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**Supplementary information**

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**Machine-learning-based dynamic-importance sampling for adaptive multiscale simulations**

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# Machine Learning Based Dynamic-Importance Sampling for Adaptive Multiscale Simulations

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# 1 Supplementary Information

## 1.1 DynIm Algorithm

Algorithm 1 outlines the functionality of DYNIM, to further facilitate understanding and use of our framework. The code and supporting examples and data are released under MIT license and can be found on github: <https://github.com/LLNL/dynim>.

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**Algorithm 1** DynIm sampling algorithm.

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```
1: procedure DYNIM.INITIALIZE(encoder)
2:   dynim.encoder  $\leftarrow$  encoder            $\triangleright$  an ML encoder that satisfies the importance hypothesis
3:   dynim.candidates  $\leftarrow$  [ ]            $\triangleright$  empty list for encoded candidates
4:   dynim.selections  $\leftarrow$  [ ]          $\triangleright$  empty list for selections
5:
6: procedure DYNIM.ADD_CANDIDATES(list_of_candidates)
7:   encoded_candidates  $\leftarrow$  dynim.encoder.encode(list_of_candidates)
8:   dynim.candidates.append_all(encoded_candidates)
9:
10: procedure DYNIM.SELECT_IMPORTANT_CANDIDATES(k)
11:   ranks  $\leftarrow$  dynim.compute_importance(dynim.candidates)
12:   dynim.candidates  $\leftarrow$  sort(dynim.candidates, key=ranks, reverse=True)
13:   important_candidates  $\leftarrow$  dynim.candidates[:k]            $\triangleright$  top k candidates
14:   dynim.candidates  $\leftarrow$  dynim.candidates[k:]            $\triangleright$  remaining candidates
15:   dynim.selections.append_all(important_candidates)
16:   return important_candidates
17:
18: procedure DYNIM.COMPUTE_IMPORTANCE(list_of_candidates)
19:   ranks = [ ]
20:   for each  $c \in$  list_of_candidates do
21:     knn = get_knn(c, target=dynim.selections, k=10)
22:     ranks.append(mean(||c - knn||))
23:   return ranks
```

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## 1.2 Supplementary Figures

Figure 1 highlights a comparison between several autoencoder models developed and tested for this work in order to choose the most suitable one, with respect to the dimensionality of the latent space and the quality of reconstruction.

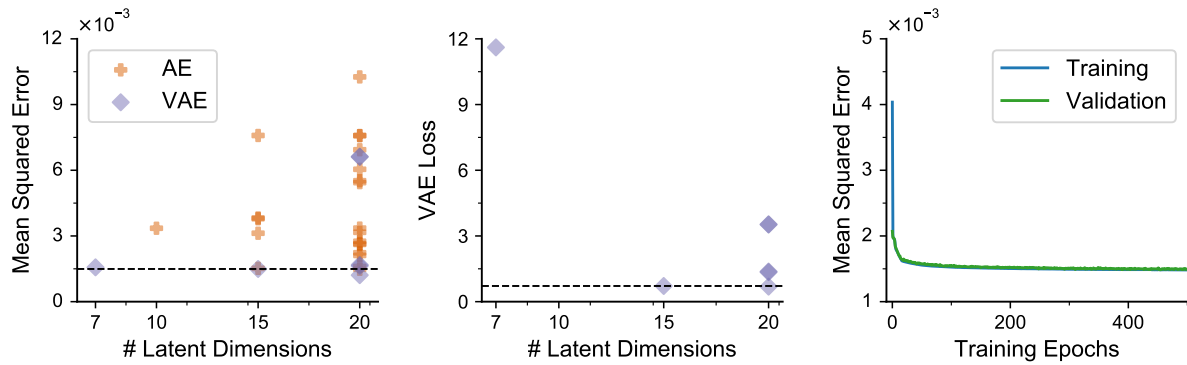


Figure 1: Identification of intrinsic dimension of data and search for a suitable model was performed by exploring several AE and VAE models. The selected VAE model was chosen as a balance between low dimensionality and reconstruction quality. Left: The mean squared error was used to assess the reconstruction quality of all models – horizontal line indicates the chosen 15-D VAE model. Middle: The VAE models were also evaluated on the VAE loss, which additionally accounts for similarity to a normal distribution – horizontal line indicates the chosen model. Right: The training history of the selected model indicates converged errors with no over-fitting.