

On various Ramanujan continued fractions: mathematical connections with some sectors of Particle physics concerning like-particle solutions and dilaton value.

Michele Nardelli¹, Antonio Nardelli

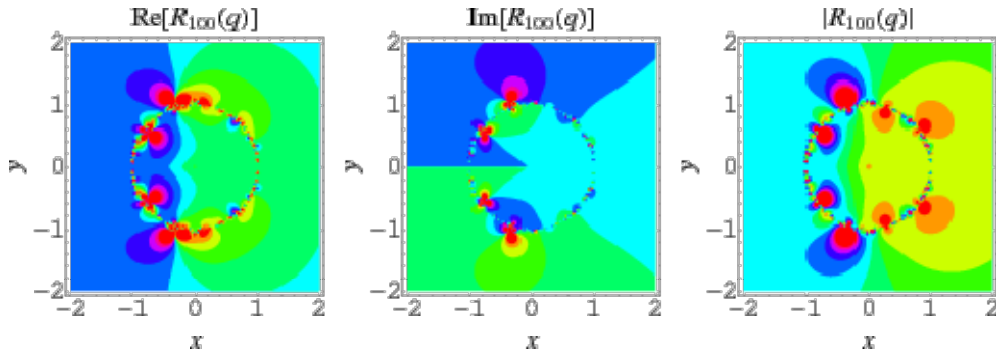
Abstract

In this research thesis, we have analyzed various Ramanujan continued fractions and described the new possible mathematical connections with some sectors of Particle physics concerning like-particle solutions and dilaton value.

¹ M.Nardelli have studied by Dipartimento di Scienze della Terra Università degli Studi di Napoli Federico II, Largo S. Marcellino, 10 - 80138 Napoli, Dipartimento di Matematica ed Applicazioni “R. Caccioppoli” - Università degli Studi di Napoli “Federico II” – Polo delle Scienze e delle Tecnologie Monte S. Angelo, Via Cintia (Fuorigrotta), 80126 Napoli, Italy



<https://twitter.com/royalsociety/status/1076386910845710337>



<http://mathworld.wolfram.com/Rogers-RamanujanContinuedFraction.html>

From:

A continued fraction of order twelve

Research Article

M.S. Mahadeva Naika, B. N. Dharmendra , K. Shivashankara- *Department of Mathematics, Bangalore University, Central College Campus, Bangalore - 560 001, India - Department of Mathematics, Yuvaraja 's College, University of Mysore, Mysore-570 001, India - Received 27 November 2007; accepted 19 April 2008*

Ramanujan has recorded several continued fractions in his notebooks. One of the fascinating continued fraction identities recorded by Ramanujan as Entry 12 in his second notebook [5], [2, Entry 12, p.24]:

$$\frac{(a^2q^3; q^4)_\infty (b^2q^3; q^4)_\infty}{(a^2q; q^4)_\infty (b^2q; q^4)_\infty} = \frac{1}{(1-ab)+} \frac{(a-bq)(b-aq)}{(1-ab)(1+q^2)+} \frac{(a-bq^3)(b-aq^3)}{(1-ab)(1+q^4)+} \dots \quad (8)$$

$|q| < 1, |ab| < 1$.

For a proof of (8), see C. Adiga, B. C. Berndt, S. Bhargava and G. N. Watson [1] and L. Jacobsen [4].

In the equation (8), replacing q by q^3 , a by aq^2 , b by q and then putting $a = 1$, we get

$$\frac{i(-q, -q^{11})}{i(-q^3, -q^7)} = \frac{1-q}{(1-q^3)+} \frac{q^3(1-q^2)(1-q^4)}{(1-q^3)(1+q^6)+} \frac{q^3(1-q^8)(1-q^{10})}{(1-q^3)(1+q^{12})+} \dots \quad (9)$$

Let

$$H(q) := \frac{q(1-q)}{(1-q^3)+} \frac{q^3(1-q^2)(1-q^4)}{(1-q^3)(1+q^6)+} \frac{q^3(1-q^8)(1-q^{10})}{(1-q^3)(1+q^{12})+} \dots \quad (10)$$

and

$$V(q) := H(q).$$

In this paper, we obtain a modular relation between the continued fractions $H(q)$ and $H(q^n)$. We also establish several reciprocity theorems, integral representation and explicit evaluations of the continued fraction $H(q)$ which are analogous to the results of Rogers-Ramanujan continued fraction and Ramanujan's cubic continued fractions.

For $q = e^{-\sqrt{5}\pi}$, we obtain:

$$H(e^{-\sqrt{5}\pi}) = \frac{\sqrt[4]{126\sqrt{5} + 72\sqrt{15} - 162\sqrt{3} - 279} - 1}{\sqrt[4]{126\sqrt{5} + 72\sqrt{15} - 162\sqrt{3} - 279} + 1},$$

$$\frac{(((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))-1))))}{(((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))+1))))}$$

$$\frac{1}{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15} - 1}} + \frac{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15} - 1}}$$

Minimal polynomial:

$$x^{16} - 1136x^{15} + 12216x^{14} - 55888x^{13} + 185564x^{12} - 455280x^{11} + 827656x^{10} - 1167056x^9 + 1308870x^8 - 1167056x^7 + 827656x^6 - 455280x^5 + 185564x^4 - 55888x^3 + 12216x^2 - 1136x + 1$$

$$1/9 * 1 / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4)))))-1)))) / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))+1)))))))))$$

Input:

$$\frac{1}{9} \times \frac{1}{\frac{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279-1}}{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279+1}}}$$

Result:

$$\frac{1 + \sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{9 \left(\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15} - 1} \right)}$$

Decimal approximation:

125.0207948017418741259298996839993367978542796511423133966...

125.02079....result practically equal to the boson Higgs mass 125.18

Alternate forms:

$$\frac{1 + \sqrt{3} \sqrt[4]{-31 - 18\sqrt{3} + 14\sqrt{5} + 8\sqrt{15}}}{9 \left(\sqrt{3} \sqrt[4]{-31 - 18\sqrt{3} + 14\sqrt{5} + 8\sqrt{15}} - 1 \right)}$$

$$\frac{\sqrt{3} \left[\text{root of } x^{16} + 124x^{12} - 58x^8 - 4x^4 + 1 \text{ near } x = 0.578377 \right] + 1}{9 \left(\sqrt{3} \left[\text{root of } x^{16} + 124x^{12} - 58x^8 - 4x^4 + 1 \text{ near } x = 0.578377 \right] - 1 \right)}$$

$$\frac{1}{9 \left(\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} - 1 \right)} + \frac{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{9 \left(\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} - 1 \right)}$$

$$1/8 * 1 / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))-1)))) / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))+1)))))))))$$

Input:

$$\frac{1}{8} \times \frac{1}{\frac{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279}-1}{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279}+1}}$$

Result:

$$\frac{1 + \sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{8 \left(\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} - 1 \right)}$$

Decimal approximation:

140.6483941519596083916711371444992538975860646075351025711...

140.64839....value very near to the rest mass of Pion 139.570

$$(27*23)+ 1 / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))-1)))) / (((((((((((((126*\text{sqrt}(5)+72*\text{sqrt}(15)-162*\text{sqrt}(3)-279)))^1/4))))+1)))))))))$$

Input:

$$27 \times 23 + \frac{1}{\frac{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279}-1}{\sqrt[4]{126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279}+1}}$$

Exact result:

$$621 + \frac{1 + \sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} - 1}$$

Decimal approximation:

1746.187153215676867133369097155994031180688516860280820569...

1746.187... result very near to the mass of scalar meson $f_0(1710)$ “candidate glueball”

$$(1746.187153215676867133369097155994031180688516860280820569)^{1/15}$$

Minimal polynomial:

$$x^{224} - 1136 x^{210} + 12216 x^{196} - 55888 x^{182} + 185564 x^{168} - 455280 x^{154} + 827656 x^{140} - 1167056 x^{126} + 1308870 x^{112} - 1167056 x^{98} + 827656 x^{84} - 455280 x^{70} + 185564 x^{56} - 55888 x^{42} + 12216 x^{28} - 1136 x^{14} + 1$$

We have also:

$$\frac{\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279\right)\right)^{1/4}\right)\right)-1\right)\right)\right)\right)\right)-1\right)\right)\right)\right)\right)^{1/4096}}{\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(126\sqrt{5}+72\sqrt{15}-162\sqrt{3}-279\right)\right)^{1/4}\right)\right)+1\right)\right)\right)\right)\right)+1\right)\right)\right)\right)\right)^{1/4096}}$$

Input:

$$\sqrt[4096]{\frac{\sqrt[4]{126\sqrt{5} + 72\sqrt{15} - 162\sqrt{3} - 279} - 1}{\sqrt[4]{126\sqrt{5} + 72\sqrt{15} - 162\sqrt{3} - 279} + 1}}$$

Decimal approximation:

0.998286210291019421519656145508340707669843748913925655326...

0.99828621.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5} - \phi + 1} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Alternate forms:

$$\left(\frac{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}}}{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} + 1} - \frac{1}{\sqrt[4]{-279 - 162\sqrt{3} + 126\sqrt{5} + 72\sqrt{15}} + 1} \right)^{(1/4096)}$$

$$\sqrt[4096]{\frac{\sqrt{3} \sqrt[4]{-31 - 18\sqrt{3} + 14\sqrt{5} + 8\sqrt{15}} - 1}{1 + \sqrt{3} \sqrt[4]{-31 - 18\sqrt{3} + 14\sqrt{5} + 8\sqrt{15}}}}$$

$$\sqrt[4096]{\frac{\sqrt{3} \left[\text{root of } x^{16} + 124x^{12} - 58x^8 - 4x^4 + 1 \text{ near } x = 0.578377 \right] - 1}{\sqrt{3} \left[\text{root of } x^{16} + 124x^{12} - 58x^8 - 4x^4 + 1 \text{ near } x = 0.578377 \right] + 1}}$$

For $q = e^{-\sqrt{7}\pi}$, we obtain:

$$H(e^{-\sqrt{7}\pi}) = \frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3} \right)^3}}{\sqrt{12\sqrt{2}} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3} \right)^3}}$$

Numerator:

$$\left(\left(\left(\left(\left(\left(\sqrt{12 \cdot \sqrt{2}} \right) - \left(\left(\left(\left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}} \right) \cdot \left(\left(\sqrt{5 + \sqrt{21}} \right) + \sqrt{\sqrt{21} - 3} \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right)^{1/4}$$

Input:

$$\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3} \right)^3}$$

Result:

$$2\sqrt[4]{2} \sqrt{3} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{\sqrt{21} - 3} + \sqrt{5 + \sqrt{21}} \right)^3}$$

Decimal approximation:

0.002022387189147699537072259421845574314522368625485931442...

Denominator:

$$\left(\left(\left(\left(\left(\sqrt{12\sqrt{2}}\right) + \left(\left(\left(\left(32 + \left(\left(\sqrt{5 + \sqrt{21}}\right) * \left(\left(\sqrt{5 + \sqrt{21}}\right) + \sqrt{\sqrt{21} - 3}\right) - 3\right)^3\right)\right)\right)\right)\right)\right)^{1/4}\right)$$

Input:

$$\sqrt{12\sqrt{2}} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3}\right)^3}$$

Result:

$$2\sqrt[4]{2}\sqrt{3} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{\sqrt{21} - 3} + \sqrt{5 + \sqrt{21}}\right)^3}$$

Decimal approximation:

8.237046188439323323784036761382197546096248607996130382946...

$$\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\sqrt{12\sqrt{2}}\right) - \left(\left(\left(\left(32 + \left(\left(\sqrt{5 + \sqrt{21}}\right) * \left(\left(\sqrt{5 + \sqrt{21}}\right) + \sqrt{\sqrt{21} - 3}\right) - 3\right)^3\right)\right)\right)\right)\right)\right)\right)\right)^{1/4}\right)\right)\right) / 8.2370461884393$$

Input interpretation:

$$\frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3}\right)^3}}{8.2370461884393}$$

Result:

0.00024552335180372...

0.0002455233518...

We have that:

$$1 / \left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\sqrt{12\sqrt{2}}\right) - \left(\left(\left(\left(32 + \left(\left(\sqrt{5 + \sqrt{21}}\right) * \left(\left(\sqrt{5 + \sqrt{21}}\right) + \sqrt{\sqrt{21} - 3}\right) - 3\right)^3\right)\right)\right)\right)\right)\right)\right)\right)^{1/4}\right)\right)\right) / 8.2370461884393233\right)$$

Input interpretation:

$$\frac{1}{\sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3}\right)^3} - \sqrt{12\sqrt{2}}}$$

8.2370461884393233

Result:

4072.9323408692504...

Input interpretation:

1630.60016562066232 + 21 × 2

Result:

1672.60016562066232

1672.6 result practically equal to the rest mass of Omega baryon 1672.45

We have also:

$$\frac{\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\sqrt{12 \cdot \sqrt{2}}\right) - \left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}}\right) \cdot \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3}\right)^3\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)^{1/4}\right)^{1/4}}{8.2370461884393}^{1/4096}$$

Input interpretation:

$$\sqrt[4096]{\frac{\sqrt{12 \sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} + \sqrt{\sqrt{21} - 3}\right)^3}}{8.2370461884393}}$$

Result:

0.997972731884807330...

0.9979727318.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = φ**

We have that:

$$H\left(e^{-\frac{\pi}{\sqrt{7}}}\right) = \frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}}(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{\sqrt{12\sqrt{2}} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}}(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}$$

Numerator:

$$\left(\left(\left(\sqrt{12\sqrt{2}} - \left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}}\right) \cdot \left(\sqrt{5 + \sqrt{21}}\right) - \sqrt{\sqrt{21} - 3}\right)\right)^3\right)\right)\right)\right)^{1/4}$$

Input:

$$\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3}\right)^3}$$

Result:

$$2\sqrt[4]{2} \sqrt{3} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3}\right)^3}$$

Decimal approximation:

1.444474422940832231298382761337628199571471558632462055729...

Denominator:

$$\left(\left(\left(\sqrt{12\sqrt{2}} + \left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}}\right) \cdot \left(\sqrt{5 + \sqrt{21}}\right) - \sqrt{\sqrt{21} - 3}\right)\right)^3\right)\right)\right)\right)^{1/4}$$

Input:

$$\sqrt{12\sqrt{2}} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3}\right)^3}$$

Result:

$$2\sqrt[4]{2} \sqrt{3} + \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3}\right)^3}$$

Decimal approximation:

6.794594152687638792022726259466414920839299417989154258658...

$$\left(\left(\left(\left(\left(\left(\left(\sqrt{12\sqrt{2}} - \left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}}\right) \cdot \left(\sqrt{5 + \sqrt{21}}\right) - \sqrt{\sqrt{21} - 3}\right)\right)^3\right)\right)\right)\right)\right)\right)^{1/4}\right) / 6.794594152687638792$$

Input interpretation:

$$\frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.794594152687638792}$$

Result:

0.2125917148957988155...

0.2125917...

We obtain:

$$1/2 * \exp \left(\left(\left(\left(\left(\left(\sqrt{12 * \sqrt{2}} \right) - \left(\left(\left(32 + \left(\sqrt{5 + \sqrt{21}} \right) * \left(\sqrt{5 + \sqrt{21}} \right) - \sqrt{\sqrt{21} - 3} \right) \right)^3 \right) \right) \right) \right) \right) \right)^{1/4} \right) / 6.794594152687638792$$

Input interpretation:

$$\frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.794594152687638792} \right)$$

Result:

0.61843977432114073210...

0.6184397743.... a result very near to the reciprocal of the golden ratio

Series representations:

$$\frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - \sqrt[4]{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) =$$

$$\frac{1}{2} \exp \left(0.14717582500559574164858 \right.$$

$$\left. \left(\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (12\sqrt{2} - z_0)^k z_0^{-k}}{k!} - \left(32 + \sqrt{z_0}^4 \right. \right.$$

$$\left. \left. \left(\sum_{k=0}^{\infty} \frac{(-1)^{1+k} \left(-\frac{1}{2}\right)_k \left((-3 + \sqrt{21} - z_0)^k - (5 + \sqrt{21} - z_0)^k \right) z_0^{-k}}{k!} \right)^3 \right. \right.$$

$$\left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (5 + \sqrt{21} - z_0)^k z_0^{-k}}{k!} \right)^{\wedge (1/4)} \right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) =$$

$$\frac{1}{2} \exp \left(0.14717582500559574164858 \right.$$

$$\left. \left(\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (12\sqrt{2} - z_0)^k z_0^{-k}}{k!} - \left(32 + \sqrt{z_0} \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} \left(-\frac{1}{2}\right)_k \right. \right. \right.$$

$$\left. \left. \left. \sqrt{z_0} \left((-3 + \sqrt{21} - z_0)^k - (5 + \sqrt{21} - z_0)^k \right) z_0^{-k} \right)^3 \right. \right.$$

$$\left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (5 + \sqrt{21} - z_0)^k z_0^{-k}}{k!} \right)^{\wedge (1/4)} \right) \right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) =$$

$$\frac{1}{2} \exp \left(0.14717582500559574164858 \right.$$

$$\left(\exp \left(i\pi \left\lfloor \frac{\arg(-x + 12\sqrt{2})}{2\pi} \right\rfloor \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left(-\frac{1}{2}\right)_k (-x + 12\sqrt{2})^k}{k!} - \right.$$

$$\left(32 + \exp \left(i\pi \left\lfloor \frac{\arg(5 - x + \sqrt{21})}{2\pi} \right\rfloor \right) \sqrt{x} \right.$$

$$\left. \left(\sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left(-\frac{1}{2}\right)_k (5 - x + \sqrt{21})^k}{k!} \right) \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} x^{-k} \left(-\frac{1}{2}\right)_k \right. \right.$$

$$\left. \left(\exp \left(i\pi \left\lfloor \frac{\arg(-3 - x + \sqrt{21})}{2\pi} \right\rfloor \right) (-3 - x + \sqrt{21})^k - \right.$$

$$\left. \left. \exp \left(i\pi \left\lfloor \frac{\arg(5 - x + \sqrt{21})}{2\pi} \right\rfloor \right) (5 - x + \sqrt{21})^k \right) \right.$$

$$\left. \left. \left. \sqrt{x} \right)^3 \right)^{\wedge (1/4)} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$1 + \frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) =$$

$$\frac{1}{2} \left(2 + \exp \left(0.14717582500559574164858 \right. \right.$$

$$\left. \left. \left(\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (12\sqrt{2} - z_0)^k z_0^{-k}}{k!} - \right. \right.$$

$$\left. \left. \left(32 + \sqrt{z_0} \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} \left(-\frac{1}{2}\right)_k \sqrt{z_0} \right. \right. \right.$$

$$\left. \left. \left. \left((-3 + \sqrt{21} - z_0)^k - (5 + \sqrt{21} - z_0)^k \right) z_0^{-k} \right)^3 \right. \right.$$

$$\left. \left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (5 + \sqrt{21} - z_0)^k z_0^{-k}}{k!} \right)^{\wedge (1/4)} \right) \right) \right) \right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$1 + \frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) =$$

$$\frac{1}{2} \left(2 + \exp \left(0.14717582500559574164858 \right. \right.$$

$$\left. \left. \left(\exp \left(i\pi \left[\frac{\arg(-x + 12\sqrt{2})}{2\pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left(-\frac{1}{2}\right)_k (-x + 12\sqrt{2})^k}{k!} - \right. \right.$$

$$\left. \left. \left(32 + \exp \left(i\pi \left[\frac{\arg(5 - x + \sqrt{21})}{2\pi} \right] \right) \sqrt{x} \right. \right.$$

$$\left. \left. \left(\sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left(-\frac{1}{2}\right)_k (5 - x + \sqrt{21})^k}{k!} \right) \right. \right.$$

$$\left. \left. \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} x^{-k} \left(-\frac{1}{2}\right)_k \left(\exp \left(i\pi \left[\frac{\arg(-3 - x + \sqrt{21})}{2\pi} \right] \right) \right. \right. \right.$$

$$\left. \left. \left. \left((-3 - x + \sqrt{21})^k - \exp \left(\right. \right. \right.$$

$$\left. \left. \left. \left. \left. i\pi \left[\frac{\arg(5 - x + \sqrt{21})}{2\pi} \right] \right) \right) (5 - x + \sqrt{21})^k \right) \right. \right.$$

$$\left. \left. \left. \left. \left. \sqrt{x} \right)^3 \right)^{\wedge (1/4)} \right) \right) \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

We have also that:

$$(729+108)+10^3((((1 + 1/2 * \exp (((((((((\sqrt{12*\sqrt{2}}) - (((((32+(\sqrt{5+\sqrt{21}})*((\sqrt{5+\sqrt{21}})-\sqrt{\sqrt{21}-3}))^3)))))))))^1/4)))))) / 6.794594152687638792))))))$$

where $729 = 27^2 = 9^3$ and $108 = 27 * 4$

Input interpretation:

$$(729 + 108) + 10^3 \left(1 + \frac{1}{2} \exp \left(\frac{\sqrt{12 \sqrt{2}} - 4 \sqrt{32 + \sqrt{5 + \sqrt{21}}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3} \right)^3}{6.794594152687638792} \right) \right)$$

Result:

2455.4397743211407321...

2455.4397... result very near to the rest mass of charmed Sigma baryon 2453.98

And:

$$108+10^3((((1 + 1/2 * \exp (((((((((\sqrt{12*\sqrt{2}}) - (((((32+(\sqrt{5+\sqrt{21}})*((\sqrt{5+\sqrt{21}})-\sqrt{\sqrt{21}-3}))^3)))))))))^1/4)))))) / 6.794594152687638792))))))$$

Input interpretation:

$$108 + 10^3 \left(1 + \frac{1}{2} \exp \left(\frac{\sqrt{12 \sqrt{2}} - 4 \sqrt{32 + \sqrt{5 + \sqrt{21}}} \left(\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3} \right)^3}{6.794594152687638792} \right) \right)$$

Result:

1726.4397743211407321...

1726.43977...result very near to the mass of scalar meson $f_0(1710)$ “candidate glueball”

Series representations:

$$\begin{aligned}
& 108 + 10^3 \left(1 + \frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) \right) = \\
& 4 \left(277 + 125 \exp \left(0.14717582500559574164858 \right. \right. \\
& \quad \left. \left(\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (12\sqrt{2} - z_0)^k z_0^{-k}}{k!} - \right. \right. \\
& \quad \left. \left(32 + \sqrt{z_0}^4 \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} \left(-\frac{1}{2}\right)_k \right. \right. \right. \\
& \quad \quad \left. \left. \left. \left((-3 + \sqrt{21} - z_0)^k - (5 + \sqrt{21} - z_0)^k \right) z_0^{-k} \right)^3 \right. \right. \\
& \quad \left. \left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (5 + \sqrt{21} - z_0)^k z_0^{-k}}{k!} \right)^{\wedge (1/4)} \right) \right) \right) \\
& \text{for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
\end{aligned}$$

$$\begin{aligned}
& 108 + 10^3 \left(1 + \frac{1}{2} \exp \left(\frac{\sqrt{12\sqrt{2}} - 4\sqrt{32 + \sqrt{5 + \sqrt{21}} (\sqrt{5 + \sqrt{21}} - \sqrt{\sqrt{21} - 3})^3}}{6.7945941526876387920000} \right) \right) = \\
& 4 \left(277 + 125 \exp \left(0.14717582500559574164858 \right. \right. \\
& \quad \left. \left(\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (12\sqrt{2} - z_0)^k z_0^{-k}}{k!} - \right. \right. \\
& \quad \left. \left(32 + \sqrt{z_0} \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^{1+k} \left(-\frac{1}{2}\right)_k \sqrt{z_0} \right. \right. \right. \\
& \quad \quad \left. \left. \left. \left((-3 + \sqrt{21} - z_0)^k - (5 + \sqrt{21} - z_0)^k \right) z_0^{-k} \right)^3 \right. \right. \\
& \quad \left. \left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (5 + \sqrt{21} - z_0)^k z_0^{-k}}{k!} \right)^{\wedge (1/4)} \right) \right) \right) \\
& \text{for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
\end{aligned}$$

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Now, we have that:

$$H(e^{-\pi\sqrt{\frac{11}{3}}}) = \frac{\sqrt[4]{18} - \sqrt[4]{2 + (\sqrt{11} + 3)^2(\sqrt{3} - 1)^3}}{\sqrt[4]{18} + \sqrt[4]{2 + (\sqrt{11} + 3)^2(\sqrt{3} - 1)^3}}$$

$$\frac{((((18)^{1/4} - (((2 + ((\sqrt{11} + 3)^2 * ((\sqrt{3} - 1)^3)))^{1/4}))))}{((((18)^{1/4} + (((2 + ((\sqrt{11} + 3)^2 * ((\sqrt{3} - 1)^3)))^{1/4}))))}$$

Input:

$$\frac{\sqrt[4]{18} - \sqrt[4]{2 + (\sqrt{11} + 3)^2(\sqrt{3} - 1)^3}}{\sqrt[4]{18} + \sqrt[4]{2 + (\sqrt{11} + 3)^2(\sqrt{3} - 1)^3}}$$

Result:

$$\frac{\sqrt[4]{2} \sqrt{3} - \sqrt[4]{2 + (\sqrt{3} - 1)^3(3 + \sqrt{11})^2}}{\sqrt[4]{2} \sqrt{3} + \sqrt[4]{2 + (\sqrt{3} - 1)^3(3 + \sqrt{11})^2}}$$

Decimal approximation:

0.002434204968175911613449619811575564415044145807636374010...

Alternate forms:

$$\frac{\sqrt[4]{2} \sqrt{3} - \sqrt[4]{-198 + 120\sqrt{3} - 60\sqrt{11} + 36\sqrt{33}}}{\sqrt[4]{-198 + 120\sqrt{3} - 60\sqrt{11} + 36\sqrt{33}} + \sqrt[4]{2} \sqrt{3}}$$

$$\frac{\sqrt[4]{3} - \sqrt[4]{-33 + 20\sqrt{3} - 10\sqrt{11} + 6\sqrt{33}}}{\sqrt[4]{3} + \sqrt[4]{-33 + 20\sqrt{3} - 10\sqrt{11} + 6\sqrt{33}}}$$

$$\frac{\boxed{\text{root of } x^{16} + 132x^{12} - 442x^8 + 132x^4 + 1 \text{ near } x = 1.30968} - \sqrt[4]{3}}{\boxed{\text{root of } x^{16} + 132x^{12} - 442x^8 + 132x^4 + 1 \text{ near } x = 1.30968} + \sqrt[4]{3}}$$

$$3 / (((((18)^{1/4} - ((2+((\sqrt{11}+3)^2*((\sqrt{3}-1)^3)))^{1/4})))) / (((((18)^{1/4} + ((2+((\sqrt{11}+3)^2*((\sqrt{3}-1)^3)))^{1/4}))))))$$

Input:

$$\frac{3}{\frac{\sqrt[4]{18} - \sqrt[4]{2+(\sqrt{11}+3)^2(\sqrt{3}-1)^3}}{\sqrt[4]{18} + \sqrt[4]{2+(\sqrt{11}+3)^2(\sqrt{3}-1)^3}}}$$

Result:

$$\frac{3 \left(\sqrt[4]{2} \sqrt{3} + \sqrt[4]{2+(\sqrt{3}-1)^3(3+\sqrt{11})^2} \right)}{\sqrt[4]{2} \sqrt{3} - \sqrt[4]{2+(\sqrt{3}-1)^3(3+\sqrt{11})^2}}$$

Decimal approximation:

1232.435246505996091334470692810017998960475171020930664651...

1232.4352...result practically equal to the rest mass of Delta baryon 1232

$$((((3 / (((((18)^{1/4} - ((2+((\sqrt{11}+3)^2*((\sqrt{3}-1)^3)))^{1/4})))) / (((((18)^{1/4} + ((2+((\sqrt{11}+3)^2*((\sqrt{3}-1)^3)))^{1/4})))))))))^{1/14}$$

Input:

$$\sqrt[14]{\frac{3}{\frac{\sqrt[4]{18} - \sqrt[4]{2+(\sqrt{11}+3)^2(\sqrt{3}-1)^3}}{\sqrt[4]{18} + \sqrt[4]{2+(\sqrt{11}+3)^2(\sqrt{3}-1)^3}}}}$$

Alternate forms:

$$\sqrt[4096]{\frac{\sqrt[4]{2} \sqrt{3} - \sqrt[4]{-198 + 120 \sqrt{3} - 60 \sqrt{11} + 36 \sqrt{33}}}{\sqrt[4]{-198 + 120 \sqrt{3} - 60 \sqrt{11} + 36 \sqrt{33}} + \sqrt[4]{2} \sqrt{3}}}$$

$$\sqrt[4096]{\frac{\sqrt[4]{3} - \sqrt[4]{-33 + 20 \sqrt{3} - 10 \sqrt{11} + 6 \sqrt{33}}}{\sqrt[4]{3} + \sqrt[4]{-33 + 20 \sqrt{3} - 10 \sqrt{11} + 6 \sqrt{33}}}}$$

$$\sqrt[4096]{\frac{\boxed{\text{root of } x^{16} + 132 x^{12} - 442 x^8 + 132 x^4 + 1 \text{ near } x = 1.30968} - \sqrt[4]{3}}{\boxed{\text{root of } x^{16} + 132 x^{12} - 442 x^8 + 132 x^4 + 1 \text{ near } x = 1.30968} + \sqrt[4]{3}}}}$$

From:

New Properties for The Ramanujan’S Continued Fraction of Order 12
*Chandrashekar Adiga**, *M. S. Surekha*, *A. Vanitha* Department of Studies in Mathematics, University of Mysore, Manasagangotri, Mysore 570 006, INDIA
 *Corresponding author: c_adiga@hotmail.com Received May 07, 2014; Revised June 24, 2014; Accepted July 03, 2014

Similarly, by Jacobi’s triple product identity, we have

$$\begin{aligned} \psi(-q^3) &= (q^3; q^{12})_{\infty} (q^9; q^{12})_{\infty} (q^{12}; q^{12})_{\infty} \\ &= \prod_{n=0}^{\infty} (1 - q^{12n+3})(1 - q^{12n+9})(1 - q^{12n+12}) \\ &= \prod_{n=0}^{\infty} (1 - q^{12n+3} (1 + q^9 + q^6 - q^{12n+9} \\ &\quad (1 + q^9 + q^3) + q^{24n+21})). \end{aligned} \tag{83}$$

For $q = 0.5$ and $n = 2$, we obtain:

$$((1-(0.5)^{27})) * (((1+0.5^9+0.5^6-0.5^{33}*(1+0.5^9+0.5^3)+0.5^{69})))$$

Input:

$$(1 - 0.5^{27}) (1 + 0.5^9 + 0.5^6 - 0.5^{33} (1 + 0.5^9 + 0.5^3) + 0.5^{69})$$

Result:

1.017578117287257556269295397434339407713819621899078451086...

1.01757811...

$$((1-(0.5)^{27}) * (((1+0.5^9+0.5^6-0.5^{33}*(1+0.5^9+0.5^3)+0.5^{69})))^{29})$$

Input:

$$(1 - 0.5^{27}) (1 + 0.5^9 + 0.5^6 - 0.5^{33} (1 + 0.5^9 + 0.5^3) + 0.5^{69})^{29}$$

Result:

1.657544140532976993172413501760433669992985095787415892724...

1.65754414..... result that is very near to the 14th root of the following Ramanujan's class invariant $Q = (G_{505}/G_{101/5})^3 = 1164,2696$ i.e. 1,65578...

Note that:

$$2\sqrt{6(((1-(0.5)^{27}) * (((1+0.5^9+0.5^6-0.5^{33}*(1+0.5^9+0.5^3)+0.5^{69})))^{29})))}$$

Input:

$$2\sqrt{6((1 - 0.5^{27})(1 + 0.5^9 + 0.5^6 - 0.5^{33}(1 + 0.5^9 + 0.5^3) + 0.5^{69})^{29})}$$

Open code

Enlarge Data Customize A Plaintext Interactive

Result:

6.30722...

6.30722...result that is a length of a circle with radius equal to 1.00383

We have also that:

$$1/((((1-(0.5)^{27}) * (((1+0.5^9+0.5^6-0.5^{33}*(1+0.5^9+0.5^3)+0.5^{69}))))))^{1/8}$$

Input:

$$\frac{1}{\sqrt[8]{(1 - 0.5^{27})(1 + 0.5^9 + 0.5^6 - 0.5^{33}(1 + 0.5^9 + 0.5^3) + 0.5^{69})}}$$

Result:

0.99782419...

0.99782419.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Since $1 - (\zeta^{11} + \zeta) = 1 - \sqrt{3}$ and $\zeta^{12} = 1$, we have

$$\begin{aligned} & \frac{f(\zeta, \zeta^{11} q^{1/3})}{(1 + \zeta)} \\ &= \prod_{n=1}^{\infty} (1 + (1 - \sqrt{3})((q^{1/3})^{2n} - (q^{1/3})^n) - q^n) \quad (82) \\ &= \prod_{n=1}^{\infty} (1 + (\alpha - 1)((q^{1/3})^{2n} - (q^{1/3})^n) - q^n). \end{aligned}$$

((((((1+(0.0864055-1)((0.5^(1/3))))^4-((0.5^(1/3))^2))))-0.5^2))))))

Input interpretation:

$$\left(\left(1 + (0.0864055 - 1) \sqrt[3]{0.5} \right)^4 - \sqrt[3]{0.5^2} \right) - 0.5^2$$

Enlarge Data Customize A Plaintext Interactive

Result:

-0.874251...

-0.874251...

sqrt(((((-3 (((((1+(0.0864055-1)((0.5^(1/3))))^4-((0.5^(1/3))^2))))-0.5^2))))))))))

Input interpretation:

$$\sqrt{-3 \left(\left(1 + (0.0864055 - 1) \sqrt[3]{0.5} \right)^4 - \sqrt[3]{0.5^2} \right) - 0.5^2}$$

Result:

1.61949...

1.61949... result that is very near to the golden ratio

$$27 \times 2 + 10^3 \sqrt{-3 \left(\left(\left(\left(1 + (0.0864055 - 1) \left(0.5^{1/3} \right) \right)^4 - \left(0.5^{1/3} \right)^2 \right) - 0.5^2 \right) \right) \right)}$$

Input interpretation:

$$27 \times 2 + 10^3 \sqrt{-3 \left(\left(\left(1 + (0.0864055 - 1) \sqrt[3]{0.5} \right)^4 - \sqrt[3]{0.5^2} \right) - 0.5^2 \right)}$$

Open code

Enlarge Data Customize A Plaintext Interactive

Result:

1673.49...

1673.49... result that is very near to the rest mass of Omega baryon 1672.45

We have also that:

$$-\left(\left(\left(\left(1 + (0.0864055 - 1) \left(0.5^{1/3} \right) \right)^4 - \left(0.5^{1/3} \right)^2 \right) - 0.5^2 \right) \right)^{1/64}$$

Input interpretation:

$$-\sqrt[64]{ \left(\left(\left(1 + (0.0864055 - 1) \sqrt[3]{0.5} \right)^4 - \sqrt[3]{0.5^2} \right) - 0.5^2 \right)}$$

Result:

-0.99670038... -

0.048964750... i

Polar coordinates:

r = 0.997902 (radius), θ = -177.188° (angle)

0.997902 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

$$\frac{1 + \sqrt[5]{\sqrt{\varphi^5 4\sqrt{5^3} - 1}}}{\sqrt{5}} - \varphi + 1$$

and to the dilaton value $0.989117352243 = \phi$

Appendix

From:

Rotating strings confronting PDG mesons

Jacob Sonnenschein and Dorin Weissman - arXiv:1402.5603v1 [hep-ph] 23 Feb 2014

c \bar{c} . **The Ψ trajectory:** The left side of figure (15) depicts the Ψ trajectory. Here we use the states $J/\Psi(1S)(3097)1^{--}$, $\chi_{c1}(1P)(3510)1^{++}$, and $\Psi(3770)1^{--}$. Since no $J = 3$ state has been observed, we use three states with $J = 1$, but with increasing orbital angular momentum ($L = 0, 1, 2$) and do the fit to L instead of J . To give an idea of the shifts in mass involved, the $J^{PC} = 2^{++}$ state χ_{c2} has a mass of 3556 MeV, and the $J^{PC} = 3^{--}$ state is expected to lie 30 – 60 MeV above the $\Psi(3770)$ [23].

The best linear fit is

$$\alpha' = 0.418, a = -4.04$$

with $\chi_l^2 = 3.41 \times 10^{-4}$, but the optimal fit is far from the linear, with endpoint masses in the range of the constituent c quark mass:

$$m_c = 1500, \alpha' = 0.979, a = -0.09$$

with $\chi_m^2 = 5 \times 10^{-7}$ ($\chi_m^2/\chi_l^2 = 0.002$). Aside from the improvement in χ^2 , by adding the mass we also get a value for the slope (and to a lesser extent, the intercept) that is much closer to that obtained in fits for the light meson trajectories.

where α' is the Regge slope (string tension)

We know also that:

$$\omega \quad | \quad 6 \quad | \quad m_{u/d} = 0 - 60 \quad | \quad 0.910 - 0.918$$

$$\omega/\omega_3 \mid 5 + 3 \mid m_{u/d} = 255 - 390 \mid 0.988 - 1.18$$

$$\omega/\omega_3 \mid 5 + 3 \mid m_{u/d} = 240 - 345 \mid 0.937 - 1.000$$

The average of the various Regge slope of Omega mesons are:

$$1/7 * (0.979 + 0.910 + 0.918 + 0.988 + 0.937 + 1.18 + 1) = 0.987428571$$

result very near to the value of dilaton and to the solution 0.987516007... of the above expression.

From:

Astronomy & Astrophysics manuscript no. ms c ESO 2019 - September 24, 2019
Planck 2018 results. VI. Cosmological parameters

The primordial fluctuations are consistent with Gaussian purely adiabatic scalar perturbations characterized by a power spectrum with a [spectral index \$n_s = 0.965 \pm 0.004\$](#) , consistent with the predictions of slow-roll, single-field, inflation.

from:

Modular equations and approximations to π - *Srinivasa Ramanujan*
 Quarterly Journal of Mathematics, XLV, 1914, 350 – 372

We have that:

Hence

$$\begin{aligned} 64g_{22}^{24} &= e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots, \\ 64g_{22}^{-24} &= 4096e^{-\pi\sqrt{22}} + \dots, \end{aligned}$$

so that

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982\dots$$

Again

$$G_{37} = (6 + \sqrt{37})^{\frac{1}{4}},$$

$$\begin{aligned} 64G_{37}^{24} &= e^{\pi\sqrt{37}} + 24 + 276e^{-\pi\sqrt{37}} + \dots, \\ 64G_{37}^{-24} &= 4096e^{-\pi\sqrt{37}} - \dots, \end{aligned}$$

so that

$$64(G_{37}^{24} + G_{37}^{-24}) = e^{\pi\sqrt{37}} + 24 + 4372e^{-\pi\sqrt{37}} - \dots = 64\{(6 + \sqrt{37})^6 + (6 - \sqrt{37})^6\}.$$

Hence

$$e^{\pi\sqrt{37}} = 199148647.999978\dots$$

Similarly, from

$$g_{58} = \sqrt{\left(\frac{5 + \sqrt{29}}{2}\right)},$$

we obtain

$$64(g_{58}^{24} + g_{58}^{-24}) = e^{\pi\sqrt{58}} - 24 + 4372e^{-\pi\sqrt{58}} - \dots = 64\left\{\left(\frac{5 + \sqrt{29}}{2}\right)^{12} + \left(\frac{5 - \sqrt{29}}{2}\right)^{12}\right\}.$$

Hence

$$e^{\pi\sqrt{58}} = 24501257751.99999982\dots$$

From:

An Update on Brane Supersymmetry Breaking

J. Mourad and A. Sagnotti - arXiv:1711.11494v1 [hep-th] 30 Nov 2017

From the following vacuum equations:

$$T e^{\gamma_E \phi} = - \frac{\beta_E^{(p)} h^2}{\gamma_E} e^{-2(8-p)C + 2\beta_E^{(p)} \phi}$$

$$16 k' e^{2C} = \frac{h^2 \left(p + 1 - \frac{2\beta_E^{(p)}}{\gamma_E} \right) e^{-2(8-p)C + 2\beta_E^{(p)} \phi}}{(7-p)}$$

$$(A')^2 = k e^{-2A} + \frac{h^2}{16(p+1)} \left(7 - p + \frac{2\beta_E^{(p)}}{\gamma_E} \right) e^{-2(8-p)C + 2\beta_E^{(p)} \phi}$$

we have obtained, from the results almost equals of the equations, putting

$4096 e^{-\pi\sqrt{18}}$ instead of

$$e^{-2(8-p)C + 2\beta_E^{(p)} \phi}$$

a new possible mathematical connection between the two exponentials. Thence, also the values concerning p , C , β_E and ϕ correspond to the exponents of e (i.e. of exp). Thence we obtain for $p = 5$ and $\beta_E = 1/2$:

$$e^{-6C + \phi} = 4096 e^{-\pi\sqrt{18}}$$

Therefore, with respect to the exponentials of the vacuum equations, the Ramanujan's exponential has a coefficient of 4096 which is equal to 64^2 , while $-6C + \phi$ is equal to $-\pi\sqrt{18}$. From this it follows that it is possible to establish mathematically, the dilaton value.

For

$\exp((-Pi*\sqrt{18}))$ we obtain:

Input:

$$\exp\left(-\pi\sqrt{18}\right)$$

Exact result:

$$e^{-3\sqrt{2}\pi}$$

Decimal approximation:

$$1.6272016226072509292942156739117979541838581136954016... \times 10^{-6}$$

$$1.6272016... * 10^{-6}$$

Property:

$e^{-3\sqrt{2}\pi}$ is a transcendental number

Series representations:

$$e^{-\pi\sqrt{18}} = e^{-\pi\sqrt{17} \sum_{k=0}^{\infty} 17^{-k} \binom{1/2}{k}}$$

$$e^{-\pi\sqrt{18}} = \exp\left(-\pi\sqrt{17} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{17}\right)^k \binom{-\frac{1}{2}}{k}}{k!}\right)$$

$$e^{-\pi\sqrt{18}} = \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 17^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)$$

Now, we have the following calculations:

$$e^{-6C+\phi} = 4096e^{-\pi\sqrt{18}}$$

$$e^{-\pi\sqrt{18}} = 1.6272016... * 10^{-6}$$

from which:

$$\frac{1}{4096}e^{-6C+\phi} = 1.6272016... * 10^{-6}$$

$$0.000244140625 e^{-6C+\phi} = e^{-\pi\sqrt{18}} = 1.6272016... * 10^{-6}$$

Now:

$$\ln\left(e^{-\pi\sqrt{18}}\right) = -13.328648814475 = -\pi\sqrt{18}$$

And:

$$(1.6272016 * 10^{-6}) * 1 / (0.000244140625)$$

Input interpretation:

$$\frac{1.6272016}{10^6} \times \frac{1}{0.000244140625}$$

Result:

0.0066650177536

0.006665017...

Thence:

$$0.000244140625 e^{-6C+\phi} = e^{-\pi\sqrt{18}}$$

Dividing both sides by 0.000244140625, we obtain:

$$\frac{0.000244140625}{0.000244140625} e^{-6C+\phi} = \frac{1}{0.000244140625} e^{-\pi\sqrt{18}}$$

$$e^{-6C+\phi} = 0.0066650177536$$

$$(((\exp((-Pi*\sqrt{18})))))) * 1 / 0.000244140625$$

Input interpretation:

$$\exp(-\pi\sqrt{18}) \times \frac{1}{0.000244140625}$$

Result:

0.00666501785...

0.00666501785...

Series representations:

$$\frac{\exp(-\pi \sqrt{18})}{0.000244141} = 4096 \exp\left(-\pi \sqrt{17} \sum_{k=0}^{\infty} 17^{-k} \binom{\frac{1}{2}}{k}\right)$$

$$\frac{\exp(-\pi \sqrt{18})}{0.000244141} = 4096 \exp\left(-\pi \sqrt{17} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{17}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)$$

$$\frac{\exp(-\pi \sqrt{18})}{0.000244141} = 4096 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 17^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)$$

Now:

$$e^{-6C+\phi} = 0.0066650177536$$

$$\exp(-\pi \sqrt{18}) \times \frac{1}{0.000244140625} =$$

$$e^{-\pi \sqrt{18}} \times \frac{1}{0.000244140625}$$

$$= 0.00666501785\dots$$

From:

$$\ln(0.00666501784619)$$

Input interpretation:

$$\log(0.00666501784619)$$

Result:

$$-5.010882647757\dots$$

$$-5.010882647757\dots$$

Alternative representations:

$$\log(0.006665017846190000) = \log_e(0.006665017846190000)$$

$$\log(0.006665017846190000) = \log(a) \log_a(0.006665017846190000)$$

$$\log(0.006665017846190000) = -\text{Li}_1(0.993334982153810000)$$

Series representations:

$$\log(0.006665017846190000) = -\sum_{k=1}^{\infty} \frac{(-1)^k (-0.993334982153810000)^k}{k}$$

$$\log(0.006665017846190000) = 2i\pi \left[\frac{\arg(0.006665017846190000 - x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (0.006665017846190000 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\log(0.006665017846190000) = \left[\frac{\arg(0.006665017846190000 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(0.006665017846190000 - z_0)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (0.006665017846190000 - z_0)^k z_0^{-k}}{k}$$

Integral representation:

$$\log(0.006665017846190000) = \int_1^{0.006665017846190000} \frac{1}{t} dt$$

In conclusion:

$$-6C + \phi = -5.010882647757 \dots$$

and for $C = 1$, we obtain:

$$\phi = -5.010882647757 + 6 = 0.989117352243 = \phi$$

Note that the values of n_s (spectral index) 0.965, of the average of the Omega mesons Regge slope 0.987428571 and of the dilaton 0.989117352243, are also connected to the following two Rogers-Ramanujan continued fractions:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\phi-1)\sqrt{5}} - \phi + 1} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}}} \approx 0.9568666373$$

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

(<http://www.bitman.name/math/article/102/109/>)

Also performing the 512th root of the inverse value of the Pion meson rest mass 139.57, we obtain:

$$((1/(139.57)))^{1/512}$$

Input interpretation:

$$\sqrt[512]{\frac{1}{139.57}}$$

Result:

0.990400732708644027550973755713301415460732796178555551684...

0.99040073.... result very near to the dilaton value **0.989117352243 = ϕ** and to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

$$\frac{\sqrt{5}}{1 + \sqrt[5]{\sqrt{\phi^5 \sqrt[4]{5^3}} - 1}} - \phi + 1$$

From:

Eur. Phys. J. C (2019) 79:713 - <https://doi.org/10.1140/epjc/s10052-019-7225-2> - Regular Article - Theoretical Physics
Generalized dilaton–axion models of inflation, de Sitter vacua and spontaneous SUSY breaking in supergravity
Yermek Aldabergenov, Auttakit Chatrabhuti, Sergei V. Ketov

Table 1 The predictions for the inflationary parameters (n_s , r), and the values of φ at the horizon crossing (φ_i) and at the end of inflation (φ_f), in the case $3 \leq \alpha \leq \alpha_*$ with both signs of ω_1 . The α parameter is taken to be integer, except of the upper limit $\alpha_* \equiv (7 + \sqrt{33})/2$

α	3	4	5	6	α_*	
$\text{sgn}(\omega_1)$	–	+	–	+/–	+	–
n_s	0.9650	0.9649	0.9640	0.9639	0.9634	0.9632
r	0.0035	0.0010	0.0013	0.0007	0.0005	0.0003
$-\kappa\varphi_i$	5.3529	3.5542	3.9899	3.2657	3.0215	2.7427
$-\kappa\varphi_f$	0.9402	0.7426	0.8067	0.7163	0.6935	0.6276

Acknowledgments

I would like to thank Prof. **George E. Andrews** Evan Pugh Professor of Mathematics at Pennsylvania State University for his availability and kindness towards me

References

New Properties for The Ramanujan'S Continued Fraction of Order 12
*Chandrashekar Adiga**, *M. S. Surekha*, *A. Vanitha* Department of Studies in
Mathematics, University of Mysore, Manasagangotri, Mysore 570 006, INDIA
*Corresponding author: c_adiga@hotmail.com Received May 07, 2014; Revised June
24, 2014; Accepted July 03, 2014

A continued fraction of order twelve

Research Article

M.S. Mahadeva Naika, *B. N. Dharmendra*, *K. Shivashankara*- Department of
Mathematics, Bangalore University, Central College Campus, Bangalore - 560 001,
India - Department of Mathematics, Yuvaraja's College, University of Mysore,
Mysore-570 001, India - Received 27 November 2007; accepted 19 April 2008

Berndt, B. et al. "***The Rogers–Ramanujan Continued
Fraction***", <http://www.math.uiuc.edu/~berndt/articles/rrcf.pdf>

Berndt, B. et al. "***The Rogers–Ramanujan Continued Fraction***"

Andrews, G. ***On the General Rogers-Ramanujan Theorem***. Providence, RI: Amer.
Math. Soc., 1974.

Andrews, G. E.; Berndt, B. C.; Jacobsen, L.; and Lamphere, R. L. ***The Continued
Fractions Found in the Unorganized Portion of Ramanujan's
Notebooks***. Providence, RI: Amer. Math. Soc., 1992.