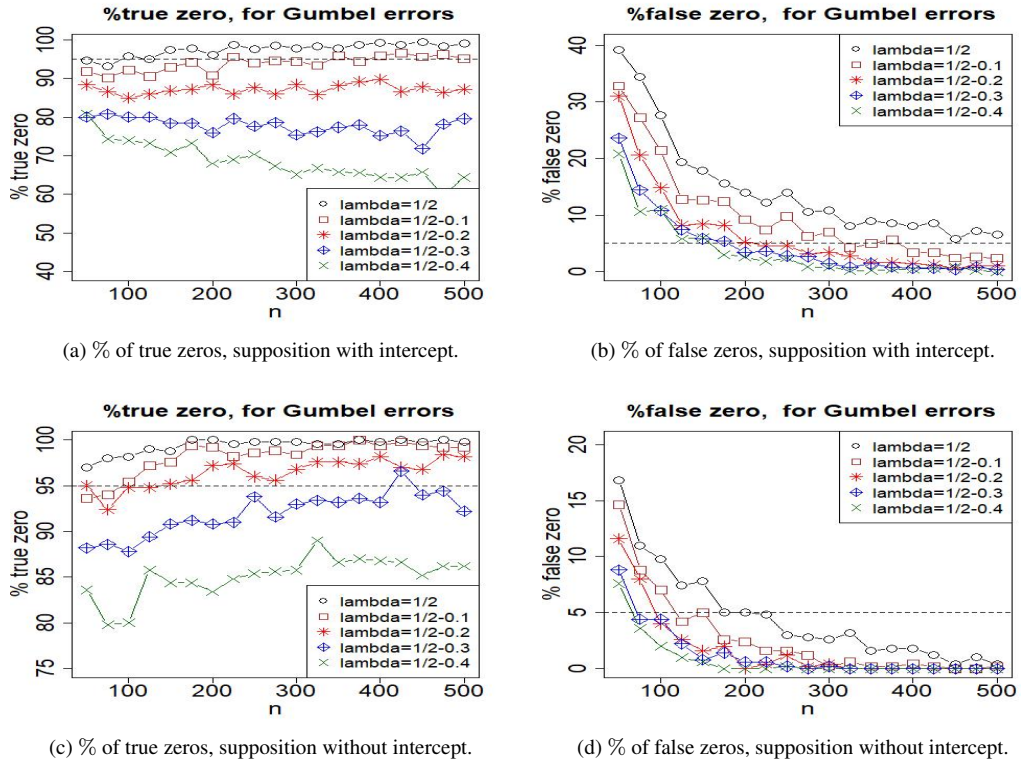


$n$	$\lambda_n = n^{1/2}$				$\lambda_n = n^{1/2-0.1}$				$\lambda_n = n^{1/2-0.2}$			
	$L2$	$SD$	% true 0	% false 0	$L2$	$SD$	% true 0	% false 0	$L2$	$SD$	% true 0	% false 0
150	0.56	0.16	99	7.6	0.48	0.15	98	4.5	0.43	0.13	97	2.2
200	0.47	0.13	99	4.9	0.40	0.12	99	2.2	0.37	0.11	98	1.2
400	0.34	0.08	100	1	0.28	0.08	99	0.04	0.25	0.08	99	0.04
1500	0.23	0.08	100	0	0.21	0.08	100	0	0.20	0.07	99	0
2000	0.24	0.10	100	0	0.22	0.10	100	0	0.21	0.10	99	0
4000	0.31	0.13	100	0	0.29	0.13	100	0	0.29	0.13	100	0

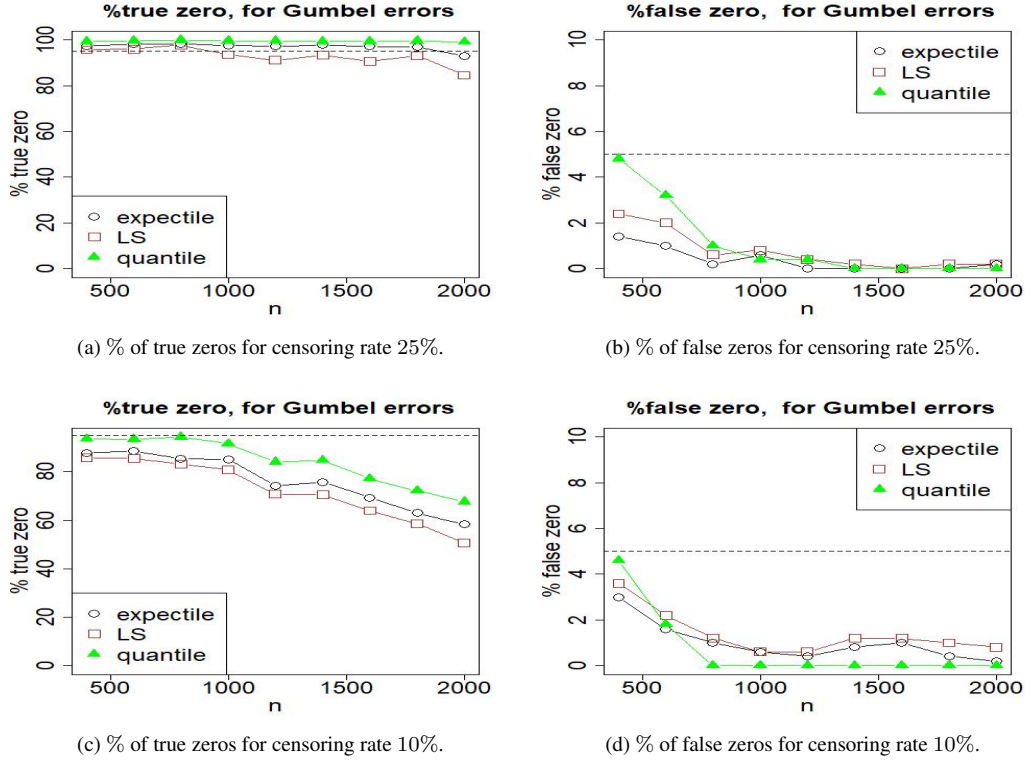
**Table 9** Accuracy results ( $L2 \equiv \|\hat{\beta}_n - \beta^0\|$ ,  $SD \equiv sd((\hat{\beta}_n - \beta^0)_A)$ ), automatic selection (% true 0 and % false 0) of  $\hat{\beta}_n$  obtained by 500 Monte Carlo replications for censored adaptive LASSO expectile method, when  $\varepsilon \sim \mathcal{G}(0, 1)$ ,  $p = 50$ ,  $\beta_0^0 = 0$ ,  $\mathcal{A} = \{1, 2, 3, 4, 5\}$ , censoring rate 25%, models estimated without intercept.

### Supplementary Material: additional simulation results

Here we provide additional simulation results to complement those in Section 4.



**Fig. 8** Percentage evolution of the true and false zeros with respect to  $n$  for five sequences  $\lambda_n$  by censored adaptive LASSO expectile method, for model without intercept ( $\beta_0^0 = 0$ ), when  $p = 10$ , censoring rate 25%,  $\varepsilon \sim \mathcal{G}(0, 1)$ .



**Fig. 9** Percentage evolution of the true and false zeros by three censored adaptive LASSO estimation methods, for model without intercept ( $\beta_0^0 = 0$ ), supposition with intercept, when  $\varepsilon \sim \mathcal{G}(0, 1)$  and  $p = 10$ .

$\beta_0^0$	$\varepsilon$	$n$	$\hat{\tau}$ of (4)	(7) starting with $\varepsilon$			(7) starting with $\eta^{(0)}(y_i)$		
				$\hat{\tau}^{(1)}$	% true 0	% false 0	$\hat{\tau}^{(1)}$	% true 0	% false 0
2	$\mathcal{G}(0, 1)$	100	0.21	0.21	94	0.6	0.56	92	0.4
		100	0.29	0.29	98	0	0.57	98	0
	$\mathcal{U}(0, 1) - 1/6$	50	0.49	0.49	93	2.5	0.57	93	2.2
		100	0.50	0.50	95	0.1	0.56	95	0.1
		500	0.50	0.56	98	0	0.63	98	0
0	$\mathcal{G}(0, 1)$	100	0.22	0.21	93	0.1	0.55	90	0.1
		100	0.28	0.28	97	0	0.55	97	0
	$\mathcal{U}(0, 1) - 1/6$	50	0.50	0.50	90	1.9	0.57	90	1.8
		100	0.49	0.48	94	0.05	0.55	94	0.05
		500	0.50	0.56	99.6	0	0.62	99.5	0

**Table 10** Estimation of  $\tau$  by 1000 Monte Carlo replications, for model without intercept ( $\beta_0^0 = 0$ ) and with intercept ( $\beta_0^0 = 2$ ), when  $p = 48$ ,  $\mathcal{A} = \{1, 2\}$ ,  $\beta_1^0 = 5$ ,  $\beta_2^0 = 1$ ,  $\lambda_n = n^{1/2-0.1}$ , censoring rate 25%.

$\beta_0^0$	$\varepsilon$	$n$	(7) starting with $\varepsilon$			(7) starting with $\eta^{(0)}(y_i)$		
			$\hat{\beta}_1^0$	$\hat{\beta}_2^0$	$\hat{\beta}_3^0$	$\hat{\beta}_1^0$	$\hat{\beta}_2^0$	$\hat{\beta}_3^0$
2	$\mathcal{G}(0, 1)$	100	4.55	0.91	-0.005	4.46	0.88	-0.01
	$\mathcal{U}(0, 1) - 1/6$	100	4.54	0.90	0.001	4.48	0.89	0.004
0	$\mathcal{G}(0, 1)$	100	5.03	1	-0.004	4.9	0.98	-0.003
	$\mathcal{U}(0, 1) - 1/6$	100	5.03	1	-0.002	4.95	0.99	-0.0008

**Table 11** Censored expectile estimation of  $\beta$  by 1000 Monte Carlo replications, for model without intercept ( $\beta_0^0 = 0$ ) and with intercept ( $\beta_0^0 = 2$ ), when  $p = 3$ ,  $\beta_1^0 = 5$ ,  $\beta_2^0 = 1$ ,  $\beta_3^0 = 0$ , censoring rate 25%.