

# Mining and Ranking of Generalized Multi-Dimensional Frequent Subgraphs

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GEFÖRDERT VOM



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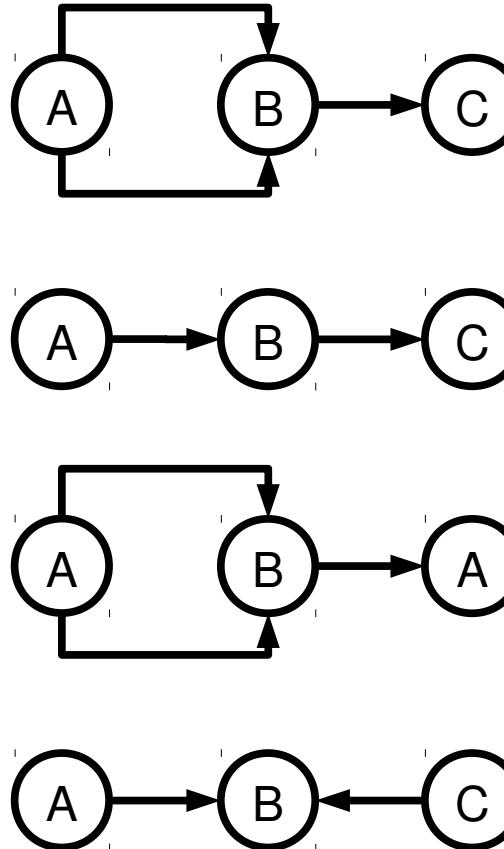
# Contents

- Problem definition and motivation
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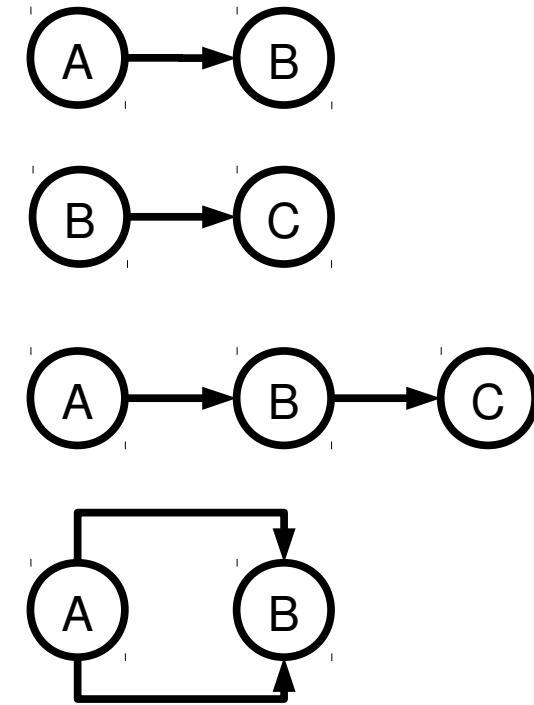
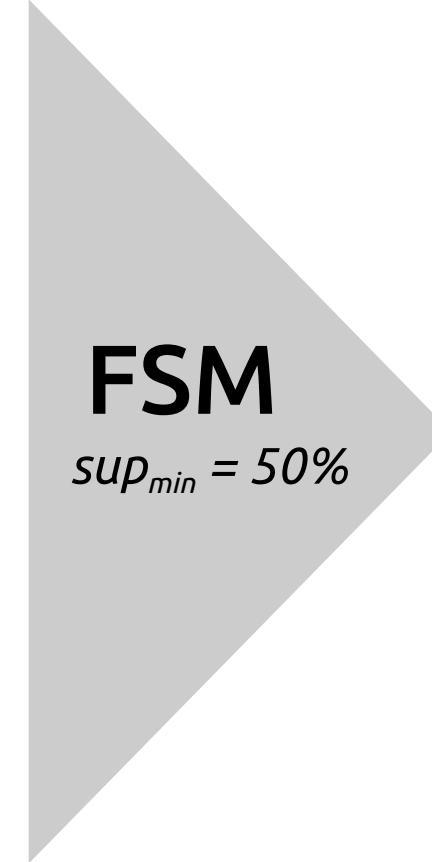
# Frequent Subgraph Mining (FSM)

- Input: Collection of graphs, threshold  $sup_{min}$
- A graph supports a pattern if there is at least one subgraph isomorphic to the pattern
- Output: Set of frequent graph patterns  
where for all  $sup(pattern) \geq sup_{min}$

# Frequent Subgraph Mining (FSM)



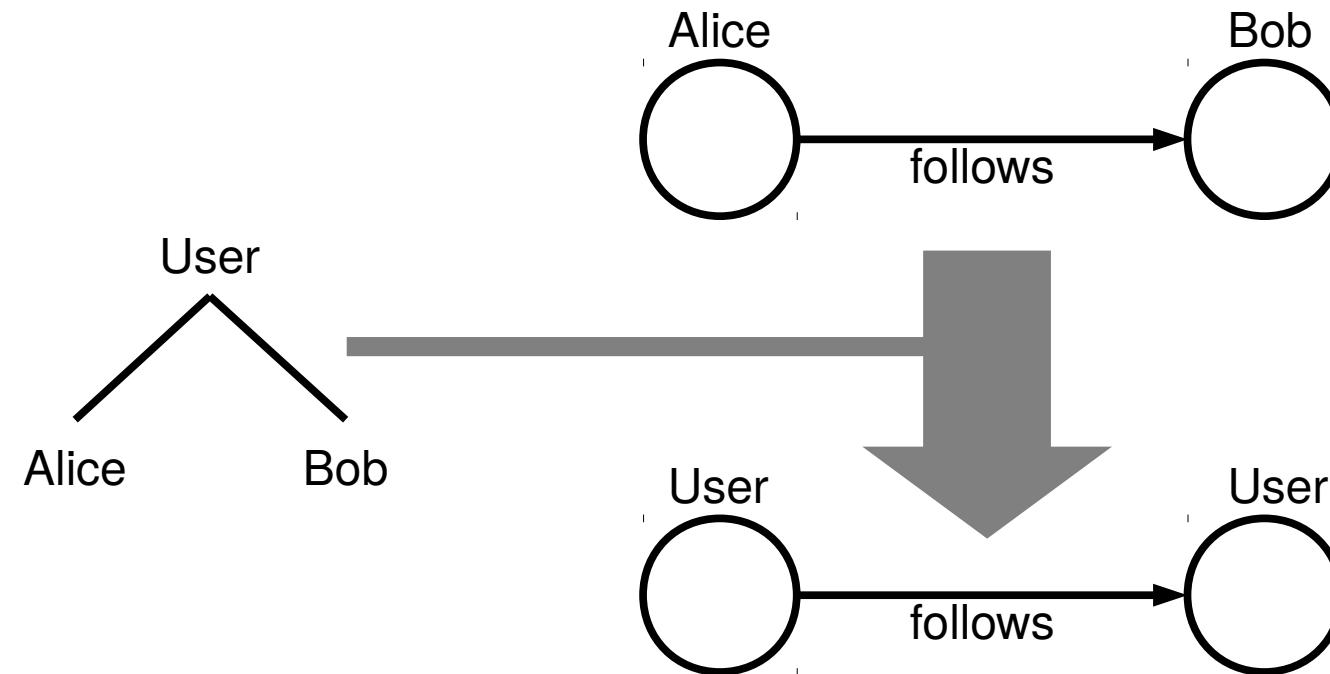
Input collection



Output collection

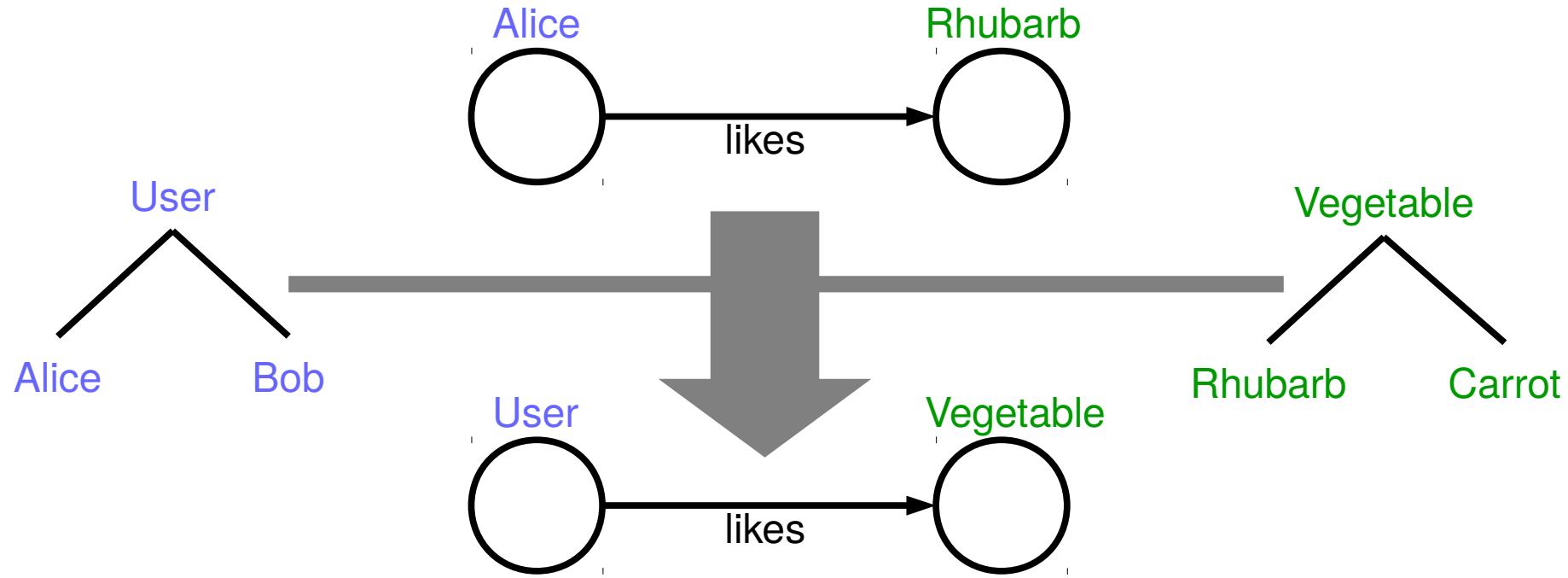
# Generalized FSM

- Vertices can be attached to a single taxonomy

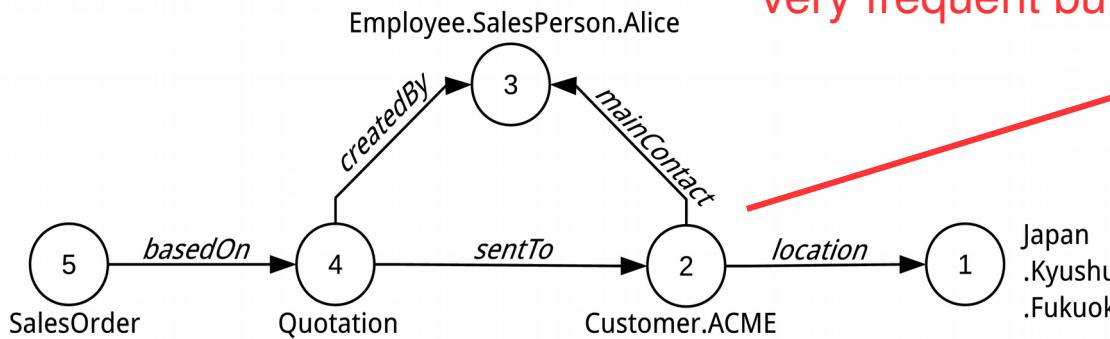


# Multi-Dimensional Generalized FSM

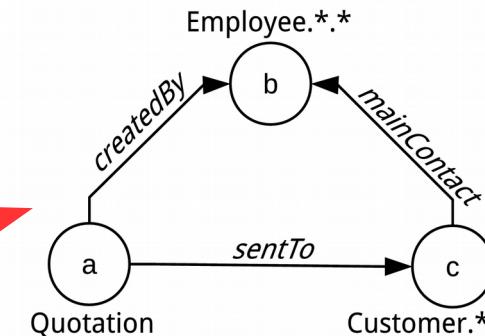
- Vertices can be attached to multiple taxonomies



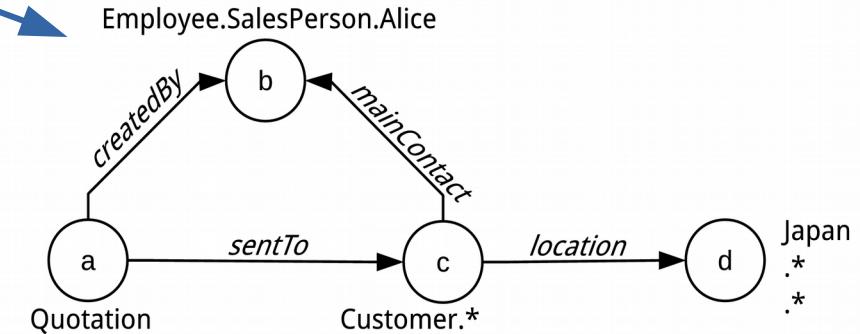
# Motivation



very frequent but trivial



less frequent but interesting

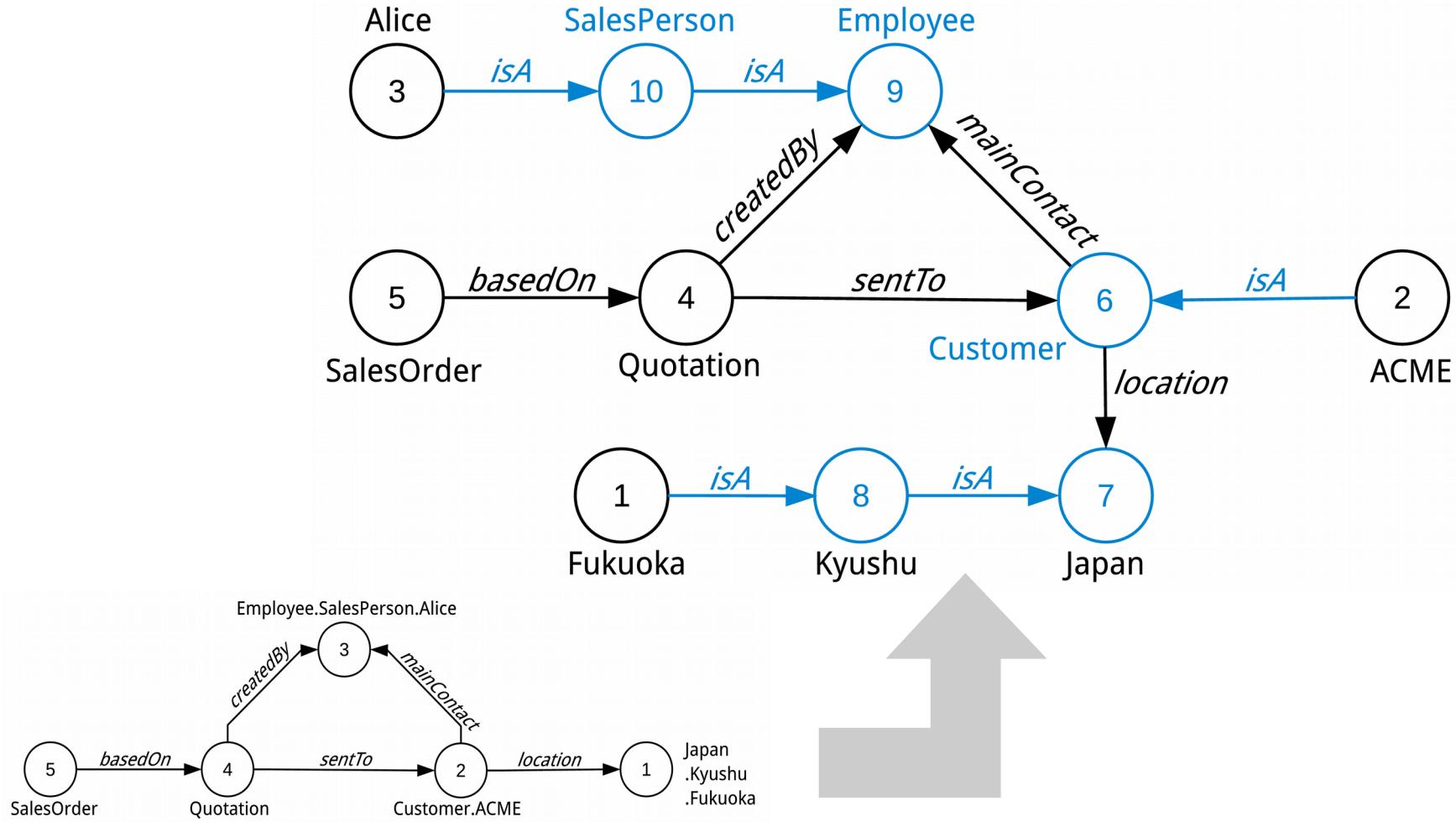


# Mining algorithms

- Based on gSpan for FSM [1]
- Two methods:
  - Path substitution
  - Decomposition into FSM and  
Generalized Frequent Vector Mining

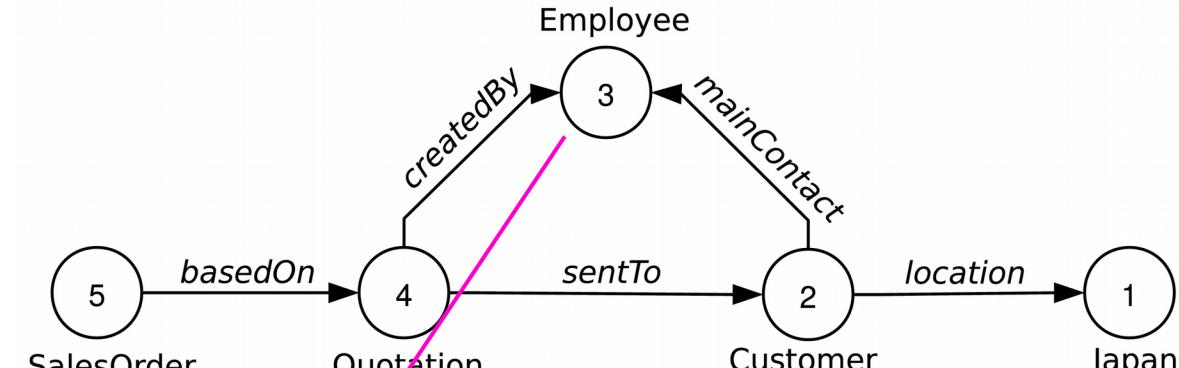
[1] X. Yan and J. Han. gspan: Graph-based substructure pattern mining. In Proc. IEEE Int. Conf. on Data Mining (ICDM), pages 721–724, 2002.

# Method 1: Path substitution



# Method 2: Decomposition

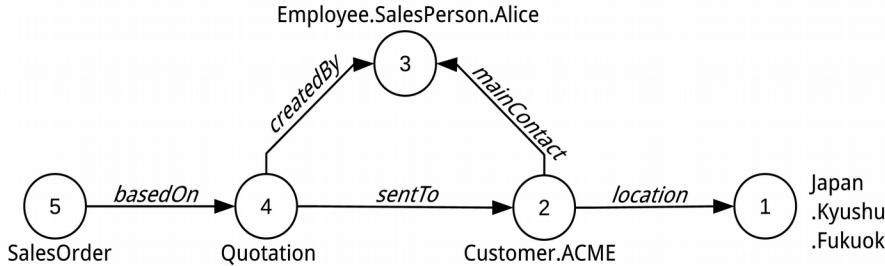
**Top-level pattern**



**Mapping**

**Lower-level vector**

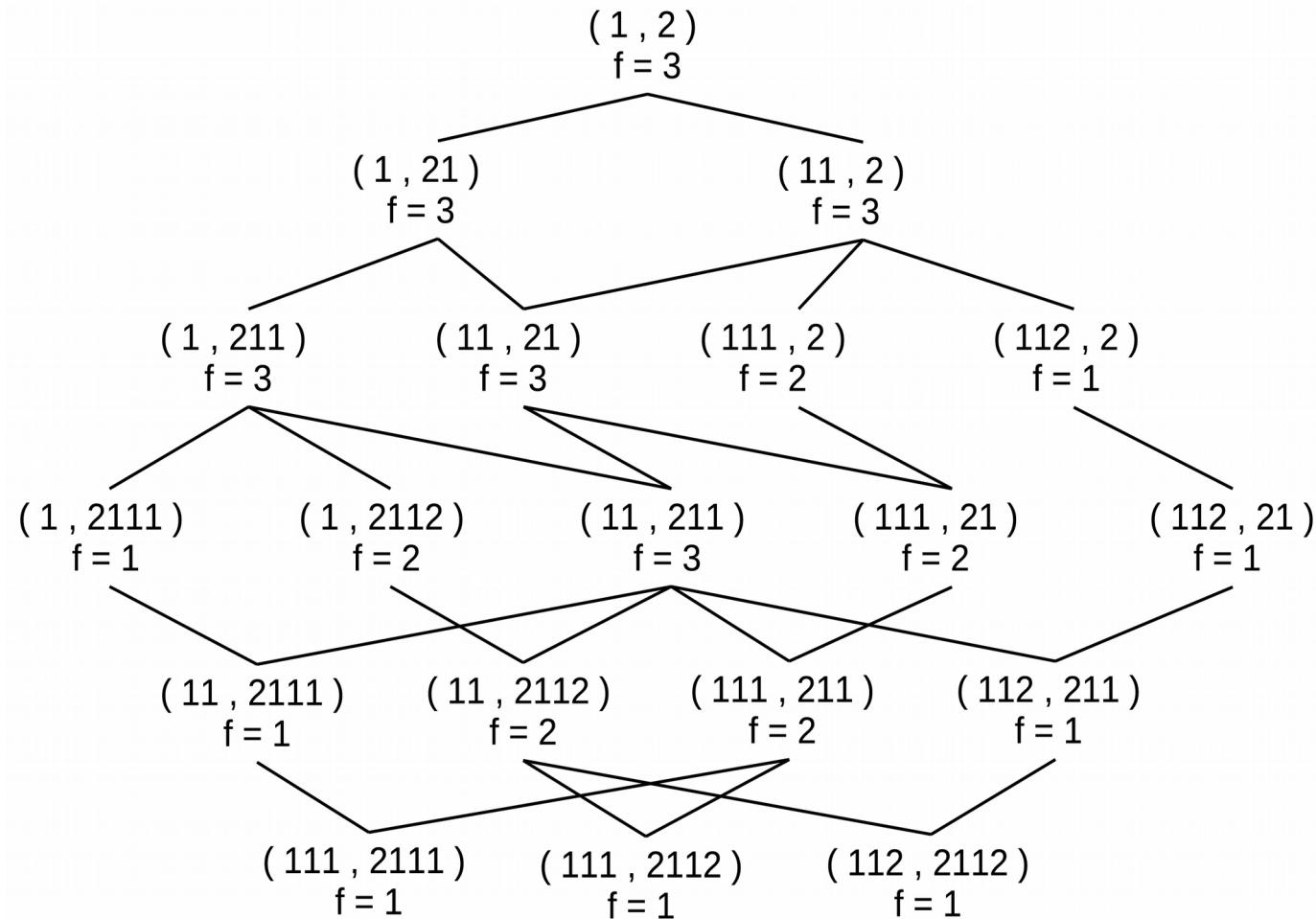
(SalesPerson.Alice, ACME, Kyushu.Fukuoka)



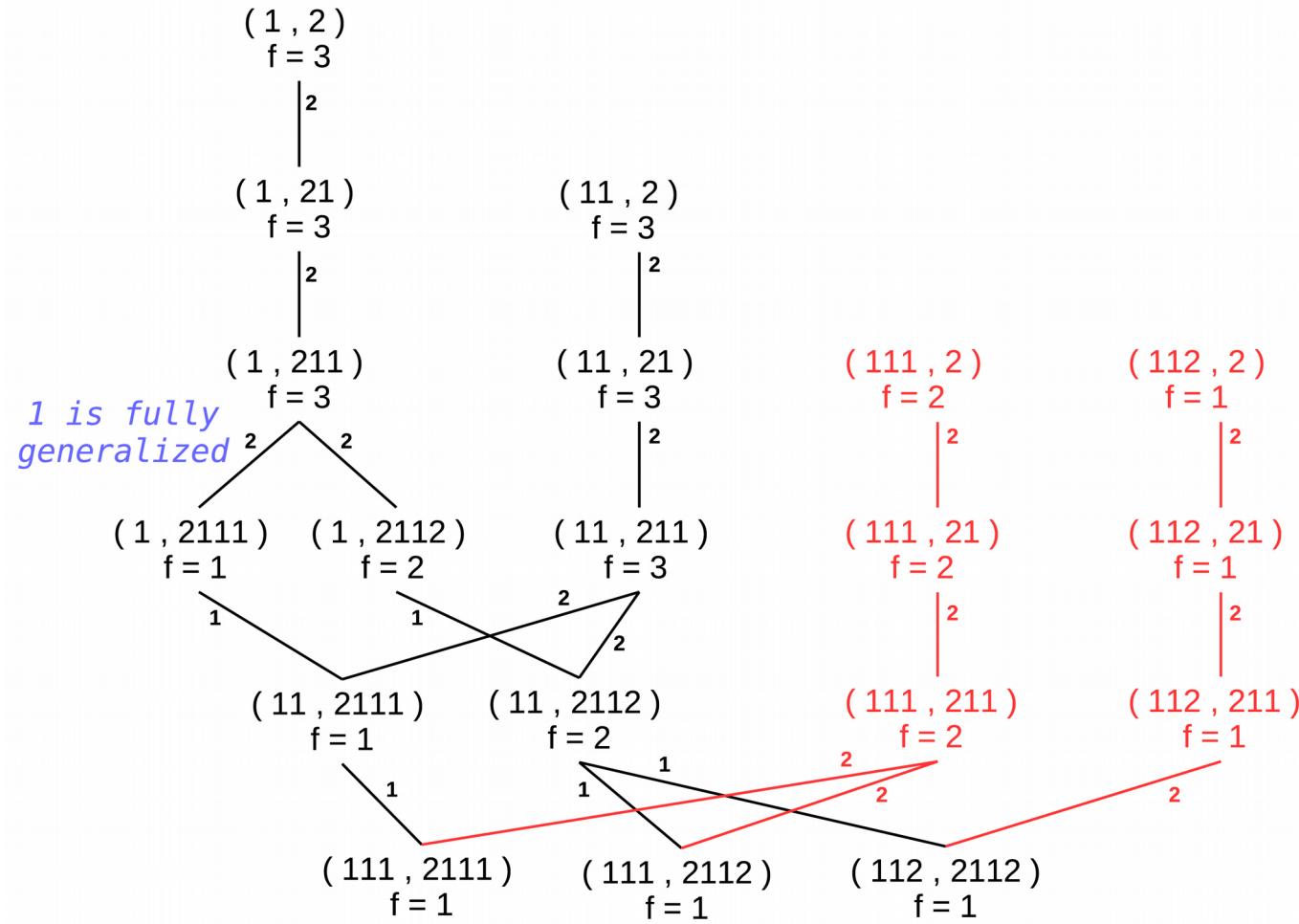
# Method comparison

- Substitution method:
  - Additional subgraph isomorphism resolutions for every inserted edge
- Decomposition method:
  - Isomorphism resolutions only on top-levels
  - Frequent specializations by vector mining

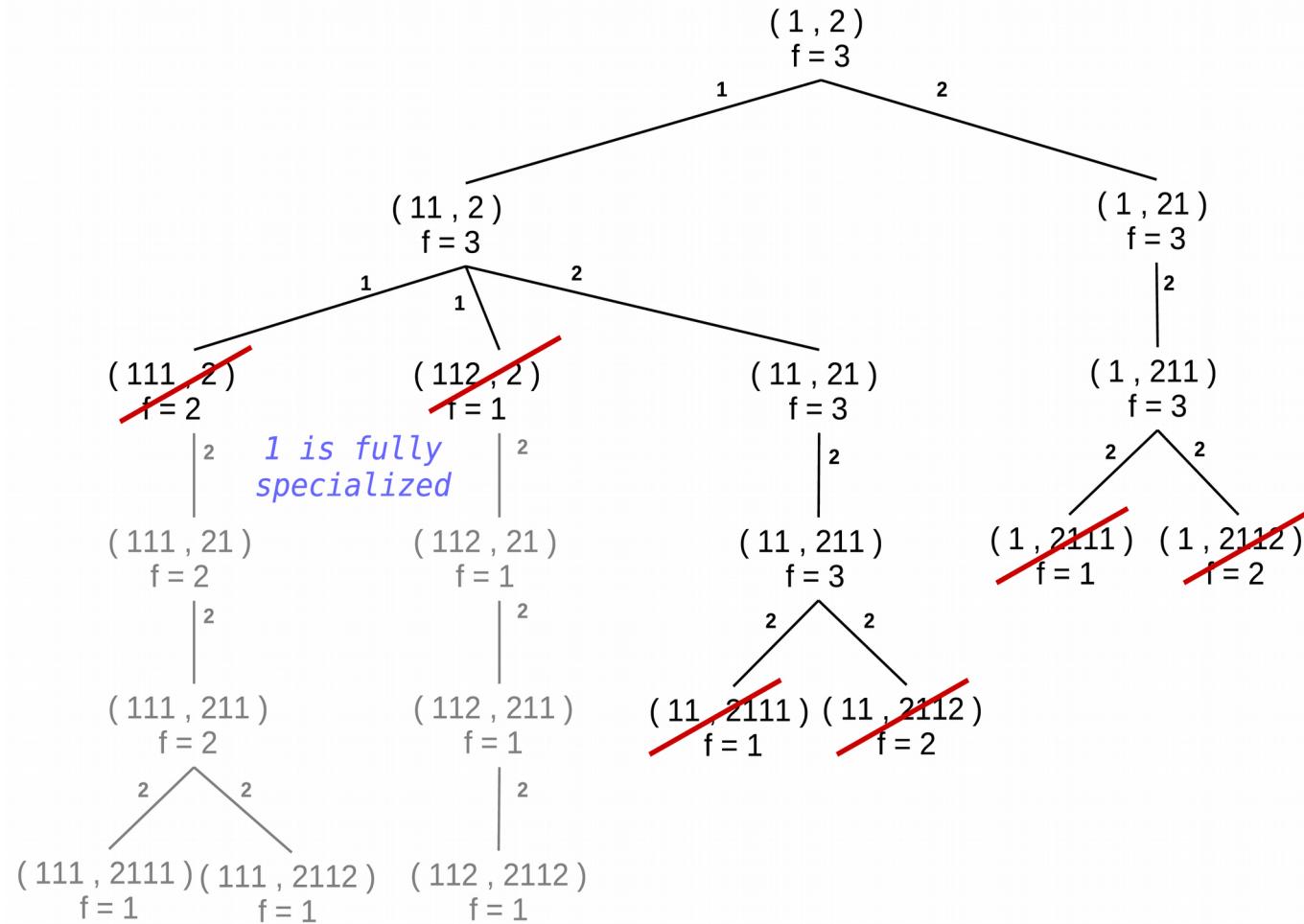
# Generalized Vector Mining (GVM)



# GVM: Bottom-up search



# GVM: Top-down search



# Result ranking

- Potentially huge number of results
- Interesting patterns should be presented first
- Significant patterns are more interesting
- Order results by p-value
- Fast analytical method [2]

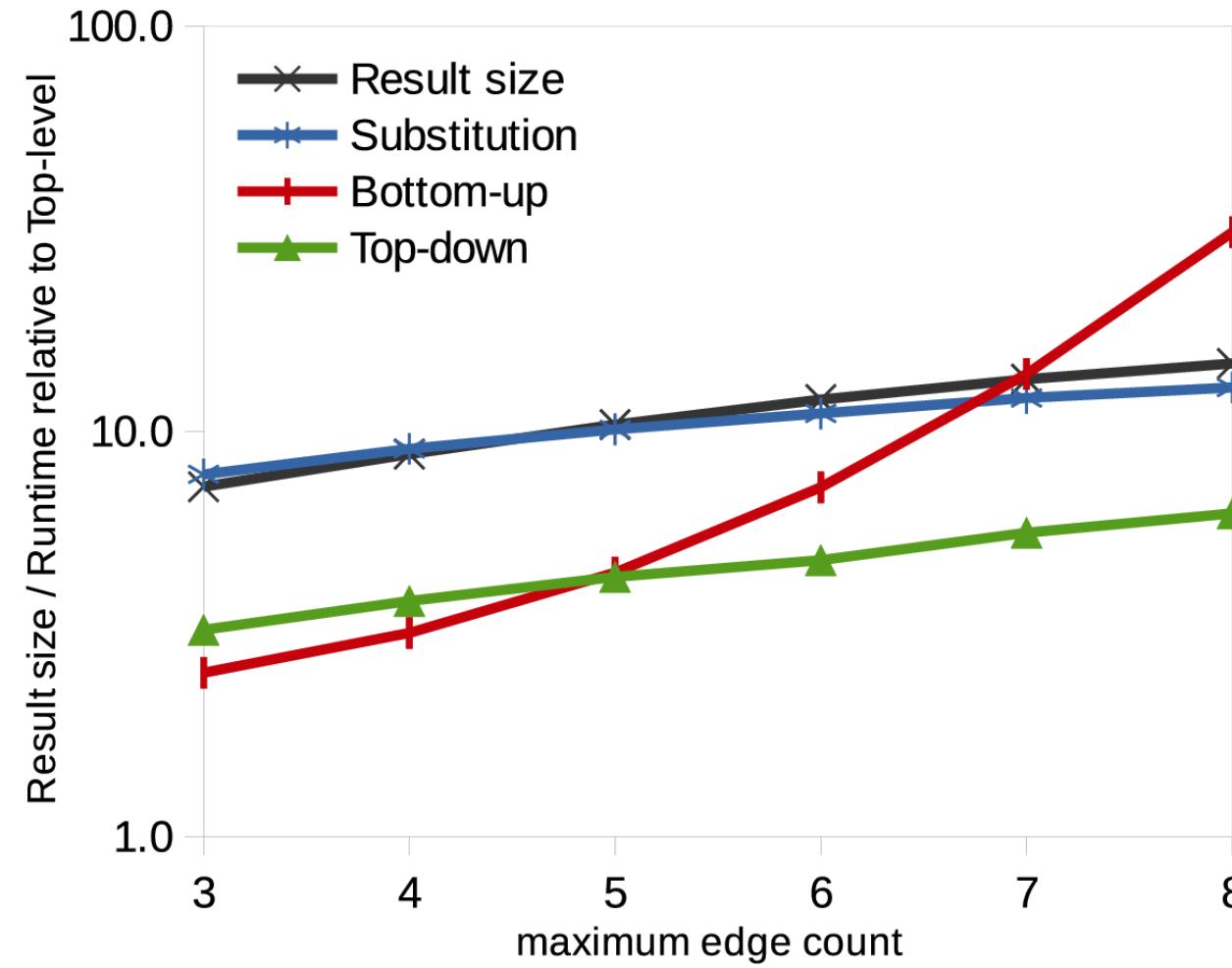
[2] G. Micale, R. Giugno, A. Ferro, M. Mongioví, D. Shasha, and A. Pul virenti.  
Fast analytical methods for finding significant colored graph motifs.  
To appear on Data Mining and Knowledge Discovery, 2017.

# Experimental evaluation

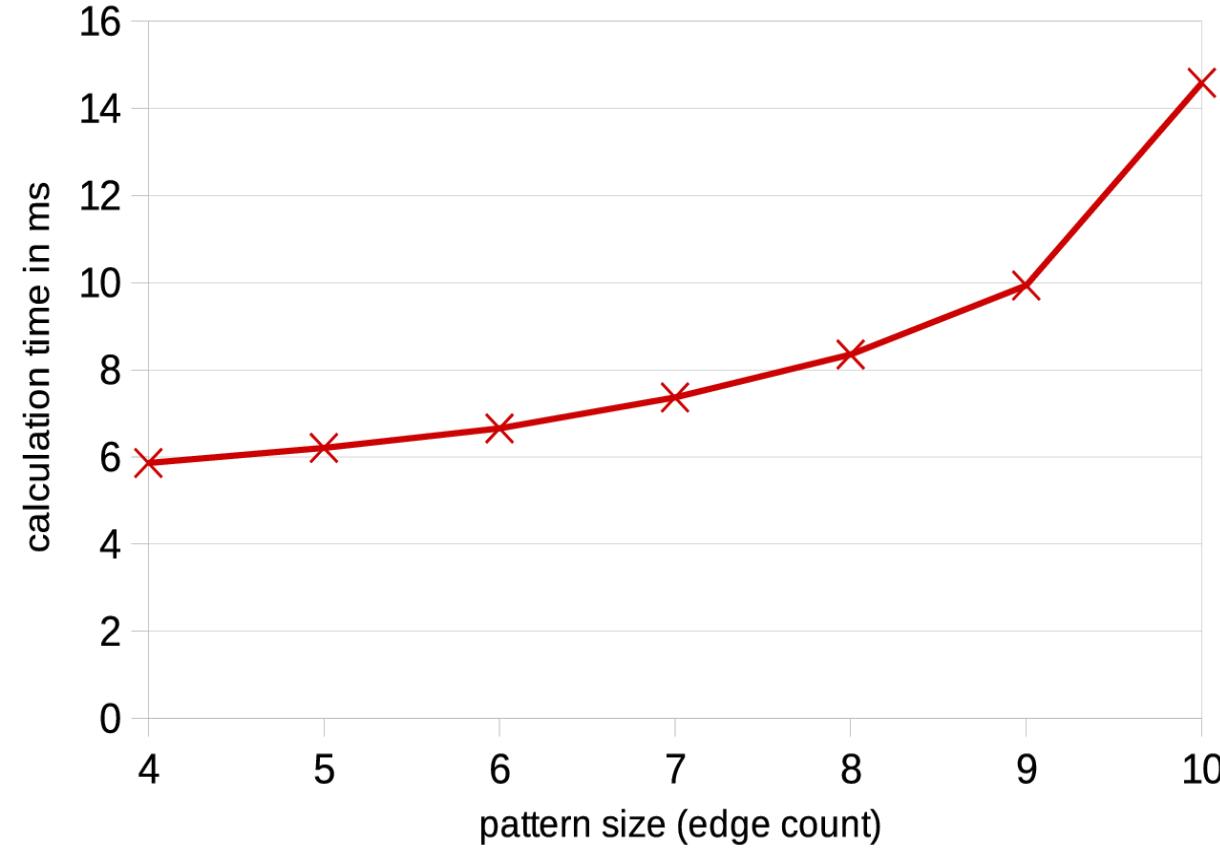
- Graphs represent Business Process Executions
- Fully isomorphic on top-level
- $\text{sup}_{\min} = 10\%$ ,  $k_{\max} = 8 \rightarrow 1\text{M}$  frequent patterns
- Generated FoodBroker [3] @ Gradoop [4]

- [3] [A. Petermann](#), M. Junghanns, R. Müller, E. Rahm:  
FoodBroker - Generating Synthetic Datasets for Graph-Based Business Analytics.  
Int. Workshop on Big Data Benchmarking (WBDB) 2014: 145-155; Springer
- [4] [A. Petermann](#), M. Junghanns, S. Kemper, K. Gómez, N. Teichmann, E. Rahm:  
Graph Mining for Complex Data Analytics.  
Demo @ Int. Conf. on Data Mining (ICDM) 2016; ICDMW 2016: 1316-1319; IEEE

# Experimental evaluation (mining)



# Experimental evaluation (ranking)



THX

Questions?