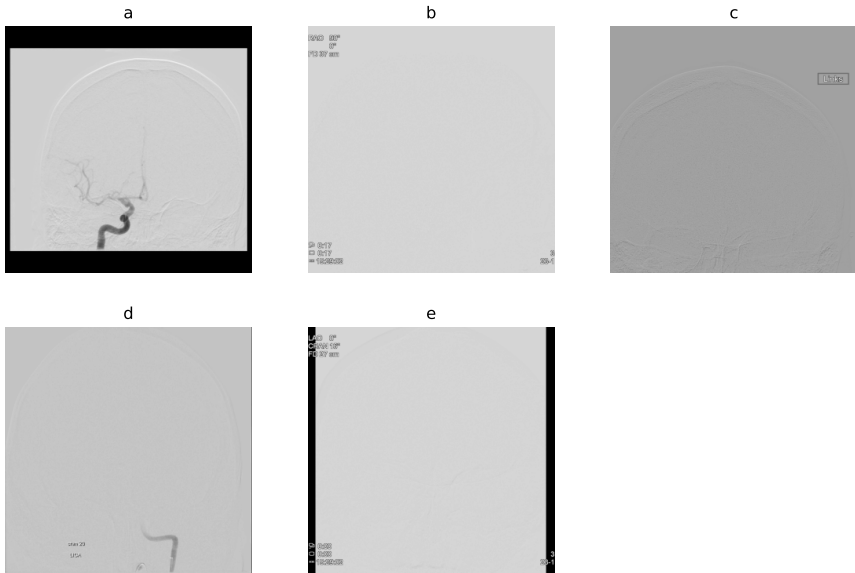
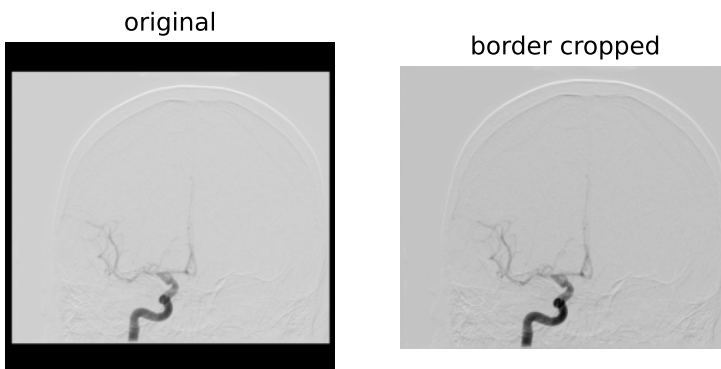


## B Supplementary data

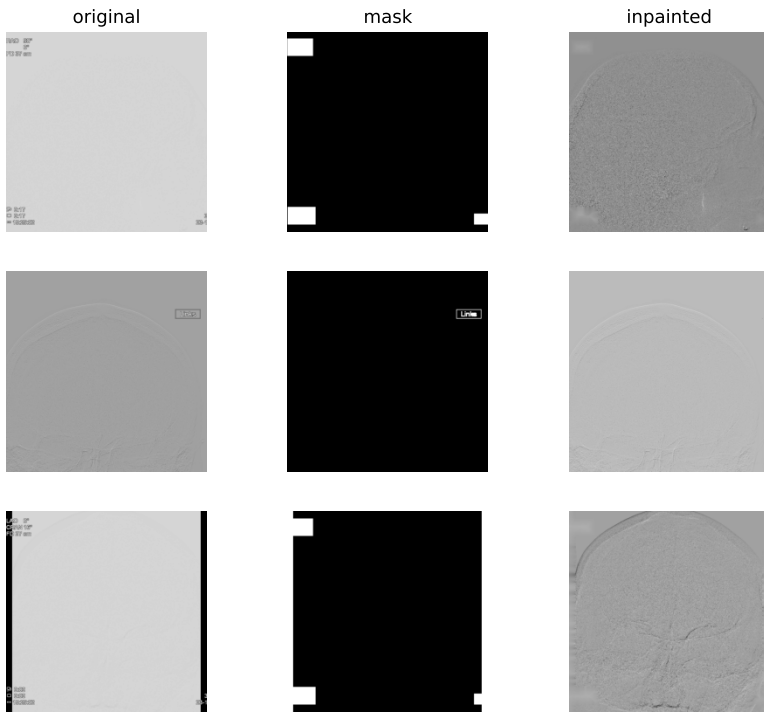
### B.1 Data pre-processing



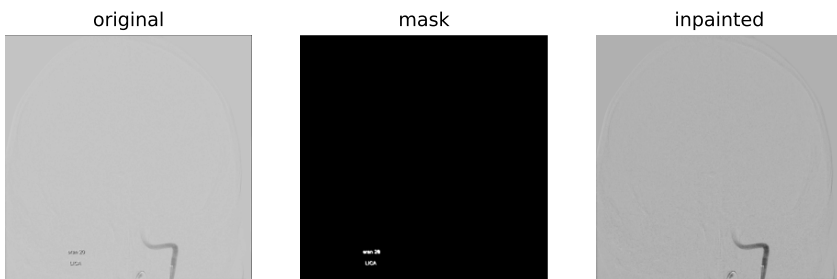
**Fig. 1** Common artefacts in DSA sequences in the Mr Clean registry. a: border artefacts. b: embedded overlays. c: embedded text with bounding box (Allura Xper device) d: embedded text (Axiom artis device) e: Combinations of border artefacts and embedded overlays.



**Fig. 2** Border removal. Border artefact in original image is automatically identified and cropped (or masked in the proceeding Figures).

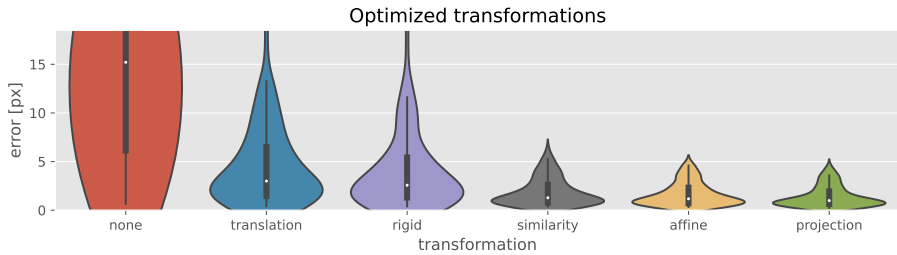


**Fig. 3** Allura Xper pre-processing. The standard overlay and text with bounding box are automatically identified, masked and inpainted using Open CV.



**Fig. 4** Axiom Artis pre-processing. Text is automatically identified, masked and inpainted using Open CV. Borders are removed if identified.

## B.2 Optimized transformations (lateral)



**Fig. 5** Average alignment error for transformations computed using manual annotations from lateral MinIP pairs. The violin represents the data distribution and inside, the median (white), interquartile range (gray, thick) and inter-adjacent value range (gray, thin) are indicated.

## B.3 Landmark model performance

The prediction error over the three fold validation for AP minIps. Two methods, argmax and centre of mass are used to infer the coordinate from the probability distributions.

**Table 2** The prediction error over the three fold validation for AP minIps.

centre of mass average prediction error [ <i>pixels</i> ] (mean + s.d.)							
Loss	mean	25 <sup>th</sup> ICA	mean ICA	75 <sup>th</sup> ICA	25 <sup>th</sup> M1	mean M1	75 <sup>th</sup> M1
$KL_{fw}$	6.6 ± 0.7	1.9 ± 0.3	7.0 ± 0.7	6.9 ± 2.6	1.7 ± 0.3	6.2 ± 0.8	5.8 ± 1.7
$KL_{bw}$	5.9 ± 0.4	1.8 ± 0.3	6.1 ± 0.6	5.7 ± 1.6	1.6 ± 0.3	5.7 ± 0.4	5.1 ± 1.0
$KL_{fw} N$	5.8 ± 1.0	1.9 ± 0.5	5.6 ± 0.8	5.7 ± 1.2	2.1 ± 0.8	6.0 ± 1.3	6.6 ± 2.0
$KL_{bw} N$	6.4 ± 0.6	2.1 ± 0.5	5.9 ± 0.4	6.2 ± 1.5	2.9 ± 0.7	6.8 ± 0.8	7.6 ± 1.7
$KL_{fw} N_s$	8.5 ± 2.2	2.5 ± 0.4	8.0 ± 2.0	7.8 ± 1.7	3.5 ± 1.1	8.9 ± 2.4	10.0 ± 2.6
$KL_{bw} N_s$	9.9 ± 3.2	3.5 ± 1.0	9.0 ± 2.1	10.5 ± 2.5	5.6 ± 3.0	10.8 ± 4.3	13.8 ± 4.6
$JS$	6.4 ± 0.7	1.9 ± 0.4	6.9 ± 0.6	6.5 ± 2.0	1.5 ± 0.4	6.0 ± 0.8	5.5 ± 1.8
$p_{comb.1}$	<b>4.3 ± 0.4</b>	<b>1.6 ± 0.1</b>	<b>4.6 ± 0.3</b>	<b>4.4 ± 0.4</b>	<b>1.4 ± 0.2</b>	<b>4.1 ± 0.6</b>	<b>3.7 ± 0.3</b>
$p_{comb.2}$	4.9 ± 0.7	1.9 ± 0.3	4.9 ± 0.4	5.0 ± 0.6	1.9 ± 0.5	5.0 ± 1.0	5.7 ± 1.0

argmax prediction error [ <i>pixels</i> ] (mean + s.d.)							
Loss	mean	25 <sup>th</sup> ICA	mean ICA	75 <sup>th</sup> ICA	25 <sup>th</sup> M1	mean M1	75 <sup>th</sup> M1
$KL_{fw}$	5.1 ± 0.4	1.8 ± 0.3	5.3 ± 0.5	5.2 ± 1.4	1.5 ± 0.4	4.8 ± 0.5	4.4 ± 1.3
$KL_{bw}$	5.1 ± 0.4	1.8 ± 0.3	5.2 ± 0.5	4.9 ± 1.3	1.5 ± 0.4	4.9 ± 1.0	4.3 ± 0.9
$KL_{fw} N$	11.0 ± 1.2	7.2 ± 1.6	11.7 ± 1.6	13.0 ± 3.0	6.8 ± 0.7	10.4 ± 0.8	12.3 ± 1.5
$KL_{bw} N$	13.0 ± 1.8	9.1 ± 2.7	13.5 ± 1.5	16.2 ± 3.0	8.9 ± 2.5	12.6 ± 2.3	15.4 ± 4.1
$KL_{fw} N_s$	12.9 ± 7.2	5.7 ± 4.5	13.2 ± 7.3	13.0 ± 6.8	4.8 ± 2.4	12.5 ± 7.1	11.6 ± 4.1
$KL_{bw} N_s$	13.4 ± 1.5	5.0 ± 2.9	10.3 ± 2.7	11.6 ± 5.1	11.8 ± 4.4	16.4 ± 5.3	20.3 ± 4.8
$JS$	6.2 ± 0.2	1.8 ± 0.3	6.6 ± 0.8	5.5 ± 1.1	<b>1.3 ± 0.2</b>	5.9 ± 1.2	4.3 ± 1.2
$p_{comb.1}$	<b>4.6 ± 0.5</b>	<b>1.6 ± 0.3</b>	<b>5.0 ± 0.6</b>	<b>4.5 ± 0.4</b>	<b>1.3 ± 0.2</b>	<b>4.1 ± 0.5</b>	<b>3.8 ± 0.4</b>
$p_{comb.2}$	11.1 ± 1.4	6.9 ± 1.5	11.8 ± 1.9	12.6 ± 2.7	6.5 ± 0.5	10.4 ± 1.0	11.8 ± 1.0

## B.4 Landmark model t-test comparisons

**Table 3** The prediction error over the three fold validation for lateral minIps.

centre of mass average prediction error [ <i>pixels</i> ] (mean + s.d.)							
Loss	mean	25 <sup>th</sup> ICA	mean ICA	75 <sup>th</sup> ICA	25 <sup>th</sup> M1	mean M1	75 <sup>th</sup> M1
$KL_{fw}$	5.5 ± 0.9	1.6 ± 0.3	5.3 ± 0.9	4.3 ± 0.4	1.9 ± 0.5	5.7 ± 0.9	5.4 ± 1.0
$KL_{bw}$	5.3 ± 1.0	1.4 ± 0.2	5.3 ± 1.2	4.0 ± 0.4	1.9 ± 0.4	5.4 ± 0.8	5.0 ± 0.7
$KL_{fw} N$	4.8 ± 0.9	1.4 ± 0.2	4.7 ± 1.1	3.8 ± 0.3	1.8 ± 0.4	4.9 ± 0.7	4.9 ± 0.8
$KL_{bw} N$	5.7 ± 0.6	2.2 ± 0.4	5.6 ± 0.8	5.5 ± 0.7	2.3 ± 0.6	5.7 ± 0.6	6.5 ± 1.2
$KL_{fw} N_s$	10.7 ± 3.9	3.3 ± 0.2	10.8 ± 3.4	10.5 ± 2.2	3.5 ± 0.3	10.6 ± 4.4	11.3 ± 3.3
$KL_{bw} N_s$	8.6 ± 2.1	4.6 ± 3.0	9.0 ± 2.2	10.2 ± 4.0	3.9 ± 2.0	8.3 ± 2.1	10.1 ± 4.7
$JS$	5.2 ± 0.6	1.4 ± 0.3	4.7 ± 0.8	3.7 ± 0.6	1.8 ± 0.4	5.7 ± 0.5	5.2 ± 1.0
$p_{comb.1}$	<b>3.9 ± 0.4</b>	<b>1.3 ± 0.1</b>	<b>3.7 ± 0.5</b>	<b>3.3 ± 0.1</b>	<b>1.6 ± 0.3</b>	<b>4.1 ± 0.4</b>	<b>4.4 ± 0.2</b>
$p_{comb.2}$	4.2 ± 0.3	1.4 ± 0.2	4.1 ± 0.4	3.8 ± 0.2	1.7 ± 0.2	4.3 ± 0.3	4.7 ± 0.1

argmax prediction error [ <i>pixels</i> ] (mean + s.d.)							
Loss	mean	25 <sup>th</sup> ICA	mean ICA	75 <sup>th</sup> ICA	25 <sup>th</sup> M1	mean M1	75 <sup>th</sup> M1
$KL_{fw}$	4.3 ± 0.7	1.3 ± 0.2	3.8 ± 0.9	3.4 ± 0.3	<b>1.7 ± 0.5</b>	4.8 ± 0.8	4.9 ± 0.7
$KL_{bw}$	4.6 ± 0.6	1.3 ± 0.2	4.3 ± 0.6	3.5 ± 0.5	1.8 ± 0.6	5.0 ± 0.6	4.7 ± 0.8
$KL_{fw} N$	10.2 ± 0.6	7.8 ± 0.3	10.6 ± 1.3	11.5 ± 0.1	7.0 ± 0.5	9.8 ± 0.0	11.9 ± 0.8
$KL_{bw} N$	11.3 ± 0.2	9.6 ± 1.9	12.9 ± 1.2	15.5 ± 1.6	6.7 ± 1.8	9.7 ± 1.2	12.1 ± 2.4
$KL_{fw} N_s$	26.6 ± 9.5	10.5 ± 2.2	25.2 ± 6.5	24.6 ± 5.4	9.7 ± 2.2	28.0 ± 12.5	30.1 ± 15.2
$KL_{bw} N_s$	10.5 ± 2.8	6.3 ± 3.6	11.8 ± 2.8	14.1 ± 5.9	3.9 ± 2.4	9.2 ± 2.9	11.1 ± 5.1
$JS$	4.9 ± 1.1	1.3 ± 0.2	4.3 ± 1.1	3.5 ± 0.5	<b>1.7 ± 0.5</b>	5.5 ± 1.2	4.9 ± 1.0
$p_{comb.1}$	<b>3.9 ± 0.4</b>	<b>1.1 ± 0.2</b>	<b>3.6 ± 0.5</b>	<b>3.2 ± 0.0</b>	1.8 ± 0.3	<b>4.2 ± 0.5</b>	<b>4.3 ± 0.1</b>
$p_{comb.2}$	10.0 ± 0.3	7.8 ± 0.3	10.4 ± 0.7	11.4 ± 0.6	6.8 ± 0.5	9.7 ± 0.8	11.6 ± 0.8

**Table 4** Students t-test comparing the model performance trained with different loss functions.  $H_0$  : the average argmax prediction error is smaller for *model*<sub>1</sub> than for *model*<sub>2</sub>. Probabilities are computed over the three fold validation. In bold if more than 95% confidence.

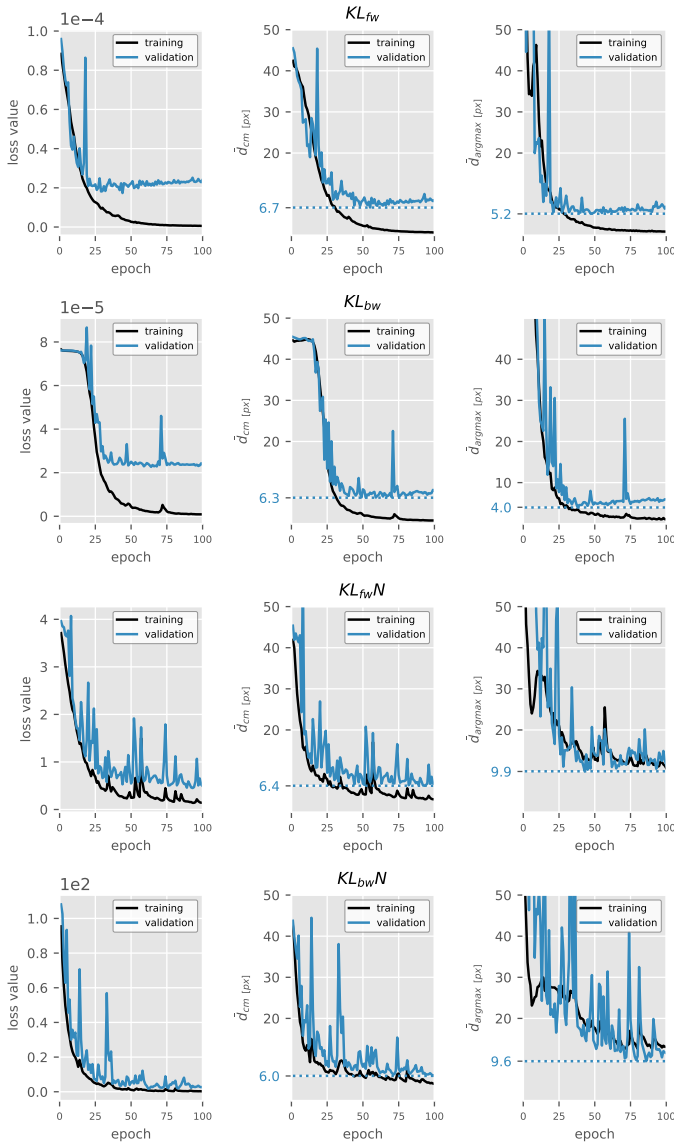
<i>model</i> <sub>1</sub>	<i>model</i> <sub>2</sub>	$KL_{fw}$	$KL_{bw}$	$KL_{fw} N$	$KL_{bw} N$	$KL_{fw} N_s$	$KL_{bw} N_s$	$JS$	$p_{comb.1}$	$p_{comb.2}$
$KL_{fw}$			0.15	0.21	0.36	0.84	0.88	0.41	0.01	0.04
$KL_{bw}$		0.85		0.45	0.79	0.91	0.92	0.81	0.01	0.08
$KL_{fw} N$		0.79	0.55		0.73	0.9	0.92	0.75	0.07	0.19
$KL_{bw} N$		0.64	0.21	0.27		0.87	0.9	0.55	0.01	0.05
$KL_{fw} N_s$		0.16	0.09	0.1	0.13		0.69	0.14	0.03	0.05
$KL_{bw} N_s$		0.12	0.08	0.08	0.1	0.31		0.11	0.04	0.05
$JS$		0.59	0.19	0.25	0.45	0.86	0.89	0.11	0.01	0.04
$p_{comb.1}$		<b>0.99</b>	<b>0.99</b>	0.93	<b>0.99</b>	<b>0.97</b>	<b>0.96</b>	<b>0.99</b>		0.82
$p_{comb.2}$		<b>0.96</b>	0.92	0.81	<b>0.95</b>	<b>0.95</b>	<b>0.95</b>	<b>0.96</b>	0.18	

**Table 5** Students t-test comparing the lateral model performance trained with different loss functions.  $H_0$  : the average argmax prediction error is smaller for *model*<sub>1</sub> than for *model*<sub>2</sub>. Probabilities are computed over the three fold validation. In bold if more than 95% confidence.

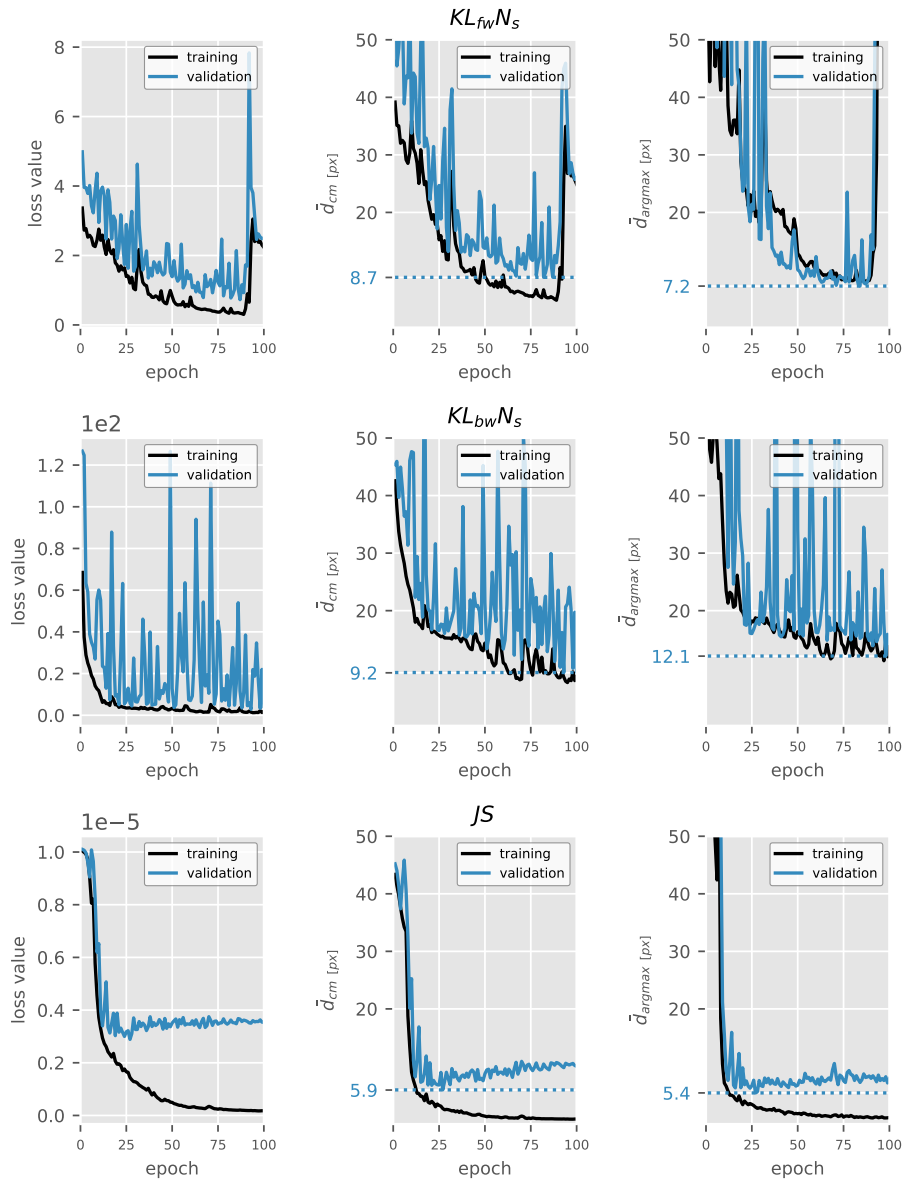
<i>model</i> <sub>1</sub>	<i>model</i> <sub>2</sub>	$KL_{fw}$	$KL_{bw}$	$KL_{fw} N$	$KL_{bw} N$	$KL_{fw} N_s$	$KL_{bw} N_s$	$JS$	$p_{comb.1}$	$p_{comb.2}$
$KL_{fw}$			0.43	0.23	0.58	0.93	0.94	0.36	0.04	0.06
$KL_{bw}$		0.57		0.3	0.65	0.94	0.94	0.45	0.07	0.1
$KL_{fw} N$		0.77	0.7		0.84	0.95	<b>0.96</b>	0.69	0.13	0.21
$KL_{bw} N$		0.42	0.35	0.16		0.93	0.93	0.25	0.01	0.02
$KL_{fw} N_s$		0.07	0.06	0.05	0.07		0.27	0.06	0.03	0.04
$KL_{bw} N_s$		0.06	0.06	0.04	0.07	0.73		0.05	0.02	0.02
$JS$		0.64	0.55	0.31	0.75	0.94	<b>0.95</b>	0.03	0.06	0.06
$p_{comb.1}$		<b>0.96</b>	0.93	0.87	<b>0.99</b>	<b>0.97</b>	<b>0.98</b>	<b>0.97</b>		0.78
$p_{comb.2}$		0.94	0.9	0.79	<b>0.98</b>	<b>0.96</b>	<b>0.98</b>	0.94	0.22	

## B.5 Landmark model training curves and metrics

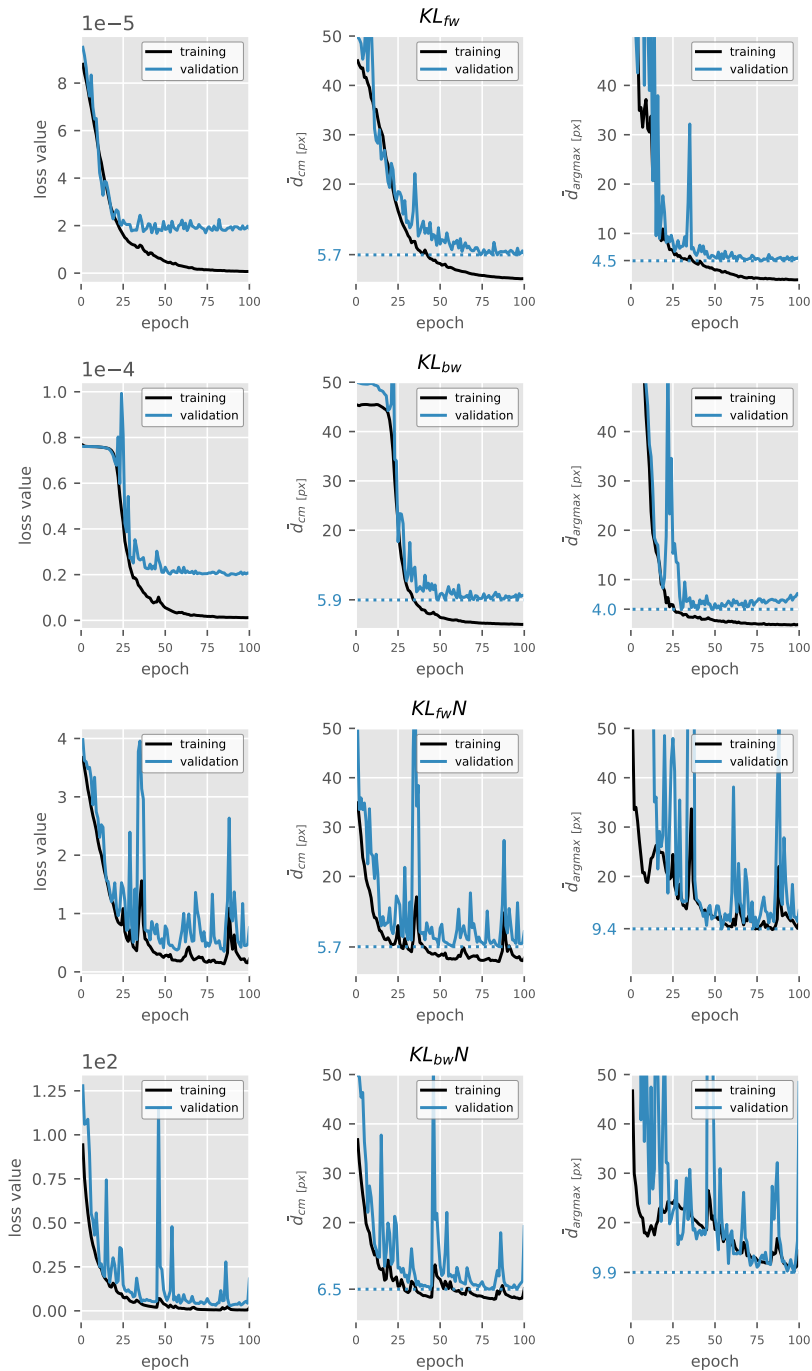
The implicit loss functions display unstable behaviour. An attempt was made to improve stability by incorporating a smoothing kernel  $\sigma = 0.5$  before computing the loss. This had a negative effect and was not resolved.



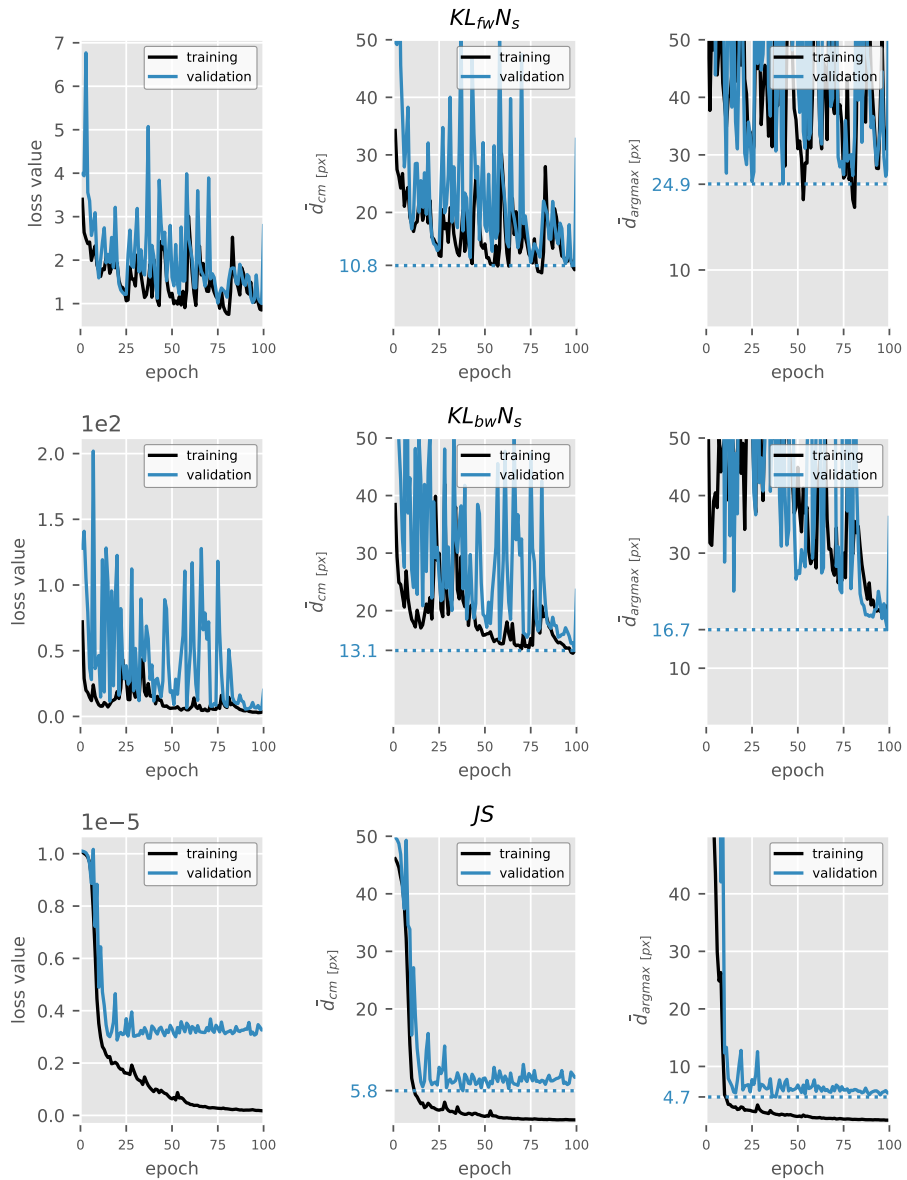
**Fig. 6** Loss curves (first column), centre-of-mass error (second column) and argmax error (third column) for loss functions indicated in the centre column and trained on AP images



**Fig. 7** Loss curves (first column), centre-of-mass error (second column) and argmax error (third column) for loss functions indicated in the centre column and trained on AP images



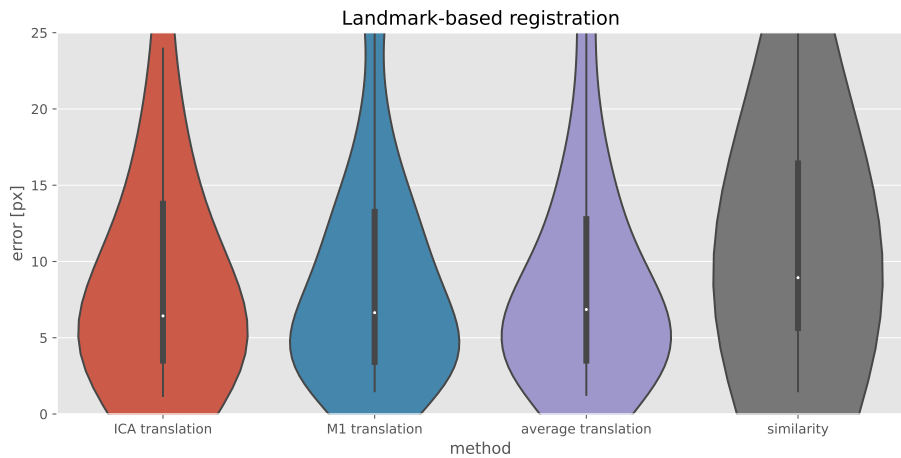
**Fig. 8** Loss curves (first column), centre-of-mass error (second column) and argmax error (third column) for loss functions indicated in the centre column and trained on lateral images



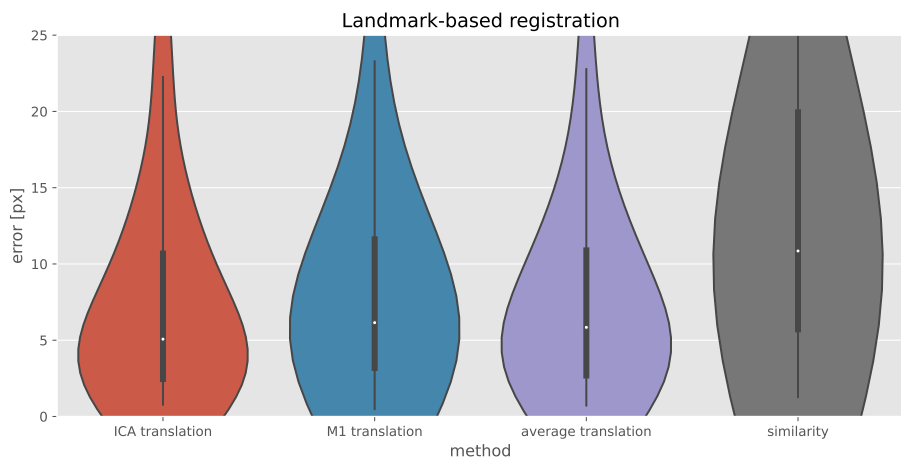
**Fig. 9** Loss curves (first column), centre-of-mass error (second column) and argmax error (third column) for loss functions indicated in the centre column and trained on lateral images



## B.6 Landmark-based registration



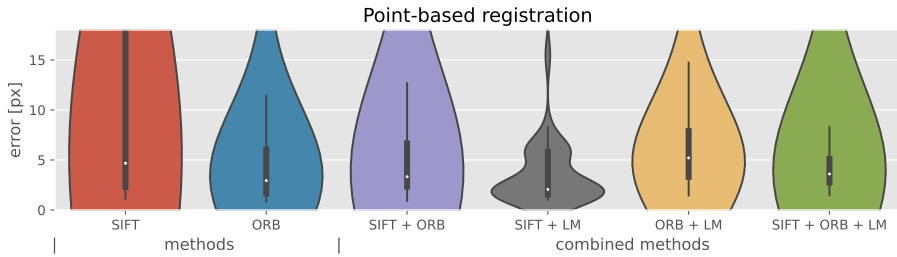
**Fig. 10** Registration error using the only the landmark point correspondences for AP DSA MinIPs.



**Fig. 11** Registration error using the only the landmark point correspondences for lateral DSA MinIPs.





**B.8 Point-based registration violin plot (AP)**

**Fig. 12** Registration error (averaged distance between annotated point-correspondences) for least-squares similarity transformations using different subsets of automatically identified point correspondences in AP images.

## B.9 Elastix registration Z-tests

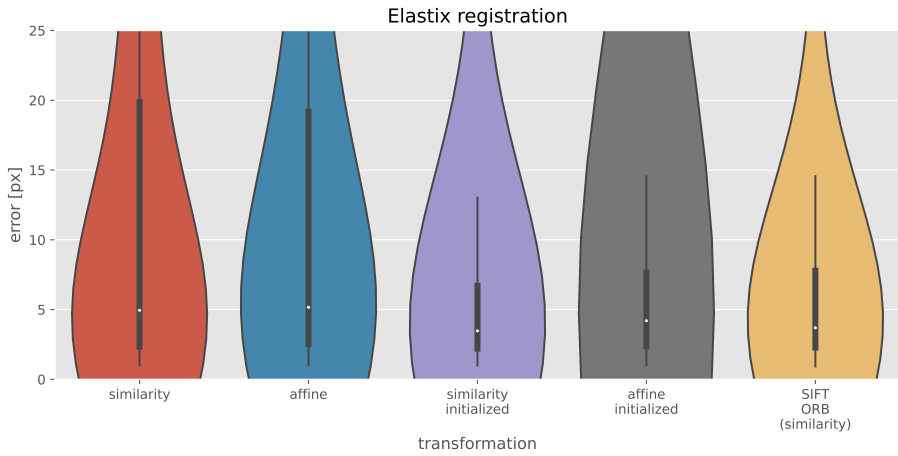
Table 3: z-test for elastix method on AP images. If method (row) has a worse mean, the probability is set to one. The best performing elastix method is highlighted in bold.

Metric	MMI			MSD			NCC			SIFT ORB							
	Transformation	similarity	affine	similarity (initialized)	affine (initialized)	similarity	affine	similarity (initialized)	affine (initialized)	similarity	affine	similarity (initialized)	affine (initialized)	similarity	affine	similarity (initialized)	affine (initialized)
MMI	similarity	1.00	0.03	0.56	1.00	0.58	1.00	0.01	0.29	1.00	1.00	0.01	0.72	1.00	0.02	0.97	1.00
	affine	1.00	1.00	1.00	1.00	1.00	1.00	0.92	1.00	1.00	0.89	1.00	1.00	1.00	0.39	1.00	1.00
	similarity (initialized)	1.00	0.08	1.00	1.00	1.00	1.00	0.05	0.62	1.00	0.06	1.00	0.04	1.00	0.04	1.00	1.00
MSD	affine (initialized)	1.00	0.08	0.97	1.00	1.00	1.00	0.04	0.59	1.00	0.04	1.00	0.98	1.00	0.04	1.00	1.00
	similarity	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.99	1.00	0.99	1.00	0.42	1.00	1.00	1.00
	affine	1.00	0.19	1.00	1.00	1.00	1.00	0.13	1.00	1.00	0.14	1.00	1.00	0.07	1.00	1.00	
NCC	similarity (initialized)	0.56	0.01	0.28	1.00	0.28	1.00	0.01	0.13	1.00	0.01	1.00	0.48	0.01	1.00	0.59	1.00
	affine (initialized)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.50	1.00	1.00	1.00
	similarity	<b>0.46</b>	<b>0.01</b>	<b>0.21</b>	<b>0.00</b>	<b>0.21</b>	<b>0.00</b>	<b>0.00</b>	<b>0.09</b>	<b>0.89</b>	<b>0.01</b>	<b>1.00</b>	<b>0.42</b>	<b>0.01</b>	<b>0.01</b>	<b>0.49</b>	<b>1.00</b>
SIFT ORB	affine	1.00	0.18	1.00	1.00	1.00	0.14	0.74	1.00	0.17	1.00	1.00	1.00	0.07	1.00	1.00	1.00
	similarity (initialized)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
	affine (initialized)	1.00	0.04	0.63	1.00	0.65	1.00	0.02	0.36	1.00	0.03	1.00	0.75	0.02	1.00	1.00	1.00
similarity	0.33	0.01	0.14	1.00	0.17	1.00	0.00	0.05	0.75	0.01	0.88	0.39	0.01	0.38	0.01	1.00	1.00

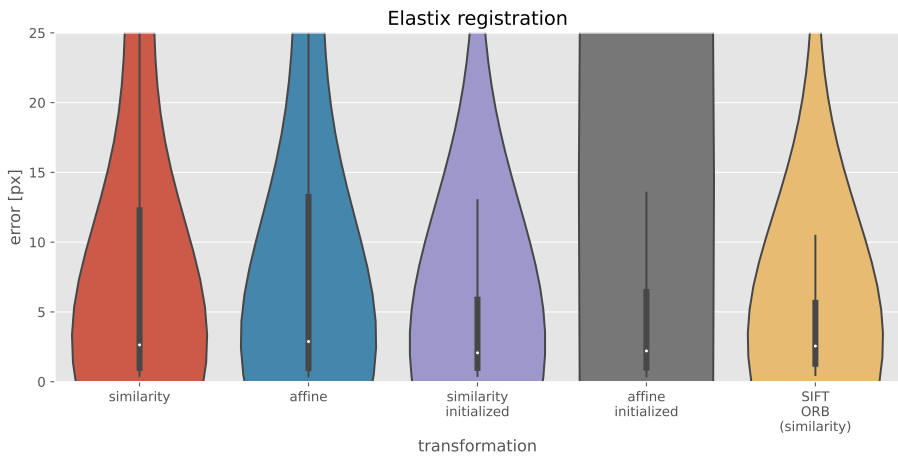
Table 4: z-test for elastix method on lateral images. If method (row) has a worse mean, the probability is set to one. The best performing elastix method is highlighted in bold.

Metric	MMI			MSD			NCC			SIFT ORB				
	Transformation	similarity	affine	similarity (initialized)	affine (initialized)	similarity	affine	similarity (initialized)	affine (initialized)	similarity (initialized)	affine (initialized)	similarity	ORB	
<b>MMI</b>	similarity	1.00	0.12	1.00	0.76	0.03	1.00	1.00	0.03	0.66	0.31	0.11	1.00	
	affine	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.98	1.00	0.57	0.17	1.00	
	<b>similarity (initialized)</b>	<b>0.59</b>	<b>0.08</b>	<b>1.00</b>	<b>0.40</b>	<b>0.01</b>	<b>0.73</b>	<b>0.74</b>	<b>0.02</b>	<b>0.44</b>	<b>0.29</b>	<b>0.10</b>	<b>0.18</b>	1.00
<b>MSD</b>	affine (initialized)	1.00	0.14	1.00	1.00	0.05	1.00	1.00	0.04	0.81	0.33	0.11	0.28	1.00
	similarity	1.00	0.62	1.00	1.00	1.00	1.00	1.00	0.50	1.00	0.47	0.14	0.77	1.00
	affine	0.84	0.10	1.00	0.61	0.02	1.00	0.99	0.02	0.58	0.30	0.11	0.22	1.00
<b>MSD</b>	similarity (initialized)	0.86	0.11	1.00	0.64	0.03	1.00	1.00	0.03	0.59	0.30	0.11	0.22	1.00
	affine (initialized)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.57	0.17	1.00	1.00
	similarity	1.00	0.22	1.00	1.00	0.21	1.00	1.00	0.11	1.00	0.35	0.12	0.36	1.00
<b>NCC</b>	affine	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.33	1.00	1.00
	similarity (initialized)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
	affine (initialized)	1.00	0.92	1.00	1.00	1.00	1.00	1.00	0.90	1.00	0.55	0.16	1.00	1.00
<b>SIFT ORB</b>	similarity	0.56	0.08	0.97	0.38	0.01	0.70	0.72	0.02	0.43	0.29	0.10	0.18	1.00

## B.10 Elastix registration violin plot



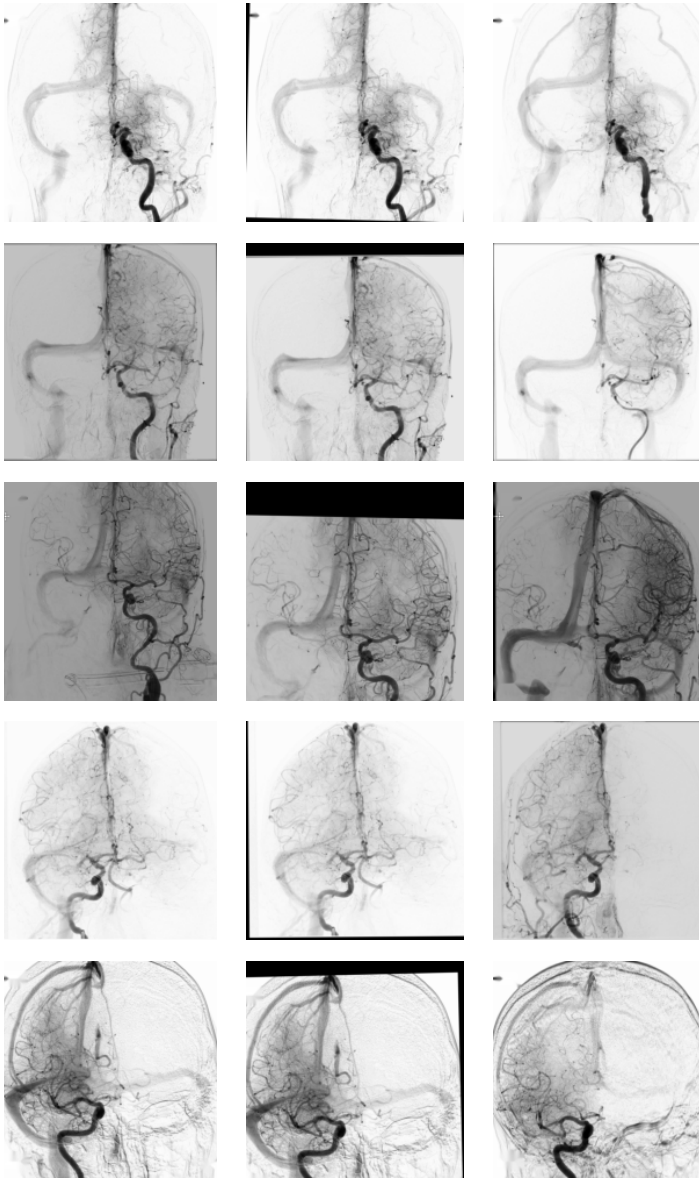
**Fig. 13** Results of elastix registration optimizing mattes mutual information for AP images



**Fig. 14** Results of registration optimizing mattes mutual information for lateral images.

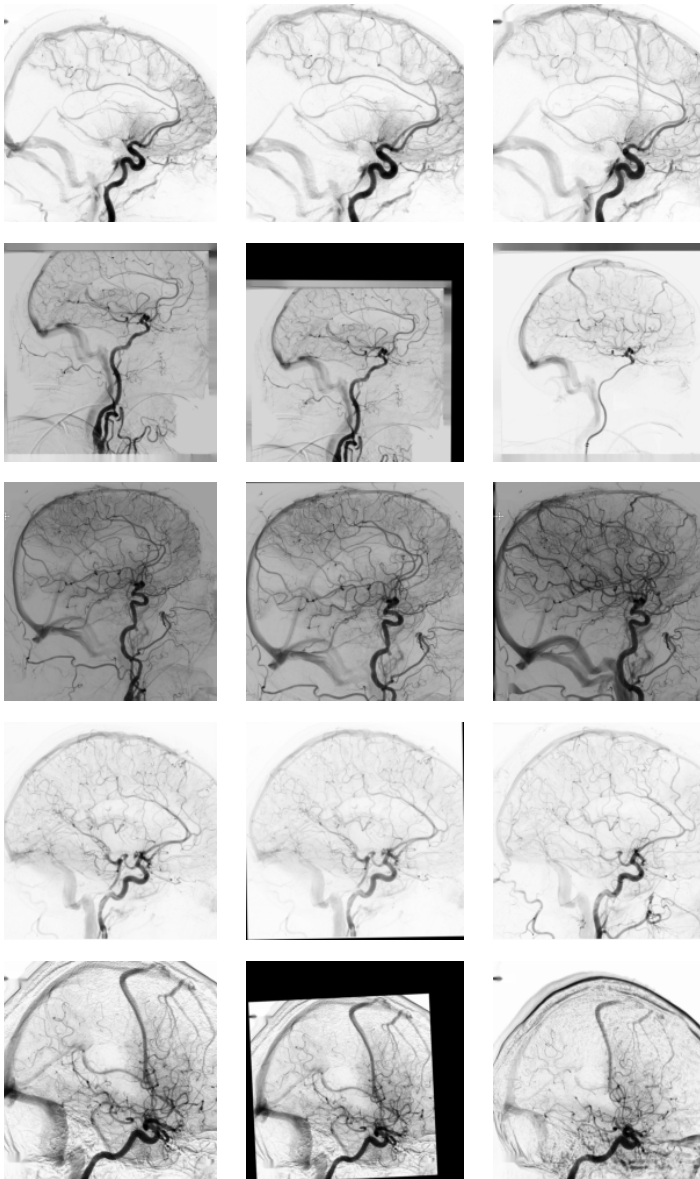
## B.11 Automatic registration examples

Images are aligned using SIFT and ORB points to compute the similarity transformation.



**Fig. 15** AP registration examples: left column pre-EVT, middle is pre-EVT aligned to post-EVT in the right column.





**Fig. 16** Lateral registration examples: left column pre-EVT, middle is pre-EVT aligned to post-EVT in the right column.