# Appendix A. NeurIPS 2021 Multimodal data integration competition participants

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#### NEURIPS 2021 - MULTIMODAL SINGLE CELL DATA INTEGRATION CHALLENGE

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Table 1: NeurIPS 2021 Multimodal data integration competition participant authors

## Appendix B. Supplementary Figures

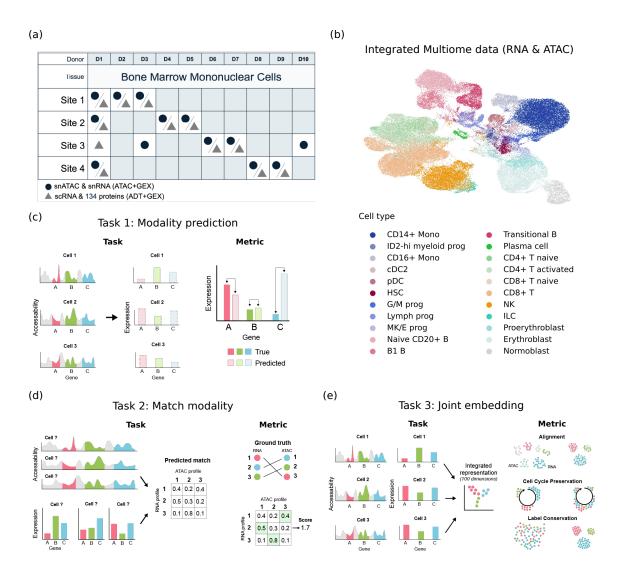


Figure 1: Competition set-up. (a) Experimental design to generate the multimodal single-cell benchmarking dataset with nested batch structure and (b) an example of an integrated representation of the Multiome data created using multiVI (Ashuach et al., 2021). (c-e) Conceptual figures of the three tasks and evaluation metrics used in the competition. Task 1 was the prediction of one modality from another based on paired training data and evaluated by RMSE. Task 2 was the matching of cells across modalities, evaluated by a match probability score. Task 3 was learning a joint embedding leveraging the variance of two modalities, evaluated by the removal of batch effects and conservation of biological signatures such as cell type and cell differentiation. See Luecken et al. (2021) for details.

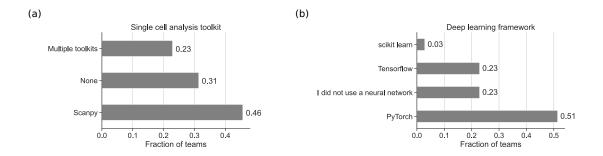


Figure 2: **Toolkit breakdown**. Software packages used by competitors for both single cell analysis (a) and deep learning (b) based on all survey responses.

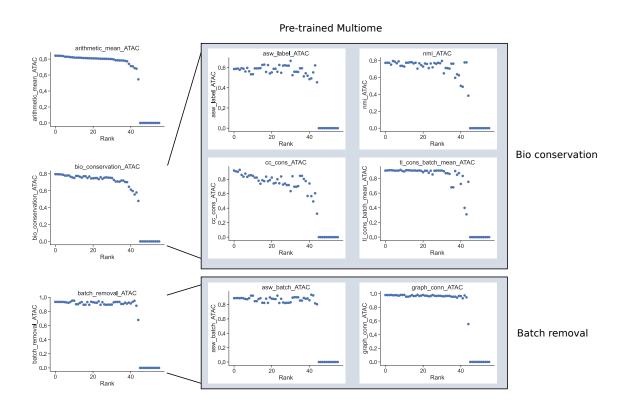


Figure 3: Task3: joint embedding evaluation metrics by rank on the pre-trained Multiome subtask. Top left shows the overall integration score, which is split up in batch removal and bio-conservation metrics. See Luecken et al. (2021) for detailed metric descriptions.

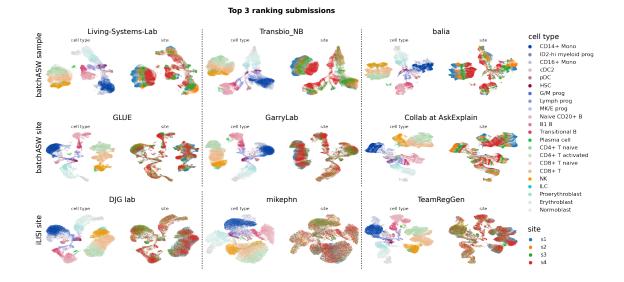


Figure 4: **Task 3: Extended joint embedding metric evaluation**. Additional best performing methods (left to right) ranked by batchASW sample, batchASW site and iLISI site.

# Appendix C. Additional method descriptions

The code for all methods described here can be found at https://github.com/openproblems-bio/neurips2021\_multimodal\_topmethods.

## C.1. Task 1: Modality prediction

GEX→ATAC - 1st place: Living Systems Lab Living Systems Lab used PCA to project the input and output modalities into 50 dimensions, and then trained a knearest neighbors regression model between these representations using 25 neighbors with the Minkowski distance metric (Fig 5). The full-dimensional output was reconstructed using the saved principal axes. The dataset was split into five folds stratified by the batches. The model was trained on each fold, and the outputs were then averaged. Hyperparameters were optimized in the local validation and public testing sets using the RMSE metric.

ATAC→GEX - 1st place: Cajal Cajal is a deep neural network method for the prediction of one modality from another. Cell-type specific features are selected as input, based on differential expression (Wilcox test) or differential accessibility (T-test after binarization of data), using an annotated reference dataset. The analysis of this reference dataset is performed using SCANPY (Wolf et al.). Feature selection is not performed when the input modality is ADT, due to the small number of proteins profiled in CITE-seq datasets. Total counts, median total counts per batch and the standard deviation in total counts per batch are also calculated and used as input features. Values for the selected features are centered and scaled before being input into the neural network. The network architecture consists of

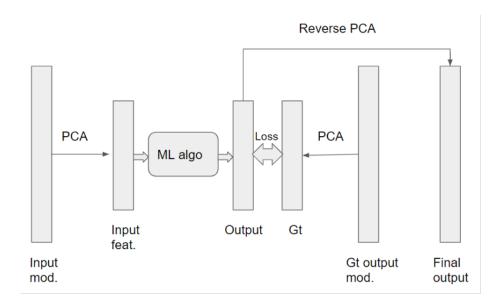


Figure 5: GEX 

ATAC: Living Systems Lab.

a dropout layer, 3 to 6 hidden layers which use the ReLU activation function, an output layer with no activation function (linear regression), and a final Lambda layer. This Lambda layer serves to clip the output to biologically reasonable values (the range present in the training data). The neural networks are implemented using TensorFlow (Abadi et al., 2016) and, during the training and validation phases, KerasTuner (O'Malley et al., 2019) was used to optimize hyperparameters (percentage dropout, number of hidden layers, number of nodes per layer).

Team Cajal initially sought to create a heteroencoder, however discovered that implementing a bottleneck architecture did not result in optimum performance across tasks. Thus, the hyperparameter search was restricted to 10-90% dropout, 3-6 hidden layers (after initial experimentation showing less than 3 resulted in reduced performance), and 10-800 nodes per layer (range chosen loosely based upon single-cell deep learning tasks reported in the literature). A number of approaches were attempted that did not improve performance, including pre-training as an autoencoder, L2 regularization, one-hot encoding of cell type as inferred by label transfer from the challenge reference dataset using ingest, and the use of additional datasets during training. To prevent overfitting, Team Cajal found that early stopping was necessary before the addition of a dropout layer. After this addition, early stopping was no longer essential, although no improvement in performance on the validation dataset was seen after 50 epochs. The final model parameters are detailed in Table 2.

GEX $\rightarrow$ ADT - 1st place: Guanlab - dengkw Team Guanlab - dengkw built a Kernel Ridge Regression (KRR) model with the Radial Basis Function (RBF) kernel  $k(x_i, x_j) = exp(-\frac{|x_i-x_j|^2}{2l^2})$ . Here, the d(.,.) is the Euclidean distance (Fig 6). Processed data was used as input to the model. Data processing was done by: (1) concatenating the data from modality 1 (Mod 1) in the training and test set with an outer join by the features and labeling them

Modality	Dropout	Layer Sizes
ATAC - GEX	0.8	320,360,620,440
GEX - ATAC	0.8	500, 20, 110, 430, 310
GEX - ADT	0.2	170, 300. 480, 330, 770
ADT - GEX	0.2	180, 140, 520

Table 2: Cajal modality prediction submission parameters

with "train" and "test"; (2) applying a truncated SVD to the combined matrix for dimension reduction; (3) applying a truncated SVD to the training data from modality 2 (Mod 2); (4) applying row-wise z-score normalization on the reduced matrix and splitting the matrix by the labels. Finally, the KRR model was fit with the normalized training matrix and the processed Mod 2 data. Outputs from predicting the test matrix were mapped back to the dimensions of test Mod 2 data by multiplying by the right singular matrix.

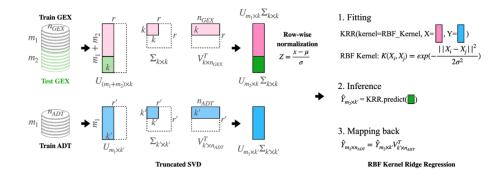


Figure 6: **GEX**→**ADT**: **Guanlab** - **dengkw**. Model overview.

In the final submission, in order to overcome memory limitations, Team Guanlab dengkw applied a training strategy consisting of random sampling and assembling (Fig 7). First, batches were randomly shuffled in the training data and two models were trained on the first and second half batches of the data. Then the steps were repeated 5 times and 10 models were generated with 10 outputs. The final predictions were the average of these outputs.

There are 4 tunable parameters in the model: the number of components for Mod 1 and Mod 2, the length scale l in the RBF kernel, and the regularization strength  $\alpha$  in ridge regression. These parameters were determined by cross-validation performances on the Phase I data. They are listed in Table 3. For the ADT2GEX task no feature reduction was applied to the ADT data.

ADT → GEX - 1st place: Novel Team Novel used an MLP with encoder-decoder structure, with most of the model capacity contained in the decoder given the high dimensional output. Although ATAC and GEX modalities were compressed via latent semantic indexing (LSI) for other input modalities, the ADT input data was not pre-processed due to its already low dimensionality. To avoid overfitting, the model was regularized using dropout

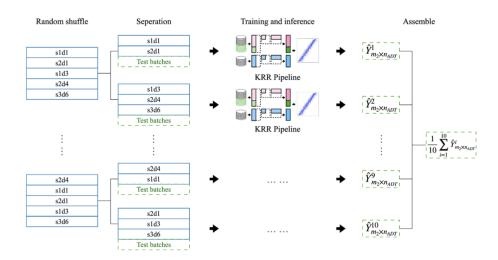


Figure 7: **GEX**→**ADT**: **Guanlab** - **dengkw**. Strategy to overcome memory limitations.

Task	# of Mod 1 components	# of Mod 2 components	l	$\alpha$
GEX2ADT	300	70	10	0.2
ADT2GEX	None	50	10	0.2
GEX2ATAC	1000	50	10	0.1
ATAC2GEX	100	50	10	0.1

Table 3: Guanlab - dengkw modality prediction submission parameters

before every hidden layer, as well as and weight decay. Alternative regularization techniques that were explored include batch swap noise and a variational prior on the latent variables, however these did not lead to beneficial results. Notably, in some cases a higher test metric score was achieved after training on a smaller data set rather than the full data set. For example, using the phase 1 data as a training dataset proved best to train the ADT2GEX model. The optuna framework was used to tune hyperparameters (LSI dimension, dropout rate before every hidden layer, depth, layer widths, activation function, learning rate, optimizer and weight decay). The optimal hyperparameter values are detailed in Table 4.

ADT→GEX - 2nd place: Living Systems Lab Living Systems lab used a similar pipeline for the ADT2GEX subtask as for the winning submission in the GEX2ATAC task (see above). They trained a neural network with 2 hidden layers, a ResNet-style neural network with skip connections and a batch prediction head with 3 hidden layers; and catboost models with Bernoulli bootstrapping and Bayesian bootstrapping on 5 folds. These models were ensembled by averaging the output features.

Overall: DANCE Team DANCE leverages a bipartite graph between cells and different modalities (GEX, ADT, and ATAC) to represent interactions. They utilize graph neural networks adapted from Battaglia et al. (2018); Kipf and Welling (2016) and Wu et al. (2020) to exploit the structural information of this bipartite graph. Specifically, the solution

	GEX2ATAC	ATAC2GEX	ADT2GEX	GEX2ADT
# HL	3	3	3	3
HL dims	[1024, 256, 2048]	[2048, 2048, 512]	[512, 512, 512]	[512, 512, 2048]
HL dropout rates	[0.30, 0.11, 0.14]	[0.26, 0.18, 0.25]	[0.0, 0.0, 0.0]	[0.20, 0.15, 0.17]
Activation functions	$\operatorname{GeLU}$	$\operatorname{GeLU}$	$\operatorname{GeLU}$	$\operatorname{GeLU}$
Learning rate	1e-05	8e-05	4e-04	3e-05
Optimizer	AdamW	AdamW	Adam	AdamW
Batch size	64	256	64	32
Weight decay	4e-04	7e-04	1e-05	1e-02
# LSI components	256	256	-	256

Table 4: Novel modality prediction submission parameters; HL - hidden layers; dims - dimensions

consists of three major components: (1) bipartite graph construction, (2) heterogeneous graph convolution, and (3) representation concatenation. In the first step, a bipartite graph is constructed between modality (GEX, ADT and ATAC) and cell nodes. In the GEX2ADT and GEX2ATAC tasks, they additionally introduced pathway data from hallmark gene sets (i.e. sets of related genes). Based on the original bipartite graph, gene features which are shown to be related in the pathway dataset were linked.

The initial node embedding of feature nodes is a one-hot index of each feature, thus, the node embedding matrix for all feature nodes  $\hat{X}_{feat} = R^{k \times k}$ , is an identity matrix (a.k.a  $\hat{X}_{feat} = I_k$ ), where k is the number of modality 1 (Mod1) features. To model the batch effect, initial cell embeddings were computed from batch features, the statistical features of all the cells in one batch. Eventually, for each cell a 9-dimensional batch feature was obtained, so that the batch features for all cell nodes could be described as  $\hat{X}_{batch} \in R^{N \times 9}$ .

This graphs was used as the basis for heterogeneous graph convolution. In the heterogeneous graph convolution, parameters for different types of edges were separated. In each convolution layer three sets of aggregation approaches were simultaneously completed to aggregate the information from different types of neighbors to the target node. The node embeddings were then updated with residual connection and a weighted sum of aggregation results:

$$X_{feat}^{l} = X_{feat}^{l-1} + \alpha * AGG_{c2f} + (1 - \alpha) * AGG_{f2f}$$
 (1)

$$X_{cell}^{l} = X_{cell}^{l-1} + AGG_{f2c}$$

$$\tag{2}$$

where l is the number of current layer,  $AGG_{f2f}$  is the pathway aggregation (i.e., the aggregation from feature to feature),  $AGG_{c2f}$  is the cell-feature aggregation,  $\alpha$  is a scalar hyper-parameter to control the ratio between those two aggregations, and  $AGG_{f2c}$  is the aggregation from features to cells. Finally, Team DANCE took the embeddings of cell nodes from each convolution layer, concatenated them and projected them to the space of downstream task via a linear transformation.

## C.2. Task 2: Match modality

All subtasks - 2nd place: Novel Team Novel approached the match modality task using a metric learning approach and post-processing adapted from graph theory. For each data type, a shallow MLP encoder was used to learn spherical sample embeddings. ATAC and GEX input data was preprocessed by latent semantic indexing (LSI) transformation (a TF-IDF transformation followed by SVD). In contrast to their approach in the Predict Modality task, the first LSI component was discarded as it was broadly associated with technical variation. ADT input data was directly fed into the network due to its lower dimensionality. The encoders were trained by minimizing the symmetric cross-entropy of cosine similarities between sample pairs. This approach was inspired by CLIP, a model designed to connect text and image data (Radford et al., 2021). Matching probabilities were inferred in a two step procedure: (1) evaluation of a dense pairwise cosine similarity matrix based on the embeddings of each modality; and (2) finding a maximum weight matching in a bipartite graph, where each vertex represents a sample in the data. To ensure computational feasibility, the input matrix was sparsified by discarding elements smaller than their corresponding row- and column-wise 0.995 quantiles. This way, the matrix was greatly sparsified while retaining values in all rows and columns. The proposed algorithm for sample matching is making hard bets rather than soft probability assignments. It is intrinsically symmetric so its output and metrics are consistent for both directions of the matching problem (i.e. ADT2GEX and GEX2ADT). For the ATAC2GEX and ADT2GEX subtasks the model was trained on Phase 2 and Phase 1 data, respectively, for 7000 epochs. Due to the high cost of the bipartite matching procedure, the competition metric was evaluated on each epoch using probabilities obtained by a row- and column-wise softmax averaged for the modality pair. The hyperparameters for the embedding model were found by an extensive search using the optuna framework and are shown in Table 5.

#### C.3. Task 3: Joint embedding

Multiome, pre-trained and CITE, pre-trained: Amateur Team Amateur's method "joint embedding with a regularized autoencoder" (JAE) was inspired from previous work on scDEC (Liu et al., 2021), which aims at simultaneous deep generative modeling and clustering of single-cell data. Here, the scDEC model was simplified by removing the discriminator networks and adding constraints to the encoder latent space so that JAE requires latent features to recover more biological knowledge, including cell type, batch, and cell-cycle phase.

In the JAE model, each modality (except ADT) is first SVD transformed (e.g. to 100 components) and concatenated. The information from cell annotations (e.g., cell label, cell cycle score, and cell batch) is incorporated to constrain the structure of latent features. In this manner some latent features should recover the cell type information and some should recover the cell cycle score. Batch-related features should recover batch labels as randomly as possible to potentially eliminate this effect. Some features in the latent space were left without constraint to ensure the flexibility of network. JAE was pre-trained using the provided annotated datasets in an end-to-end fashion (Adam optimizer,  $lr = 10^{-4}$ ), where multiple loss functions were used, including autoencoder reconstruction loss, cell type prediction cross entropy loss, cell cycle phase score mean squared error (MSE) loss, and batch

	$\mathbf{ADT} \leftrightarrow \mathbf{GEX}$	$\mathbf{ATAC} \leftrightarrow \mathbf{GEX}$
Learning rate	8e-05	6e-04
Optimizer	AdamW	$\operatorname{AdamW}$
Weight decay	0	0
Batch size	2048	16384
Embedding dimension	64	256
# HL in GEX encoder	2	2
# HL in Mod 2 encoder	2	1
HL dims (GEX)	[1024,512]	[1024, 1024]
HL dims (Mod 2)	[512, 2048]	[2048]
HL dropout rates(GEX)	[0.01, 0.25]	[0.54, 0.4]
HL dropout rates(Mod 2)	[0.02, 0.3]	[0.66]
Initial temperature (symmet-	3.46	3.06
rical cross-entropy [log])		
Number of LSI components	128 for GEX	512 for ATAC, 64 for GEX

Table 5: Novel match modality submission parameters; HL - hidden layers; dims - dimensions

loss. These losses were balanced, resulting in a total loss of  $0.7\,\mathrm{AE} + 0.2\,\mathrm{CT} + 0.05\,\mathrm{CC} + 0.05\,\mathrm{Batch}$ . In the online testing stage where cell annotations were not available, the model was fine-tuned only based on the autoencoder reconstruction loss. This was done for 1 epoch with learning rate of  $10^{-4}$  and 2 epochs with a learning rate of  $2*10^{-5}$  for the Multiome and CITE-seq data, respectively. Finally, all the features in the JAE latent space were used as the joint embedding.

Multiome, online: Living Systems Lab The Living Systems Lab team solved this task using a concatenated autoencoder (cAE) architecture. The cAE consists of two encoders, each with a single hidden layer that is concatenated and then projected down to an embedding layer, a concatenated inverse layer, and two decoder layers. Before training the cAE, the data were pre-processed by (1) identifying highly variable genes and (2) setting a threshold to filter peaks that are rarely identified (3% or less of cells). Furthermore, a weight orthogonality constraint was applied to both encoding layers, enhancing the embedding's discriminability and representability.

Each encoder, which receives data from a different modality, has 64 dimensions, leading to 128 dimensions after concatenation. The embedded layer, which contains the two domain's integrated low-dimensional representation, again consists of 64 dimensions. ReLU was used as an activation function for all layers with a dropout value of 0.1 applied to two encoding layers, except in the bottleneck layer, where a linear activation function was used. Training was performed with the ADAM optimizer for 600 epochs at a learning rate of lr = 0.0001 and a batch size of 32. An MSE loss function was used.

CITE, online: Guanlab - dengkw Team Guanlab - dengkw solved the CITE online subtask using the same linear approach as in task 1. Truncated SVD was applied to the

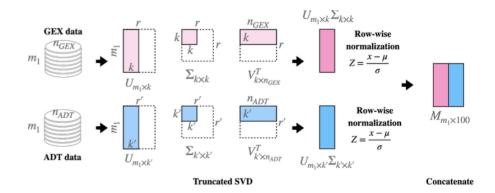


Figure 8: Joint embedding (CITE, online): Guanlab - dengkw.

modality 1 and the modality 2 data, respectively, and normalized on the rows for each matrix. The output is a simple concatenation of the reduced features. The numbers of components for each modality were determined by submission performance in experiments using the Phase 1 data. In the task of embedding the CITE data, the dimensions for GEX and ADT are 73 and 27, respectively. More details and a schematic diagram can be found in Figure 8.

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