### Reviewers' comments:

Reviewer #1 (Remarks to the Author):

Most network analysis of the human brain uses the modularity maximization algorithm to detect meso-scale network architecture, which assumes the brain is composed of assortative communities. This assumption may not be valid, however, so this manuscript relates the modularity maximization algorithm to another algorithm, WBSM (weighted stochastic blockmodel), that does not assume assortative community structure. This is a compelling argument and an important exploration to help the field most accurately estimate community structure. This manuscript is well-organized and well-written. As will be elaborated below, the reasons for proposing that all assortative communities is not a valid description of the brain's network structure need to be fleshed out to increase the impact of this manuscript.

More detailed comments:

Your argument is compelling and the introduction sets the problem up well. I found myself wondering, however, about concrete examples, where nodes and edges are known, of these different types of meso-scale architectures. To elaborate, many of the early modularity articles talk about small world/modular organization that has mainly assortative communities, and how those are observed in biology, nature and society when we can measure all connections, as well as in central nervous systems where we can measure all neurons and synapses (i.e., c. elegans). Those examples provide a strong argument that the brain may work in a similar efficient manner to all these other network examples. Are there concrete examples of these other types of meso-scale architectures, or a reason why fully assortative structure may work for some categories of networks but fall apart in the brain?

On a somewhat related note, the addition of other species, where we have better measurements of edges, is a strength of this manuscript. However, the main text is limited to general "and results are similar in other species" statements. This is 1) not fully accurate, since in reading the supplementary materials there are nuanced differences that may be important; and 2) reduces the strength of your argument. As of now, that data is a supplemental side note, but mentioned in the title, abstract and discussion as if it were a main part of the paper as well. If possible, I would add results from the other datasets into the main text. If you do not have space, I would make it more clear that the non-human datasets are not equal to the human dataset in terms of explanation in the paper, which would mean taking non-human out of the title and other parts of the manuscript that imply that you considered all equally.

Your last paragraph of the "Connectomes support diverse meso-scale architecture" Results section seems to be a bit strong of a conclusion given the analyses you conducted. You compared assortativity between Qmax and WSBM methods, and should expect assortativity to be lower in the WSBM method based on its algorithm versus that of Qmax, as you wrote earlier in that section. So this is more of a validation that the different algorithms are doing what you think they are than that the differences are functionally meaningful. Adding other network metrics that are thought to be important for cognition and comparing their values across algorithms would make that conclusion more appropriate...or not making that claim until you relate these two community structures to cognition or other metrics below.

Similarly, your first paragraph of the "Functional relevance of the WSBM" section "To this point, we have used the WSBM to demonstrate that connectomes exhibit diverse, non-assortative meso-scale structure...suggesting that the richer, non-assortative communities are closer to the brains canonical architecture." seems like a straw man, since the algorithm that allows for non-assortative meso-scale

structure finds some non-assortative communities, while the algorithm that limits its results to maximizing assortativity finds all assortative communities. This argument (that is scattered throughout the manuscript) needs an explanation regarding why maximizing assortativity to the exclusion of other types of communities is not as biologically plausible as allowing multiple types of community structure. There have been many papers arguing why algorithms maximizing modularity are biologically plausible. This concept that we are limiting our investigations by doing so is very compelling, but it needs more biological motivation (as well as functional relevance...see other comments about that below) to have a strong impact on the field.

You state later in that section that "Intuitively, functionally-related brain regions are linked by strong functional connections. If a community does a good job identifying sets of such regions, then the within-community density of functional connections should be greater than the between-community density." But the point of the manuscript is that assuming communities have this strong-within and weak-between connectivity is not necessarily correct, and we should allow for other types of communities (Figure 1). That sentence seems to contradict the main point of the manuscript. It is very possible that I am missing something, but regardless that concept should be clarified so as to not seem contradictory if it isn't. Further, the result that follows appears to show that even with WSBM, when averaging across the whole brain, communities are assortative (strong within, weaker between). It is also unclear to me how both within and between-community connections can be more dense if the nodes and edges are matched across algorithms, so more explanation about that is needed as well.

"Community morphospace reveals rules for between-community interactions": how do the previouslydescribed results offer "a better explanation for human brain function and mouse genetic expression than that provided by assortative communities alone"? Thus far, I am convinced that it is "different", but have seen no evidence that it is "better".

Also in that section, your description of the results is that the WSBM algorithm identifies a significant number of core-periphery interactions (which I see in Figure 6) and disassortative interactions (which I do not see). It looks to me that the proportion of disassortative interactions using WSBM, and the difference between WSBM and Qmax, are both 0. Please clarify in the text and the figure what you mean by this.

Your brain figures exclude subcortical brain regions, yet they keep popping up in the article as diverse and one of the groups of regions that would be better defined using WSBM. Please add images of the subcortical structures as well (this goes for all figures that show where in the brain different node types are).

Behavioral relevance section: it would be interesting to do this analysis using Qmax to define community structure as well, to determine which of the two algorithms best explains behavior. If WSBM is more related to behavior on these cognitive control tasks, that is an argument for the functional relevance (and potentially higher accuracy) of community structure derived from that algorithm.

In your first sentence of the discussion, while I don't disagree that having different types of communities is plausible, I have not seen a strong argument for that other than that an algorithm that attempts to find these different types of communities can. This to me is no less biased than modularity maximization being biased to find an assortative community structure. This argument should be made more explicit and linked to biology throughout the manuscript to support your conclusions.

Your sentence: "Moreover, communities detected using the weighted stochastic blockmodel better

recapitulated observed intrinsic functional relationships among brain regions in the human, and relationships between gene co-expression patterns in the mouse, compared to more commonly-used techniques such as modularity maximization." See my point above about this results section. This argument does not logically follow to me.

The last full sentence on page 12 is the first I have seen that gives a biological reason for looking for non-assortative community structure. If this and other related arguments are highlighted more in both the introduction and discussion, this paper will be more convincing.

### Reviewer #2 (Remarks to the Author):

"Diversity of meso-scale architecture" by Betzel et al. compares two forms of community decompositions applied to structural connectomic data – a classic decomposition that maximises the assortativity (Qmax) of the decomposition with a more recently developed weighted stochastic block algorithm (WSBM). The WSBM appears to group nodes into modules such that the likelihood of intermodule connections is approximately even for all nodes within each module (i.e. does not depend upon heavily upon each individual module). There is substantial interesting material in this manuscript which is clearly written and nicely illustrated. I do however hold a number of concerns:

1. One of the major findings is not really that surprising and I think more work is required to establish the significance of the finding. Namely, it is not surprising that any decomposition that does not maximise the assortativity of a module decomposition is less assortative than one that does! i.e. there is an element of circularity in the central finding of the paper. The question that seems not to be answered is not whether the WSBM decomposition reveals a less assortative community structure than Qmax, but whether the degree of core-periphery and disassortativity in the human connectome is greater or lesser than expected by chance: Since we already know that Qmax-sorted connectomes are more assortative than degree and strength preserving random surrogates, we should now check whether WSBM ones are likewise more or less arranged when such surrogates also account for the geometric embedding of real connectomes into three dimensions? Only after this has been established, do I think the more fine-grained analyses of figure 3-5 make sense.

2. I doubt as presented, many readers will understand what the WSBM actually does do, other than being "not maximally pro-assortative". There is a brief heuristic for the standard block model that seeks to minimise a cost function that penalises the heterogeneity of inter-module connectivity amongst nodes within the same module (that is my reading of equation (1). The WSBM is more complex, but I assume it is a generalisation of the same principle to accommodate edge weights. I think the authors should provide a better heuristic explanation of the WSBM minimization and put it at the beginning of the Results so that the general reader can understand what is being optimized.

3. I also think the paper would be improved with some groundtruth validations, using growth models, to show that the WSBM algorithm does what the authors assume it does – namely that Qmax and WSBM should converge if applied to networks that are generated by suitable preferential attachment models, that add new edges to maximize assortativity (the authors are leading experts in such generative modelling); Also that they should strongly diverge when such networks are grown to maximise core-periphery arrangements and for maximally disassortative networks.

4. I found the choice of the statistic for comparing functional and structural connectivity somewhat counter-intuitive: Namely of seeing if the corresponding functional networks (when grouped into the

corresponding modules) were maximally assortative. Its interesting, although counter-intuitive that WSBM outperforms Qmax on this metric. The authors should likely also be cautious that network measures based on linear correlations induce artificial assortativity through the nature of the measure [1].

5. Novelty: As the authors cite, there is already substantial work using SBMs in human connectomes. A brief summary of what is new here would help. Also, there are elements of the current findings that could be unpacked from prior work: for example, [2] previously showed that rich club nodes preferentially existed as apex nodes in open motifs of 3 nodes (that is maximally disassortative motifs [3]). Also, Figure 10a of [4] shows that very high degree nodes are actually less often inter-connected than by chance – i.e. have a "cartel-like" disassortative property. The present finding, by very different methods, seems reassuringly convergent.

6. I am somewhat (pleasantly) surprised, given the very noisy nature of individual tractography data that I have seen (expect perhaps for carefully reconstructed connectomes from the highly curated human connectome project) that individual correlations with performance were discovered. Brief details of acquisition and reconstruction must be provided in the Methods here, since this remains a contentious area. What was the connection density? Also, a very brief summary of these data could be given at the beginning of the Results.

7. Section on "Behavioural relevance...": Why/how were differences in total connection weight partialled out? Why not normalize the matrices to have uniform weights before the analysis? Were do the differences arise (e.g. do they correlate with white matter volume)? Also, what was the nature of the FDR correction? How many tests were performed/corrected for?

Minor:

1. Most of the first paragraph of the section "Connectomes support diverse ..." simply repeats the Intro and could be deleted.

2. I found it impossible to see any differences between Qmax and WSBM in Figure 3B.

3. Why are the WSBM networks more assortative than the null distribution in Fig 3C?

4. Suggest delete the interpretive phrase "suggesting the capacity for an equally ..." from p6 of the Results.

5. It is the authors' own preference, but I found aspects of the Discussion highly speculative for an original research article.

6. p13: The cite regarding repertoire diversity might also consider [3].

7. p15: How did the authors go from a whole group consistency-based connectome back to individual subjects?

8. p16: were the structural and functional connectomic data and the behavioural data all from the same subjects? Why 30 for structural connectivity and 70 for functional connectivity?

References:

1. Zalesky, A., Fornito, A., & Bullmore, E. (2012). On the use of correlation as a measure of network connectivity. Neuroimage, 60(4), 2096-2106.

2. Harriger L, Van Den Heuvel MP, Sporns O. 2012 Rich club organization of macaque cerebral cortex and its role in network communication. PLoS ONE 7,

3. Sporns O, Kotter R (2004) Motifs in brain networks. PLoS Biology 2: e369.

4. Roberts JA, Perry A, Lord AR, Roberts G, Mitchell PB, Smith RE, Breakspear M (2016) The contribution of geometry to the human connectome. Neuroimage 124: 379-393.

Reviewer #3 (Remarks to the Author):

I quite enjoyed reading this report, which challenges the classical view of the view of the connectome being composed of segregated communities and introduces the alternative view on the existence of more heterogeneous community configurations.

Unlike to the standard methods used to define communities of the structural connectome, the authors utilize a different technique, weighted stochastic block model (WSBM), one that does not explicitly impose the assumption of the modularity maximization and hence segregated communities. Using the WSBM, this work "reveals" other kinds of communities and community interactions, where the newly found communities show a better overlap with the functional networks of the brain. It is also quite interesting to see that the intersubject variability in diversity of the community profiles of certain brain regions shows some correlation with the behavioral performance.

I think the paper introduces a novel and quite interesting perspective on the diversity of community organization in the connectome. My major comment is about the lack of true ground truth for the studied problem. As a logical decision, the authors chose to compare to the most commonly used state-of-the art method, modularity maximization, referred as Qmax here. However, this algorithm, as also stated by the authors is designed to maximize modularity and hence assortativeness. Hence, removing this particular constraint – modularity maximization – as in the case of using WSBM, naturally leads to less assortative community structures compared to Qmax, which by design extracts segregated communities. My main question is how do we know that the partitions returned by WSBM are more "correct" compared to those detected by Qmax? Having said that, I would acknowledge that this is not a drawback of the method presented here but a general concern about the lack of a true ground truth for the problem at hand. It may be important to at least mention or discuss this point and maybe point out that the results drastically change when the modularity maximization constraint is removed, although a true ground truth for neither algorithm exists.

Please find below some questions and comments about the specifics of the method and statistics used.

1) How does the approach followed by the authors differ from the hierarchical clustering method, cited as ref [35] in the manuscript, as to my knowledge this method also falls outside of the modularity maximization framework. Also, what was the motivation behind the choice of WSBM instead of for instance the hierarchical clustering approach as in [35]?

2) Page 2, first paragraph: "Next, we define a node-level diversity index that quantifies the extent to which individual neural elements participate in communities of all classes." Can a node (neural element) belong to multiple clusters; i.e. the communities can be overlapping and are not disjoint?

3) Fig. 3a: Are the within-technique variation of information (VI) scores based on the comparison of partitions with the same number of communities on two different subjects' datasets? As the comparisons are performed on partitions with the same number of communities, I assume two different partitions using the same technique can come from the use of different datasets. However, that is not clear at that point of the manuscript, as any information on different subjects' data etc. has been provided yet. The authors may want to explain what leads to different partitions with the same number of communities, which are used for comparison.

4) Fig. 3A: Also, the authors mention that both techniques, WSBM and Qmax lead to self-similar partitions that are statistically different between techniques. In Fig. 3A, the variation of information (VI) scores of WSBM are much higher than those of Qmax and for K=10, the within-technique VI for

WSBM is even higher than between-technique VI. What is the cause of such difference in withintechnique VI observed between the two techniques? Are the WSBM partitions reliable, if they show such high within technique VI scores?

5) The authors mention: "We compared these curves using functional data analysis, which is a set of statistical tools for comparing continuous curves [47,48]. We found that the observed scores were smaller than those obtained under the null model (p < 10-3), confirming that WSBM communities tend to be less assortative than Qmax (Fig. 3C)". Aren't these curves discrete set of measurements, hence allowing for a comparison for instance by Monte-Carlo approach; simply by shuffling the labels of assortativity scores between two methods over multiple comparisons?

6) I fail to understand Fig. 3C and the stats performed with functional data analysis. What does the yaxis labeled as "Probability" represent? The authors mention "Specifically, we generated a statistic by performing a pointwise subtraction and summation of the curves A<sup>-</sup>(N) obtained for the WSBM and Qmax. The value of this statistic quantifies the difference between mean community assortativity across communities of all sizes and is negative when communities detected using Qmax are more assortative than WSBMs. We compared this statistic against a null distribution obtained from a null model wherein we perserved the number and size of communities in a given partition but permute nodes' assignments uniformly and randomly (1000 repetitions)." What does the pointwise subtraction and summation of the curves A<sup>-</sup>(N) yield, is it average difference between the two curves? For the null distribution, doesn't the permutation of nodes result in non-continuous clusters, similar to a random assignment? Would that be a fair comparison to use?

7) The communities detected by WSBM more closely reflect the functional networks. However, I believe it is important to point out that functional networks emerge from the dynamics and interactions between neural elements that is constrained by the structural connections but not purely determined by them. Hence, although some degree of overlap between structure and function is expected, it is not expected that they will be the same or very similar. The effect of the dynamics would play a crucial role in the emergence of the functional networks.

8) The authors state "To test whether this was the case, we imposed partitions obtained from the WSBM and Qmax applied to the structural connectome onto the FC matrix and computed the difference of withinand betweencommunity FC density.We found that over a range K = 2, ..., 10, the WSBM consistently uncovered communities whose internal FC density exceeded their betweencommunity density (Fig. 5A)." The functional networks are defined on the FC matrix, hence I would have thought that they would superimpose FC matrix parcellation onto the structural connectome (SC) partitions. For instance Fig. 5A caption states: "Functional connectivity (FC) matrix ordered by functional system". As both, FC connectivity and the labeling of the functional systems come from the functional connectivity, how does this figure capture the partitions of the structural connectome? Is it a misunderstanding on my side or is there a confusion between SC and FC in the wording here?

9) I think the correlations between the diversity index and performance categorized according to functional networks is very interesting. From what I can see in Fig. 8B, one can conclude that some networks require certain type of motifs (interactions) such as the visual network and the DAN, whereas others such as the control network, subcortical areas and maybe also the default mode network contain interactions of various kinds for a good cognitive performance. What about the whole brain diversity of connections? Would that make any inference on the cognitive performance?

Minor points:

- Page1: What is the difference between clusters and communities? I found the illustration of different connectivity profiles in Fig. 1 very useful. It may be very helpful to illustrate the concepts of region, community, partition in a similar manner for the naïve reader, if possible, at least as supplementary material.

- Page 1: what do individual network nodes represent? Brain regions? It would be useful to specify here.

- Is assortative architecture the same as small-world, as used in some reports on connectome's architecture?

- Fig. 2: Community labeled with purple seems to consist of only one small brain region in the right hemisphere, which does not seem to have any correspondence in the left hemisphere, whether labeled as the same community or not. Where does this asymmetry stem from? Is it an algorithmic artifact?

- Fig. 3. Caption: Q\_max should be Q\_{max} in latex notation, "perserved" should be "preserved".

- Fig. 3F, what do the upper and lower limits of the box plot represent?

- Fig. 4C, how were the rich club nodes labeled/estimated?
- What is the difference between a core community and a hub?

- Page 13, first paragraph: I would say "functional connectivity" (FC) instead of "functional dynamics", as the comparison was done to FC and with the emergence of new methods such as dynamic functional connectivity etc, "functional dynamics" is now understood as changing functional connectivity.

- What was the motivation behind using a 128 parcellation and can the authors comment on if/how the change of parcellation may change the observed effects?

- Page 18: In section "Community and regional assortativity" the authors provide the equations for both directed and undirected graphs. Is that done so for the generalization of the provided methods for directed graphs? As far as I understand the results in the actual manuscript are based on undirected graphs. I believe the directed graph use may be necessary for the mouse data? If so, it may be worth mentioning this in the manuscript.

- Eq. (8): it could be easier for the reader if a different notation instead of double indexing was used to refer a\_i and a\_{iz\_i}. It is not clear to me what a\_{iz\_i} represents.

- It may also be useful to express the diversity index mathematically.

- The macaque connectome results seem to show the opposite trade in terms of being assigned to maximally assortative set as rich club and non-rich club members (Fig. S4O). Do the authors have any speculative idea on what may be the reason for this opposite trade?

# <sup>29</sup> Reviewer #1

## 30 Comment 1

Most network analysis of the human brain uses the modularity maximization algorithm to detect meso-scale 31 network architecture, which assumes the brain is composed of assortative communities. This assumption may 32 not be valid, however, so this manuscript relates the modularity maximization algorithm to another algorithm. 33 WBSM (weighted stochastic blockmodel), that does not assume assortative community structure. This is a 34 compelling argument and an important exploration to help the field most accurately estimate community 35 structure. This manuscript is well-organized and well-written. As will be elaborated below, the reasons for 36 proposing that all assortative communities is not a valid description of the brains network structure need to 37 be fleshed out to increase the impact of this manuscript. 38

Your argument is compelling and the introduction sets the problem up well. I found myself wondering, 39 however, about concrete examples, where nodes and edges are known, of these different types of meso-scale 40 architectures. To elaborate, many of the early modularity articles talk about small world/modular organization 41 that has mainly assortative communities, and how those are observed in biology, nature and society when 42 we can measure all connections, as well as in central nervous systems where we can measure all neurons 43 and synapses (i.e., c. elegans). Those examples provide a strong argument that the brain may work in a 44 similar efficient manner to all these other network examples. Are there concrete examples of these other 45 types of meso-scale architectures, or a reason why fully assortative structure may work for some categories 46 of networks but fall apart in the brain? 47 This is a good point. Most work in modern network science has focused on assortative communities 48

(oftentimes detected by maximizing a modularity quality function). Consequently, there is no shortage when
 it comes to finding examples in the literature of this type of community. However, there is also a parallel
 literature on blockmodeling that originated in the social sciences and statistics [1, 2] that has only recently
 been widely appreciated in other fields, like physics and computer science [3]. In any case, we agree that
 it would be good to note examples of non-assortative communities (core-periphery and disassortative) in
 complex networks.

<sup>55</sup> We have now added the following sentences to the **Introduction** section:

• "While this perspective has proven useful, it has a number of drawbacks, of which we focus on two. 56 First, it makes the strong assumption that connectome meso-scale architecture is strictly assortative 57 (Fig. 1A). This assumption stems in part from the algorithms used to detect communities, the most 58 popular of which seek internally dense and externally sparse sub-networks [4, 5]. As a result, these 59 algorithms are incapable of detecting non-assortative structure, such as core-periphery (Fig. 1B) and 60 disassortative (Fig. 1C) communities or mixtures of different community types (Fig. 1D), all of which 61 are evident in real-world socio-technical and biological networks [6, 7, 8, 9, 10, 11, 12]. Moreover, mod-62 ularity maximization and related techniques may overlook important and functionally-relevant charac-63 teristics of neural circuits, which exhibit non-assortative, cell type-specific wiring diagrams [13, 14, 15]. 64 It is unclear, then, whether the assortative communities uncovered using these algorithms represent 65 an accurate picture of connectome meso-scale structure or whether they reflect the assumptions and 66 limitations of the algorithms themselves." 67

The reviewer also suggests that it might be useful to test the WSBM framework on a network for which we have complete knowledge of its connectivity. To address this point, we used both  $Q_{max}$  and WSBM to detect communities in the *C. elegans* network of chemical synapses (we ignored electrical synapses, as it was unclear how to combine weight information about electrical and chemical synapses into the same network model and still retain interpretable and neurobiologically meaningful edge weights) [16].

Our analysis consists of two components. First, from communities detected using the WSBM and  $Q_{max}$ and with identical methods as in the main text, we constructed a morphospace of community interactions (Fig. 1). This figure demonstrates that when we use  $Q_{max}$  to uncover communities (and varying the number of communities from K = 2 to K = 10), they are *always* arranged in assortative motifs. Using the WSBM, on the other hand, we consistently identify both core-periphery and disassortative motifs. This finding indicates that the WSBM, indeed, detects non-assortative community structure. Moreover, because the *C. elegans* connectome has been painstakingly mapped out at the cellular level, we can rule out the possibility that the

- <sup>80</sup> non-assortative communities we reported in the original submission are a product of scale (inter-areal versus
- <sup>81</sup> inter-cellular connectomes).



Figure 1: Community morphospace for *C. elegans* connectome. The top panels depict the community morphospace (in log scale) for community dyads recovered from partitions detected using  $Q_{max}$  (left) and the WSBM (right). The color of each point represents each dyad's classification: cyan = assortative, yellow = core-periphery, and red = disassortative. The top plots are depicted with the number of communities fixed at K = 5. The bottom panels depict the proportion of dyad classes as we varied the number of communities from K = 2 to K = 10. In general,  $Q_{max}$  only detected assortative community dyads while the WSBM detected all three types.

As a second comparison of  $Q_{max}$  and the WSBM applied to C. elegans connectome data, we identified 82 representative partitions for each technique as we varied the number of communities from K = 2 to K = 10. 83 We then reordered and blocked the C. elegans connectivity matrix according to the communities uncovered 84 by the WSBM (Fig. 2A). In the margins of each plot, we color-coded each node's corresponding community 85 label as detected using  $Q_{max}$ . Had the two techniques generated similar community partitions, then we 86 would expect the  $Q_{max}$  labels to be homogeneous within each block. However,  $Q_{max}$  community labels are 87 heterogenously distributed within WSBM communities, demonstrating qualitatively that the two techniques 88 uncover communities of different character. 89

In addition, for the representative WSBM communities, we also show the density (average weight of all possible connections) of each block (Fig. 2B). While certain pairs of communities are configured in assortative relationships, many are not. These results suggest that the WSBM identifies non-assortative communities in the *C. elegans* connectome. Seeing this structure at the cellular scale in a fully-mapped connectome further supports the conclusions of our manuscript.

We now include these additional analyses in the Supplementary Materials under the section WSBMs
 at the cellular level:

"The human connectome data analyzed in the main text and the non-human connectomes analyzed in this supplement are examples of inter-regional networks. Individual cells and populations have been aggregated into spatially-contiguous, macroscopic parcels or regions. While this approach is common

and serves to reduce the dimensionality of a network (making it more manageable for analysis), it also averages over the properties of those cells and populations. If regions are homogeneous in terms of the cells that they contain, then region-level analysis loses very little information. However, if a region's constituent cells exhibit heterogeneity in terms of their connectivity patterns, then we lose access to this information. It is unclear, then, how the WSBM would behave when applied to a cellular-level network.

In this section, we apply the WSBM to the network of the nematode C. elegans. We analyze the 106 directed and weighted network of chemical synapses described in [16]. This network consists of 279 107 neurons, 2194 connections, and 6394 synapses (neurons can synapse onto one another more than once). 108 Our aim is to show that, even at this cellular scale, the WSBM identifies high levels of non-assortativity 109 while  $Q_{max}$  does not. As we note in the main text, this does not demonstrate conclusively that the 110 "true" meso-scale structure of C. elegans is composed of non-assortative communities. Instead, it 111 complements other recent papers [9] highlighting the apparent utility of blockmodels for identifying 112 non-trivial communities in cellular-level data. 113

Our analysis consisted of two components. First, using identical methods as in the main text, we constructed a morphospace of community interactions (Fig. 1). This figure demonstrates that when we use  $Q_{max}$  to uncover communities and vary the number of communities from K = 2 to K = 10, communities are *always* arranged in assortative motifs. Using the WSBM, on the other hand, we consistently identify both core-periphery and disassortative motifs.

As a second comparison of  $Q_{max}$  and the WSBM applied to C. elegans connectome data, we identified 119 representative partitions for each technique as we varied the number of communities from K = 2120 to K = 10. We then reordered and blocked the C. elegans connectivity matrix according to the 121 communities uncovered by the WSBM (Fig. 2A). In the margins of each plot, we color-coded each 122 123 node's corresponding community label as detected using  $Q_{max}$ . Had the two techniques generated similar community partitions, then we would expect the  $Q_{max}$  labels to be homogeneous within each 124 block. However,  $Q_{max}$  community labels are heterogeneously distributed within WSBM communities, 125 demonstrating qualitatively that the two techniques uncover communities of different character. 126

In addition, for the representative WSBM communities, we also show the density (average weight of all possibile connections) of each block (Fig. 2B). While certain pairs of communities are configured in assortative relationships, many are not. These results suggest that the WSBM identifies non-assortative communities in the *C. elegans* connectome. Seeing this structure at the cellular scale in a fully-mapped connectome further supports the conclusions of our manuscript."

### 132 Comment 2

On a somewhat related note, the addition of other species, where we have better measurements of edges, is 133 a strength of this manuscript. However, the main text is limited to general "and results are similar in other 134 species" statements. This is 1) not fully accurate, since in reading the supplementary materials there are 135 nuanced differences that may be important; and 2) reduces the strength of your argument. As of now, that 136 data is a supplemental side note, but mentioned in the title, abstract and discussion as if it were a main part 137 of the paper as well. If possible, I would add results from the other datasets into the main text. If you do 138 not have space, I would make it more clear that the non-human datasets are not equal to the human dataset 139 in terms of explanation in the paper, which would mean taking non-human out of the title and other parts 140 of the manuscript that imply that you considered all equally. 141

We agree and thank the reviewer for noting this. As mentioned earlier, the main text now focuses more clearly on the human dataset. Our rationale for not acknowledging the nuanced differences between human and non-human datasets was that while the non-human datasets added breadth to our submission by representing alternative and arguably higher fidelity connectome reconstruction techniques, they also suffered from certain peculiarities, e.g. the macaque connectome is incomplete (full connection information on 29 of 91 regions) while the mouse and rat data represent single hemispheres. In any case, we now explicitly note the differences between non-human and human connectome datasets.

<sup>149</sup> In the section, **Connectomes support diverse meso-scale architecture**, we now write:

### Ordered by WSBM communites



Figure 2: *C. elegans* connectivity matrix reordered by community assignments. (A) Each panel in the top row depicts the same connectivity matrix of chemical synapses among N = 279 neurons of the nematode *C. elegans*. Edge weights represent the number of synapses and are indicated by both the color and the size of each edge. The rows and columns of each matrix are ordered according to WSBM community assignments. Along both the x- and y-axes are colored plots. The color of each row and column represents the  $Q_{max}$  community assignment of the corresponding neuron. Note: in general, the  $Q_{max}$  assignments are heterogeneously distributed across WSBM communities, suggesting an inexact correspondence. (B) Panels in the bottom row depict the connection weight density of the blocks defined by the WSBM community assignments. Note that in general, connection density is not strongest along the diagonal, which would indicate assortative communities. Instead, the density of off-diagonal blocks is sometimes greater than that of the diagonal blocks, which indicates the presence of non-assortative communities.

- "While these results were, overall, consistent in the non-human connectome datasets, there were 150 nonetheless some differences (Fig. S5). For example, in the mouse dataset the relationship between 151 node degree and change in regional assortativity was practically non-existent. The source of this vari-152 ation is unclear, though it is important to note that, while the non-human datasets are reconstructed 153 using what are arguably higher-fidelity techniques, e.g. tract tracing, they nonetheless suffer from 154 pecularities, notably incompleteness. The macaque connectome includes connection data on only 29 155 of 91 brain areas while the mouse and rat data include only a single hemisphere. For this reason, it is 156 difficult to ascertain whether differences in connectome meso-scale structure across species arises due 157 to genuine architectural differences or whether complete connectivity information would improve the 158 consistency of results." 159
- <sup>160</sup> We also address this issue in the section Many (but not all) communities are assortative:

• "As in the previous section, while we find similar results in non-human connectome datasets, we also note some differences (Fig. S4). For instance, the *Drosophila* dataset is unique in that the relationship between node strength and the probability of being assigned to the maximally assortative set exhibits a u-shaped curve (Fig. S4F). The macaque dataset exhibits a similarly-shaped curve, and possibly as a
 consequence of where we drew the cutoff for rich club assignment or the incompleteness of the macaque
 connectome, rich club nodes are actually more likely to be assigned to the maximally assortative set
 than to non-rich club nodes (Fig. S4O)."

<sup>168</sup> Finally, in the section **Community morphospace reveals rules for between-community interactions**:

• "Again, these findings were largely replicated in non-human connectome data, though the relative proportions of motif types was variable (Fig. S6). While the incompleteness of the non-human connectome datasets make cross-species comparisions difficult, these differences raise the prospect that the

meso-scale structure of different organisms features nuanced, organism-specific motifs."

# 173 Comment 3

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Your last paragraph of the "Connectomes support diverse meso-scale architecture" Results section seems to 174 be a bit strong of a conclusion given the analyses you conducted. You compared assortativity between Qmax 175 and WSBM methods, and should expect assortativity to be lower in the WSBM method based on its algorithm 176 versus that of Qmax, as you wrote earlier in that section. So this is more of a validation that the different 177 algorithms are doing what you think they are than that the differences are functionally meaningful. Adding 178 other network metrics that are thought to be important for cognition and comparing their values across 179 algorithms would make that conclusion more appropriate ... or not making that claim until you relate these 180 two community structures to cognition or other metrics below. 181

We agree with the reviewer that the results presented in the section **Connectomes support diverse** meso-scale architecture offer no evidence that one method is better or worse than the other. The aim of that section was to show that the WSBM detects communities whose character was fundamentally *different* than those detected using  $Q_{max}$  (not necessarily better or worse). Specifically, whereas  $Q_{max}$  communities are highly assortative and segregated, the WSBM detects communities that are more integrated thanks to many cross-community links. We have softened the tone of this paragraph to more accurately reflect the content of this section.

We note, however, that elsewhere in the **Results** section we leverage well-established methods and present 189 objective, quantifiable evidence documenting that the WSBM outperforms  $Q_{max}$ . Specifically, we show that 190 WSBM communities in the human and mouse connectomes partition functional connectivity and gene co-191 expression networks into segregated modules (we discuss this later in our response to the reviewer). We 192 also derive a region-level diversity index and show that this index is predictive of subjects' performances on 193 cognitive tasks. Importantly, when communities are assortative (as they are when detected using  $Q_{max}$ ). 194 the diversity index of every brain region has a value of zero and the index is no longer informative. So while 195 we agree that the current section does not constitute evidence of superiority, the main findings of the paper 196 support the hypothesis that non-assortative community structure out-performs assortative communities along 197 neuroscientifically relevant dimensions. 198

<sup>199</sup> We have revised the opening paragraph of this section accordingly:

"The brain's meso-scale structure is generally assumed to be uniformly assortative (i.e., communities are segregated from one another), a feature thought to support specialized information processing [17]. The WSBM challenges this view, detecting less assortative (and hence increasingly integrated) communities, suggesting that communities might play a more diverse range of functional roles. Demonstrating this empirically, however, remains a challenge."

We are also intrigued by the reviewer's suggestion to test whether other network measures that have been shown to correlate with behavioral measures also vary with community detection technique. Of course, it is important to note that irrespective of the technique we use, the underlying network is fundamentally the same, so any metrics we compare must be sensitive to changes in detected communities. One possibility is the participation coefficient [18], which measures the extent to which a node's links are concentrated within its own community versus distributed evenly over other communities. Accordingly, we compared partitions detected using both methods,  $Q_{max}$  and WSBM, in terms of their participation coefficient.

First, we separated partitions by number of communities, k = 2, ..., 10. Then, for each k we calculated the mean regional participation coefficient. We repeated this analysis for each method separately. To compare the two techniques, we computed the Pearson correlation coefficient between the two  $N \times 1$  vectors of mean regional participation coefficients. When k was small (k = 2 and k = 3), we found that the correlation was weak (Fig. 3). As k increased, however, the correlation also increased in magnitude. To some extent, this is to be expected. In the limiting case when k = N (each node is in its own community), the algorithms converge to the same result. However, over the range k = 2, ..., 10, the correlation between regional participation coefficient values is similar.



Participation coefficient, WSBM

Figure 3: Regional participation coefficient for WSBM and  $Q_{max}$  averaged across partitions. Each panel depicts the mean regional participation coefficients for brain regions estimated from partitions detected using either the WSBM (x-axis) or  $Q_{max}$  (y-axis).

The previous analysis would seem to suggest that both techniques result in similar intuitions about 220 nodes' roles in the network. However, this is not true. A participation coefficient close to 1 means that a 221 node's connections are distributed almost evenly across communities, while a value close to 0 means that 222 its connections are concentrated within own community. Therefore, we can calculate the mean participation 223 coefficient over all brain regions to assess whether connections tend to fall within or between communities. 224 When we perform this analysis, we see that the WSBM results in much greater average participation than 225  $Q_{max}$  (maximum  $p < 10^{-97}$  over all k) indicating that while both techniques identify similar high and low 226 participation brain regions, those values are consistently greater with the WSBM (Fig. 4). This means that 227 connections tend to cross the boundaries of communities, which aligns exactly with the results we reported 228 in the main text. 229



Figure 4: Boxplots of participation coefficient for WSBM and  $Q_{max}$  averaged across brain regions. For a given number of communities, k, the WSBM consistently results in higher participation coefficients than  $Q_{max}$ .

### 230 Comment 4

Similarly, your first paragraph of the "Functional relevance of the WSBM" section "To this point, we 231 have used the WSBM to demonstrate that connectomes exhibit diverse, non-assortative meso-scale struc-232 ture...suggesting that the richer, non-assortative communities are closer to the brains canonical architecture." 233 seems like a straw man, since the algorithm that allows for non-assortative meso-scale structure finds some 234 non-assortative communities, while the algorithm that limits its results to maximizing assortativity finds all 235 assortative communities. This argument (that is scattered throughout the manuscript) needs an explanation 236 regarding why maximizing assortativity to the exclusion of other types of communities is not as biologically 237 plausible as allowing multiple types of community structure. There have been many papers arguing why algo-238 rithms maximizing modularity are biologically plausible. This concept that we are limiting our investigations 239 by doing so is very compelling, but it needs more biological motivation (as well as functional relevance ... see 240 other comments about that below) to have a strong impact on the field. 241

We agree with the reviewer that the opening paragraph of this section is a bit strong. We have revised it to read:

### • "To this point, we have used the WSBM to characterize the meso-scale structure of human and nonhuman connectomes. Using this method, we find a diverse meso-scale structure that includes nonassortative communities."

The reviewer's second point – why might we expect a neural system to have non-assortative communities? 247 - is a critical one. The hypothesis that we posit in the introduction can be summarized as follows. Assortative 248 meso-scale structure is beneficial for networks whose sub-systems are intended to function in isolation and 249 autonomously from one another. If the brain is organized into strictly assortative communities it suggests 250 that all communities are used in this same way, namely to carry out specialized information processing. On 251 the other hand, we think that the integration of information from many systems is a critical component of 252 higher-order cognitive processes, mentalizing, and planning [19]. In order to accomplish this, communities 253 need to interact with one another. That is, the brain's meso-scale must deviate (even if only slightly) from 254 the strictly assortative model that  $Q_{max}$  imposes upon it. Following this reasoning, we hypothesized that 255 non-assortative interactions among communities help the brain to support complex cognitive processes. 256

The reviewer is also correct that the network neuroscience literature lacks a balanced discussion of assortative *versus* non-assortative communities. Though we can only speculate on why this is the case, one likely contributor is the fact that modularity maximization and infomap algorithms are fast, easily implemented, and already pervasive throughout network neuroscience research. These factors could effectively reinforce the assumption that brain communities "should" or "must" be assortative, spurring further empirical and theoretical research on that type of meso-scale structure.

Nonetheless, there are many compelling theoretical and empirical findings suggesting that non-assortative

communities confer advantages to neural systems and represent more accurate models of their network 264 organization. The mammalian visual system for instance, exhibits feed-forward like structure (a chain-like, 265 non-assortative topology) as it encodes progressively more abstract details of visual information. This type 266 of organization is evident at the inter-areal level [20] but also at the microscale, where retinal neurons are 267 wired according to cell-specific, distance-dependent, and function-driven rules [21, 22]. Elsewhere, analysis of 268 C. elegans' meso-scale structure using mixture models (a relative of the stochastic blockmodel) revealed non-269 assortative communities, including a "rich" community composed of highly-connected inter-neurons known to 270 play critical roles in mechanosensation and locomotion, highlighting the community's apparent role in control 271 of behavior [9]. Similarly, the inter-areal neurochemical rat connectome exhibits core-periphery organization, 272 where the core is composed of seratonergic structures associated with sleep-wake cycles, arousal, and stress, 273 suggesting a "pacemaker"-like role for the core [23]. This same kind of organization has been observed in 274 mouse and macaque connectomes, where the cores are dominated by associative areas, again suggesting that 275 cores and non-assortative structures play pivotal roles in integrative neural processes [24]. 276

These same studies [23, 24] also demonstrated that the core-periphery organization is compatible with an exponential distance rule, in which the connection strength decreases with length [25]. Concurrently, a recent modeling study of human connectome data suggested the existence of a non-assortative "geometric core" composed of brain regions that emerges naturally under wiring cost constraints [26]. Collectively these findings suggests that, like networks with assortative communities, core-periphery organization can be embedded efficiently in three-dimensional space so as to reduce the network's total cost of wiring.

Lastly, while we claim that modularity maximization precludes the possibility of detecting non-assortative 283 communities, we make no claim that the brain exhibits *strictly* non-assortative communities. We devote a 284 full subsection to this topic: Many (but not all) communities are assortative. In the human connec-285 tome, in fact, we find both assortative and core-periphery community motifs, but very few disassortative 286 (bipartite) interactions. So while modularity maximization might miss out on some of the richness of the 287 288 brain's community structure, it is possible that communities detected with the WSBM might retain many of the functional and evolutionary advantages associated with assortative communities (e.g. efficient spa-289 tial embedding, robustness to perturbations, etc.), while non-assortative communities increase the network's 290 diversity and confer additional functionality to the network. 291

We have revised the manuscript to reflect the above statements. In the introduction, we restate our hypotheses more clearly and in the discussion we include a paraphrased version of the above paragraphs.

"Secondly, this view implies that the connectome's meso-scale structure is rigidly uni-functional. That
is, networks with assortative communities are well-poised for specialized, segregated information processing, but are not suited for integrative function. Higher order cognitive processes, for example, are
thought to emerge through integration of information originating in different brain systems [19], which
can only occur via the interaction of communities with one another. We hypothesize, then, that in order to produce complex thought and adaptive behavior, the brain's underlying meso-scale architecture
must deviate (even if only slightly) from the strictly assortative model."

"These findings build upon and extend other recent studies reporting non-assortative structure in 301 connectome data. The mammalian visual system for instance, exhibits feed-forward like structure (a 302 chain-like, non-assortative topology) at both the inter-areal level [20] and at the microscale [21, 22]. A 303 previous analysis of C. elegans' meso-scale structure using mixture models (a relative of the stochas-304 tic blockmodel) revealed a core-like community composed of highly-connected inter-neurons known to 305 play critical roles in mechanosensation and locomotion, highlighting its apparent role in the control of 306 behavior [9]. Similarly, the inter-areal mouse, rat, and macaque connectomes exhibit core-periphery 307 organization, where the core is composed of associative brain areas and proposed to act as a "pace-308 maker" [24, 23]. Moreover, this type of architecture is consistent with wiring-cost reduction models. 309 suggesting that core-periphery structure, like assortative communities, can be efficiently embedded in 310 three-dimensional space [25]." 311

# 312 Comment 5

You state later in that section that "Intuitively, functionally-related brain regions are linked by strong func-

density of functional connections should be greater than the between-community density." But the point of 315 the manuscript is that assuming communities have this strong-within and weak-between connectivity is not 316 necessarily correct, and we should allow for other types of communities (Figure 1). That sentence seems to 317 contradict the main point of the manuscript. It is very possible that I am missing something, but regardless 318 that concept should be clarified so as to not seem contradictory if it isnt. Further, the result that follows 319 appears to show that even with WSBM, when averaging across the whole brain, communities are assortative 320 (strong within, weaker between). It is also unclear to me how both within and between-community connections 321 can be more dense if the nodes and edges are matched across algorithms, so more explanation about that is 322 needed as well. 323

We agree with the reviewer that, as written, our previous explanation for why we expect the withincommunity density of *functional connections* to be greater than between-community density (even if communities are non-assortative) was only weakly justified. We take this opportunity to detail our rationale.



Figure 5: **Matching index.** We show two example adjacency matrices: one for a bipartite network and another with assortative communities. We compute the matching index for all pairs of nodes to show that both networks, despite their vastly different connectivity patterns, result in similar patterns of matching index.

In past work when empirical estimates of FC could not be easily obtained, the similarity of brain region's 327 structural connectivity profiles (as measured by the "matching index") was treated as a measure of their 328 functional connectedness [27, 28, 29]. Importantly, the matching index can be strong between disconnected 329 regions, so long as their inputs and outputs are similar. This implies that even bipartite communities with 330 no internal structural connections will have strong within-community matching. We demonstrate this using 331 two toy networks: one with bipartite communities and the other with assortative communities (Fig. 10). The 332 point of this demonstration is to show that there is both an historical and structural rationale for expecting 333 high levels of within-community FC in both assortative as well as non-assortative communities. 334

Though via different mechanisms, both the WSBM and  $Q_{max}$  produce communities composed of brain regions with similar patterns of incoming and outgoing connections. In the case of  $Q_{max}$ , this similarity is entirely incidental – nodes get grouped into internally dense, mutually-connected clusters, inflating their similarity. The WSBM, on the other hand, explicitly defines communities as clusters of nodes whose connections were generated by the same statistical process; by definition pairs of nodes in the same community
 will have similar connectivity patterns even if they, themselves, are not directly connected.

Because the similarity of regions' structural connectivity is associated with strong functional connectivity. 341 we expect that two nodes in the same community should be more strongly functionally connected to one 342 another than two nodes in different communities, irrespective of which technique was used to define the 343 communities. However, the WSBM and  $Q_{max}$  represent vastly different hypotheses about how brain networks 344 function. A strictly assortative brain is aligned with the hypothesis that the brain is composed of communities 345 operating independently, while a brain that allows for some non-assortative communities implies that brain 346 function arises not solely from contributions of independent communities, but from the interactions between 347 communities. 348

We can compare these two hypotheses of brain function with cross-validation methods using empirical 349 functional connectivity as metadata [30, 31]. We reasoned that if functional connectivity emerges from 350 interactions among brain regions in independent, autonomous clusters, then its organization will be closely 351 aligned to the communities detected using  $Q_{max}$ . On the other hand, if functional connectivity is the 352 result of non-assortative, integrated clusters, then the WSBM communities will more closely resemble the 353 brain's functional connectivity. To compare communities with functional connectivity, we classified every 354 functional connection as "within-community" or "between-community". We calculated the mean weight of 355 all connections assigned to each class and finally the difference between those values. This measure – the 356 difference between mean within- and between-community functional connections – serves as a measure with 357 which we can evaluate the performance of the two algorithms. 358

We have added the following text to the section **Functional relevance of the WSBM** to better reflect our assumptions and hypotheses:

• "It is generally agreed upon that brain structural connectivity determines the partners that any given 361 region can "talk to", and therefore constrains communication patterns among brain regions, shaping 362 the correlation pattern of ongoing neural activity, i.e. functional network organization. We reasoned 363 that if two brain regions receive input from the same set of brain regions and deliver output to the 364 same set of regions, then their activity over time should be correlated, i.e. those regions would appear 365 functionally connected to one another. This set of assumptions has a long tradition in the network 366 neuroscience community. In the past when empirical estimates of FC could not be easily obtained, 367 measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been 368 used as a stand-in [27, 28, 29]. 369

Though via different mechanisms, both the WSBM and  $Q_{max}$  produce communities composed of brain regions with similar patterns of incoming and outgoing connections. In the case of  $Q_{max}$ , this similarity is entirely incidental – nodes get grouped into internally dense, mutually-connected clusters, inflating their similarity. The WSBM, on the other hand, explicitly defines communities as clusters of nodes whose connections were generated by the same statistical process; by definition pairs of nodes in the same community will have similar connectivity patterns even if they, themselves, are not directly connected.

Because the similarity of regions' structural connectivity is associated with strong functional connectiv-377 ity, we expect that two nodes in the same community should be more strongly functionally connected 378 to one another than two nodes in different communities, irrespective of which technique was used to 379 define the communities. However, the WSBM and  $Q_{max}$  represent vastly different hypotheses about 380 how brain networks function. A strictly assortative brain is aligned with the hypothesis that the 381 brain is composed of communities operating independently, while a brain that allows for some non-382 assortative communities implies that brain function arises not solely from contributions of independent 383 communities, but from the interactions between communities. 384

We can compare these two hypotheses of brain function with cross-validation methods using empirical functional connectivity as metadata [30, 31]. We reasoned that if functional connectivity emerges from interactions among brain regions in independent, autonomous clusters, then its organization will be closely aligned to the communities detected using  $Q_{max}$ . On the other hand, if functional connectivity is the result of non-assortative, integrated clusters, then the WSBM communities will more closely resemble the brain's functional connectivity. To compare communities with functional connectivity, we classified every functional connection as "within-community" or "between-community". We calculated
 the mean weight of all connections assigned to each class and finally the difference between those values.
 This measure – the difference between mean within- and between-community functional connections –

serves as a measure with which we can evaluate the performance of the two algorithms."

# 395 Comment 6

<sup>396</sup> "Community morphospace reveals rules for between-community interactions": how do the previously-described <sup>397</sup> results offer "a better explanation for human brain function and mouse genetic expression than that provided <sup>398</sup> by assortative communities alone"? Thus far, I am convinced that it is "different", but have seen no evidence <sup>399</sup> that it is "better".

This is an important point. In general, it is difficult to demonstrate conclusively that one community detection method is objectively better than another and, of course such a demonstration depends on how one defines "better". However, cross-validation through meta-data represents a powerful technique for objectively and quantitatively comparing different methods [30, 31]. By drawing on domain-specific knowledge of how the structure and function of neural systems are related to one another, we formed hypotheses and designed objective functions that, when evaluated for both the WSBM and  $Q_{max}$ , clearly favored the WSBM over  $Q_{max}$ . In the text, we have also explicitly defined what we mean when we use the term "better".

407 We have now edited the main text to better emphasize these points.

• "We can compare these two hypotheses of brain function with cross-validation methods using empirical 408 functional connectivity as metadata [30, 31]. We reasoned that if functional connectivity emerges from 409 interactions among brain regions in independent, autonomous clusters, then its organization will be 410 closely aligned to the communities detected using  $Q_{max}$ . On the other hand, if functional connectivity 411 is the result of non-assortative, integrated clusters, then the WSBM communities will more closely 412 resemble the brain's functional connectivity. To compare communities with functional connectivity, we 413 classified every functional connection as "within-community" or "between-community". We calculated 414 the mean weight of all connections assigned to each class and finally the difference between those values. 415 This measure – the difference between mean within- and between-community functional connections -416 serves as a measure with which we can evaluate the performance of the two algorithms." 417

# 418 Comment 7

Also in that section, your description of the results is that the WSBM algorithm identifies a significant number of core-periphery interactions (which I see in Figure 6) and disassortative interactions (which I do not see). It looks to me that the proportion of disassortative interactions using WSBM, and the difference between WSBM and Qmax, are both 0. Please clarify in the text and the figure what you mean by this.

We thank the reviewer for bringing this to our attention. Overall, the WSBM uncovers many more assortative and core-periphery motifs than disassortative motifs. In fact, from K = 2 to K = 4 it uncovers exclusively assortative and core-periphery motifs. From K = 5 to K = 10 the relative proportion of disassortative motifs is always less than 2%, and in Figure 6, amounts to exactly 0.2%. In that figure, there are a small number of red points (representing the disassortative motifs), but they are difficult to see because of the large number of yellow and cyan points and because of the beige background. In the revised manuscript, we have changed the opacity of the red points to make them more visible (Fig. 6).

# 430 Comment 8

Your brain figures exclude subcortical brain regions, yet they keep popping up in the article as diverse and one of the groups of regions that would be better defined using WSBM. Please add images of the subcortical structures as well (this goes for all figures that show where in the brain different node types are).

We agree with the reviewer that this is a useful visualization. We now depict sub-cortical structures alongside the surface plots.



Figure 6: A rich community morphospace. (A) A community motif is constructed as the average over blocks of the connectivity matrix. Here, we show blocks within and between two communities, labeled r and s. (B) Given withinand between-community connection densities, it is possible to classify each pair of communities into one of three motifs: assortative, disassortative, or core-periphery. (C,D) All pairs of communities placed in a network morphospace and colored by their motif type. Note: axes are log-scaled. (E) The relative proportion of each motif type as a function of the number of detected communities, K, for  $Q_{max}$ (*left*), the WSBM (*middle*), and their difference (*right*).

## 436 Comment 9

Behavioral relevance section: it would be interesting to do this analysis using Qmax to define community
 structure as well, to determine which of the two algorithms best explains behavior. If WSBM is more related

to behavior on these cognitive control tasks, that is an argument for the functional relevance (and potentially

440 higher accuracy) of community structure derived from that algorithm.

We agree that, in principle, this would be interesting and make for a more compelling comparison. However, because the  $Q_{max}$  algorithm uncovers only assortative community interaction motifs, the diversity of every region (measured as an entropy) is zero. We now note this in the main text at the end of the section **Community motifs identify a class of diversely connected nodes**:

• "Note that because  $Q_{max}$  uncovers only assortative community motifs, each brain region's diversity score is effectively zero. Accordingly, we never assessed the distribution of diversity scores for the  $Q_{max}$ partitions over functional systems."

### 448 Comment 10

In your first sentence of the discussion, while I dont disagree that having different types of communities
is plausible, I have not seen a strong argument for that other than that an algorithm that attempts to find
these different types of communities can. This to me is no less biased than modularity maximization being
biased to find an assortative community structure. This argument should be made more explicit and linked
to biology throughout the manuscript to support your conclusions.

The last full sentence on page 12 is the first I have seen that gives a biological reason for looking for non-assortative community structure. If this and other related arguments are highlighted more in both the introduction and discussion, this paper will be more convincing.

These two comments deal with the same concern (which was also raised in the reviewer's **Comment 4**) and so we respond to them with a single, cohesive reply. In addition to more fully fleshing out the sentence <sup>459</sup> on page 12 that the reviewer refers to, we now include a lengthier explanation of other studies that have <sup>460</sup> found some evidence of non-assortative structure in connectome datasets.

• "These findings build upon and extend other recent studies reporting non-assortative structure in 461 connectome data. The mammalian visual system for instance, exhibits feed-forward like structure 462 (a chain-like, non-assortative topology) at both the inter-areal level [20] but also at the microscale 463 [21, 22]. A previous analysis of C. elegans' meso-scale structure using mixture models (a relative 464 of the stochastic blockmodel) revealed a core-like community composed of highly-connected inter-465 neurons known to play critical roles in mechanosensation and locomotion, highlighting its apparent 466 role in the control of behavior [9]. Similarly, the inter-areal mouse, rat, and macaque connectomes 467 exhibit core-periphery organization, where the core is composed of associative brain areas and proposed 468 to act as a "pacemaker" [24, 23]. Moreover, this type of architecture is consistent with wiring-cost 469 reduction models, implying that core-periphery structure, like assortative communities, can be efficiently 470 embedded in three-dimensional space [25]." 471

# 472 Comment 11

Your sentence: "Moreover, communities detected using the weighted stochastic blockmodel better recapitulated 473 observed intrinsic functional relationships among brain regions in the human, and relationships between 474 gene co-expression patterns in the mouse, compared to more commonly-used techniques such as modularity 475 maximization." See my point above about this results section. This argument does not logically follow to me. 476 This sentence was intended to be a summary of the metadata cross-validation of the communities. In 477 that analysis we showed that compared to  $Q_{max}$ , WSBM communities were enriched for strong functional 478 connections and correlated patterns of gene expression in human and mouse, respectively. In line with our 479 reply to the reviewer's **Comment 6**, we have revised this sentence to better clarify its intended meaning. 480

• "Moreover, by cross-validating communities using metadata (a technique that has been employed elsewhere [30, 31]), we showed that meso-scale structure uncovered by the WSBM was more closely aligned with functional connectivity compared to  $Q_{max}$ ."

As we noted in our reply to **Comment 4**, we also include a longer description explaining why the cross-validation is an appropriate method for objectively comparing the WSBM with  $Q_{max}$ :

• "It is generally agreed upon that brain structural connectivity determines the partners that any given 486 487 region can "talk to", and therefore constrains communication patterns among brain regions, shaping the correlation pattern of ongoing neural activity, i.e. functional network organization. We reasoned 488 that if two brain regions receive input from the same set of brain regions and deliver output to the 489 same set of regions, then their activity over time should be correlated, i.e. those regions would appear 490 functionally connected to one another. This set of assumptions has a long tradition in the network 491 neuroscience community. In the past when empirical estimates of FC could not be easily obtained, 492 measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been 493 used as a stand-in [27, 28, 29]. 494

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities of brain 495 regions with similar patterns of connections. However, these methods differ in that communities 496 are defined according to two vastly different topological principles.  $Q_{max}$  assumes that the brain's 497 meso-scale organization is based on assortative and segregated sub-systems, while the WSBM allows 498 communities to be both assortative and non-assortative. These differences in meso-scale structure 499 imply differences in brain function. A strictly assortative brain is aligned with the hypothesis that 500 the brain is composed of communities operating nearly autonomously, while a brain composed of some 501 non-assortative communities implies that brain function arises not from independent communities, but 502 from the interactions between communities. 503

Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions using empirical FC as metadata (See **Materials and Methods** for more details on FC reconstruction from BOLD signals). This approach – cross-validation through metadata – is well-established and has

been used extensively in past studies [31, 30]. In essence, it assumes that metadata better represents 507 some aspect of a network's ground truth organization than its structural topology alone. Community 508 detection methods that are more closely aligned with the metadata may be more sensitive to the 509 network's ground truth organization and are considered, in this quantitative and objective sense, 510 superior to those that do not. We reasoned that if the brain's correlated activity pattern is better 511 described by assortative communities behaving autonomously, then the FC network will be more closely 512 aligned with  $Q_{max}$  communities. On the other hand, if the correlation pattern is better described by 513 interacting, non-assortative communities, the alignment of FC to WSBM communities will be greater. 514 Here, we quantify this alignment as the mean weight of within-community functional connections minus 515 the mean weight of between-community functional connections." 516

• "We note that the use of a Pearson correlation as a measure of FC results in increased transitivity (if a strong correlation exists between nodes A and B as well as B and C, then A and C will tend to be

strongly correlated), which can reinforce block structure in correlation matrices [32]."

# 520 Reviewer #2

<sup>521</sup> "Diversity of meso-scale architecture" by Betzel et al. compares two forms of community decompositions <sup>522</sup> applied to structural connectomic data a classic decomposition that maximises the assortativity (Qmax) of <sup>523</sup> the decomposition with a more recently developed weighted stochastic block algorithm (WSBM). The WSBM <sup>524</sup> appears to group nodes into modules such that the likelihood of inter-module connections is approximately <sup>525</sup> even for all nodes within each module (i.e. does not depend upon heavily upon each individual module). There <sup>526</sup> is substantial interesting material in this manuscript which is clearly written and nicely illustrated.

527 We thank the reviewer for the kind comments.

# 528 Comment 1

One of the major findings is not really that surprising and I think more work is required to establish the 529 significance of the finding. Namely, it is not surprising that any decomposition that does not maximise the 530 assortativity of a module decomposition is less assortative than one that does! i.e. there is an element of 531 circularity in the central finding of the paper. The question that seems not to be answered is not whether 532 the WSBM decomposition reveals a less assortative community structure than Qmax, but whether the degree 533 of core-periphery and disassortativity in the human connectome is greater or lesser than expected by chance: 534 Since we already know that Qmax-sorted connectomes are more assortative than degree and strength preserv-535 ing random surrogates, we should now check whether WSBM ones are likewise more core-periphery or more 536 disassortative than strength-sequence matched surrogates. Are they likewise more or less arranged when such 537 surrogates also account for the geometric embedding of real connectomes into three dimensions? Only after 538 this has been established, do I think the more fine-grained analyses of figure 3-5 make sense. 539

We thank the reviewer for these comments and for the opportunity to clarify our aims. The reviewer brings up two points – one related to the central question of the paper "does the brain have strictly assortative communities and can we find them?" and a second question related to structural null models. We address these two separately, starting with the question on null models.

We agree that applying the WSBMs to some variation of a randomly rewired network would serve as an 544 important control, and that a strength-preserving null model is a good place to start. In general, randomly 545 rewiring a network will decrease the frequency of triangle motifs – nodes a, b, and c that are mutually 546 connected. These sorts of triangles inflate a network's clustering coefficient, "fill out" modules, and lead to 547 the formation of assortative communities. Accordingly, if we rewire a network and destroy its triangles, we 548 would actually expect a decrease in assortative communities. Accordingly, we expect an increase in non-549 assortative communities as a result of rewiring. We confirm this hypothesis using two separate tests (and 550 in the process, we show that observed networks have different community statistics than randomly-rewired 551 networks). 552

First, we generated 100 rewired networks (for the human network) in which we preserved degree sequence exactly but allowed strength sequence to vary [33]. Then, using a simulated annealing algorithm, we shuffled edge weights until the node strength sequence was almost exactly preserved (in general, it is not possible to preserve a precise set of edge weights and the strength sequence exactly). Over the 100 realizations, the average correlation of the empirical network's strength sequence with those of the rewired networks was  $r = 0.999994 \pm 0.000002$ , suggesting excellent correspondence. We then used the WSBM to cluster each of the 100 networks, repeating the optimization 10 times for each K of the range K = 2 to K = 10 (we used 10 optimizations in place of the 250 in the main text to reduce total runtime).



Figure 7: Summary of strength-preserving null models. (A) Scatterplot showing strong correlation of observed and randomized strength sequences. (B) Mean connectivity matrix obtained by averaging over all 100 realizations of the null model.

As a first comparison, we calculated community assortativity as a function of community size (Fig. 8). 561 The assortativity scores are computed using partitions detected based on rewired networks. The construction 562 of this figure is identical to Figure 2B in the main text. For ease of interpretation, we only plotted the mean 563 community assortativity curves. As expected, applying the WSBM to randomly rewired networks resulted 564 in communities that were less assortative than when applied to the observed network, and far less assortative 565 than those detected when  $Q_{max}$  was applied to the observed network. This demonstrates that communities 566 detected using both the WSBM and  $Q_{max}$  are distinct from one another and also differ from randomly 567 rewired networks. 568

As a second comparison, we computed the morphospace of community interaction motifs based on com-569 munities detected in the rewired networks. As in the main text, this involved generating for each network 570 and partition a set of community interaction motifs and classifying them as either "core-periphery", "assor-571 tative", or "disassortative" (Fig. 9A). We then calculate the proportion of each motif type as a function of 572 the number of communities. We show these proportions for the rewired networks (Fig. 9B), the observed 573 network (Fig. 9C), and the difference between the two (Fig. 9D). As expected, the rewired networks exhib-574 ited far fewer assortative motifs than the observed network and far more core-periphery and disassortative 575 motifs. 576

These additional analyses demonstrate that observed brain networks exhibit different community statis-577 tics compared to rewired brain networks. These findings inform the results in the main text. The application 578 of the WSBM to brain networks results in less assortative communities than if  $Q_{max}$  had been used to detect 579 communities. This level of disassortativity, however, is not as severe as that observed in random networks, 580 suggesting that the observed brain networks, in fact, maintain an unexpected level of assortative commu-581 nities. This is an important point, as the functional and evolutionary advantages of assortative community 582 structure have been well-documented [17], indicating that brains may balance these advantages with other 583 additional advantages conferred by possessing a small proportion of non-assortative communities. 584

The results of these analyses have now been summarized and added to the **Supplementary Materials** under the subsection entitled **Application of the WSBM to rewired networks**:

587

• "The WSBM is a flexible tool for detecting communities in networks using statistical inference. To



Figure 8: **Community assortativity comparisons.** Mean community assortativity curves as a function of community size for  $Q_{max}$  and the WSBM applied to the observed network and then for the WSBM applied to the strength-preserved null randomized networks.

properly contextualize the results presented in the main text, we applied the blockmodel to randomly-588 rewired networks. Specifically, we compared the observed brain network to networks with precisely 589 the same degree sequence and approximately the same strength sequence. This process entailed first 590 using a standard edge rewiring algorithm to rewire the observed network while preserving its exact 591 degree sequence [33]. However, this procedure does not preserve nodes' strengths. To approximate the 592 observed strength sequence, we randomly swapped the weights of existing edges and, using a simulated 593 annealing algorithm, gradually found configurations of edge weights such that nodes' strengths were 594 minimally different from that of the observed network (Fig. 7A). We repeated the algorithm 100 times, 595 generating 100 realizations of the rewired network (Fig. 7B). 596

We then used the WSBM to uncover the mesoscale structure of each rewired network. We varied the number of communities from k = 2 to k = 10 and repeated the algorithm 10 times. Next, we calculated the assortativity of each detected community based on the connection pattern of the rewired network. We found that in randomly rewired networks, the assortativity of communities detected using the WSBM was far less than that of the observed network. This is because the rewiring procedure tends to reduce the number of triangles and cliques in the network. Because these structures reinforce assortative communities, a reduction in their prevelance corresponds to a reduction in the overall



Figure 9: Community morphospace for strength preserved randomized network. (A) Each point represents a two-community motif classification. (B) and (C) Proportion of community interaction types at different numbers of communities, k = 2 to k = 10, for the randomized and observed networks. (D) The difference in community interaction type proportions.

assortativity of communities (Fig. 8). We traced out the average assortativity of communities as a function of community size and compared the resulting curves using functional data analysis. We found that the assortativity of communities in the observed network was significantly greater than that of the communities detected in the rewired networks ( $p < 10^{-4}$ ).

Next, we submit the rewired networks to a morphospace analysis. As in the main text, this process entailed enumerating and classifying all two-community interaction motifs as "assortative", "coreperiphery", or "disassortative" (Fig. 9A). This process was repeated as we varied the number of communities from k = 2 to k = 10. For each k, we calculated the proportion of motifs within each class (Fig. 9B-D). From this analysis we found that the rewired networks resulted in a decrease in the fraction of assortative motifs. In parallel, this reduction in assortative motifs was accompanied by an increase in core-periphery and disassortative motifs.

These additional analyses demonstrate that observed brain networks exhibit different community statis-615 tics compared to rewired brain networks. These findings inform the results in the main text. The 616 application of the WSBM to brain networks results in less assortative communities than if  $Q_{max}$  had 617 been used to detect communities. This level of disassortativity, however, is not as severe as in ran-618 dom networks, suggesting that the observed brain networks, in fact, maintain an unexpected level of 619 assortative communities. This is an important point, as the functional and evolutionary advantages of 620 assortative community structure have been well-documented [17], indicating that brains may balance 621 these advantages with whatever additional advantages are conferred by possessing a small proportion 622 of non-assortative communities." 623

<sup>624</sup> We also discuss these results and their implications in the main text in the **Discussion** section:

• "Moreover, we also show in the supplementary section Application of the WSBM to rewired networks that the diversity of communities in the observed brain networks is distinct from that of rewired controls." The reviewer also raised a question about the central topic of the paper, namely the existence of nonassortative community structure in brain networks. We take this opportunity to clarify our aims, and to restate and restructure our main arguments.

Our motivation for writing this paper was as follows: Our current view of the brain's meso-scale archi-631 tecture might be biased by heavy use of  $Q_{max}$  and related algorithms. We felt it necessary to present an 632 alternative view of the brain's meso-scale architecture in which we apply a relatively new method (WSBMs. 633 in this case) capable of detecting more general types of communities. We also wanted to, if possible, demon-634 strate the superiority of one method over the other. To this end, we used a well-established cross-validation 635 procedure in which we compared communities to metadata [31, 30]. This approach assumes there exists 636 some form of independent metadata at either the level of network nodes or edges that captures a network's 637 ground-truth organization better than its structural communities, i.e. divisions of the network estimated 638 from its topology alone. In our case, we used human resting state functional connectivity and mouse gene 639 co-expression patterns. We demonstrated that in both cases, communities estimated from the WSBM better 640 matched the organization of these metadata, indicating that not only did WSBM and  $Q_{max}$  communities 641 differ, but along these dimensions the WSBM was objectively better. 642

Reviewer #1 raised a similar point, prompting us to write a better explanation of the cross-validation method, including the underlying assumptions and interpretation of the results. This explanation now appears in the **Results: Functional relevance of the WSBM**:

646

"It is generally agreed upon that brain structural connectivity determines the partners that any given 647 region can "talk to", and therefore constrains communication patterns among brain regions, shaping 648 the correlation pattern of ongoing neural activity, i.e. functional network organization. We reasoned 649 that if two brain regions receive input from the same set of brain regions and deliver output to the 650 same set of regions, then their activity over time should be correlated, i.e. those regions would appear 651 functionally connected to one another. This set of assumptions has a long tradition in the network 652 neuroscience community. In the past when empirical estimates of FC could not be easily obtained. 653 measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been 654 used as a stand-in [27, 28, 29]. 655

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities of brain 656 regions with similar patterns of connections. However, these methods differ in that communities 657 are defined according to two vastly different topological principles.  $Q_{max}$  assumes that the brain's 658 meso-scale organization is based on assortative and segregated sub-systems, while the WSBM allows 659 communities to be both assortative and non-assortative. These differences in meso-scale structure 660 imply differences in brain function. A strictly assortative brain is aligned with the hypothesis that 661 the brain is composed of communities operating nearly autonomously, while a brain composed of some 662 non-assortative communities implies that brain function arises not from independent communities, but 663 from the interactions between communities. 664

Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions 665 using empirical FC as metadata (See Materials and Methods for more details on FC reconstruction 666 from BOLD signals). This approach – cross-validation through metadata – is well-established and has 667 been used extensively in past studies [31, 30]. In essence, it assumes that metadata better represents 668 some aspect of a network's ground truth organization than its structural topology alone. Community 669 detection methods that are more closely aligned with the metadata may be more sensitive to the 670 network's ground truth organization and are considered, in this quantitative and objective sense. 671 superior to those that do not. We reasoned that if the brain's correlated activity pattern is better 672 described by assortative communities behaving autonomously, then the FC network will be more closely 673 aligned with  $Q_{max}$  communities. On the other hand, if the correlation pattern is better described by 674 interacting, non-assortative communities, the alignment of FC to WSBM communities will be greater. 675 Here, we quantify this alignment as the mean weight of within-community functional connections minus 676 the mean weight of between-community connections." 677

## 678 Comment 2

I doubt as presented, many readers will understand what the WSBM actually does do, other than being "not maximally pro-assortative". There is a brief heuristic for the standard block model that seeks to minimise a cost function that penalises the heterogeneity of inter-module connectivity amongst nodes within the same module (that is my reading of equation (1). The WSBM is more complex, but I assume it is a generalisation of the same principle to accommodate edge weights. I think the authors should provide a better heuristic explanation of the WSBM minimization and put it at the beginning of the Results so that the general reader can understand what is being optimized.

We thank the reviewer for this point. We have now included a better intuitive description of the WSBM when we first introduce it to the reader. A longer, more detailed description is included in the methods section.

• "Briefly, the WSBM assumes that a network's nodes can be partitioned into communities and that 689 both the probability of a connection forming between two nodes and the weight of that connection 690 are governed by parameterized generative processes. Importantly, these processes depend only on the 691 communities to which two nodes are assigned. Using the WSBM to uncover a network's community 692 structure involves inferring both the parameters of these processes and nodes' community assignments 693 that maximize the log-evidence that the WSBM generated the observed network. The resulting com-694 munities, therefore, reflect similarities in nodes' connectivity profiles and are not constrained to be 695 assortative." 696

# 697 Comment 3

I also think the paper would be improved with some groundtruth validations, using growth models, to show that the WSBM algorithm does what the authors assume it does namely that Qmax and WSBM should converge if applied to networks that are generated by suitable preferential attachment models, that add new edges to maximize assortativity (the authors are leading experts in such generative modelling); Also that they should strongly diverge when such networks are grown to maximise core-periphery arrangements and for maximally disassortative networks.

Ground truth validations are essential for any new model to ensure that it does what its creators claim it does. As we note in the submission, the WSBM is not an entirely novel method (though its application to connectome data is) and has existed in the literature for several years [34, 35]. We refer the reviewer to these manuscripts, which introduce the WSBM and in which the authors perform extensive validation on synthetic and real-world networks, demonstrating that the WSBM is capable of detecting generalized, blockwise communities (assortative or otherwise) in weighted and directed networks.

# 710 Comment 4

 I found the choice of the statistic for comparing functional and structural connectivity somewhat counterintuitive: Namely of seeing if the corresponding functional networks (when grouped into the corresponding modules) were maximally assortative. Its interesting, although counter-intuitive that WSBM outperforms
 Qmax on this metric. The authors should likely also be cautious that network measures based on linear correlations induce artificial assortativity through the nature of the measure [1].

This concern is similar to Comment 5 from Reviewer #1. We use this opportunity to restate our reasoning for why even non-assortative communities should be internally dense in terms of functional connections.

In past work when empirical estimates of FC could not be easily obtained, the similarity of brain region's 718 structural connectivity profiles (as measured by the "matching index") was treated as a measure of their 719 functional connectedness [27, 28, 29]. Importantly, the matching index can be strong between disconnected 720 regions, so long as their inputs and outputs are similar. This implies that even bipartite communities with 721 no internal structural connections will have strong with-community matching. We demonstrate this using 722 two toy networks: one with bipartite communities and the other with assortative communities (Fig. 10). The 723 point of this demonstration is to show that there is both an historical and structural rationale for expecting 724 high levels of within-community FC in both assortative as well as non-assortative communities. 725



Figure 10: Matching index. We show two example adjacency matrices: one for a bipartite network and another with assortative communities. We compute the matching index for all pairs of nodes to show that both networks, despite their vastly different connectivity patterns, result in similar patterns of matching index.

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities composed of brain regions with similar patterns of incoming and outgoing connections. In the case of  $Q_{max}$ , this similarity is entirely incidental – nodes get grouped into internally dense clusters and as a result they tend to be mutually connected, inflating the similarity of their connectivity profiles. The WSBM, on the other hand, assumes that the connectivity profiles of the nodes that make up a community are generated by the same statistical process and, by definition, should be similar to one another.

Because both methods result in communities composed of nodes with similar connectivity profiles, and 732 because this similarity is associated with strong functional connectivity, we expect that two nodes in the same 733 community should be more strongly functionally connected to one another than two nodes in different com-734 munities. However, both methods also define communities according to two vastly different organizational 735 principles.  $Q_{max}$  assumes that the brain's meso-scale organization is based on assortative and segregated 736 sub-systems while the WSBM assumes that communities can be segregated, but that they can also form 737 cores and peripheries, and sometimes disassortative structures as well. These differences in network orga-738 nization imply differences in brain function, too. A strictly assortative brain is aligned with the hypothesis 739 that the brain is composed of communities operating nearly autonomously, while a brain composed of some 740 non-assortative communities implies that brain function arises not from independent communities, but from 741 the interactions between communities. 742

We can test these two hypotheses of brain organization and function through cross-validation using empirical functional connectivity as metadata. We reason that if the brain's correlated activity pattern is better described by assortative communities behaving autonomously, then the functional network will be more closely aligned with those communities. We measure this alignment as the mean weight of withincommunity functional connections minus the mean weight of between-community connections. We can compute a similar measure to assess the functional network alignment to WSBM communities. We can compare these two measurements to support the claim that one or the other method is better aligned with <sup>750</sup> the brain's functional architecture.

We have added the following text to the section **Functional relevance of the WSBM** to better reflect our assumptions and hypotheses:

• "It is generally agreed upon that brain structural connectivity determines the partners that any given 753 region can "talk to", and therefore constrains communication patterns among brain regions, shaping 754 the correlation pattern of ongoing neural activity, i.e. functional network organization. We reasoned 755 that if two brain regions receive input from the same set of brain regions and deliver output to the 756 same set of regions, then their activity over time should be correlated, i.e. those regions would appear 757 functionally connected to one another. This set of assumptions has a long tradition in the network 758 neuroscience community. In the past when empirical estimates of FC could not be easily obtained, 759 measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been 760 used as a stand-in [27, 28, 29]. 761

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities of brain 762 regions with similar patterns of connections. However, these methods differ in that communities 763 are defined according to two vastly different topological principles.  $Q_{max}$  assumes that the brain's 764 meso-scale organization is based on assortative and segregated sub-systems, while the WSBM allows 765 communities to be both assortative and non-assortative. These differences in meso-scale structure 766 imply differences in brain function. A strictly assortative brain is aligned with the hypothesis that 767 the brain is composed of communities operating nearly autonomously, while a brain composed of some 768 non-assortative communities implies that brain function arises not from independent communities, but 769 from the interactions between communities. 770

Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions 771 using empirical FC as metadata (See Materials and Methods for more details on FC reconstruction 772 from BOLD signals). This approach – cross-validation through metadata – is well-established and has 773 been used extensively in past studies [31, 30]. In essence, it assumes that metadata better represents 774 some aspect of a network's ground truth organization than its structural topology alone. Community 775 detection methods that are more closely aligned with the metadata may be more sensitive to the 776 network's ground truth organization and are considered, in this quantitative and objective sense, 777 superior to those that do not. We reasoned that if the brain's correlated activity pattern is better 778 described by assortative communities behaving autonomously, then the FC network will be more closely 779 aligned with  $Q_{max}$  communities. On the other hand, if the correlation pattern is better described by 780 interacting, non-assortative communities, the alignment of FC to WSBM communities will be greater. 781 Here, we quantify this alignment as the mean weight of within-community functional connections minus 782 the mean weight of between-community connections." 783

• "We note that the use of Pearson correlation as a measure of FC results in increased transitivity (if a strong correlation exists between nodes A and B as well as B and C, then A and C will tend to be strongly correlated), which can reinforce block structure in correlation matrices [32]."

### 787 Comment 5

Novelty: As the authors cite, there is already substantial work using SBMs in human connectomes. A brief summary of what is new here would help. Also, there are elements of the current findings that could be unpacked from prior work: for example, [2] previously showed that rich club nodes preferentially existed as apex nodes in open motifs of 3 nodes (that is maximally disassortative motifs [3]). Also, Figure 10a of [4] shows that very high degree nodes are actually less often inter-connected than by chance i.e. have a "cartel-like" disassortative property. The present finding, by very different methods, seems reassuringly convergent.

This is a good suggestion. Our paper makes several important contributions above and beyond the papers that the author cites and past applications of SBMs to connectome data. Though there are several papers that used variations of the SBM with unweighted structural connectome data from other species, e.g. *C. elegans* [9], and others that have used blockmodels with human functional connectivity networks, e.g. [36, 37, 38, 39, 40], to our knowledge there are no papers that have applied the SBM (weighted or otherwise) to human *structural connectivity* data. For the same reason, we are the first to apply any kind of SBM to macaque, mouse, rat, and *Drosophila* structural connectivity data, as well.

We also make several methodological contributions. For instance, the use of a community morphospace 802 to study interactions among pairs of communities seems to be a potentially profitable way of studying a 803 network's meso-scale structure. Based on the concept of a community motif, we defined a diversity score 804 that we could map back to individual brain regions. The diversity index, at least in human data, corroborated 805 some of our hypotheses. Namely, that it should be greatest in poly-functional, association areas (indeed, we 806 find that control and sub-cortical areas achieve the greatest diversity score). Even more interesting is that 807 intersubject variability in the regional diversity of precisely these same areas is correlated with performance 808 on cognitive control tasks. We show that these areas are neither the most highly- nor the most weakly-809 connected, suggesting possible functional roles for these "middle class" brain areas. Lastly, we find many of 810 the same architectural principles in the non-human datasets. 811

The reviewer points to two important papers linking non-assortative network properties to rich clubs. 812 While those papers represent important contributions to the field of network neuroscience, they nonetheless 813 differ from our submission in at least one important way. Whereas our paper focuses on patterns in the 814 meso-scale structure of neural systems, those two papers focus on properties of individual nodes and edges. 815 Certainly, both scales matter and the fact that they converge to highlight non-assortative structure in brain 816 networks is, indeed, comforting. However, non-assortative community structure is not identical to "open" 817 motifs among nodes. In principle, individual nodes can independently form non-assortative links and edge-818 level motifs. At the meso-scale, however, non-assortative interactions among communities indicates collective 819 and cooperative behavior among groups of nodes. 820

The section **Community and meso-scale connectome analyses** now discusses these issues in greater detail:

"Our study represents one of the first to explore the utility of blockmodels in conjunction with human and animal structural connectome data (though past studies have investigated blockmodels in the context of functional connectivity [36, 37, 38, 39, 40]). Furthermore, we demonstrate the potential benefits of this approach, linking blockmodels to behavior as well as functional connectivity (in the human) and gene co-expression (in the mouse). Future studies may wish to extend these approaches to the study of neurodevelopment [41], or the alteration of connectomic structure in psychiatric disease [42, 43] and neurological disorders [44, 45]".

# 830 Comment 6

I am somewhat (pleasantly) surprised, given the very noisy nature of individual tractography data that I 831 have seen (expect perhaps for carefully reconstructed connectomes from the highly curated human connec-832 tome project) that individual correlations with performance were discovered. Brief details of acquisition and 833 reconstruction must be provided in the Methods here, since this remains a contentious area. What was the 834 connection density? Also, a very brief summary of these data could be given at the beginning of the Results. 835 We apologize for this oversight and now include a more detailed description of the acquisition and recon-836 struction procedures for the human connectome data. Additionally, across subjects, the binary connection 837 density and average node strength were  $d = 0.58 \pm 0.04$  and  $\langle s \rangle = 85.49 \pm 11.82$ , respectively (mean plus/minus 838 standard deviation across subjects). 839

In addition to describing these data briefly at the beginning of the **Results** section, we also include a more comprehensive description of diffusion imaging and tractography in the section **Materials and Methods:** Human connectome dataset:

- 843 844
- "We fit the weighted stochastic blockmodel (WSBM) to group-representative human connectome data reconstructed from diffusion spectrum images with state-of-the-art tractography algorithms".

"Diffusion spectrum images (DSI) were acquired for a total of 30 subjects along with a T1-weighted anatomical scan. We followed a parallel strategy for data acquisition and construction of streamline adjacency matrices as in previous work [46]. DSI scans sampled 257 directions using a Q5 half-shell acquisition scheme with a maximum b-value of 5,000, an isotropic voxel size of 2.4 mm, and an axial acquisition with the following parameters: repetition time (TR) = 5 s, echo time (TE)= 138 ms, 52

slices, field of view (FoV) (231, 231, 125 mm). All procedures were approved in a convened review by the
 University of Pennsylvania's Institutional Review Board, and were carried out in accordance with the
 guidelines of the Institutional Review Board/Human Subjects Committee, University of Pennsylvania.
 All participants volunteered with informed consent in writing prior to data collection.

DSI data were reconstructed in DSI Studio (www.dsi-studio.labsolver.org) using q-space diffeomorphic 854 reconstruction (QSDR) [47]. QSDR first reconstructs diffusion-weighted images in native space and 855 computes the quantitative anisotropy (QA) in each voxel. Then, it warps the images to a template 856 QA volume in Montreal Neurological Institute (MNI) space using the statistical parametric mapping 857 (SPM) nonlinear registration algorithm. Once in MNI space, spin density functions were reconstructed 858 with a mean diffusion distance of 1.25 mm using three fiber orientations per voxel. Fiber tracking was 859 performed in DSI studio with an angular cutoff of 55°, step size of 1.0 mm, minimum length of 10 mm. 860 spin density function smoothing of 0.0, maximum length of 400 mm and a QA threshold determined 861 by DWI signal in the colony-stimulating factor. Deterministic fiber tracking using a modified FACT 862 algorithm was performed until 1,000,000 streamlines were reconstructed for each individual. 863

Anatomical scans were segmented using FreeSurfer59 and parcellated using the connectome mapping 864 toolkit [48]. A parcellation scheme including n = 129 regions was registered to the B0 volume from 865 each subject's DSI data. The B0 to MNI voxel mapping was used to map region labels from native 866 space to MNI coordinates. To extend region labels through the grey-white matter interface, the atlas 867 was dilated by 4 mm [49]. Dilation was accomplished by filling non-labelled voxels with the statistical 868 mode of their neighbors' labels. In the event of a tie, one of the modes was selected uniformly at 869 random. From these data, we constructed a structural connectivity matrix, A whose element  $A_{ij}$ 870 represented the number of streamlines connecting region i to region j, divided by the sum of volumes 871 for regions i and j." 872

• "Each individual's resulting network was undirected (i.e.  $A_{ij} = A_{ji}$ ) with density and mean node strength of  $d = 0.58 \pm 0.04$  and  $\langle s \rangle = 85.49 \pm 11.82$ ), respectively."

### 875 Comment 7

Section on "Behavioural relevance ...": Why/how were differences in total connection weight partialled out?
Why not normalize the matrices to have uniform weights before the analysis? Were do the differences arise
(e.g. do they correlate with white matter volume)? Also, what was the nature of the FDR correction? How

879 many tests were performed/corrected for?

The reviewer raises important details that were not included in our original description. In general, the 880 reviewer is absolutely correct that differences in coarse, non-specific measures like total connection weight 881 propagate to local measures. That is, apparent differences or correlations in regional properties of a network 882 can oftentimes be attributed to less interesting global differences in the network's density or total weight. 883 We were interested, specifically, in comparing the diversity index (a regional measure) and subjects' task 884 performances. Accordingly, we wished to control for whole-brain measures like total connection weight (row 885 and column sum of subjects' connectivity matrices). To do this, we calculated total connection weight for 886 all subjects and partialed out this variable from the diversity indices of brain regions. We then calculated 887 the correlation of task performance with the residuals of this regression analysis. 888

Beyond artifactual sources, we accept that brains are different from one individual to another, and while 889 we expect subjects to be similar to one another at a coarse scale, we also expect that fine-scale aspects 890 of their white-matter architecture will differ. These differences could be focal, highly localized effects at 891 the level of particular tracts, or a brainwide effect in which all (or a majority) of tracts are stronger or 892 weaker than those of other subjects. Though imperfect, the neurobiological interpretation of white-matter 803 network architecture is clear, and under ideal settings recapitulates in myelinated fiber tracts the same axonal 894 projections identified in non-human tract-tracing experiments [50, 51] and microstructural properties noted 895 in post-mortem studies [52]. 896

Irrespective of the source of individual variation, we would like to note that if we did not correct for global differences in connectivity, then the spatial pattern of correlations we report in the main text are, in fact, largely unchanged. In fact, in the absence of a correction, the pattern is nearly identical but the overall magnitude of correlations is much stronger. We include in this response (as well as the Supplementary

- <sup>901</sup> Materials) a figure indicating precisely this.
- <sup>902</sup> This figure is now called out in the main text:

• "(In the **Supplementary Material** we show that we get similar results without partialing out total connection weight; Fig. S17.)"



Figure 11: Effect of total network weight corrections on correlations between diversity scores and task performance. Each point represents the region-level correlation coefficient and the blue line represents the break-even line. If two brain regions had identical correlations with and without corrections for total network weight then they would fall along this line.

To the reviewer's findal point, we performed an FDR correction for multiple comparisons. Because we aimed to assess system-level effects, this correction was performed after correlations had been aggregated and averaged by brain system. Note, that the *p*-values associated with these correlations were obtained non-parametrically *via* a permutation test (eight tests in total).

### 909 Comment 8

Most of the first paragraph of the section "Connectomes support diverse ..." simply repeats the Intro and could be deleted.

<sup>912</sup> We thank the reviewer for this suggestion. We have rewritten that paragraph to have less overlap with <sup>913</sup> introduction.

• "The human connectome's ground truth meso-scale structure is unknown. This motivates studying alternative methods for uncovering communities and characterizing their similarities and differences. In this section, we compare the results of applying two well-known community detection methods: a weighted stochastic blockmodel (WSBM) and modularity maximization  $(Q_{max})$ ."

### 918 Comment 9

<sup>919</sup> I found it impossible to see any differences between Qmax and WSBM in Figure 3B.

We apologize for the lack of visual clarity in this figure. To encapsulate the full range of individual community assortativity scores we had to extend the y-axis, which obscured the differences between the mean curves. We have included an inset that shows the two curves in the absence of individual points within a restricted range. We have included this new figure below (see Fig. 12).



Figure 12: Modularity maximization and the weighted stochastic blockmodel uncover fundamentally different architectural signatures.

### 924 Comment 10

<sup>925</sup> Why are the WSBM networks more assortative than the null distribution in Fig 3C?

The statistic that we compare to the null distribution is the summed difference between orange and blue 926 curves in Fig 3B. The statistic is computed as the difference between the mean assortativity of all size-927  $N_r$  communities detected using the WSBM and  $Q_{max}$  summed over all possible values of  $N_r$ . Its value is 928 negative because we subtract  $Q_{max}$  assortativity from WSBM assortativity (note that the observed statistic, 929 which is shown in yellow, is large and negative). The null distribution was estimated by randomly permuting 930 community assignments, computing mean assortativity for every community of size  $N_r$ , and computing the 931 summed difference across all  $N_r$ . This null model tests whether differences in assortativity can be attributed 932 to community size and number. 933

### 934 Comment 11

Suggest delete the interpretive phrase "suggesting the capacity for an equally ..." from p6 of the Results.
We have removed the above phrase.

### 937 Comment 12

<sup>938</sup> It is the authors own preference, but I found aspects of the Discussion highly speculative for an original <sup>939</sup> research article.

We thank the reviewer for the suggestion and, while we retained the section and its overall spirit, we have removed the more far-fetched aspects of the discussion. Specifically, we made the following changes:

• We removed the phrase "computationally-relevant" in the section **Discussion: Community and** meso-scale connectome analyses.

• In the same section, we changed the sentence, "To comprehend the organization of connectome data, especially at the cellular scale, requires dimension reduction techniques like community detection that can distill the important organizational principles from those that are less useful" so that it now reads <sup>947</sup> "To comprehend the organization of connectome data, especially at the cellular scale, may require <sup>948</sup> dimension reduction techniques like community detection that can distill the important organizational <sup>949</sup> principles from those that are less useful."

• In the section **Discussion: Connectomes exhibit rich, non-assortative structure**, we changed the phrase "... into a more varied landscape that supports top-down ..." so that it now reads "... into a more varied landscape that possibly supports top-down ...."

# 953 Comment 13

<sup>954</sup> p13: The cite regarding repertoire diversity might also consider [3].

We had discussed this reference in other parts of the manuscript, but now also include it in the section **Discussion: Connectomes exhibit rich, non-assortative structure**.

# 957 Comment 14

<sup>958</sup> p15: How did the authors go from a whole group consistency-based connectome back to individual subjects? <sup>959</sup> We apologize for any confusion. Throughout most of the main text, we analyze a group-representative <sup>960</sup> matrix that was constructed from 30 subject-level matrices through an averaging procedure. We use this <sup>961</sup> group matrix to illustrate the basic differences between communities detected using  $Q_{max}$  and the WSBM. <sup>962</sup> For the final section, in which we demonstrate that regional diversity tracks behavior, we no longer analyze <sup>963</sup> the group-representative matrix, but instead apply the WSBM directly to single-subject matrices.

# 964 Comment 15

p16: were the structural and functional connectomic data and the behavioural data all from the same subjects?
 Why 30 for structural connectivity and 70 for functional connectivity?

We tried to locate the reference to 70 subjects, but were unable to do so. In any case, the functional and structural connectivity data were recorded as part of the same study and included 30 individuals.

# 969 **Reviewer references**

970 References:

1. Zalesky, A., Fornito, A., & Bullmore, E. (2012). On the use of correlation as a measure of network connectivity. Neuroimage, 60(4), 2096-2106.

2. Harriger L, Van Den Heuvel MP, Sporns O. 2012 Rich club organization of macaque cerebral cortex and its role in network communication. PLoS ONE 7,

3. Sporns O, Kotter R (2004) Motifs in brain networks. PLoS Biology 2: e369.

4. Roberts JA, Perry A, Lord AR, Roberts G, Mitchell PB, Smith RE, Breakspear M (2016) The contribution of geometry to the human connectome. Neuroimage 124: 379-393.

# 978 Reviewer #3

I quite enjoyed reading this report, which challenges the classical view of the view of the connectome being composed of segregated communities and introduces the alternative view on the existence of more heterogeneous community configurations.

Unlike to the standard methods used to define communities of the structural connectome, the authors utilize a different technique, weighted stochastic block model (WSBM), one that does not explicitly impose the assumption of the modularity maximization and hence segregated communities. Using the WSBM, this work "reveals" other kinds of communities and community interactions, where the newly found communities show a better overlap with the functional networks of the brain. It is also quite interesting to see that the intersubject variability in diversity of the community profiles of certain brain regions shows some correlation with the behavioral performance.

I think the paper introduces a novel and quite interesting perspective on the diversity of community 989 organization in the connectome. My major comment is about the lack of true ground truth for the studied 990 problem. As a logical decision, the authors chose to compare to the most commonly used state-of-the art 991 method, modularity maximization, referred as Qmax here. However, this algorithm, as also stated by the 992 authors is designed to maximize modularity and hence assortativeness. Hence, removing this particular 993 constraint modularity maximization as in the case of using WSBM, naturally leads to less assortative 994 community structures compared to Qmax, which by design extracts segregated communities. My main question 995 is how do we know that the partitions returned by WSBM are more "correct" compared to those detected by 996 Qmax?997

Having said that, I would acknowledge that this is not a drawback of the method presented here but a general concern about the lack of a true ground truth for the problem at hand. It may be important to at least mention or discuss this point and maybe point out that the results drastically change when the modularity maximization constraint is removed, although a true ground truth for neither algorithm exists.

We thank the reviewer for their overall positive comments. The reviewer raises an important and timely 1002 question (one that is also repeated by Reviewers 1 & 2): Given two community detection algorithms that 1003 partition a network differently, can we claim that one is more "correct" or "better" than the other? This 1004 is a challenging problem that is being actively researched [53]. One common approach for comparing two 1005 community detection algorithms or sets of partitions is by cross-validation using metadata [31, 30]. In short, 1006 this approach assumes that there exists node-/edge-level metadata that reflect a network's ground truth 1007 communities better than those estimated from its topology alone. In the present study, we use whole-brain 1008 functional connectivity (human) and gene co-expression patterns (mouse). We can compare communities 1009 detected using the WSBM and  $Q_{max}$  by quantifying how well they are aligned to these metadata. If one or 1010 the other community detection method consistently outperforms the other then we can claim that, at least 1011 along these specific dimensions, that method is superior to the other. 1012

The results of our cross-validation procedure, which we document in the section **Functional relevance** of the WSBM, show that the WSBM does, indeed, outperform  $Q_{max}$  when we compare their respective communities to the metadata. Moreover, because we recognize functional connectivity and gene co-expression as being important to the function of neural systems, we interpret these results as an indication that the WSBM communities capture functionally relevant patterns of connectivity.

<sup>1018</sup> We now include extensive discussion of the cross-validation procedure in the **Results** section:

• "Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions 1019 using empirical FC as metadata (See Materials and Methods for more details on FC reconstruction 1020 from BOLD signals). This approach – cross-validation through metadata – is well-established and has 1021 been used extensively in past studies [31, 30]. In essence, it assumes that metadata better represents 1022 some aspect of a network's ground truth organization than its structural topology alone. Community 1023 detection methods that are more closely aligned with the metadata may be more sensitive to the 1024 network's ground truth organization and are considered, in this quantitative and objective sense. 1025 superior to those that do not. We reasoned that if the brain's correlated activity pattern is better 1026 described by assortative communities behaving autonomously, then the FC network will be more closely 1027 aligned with  $Q_{max}$  communities. On the other hand, if the correlation pattern is better described by 1028 interacting, non-assortative communities, the alignment of FC to WSBM communities will be greater. 1029 Here, we quantify this alignment as the mean weight of within-community functional connections minus 1030 1031 the mean weight of between-community connections."

### 1032 Comment 1

How does the approach followed by the authors differ from the hierarchical clustering method, cited as ref [35] in the manuscript, as to my knowledge this method also falls outside of the modularity maximization framework. Also, what was the motivation behind the choice of WSBM instead of for instance the hierarchical clustering approach as in [35]?

The hierarchical method proposed by Clauset et al. shares many properties with the WSBM, most prominently the use of a statistical model and maximization of a likelihood function to infer communities. However, it differs in a few important ways. For example, the hierarchical method is not compatible with weighted networks. It does, however, have the distinct advantage of inferring a hierarchy of communities rather than a single partition. So the method of Clauset et al. will identify an entire tree of community partitions. Nonetheless, we decided to use the weighted version of the stochastic blockmodel presented by [34, 35]. This decision was motivated by the fact that most brain network data are weighted in some way and because we, as neuroscientists, believe that those weights are of neurobiological relevance.

### 1045 Comment 2

Page 2, first paragraph: "Next, we define a node-level diversity index that quantifies the extent to which individual neural elements participate in communities of all classes." Can a node (neural element) belong to multiple clusters; i.e. the communities can be overlapping and are not disjoint?

We apologize for any confusion. The WSBM results in a hard partition of network nodes (neural ele-1049 ments) into one and only one community. Given a single partition, we classified the interactions between 1050 pairs of communities as either assortative, core-periphery, or disassortative. We then counted, for each com-1051 munity, the number of times it participated in each type of interaction. The diversity index of a community 1052 is quantified as the entropy over that distribution and assigned, uniformly, to all nodes comprising that 1053 community. Thus, communities whose inter-community interactions are of one type, e.g. only assortative, 1054 contain nodes of low diversity. Conversely, if a community's inter-community interactions are varied, then 1055 its constituent nodes will have high diversity. 1056

<sup>1057</sup> We have now added a subsection in **Materials and Methods** further detailing the calculation of the <sup>1058</sup> diversity index.

• "A partition of a network into communities induces a set of two-community motifs based on connection densities. In the previous section, we presented rules for classifying those motifs into one of three classes. For a K-community partition, community r participates in K - 1 interactions. We can calculate for each motif class (now differentiating between cores and peripheries, resulting in four distinct classes), how frequently it appears among community r's K-1 interactions. If we express these frequencies as probabilities,  $P_a$ ,  $P_c$ ,  $P_p$ , and  $P_d$  (subscripts indicate "assortative", "core", "periphery", and "disassortative" motif frequencies, respectively), we can then calculate an entropy:

$$H_r = -[P_a \log_2 P_a + P_c \log_2 P_c + P_p \log_2 P_p + P_d \log_2 P_d].$$
 (1)

This entropy is zero if community r participates in only one motif class and is maximized when rparticipates in all classes equally. We then assign this score to all nodes  $i \in r$ . The resulting vector of length  $[N \times 1]$  specifies the single-partition diversity index for each node. We can calculate this vector for all K-community partitions and estimate mean diversity indices for each node by averaging across partitions."

### 1071 Comment 3

Fig. 3a: Are the within-technique variation of information (VI) scores based on the comparison of partitions with the same number of communities on two different subjects datasets?

As the comparisons are performed on partitions with the same number of communities, I assume two different partitions using the same technique can come from the use of different datasets. However, that is not clear at that point of the manuscript, as any information on different subjects data etc. has been provided yet. The authors may want to explain what leads to different partitions with the same number of communities, which are used for comparison.

We apologize for any confusion. We only calculate VI for pairs of partitions that result in the same number of communities. However, the comparisons are not carried out at the single-subject level. Because both  $Q_{max}$  and the WSBM algorithms are non-deterministic – i.e. repeated runs of the algorithm usually result in slightly different solutions – we computed VI between pairs of partitions uncovered using the same community detection algorithm and also between algorithms. We now clarify this in the manuscript and figure caption.

In the section Connectomes support diverse meso-scale architecture we now include the statement: • "Specifically, we computed VI separately for three different subsets of partitions: partitions detected using WSBM with other WSBM partitions; partitions detected using  $Q_{max}$  with other  $Q_{max}$  partitions; partitions detected using the WSBM with  $Q_{max}$  partitions."

### 1090 Comment 4

Fig. 3A: Also, the authors mention that both techniques, WSBM and Qmax lead to self-similar partitions that are statistically different between techniques. In Fig. 3A, the variation of information (VI) scores of WSBM are much higher than those of Qmax and for K=10, the within-technique VI for WSBM is even higher than between-technique VI. What is the cause of such difference in within-technique VI observed between the two techniques? Are the WSBM partitions reliable, if they show such high within technique VI scores?

We thank the reviewer for pointing this out. The reviewer has correctly interpreted the figure – on average, partition similarity is greater for repeated runs of  $Q_{max}$  than for the WSBM and for K = 10 the between technique similarity is greater than within-technique similarity of the WSBM. We believe that this may be a peculiarity of the human connectome dataset – we see more comparable levels of similarity when investigating the non-human connectome data. See Mouse and Drosophila in Fig. S2.

It is also important to note that, like  $Q_{max}$ , the WSBM must infer the community assignments of N nodes. In addition, however, the WSBM must also estimate the parameters for each of K(K-1) within/between community blocks. This results in a larger parameter space and may lead to more variability from run to run.

<sup>1105</sup> Despite this, the communities uncovered using WSBM converge across species to paint a picture of a <sup>1106</sup> non-assortative brain, offer superior predictions meta-data (FC and gene co-expression) compared to  $Q_{max}$ , <sup>1107</sup> and can be used to predict behavioral measures. This highlights the utility and reliability of the WSBM and <sup>1108</sup> paves the way for future studies.

### 1109 Comment 5

The authors mention: "We compared these curves using functional data analysis, which is a set of statistical tools for comparing continuous curves [47,48]. We found that the observed scores were smaller than those obtained under the null model ( $p < 10^3$ ), confirming that WSBM communities tend to be less assortative than Qmax (Fig. 3C)". Arent these curves discrete set of measurements, hence allowing for a comparison for instance by Monte-Carlo approach; simply by shuffling the labels of assortativity scores between two methods over multiple comparisons?

The reviewer is correct. An alternative approach for comparing community assortativity is to proceed 1116 point by point (where each point represents community size), and compute a point-wise p-value by randomly 1117 permuting community labels. This would result in a series of *p*-values, which would allow us to independently 1118 assess whether communities of a given size differ in their assortativity. However, it would also pose a multiple 1119 comparison problem, as separate tests are performed at each value of community size. By contrast, our aim 1120 was simply to test whether community assortativity, on average, differed between techniques, which motivates 1121 the use of FDA, which is a tool for the statistical comparison of curve shapes that circumvents the multiple 1122 comparisons problem by performing tests between the full curves rather than at many points. 1123

### 1124 Comment 6

I fail to understand Fig. 3C and the stats performed with functional data analysis. What does the y-axis 1125 labeled as "Probability" represent? The authors mention "Specifically, we generated a statistic by performing 1126 a pointwise subtraction and summation of the curves A (N) obtained for the WSBM and Qmax. The value of 1127 this statistic quantifies the difference between mean community assortativity across communities of all sizes 1128 and is negative when communities detected using Qmax are more assortative than WSBMs. We compared this 1129 statistic against a null distribution obtained from a null model wherein we perserved the number and size of 1130 communities in a given partition but permute nodes assignments uniformly and randomly (1000 repetitions)." 1131 What does the pointwise subtraction and summation of the curves A(N) yield, is it average difference between 1132 the two curves? For the null distribution, doesn't the permutation of nodes result in non-continuous clusters. 1133

Again, we apologize for any confusion. The FDA computes the difference in mean assortativity of communities detected using the WSBM and  $Q_{max}$ . These differences are then summed over all possible community sizes. This sum is treated as a test statistic. We compare this statistic against a null distribution generated after permuting nodes' community assignments and recomputing community assortivity scores. This null model tests whether we would expect the observed test statistic given communities of the same size and number, but randomly assigned. The "probability" label in the figure represents an estimate of the probability that we observe a particular test statistic under the null model.

The reviewer's question about non-continuous clusters is an interesting one. In general, the answer is 1142 "yes" – randomly permuting community assignments will oftentimes result in spatially-disjoint communities. 1143 It is also the case that, in practice, most (but not all) community detection algorithms applied to structural 1144 connectome data result in spatially-contiguous communities. However, the origin of this spatial continguity 1145 has been debated, and it remains unclear whether the spatial continguity is a consequence of biases in 1146 tractography or a feature of the network [25, 54]. While we agree that it would be potentially interesting 1147 to test a null model that results in comparable spatial distributions of communities, (1) it is not usually 1148 possible to permute community assignments while preserving the same spatial distribution of the observed 1149 communities; (2) performing such a test would mean engaging a contentious literature whose topic is beyond 1150 the scope of the present study. 1151

Lastly, we agree with the reviewer that there are certainly different null models that we could test. However, in the absence of an explicit hypothesis, the test we used represents a reasonable initial point of comparison. We now include a more detailed description of these analyses in the section **Results: Connectomes support diverse meso-scale architecture**:

• "Next, we wished to confirm that the WSBM uncovered non-assortative communities, specifically. To 1156 test this hypothesis, we computed for each community r, its size,  $N_r$ , and assortativity score,  $\mathcal{A}_r$ , 1157 which measured its internal density of connections less its maximum density of connections to any 1158 other community (See Materials and Methods). We then aggregated all detected communities 1159 and computed the mean assortativity score as a function of community size,  $\mathcal{A}(N)$  (Fig. 3B). These 1160 procedures were performed separately for the WSBM and  $Q_{max}$ . We compared these curves using 1161 functional data analysis, which is a set of statistical tools for comparing continuous curves [55, 56]. 1162 Specifically, we computed the summed pointwise difference in both curves, which we treated as a test 1163 statistic. We found that the observed statistic was smaller than those obtained under a permutation-1164 based null model  $(p < 10^{-3})$ , confirming that WSBM communities tend to be less assortative than 1165  $Q_{max}$  (Fig. 3C). Again, these findings are consistent across connectome data obtained from all species 1166 (Fig. S3). 1167

### 1168 Comment 7

The communities detected by WSBM more closely reflect the functional networks. However, I believe it is important to point out that functional networks emerge from the dynamics and interactions between neural elements that is constrained by the structural connections but not purely determined by them. Hence, although some degree of overlap between structure and function is expected, it is not expected that they will be the same or very similar. The effect of the dynamics would play a crucial role in the emergence of the functional networks.

The reviewer is exactly correct. The organization of FC depends a great deal on the underlying config-1175 uration of structural connections, though the extent to which FC comes to resemble SC is also dependent 1176 upon the nature of the network's dynamics – i.e. the evolution operator that propagates each brain regions' 1177 state at time t to a new state at time  $t + \Delta t$ . The measure used to estimate FC also plays a role; correla-1178 tion measures are known to induce transitive functional connections. Our approach, in line with the aims 1179 of this paper, was to focus on the role of the brain's underlying structural connectivity in influencing FC. 1180 Though over short time intervals, the mapping of structure to function is less constrained [57], there is a 1181 long-standing expectation that over longer time intervals the correlation pattern of the brain's spontaneous. 1182 resting activity will come to resemble its underlying anatomical structure [58]. 1183

However, we also agree with that, as written, our explanation for why we might expect a high density of functional connections within non-assortative communities is unclear. We take this opportunity to detail our rationale. Specifically, we hypothesized that brain regions with similar incoming and outgoing connections receive and deliver similar input and output signals, and should therefore exhibit temporally correlated activity. The existence of this relation is a long-standing assumption in the network neuroscience community. In fact, in past studies where empirical estimates of FC could not be easily obtained, a measure called the "matching index" (which calculates the similarity of regions' connectivity profiles) has been used as a stand-in [59].

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities of brain regions 1192 with similar patterns of connections. However, these methods differ in that communities are defined according 1193 to two vastly different topological principles.  $Q_{max}$  assumes that the brain's meso-scale organization is based 1194 on assortative and segregated sub-systems, while the WSBM allows communities to be both assortative and 1195 non-assortative. These differences in meso-scale structure imply differences in brain function. A strictly 1196 assortative brain is aligned with the hypothesis that the brain is composed of communities operating nearly 1197 autonomously, while a brain composed of some non-assortative communities implies that brain function 1198 arises not from independent communities, but from the interactions between communities. 1199

Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions using 1200 empirical FC as metadata (See Materials and Methods for more details on FC reconstruction from 1201 BOLD signals). This approach – cross-validation through metadata – is well-established and has been used 1202 extensively in past studies [31, 30]. In essence, it assumes that metadata better represents some aspect of 1203 a network's ground truth organization than its structural topology alone. Community detection methods 1204 that are more closely aligned with the metadata may be more sensitive to the network's ground truth 1205 organization and are considered, in this quantitative and objective sense, superior to those that do not. 1206 We reasoned that if the brain's correlated activity pattern is better described by assortative communities 1207 behaving autonomously, then the FC network will be more closely aligned with  $Q_{max}$  communities. On the 1208 other hand, if the correlation pattern is better described by interacting, non-assortative communities, the 1209 alignment of FC to WSBM communities will be greater. Here, we quantify this alignment as the mean weight 1210 of within-community functional connections minus the mean weight of between-community connections. 1211

In addition to noting the limitations of assuming that FC is shaped by structure alone, we have also amended the **Results: Functional relevance of the WSBM** to better reflect our assumptions and hypotheses:

• "While the results of this section suggest that the WSBM is closely aligned with human FC (and mouse 1215 gene-coexpression; see the **Supplementary Materials**), we report several caveats. First, our analysis 1216 assumes a close relationship of FC with the underlying structure. While structure constrains FC, the 1217 mapping between the two is imperfect and fluctuates over shorter timescales [57] and can vary when 1218 different measures of FC are used. The use of a Pearson correlation, for example, induces transitive 1219 functional connections by placing statistical bounds on correlations among triplets of nodes [32]. This 1220 implies that the correlation values are not independent, which may influence our estimates of mean 1221 within- and between-community FC magnitude." 1222

"It is generally agreed upon that brain structural connectivity determines the partners that any given 1223 region can "talk to", and therefore constrains communication patterns among brain regions, shaping 1224 the correlation pattern of ongoing neural activity, i.e. functional network organization. We reasoned 1225 that if two brain regions receive input from the same set of brain regions and deliver output to the 1226 same set of regions, then their activity over time should be correlated, i.e. those regions would appear 1227 functionally connected to one another. This set of assumptions has a long tradition in the network 1228 neuroscience community. In the past when empirical estimates of FC could not be easily obtained, 1229 measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been 1230 used as a stand-in [27, 28, 29]. 1231

Though through different mechanisms, both the WSBM and  $Q_{max}$  produce communities of brain regions with similar patterns of connections. However, these methods differ in that communities are defined according to two vastly different topological principles.  $Q_{max}$  assumes that the brain's meso-scale organization is based on assortative and segregated sub-systems, while the WSBM allows communities to be both assortative and non-assortative. These differences in meso-scale structure imply differences in brain function. A strictly assortative brain is aligned with the hypothesis that

the brain is composed of communities operating nearly autonomously, while a brain composed of some 1238 non-assortative communities implies that brain function arises not from independent communities, but 1239 from the interactions between communities. 1240

Here, we test these two hypotheses by cross-validating and comparing WSBM and  $Q_{max}$  partitions 1241 using empirical FC as metadata (See Materials and Methods for more details on FC reconstruction 1242 from BOLD signals). This approach - cross-validation through metadata - is well-established and has 1243 been used extensively in past studies [31, 30]. In essence, it assumes that metadata better represents 1244 some aspect of a network's ground truth organization than its structural topology alone. Community 1245 detection methods that are more closely aligned with the metadata may be more sensitive to the 1246 network's ground truth organization and are considered, in this quantitative and objective sense. 1247 superior to those that do not. We reasoned that if the brain's correlated activity pattern is better 1248 described by assortative communities behaving autonomously, then the FC network will be more closely 1249 aligned with  $Q_{max}$  communities. On the other hand, if the correlation pattern is better described by 1250 interacting, non-assortative communities, the alignment of FC to WSBM communities will be greater. 1251 Here, we quantify this alignment as the mean weight of within-community functional connections minus 1252 the mean weight of between-community functional connections." 1253

1254 1255

• "We note that the use of Pearson correlation as a measure of FC results in increased transitivity (if a strong correlation exists between nodes A and B as well as B and C, then A and C will tend to be strongly correlated), which can reinforce block structure in correlation matrices [32]." 1256

#### Comment 8 1257

The authors state "To test whether this was the case, we imposed partitions obtained from the WSBM and 1258 Qmax applied to the structural connectome onto the FC matrix and computed the difference of within- and 1259 between-community FC density. We found that over a range  $K = 2, \ldots, 10$ , the WSBM consistently 1260 uncovered communities whose internal FC density exceeded their between-community density (Fig. 5A)." The 1261 functional networks are defined on the FC matrix, hence I would have thought that they would superimpose 1262 FC matrix parcellation onto the structural connectome (SC) partitions. For instance Fig. 5A caption states: 1263 "Functional connectivity (FC) matrix ordered by functional system". As both, FC connectivity and the 1264 labeling of the functional systems come from the functional connectivity, how does this figure capture the 1265 partitions of the structural connectome? Is it a misunderstanding on my side or is there a confusion between 1266 SC and FC in the wording here? 1267

The reviewer is correct. The FC matrix depicted in Fig. 5A is ordered according to functional systems 1268 so that the reader can develop some intuition for the matrix's structure. We chose not to order the matrix 1269 by partitions detected by either WSBM or Qmax because there were thousands of such partitions and 1270 choosing a representative partition from among those was not trivial. We note that, in general, discerning 1271 the differences between the two techniques based on a visual comparison is not especially illuminating; it 1272 was only by performing detailed statistical comparisons that we were able to confirm that the WSBM better 1273 segregates FC compared to  $Q_{max}$ . 1274

In any case, we show here, an example of the FC matrix with its nodes ordered according to consensus 1275 communities and with k = 5 for both the WSBM and  $Q_{max}$  (Fig. 13). We obtained the consensus commu-1276 nities by reclustering an association matrix, which we constructed separately for partitions detected using 1277 either method. 1278

Because we believe that this figure does not contribute much beyond what we already mention in the 1279 main text, we opted to not include it in the manuscript. We have, however, edited the caption for Figure 1280 5A to make clear that the ordering of nodes represents the functional systems described in [60]. 1281

• "Note that the order of nodes shown in this panel does not correspond to partitions generated by either 1282 the WSBM or  $Q_{max}$ ." 1283

#### Comment 9 1284

I think the correlations between the diversity index and performance categorized according to functional 1285 networks is very interesting. From what I can see in Fig. 8B, one can conclude that some networks require 1286



Figure 13: FC matrix ordered by WSBM and  $Q_{max}$  partitions. Rows and columns of the FC matrix are reordered so that nodes assigned to the same community are next to one another.

certain type of motifs (interactions) such as the visual network and the DAN, whereas others such as the control network, subcortical areas and maybe also the default mode network contain interactions of various kinds for a good cognitive performance. What about the whole brain diversity of connections? Would that make any inference on the cognitive performance?

We agree that it would be interesting to test whether diversity as a global statistic was related to subject performance. To do so, we calculated the Pearson and Spearman correlation of performance on the Stroop and Navon tasks (we tested their performance separately and also their average performance on both tasks) with a node-averaged measure of diversity. The greatest magnitude correlation we observed was using the Spearman measure to relate total accuracy on the Stroop task with average diversity ( $\rho = 0.18$ ; p > 0.05). All other correlations were weaker and also not significant.

We note that while global diversity does not appear to track Stroop or Navon task performance, it may be useful for future studies. Accordingly, we now note this in the main text in Materials and Methods: Diversity index:

"Note that while we define the diversity index at the level of individual brain regions (network nodes), it would be straightforward to average node-level diversity scores to compute a global diversity score that could serve to characterize the diversity of meso-scale structure in the network as whole. Alternatively, a global diversity index could be computed straightforwardly as an entropy based on the complete set of community motif frequences."

## 1305 Comment 10

Page1: What is the difference between clusters and communities? I found the illustration of different con nectivity profiles in Fig. 1 very useful. It may be very helpful to illustrate the concepts of region, community,
 partition in a similar manner for the nave reader, if possible, at least as supplementary material.

We apologize for any confusion. In many applications, the terms cluster, community, module, and group (among others) have come to mean the same thing. So when we refer to a "cluster" or "community" we are referring to a set of brain regions grouped together according to some topological principle, e.g. by maximizing Q or using the WSBM. We have added a figure in the supplement illustrating the different topological scales of a network (node  $\rightarrow$  community  $\rightarrow$  whole network).

### 1314 Comment 11

<sup>1315</sup> Page 1: what do individual network nodes represent? Brain regions? It would be useful to specify here.

The reviewer is correct – in all five connectome datasets, nodes represent brain areas whose boundaries are delineated based on their function, morphology, cyto-architecture, or related measures. We note this in the main text in the section Human connectome dataset and in the Supplementary Material under the section Non-human connectome data.

### 1320 Comment 12

Is assortative architecture the same as small-world, as used in some reports on connectomes architecture? 1321 Assortative architecture and small-worldness are distinct concepts. Small-worldness refers to a global 1322 property of a network in which it simultaneously exhibits high levels of clustering (nodes' neighbors tend 1323 to be connected to one another) and short path length (the mean number of steps between nodes is small). 1324 Assortative architecture refers to a property of small groups or communities of nodes (so it is not a global 1325 property of a network) in which nodes that belong to a group prefer to connect to other nodes in the same 1326 group compared to nodes in different groups. While it is possible for a network with assortative structure to 1327 also possess small-world qualities (dense communities with a few links between communities) and vice versa, 1328 in general that is not the case. 1329

## 1330 Comment 13

Fig. 2: Community labeled with purple seems to consist of only one small brain region in the right hemisphere, which does not seem to have any correspondence in the left hemisphere, whether labeled as the same community or not. Where does this asymmetry stem from? Is it an algorithmic artifact?

We appreciate the reviewer's attention to detail. In this case, the purple community and its relatively 1334 small size is a result of the stochasticity of the WSBM algorithm. That is, in attempting to optimize their 1335 respective objective functions, the output of both the WSBM and  $Q_{max}$  will vary somewhat. The commu-1336 nities shown in Figure 2 represent the outputs of single runs of the algorithm and should not be treated as 1337 necessarily representative of the network's ground truth communities. It is not difficult to identify a different 1338 partition of the same network into the same number of communities with comparably-sized communities. 1339 To demonstrate this, we show an alternative partition of the network into five communities. Specifically, we 1340 chose the partition with the most similarly-sized communities  $(25.6 \pm 2.07 \text{ nodes per community})$ . We have 1341 also replaced the WSBM partition in Figure 2 with the communities shown here. 1342



Figure 14: Surface plot showing similar-sized communities detected using the WSBM. Colors represent different community labels.

It is essential to note that in the main text we intentionally avoid defining a single "representative" partition from among the ensemble of detected partitions. In general, most networks have "fuzzy" mesoscale structure, with a near-degeneracy of optimal partitions. That is, there may be many partitions judged to be of similar quality but which possibly differ a bit from one another. In the main text, we embrace this variability and focus on the statistical properties of this ensemble of near-optimal partitions.

### 1348 Comment 14

<sup>1349</sup> Fig. 3. Caption:  $Q_max$  should be  $Q_{max}$  in latex notation, "perserved" should be "preserved".

<sup>1350</sup> We thank the reviewer for pointing this out. We have corrected both typos.

### 1351 Comment 15

1352 Fig. 3F, what do the upper and lower limits of the box plot represent?

The upper and lower limits of each box represent the 25th and 75th percentiles of each system's assortativity.

### 1355 Comment 16

### <sup>1356</sup> Fig. 4C, how were the rich club nodes labeled/estimated?

To identify putative rich clubs, we maximized a weighted rich club coefficient [61]. This coefficient is calculated at different levels, k, corresponding to nodes' degrees. For a given, k, we first identify all nodes of degree k or greater, the number of connections among those nodes  $(E_{>k})$ , and the total weight of those connections  $(W_{>k})$ . We divide  $W_{>k}$  by the total weight of the strongest  $E_{>k}$  edges in the network,  $W_{max} = \sum_{l=1}^{E_{>k}} w_l^{rank}$ , where  $w_l^{rank}$  is the set of all network edge weights ordered from strongest to weakest. This measure defines the weighted rich club coefficient:

$$\phi^w(k) = \frac{W_{>k}}{W_{max}} \ . \tag{2}$$

This coefficient measures, for every possible node degree, k, the total weight of connections among nodes whose degrees are greater than k divided by the maximum possible value of the same number of connections. We compared  $\phi^w(k)$  for the observed network against an ensemble of 100 randomized networks with the same degree sequence as the observed network. For every possible k, we calculated the fraction of all randomized networks whose rich club coefficient was in excess of the observed network's. This fraction served as a p-value for associated statistical tests and made it possible to identify statistically significant rich clubs (p < 0.05).

In practice, this procedure often leads to a range of k over which rich clubs are considered statistically significant. Rather than explore this entire range, we focused on a 20-80 split of network nodes assigned to and not assigned to the rich club. We justify this split on the grounds that (i) all networks we observed exhibited a statistically significant rich club in this range, making it unneccessary to develop separate criteria for studying rich clubs across species, and (ii) a rich club composed of 20% of a network's nodes is exclusive enough to be of interest but not so large as to be trivial.

We now include a more detailed explanation of these procedures in our manuscript in the Materials and Methods section.

• "We identified putative rich club nodes by maximizing a weighted rich club coefficient,  $\phi^w(k)$ , where k is node degree [61]. Intuitively, a weighted rich club is composed of highly connected nodes linked to one another by connections with strong weights. To calculate  $\phi^w(k)$ , we first identify the sub-network composed only of nodes whose degree is k or greater, the number of connections among those nodes,  $E_{>k}$ , and the total weight of those connections  $W_{>k}$ . We also calculate  $W_{k>}^{max} = \sum_{l=1}^{E_{>k}} w_l^{rank}$ , which measures the maximum possible value that  $E_{>k}$  connections could have given the edge weights present in the network.

1384

$$\phi^w(k) = \frac{W_{>k}}{W_{k>}^{max}} \ . \tag{3}$$

<sup>1386</sup> We compared  $\phi^w(k)$  for the observed network against the same measure made over an ensemble of 100 <sup>1387</sup> randomized networks with the same degree sequence. For every possible k, we calculated the fraction <sup>1388</sup> of all randomized networks whose rich club coefficient was in excess of the observed network's. This <sup>1389</sup> fraction served as a p-value for performing statistical tests and made it possible to identify statistically <sup>1390</sup> significant rich clubs (p < 0.05).

This procedure results in a range of k over which rich clubs are considered statistically significant. Rather than characterize this entire range, we focused on a 20-80 split of network nodes into rich and non-rich groups. We justify this split on the grounds that (i) all of the networks we studied exhibited a statistically significant rich club in this range, making it unneccessary to develop separate criteria for studying rich clubs across species, and (ii) a rich club composed of 20% of a network's nodes is exclusive enough to be of interest but not so large as to be trivial (Fig. 15)."

<sup>1397</sup> We also include the following figure:

1385



Figure 15: Rich club analysis. (A) Here we display *p*-values for rich clubs across all five species. (B) The number of statistically significant rich clubs as a fraction of network size.

### 1398 Comment 17

1399 What is the difference between a core community and a hub?

Though the definition of a "hub" region is not settled upon, it generally refers to a node with a high level of connectivity (high-degree and/or high-strength) that occupies a position of centrality and influence in the network. A core community refers to a group or community of nodes, all with similar connectivity profiles,
that interacts with a peripheral community. Specifically, the core nodes connect both to one another and
also to the periphery, while the peripheral nodes do not connect to one another but do connect to the core.
Cores, like hubs, represent structures in the network that are associated with influence and centrality. Unlike
hubs, however, cores explicitly refer to groups of nodes, rather than to any particular node.

### 1407 Comment 18

Page 13, first paragraph: I would say "functional connectivity" (FC) instead of "functional dynamics", as the comparison was done to FC and with the emergence of new methods such as dynamic functional connectivity etc., "functional dynamics" is now understood as changing functional connectivity.

<sup>1411</sup> We have made this change.

### 1412 Comment 19

What was the motivation behind using a 128 parcellation and can the authors comment on if/how the change of parcellation may change the observed effects?

The 128-node parcellation is a sub-division of the well-known Desikan-Killiany atlas [62]. This particular sub-division is implemented in the Connectome Mapper Toolkit [48]. Though this software includes both coarser and finer sub-divisions, the division into 129 nodes (128 after excluding brainstem) is particularly appealing, as cortical and sub-cortical regions have approximately the same volume, which reduces potential volume-related biases in tractography and network reconstruction.

As the reviewer correctly notes, choice of parcellations can induce biases in the structure of the network. 1420 Because there is considerable debate about what parcellation is the best (especially when used to define 1421 the nodes of a structural connectivity network), dealing with this issue is non-trivial. One strategy to deal 1422 with this issue is to demonstrate that one's results are robust to reasonable variation of parcellation scheme. 1423 In our case, the nested sub-divisions of the Desikan-Killiany are benefitial, because we can test whether 1424 results obtained using any particular sub-division generalize to the next-coarser and next-finer parcellations. 1425 Here, we show that our main results remain qualitatively the same when we change the number of nodes 1426 from 128 to 82 and to 233. Specifically, we find across different numbers of nodes, the mean system-level 1427 diversity scores are correlated with scores obtained from the 128-node network described in the main text 1428 (Fig. 16B,D). We note that these correlations are intended to be qualitative demonstrations of the robustness 1429 of our results. With only eight systems (corresponding to eight observations), neither correlation passes a 1430 p < 0.05 threshold (p = 0.09 and p = 0.43 for the 82- and 233-node networks). Nonetheless, these findings 1431 1432 suggest a broad correspondence across scales.

We also repeated the behavioral analysis and calculated the correlation of regional diversity scores with 1433 the Stroop and Navon task accuracy. Comparing the 82-, 128-, and 233-node results was complicated by the 1434 fact that network nodes were defined differently in each case. To facilitate comparison across the differently 1435 sized networks we focused on system-level statistics [60]. This entailed aggregating all nodes assigned to the 1436 same system and averaging their diversity-by-behavior correlations to obtain a system-level mean. Because 1437 the number and identities of systems were consistent across the different-sized networks, this enabled us to 1438 relate the system-level scores between networks. We obtained mean system-level scores as we varied the 1439 number of communities from k = 2 to k = 10, aggregated all system scores and computed two correlations. 1440 First we computed the correlation of system-level scores for the 82- and 128-node networks (r = 0.32, 1441 p < 0.01). We then computed a similar correlation using system-level scores obtained for the 128- and 1442 233-node networks (r = 0.32, p < 0.01) (Fig. 17A, B). As with the previous section, the comparison between 1443 scales was not perfect, but confirmed similar overall patterns, suggesting that our results were robust to 1444 reasonable variation in choice of parcellation. 1445

### 1446 Comment 20

Page 18: In section "Community and regional assortativity" the authors provide the equations for both directed and undirected graphs. Is that done so for the generalization of the provided methods for directed graphs? As far as I understand the results in the actual manuscript are based on undirected graphs. I believe



Figure 16: Comparison of system-level diversity scores with 82- and 233node networks. (A) System-level diversity scores for 82-node network. (B) Rank correlation of system-level scores obtained for the 82-node and 128-node networks. Panels (C) and (D) are the same as (A) and (B) but for the 233-node network.

the directed graph use may be necessary for the mouse data? If so, it may be worth mentioning this in the manuscript.

With the exception of the human connectome data, all networks we analyze are directed. In general, our measures generalize to directed networks. In the section **Materials and methods: Community and** regional assortativity, we describe how we deal with directed networks. In short, we have the option of considering for a node or community the density of its incoming or outgoing connections to other communities. Our solution was to take the maximum of the two density measurements as a sort of "worst-case" scenario. That is, we consider a community disassortative if *either* its incoming or outgoing connections would lead to such a classification.

## 1459 Comment 21

Eq. (8): it could be easier for the reader if a different notation instead of double indexing was used to refer  $a_i$  and  $a_{iz_i}$ . It is not clear to me what  $a_{iz_i}$  represents.

<sup>1462</sup> We agree with the reviewer that this notation is confusing. The variable  $a_{i,z_i}$  represents the density of <sup>1463</sup> node *i*'s connections to its own community,  $z_i$ . Similarly,  $a_{i,r}$  represents the density of node *i*'s connections <sup>1464</sup> to community *r*. We leave these definitions intact but have changed the regional assortativity variable name <sup>1465</sup> from  $a_i$  to  $\eta_i$ .

### 1466 **Comment 22**

1467 It may also be useful to express the diversity index mathematically.

<sup>1468</sup> We have now added a subsection in **Materials and Methods** detailing the calculation of the diversity <sup>1469</sup> index.



Figure 17: Comparison of system-level correlations of diversity and task performance with 82- and 233-node networks. (A) Comparison of system-level correlations between the 82- and 128-node networks for all K = 2 to K = 10. (B) Same as panel (A), but for the 233-node network.

• "A partition of a network into communities induces a set of two-community motifs based on connection densities. In the previous section we presented rules for classifying those motifs into one of three classes. For a K-community partition, community r participates in K-1 interactions. We can calculate for each motif class (now differentiating between cores and peripheries, resulting in four distinct classes), how frequently it appears among community r's K-1 interactions. If we express these frequencies as probabilities,  $P_a$ ,  $P_c$ ,  $P_p$ , and  $P_d$  (subscripts indicate "assortative", "core", "periphery", and "disassortative" motif frequencies, respectively), we can then calculate an entropy:

$$H_r = -[P_a \log_2 P_a + P_c \log_2 P_c + P_p \log_2 P_p + P_d \log_2 P_d].$$
(4)

This entropy is zero if community r participates in only one motif class and is maximized when rparticipates in all classes equally. We then assign this score to all nodes  $i \in r$ . The resulting vector of length  $[N \times 1]$  specifies the single-partition diversity index for each node. We can calculate this vector for all K-community partitions and estimate mean diversity indices for each node by averaging across partitions."

### 1482 Comment 23

The macaque connectome results seem to show the opposite trade in terms of being assigned to maximally assortative set as rich club and non-rich club members (Fig. S4O). Do the authors have any speculative idea on what may be the reason for this opposite trade?

The macaque connectome is peculiar in several ways, all of which could lead to atypical results. First, it is the smallest network we study. Consequently, the network's global structure can be disproportionately influenced by the behavior of one or two nodes. Second, whereas the other networks are either whole-brain or whole-hemisphere, the macaque network is incomplete; connectivity information is available for 29 of 93 total nodes. This means that macaque network properties will likely change as more data becomes available.

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Reviewers' comments:

Reviewer #1 (Remarks to the Author):

The authors responded to the reviewer comments thoroughly and, as a result, the manuscript is much stronger. I have a few minor comments, but no remaining substantial concerns.

Your reference to supplementary figures in the main text needs to be updated to reflect additional figures.

In the Results section "Connectomes support diverse meso-scale architecture", I believe that the asterisks in Figure 3A represent 1-tailed t-tests for each K relating VI(Qmax-WSBM) to the average of VI(Qmax) and VI(WSBM). Given how much higher VI(WSBM) is, that seems misleading. If you conduct 1-tailed t-tests relating VI(Qmax-WSBM) to VI(WSBM), and also VI(Qmax) to VI(WSBM), are there consistent significant differences across K? A conclusion that Qmax results in more consistent partitions than WSBM or the Qmax-WSBM comparison is different than Qmax and WSBM both result in equivalently consistent partitions that are different from each other. I realize there is some variability in the other connectomes, but of the other four, it looks like 2/4 show similar results (where VI(Qmax-WSBM) and VI(WSBM) are relatively similar), and the other 2 do in a K-dependent manner (Figure S5).

Also in the Results section, in "Functional relevance of the WSBM", I think this sentence should be rephrased: "A strictly assortative brain is aligned with the hypothesis that the brain is composed of communities operating independently, while a brain that allows for some non-assortative communities implies that brain function arises not solely from contributions of independent communities, but from the interactions between communities." No one would argue that Qmax would ever find that a brain is "strictly assortative", or has zero connections across communities. Brain community structure derived from Qmax would find that brain function arises both from contributions of independent communities, as well as interactions across those communities. Even if all communities are assortative, they are not strictly assortative with no between-network connections. Perhaps rephrase to emphasize that WSBM-derived partitions allow for more types of interactions that are thought to be important for brain function. Further, I still think this section could use some clarification. I believe the point, which is not explicitly stated, is that both algorithms maximize within > between connectivity, so the algorithm that matches it is assumed to more accurately reflect true underlying connectivity. If a statement like this is the last sentence of the last paragraph on page 7, it will make that last logical step more clear to the readers.

Figure 6: I appreciate the clarification about the existence of disassortative communities from your response to the reviews and more opaque coloring of the disassortative communities in 6D. I think that you should explicitly state the value of WBSM-Qmax disassortative communities in 6E, since it looks like the value is 0 even though in your response you mentioned that it is slightly positive. Including that in the caption would clarify.

Reviewer #2 (Remarks to the Author):

I thank the authors for their comprehensive and very clear response to my prior concerns.

Reviewer #3 (Remarks to the Author):

In the revised version, I see that the authors included two major revisions:

1) comparison of the main results to those of a randomised network,

2) comparison of the main results to those of different parcellations.

In my opinion, these new extensions of the validation, clearly improve the quality of the analysis. The conclusions drawn from the randomized network analysis support the general hypothesis of the paper quite nicely; i.e. that the brain networks show some level of disassortativity, which, as shown with this new comparison, is not as severe as in random networks. Although, the comparison across different parcellations yields insignificant correlations between the results of different parcellations, there exist positive correlations and the insignificance can be attributed to the small number of samples as claimed by the authors.

Based on the new clarifications of the authors, my major concern is however, the seeming lack of convergence of WSBM (and potentially also of Qmax) across different trials:

In their response to my previous Comment 3, the authors state: 'Because both Qmax and the WSBM algorithms are non-deterministic – i.e. repeated runs of the algorithm usually result in slightly different solutions – we computed VI between pairs of partitions uncovered using the same community detection algorithm and also between algorithms. We now clarify this in the manuscript and figure caption. In the section Connectomes support diverse meso-scale architecture we now include the statement: "Specifically, we computed VI separately for three different subsets of partitions: partitions detected using WSBM with other WSBM partitions; partitions detected using Qmax with other Qmax partitions; partitions detected using the WSBM with Qmax partitions."

Firstly, the newly added part and the Figure caption do not clearly state what the authors explain in their reply to the comment. For clarity of presentation and to aid the understanding of the general reader, I would suggest stating clearly in the manuscript, as in their reply above, such as: 'As both Qmax and the WSBM algorithms are non-deterministic – i.e. repeated runs of the algorithm usually result in slightly different solutions – we run both algorithms <nr of trials> times and computed VI between pairs of partitions across different trials uncovered using the same community detection algorithm and also between algorithms.'

Secondly, the large within-technique differences across different trials of WSBM algorithm (see my previous Comment 4) naturally raise the question about the potential lack of convergence of the algorithm. I assume, as in all non-deterministic algorithms, although the method may be expected to yield slightly different results, if it converges, these differences are not expected to vary dramatically.

Furthermore, in their replies to my previous comments 8 and 13, the authors state: 'We chose not to order the matrix by partitions detected by either WSBM or Qmax because there were thousands of such partitions and choosing a representative partition from among those was not trivial.'

'We appreciate the reviewer's attention to detail. In this case, the purple community and its relatively small size is a result of the stochasticity of the WSBM algorithm. That is, in attempting to optimize their respective objective functions, the output of both the WSBM and Qmax will vary somewhat. The communities shown in Figure 2 represent the outputs of single runs of the algorithm and should not be treated as necessarily representative of the network's ground truth communities. It is not difficult to identify a different partition of the same network into the same number of communities with comparably-sized communities. To demonstrate this, we show an alternative partition of the network

into five communities. Specifically, we chose the partition with the most similarly-sized communities. We have also replaced the WSBM partition in Figure 2 with the communities shown here.'

The communities in Figure 14 in the response to reviews and Figure 2 in the current manuscript seem more anatomically and functionally meaningful to me. However, the significant variation between different community assignments (see Figure 2 in the current and previous versions of the manuscript) resulting from two different runs of the same algorithm with the same initial parameters as well as the statement that any such partitioning could not be considered representative raise my concern about the potential lack of convergence and the reliability of the results. Can the authors please clarify this?

### Minor comments:

- Page 3, in the newly added paragraph: 'Higher order cognitive processes, for example, are thought to emerge through integration of information originating in different brain systems [44], which can only occur via the interaction of communities with one another.' I wouldn't include the word "only" here, as the exact mechanism underlying the integration of information in the brain is currently unknown and there may be other possibilities than the one-to-one interaction between communities, as claimed here.

- Figure 3F: please state that the upper and lower limits of each box represent the 25th and 75th percentiles of each system's assortativity in the figure caption.

- Page 7, Functional relevance of the WSBM: "In the past when empirical estimates of FC could not be easily obtained, measures of similarity between brain regions' connectivity profiles (e.g., matching index) have been used as a stand-in [27, 28, 29]" Why would they not be easily obtained, as the FC estimates are simple correlations between different brain regions. Do the authors maybe mean 'before the empirical estimates of FC have been discovered'?

- Supplementary material, Page 9: '... and calculated the correlation of all system-level scores, obtaining coefficients of r=0.32 and r=32 (p<0.01)'. I believe r=32 is a typo here.

- Figure S7: The abbreviations RC and nonRC used in the figure caption are not defined in the supplementary material as rich club and non-rich club.

# <sup>28</sup> Reviewer #1

<sup>29</sup> The authors responded to the reviewer comments thoroughly and, as a result, the manuscript is much stronger.

- <sup>30</sup> I have a few minor comments, but no remaining substantial concerns.
- 31

32

 $_{\tt 33}$   $\,$  We thank the reviewer for the positive remark.

# <sup>34</sup> Comment 1

<sup>35</sup> Your reference to supplementary figures in the main text needs to be updated to reflect additional figures.

36 37

We apologize for this oversight. We now include references to the new supplementary figures throughout the main text and make sure that each Supplementary Figure is called out. In the beginning of the **Results** section (p.4), we now note that Figures S1 - S3 deal with null models and that we also test a cellular level, *C. elegans* network, and present the results in Figures S13 - S14. Later in the sections **Many (but not all)** munities are assortative and **Behavioral relevance of motif diversity** we now call out Figures

<sup>43</sup> S12, S15 - S17, which discuss rich clubs and the influence of brain parcellation.

# 44 Comment 2

In the Results section "Connectomes support diverse meso-scale architecture", I believe that the asterisks 45 in Figure 3A represent 1-tailed t-tests for each K relating VI(Qmax-WSBM) to the average of VI(Qmax) 46 and VI(WSBM). Given how much higher VI(WSBM) is, that seems misleading. If you conduct 1-tailed 47 t-tests relating VI(Qmax-WSBM) to VI(WSBM), and also VI(Qmax) to VI(WSBM), are there consistent 48 significant differences across K? A conclusion that Qmax results in more consistent partitions than WSBM 49 or the Qmax-WSBM comparison is different than Qmax and WSBM both result in equivalently consistent 50 partitions that are different from each other. I realize there is some variability in the other connectomes, 51 but of the other four, it looks like 2/4 show similar results (where VI(Qmax-WSBM) and VI(WSBM) are 52 relatively similar), and the other 2 do in a K-dependent manner (Figure S5). 53 54 55

<sup>56</sup> We apologize for any confusion. The tests performed in the main text were, in fact, two separate 1-tailed <sup>57</sup> *t*-tests: the first compared VI( $Q_{max}$ ) with VI( $Q_{max}$ ,WSBM) while the second compared VI(WSBM) with <sup>58</sup> VI(Qmax,WSBM). The asterisks represent values of *K* at which *both* tests were statistically significant. <sup>59</sup> The reviewer is correct in noting that there are cases where the difference in means of VI(WSBM) and <sup>60</sup> VI( $Q_{max}$ ,WSBM) are small, but because each group comprises 250<sup>2</sup> elements, the *t*-tests are powered enough <sup>61</sup> discern statistical differences. We have now added additional clarifying remarks:

<sup>62</sup> In the section Connectomes support diverse meso-scale architecture:

• This procedure resulted in a series of within- and between- technique VI scores as a function of K. At 63 each K, we computed one-tailed t-tests to assess whether the mean within-technique dissimilarity of 64 partitions detected with either the WSBM or  $Q_{max}$  was smaller than the between-technique dissimi-65 larity. We observed that from  $K = 2, \ldots, 9$ , both the WBSM and  $Q_{max}$  uncovered partitions that were 66 self-consistent yet distinct from one another (maximum  $p < 10^{-15}$ ) (Note: asterisks in Fig. 3A indicate 67 that both t-tests were statistically significant). This observation was consistent across the non-human 68 connectome data as well (Fig. S5), confirming that the WSBM and  $Q_{max}$  generate statistically different 69 estimates of connectome community structure. 70

The reviewer's comments also speak more broadly to the issue of variability in the partitions detected by the WSBM and are therefore similar to Comment 2 made by Reviewer #3 concerning the performance of the WSBM algorithm. To address this point, we have provided two additional analyses of the human connectome dataset. First, we demonstrate qualitatively and visually that partitions detected using the WSBM are similar to one another. Second, we use statistical methods to quantify the observed level of <sup>76</sup> similarity and show that it is much greater than what would be expected under a permutation-based null
 <sup>77</sup> model. These results demonstrate that the WSBM partitions are statistically reliable, supporting the use of
 <sup>78</sup> the WSBM for community detection in network neuroscience.

In the main text we used the WSBM to partition brain networks into K = 2, ..., 10 communities. Because 79 the WSBM algorithm was non-deterministic, we ran it multiple times from different initial conditions (250 80 repetitions), generating partition ensembles at each value of K. Here, we provide visual evidence suggesting 81 that the partitions comprising each ensemble are, in fact, similar to one another. Specifically, we compute 82 for each partition ensemble its association matrix,  $\mathbf{T} \in \mathbb{R}^{N \times N}$ , whose element,  $T_{ij}$ , is equal to the fraction 83 of partitions in which nodes, i and j, are assigned to the same community. If partitions were dissimilar to 84 one another, the association matrix would exhibit no structure. In Figure 3 we show examples of association 85 matrices generated from partitions obtained using the WSBM. Note that these matrices exhibit structure in 86 the form of non-uniform community co-assignment, providing visual confirmation that partitions generated 87 by the WSBM are relatively consistent across multiple runs of the algorithm. 88

Next, we quantify the average similarity of partitions to one another and show that this level of similarity 89 is much greater than what is expected by chance. As in the main text, we use variation of information (VI) 90 to quantify the similarity of two partitions to one another. We define the average similarity of each partition 91 ensemble as the mean pairwise VI across all possible pairs of partitions. To show that the detected partitions 92 are more similar to one another than expected by chance, we compare the observed mean pairwise VI of 93 each partition ensemble against a null distribution generated by a permutation-based null model in which 94 a node's community assignment is swapped with that of another in the same partition with probability r. 95 We vary the value of r from  $r \approx 0.0017$  to r = 1 in 30 logarithmically-spaced steps and generate 100 null 96 values at each step. We then perform one-tailed non-parametric t-tests that the observed mean pairwise VI 97 is less than that of the null distribution and find that even when r is small, the observed value is statistically 98 smaller than expected by chance  $(p < 10^{-2}; \text{ corrected for multiple comparisons with a false-discovery rate$ 99 of 0.05) (Fig. 4). These results provide statistical evidence that the partitions detected using the WSBM 100 are, in fact, more similar to one another than expected. These results extend and complement the visual 101 evidence presented earlier. 102

Finally, it is worth noting that there are some reasons that we might expect partitions detected using the WSBM to be more variable than those detected using  $Q_{max}$ . Both algorithms are tasked with estimating nodes' community assignments. This problem is, of course, computationally intractable for all but the most trivial cases [1]. However, the problem is compunded for the WSBM, which must also estimate for every pair of communities a binary connection probability and the mean/variance of edges that fall between those communities. All else being equal, this means that the space of possible solutions is much larger for the WSBM than  $Q_{max}$ , leading to many near-optimal solutions on repeated runs.

110 111

<sup>112</sup> We include these analyses in the Supplementary Material:

Here we summarize additional analyses of the human connectome dataset to characterize the variance of solutions obtained using the WSBM. First, we demonstrate qualitatively and visually that partitions detected using the WSBM are similar to one another. Second, we use statistical methods to quantify the observed level of similarity and show that it is much greater than what would be expected under a permutation-based null model. These results demonstrate that the WSBM partitions are statistically reliable, supporting the use of the WSBM for community detection in network neuroscience.

In the main text we used the WSBM to partition brain networks into  $K = 2, \ldots, 10$  communities. 119 Because the WSBM algorithm was non-deterministic, we ran it multiple times from different initial 120 conditions (250 repetitions), generating partition ensembles at each value of K. Here, we provide 121 visual evidence suggesting that the partitions comprising each ensemble are, in fact, similar to one 122 another. Specifically, we compute for each partition ensemble its association matrix,  $\mathbf{T} \in \mathbb{R}^{N \times N}$ 123 whose element,  $T_{ij}$ , is equal to the fraction of partitions in which nodes, i and j, are assigned to the 124 same community. If partitions were dissimilar to one another, the association matrix would exhibit no 125 structure. In Figure 3 we show examples of association matrices generated from partitions obtained 126 using the WSBM. Note that these matrices exhibit structure in the form of non-uniform community 127 co-assignment, providing visual confirmation that partitions generated by the WSBM are relatively 128



Figure 1: Association matrices computed from partitions output by WSBM. Each panel depicts a square, brain region × brain region association matrix, whose elements indicate the fraction of all partitions in which two nodes were co-assigned to the same community. Brain areas are ordered according to a randomly selected partition. Sub-panels correspond to different numbers of communities, K = 2, ..., 10.

### <sup>129</sup> consistent across multiple runs of the algorithm.

Next, we quantify the average similarity of partitions to one another and show that this level of 130 similarity is much greater than what is expected by chance. As in the main text, we use variation of 131 information (VI) to quantify the similarity of two partitions to one another. We define the average 132 similarity of each partition ensemble as the mean pairwise VI across all possible pairs of partitions. 133 To show that the detected partitions are more similar to one another than expected by chance, we 134 compare the observed mean pairwise VI of each partition ensemble against a null distribution generated 135 by a permutation-based null model in which a node's community assignment is swapped with that of 136 another in the same partition with probability r. We vary the value of r from  $r \approx 0.0017$  to r = 1 in 137 30 logarithmically-spaced steps and generate 100 null values at each step. We then perform one-tailed 138 non-parametric t-tests that the observed mean pairwise VI is less than that of the null distribution 139 and find that even when r is small, the observed value is statistically smaller than expected by chance 140  $(p < 10^{-2})$ ; corrected for multiple comparisons with a false-discovery rate of 0.05) (Fig. 4). These results 141 provide statistical evidence that the partitions detected using the WSBM are, in fact, more similar 142 to one another than expected. These results extend and complement the visual evidence presented 143 earlier. 144

<sup>145</sup> Finally, it is worth noting that there are some reasons that we might expect partitions detected using



Figure 2: Mean pairwise variation of information (VI) of original and randomized partitions. For a given number of communities, K, we estimated the mean pairwise VI, which serves as a measure of partition similarity. Lower values of VI imply greater similarity. The VI of the original partitions is shown as a red line. Using a parameterized permutation-based null model, we generate randomized partitions and compute null distributions for the mean pairwise VI. For all values of K = 2, ..., 10, and for all parameter values, even small changes to community assignments result in statistically significant increases in mean pairwise VI. These observations support the hypothesis that the WSBM algorithm is converging to a set of solutions that are consistent and self-similar.

the WSBM to be more variable than those detected using  $Q_{max}$ . Both algorithms are tasked with estimating nodes' community assignments. This problem is, of course, computationally intractable for all but the most trivial cases [1]. However, the problem is compunded for the WSBM, which must also estimate for every pair of communities a binary connection probability and the mean/variance of edges that fall between those communities. All else being equal, this means that the space of possible solutions is much larger for the WSBM than  $Q_{max}$ , leading to many near-optimal solutions on repeated runs.

<sup>153</sup> We also call out these analyses and figures in the main text in the section Weighted stochastic block-<sup>154</sup> model:

• We explore the convergence of the WSBM across multiple repetitions and the similarity of detected partitions in the **Supplementary Material** (Figs. S18, S19).

### 157 Comment 3

Also in the Results section, in "Functional relevance of the WSBM", I think this sentence should be rephrased: "A strictly assortative brain is aligned with the hypothesis that the brain is composed of communities operating independently, while a brain that allows for some non-assortative communities implies that brain function arises not solely from contributions of independent communities, but from the interactions between communities." No one would argue that Qmax would ever find that a brain is "strictly assortative", or has zero connections across communities. Brain community structure derived from Qmax would find that brain

function arises both from contributions of independent communities, as well as interactions across those com-164 munities. Even if all communities are assortative, they are not strictly assortative with no between-network 165 connections. Perhaps rephrase to emphasize that WSBM-derived partitions allow for more types of interac-166 tions that are thought to be important for brain function. Further, I still think this section could use some 167 clarification. I believe the point, which is not explicitly stated, is that both algorithms maximize within >168 between connectivity, so the algorithm that matches it is assumed to more accurately reflect true underlying 169 connectivity. If a statement like this is the last sentence of the last paragraph on page 7, it will make that 170 last logical step more clear to the readers. 171

172 173

We agree with the reviewer that even when brain network communities are assortative, in practice we tend to find a small fraction of brain areas whose links span communities. The point that we intended to make was that non-assortative community structure implies that there exist entire *groups* of brain areas (not just individual areas) whose collective connectivity pattern may predispose them to integrative function, rather than functioning in isolation. The reviewr is also correct in noting that both algorithms, in theory, detect communities that we would expect to exhibit greater within-community *functional* connectivity than between.

<sup>181</sup> In line with the reviewer's suggestion, we have added clarifying remarks to this section.

• Though via different mechanisms, both the WSBM and  $Q_{max}$  produce communities composed of 182 brain regions with similar patterns of incoming and outgoing connections and so we would expect the 183 resulting communities to be internally dense in terms of functional connectivity. In the case of  $Q_{max}$ , 184 this similarity is entirely incidental – nodes get grouped into internally dense, mutually-connected 185 clusters, inflating their similarity. The WSBM, on the other hand, explicitly defines communities as 186 clusters of nodes whose connections were generated by the same statistical process; by definition pairs 187 of nodes in the same community will have similar connectivity patterns even if they, themselves, are 188 not directly connected. 189

• Because the similarity of regions' structural connectivity is associated with strong functional connectiv-190 ity, we expect that two nodes in the same community should be more strongly functionally connected 191 to one another than two nodes in different communities, irrespective of which technique was used to de-192 fine the communities. However, the WSBM and  $Q_{max}$  represent vastly different hypotheses about how 193 brain networks function. An assortative brain is aligned with the hypothesis that communities function 194 and process information relatively independently from one another, while a brain that allows for some 195 non-assortative communities implies that function arises not solely from contributions of independent 196 communities, but from the interactions between communities. Whereas past work has emphasized the 197 assortative model of brain function, in which integration is performed by a few outlying nodes whose 198 connections span community boundaries, the non-assortative model holds that integration is funda-199 mentally a community-level action performed by clusters of brain areas with similar (non-assortative) 200 connectivity profiles. 201

# 202 Comment 4

Figure 6: I appreciate the clarification about the existence of disassortative communities from your response to the reviews and more opaque coloring of the disassortative communities in 6D. I think that you should explicitly state the value of WBSM-Qmax disassortative communities in 6E, since it looks like the value is 0 even though in your response you mentioned that it is slightly positive. Including that in the caption would clarify.

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<sup>210</sup> We have now included a clarifying remark in the caption of Figure 6D.

• Note: The WSBM does, in fact, generate a small fraction of disassortative communities and so points on the red curves in *D* and *E* are not equal to zero.

# 213 Reviewer #2

<sup>214</sup> I thank the authors for their comprehensive and very clear response to my prior concerns.

215 216

<sup>217</sup> We appreciate the reviewer's response.

# 218 Reviewer #3

<sup>219</sup> In the revised version, I see that the authors included two major revisions:

• comparison of the main results to those of a randomised network.

• comparison of the main results to those of different parcellations.

In my opinion, these new extensions of the validation, clearly improve the quality of the analysis. The conclusions drawn from the randomized network analysis support the general hypothesis of the paper quite nicely; i.e. that the brain networks show some level of disassortativity, which, as shown with this new comparison, is not as severe as in random networks. Although, the comparison across different parcellations yields insignificant correlations between the results of different parcellations, there exist positive correlations and the insignificance can be attributed to the small number of samples as claimed by the authors.

Based on the new clarifications of the authors, my major concern is however, the seeming lack of convergence of WSBM (and potentially also of Qmax) across different trials:

In their response to my previous Comment 3, the authors state: "Because both Qmax and the WSBM 230 algorithms are non-deterministic *i.e.* repeated runs of the algorithm usually result in slightly different solu-231 tions we computed VI between pairs of partitions uncovered using the same community detection algorithm 232 and also between algorithms. We now clarify this in the manuscript and figure caption. In the section Con-233 nectomes support diverse meso-scale architecture we now include the statement: "Specifically, we computed 234 VI separately for three different subsets of partitions: partitions detected using WSBM with other WSBM 235 partitions; partitions detected using Qmax with other Qmax partitions; partitions detected using the WSBM 236 with Qmax partitions." 237

# 238 Comment 1

Firstly, the newly added part and the Figure caption do not clearly state what the authors explain in their reply to the comment. For clarity of presentation and to aid the understanding of the general reader, I would suggest stating clearly in the manuscript, as in their reply above, such as: "As both Qmax and the WSBM algorithms are non-deterministic i.e. repeated runs of the algorithm usually result in slightly different solutions we run both algorithms <nr of trials> times and computed VI between pairs of partitions across different trials uncovered using the same community detection algorithm and also between algorithms."

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We apologize for the lack of clarification and agree with the reviewer that the manuscript should clearly reflect the number of trials and partition pairs over which VI was computed. We have now included the following statement in the main text:

<sup>250</sup> In the first paragraph of **Results**:

- As both the  $Q_{max}$  and WSBM algorithms are non-deterministic i.e. repeated runs of the algorithm usually result in slightly different solutions – we varied the number of communities from K = 2 to K = 10 and repeated both algorithms 250 times for each K.
- And in the section **Connectomes support diverse meso-scale structure**:
- Specifically, we computed pairwise VI among all 250 partitions detected using  $Q_{max}$  and separately for partitions detected using the WSBM. We also computed pairwise VI between the 250  $Q_{max}$  partitions and the 250 WSBM partitions. This process was repeated separately for different values of K, the number of detected communities, which made the comparison as fair as possible.

### 259 Comment 2

Secondly, the large within-technique differences across different trials of WSBM algorithm (see my previous
 Comment 4) naturally raise the question about the potential lack of convergence of the algorithm. I assume,

as in all non-deterministic algorithms, although the method may be expected to yield slightly different results,

<sup>263</sup> *if it converges, these differences are not expected to vary dramatically.* 

Furthermore, in their replies to my previous comments 8 and 13, the authors state: "We chose not to order the matrix by partitions detected by either WSBM or Qmax because there were thousands of such partitions and choosing a representative partition from among those was not trivial."

"We appreciate the reviewer"s attention to detail. In this case, the purple community and its relatively 267 small size is a result of the stochasticity of the WSBM algorithm. That is, in attempting to optimize their 268 respective objective functions, the output of both the WSBM and Qmax will vary somewhat. The communities 269 shown in Figure 2 represent the outputs of single runs of the algorithm and should not be treated as necessarily 270 representative of the network"s ground truth communities. It is not difficult to identify a different partition of 271 the same network into the same number of communities with comparably-sized communities. To demonstrate 272 this, we show an alternative partition of the network into five communities. Specifically, we chose the partition 273 with the most similarly-sized communities. We have also replaced the WSBM partition in Figure 2 with the 274 communities shown here." 275

The communities in Figure 14 in the response to reviews and Figure 2 in the current manuscript seem more anatomically and functionally meaningful to me. However, the significant variation between different community assignments (see Figure 2 in the current and previous versions of the manuscript) resulting from two different runs of the same algorithm with the same initial parameters as well as the statement that any such partitioning could not be considered representative raise my concern about the potential lack of convergence and the reliability of the results. Can the authors please clarify this?

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We agree with the reviewer that the convergence of the WSBM algorithm is an important technical point 284 and one that we wish to clarify. We also note that the Reviewer's comment – dealing with the variability 285 of optimal partitions – is similar to Comment 2 made by Reviewer #1. Here, the reviewer asks whether 286 the WSBM is arriving at dissimilar solutions over different runs. To address this point, we have provided 287 two additional analyses of the human connectome dataset. First, we demonstrate qualitatively and visually 288 that partitions detected using the WSBM are similar to one another. Second, we use statistical methods 289 to quantify the observed level of similarity and show that it is much greater than what would be expected 290 under a permutation-based null model. These results demonstrate that the WSBM partitions are statistically 291 reliable, supporting the use of the WSBM for community detection in network neuroscience. 292

In the main text we used the WSBM to partition brain networks into  $K = 2, \ldots, 10$  communities. Because 293 the WSBM algorithm was non-deterministic, we ran it multiple times from different initial conditions (250) 294 repetitions), generating partition ensembles at each value of K. Here, we provide visual evidence suggesting 295 that the partitions comprising each ensemble are, in fact, similar to one another. Specifically, we compute 296 for each partition ensemble its association matrix,  $\mathbf{T} \in \mathbb{R}^{N \times N}$ , whose element,  $T_{ij}$ , is equal to the fraction 297 of partitions in which nodes, i and j, are assigned to the same community. If partitions were dissimilar to 298 one another, the association matrix would exhibit no structure. In Figure 3 we show examples of association 299 matrices generated from partitions obtained using the WSBM. Note that these matrices exhibit structure in 300 the form of non-uniform community co-assignment, providing visual confirmation that partitions generated 301 by the WSBM are relatively consistent across multiple runs of the algorithm. 302

Next, we quantify the average similarity of partitions to one another and show that this level of similarity 303 is much greater than what is expected by chance. As in the main text, we use variation of information (VI) 304 to quantify the similarity of two partitions to one another. We define the average similarity of each partition 305 ensemble as the mean pairwise VI across all possible pairs of partitions. To show that the detected partitions 306 are more similar to one another than expected by chance, we compare the observed mean pairwise VI of 307 each partition ensemble against a null distribution generated by a permutation-based null model in which 308 a node's community assignment is swapped with that of another in the same partition with probability r. 309 We vary the value of r from  $r \approx 0.0017$  to r = 1 in 30 logarithmically-spaced steps and generate 100 null 310 values at each step. We then perform one-tailed non-parametric t-tests that the observed mean pairwise VI 311



Figure 3: Association matrices computed from partitions output by WSBM. Each panel depicts a square, brain region × brain region association matrix, whose elements indicate the fraction of all partitions in which two nodes were co-assigned to the same community. Brain areas are ordered according to a randomly selected partition. Sub-panels correspond to different numbers of communities, K = 2, ..., 10.

<sup>312</sup> is less than that of the null distribution and find that even when r is small, the observed value is statistically <sup>313</sup> smaller than expected by chance ( $p < 10^{-2}$ ; corrected for multiple comparisons with a false-discovery rate <sup>314</sup> of 0.05) (Fig. 4). These results provide statistical evidence that the partitions detected using the WSBM <sup>315</sup> are, in fact, more similar to one another than expected. These results extend and complement the visual <sup>316</sup> evidence presented earlier.

Finally, it is worth noting that there are some reasons that we might expect partitions detected using the WSBM to be more variable than those detected using  $Q_{max}$ . Both algorithms are tasked with estimating nodes' community assignments. This problem is, of course, computationally intractable for all but the most trivial cases [1]. However, the problem is compunded for the WSBM, which must also estimate for every pair of communities a binary connection probability and the mean/variance of edges that fall between those communities. All else being equal, this means that the space of possible solutions is much larger for the WSBM than  $Q_{max}$ , leading to many near-optimal solutions on repeated runs.

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<sup>326</sup> We include these analyses in the Supplementary Material:

• Here we summarize additional analyses of the human connectome dataset to characterize the variance of solutions obtained using the WSBM. First, we demonstrate qualitatively and visually that partitions



Figure 4: Mean pairwise variation of information (VI) of original and randomized partitions. For a given number of communities, K, we estimated the mean pairwise VI, which serves as a measure of partition similarity. Lower values of VI imply greater similarity. The VI of the original partitions is shown as a red line. Using a parameterized permutation-based null model, we generate randomized partitions and compute null distributions for the mean pairwise VI. For all values of K = 2, ..., 10, and for all parameter values, even small changes to community assignments result in statistically significant increases in mean pairwise VI. These observations support the hypothesis that the WSBM algorithm is converging to a set of solutions that are consistent and self-similar.

detected using the WSBM are similar to one another. Second, we use statistical methods to quantify the observed level of similarity and show that it is much greater than what would be expected under a permutation-based null model. These results demonstrate that the WSBM partitions are statistically reliable, supporting the use of the WSBM for community detection in network neuroscience.

In the main text we used the WSBM to partition brain networks into  $K = 2, \ldots, 10$  communities. 333 Because the WSBM algorithm was non-deterministic, we ran it multiple times from different initial 334 conditions (250 repetitions), generating partition ensembles at each value of K. Here, we provide 335 visual evidence suggesting that the partitions comprising each ensemble are, in fact, similar to one 336 another. Specifically, we compute for each partition ensemble its association matrix,  $\mathbf{T} \in \mathbb{R}^{N \times N}$ 337 whose element,  $T_{ij}$ , is equal to the fraction of partitions in which nodes, i and j, are assigned to the 338 same community. If partitions were dissimilar to one another, the association matrix would exhibit no 339 structure. In Figure 3 we show examples of association matrices generated from partitions obtained 340 using the WSBM. Note that these matrices exhibit structure in the form of non-uniform community 341 co-assignment, providing visual confirmation that partitions generated by the WSBM are relatively 342 consistent across multiple runs of the algorithm. 343

Next, we quantify the average similarity of partitions to one another and show that this level of similarity is much greater than what is expected by chance. As in the main text, we use variation of information (VI) to quantify the similarity of two partitions to one another. We define the average similarity of each partition ensemble as the mean pairwise VI across all possible pairs of partitions. To show that the detected partitions are more similar to one another than expected by chance, we

compare the observed mean pairwise VI of each partition ensemble against a null distribution generated 349 by a permutation-based null model in which a node's community assignment is swapped with that of 350 another in the same partition with probability r. We vary the value of r from  $r \approx 0.0017$  to r = 1 in 351 30 logarithmically-spaced steps and generate 100 null values at each step. We then perform one-tailed 352 non-parametric t-tests that the observed mean pairwise VI is less than that of the null distribution 353 and find that even when r is small, the observed value is statistically smaller than expected by chance 354  $(p < 10^{-2})$ ; corrected for multiple comparisons with a false-discovery rate of 0.05) (Fig. 4). These results 355 provide statistical evidence that the partitions detected using the WSBM are, in fact, more similar 356 to one another than expected. These results extend and complement the visual evidence presented 357 earlier. 358

Finally, it is worth noting that there are some reasons that we might expect partitions detected using 359 the WSBM to be more variable than those detected using  $Q_{max}$ . Both algorithms are tasked with 360 estimating nodes' community assignments. This problem is, of course, computationally intractable for 361 all but the most trivial cases [1]. However, the problem is compunded for the WSBM, which must 362 also estimate for every pair of communities a binary connection probability and the mean/variance of 363 edges that fall between those communities. All else being equal, this means that the space of possible 364 solutions is much larger for the WSBM than  $Q_{max}$ , leading to many near-optimal solutions on repeated 365 runs. 366

We also call out these analyses and figures in the main text in the section Weighted stochastic blockmodel:

• We explore the convergence of the WSBM across multiple repetitions and the similarity of detected

partitions in the **Supplementary Material** (Figs. S18, S19).

# 371 Comment 2

Page 3, in the newly added paragraph: "Higher order cognitive processes, for example, are thought to emerge through integration of information originating in different brain systems [44], which can only occur via the interaction of communities with one another." I wouldn't include the word "only" here, as the exact mechanism underlying the integration of information in the brain is currently unknown and there may be other possibilities than the one-to-one interaction between communities, as claimed here.

377 378

 $_{\rm 379}$   $\,$  We agree with the reviewer and have made the suggested change.

# 380 Comment 3

Figure 3F: please state that the upper and lower limits of each box represent the 25th and 75th percentiles of each system's assortativity in the figure caption.

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384

<sup>385</sup> We have followed the reviewers's suggestion and now define the limits of the box in each plot.

• The limits of each box represent the interquartile range (25th and 75th percentiles).

# 387 Comment 4

Page 7, Functional relevance of the WSBM: "In the past when empirical estimates of FC could not be easily obtained, measures of similarity between brain regions" connectivity profiles (e.g., matching index) have been used as a stand-in [27, 28, 29]" Why would they not be easily obtained, as the FC estimates are simple correlations between different brain regions. Do the authors maybe mean "before the empirical estimates of FC have been discovered"?

393 394 The "matching index" and other metrics that quantified the structural overlap of connections have been, in the past, used as stand-ins for FC or the functional relatedness of brain areas with respect to one another. The usage of these metrics predates the now widespread practice of estimating functional connectivity empirically from the correlation of activity time series. We now note this more clearly.

<sup>399</sup> The passage now reads:

• In the past before it was common to empirically estimate FC as the correlation of neural activity,

measures of similarity between brain regions' connectivity profiles (e.g., matching index) were used as
 a stand-in.

## 403 Comment 4

Supplementary material, Page 9: "... and calculated the correlation of all system-level scores, obtaining coefficients of r=0.32 and r=32 (p<0.01)". I believe r=32 is a typo here.

406 407

The reviewer is correct: this was a typographical error leaving out the decimal point. By coincidence, the correlation coefficients were both r = 0.32.

# 410 Comment 6

Figure S7: The abbreviations RC and nonRC used in the figure caption are not defined in the supplementary material as rich club and non-rich club.

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415 We have updated the caption to indicate what RC and non-RC refer to.

• The labels RC and non-RC used in panels *C*,*G*,*K*,*O* indicate nodes that were assigned to or not assigned to putative rich clubs See **Rich club estimation** for more details.

# 418 References

[1] Santo Fortunato. Community detection in graphs. *Physics reports*, 486(3):75–174, 2010.

## REVIEWERS' COMMENTS:

Reviewer #1 (Remarks to the Author):

The authors thoroughly responded to this most recent round of reviews and I have no further comments. When published, this article will make an important contribution to the literature.

Reviewer #3 (Remarks to the Author):

I thank the authors for addressing my raised concerns and attending my suggestions. I believe the newly added analysis nicely shows the convergence of the WSBM, which was my major question. I do not have any further comments or questions.

Dear Reviewers and Editor,

The referees raised no additional comments/questions in this last round of review (we include their final remarks, below). We thank them and the editor for their suggestions throughout the review process. As a result, the manuscript has been improved substantially.

Sincerely, The authors

Reviewer #1 (Remarks to the Author):

The authors thoroughly responded to this most recent round of reviews and I have no further comments. When published, this article will make an important contribution to the literature.

Reviewer #3 (Remarks to the Author):

I thank the authors for addressing my raised concerns and attending my suggestions. I believe the newly added analysis nicely shows the convergence of the WSBM, which was my major question. I do not have any further comments or questions.