• Supplementary File •

## Reinforcement Learning with Actor-critic for Knowledge Graph Reasoning

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## Appendix A The whole MAP results

In the supplementary file, we give the whole tasks MAP results in Table A1 and detailed experimental result analysis. For the overall MAP shown in the last row of Table A1, our approach significantly outperforms the other three methods [1–3], which validates the strong reasoning ability of our model. For most relations, our method shows high improvement effects. However, there exist some relations that are slightly influenced due to some reason.

Since actor-critic combines policy-based and value-based networks, our model ACRL covers the original network of DeepPath. The reasoning paths found by ACRL contains almost all ones found by DeepPath. What's more, because of the evaluation of the value-based network and the interaction between 'actor' and 'critic', ACRL can find more effective reasoning paths and eliminate the wrong paths or path circles, improving the performance of fact prediction. Thus, ACRL outperforms most tasks in fact prediction substantially. However, when the original paths are already correct and complete, ACRL will show little improvement effect. Overall, ACRL shows great improvement effects than other methods.

Tasks	ACRL	DeepPath	TransE	TransD	Improvement
personBornInLocation	0.4878	0.2895	0.2652	0.0924	+68.50%
athletePlaysForTeam	0.4384	0.2435	0.1400	0.1494	+80.04%
teamPlaysSport	0.4120	0.3084	0.3567	0.1216	+33.59%
athleteHomeStadium	0.7291	0.7291	0.3810	0.0830	+0.00%
agentBelongsToOrganization	0.3287	0.3308	0.3498	0.1286	-0.64%
athletePlaysInLeague	0.5199	0.5059	0.4676	0.0762	+2.77%
personLeadsOrganization	0.4831	0.4785	0.3494	0.2496	+0.96%
${\it organization} {\it Head} {\it Quartered} {\it In} {\it City}$	0.6420	0.5929	0.2569	0.1520	+8.28%
organization Hired Person	0.5257	0.4475	0.3073	0.3554	+17.47%
teamPlaysInLeague	0.7300	0.6532	0.7186	0.1421	+11.76%
worksFor	0.4818	0.4611	0.2313	0.2494	+4.49%
athletePlaysSport	0.4254	0.5247	0.5224	0.2651	-23.34%
Overall	0.5170	0.4638	0.3622	0.1720	+11.47%

Table A1	Fact	prediction	results	(MAP	)
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## Appendix B Examples of reasoning paths found by ACRL and DeepPath

Table B1 and Table B2 are some examples of reasoning paths found by ACRL and DeepPath, respectively. These relations of experimental tasks come from NELL-995 [4]. Inverses of existing relations are denoted by '\_inv'.

Take for example task 'athletePlaysForTeam', DeepPath finds one more reasoning path 'athleteLedSportsTeam  $\rightarrow$  team-PlaysAgainstTeam' than ACRL, which is a fake one. ACRL evaluates this policy through the critic part, and does not employ this reasoning path. Therefore, ACRL achieves high improvement in the task 'athletePlaysForTeam'. For the same reason, task 'organizationHiredPerson', 'organizationHeadQuarteredInCity' and 'worksfor' show better results by ACRL.

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Besides, ACRL's critic part can assess actor's performance in order to prevent the emergence of the reasoning path circles, which reduces the validity of KG reasoning. In the task 'personBornInLocation', DeepPath finds some circle reasoning paths like 'personGraduatedFromUniversity  $\rightarrow$  personGraduatedFromUniversity.inv  $\rightarrow$  personBornInCity', 'personGraduatedFromUniversity  $\rightarrow$  personGraduatedSchool\_inv  $\rightarrow$  personBornInCity' and 'personBelongsToOrganization  $\rightarrow$  personBelongsToOrganization\_inv  $\rightarrow$  personBornInCity'. Conversely, ACRL eliminates these circle paths and performs better. Tasks 'athletePlaysInLeague' and 'personLeadsOrganization' have the same phenomenon.

However, the result of task 'athletePlaysSport' shows a special case that there's some probability the optimal path cannot be reserved until the end in multistep relation reasoning. It is a universality in all methods that multistep process reserves partial relations rather than the whole in each step according to the rules and computing power, which may influence the results.

In addition, ACRL shows little improvement in some tasks like 'athleteHomeStadium' and 'agentBelongsToOrganization'. According to the comparison between ACRL and DeepPath's reasoning path, it is obvious that they find almost the same reasoning paths 'athletePlaysForTeam  $\rightarrow$  teamHomeStadium' and 'athleteLedSportsTeam  $\rightarrow$  teamHomeStadium' about relation 'athleteHomeStadium'. ACRL can hardly improve results under the circumstance that reasoning paths are already correct and complete.

As we can see, since DeepPath fails to use the relation information entirely in the KG, it generally performs worse than our method ACRL. Our method ACRL achieves better MAP with a more compact set of learned paths. However, when there are not enough extra paths between entities, our method and DeepPath can find almost the same reasoning paths, which leads to the little improvement. In conclusion, ACRL experimental results of the fact prediction task on NELL-995 dataset shows larger performance improvement compared with the state-of-the-art methods as a whole.

Table D1 Example reasoning paths found by ACIL		
Relation	Reasoning Path	
personBornInLocation	personBornInCity	
athletePlaysForTeam	athleteLedSportsTeam	
	athleteHomeStadium $\rightarrow$ teamHomeStadium_inv	
athleteHomeStadium	athlete PlaysForTeam $\rightarrow$ teamHomeStadium	
	athleteLedSportsTeam $\rightarrow$ teamHomeStadium	
agentBelongsToOrganization	agentCollaboratesWithAgent	
	subpartOf	
athletePlaysInLeague	athlete PlaysForTeam $\rightarrow$ teamPlaysInLeague	
	athleteLedSportsTeam $\rightarrow$ teamPlaysInLeague	
personLeadsOrganization	personBelongsToOrganization	
	worksFor	
${\it organization} Head Quartered In City$	radioStationInCity	
	televisionStationInCity	
	hasOfficeInCity	
	headQuarteredIn	
organization Hired Person	worksFor_inv	
	organizationTerminatedPerson	
	personBelongsToOrganization_inv	
	coachesTeam_inv	
worksFor	organizationHiredPerson_inv	
	personLeadsOrganization	
	agentCollaboratesWithAgent_inv	
	journalistWritesForPublication	
athletePlaysSport	athletePlaysForTeam $\rightarrow$ teamPlaysSport	
	athleteledSportsTeam $\rightarrow$ teamPlaysSport	
	athletePlaysInLeague $\rightarrow$ teamPlaysInLeague_inv $\rightarrow$ teamPlaysSport	
	athleteFlyOutToSportsTeamPosition $\rightarrow$ sportHasSportsTeamPosition_inv $\rightarrow$	
	$sportFansInCountry \rightarrow sportFansInCountry\_inv$	

Table B1 Example reasoning paths found by ACRL

## References

- Xiong W, Hoang T, Wang W Y. DeepPath: A Reinforcement Learning Method for Knowledge Graph Reasoning. In EMNLP, 2017:564-573.
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- 3 Guoliang J, Shizhu H, Liheng X, et al. Knowledge graph embedding via dynamic mapping matrix. In: ACL, 2015:687–696.
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	Example reasoning paols found by Deepi and	
Relation	Reasoning Path	
personBornInLocation	personBornInCity personGraduatedFromUniversity $\rightarrow$ personGraduatedFromUniversity_inv – personBornInCity	
	personGraduatedFromUniversity $\rightarrow$ personGraduatedSchool_inv $\rightarrow$ personBornInCity	
	person BelongsToOrganization $\rightarrow$ person BelongsToOrganization_inv $\rightarrow$ person BornInCity	
athlete Plays For Team	athleteLedSportsTeam athleteHomeStadium $\rightarrow$ teamHomeStadium_inv athleteLedSportsTeam $\rightarrow$ teamPlaysAgainstTeam	
athleteHomeStadium	athletePlaysForTeam $\rightarrow$ teamHomeStadium athleteLedSportsTeam $\rightarrow$ teamHomeStadium	
agentBelongsToOrganization	agentCollaboratesWithAgent subpartOf agentControls_inv agentCollaboratesWithAgent_inv	
athletePlaysInLeague	athletePlaysForTeam $\rightarrow$ teamPlaysInLeague athleteLedSportsTeam $\rightarrow$ teamPlaysInLeague athleteHomeStadium $\rightarrow$ leagueStadiums_inv athletePlaysSport $\rightarrow$ teamPlaysSport_inv $\rightarrow$ teamPlaysInLeague	
	$athletePlaysForTeam \rightarrow teamPlaysAgainstTeam\_inv \rightarrow teamPlaysInLeague athletePlaysSport \rightarrow teamPlaysSport\_inv \rightarrow teamPlaysAgainstTeam\_inv - teamPlaysInLeague athleteFlyOutToSportsTeamPosition \rightarrow athleteFlyOutToSportsTeamPosition\_inv \rightarrow athletePlaysSport \rightarrow teamPlaysSport\_inv \rightarrow teamPlaysInLeague athletePlaysSport \rightarrow teamPlaysSport\_inv \rightarrow teamPlaysInLeague athletePlaysSport → teamPlaysSport\_inv → teamPlaysInLeague athletePlaysSport\_inv → teamPlaysSport\_inv → teamPlaysInLeague athletePlaysSport → teamPlaysSport\_inv → teamPlaysInLeague athletePlaysSport\_inv → teamPlaysInLeague athletePlaysInLeague athletePlaysInLe$	
personLeadsOrganization	personBelongsToOrganization worksFor organizationTerminatedPerson_inv mutualProxyFor_inv organizationHiredPerson_inv agentCollaboratesWithAgent_inv worksFor → worksFor_inv → worksFor	
organizationHeadQuarteredInCity	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	
organizationHiredPerson	worksFor_inv organizationTerminatedPerson personBelongsToOrganization_inv coachesTeam_inv mutualProxyFor personLeadsOrganization_inv	
worksFor	organizationHiredPerson_inv personLeadsOrganization agentCollaboratesWithAgent_inv journalistWritesForPublication topmemberOfOrganization	
athletePlaysSport	$\begin{array}{l} a the tep PlaysFor Team \rightarrow team PlaysSport\\ a the teled Sports Team \rightarrow team PlaysSport\\ a the tep PlaysIn League \rightarrow team PlaysIn League\_inv \rightarrow team PlaysSport\\ a the tep PlaysIn League \rightarrow team PlaysIn LeagueStadiums \rightarrow sportUsesStadium\_inv\\ a the tep PlaysIn League \rightarrow subpart Of Organization\_inv \rightarrow team PlaysSport\\ \end{array}$	

 ${\bf Table \ B2} \quad {\rm Example \ reasoning \ paths \ found \ by \ DeepPath}$