

# Constraints from material properties on the dynamics and evolution of Earth's core

Christopher Davies<sup>1,3</sup>, Monica Pozzo<sup>2</sup>, David Gubbins<sup>1,3</sup>, Dario Alfè<sup>2,4</sup>

<sup>1</sup>*School of Earth and Environment, University of Leeds, Leeds LS2 9JT, U.K.*

<sup>2</sup>*Department of Earth Sciences and Thomas Young Centre at UCL, UCL, Gower Street, WC1E 6BT, London, U.K.*

<sup>3</sup>*Institute of Geophysics and Planetary Physics, Scripps Institution of Oceanography, University of California San Diego, 9500 Gilman Drive, La Jolla, CA 92093-0225*

<sup>4</sup>*Department of Physics and Astronomy and London Centre for Nanotechnology, UCL, Gower Street, WC1E 6BT, London, U.K.*

This document contains four tables. Supplementary Table 1 is a more complete version of Table 1 in the main text that gives values for depth-varying quantities at the inner core boundary (ICB) as well as the core-mantle boundary (CMB) and provides error estimates where available. Supplementary Tables 2–4 list polynomial coefficients for depth-dependent properties listed in Table 1. Diffusion coefficients for Oxygen and Silicon,  $D_O$  and  $D_{Si}$  ( $\text{m}^2 \text{ s}^{-1}$ ), thermal conductivity  $k$  ( $\text{W m}^{-1} \text{ K}^{-1}$ ), density  $\rho$  ( $\text{kg m}^{-3}$ ), electrical conductivity  $\sigma$  ( $\text{S m}^{-1}$ ), adiabatic temperature  $T_a$  (K), viscosity  $\nu$  (mPa s), melting temperature  $T_m$  (K), and thermal expansion coefficient  $\alpha_T$  ( $\text{K}^{-1}$ ) are presented up to third order in pressure  $P$ .

Symbol	Definition	Units	100%Fe	82%Fe-8%O-10%Si	79%Fe-13%O-8%Si	81%Fe-17%O-2%Si
$\Delta\rho$	ICB density jump	gm cc <sup>-1</sup>	0.24 [1]	0.6 [2]	0.8 [3]	1.0 [3]
$c_O^S$	O concentration (solid)		—	0.0002 [4]	0.0004 [4]	0.0006 [5]
$c_{Si}^S$	Si concentration (solid)		—	0.0554 [4]	0.0430 [4]	0.0096 [5]
$c_O^L$	O conc (liquid)		—	0.0256 [4]	0.0428 [4]	0.0559 [5]
$c_{Si}^L$	Si conc (liquid)		—	0.0560 [4]	0.0611 [4]	0.0115 [5]
$C_p$	Specific heat	J kg <sup>-1</sup> K <sup>-1</sup>	715 [6] — 800 [7] 1.4 [8] — 1.5 [1, 6] 1.05 (0.05) [1] 0.75 (0.1) 6350 (300) [1, 9]	—	—	—
$\gamma$	Grüneisen parameter		—	—	—	—
$\Delta S$	Entropy of Melting ( $r_i$ )	$k_B$	—	—	—	—
$L$	Latent heat ( $r_i$ )	MJ kg <sup>-1</sup>	—	—	—	—
$T_m$	Melting point ( $r_i$ )	K	—	5900 (300)	5580 (300)	5320 (300)
$\alpha_T$	Thermal expansivity	$K^{-1} \times 10^{-5}$	1.0 [6, 10] 6350 (300) 1, 9 4735 (300) [1]	$r_i$ 5900 (300) 6.25 10.9 9.01 12.9 9.01 -0.35 -1.03 -0.48 -1.39	$r_o$ — — 9.75 6.01 12.9 9.01 -0.34 -1.00 -0.48 -1.39	$r_i$ — — 9.41 5.81 9.01 -0.33 -0.48
$T_a$	Temperature	K	—	5900 (300)	5580 (300)	5330 (300)
$\frac{\partial T_a}{\partial P}$	K GPa <sup>-1</sup>	6.96	—	4290 (300)	4105 (300)	3910 (300)
$\frac{dT_m}{dP}$	K GPa <sup>-1</sup>	9.01	—	—	—	—
$\frac{\partial T_a}{\partial r}$	K km <sup>-1</sup>	-0.39	—	—	—	—
$\frac{dT_m}{dr}$	K km <sup>-1</sup>	-0.48	—	—	—	—
$C_r$	$\frac{dr_i}{dt} = C_r dT_o / dt$	m K <sup>-1</sup>	-14.96	-10.39	-9.50	-8.75
$C_c$	$\frac{dC_X}{dt} = C_c C_r dT_o / dt$	10 <sup>-9</sup>	-3.16	-3.16	-5.28	-6.90
$\sigma$	Electrical conductivity	S m <sup>-1</sup> × 10 <sup>6</sup>	1.56 (1) [II], 1.6 [12] 2.32 [13, a]	$r_i$ $r_o$ 1.36 (1) [II], 1.4 [12] 1.86 [13, b]	$r_i$ $r_o$ 1.27 (1) [II] 1.12 (1) [II]	$r_i$ $r_o$ 1.11 (1) [II] 1.33 (1) [II]
$k$	Thermal conductivity	W m <sup>-1</sup> K <sup>-1</sup>	246 [11], 230 [12] 281 [13]	$r_i$ $r_o$ 159 (1) [11], 150 [12] 170 [13]	$r_i$ $r_o$ 1.07 (1) [11] 1.24 (1) [II]	$r_i$ $r_o$ 1.18 (1) [II]
$D_O$	O Diffusivity [11]	$m^2 s^{-1} \times 10^{-8}$	—	—	—	—
$D_{Si}$	Si Diffusivity [11]	$m^2 s^{-1} \times 10^{-8}$	—	—	—	—
$\nu$	Viscosity [11]	mPa s	11.9 (9)	6.9 (4)	11.7 (10)	6.7 (8)
$\alpha_O^D$	Barodiffusion coeff (O)	kg m <sup>-3</sup> s × 10 <sup>-12</sup>	—	0.72	0.97	1.11
$\alpha_{Si}^D$	Barodiffusion coeff (Si)	kg m <sup>-3</sup> s × 10 <sup>-12</sup>	—	1.19	1.10	40.6
$\alpha_c$	Chemical expansivity [14, 15]	$\times 10^{10}$ ev/atom	—	—	—	—
$(\partial \mu / \partial c)_{P,T}$			—	—	—	—

**Table 1: Core material properties for pure iron and three Fe-O-Si mixtures.** Models are named after the mass concentrations of mixtures of Fe, O, and Si corresponding to the given density jump. Quantities in the first section define the core chemistry model used in this review. Numbers in the second section determine the core temperature properties given in the third section. The core temperature is assumed to follow an adiabat, denoted  $T_a$ , which intersects the melting temperature  $T_m$  of the mixture at the inner core boundary (ICB).  $C_r = [T_i/T_o][\rho(r_i)g(r_i)(\frac{dT_m}{dP} - \frac{\partial T_a}{\partial P})]^{-1}$  specifies the inner core growth rate for a given cooling rate;  $C_c = 4\pi r_i^2 \rho(r_i) (c_X^l - c_X^s) / M_{oc}$ , together with  $C_r$ , determines the rate of change of light elements in the outer core.  $T_i = T_a(r_i)$  and  $T_o = T_a(r_o)$  are respectively the temperatures at the ICB (radius  $r_i$ ) and CMB (radius  $r_o = 3480$  km),  $M_{oc} = 1.85 \times 10^{24}$  kg is the mass of the outer core and  $k_B$  is Boltzmann's constant. All values given at the ICB radius pertain to the present-day. All values are accompanied by a reference unless they are derived quantities. Where a range is given, numbers highlighted in red are used in the core models in section 3. <sup>a</sup>: This value was derived at a presumed ICB temperature of 4971 K; <sup>b</sup>: This value was derived at a presumed CMB temperature of 3750 K.  $\mu$  is the chemical potential.

Quantity	1	P	$P^2$	$P^3$
$D_O$	$3.15284 \times 10^{-9}$	$1.58911 \times 10^{-10}$	$-7.79726 \times 10^{-13}$	$1.08753 \times 10^{-15}$
$D_{Si}$	$9.67659 \times 10^{-9}$	$-5.52376 \times 10^{-11}$	$1.92294 \times 10^{-13}$	$-2.31242 \times 10^{-16}$
$k$	69.541	0.24992	0.000289419	$-6.57978 \times 10^{-7}$
$\rho$	7597.11	21.3527	-0.0314965	$2.64104 \times 10^{-5}$
$\sigma$	844513	3295.58	-11.59	0.0166341
$T_a$	2941.37	10.8331	-0.00743569	$-2.07225 \times 10^{-8}$
$\nu$	20.4292	-0.229596	0.00119676	$-1.76303 \times 10^{-6}$
$T_m$	1698.55	27.3351	-0.0664736	$7.94628 \times 10^{-5}$
$\alpha_T$	$3.09159 \times 10^{-5}$	$-1.58122 \times 10^{-7}$	$4.47468 \times 10^{-10}$	$-4.87145 \times 10^{-13}$

Table 2: Coefficients for polynomial fits to depth-dependent core properties obtained from *ab initio* calculations<sup>11</sup>.  $\Delta\rho = 0.6 \text{ gm cc}^{-1}$ .

Quantity	1	P	$P^2$	$P^3$
$D_O$	$8.13315 \times 10^{-9}$	$1.01693 \times 10^{-10}$	$-6.27438 \times 10^{-13}$	$9.96886 \times 10^{-16}$
$D_{Si}$	$5.41447 \times 10^{-9}$	$-2.77825 \times 10^{-12}$	$-3.44781 \times 10^{-14}$	$8.53179 \times 10^{-17}$
$k$	49.5315	0.435578	-0.000563041	$4.67761 \times 10^{-7}$
$\rho$	7580.08	20.8655	-0.0306676	$2.59429 \times 10^{-5}$
$\sigma$	$1.05182 \times 10^6$	-126.985	5.1831	-0.00919998
$T_a$	2733.82	12.2139	-0.0162101	$1.42997 \times 10^{-5}$
$\nu$	4.04062	0.0188676	$-2.88082 \times 10^{-6}$	$9.16488 \times 10^{-8}$
$T_m$	1498.55	27.3351	-0.0664736	$7.94628 \times 10^{-5}$

Table 3: Coefficients for polynomial fits to depth-dependent core properties obtained from *ab initio* calculations<sup>11</sup>.  $\Delta\rho = 0.8 \text{ gm cc}^{-1}$ .

Quantity	1	P	$P^2$	$P^3$
$k$	44.5507	0.539047	-0.0011221	$1.39095 \times 10^{-6}$
$\sigma$	0.895385	0.00327394	$-1.07115 \times 10^{-5}$	$1.45871 \times 10^{-8}$
$T_a$	2594.91	11.6949	-0.0131957	$8.20578 \times 10^{-6}$
$T_m$	1298.55	27.3351	-0.0664736	$7.94628 \times 10^{-5}$

Table 4: Coefficients for polynomial fits to depth-dependent core properties obtained from *ab initio* calculations<sup>5</sup>.  $\Delta\rho = 1.0 \text{ gm cc}^{-1}$ .

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