

Intrinsic spin Hall torque in a moiré Chern magnet

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SUPPLEMENTARY MATERIALS

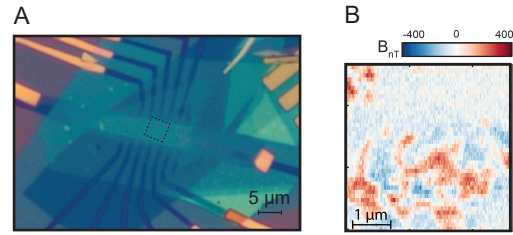


Fig. S1. **NanoSQUID imaging at $\nu = -1$ on monolayer MoTe₂/monolayer WSe₂ device.** (A) Optical image of a monolayer MoTe₂/monolayer WSe₂ device. (B) NanoSQUID imaging revealed qualitatively similar magnetism and anomalous Hall resistances in this device. This device was rather disordered and did not show quantization of anomalous Hall resistance.

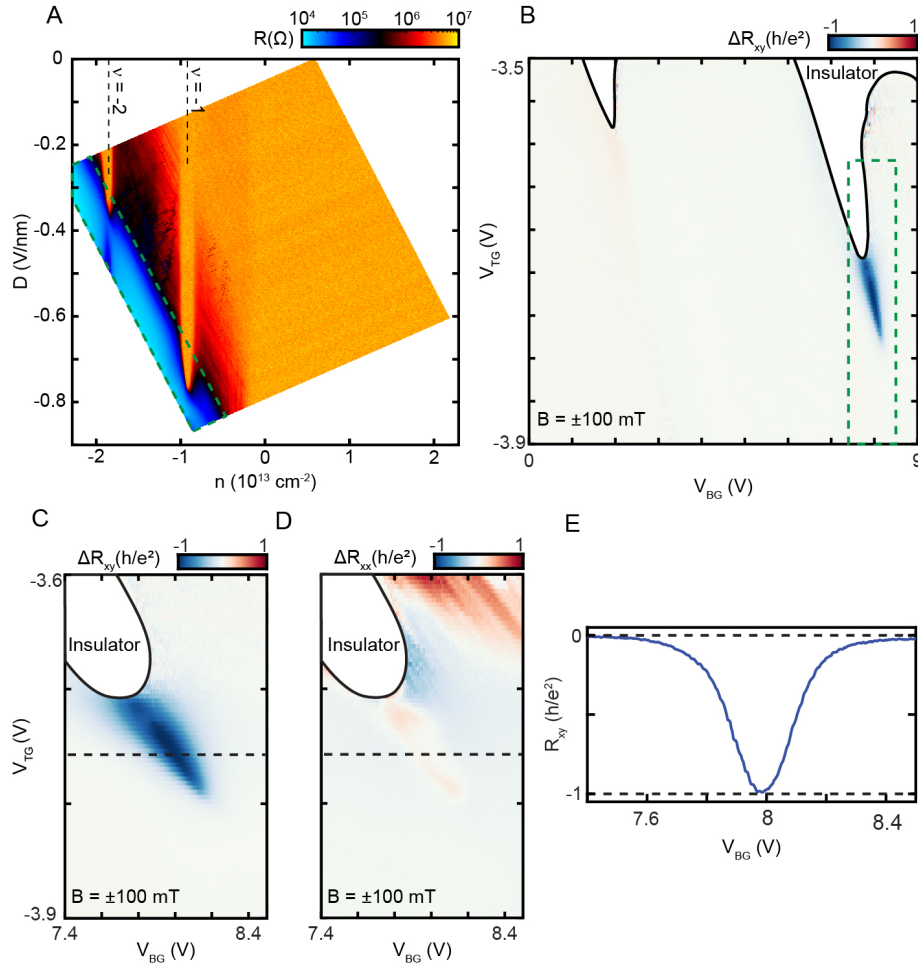


Fig. S2. **Phase diagram from transport data** (a) Two terminal resistance of device (measured between contacts $abcd$ and j) plotted as a function of electron density n and displacement field D , where $D = \frac{V_{TG} - V_{BG}}{d_t + d_b}$, $n = \epsilon\epsilon_0(V_{TG}/d_t + V_{BG}/d_b) + n_0$. Here $d_t = 2.7$ nm is the thickness of the top hBN layer, $d_b = 12.1$ nm is the thickness of the bottom hBN layer, $\epsilon \approx 3$ is the relative dielectric constant of hBN, and n_0 is the offset charge carrier density, $5.9 \times 10^{12} \text{ cm}^{-2}$. At low displacement fields $\nu = -1$ and $\nu = -2$ both host topologically trivial insulating states, with the $\nu = -1$ insulator presumably interaction-driven. In the electron-doping regime large contact resistances hamper transport measurements. (b) ΔR_{xy} measurement in the region inside the green dotted line in a. A finite ΔR_{xy} appears near $\nu = -1$ in a narrow range of D . (c) ΔR_{xy} measurement in the region inside the green dotted line in b. Precise quantization of ΔR_{xy} obtains over a range of displacement fields at $\nu = -1$. (d) Symmetrized R_{xx} measurement in the region inside the dotted line in b. (e) Linecut of ΔR_{xy} along the dotted line in c illustrating the appearance of a QAH effect.

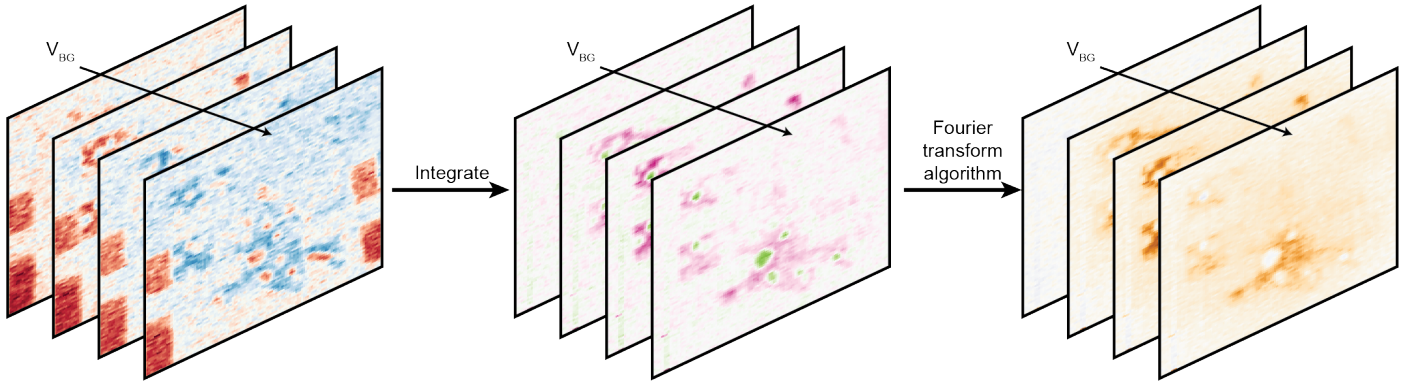


Fig. S3. **AC bottom gate conversion to magnetization.** (a) AC bottom gate magnetometry produces $\delta B_z / \delta V_{BG}(x, y, V_{BG})$. (b) We integrate $\delta B_z / \delta V_{BG}(x, y, V_{BG})$ with respect to V_{BG} to obtain $B_z(x, y, V_{BG})$ (c) For each value of V_{BG} we invert $B(x, y)$ to produce $m_z(x, y, V_{BG})$, which is presented as a video of the out-of-plane magnetization as V_{BG} enters and then leaves the QAH regime in the supplementary data.

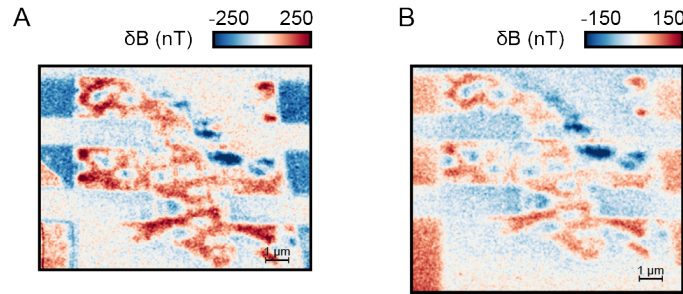


Fig. S4. **Repeated cooldowns** (a) Magnetic structure measured at 28 mT, $V_{TG} = -3.734$ V, $V_{BG} = 7.818$ V at a height of 125 nm with nanoSQUID diameter $\phi = 159$ nm. (b) Magnetic structure measured at 36 mT, $V_{TG} = -3.756$ V, $V_{BG} = 7.943$ V during a subsequent cooldown at a height of 175 nm with nanoSQUID diameter $\phi = 113$ nm.

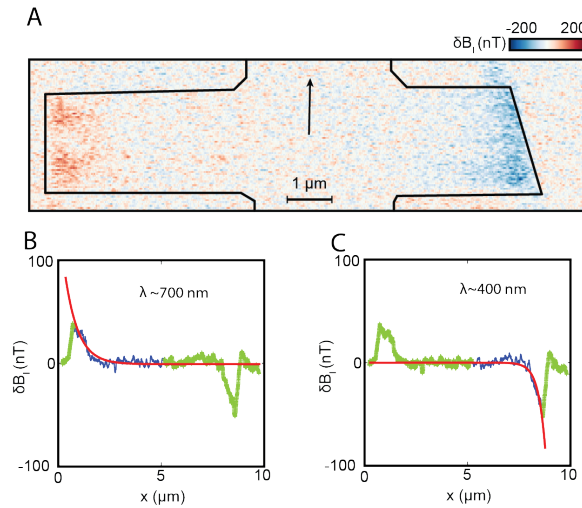


Fig. S5. **Spin diffusion length** (a) Spin Hall effect near $\nu = -1$ (b) Fit of the left edge. Green regions are masked from the fit, blue is fit to an exponential decay function, $B(x) = A \cdot e^{-x/\lambda} - c$. Approximate spin diffusion length λ is 700 nm. (c) Fit of the right edge, approximate spin diffusion length λ is 400 nm.

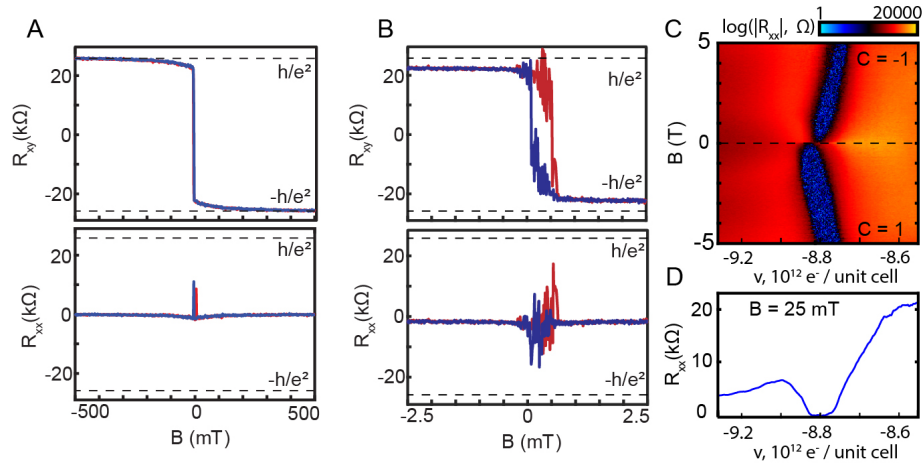


Fig. S6. **Additional transport properties of the magnetic Chern insulator** (a) Magnetic hysteresis loop in QAH regime. At ± 500 mT quantization reaches $1.000 \pm 0.006 h/e^2$ and $-0.996 \pm 0.005 h/e^2$. (b) Close to $B = 0$ $R_{xy} \approx 0.9 h/e^2$. Coercive fields are less than 1 mT at the measurement temperature of 1.6K. (c) Dependence of the degeneracy of the Chern band on B reveals the Chern number of the ground state at finite field, which is -1 in this system. (d) Linecut shows R_{xx} reaches $-93 \Omega \pm 115 \Omega$.

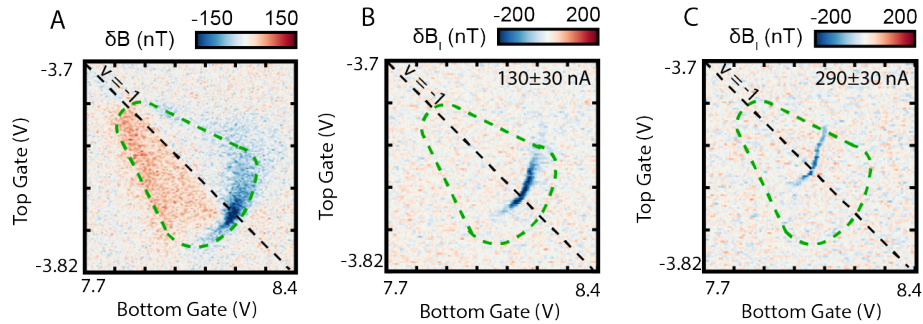


Fig. S7. **Current-switching phase diagram** (a) Bottom gate modulation magnetometry phase diagram taken at the point at which measurements for Fig. 4g were performed. The green dotted outline appears in that figure. $\delta V_{BG} = 35$ mV was used. (b) Current-induced magnetic domain switching signal δB_I as a function of top and bottom gate voltages with $I_{SD} = 130$ nA, $\delta I_{SD} = 30$ nA. (c) The same measurement with $I_{SD} = 290$ nA, $\delta I_{SD} = 30$ nA. Magnetic switching appears over broad regions of the magnetic phase diagram, although currents required to effect domain switching vary with gate voltages.