D*. The contrastive learning component with Double levels of negative samples is designed to enhance the semantics of the relation-dependent entity representation. Dropping this component means that we remove the contrastive loss  $\mathcal{L}_{cl}$ . Please note that the *D* component is based on the *C* component, if we drop the *C* component, the *D* component will be dropped simultaneously. Based on the above-

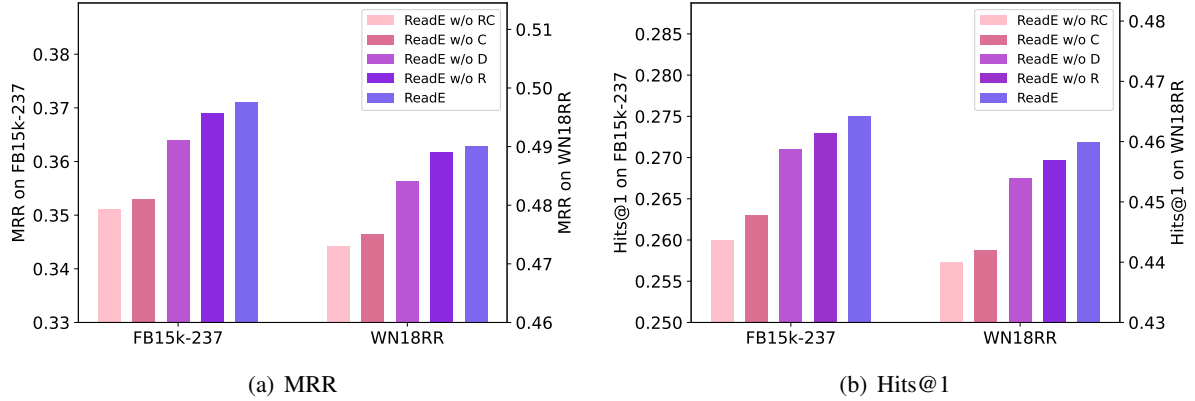


Figure 3: Performances of variants of ReadE that exclude one or more components on FB15k-237 and WN18RR.

defined components, we propose four variants of ReadE: ReadE w/o  $R$ , ReadE w/o  $D$ , ReadE w/o  $C$ , ReadE w/o  $RC$ . The four variants are compared with the original ReadE on FB15k-237 and WN18RR and results are shown in Fig 3.

From the result, we can have the following observations. First, ReadE w/o  $C$  which removes the most basic component  $C$  will induce a significant performance drop when compared with the complete ReadE, suggesting the importance of taking the relation into account when learning the entity representation. Second, without using the proposed CL component (*i.e.*, ReadE w/o  $D$ ), an immediate performance drop is observed on FB15k-237 and WN18RR, which demonstrates the necessity of utilizing the designed CL method to further improve our relation-dependent entity representation. Third, ReadE w/o  $C$  is better than ReadE w/o  $RC$ , demonstrating that even if we solely learn a unique relation-independent entity representation as previous methods do, improving the quality of the relation representation can still improve the performance. Also, ReadE w/o  $R$  works worse than ReadE, which indicates that similarity-preserving relation representations can better control the information aggregation from the entity’s neighbors. Last but not least, if we remove all three components (*i.e.*, ReadE w/o  $RC$ ), the performance is poorest, confirming the validity of the proposed ReadE.

#### 4.4 Impacts of Different Levels of Negative Samples

In this section, we evaluate the influence of relation-level and entity-level negative samples in the denominator of (14). MRR on FB15-237 and WN18RR datasets when using one of these two

	FB15-237	WN18RR
w/o Entire $\mathcal{L}_{cl}$	0.364	0.484
+ Relation-Level	<b>0.369</b>	<b>0.488</b>
+ Entity-Level	0.366	0.486
+ Entire $\mathcal{L}_{cl}$	0.371	0.490

Table 3: MRR when using one of the relation-level and entity-level negative samples on FB15-237 and WN18RR.

kinds of negative samples are shown in Table 3. Note that no matter which negative samples we use, the positive samples are unchanged and always be considered when calculating the contrastive loss.

We can see that the performances brought by CL with solely relation-level negative samples are more excellent than the ones brought by CL with solely entity-level negative samples on both FB15k-237 and WN18RR. In this paper, given an entity, CL with relation-level negative samples aims to increase the distances between different relation-dependent entity representations of it among different relations, which is consistent with our motivation of learning an entity representation of which semantics will vary depending on its relation. Therefore, it may explain why CL with relation-level negative samples achieves a greater result. Also, the model performs best if two levels of negative samples are considered together at the same time, indicating the credibility of the proposed CL method to enhance the entity’s semantics.

#### 4.5 Impacts of Parameter $\lambda$

In ReadE, we introduce the hyper-parameter  $\lambda$ , which controls the trade-off between the cross-entropy loss and the contrastive loss. In this section, we investigate the sensitivity of  $\lambda$ . We manually

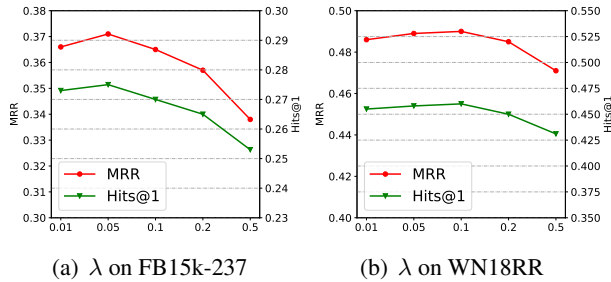


Figure 4: MRR and Hits@1 of ReadE under different values of  $\lambda$  on FB15k-237 and WN18RR.

select the values of  $\lambda$  from  $\{0.01, 0.05, 0.1, 0.2, 0.5\}$ . MRR and Hits@1 w.r.t  $\lambda$  on FB15k-237 and WN18RR datasets are illustrated in Fig 4.

It is shown that as  $\lambda$  grows up, the performance of ReadE first increases and reaches the peak when  $\lambda = 0.05$  and  $0.1$  on FB15k-237 and WN18RR respectively. Afterwards, if  $\lambda$  is larger, the improvement is neutralized and lost. This phenomenon shows that the performance is sensitive to the hyperparameter  $\lambda$ . And in practice, we suggest that the loss weight for the contrastive loss can be set to  $[0.01, 0.1]$  for exploiting the potentialities of the model.

## 5 Related Work

Nowadays, knowledge graph embedding (KGE) methods play an important role in KGC. Given a triplet  $\langle e_1, r, e_2 \rangle$ , TransE (Bordes et al., 2013) learns the representation of the entity and relation according to the translation-based constraint of  $e_1 + r \approx e_2$ . Later, TransH (Wang et al., 2014), TransR (Lin et al., 2015), and TransD (Ji et al., 2015) extend the translation-based constraint to model more complex features. To further learn more expressive representation, ConvE (Dettmers et al., 2018) adopts multi-layer CNN architecture to capture the deeper correlation between  $e_1$  and  $r$ . Then, ConvKB (Nguyen et al., 2018) further extends ConvE to consider correlation between the entire triplet  $(e_1, r, e_2)$ . InteractE (Vashishth et al., 2020) introduces more types of interactions between entity and relation in ConvE. For more details, we refer interested readers to some surveys (Wang et al., 2017; Nguyen, 2020).

Although good performance can be observed in the above method, these methods process each triplet independently and ignore the latent information in the neighborhood of a given entity in the KG. To address this, Nathani et al. (2019) adopt

the graph attention network to aggregate the information from neighbors to obtain a meaningful entity representation. Similarly, SACN (Shang et al., 2019) adopts the weighted graph convolutional network to learn better entity representation. Further, HRAN (Li et al., 2021) divides the KG into sub-graph levels, where each sub-graph contains all the entities but only 1 relation, to capture the heterogeneous features. Although these methods prove the effectiveness of the introduction of encoders, they only assign a unique representation to each entity. In this paper, we aim at learning a relation-dependent entity representation of which semantics information will vary depending on the relation in a given triplet.

Another approach to KGE is to adopt the Transformer architecture (Vaswani et al., 2017), e.g., KGBERT (Yao et al., 2019) and StAR (Wang et al., 2021). These models adopt the deep Transformer architecture to learn a more meaningful representation and then advance the KGC, but they are usually urgent for huge computing resources.

The intuition of our work seems somewhat similar to TransR (Lin et al., 2015), but in fact quite different from it. The TransR (Lin et al., 2015) first assigns each entity a unique representation and then projects the entity representation into the relation space. But in our work, instead of learning an identical entity representation, we let the relation deeply take part in the whole GCN-based encoding stage to control the neighborhood aggregation, and consequently produce the relation-dependent entity representation.

## 6 Conclusion

In this paper, we proposed a novel knowledge graph embedding method, namely ReadE. In ReadE, we managed to introduce the relation-controlled gate mechanism to control the information flow in the aggregation step of the graph neural network, and thus obtained relation-dependent entity representations. Further, we proposed a contrastive learning method with both relation-level and entity-level negative samples for the particular purpose of enhancing the meaningful semantic information of entities' representations. Extensive experiments have shown that ReadE significantly outperformed existing baselines.



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## 771 A Training Details

772 According to the performance observed on the vali-  
773 dation set, We determine the batch size from {4, 32,  
774 128, 256, 1024}, the embedding size from {100,  
775 200, 300}, the learning rate from {1e-3, 5e-4, 5e-5,  
776 1e-5, 5e-6}, the dropout rate from {0.1, 0.3, 0.5},  
777 the temperature  $\tau$  from {0.1, 0.5, 1, 2, 10}, and  
778 the  $\lambda$  from {0.01, 0.05, 0.1, 0.2, 0.5}, with the best  
779 used for evaluation on the test set. All experiments  
780 are conducted on a single 11G NVIDIA 2080Ti  
781 GPU. Each experiment is repeated 10 times, and  
782 the average results are reported.

## 783 B KG Data Augmentations for Creating 784 Positive Pairs

785 In CL, a popular way to construct the positive pair  
786 on graph-structure data is to corrupt the graph struc-  
787 ture to change the adjacency information of each  
788 entity, therefore defining the different views of  
789 the same node as the positive pair. Inspired by  
790 GraphCL (You et al., 2020), we design two types  
791 of knowledge-graph-level data augmentations to  
792 realize the corruption.

**Entity Dropping.** Given the knowledge graph  $G_e$ ,  
793 edge dropping will randomly discard certain por-  
794 tion of entities (*i.e.*, nodes) and all the edges asso-  
795 ciated with them. Specifically, the probability of  
796 an entity to be chosen is defined as:  
797

$$798 p_c(e_i) \propto \frac{1}{d(i)^{\frac{3}{4}}}, \quad (16)$$

799 where  $d(i)$  is the degree of the entity  $e_i$ . The reason  
800 for using the reciprocal is that removing nodes  
801 with higher degree will impact more on the graph  
802 structure.

**Relation Dropping.** Relation dropping will first  
803 randomly choose a certain ratio of non-repetitive  
804 relations and remove all the edges that are included  
805 in these chosen relations. The definition of prob-  
806 ability that a relation  $r$  to be chosen is similar to  
807 (16) with replacing the degree with the number of  
808 the edges that associated with  $r$ .  
809

810 For each iteration, the random augmentations are  
811 operated twice and two different views of an entity  
812  $e_i$  will be generated. Also, we repeatedly random  
813 sample entities and relations without replacement  
814 to make sure that a certain ratio (named as  $\beta$ ) of  
815 entities and relations are dropped.