# Dynamic Resource Allocation for Spot Markets in Cloud Computing Environments

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Introduction Motivation Our Contribution Related Work

#### Introduction

- Cloud computing aims at providing compute resources like public utilities
  - Resources can be rapidly acquired and released on-demand

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  - High demand may cause request rejection, resulting in low customer satisfaction

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  - Low demand causes low resource utilization
  - High demand may cause request rejection, resulting in low customer satisfaction
- Market-based resource allocation is gaining popularity
  - Let the price fluctuates with supply and demand

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#### Amazon EC2 Spot Instance Service

- Launched on Dec. 15, 2009
- Multiple VM types per availability zone
- Customers submit requests the specify number of VMs and bidding prices
- Spot price fluctuates with supply and demand according to Amazon
- Instances may be terminated without prior notice



Figure 1: Price of a small Linux instance in a week

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Introduction Motivation Our Contribution Related Work

### Introduction (Con't)

- Energy is another major concern of Cloud providers
  - Accounts for 20% of total annual expense

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- The best way to save energy is to set unused servers to a power-saving state (e.g. turn them off)

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- Energy is another major concern of Cloud providers
  - Accounts for 20% of total annual expense
- The best way to save energy is to set unused servers to a power-saving state (e.g. turn them off)
- However, frequently switching a server in and out of power-saving state will cause wear-and-tear effect and reduce its life time
  - It is necessary to model this penalty in the cost function

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- Multiple spot markets sharing the same data center capacity
  - As request arrival can be highly dynamic, sometimes certain markets may be hotter than others

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  - As request arrival can be highly dynamic, sometimes certain markets may be hotter than others
- The dynamic capacity provisioning problem
  - When demand is high, decide how many resources should be allocated to each market
  - When demand is low, decide how many servers should be set to the sleep state

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- The dynamic capacity provisioning problem
  - When demand is high, decide how many resources should be allocated to each market
  - When demand is low, decide how many servers should be set to the sleep state
- There are penalties for adjusting both price and capacity
  - Rapid change of prices can cause frequent preemption of customer's tasks
  - Rapid change of capacity can hurt server lifetime

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## Our Contribution

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- We study the online dynamic capacity provisioning problem
- We formulate dynamic capacity provisioning as an optimization problem that considers
  - Demand fluctuation
  - Energy cost
  - Penalty for capacity adjustment

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# Our Contribution

- We study the online dynamic capacity provisioning problem
- We formulate dynamic capacity provisioning as an optimization problem that considers
  - Demand fluctuation
  - Energy cost
  - Penalty for capacity adjustment
- We present a Model Predictive Control (MPC) framework for the dynamic capacity provisioning problem for Amazon EC2 spot markets
  - Amazon EC2 is the only cloud provider currently offer spot instance services

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- Market-based Resource Allocation
  - Most of the existing work assumes fixed capacity
  - Does not consider electricity cost

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- Automatic Capacity Provisioning
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- Automatic Capacity Provisioning
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- Resource Allocation in Electricity Spot Market
  - Similar problem but with single type of goods
  - Control theory is widely used in this context

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System Architecture System Model Designing the MPC controller

#### System Architecture



#### Figure 2: System Model

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#### **Demand Model**

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- Let  $p_k^i$  denote the price for VM type *i* at time *k*
- Demand is a monotonic decreasing function  $I(\cdot)$  of price

$$d_k^i = l^i(k, p_k^i) + v_k^i \tag{1}$$

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- To simplify the model, we approximate  $l(\cdot)$  locally using a linear function
  - This is reasonable since the model penalizes rapid price change

$$d_k^i = \bar{d}_k^i - \alpha^i (p_k^i - \bar{p}_k^i) + v_k^i$$
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• We assume the model parameters can be obtained using linear regression or other methods

System Architecture System Model Designing the MPC controller

#### System Model

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  - Can be extend to multiple generations of identical machines

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- Denote by  $e^i$  the energy cost of a machine dedicated to type i
- State equation for capacity is

$$x_{k+1}^{i} = x_{k}^{i} + u_{k}^{i}$$
 (3)

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# System Model (Con't)

• Denote by  $p_k^i$  the price of VM type *i* at time *k* 

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- The spot instance service can be modeled as a M/G/c queue with average arrival rate  $\lambda_k^i = d_k^i/T$  and processing rate  $\mu^i$
- The net income can be expressed as

$$\mathbb{E}(R_k^i) = \min\left(1, \frac{\mathbb{E}(\lambda_t^i)}{\mu^i C x_k^i}\right) p_k^i T - C e^i x_k^i$$
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(5)

• The net income is maximized when supply  $\mu^i C x_k^i$  matches demand  $\mathbb{E}(\lambda_t^i)$ 

System Architecture System Model Designing the MPC controller

# System Model (Con't)

• Even though it is desirable to match supply and demand, 100% utilization can cause unacceptable queuing delay

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- Even though it is desirable to match supply and demand, 100% utilization can cause unacceptable queuing delay
- $\bullet$  Assume there is a desirable average queuing delay, we translate it into a desirable utilization level  $\rho^i$

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- Even though it is desirable to match supply and demand, 100% utilization can cause unacceptable queuing delay
- $\bullet$  Assume there is a desirable average queuing delay, we translate it into a desirable utilization level  $\rho^i$
- The objective is to minimize

$$\mathbb{E}(R) = \mathbb{E}\left[\sum_{i=1}^{N}\sum_{k=1}^{K} -R_{k}^{i} + q^{i}(Cx_{k}^{i} - \sigma^{i}d_{k}^{i})^{2} + r_{1}^{i}(u_{k}^{i})^{2} + r_{2}^{i}(p_{k}^{i})^{2}\right]$$

where  $\sigma^i$  is a constant weight factor,  $q^i$ ,  $r_1$  and  $r_2$  are penalty factors for modeling the cost for meeting desired utilization level, changing capacity and price, respectively

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#### Designing the MPC controller

• The optimization problem is a linear quadratic program that can be solved optimally in polynomial time

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System Architecture System Model Designing the MPC controller

# Designing the MPC controller

- The optimization problem is a linear quadratic program that can be solved optimally in polynomial time
- However, resource controller needs to solve the problem online
- We devise a MPC algorithm for the problem
  - (1) At time k, predict future demand for a window  $\mathcal{K}$
  - 2 Solve the problem optimally to determine  $u_k$  and  $\pi_k$
  - Solution Apply change  $(u_k \text{ and } \pi_k)$  at the end of time slot k
  - Repeat Step 1-3

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Experiments Setup Workload Characteristics Experiment Results

#### **Experiments Setup**

• We have implemented the scheduler and controller in Matlab

#### Table 1: Types of VMs used in the experiments

| VM Type | CPU Capacity | Memory Size | average duration | Avg. bidding |
|---------|--------------|-------------|------------------|--------------|
|         | (Cores)      | (MB)        | (seconds)        | price (\$)   |
| small   | 1            | 64          | 1694             | 0.038        |
| medium  | 1            | 128         | 4862             | 0.039        |
| large   | 1            | 256         | 14049            | 0.041        |

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- We have implemented the scheduler and controller in Matlab
- For cloud workload, we use the publically available trace from Google compute clusters
- However, needs to pre-process the dataset
  - Match VM size with the ones used in SpotCloud
  - Generate prices from random gaussian distributions

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Experiments Setup Workload Characteristics Experiment Results

#### Task Arrival Rate in Google's Workload Traces



Figure 3: Task Arrival Rate in Google Workload Traces

Experiments Setup Workload Characteristics Experiment Results

#### Resource Usage and Allocation



Figure 4: Num. of small VMs in the cluster





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Figure 6: Num. of large VMs in the cluster

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#### Price and Utilization



Figure 7: Price for each VM service



# Figure 8: Utilization of allocated servers per hour



• Market-based resource allocation is a promising approach for resource allocation in Clouds

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### Conclusion

- Market-based resource allocation is a promising approach for resource allocation in Clouds
- We have presented a framework that dynamically adjust supply and price for different spot markets that considers
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  - Energy cost
  - Penalty for capacity adjustment

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Conclusion

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- We have presented a framework that dynamically adjust supply and price for different spot markets that considers
  - Demand fluctuation
  - Energy cost
  - Penalty for capacity adjustment
- Future work
  - Analyze the problem from customers point of view
  - Design incentive compatible auction mechanism that achieves optimal revenue

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