Higgs-Free Symmetry Breaking from Critical Behavior near Dimension Four

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Abstract

Starting from the infrared limit of Yang-Mills theory, we introduce here a Higgs-free model in which symmetry breaking arises from critical behavior near dimension four. Electroweak bosons develop mass near the Wilson-Fisher point of Renormalization Group flow. The family structure of Standard Model is recovered using the technique of "epsilon expansion". We also find that dimensional regularization offers a straightforward solution to the cosmological constant problem.

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1. **Introduction**

The Standard Model of particle physics (SM) is a highly successful theory that has been in place for more than 35 years. It includes the $SU(3) \otimes SU(2) \otimes U(1)$ gauge model of strong and electroweak interactions along with the Higgs mechanism that spontaneously breaks the electroweak $SU(2) \otimes U(1)$ group down to the $U(1)$ group of electromagnetism. Despite its outstanding reliability, SM is viewed as a low-energy framework that is likely to be amended by new phenomena occurring in the Terascale region. The elementary Higgs boson picture of electroweak (EW) and flavor symmetry breaking suffers from several drawbacks. In particular [1, 2]:

- It does not provide a dynamical explanation for electroweak symmetry breaking (EWSB).
- It appears to be highly contrived, requiring fine tuning of parameters to enormous precision.
- It has a hierarchy problem of widely different energy scales.
- It provides no insight into flavor physics.
- It is at odds with the measured value of the cosmological constant.

Similar or different drawbacks persist in supersymmetric extensions of Higgs theories (MSSM) and alternative models of EWSB such as Technicolor [3, 4].

2. **Challenges of Yang-Mills theory**

In our view, there are a couple of key roadblocks that have slowed down progress on the theoretical side of high-energy physics for the past 35 years:

- Because Yang-Mills field is self-interacting, it is inherently nonlinear and prone to undergo complex behavior [5].
- Dynamics of Yang-Mills field is strongly coupled in the infrared (IR) where perturbation theory breaks down and traditional methods of quantum field theory (QFT) fail to apply.

3. **New tools: nonlinear dynamics and critical behavior**

To deal with these challenges, we start from a far less explored vantage point. Specifically, we exploit the fact that both mapping theorem [6] and the Landau-Ginzburg-Wilson (LGW) model of critical behavior [7, 19] enable understanding of the IR regime of gauge field theory using the principles of Renormalization Group program (RG).

• **The mapping theorem**

The electroweak group $SU(2) \otimes U(1)$ is broken at a scale approximately given by $\mu_{EW} = G_F^{-1/2} = 293$ GeV, in which G_F is the Fermi constant. Yang-Mills fields associated with *SU*(2) are vectors denoted as $A^a_\mu(x)$, in which $\mu = 0, 1, 2, 3$ is the Lorentz index and

 $a = 1, 2, 3$ is the group index. To manage the large number of equations derived from the Yang-Mills theory, it is desirable to devise a method whereby $A^a_\mu(x)$ are reduced to analog fields having less complex structure. The *mapping theorem* allows for such a reduction. The action functional of classical scalar field theory defined in fourdimensional space-time is defined as

$$
S[\Phi] = \int d^4x \left[\frac{1}{2}(\partial \Phi)^2 - \frac{1}{4!}g^2 \Phi^4\right]
$$
 (1)

An extremum of (1) is also an extremum of the *SU*(2) Yang-Mills action provided that: a) *g* represents the coupling constant of the Yang-Mills field,

b) some components of $A^a_\mu(x)$ are chosen to vanish and others to equal each other. In the most general case, the following approximate mapping between Yang-Mills fields and scalar $\Phi(x)$ holds [6]:

$$
A_{\mu}^{a}(x) = \eta_{\mu}^{a} \Phi(x) + O(\frac{1}{\sqrt{2}g})
$$
 (2)

where η^a_μ are properly chosen constants. The mapping becomes exact in the Lorenz gauge $\partial^{\mu}A_{\mu}^{a}(x) = 0$ and in the IR regime of strong coupling ($g \rightarrow \infty$).

• **LGW theory near dimension four: a brief overview**

Consider the Euclidean space LGW action in *D* − dimensional space-time [7, 8, 19]

$$
S[\Phi] = \int d^D x \left[\frac{1}{2} (\partial \Phi)^2 + V(\Phi)\right]
$$
 (3)

In particular,

$$
V(\Phi) = \frac{r}{2}\Phi^2 + \frac{g^2}{4!}\Phi^4 - j\Phi
$$
 (4)

in which *j* denotes the external current coupled to Φ and *r* stands for the deviation from the critical temperature ($r = T - T_c$). According to the RG program, rescaling the

cutoff $\Lambda \rightarrow \Lambda' = \frac{\Lambda}{l}$, $b > 1$ *b* $\Lambda \to \Lambda' = \frac{\Lambda}{I}$, $b > 1$ and integrating out fast modes within $\Lambda' < |k| < \Lambda$, turns the original action into an *effective* action. The effective theory built with this prescription represents a lower-energy image of the original theory, namely

$$
S[\Phi] \Lambda \to S_{\text{eff}}[\Phi_{<}], \Lambda' \tag{5}
$$

Here, $\Phi_{\leq}(x)$ are the slow modes of the field ($|k| < \Lambda'$),

$$
\Phi_{\leq}(x) = \int_{|k| < \Lambda} \frac{d^D k}{(2\pi)^D} \Phi(k) \exp(ikx) \tag{6}
$$

and

$$
\int D_{\Lambda}[\Phi] \exp(-S[\Phi]) \approx \exp(-S_{\text{eff}}[\Phi_{<}])
$$
\n(7)

with

$$
S_{\text{eff}}[\Phi_{<}] = \int d^{D}x \left[\frac{1}{2} (\partial \Phi_{<})^{2} + V_{\text{eff}} (\Phi_{<})\right]
$$
 (8)

Invoking the limit of infinitesimal scaling $b = 1 + dt$, $dt \ll 1$ along with the local potential approximation leads to [7, 8, 19],

$$
S_{\text{eff}}[\Phi_{\leq}] = S[\Phi_{\leq}] + \frac{Q}{2} \int d^D x \log[\Lambda^2 + \frac{\partial^2 V[\Phi_{\leq}]}{\partial \Phi_{\leq}^2}] \tag{9}
$$

where

$$
Q = \frac{\Lambda^D dt}{(2\pi)^D} \frac{2\pi^{D/2}}{\Gamma(D/2)}
$$
(10)

When applied to (4), the logarithmic correction on the right hand side of (9) may be expanded as

$$
\log[1 + \frac{\partial^2 V}{\partial \Phi_{\leq}}] = \log[1 + r] + \frac{g^2}{2(1+r)} \Phi_{\leq}^2 - \frac{g^4}{8(1+r)} \Phi_{\leq}^4 + \dots
$$
 (11)

in which Λ has been normalized to unity ($\Lambda = 1$). On account of (11), sufficiently small deviations from criticality ($r \ll 1$) produce the following approximations

$$
S_{\text{eff}}[\Phi_{<}] \sim S[\Phi], \qquad V_{\text{eff}}[\Phi_{<}] \sim V[\Phi] \tag{12}
$$

4. Assumptions

4.1) As previously stated, the mapping theorem applies when comparing Yang-Mills fields with classical scalar fields. We extend this ansatz and assume that the theorem holds sufficiently well for *quantum* scalar field theory. This assumption may be motivated by considering the close analogy between quantum field theory (QFT) and statistical systems *near criticality* [9]. On this basis, we assume that the Yang-Mills model is reasonably well approximated by the LGW theory of equilibrium critical behavior.

4.2) From (4.1) it follows that the dimensional parameter of LGW theory and dimensional regulator of Yang-Mills theory $\varepsilon = 4 - D$ are identical entities. This identity is made explicit in the first row of Tab. 1 below.

4.3) We analyze on the IR regime of Yang-Mills theory in which $\mu_{EW} = G_F^{-1/2}$ stands for the EW scale, μ for the running scale and the ultraviolet (UV) scale $\Lambda = \Lambda_{UV} > \mu > \mu_{EW}$ for the cutoff. The dimensional parameter is then given by [10, 13],

$$
\varepsilon = \frac{1}{\log(\frac{\Lambda_{UV}^2}{\mu^2})} > 0
$$
\n(13)

Moreover, to simplify the derivation, it is convenient to take advantage of the large numerical disparity between the two scales entering the logarithm and substitute (13) with

$$
\varepsilon \sim \frac{\mu^2}{\Lambda_{UV}^2} \tag{14}
$$

It is seen from (14) that,

- maximal deviation from $D = 4$ occurs near the limit $\mu \rightarrow \Lambda_{UV}$. This finding is consistent with quantum gravity theories asserting that space-time turns $2+1$ dimensional at ultra-high energies [11].
- minimal deviation from $D = 4$ ($\varepsilon \rightarrow 0$) occurs as μ approaches the EW scale, that is, when $\mu \rightarrow \mu_{EW}$.

4.4) The UV cutoff is not uniquely determined but smeared out by high-energy noise [12]. The UV cutoff spans a range of values

$$
\Lambda_{UV} \in \delta \Lambda_{UV} \tag{15}
$$

(15) implies that, at any given μ and Λ_{UV} , dimensional parameter ε falls in the range

$$
\left|\delta\varepsilon\right| = 2\mu \frac{\delta\Lambda_{UV}}{\Lambda_{UV}}\tag{16}
$$

5. Dynamics of RG flow equations

Elaborating from these premises leads to the following side-by-side comparison between parameters of LGW and Yang-Mills theories:

Tab. 1: Comparison between LGW and Yang-Mills theories

Under these circumstances, RG flow equations for $r = \delta \mu$, $u = g^2$ and fermion current $j = j_f$ read, respectively [13]

$$
\frac{\partial(\delta\mu)}{\partial t} = (\delta\mu)(2 + bg^2) + ag^2
$$

$$
\frac{\partial g^2}{\partial t} = \varepsilon g^2 - 3b(g^2)^2
$$

$$
\frac{\partial j_f}{\partial t} = (3 - \frac{\varepsilon}{2})j_f
$$
 (17)

Here,

$$
a = 3K_4 \Lambda_{UV}^2, \qquad b = 3K_4, \qquad K_4 = (8\pi^2)^{-1}
$$
 (18)

On account of (12), the Wilson-Fisher (WF) fixed point of (17) is defined by the pair

$$
(\delta \mu)^* = -\frac{a}{6b} \varepsilon, \qquad (g^2)^* = \frac{\varepsilon}{3b} \tag{19}
$$

(19) acts as a non-trivial attractor of the RG flow. Because it resides on the critical line $\mu = \mu_{EW}$, it describes by definition a *massless* field theory ($r = \delta \mu = 0$) [19]. The non-vanishing vacuum of Φ at the WF point results from minimization of (4), that is,

$$
v^* = \pm \sqrt{\frac{6(-\delta\mu)^*}{(g^2)^*}} = \pm 3(K_4)^{\frac{1}{2}} \Lambda_{UV}
$$
 (20)

(19) and (20) show how massive gauge bosons develop at the WF point from critical behavior near $D = 4$. Let $v^* = M$ denote the mass acquired by the gauge boson. Combining (14), (18), (19) and (20) yields

$$
(g2)*M2 = \mu_{EW}^2 = const.
$$

$$
(g*)2 \sim m_f^* \sim \varepsilon
$$
 (21)

in which $m_f^* = O(j_f)$ stands for the normalized fermion mass [13]. On account of assumptions 4.3), 4.4) and (21), the WF attractor (20) changes from a *single isolated* point to a *distribution* of points. Our next step is to explore the link between the structure of the WF attractor and the parameters of SM.

6. Wilson-Fisher point as source of particle masses and gauge charges

We are now ready to analyze the dynamics of (17) using the standard methods employed in the study of nonlinear systems [14]. To this end, we first note that the last equation in (17) is uncoupled to the first two. This enables us to reduce (17) to a planar system of differential equations. We next cast (17) in the form of a two-dimensional map, namely

$$
(g^{2})_{n+1} = (1 + \varepsilon \Delta t)(g^{2})_{n} - 3b\Delta t(g^{2})_{n}
$$
 (22a)

$$
(\delta \mu)_{n+1} = (\delta \mu)_n [1 + 2\Delta t + b\Delta t (g^2)_n] + a\Delta t (g^2)_n
$$
 (22b)

where ∆*t* represents the increment of the sliding scale. Linearizing (22) and computing its Jacobian *J* gives

$$
J = 1 + (2 + \varepsilon)\Delta t > 1\tag{23}
$$

Thus map (23) is dissipative for $\varepsilon \neq 0$ and asymptotically conservative in the limit $\varepsilon = \Delta t = 0$. Invoking universality arguments [14, 18] we conclude that, near criticality, (23) shares the same universality class with the quadratic map. Furthermore, in the neighborhood of Feigenbaum's attractor, ε approaches $\varepsilon_{\infty} = 0$ according to:

$$
\varepsilon_n - \varepsilon_\infty \approx a_n \cdot \overline{\delta}^{-n} \tag{24}
$$

Here, $n \gg 1$ is the index counting the number of cycles generated through the period doubling cascade, $\overline{\delta}$ is the rate of convergence (in general, different from Feigenbaum's constant for the quadratic map) and a_n is a coefficient which becomes asymptotically independent of *n*, that is, $a_{\infty} = a$ [15]. Substituting (24) in (21) yields

$$
P_j(n) = \begin{bmatrix} M_n^{-2} & (g^*)_n^2 & (m_j^*)_n \end{bmatrix} \propto \overline{\delta}^{-n} \quad \text{if} \quad n >> 1 \tag{25}
$$

in which $j = 1, 2, 3$ indexes the three entries of (25). Period-doubling cycles are characterized by $n = 2^p$, with $p \gg 1$. The ratio of two consecutive terms in (25) is then given by

$$
\frac{P_j(p+1)}{P_j(p)} = O\left[\overline{\delta}^{-(2^p)}\right]
$$
\n(26)

Numerical results derived from (26) are displayed in Tab. 3. This table contains a sideby-side comparison of estimated versus actual mass ratios for charged leptons and quarks and a similar comparison of coupling strength ratios. Tab. 2 contains the set of known quark and gauge boson masses as well as the SM coupling strengths. All quark masses

are reported at the energy scale given by the top quark mass and are averaged using reports issued by the Particle Data Group [16]. Gauge boson masses are evaluated at the EW scale and the coupling strengths at the scale set by the mass of the *Z* boson. The best-fit rate of convergence is $\overline{\delta} = 3.9$ which falls close to the numerical value of the Feigenbaum constant corresponding to hydrodynamic flows [13, 15, 17].

(21) and (25) imply that there is a series of terms containing massive electroweak bosons, namely

$$
(M_n g_n^*)^2 = (M_{n+1} g_{n+1}^*)^2 = \dots = (M_{n+q} g_{n+q}^*)^2 = \dots = const.
$$
 (27)

For the first two terms of this series we obtain

$$
\frac{M_Z^2}{M_W^2} = \frac{g_2^2 + e^2}{g_2^2} = 1 + \frac{\alpha_{EM}}{\alpha_2}
$$
\n(28)

in which $\alpha_{EM} = e^2$ $\alpha_{EM} = e^2 / 4\pi$ is the electromagnetic coupling strength and $\alpha_2 = \frac{g^2}{4\pi}$ $2 = \frac{82}{4}$ $\alpha_2 = \frac{g_2^2}{4\pi}$ the strength of the weak interaction. The rationale for (28) lies in the fact that the charged gauge boson W^{\pm} carries a superposition of weak and electromagnetic charges, whereas the neutral gauge boson Z^0 carries only the weak isospin charge. Inverting (28) and taking into account the last rows of Table 3, leads to

$$
\frac{M_W^2}{M_Z^2} = \frac{1}{1 + \frac{\alpha_{EM}}{\alpha_2}} = \frac{1}{1 + \frac{1}{\delta}} \approx 1 - \frac{1}{\delta} = \cos^2 \theta_W
$$
\n(29)

(29) suggests a natural explanation for the Weinberg angle θ_W . Likewise, we may write (27) as

$$
\frac{g_2^2}{M_W^2} = \frac{g_2^2 + e^2}{M_Z^2} = const
$$
\n(30a)

This relation offers a straightforward interpretation for both Fermi constant and the mass of the *hypothetica*l Higgs boson. Indeed, in SM we have [13]

$$
\frac{g_2^2}{M_W^2} = 4\sqrt{2}G_F
$$
 (30b)

and

$$
v(\varphi^0) \propto \sqrt{\frac{1}{G_F \sqrt{2}}} \approx 246.22 \text{ GeV}
$$
 (30c)

where $v(\varphi^0)$ denotes the vacuum expectation value for the neutral component of the "would-be" Higgs doublet.

Tab. 2: Actual values of selected SM parameters.

Parameter ratio	Behavior	Actual	Predicted
m_{ν} $\frac{m_{\nu}}{m_{\nu}}$	$\overline{\delta}^{-4}$	3.365×10^{-3}	4.323×10^{-3}
m_c / m_t	$\overline{\delta}^{-4}$	3.689×10^{-3}	4.323×10^{-3}
m_d $\frac{m_d}{m_s}$	$\overline{\delta}^{-2}$	0.052	0.066
$\frac{m_s}{m_h}$	$\overline{\delta}^{-2}$	0.028	0.066
m_e m_u	$\overline{\delta}^{-4}$	4.745×10^{-3}	4.323×10^{-3}
m_{μ} $\frac{m_{\mu}}{m_{\tau}}$	$\overline{\delta}^{-2}$	0.061	0.066
M_{W} _{M_z}	$\left(1-\frac{1}{5}\right)^{1/2}$	0.8823	0.8623
$(\alpha_{EM}/\alpha_w)^2$	$\overline{\delta}^{-2}$	0.053	0.066
$(\alpha_{EM} / \alpha_s)^2$	$\overline{\delta}^{-4}$	4.034×10^{-3}	4.323×10^{-3}

Tab 3: Actual versus predicted ratios of SM parameters

7. A natural solution for the hierarchy problem

It is known that the technique of renormalization in perturbative QFT is conceived as a two-step program: regularization and subtraction. One first controls the divergence

present in momentum integrals by inserting a suitable "regulator", and then brings in a set of "counter-terms" to cancel out the divergence. Momentum integrals in QFT have the generic form

$$
I = \int_0^\infty d^4q F(q) \tag{31}
$$

Two regularization techniques are frequently employed to manage (31), namely "momentum cutoff" and "dimensional regularization". When the momentum cutoff scheme is applied for regularization in the UV region, the upper limit of (31) is replaced by a finite cutoff Λ ,

$$
I \to I_{\Lambda} = \int_0^{\Lambda} d^4q F(q) \tag{32}
$$

Explicit calculation of the convergent integral (32) amounts to a sum of three polynomial terms

$$
I_{\Lambda} = A(\Lambda) + B + C(\frac{1}{\Lambda})
$$
\n(33)

Dimensional regularization proceeds instead by shifting the momentum integral (33) from a four-dimensional space to a continuous *D* - dimensional space

$$
I \to I_D = \int_0^\infty d^D q F(q) \tag{34}
$$

Introducing the dimensional parameter $\varepsilon = 4 - D$ leads to

$$
I_D \to I_{\varepsilon} = A'(\varepsilon) + B' + C'(\frac{1}{\varepsilon})
$$
\n(35)

In general, Λ and ε are not independent regulators and relate to each other via the approximate connection (13)

$$
\varepsilon = 4 - D = \frac{1}{\log(\Lambda^2/\mu_0^2)}\tag{36}
$$

where $\mu_0 < \Lambda$ stands for an arbitrary but non-vanishing reference scale.

A similar technique can be used to regularize field theory in the IR limit whereby Γ is taken to represent the lowest bound scale. A strictly positive ε on less than four dimensions ($D < 4$) requires taking the reciprocal of the logarithm in (36) to comply with μ_0 > Γ. The infrared version of (36) accordingly reads:

$$
\varepsilon' = 4 - D = \frac{1}{\log(\frac{\mu_0^2}{\Gamma^2})}
$$
(37)

We next proceed with the following assumptions

7.1) The deep IR cutoff of field theory is set by the cosmological constant scale

$$
\Gamma = \left(\Lambda_{cc}\right)^{\frac{1}{4}}\tag{38}
$$

where Λ_{cc} represents the cosmological constant.

7.2) The deep UV cutoff of field theory is set by the Planck scale:

$$
\Lambda_{UV} = \Lambda_{Pl} \tag{39}
$$

Combining 7.1) and 7.2) implies that, as the EW scale is approached from above or below, (36) and (37) naturally converge to a common value. Taking $\mu_0 = \mu_{EW}$ and substituting in (36) and (37) yields

$$
\frac{\mu_{EW}}{\Gamma} = \frac{\Lambda_{Pl}}{\mu_{EW}} \rightarrow (\Lambda_{cc})^{1/4} = \frac{\mu_{EW}^2}{\Lambda_{Pl}}
$$
\n(40)

Several conclusions may be drawn from (40) ,

a) Asymptotic approach to four-dimensional space-time explains the existence of the deep IR cutoff ($Λ_{cc}$) and deep UV cutoff ($Λ_{Pl}$). Stated differently, fractal space-time

description supplied by the condition $\varepsilon > 0$ and $\varepsilon' > 0$ appears to be linked to these natural bounds [20].

b) Fixing two out of the three scales involved in (40) automatically determines the third one.

c) The gauge hierarchy problem, cosmological constant problem and the existence of the EW phase transition appear to be deeply interconnected.

d) The derivation presented here stands in sharp contrast with sophisticated approaches to the hierarchy problem based on supersymmetry, Technicolor, extra-dimensions, anthropic arguments, fine-tuning or gauge unification near the Planck scale.

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