Supplementary Information

What dictates soft clay-like Lithium superionic conductor formation from rigid-salts mixture

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Supplementary Note 1: Training, validating, and benchmarking DeepMD PE model

Supplementary Note 1.1: Training the DeepMD PE model

To train the DeepMD PE model, atomic configurations of 13 stable crystalline phases (unary, binary, and ternary), marked red, in the Ga-F-Li-Cl quaternary chemical space (Supplementary Figure 1 a-d) along with slab-like structures of LiCI|GaF₃ with different thicknesses (Supplementary Figure 1 e-g) were used. The slab-like structures were constructed from multilayer slabs of $[001]$ LiCl and $[001]$ GaF₃, which were vertically interfaced "|", and separated by 3 Å. A maximum strain of \sim 5 % was applied to match the lattice constants of LiCl and GaF₃ slabs in the LiCl $|GaF_3$ geometry. The training data consisted of atomic configurations obtained by melting and quenching the different systems (specified in Supplementary Figure 1 and Supplementary Table 1) using AIMD simulations with parameters listed (see Notes) in Supplementary Table 1. In total, over 700k AIMD frames were generated, out of which 250k atomic configurations were randomly selected to train the DeepMD model. Among the 250k configurations, 80% of them were used for training and 20% for validation. The DeepMD model was trained for $8x10⁵$ iterations until the root mean square error (RMSE) in energy and forces became constant, with the RMSE values for energy and forces being <1 meV/atom, and <70 meV/Å, respectively (see Supplementary Figure 2).

Supplementary Figure 1: Chemical systems used for training the interatomic potential energy model for the Ga-F-Li-Cl chemical space. Ternary phase diagrams of (a) Li-Cl-F, (b) Ga-Cl-F, (c) Li-Ga-F, and (d) Li-Ga-Cl. Only systems marked in red were used for training. (e, f, g) Slab-like structures of LiCl|GaF3, where multilayer slabs of [001] LiCl and [001] GaF₃ are interfaced "|" in a vertical geometry and have different thicknesses.

Supplementary Table 1: Different chemical systems used in the training and validation of DeePMD PE model

Supplementary Figure 2. The evolution of root-mean-squared-error (RMSE) in forces (F) and energy/atom (E) during the deep neural network training (trn) and validation (val) steps.

Supplementary Note 1.2: Testing and benchmarking trained DeepMD PE model

To assess the accuracy of the trained DeepMD PE model, several atomic configurations not included in the training and validation set were used for testing. Supplementary Figure 3 displays some examples of model testing, where the test structures were derived from slab-like geometry of LiCl|GaF3 with varied thicknesses (Supplementary Figure 3 a,b) and a random Li-Cl-Ga-F structure constructed from only the LiCl and GaF₃ monomer molecules (initial structure in Supplementary Figure 3c). The slab-like structures were constructed from multilayer slabs of [001] LiCl and [001] GaF₃, which were vertically interfaced "|", and separated by 3 Å. A maximum strain of \sim 5 % was applied to match the lattice constants of LiCl and GaF₃ slabs in the LiCl|GaF₃ geometry. AIMD simulations of these test structures were performed at different temperatures (see caption Supplementary Figure 3) to generate the atomic configurations, and the trained DeepMD PE model was tested on these configurations. The comparison of energy and forces predicted by the DeepMD PE model and actual AIMD-DFT calculations is shown in the bottom panels of Supplementary Figure 3. The small RMSE error in both energy and forces indicates the high accuracy of our model.

The accuracy of the trained DeepMD PE model in analyzing the dynamics of Ga-F-Li-Cl chemical space was further evaluated through benchmarking against DFT-AIMD calculations of tensile stress-strain response and Li-ion conductivity in test structures. A comparison of the tensile stress-strain response of a test structure obtained from DFT-AIMD simulations and classical MD simulations using LAMMPS with the DeepMD PE model is presented in Supplementary Figure 4, which demonstrates a good agreement. Furthermore, Supplementary Table 2 displays a comparison of the bulk modulus and Li-ion conductivity obtained through the DeepMD-LAMMPS and DFT-AIMD calculations, which again show good agreement. These findings confirm the accuracy of the trained DeepMD model for studying the dynamics of Ga-F-Li-Cl chemical space.

To obtain the tensile stress-strain response, presented in Supplementary Figure 4b, of the

test structure shown in Supplementary Figure 4a, MD simulations were carried out at $T = 300$ K using both DFT-AIMD and DeepMD-LAMMPS. The simulations were conducted under the NVT ensemble, with a starting tensile strain of 0.01 applied along the z-direction. The simulation was done for $t = 3$ ps at the fixed strained volume, and the average stress σ_z was calculated. The structure obtained after this simulation was used as the initial structure for the next calculation, and a total tensile strain of 0.02 was applied along the z-direction. The simulation was again done for $t = 3$ ps at the fixed strained volume, and the average stress σ_z was evaluated. This procedure was repeated until the total tensile strain along the z-direction reached 0.1. Additionally, the Liion conductivity was computed from the mean squared displacements of Li-ions during the MD simulations and using the Nernst–Einstein approximation, which is based on the methodology established in a previous work¹. MD simulations were carried out under the NVT ensemble at the respective temperatures shown in Supplementary Table 2 using both AIMD-DFT and DeepMD-LAMMPS.

Supplementary Figure 3: Comparison of energy and forces computed by trained DeepMD PE model and DFT-AIMD for various structures (a) NVT AIMD run at $T = 800$ K of a Ga-F-Li-Cl structure with a slab like geometry, (b) NVT AIMD run at $T = 750$ K of another Ga-F-Li-Cl structure with a slab like geometry, and (c) NVT AIMD run at $T = 800$ K of a random Ga-F-Li-Cl structure constructed from LiCl and GaF₃ monomers.

Supplementary Figure 4: Comparison of tensile stress-strain response at $T = 300$ K of a Ga-F-Li-Cl structure shown in (a) and its stress (σ_z) - strain response shown in (b). In (b) the values calculated with DFT-AIMD and DeePMD-LAMMPS are compared.

Supplementary Table 2: A comparison of properties of structure in Supplementary Figure 4 by trained DeePMD PE model and DFT calculations

Supplementary Note 1.3: Testing the accuracy of DeepMD PE model on properties of amorphous systems

The trained DeepMD PE model was further tested on the properties of different amorphous systems in the Ga-F-Li-Cl chemical space. Amorphous phases of different chemical systems LiCl, LiF, GaCl₃, LiGaCl₄, and Li₃GaF₆ were created by melting and quenching each of the crystalline phases using AIMD-DFT and DeepMD-LAMMPS (DP) model. Melting was obtained by performing NVT simulation for each of the structures at $T = 3000$ K for $t = 5$ ps. The atomic configuration at $t = 5$ ps was subsequently relaxed at $T = 0$ K to obtain the amorphous phase. Supplementary Figure 5 shows a comparison of the radial pair distribution function of the amorphous systems, the energy of the amorphous systems with respect to their crystalline phase, and the density of the amorphous systems obtained with DFT and the trained DP model. The results obtained with DFT and the trained DP model are in good agreement.

Supplementary Figure 5: (a) Comparison of the radial pair distribution function $g(r)$ of amorphous (amr.) LiF and amorphous Li $_3$ GaF₆ obtained with AIMD-DFT and trained DP model. (b) The relative energy of the amorphous (amr.) phase of different chemical systems with respect to their crystalline (cry.) phase obtained with AIMD-DFT and trained DP model. (c) Comparison of the density of different amorphous systems obtained with AIMD-DFT and the trained DP model. (d - f) Parity plot showing the atomic forces obtained by AIMD-DFT simulations at $T = 3000$ K and predicted by DP model for the different amorphous systems.

Supplementary Note 2: Creating an amorphous structure

The amorphous structure was designed in 3 steps.

Step - 1: Firstly, a slab-like geometry of LiCl|GaF₃ was constructed, where a multilayer slab of [001] LiCl and [001] GaF₃ was vertically "|" interfaced and separated by 3 Å. A maximum strain of ~5 % was applied to match the lattice constants of LiCl and GaF₃ slabs in the LiCl|GaF₃ geometry and the molar ratio of LiCl:GaF₃ was 2. This structure had a total of 320 atoms and the lattice constant along the z direction was \sim 2.5 nm. Subsequently, to equilibrate the interface, the structure was subjected to AIMD simulation for $t = 5$ ps at $T = 800$ K, and then relaxed at $T = 0$ K to a local energy minimum. The obtained structure is shown in Supplementary Figure 6a.

Step - 2: The structure from the previous step as shown in Supplementary Figure 6a was then periodically repeated along the x and y directions (perpendicular to the interface) and an aperiodic cubic "particle" of size ~2.5 nm (Supplementary Figure 6b) was cut out from it. The center (middle point) of the aperiodic cubic particle was the same as the center of the structure in Supplementary Figure 6a. Eight such identical aperiodic particles were then arranged in a large supercell of size \sim 5.4 nm to obtain a structure containing 9088 (\sim 10k) atoms (Supplementary Figure 6b). Each of the \sim 2.5 nm particles were rotated 90 $^{\circ}$ with respect to their neighbors to ensure that the axis normal to the interface between LiCl and $GaF₃$ did not point in the same direction between neighboring *particles*. This rotation was performed to create a more randomized configuration of atoms. Domains of LiCI and GaF_3 in the initial large structure with \sim 10k atoms can be seen (Supplementary Figure 6b). The ratio of LiCl:GaF₃ was 2. The initial structure is representative of that in experiments, where during ball-milling, LiCl and GaF_3 particles are interfaced with each other and react.

Step - 3: Subsequently, the structure with 9088 (~10k) atoms (Supplementary Figure 6b) was relaxed in LAMMPS at $T = 0$ K to a local energy minimum, and then equilibrated in a hightemperature classical MD NVT simulation using LAMMPS for $t = 50$ ps at $T = 900$ K to allow mixing of the atoms. To obtain a representative structure in which domains of reactant materials are visible, an atomic configuration at $t = 50$ ps was chosen for further evaluation. This configuration was relaxed in LAMMPS at $T = 0$ K to a local energy minimum and then equilibrated (using LAMMPS) under the NPT ensemble for $t = 1$ ns at $T = 300$ K and zero external stress until there was no further change in density, lattice constant, angles, or total potential energy. The resulting amorphous structure shown in Supplementary Figure 6c, was then used in the subsequent analysis.

Supplementary Figure 6: (a) A slab-like geometry of LiCl|GaF3, where a multilayer slab of [001] LiCl and [001] GaF3 is "|" interfaced in a vertical geomtery. (b) Two different views of a large atomic structure of 2LiCI:GaF₃ containing 9088 (~10k) atoms and constructed from 8 identical aperiodic cubic particles of size \sim 2.5 nm. The *aperiodic* cubic particle was cut out from the x, y periodically repeated structure in (a). (c) An amorphous atomic structure representing 2LiCl:GaF3 obtained after high temperature MD simulations of structure in (b) (details above in Supplementary Note 2)

Supplementary Note 2.1: Effect of heating temperature on the behavior of the amorphous system

In addition to the heating simulation at $T = 900$ K (Supplementary Figure 6), we also did similar simulations at $T = 1200$ K and $T = 1500$ K. Supplementary Figure 7a shows the element-wise radial pair distribution function $g(r)$ before and after the high temperature (T = 900 K, 1200 K, and 1500 K) MD simulation of $t = 50$ ps. We find that in all the three temperature cases, the Ga-F and Li-Cl peak decrease, while the Ga-Cl and Li-F peak increase, indicating that anion exchange occurs when the two salts are mixed. This anion exchange is consistent with the thermodynamic driving force and with the experimental EXAFS (Figure 3a, main text). The Ga-F and Li-Cl peak decreases by larger amounts on increasing the temperature from 900 K - 1500 K, indicating that the extent of the anion exchange increases with increasing the temperature. However, anion exchange behavior is still captured by simulations at $T = 900$ K, which is consistent with experimental EXAFS (Figure 3a, main text). We also simulated the shear stress-strain response of the systems obtained after heating MD runs at three different temperatures. A procedure similar to that described in the main text for strain-controlled MD simulation was used to obtain the stressstrain response. Supplementary Figure 7b shows the shear stress-strain response of the structures at an applied shear strain rate of 10 9 s⁻¹ on the yz plane. The stress-strain response curve of the 3 different structures looks very similar, indicating that they show similar mechanical behavior. We believe that $T = 900$ K is sufficient to capture the reaction mechanism and mechanical behavior of the amorphous system.

Supplementary Figure 7: (a) The element-wise radial pair distribution function $g(r)$ plotted at $t = 1$ ps and t = 50 ps of the MD simulation at T = 900 K, T = 1200 K, and T = 1500 K. (b) Shear stress (σ_{yz}) strain (γ_{yz}) response of the amorphous structures at T = 300 K at a constant applied shear strain rate of 10⁹ s⁻¹. The three curves correspond to the behavior of the three systems obtained after heating MD runs at $T = 900$ K, $T = 1200$ K, and $T = 1500$ K.

Supplementary Note 3: Interface reaction LiCl+GaF3: maximum thermodynamic driving force and most likely products

Supplementary Figure 8: The reaction energy of LiCl - GaF₃ reaction, taken from entries in the Materials Project database.

All salt precursors considered in this study for the possibility of soft-clay formation. Interface reaction among salt precursors with maximum thermodynamic driving force (most negative reaction energy E_{rxn} , taken from entries in the Materials Project database.

Interface reaction with maximum thermodynamic driving force between salt precursors considered for soft-clay formation in a prior work². The data is taken from entries in the Materials project database.

1. 0.412GaF₃ + 0.588NaCl → 0.147NaGaCl₄ + 0.088Na₅Ga₃F₁₄ E_{rxn} = -45 meV/atom 2. 0.857LiCl + 0.143InF₃ → 0.143Li₃InCl₆ + 0.429LiF E_{rxn} = -68 meV/atom 3. 0.25LiCl + 0.75Ga₂O₃ → 0.25LiGa₅O₈ + 0.25GaClO E_{rxn} = -1 meV/atom 4. 0.25GaF₃ + 0.75LiOH → 0.25GaHO₂ + 0.25H₂O + 0.75LiF $E_{rxn} = -197$ meV/atom 5. 0.667Li₂O + 0.333GaF₃ → 0.333LiGaO₂ + LiF $E_{rxn} = -442$ meV/atom 6. 3LiCl + $1\text{LaF}_3 \rightarrow \text{No}$ reaction 7. 0.4GaF₃ + 0.6LiBr \rightarrow 0.2GaBr₃ + 0.2Li₃GaF₆ E_{rxn} = -128 meV/atom (GaBr₃ is a molecular solid) 8. 3 NaCl + GaF₃ \rightarrow 3 NaF + GaCl₃ $E_{rxn} = 0.474$ eV (46 kJ mol⁻¹)

Supplementary Table 3: Different possible molecular solid (MS) compounds and the corresponding mp-id obtained from the Materials Project (mp) database. The highlighted compounds are discussed in more detail in the main text. Possible anion exchange reaction with the most negative reaction energy E_{rxn} to form the MS is also listed. Li-based salts were considered as one of the reactants in the anion exchange reaction.

Supplementary Figure 9: The specific volume vs temperature plot obtained from the MD simulations of amorphous 2LiCl-1GaF₃, illustrating a glass-like phase transition at $T_g \sim$ -58 °C. The structures were equilibrated in LAMMPS for $t = 2$ ns at different temperatures under the NPT ensemble.

Supplementary Note 4: Experimental results: XRD spectra and EIS

Supplementary Figure 10: (a), (b), (c), (e) X-ray diffraction (XRD) spectra of different materials after ball milling (BM) and the peak assignments of the products formed. (d) XRD spectra of 3Lil-InBr₃ with time during BM. The InI3 peak appears just after 20 mins of BM. (f) Differential scanning calorimetry (DSC) analysis of 3LiCl-1SbF₃ material after BM. An endothermic peak around ~64 °C and ~210 °C corresponds to melting and boiling of SbCl3, which is formed during BM.

Supplementary Figure 11: Electrochemical Impedance Spectroscopy (EIS) measurements showing the Nyquist plot used to determine the Li-ion conductivity in 2LiCl-1GaF3 soft clay-like material.

Supplementary Note 5: Details of non-affine displacement $(D²_{min})$ calculations

A similar procedure as outlined before 3 was used to calculate the non-affine displacement $D^2{}_{\sf min}$ (Supplementary Eq. 1-4).

where the indices i and j denote spatial coordinates and the index n runs over the atoms within the interaction range ($r_{\rm cut}$) of the reference atom n_0 . Here, $r_{\rm cut}$ = 4 Å was used. $r_n'(t)$ is the $i^{\rm th}$ component of the position of the nth atom at time t. D²_{min}(t, ∆t) is then the local deviation from affine deformation during the time interval $t - \Delta t$, t . This is implemented in the Ovito software.

Supplementary Figure 12: The applied external shear stress σ_{xz} , accumulated shear strain γ_{xz} , and total potential energy change ΔE of the amorphous structure as a function of time in the MD simulation at $T =$ 300 K. The external shear stress ranged from 10 to 50 MPa. The accumulated shear strain after three cycles is non-negligible ($y_{xz} \neq 0$), signifying permanent deformation. Here, the xz-component of external stress was applied and other components were kept at zero (using a similar procedure as used for Figure 1c (main text)).

Supplementary Figure 13: Ga K-edge EXAFS of different materials, bulk GaF₃, bulk GaCl₃, and clay-like 2LiCl-1GaF3 and 3LiCl-1GaF3. |χ(r)|, magnitude of Fourier transformed EXAFS.

Supplementary Figure 14: The energy of the different chemical systems obtained using DFT calculations with different k-grid sizes. N_{k-point} is the total number of k-points in the k-grid. The energy is referenced to the value obtained with one k -point.

Supplementary Figure 15: The Li-Cl and Li-F pair distribution function $q(r)$ of Li-atoms with largest (D^2_{min}) > 90% of maximum) and smallest (D^2 _{min} < 10% of maximum) non-affine displacement values. The $g(r)$ values were averaged over the strain interval $y_{yz} = 0.09 - 0.14$. The Li atoms in the areas involved in plastic deformation have a CI-rich environment, as evidenced by the lower Li-F peak for Li atoms with D^2 _{min} >90% of maximum compared to those with D^2 _{min} values <10% of maximum.

Supplementary References

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