

# **On Ramanujan's mathematics applied to various sectors of Theoretical Physics and Cosmology: further possible new mathematical connections. II**

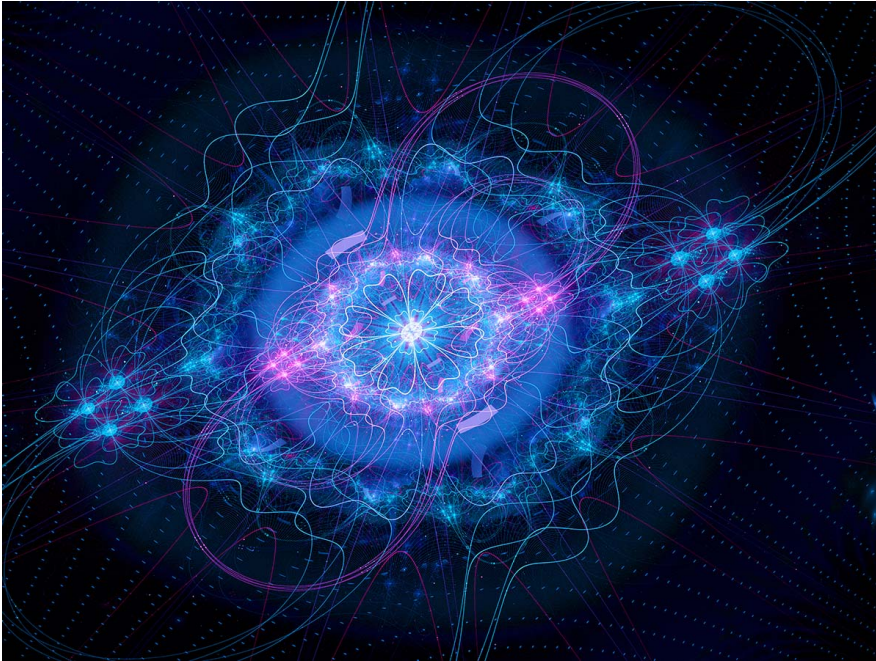
**Michele Nardelli<sup>1</sup>, Antonio Nardelli**

## **Abstract**

*In this research thesis, we have analyzed further Ramanujan equations and described the new possible mathematical connections with various sectors of Theoretical Physics (principally like-Higgs boson dilaton mass solutions) and Cosmology*

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<https://asgardia.space/en/news/Seems-There-a-Fifth-Fundamental-Force-in-Town>

**All the known forces of nature can be traced to 4 fundamental interactions: gravitational, electromagnetic, strong and weak forces. After spotting the same anomaly twice in two different atoms, scientists suggest that there's a fifth force mediated by newly-discovered boson, a so-called X-17 particle**

<https://imsbharat.wordpress.com/2016/12/22/national-mathematics-day-celebrating-ramanujams-birth-anniversary/>



An equation means nothing to me  
unless it expresses a thought of  
God.

— *Srinivasa Ramanujan* —

AZ QUOTES

From:

**Islands outside the horizon**

*Ahmed Almheiri, Raghu Mahajan, Juan Maldacena*

arXiv:1910.11077v2 [hep-th] 11 Nov 2019

We have that:

$$S = \frac{c}{3} \log \frac{\beta}{\pi}. \tag{27}$$

$$S = \frac{c}{3} \log \left[ \frac{\pi}{\beta} \cosh \left( \frac{2\pi t}{\beta} \right) \right] \rightarrow \frac{2\pi}{3} c \frac{t}{\beta} + \dots \quad \text{for } t \gg \beta. \tag{31}$$

where S represent the entropy. Now, we have, for to obtain  $\beta$ :

$$54 \cdot 10^8 / 3 \cdot \ln(x/\pi) = (2\pi \cdot 54 \cdot 10^8 \cdot 16777216) \cdot 1/(3x)$$

Where  $t = 16777216 = 64^4$  and  $c = 54 \cdot 10^8$

**Input interpretation:**

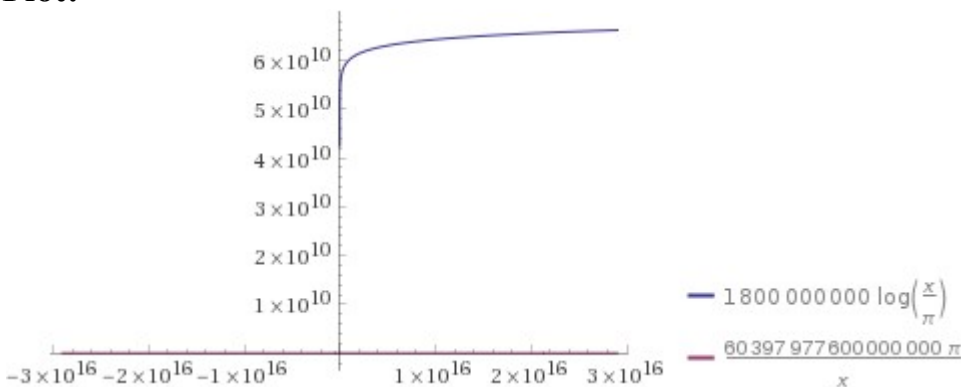
$$\frac{54 \times 10^8}{3} \log\left(\frac{x}{\pi}\right) = (2\pi \times 54 \times 10^8 \times 16\,777\,216) \times \frac{1}{3x}$$

$\log(x)$  is the natural logarithm

**Result:**

$$1\,800\,000\,000 \log\left(\frac{x}{\pi}\right) = \frac{60\,397\,977\,600\,000\,000 \pi}{x}$$

**Plot:**



**Alternate form assuming x is real:**

$$\frac{33554432 \pi}{x} + \log(\pi) = \log(x)$$

**Alternate form:**

$$180000000 (\log(x) - \log(\pi)) = \frac{60397977600000000 \pi}{x}$$

**Alternate form assuming x>0:**

$$180000000 \log(x) - 180000000 \log(\pi) = \frac{60397977600000000 \pi}{x}$$

**Alternate form assuming x is positive:**

$$x \log(\pi) + 33554432 \pi = x \log(x)$$

**Solution:**

$$x \approx 7.19817 \times 10^6$$

$$t = 16777216 = 64^4 ; \beta = 7198170$$

we have:

$$b > \beta.$$

$$a \approx b + \frac{\beta}{2\pi} \log\left(\frac{24\pi\phi_r}{c\beta}\right), \quad \text{for } \frac{\phi_r}{c\beta} \gg 1. \tag{21}$$

For the following data:

$$b = 7600000; \quad \frac{\phi_r}{c\beta} \gg 1 = 16 ; \beta = 7198170 \quad \phi_r = 16 * 54 * 10^8 * 7198170 = 621.921.888.000.000.000$$

$$\phi_r = 6.219218880000000000 * 10^{17}$$

$$c = 54q; \quad q \ll 10^{15} ; \quad c = 54 * 10^8$$

$$7600000 + (7198170 / (2\pi)) \ln \left( \frac{24\pi * 621921888000000000}{54 * 621921888000000000} \right)$$

**Input:**

$$7600000 + \frac{7198170}{2\pi} \log\left(\frac{24\pi \times 621921888000000000}{54 \times 621921888000000000}\right)$$

log(x) is the natural logarithm

**Exact result:**

$$7600000 + \frac{3599085 \log\left(\frac{4\pi}{9}\right)}{\pi}$$

**Decimal approximation:**

$$7.98240902511933667900382839353515906024022057534989166... \times 10^6$$

$$7.9824090251193 \times 10^6$$

**Alternate forms:**

$$7600000 + \frac{3599085 \left( \log(\pi) - \log\left(\frac{9}{4}\right) \right)}{\pi}$$

$$\frac{5 \left( 1520000 \pi + 719817 \log\left(\frac{4\pi}{9}\right) \right)}{\pi}$$

$$7600000 + \frac{7198170 \log(2) - 7198170 \log(3)}{\pi} + \frac{3599085 \log(\pi)}{\pi}$$

**Alternative representations:**

$$7600000 + \frac{\log\left(\frac{24\pi 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 + \frac{7198170 \log_e\left(\frac{14926125312000000000\pi}{33583781952000000000}\right)}{2\pi}$$

$$7600000 + \frac{\log\left(\frac{24\pi 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 + \frac{7198170 \log(a) \log_a\left(\frac{14926125312000000000\pi}{33583781952000000000}\right)}{2\pi}$$

$$7600000 + \frac{\log\left(\frac{24\pi 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 - \frac{7198170 \operatorname{Li}_1\left(1 - \frac{14926125312000000000\pi}{33583781952000000000}\right)}{2\pi}$$

**Series representations:**

$$7600000 + \frac{\log\left(\frac{24\pi 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 - \frac{3599085 \sum_{k=1}^{\infty} \frac{\left(1 - \frac{4\pi}{9}\right)^k}{k}}{\pi}$$

$$7600000 + \frac{\log\left(\frac{24\pi \cdot 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 + 7198170 i \left[ \frac{\arg\left(\frac{4\pi}{9} - x\right)}{2\pi} \right] +$$

$$\frac{3599085 \log(x)}{\pi} - \frac{3599085 \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{4\pi}{9} - x\right)^k x^{-k}}{k}}{\pi} \quad \text{for } x < 0$$

$$7600000 + \frac{\log\left(\frac{24\pi \cdot 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 + 7198170 i \left[ \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] +$$

$$\frac{3599085 \log(z_0)}{\pi} - \frac{3599085 \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{4\pi}{9} - z_0\right)^k z_0^{-k}}{k}}{\pi}$$

### Integral representations:

$$7600000 + \frac{\log\left(\frac{24\pi \cdot 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} = 7600000 + \frac{3599085}{\pi} \int_1^{\frac{4\pi}{9}} \frac{1}{t} dt$$

$$7600000 + \frac{\log\left(\frac{24\pi \cdot 621921888000000000}{54 \cdot 621921888000000000}\right) 7198170}{2\pi} =$$

$$7600000 - \frac{3599085 i}{2\pi^2} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(-1 + \frac{4\pi}{9}\right)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \quad \text{for } -1 < \gamma < 0$$

$\Gamma(x)$  is the gamma function

Thence:  $a = 7.9824090251193 \cdot 10^6$

We have that:

The computation of the bulk entanglement entropy is similar to that of a thermal state on the plane, except that we have to include the appropriate warp factor term from the metric (18). In fact, the bulk entropy computation is simplest in the  $(x^+, x^-)$  coordinates since the stress tensor vanishes and we have just the vacuum formulas. We then have to transform to  $(y^+, y^-)$  coordinates and keep track of the warp factors and transformation of the UV cutoffs.

We consider an interval on the right side of the form  $[0, b]_{\mathcal{R}}$  that includes part of the right bath and the quantum mechanical degrees of freedom at  $0_{\mathcal{R}}$ . We look for an entanglement wedge that consists of the interval  $[-a, b]$ , see figure 4. Its generalized entropy is

$$S_{\text{gen}}(a) = \frac{2\pi\phi_r}{\beta} \frac{1}{\tanh \frac{2\pi}{\beta} a} + \frac{c}{6} \log \frac{\sinh^2 \frac{\pi(a+b)}{\beta}}{\sinh \frac{2\pi a}{\beta}} + \text{constant} . \quad (19)$$

From

$$S_{\text{gen}}(a) = \frac{2\pi\phi_r}{\beta} \frac{1}{\tanh \frac{2\pi}{\beta} a} + \frac{c}{6} \log \frac{\sinh^2 \frac{\pi(a+b)}{\beta}}{\sinh \frac{2\pi a}{\beta}} + \text{constant} . \quad (19)$$

we obtain:

$$(2\pi \cdot 6.21921888 \times 10^{17}) / 7198170 \cdot 1 / (\tanh(2\pi \cdot 7.9824090251193 \times 10^6) / 7198170)$$

$$(2\pi \cdot 6.21921888 \times 10^{17}) / 7198170$$

**Input interpretation:**

$$\frac{2\pi \times 6.21921888 \times 10^{17}}{7198170}$$

**Result:**

$$5.42867211 \dots \times 10^{11}$$

$$5.42867211 \times 10^{11} \cdot 1 / \tanh(((2\pi \cdot 7982409.025) / 7198170))$$

**Input interpretation:**

$$5.42867211 \times 10^{11} \times \frac{1}{\tanh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)}$$

$\tanh(x)$  is the hyperbolic tangent function

**Result:**

$$5.42868174 \dots \times 10^{11}$$

$$5.42868174 \dots \times 10^{11}$$

$$(54 \times 10^8)/6$$

$$\ln(\frac{\sinh^2(\frac{\pi(7600000+7982409.025)}{7198170})}{\sinh(\frac{2\pi \cdot 7600000}{7198170})})$$

**Input interpretation:**

$$\frac{54 \times 10^8}{6} \log \left( \frac{\sinh^2\left(\pi \times \frac{7600000+7.982409025 \times 10^6}{7198170}\right)}{\sinh\left(\frac{2\pi \times 7600000}{7198170}\right)} \right)$$

sinh(x) is the hyperbolic sine function  
log(x) is the natural logarithm

**Result:**

$$5.647130122... \times 10^9$$

Thence, in conclusion, we obtain from

$$S_{gen}(a) = \frac{2\pi\phi_r}{\beta} \frac{1}{\tanh\frac{2\pi}{\beta}a} + \frac{c}{6} \log \frac{\sinh^2 \frac{\pi(a+b)}{\beta}}{\sinh \frac{2\pi a}{\beta}} + \text{constant} . \tag{19}$$

$$5.42867211 \times 10^{11} * 1/\tanh(\frac{2\pi \cdot 7982409.025}{7198170}) + (54 \times 10^8)/6 \ln(\frac{\sinh^2(\frac{\pi(7600000+7982409.025)}{7198170})}{\sinh(\frac{2\pi \cdot 7600000}{7198170})})$$

**Input interpretation:**

$$5.42867211 \times 10^{11} \times \frac{1}{\tanh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} + \frac{54 \times 10^8}{6} \log \left( \frac{\sinh^2\left(\pi \times \frac{7600000+7.982409025 \times 10^6}{7198170}\right)}{\sinh\left(\frac{2\pi \times 7600000}{7198170}\right)} \right)$$

tanh(x) is the hyperbolic tangent function  
sinh(x) is the hyperbolic sine function  
log(x) is the natural logarithm

**Result:**

$$5.48515304... \times 10^{11}$$

**5.48515304... \* 10<sup>11</sup> that is the generalized entropy**

Or, for a = 7290000 = 729 \* 10<sup>4</sup> where 729 is the Ramanujan cube 9<sup>3</sup>, we obtain:



$$5.42867211 \times 10^{11} * 1 / \tanh(((2\text{Pi}*7982409.025)/7198170)) + (54*10^8)/6$$

$$\ln((((((\sinh^2(((\text{Pi}(7290000+7982409.025))/(7198170)))))/((\sinh(((2\text{Pi}*7290000)/(7198170))))))))))$$

**Input interpretation:**

$$5.42867211 \times 10^{11} \times \frac{1}{\tanh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} + \frac{54 \times 10^8}{6} \log\left(\frac{\sinh^2\left(\pi \times \frac{7290000 + 7.982409025 \times 10^6}{7198170}\right)}{\sinh\left(\frac{2\pi \times 7290000}{7198170}\right)}\right)$$

tanh(x) is the hyperbolic tangent function

sinh(x) is the hyperbolic sine function

log(x) is the natural logarithm

**Result:**

$$5.4851530454309748065063333097680173447294664989138989... \times 10^{11}$$

5.48515304... \* 10<sup>11</sup> exactly the same above result!

Inserting this value of entropy 5.485153e+11 in the Hawking radiation calculator, we obtain:

$$\text{Mass} = 0.006900779$$

$$\text{Radius} = 1.024663\text{e-}29$$

$$\text{Temperature} = 1.778355\text{e+}25$$

From the Ramanujan-Nardelli mock formula, we obtain:

$$\sqrt{\left[ \left[ \left[ \left[ \left[ \left[ \frac{1}{\left( \frac{4 \times 1.962364415 \text{e+}19}{5 \times 0.0864055^2} \times \frac{1}{0.006900779} \right)} \right] \right] \right] \right] \right] \times \sqrt{\left[ - \left( \left( \left( 1.778355 \text{e+}25 \times 4 \times \text{Pi} \times (1.024663 \text{e-}29)^3 - (1.024663 \text{e-}29)^2 \right) \right) \right) \right] / \left( (6.67 \times 10^{-11}) \right) \right] \right] \right] \right] \right]$$

**Input interpretation:**

$$\sqrt{\left( \left( \left( \left( \left( \frac{4 \times 1.962364415 \times 10^{19}}{5 \times 0.0864055^2} \times \frac{1}{0.006900779} \right) \right) \right) \right) \right) \times \sqrt{\left( - \frac{1.778355 \times 10^{25} \times 4 \pi (1.024663 \times 10^{-29})^3 - (1.024663 \times 10^{-29})^2}{6.67 \times 10^{-11}} \right) \right) \right) \right) \right)$$

**Result:**

1.618249415571316958887687260737558532653671011636047668745...

1.6182494155...

And:

$$1/\sqrt{[1/((((((4*1.962364415e+19)/(5*0.0864055^2)))*1/(0.006900779) * \sqrt{[-((1.778355e+25 * 4*Pi*(1.024663e-29)^3-(1.024663e-29)^2))]) / ((6.67*10^-11)))]])]$$

**Input interpretation:**

$$\sqrt{\frac{1}{\frac{4 \times 1.962364415 \times 10^{19}}{5 \times 0.0864055^2} \times \frac{1}{0.006900779} \sqrt{\frac{1.778355 \times 10^{25} \times 4 \pi (1.024663 \times 10^{-29})^3 - (1.024663 \times 10^{-29})^2}{6.67 \times 10^{-11}}}}}$$

**Result:**

0.617951713980353087925763741301304436822867176137611862466...

0.617951713...

Furthermore, we obtain also:

$$1/((((((5.42867211 \times 10^{11} * 1/ \tanh(((2\pi*7982409.025)/7198170)))+(54*10^8)/6 \ln((((sinh^2(((\pi(7600000+7982409.025)/(7198170)))))/((sinh(((2\pi*7600000)/(7198170))))))))))))))^{1/4096}$$

**Input interpretation:**

$$1 / \left( \left( 5.42867211 \times 10^{11} \times \frac{1}{\tanh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} + \frac{54 \times 10^8}{6} \log\left(\frac{\sinh^2\left(\pi \times \frac{7600000 + 7.982409025 \times 10^6}{7198170}\right)}{\sinh\left(\frac{2\pi \times 7600000}{7198170}\right)}\right) \right) \right)^{(1/4096)}$$

tanh(x) is the hyperbolic tangent function  
sinh(x) is the hyperbolic sine function  
log(x) is the natural logarithm

**Result:**

0.993422488624...

0.993422488624.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}}}{1 + \sqrt[5]{\sqrt{\varphi^5 \sqrt[4]{5^3}} - 1}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

$$1/[1/((((((5.42867211 \times 10^{11} * 1/\tanh(((2\text{Pi}*7982409.025)/7198170)))+(54*10^8)/6 \ln((((\sinh^2((\text{Pi}(7600000+7982409.025)/(7198170)))))/((\sinh((2\text{Pi}*7600000)/(7198170)))))))))))))^1/4096]^744$$

**Input interpretation:**

$$1/\left(1/\left(5.42867211 \times 10^{11} \times \frac{1}{\tanh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} + \frac{54 \times 10^8}{6} \log\left(\frac{\sinh^2\left(\pi \times \frac{7600000 + 7.982409025 \times 10^6}{7198170}\right)}{\sinh\left(\frac{2\pi \times 7600000}{7198170}\right)}\right)\right)\right)^{744}$$

$\tanh(x)$  is the hyperbolic tangent function

$\sinh(x)$  is the hyperbolic sine function

$\log(x)$  is the natural logarithm

**Result:**

135.616828...

135.616828.... result very near to the rest mass of Pion meson 134.9766

Now, we have that:

$$b = 7600000; \quad \frac{\phi_r}{c\beta} \gg 1 = 16; \quad \beta = 7198170 \quad \phi_r = 16 * 54 * 10^8 * 7198170 = 621.921888.000.000.000; \quad \phi_r = 6.219218880000000000 * 10^{17}; \quad c = 54q; \\ q \ll 10^{15}; \quad c = 54 * 10^8 \quad a = 7.9824090251193 * 10^6$$

From

$$S_{\text{gen}}(a) = \phi_0 + \frac{\phi_r}{a} + S_{\text{bulk}}, \quad S_{\text{bulk}} = \frac{c}{6} \log \left[ \frac{(a+b)^2}{a} \right] + \text{constant}. \quad (5)$$

we obtain:

$$(54e+8/6) \ln \left( \frac{(7.982409025e+6 + 7600000)^2}{7.982409025e+6} \right)$$

**Input interpretation:**

$$\frac{54 \times 10^8}{6} \log \left( \frac{(7.982409025 \times 10^6 + 7600000)^2}{7.982409025 \times 10^6} \right)$$

log(x) is the natural logarithm

**Result:**

$$1.5507500051... \times 10^{10}$$

$$1.5507500051... * 10^{10}$$

From the ratio between the previous result, we obtain:

$$(5.48515304e+11 / 1.5507500051 \times 10^{10}) * 1 / (\text{golden ratio})^2 - 0.9568666373$$

Where 0.9568666373 is the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{5}}}{\sqrt{(\phi-1)\sqrt{5}} - \phi + 1} = 1 - \frac{e^{-\pi}}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-3\pi}}{1 + \frac{e^{-4\pi}}{1 + \dots}}}} \approx 0.9568666373$$

**Input interpretation:**

$$\frac{5.48515304 \times 10^{11}}{1.5507500051 \times 10^{10}} \times \frac{1}{\phi^2} - 0.9568666373$$

φ is the golden ratio

**Result:**

$$12.5536413...$$

12.5536413... result very near to the  $S_{\text{BH}}$  entropy 12.5664

Or:

$$(5.48515304e+11 / 1.5507500051 \times 10^{10}) * 1 / (\text{golden ratio})^2 - 0.9991104684$$

Where 0.9991104684 is the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

**Input interpretation:**

$$\frac{5.48515304 \times 10^{11}}{1.5507500051 \times 10^{10}} \times \frac{1}{\phi^2} - 0.9991104684$$

$\phi$  is the golden ratio

**Result:**

12.5113975...

12.5113975... result very near to the S entropy 12.5372

Now, from (5), we can to obtain  $\phi_0$

$$S_{\text{gen}}(a) = \phi_0 + \frac{\phi_r}{a} + S_{\text{bulk}}, \quad S_{\text{bulk}} = \frac{c}{6} \log \left[ \frac{(a+b)^2}{a} \right] + \text{constant}. \quad (5)$$

$$5.48515304e+11 = x + (6.21921888e+17/7.982409025e+6)+(54e+8/6) \ln \left( \frac{(7.982409025e+6 + 7600000)^2}{7.982409025e+6} \right)$$

**Input interpretation:**

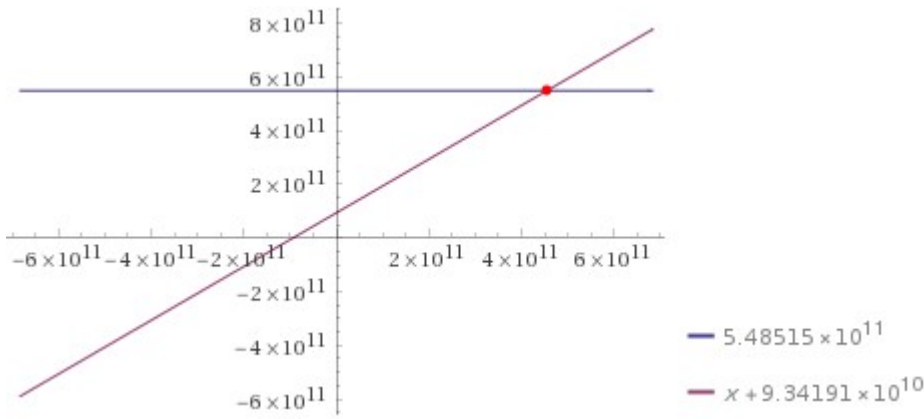
$$5.48515304 \times 10^{11} = x + \frac{6.21921888 \times 10^{17}}{7.982409025 \times 10^6} + \frac{54 \times 10^8}{6} \log \left( \frac{(7.982409025 \times 10^6 + 7600000)^2}{7.982409025 \times 10^6} \right)$$

$\log(x)$  is the natural logarithm

**Result:**

$$5.48515 \times 10^{11} = x + 9.34191 \times 10^{10}$$

**Plot:**



**Alternate forms:**

$$5.48515 \times 10^{11} = x + 9.34191 \times 10^{10}$$

$$4.55096 \times 10^{11} - x = 0$$

**Solution:**

$$x \approx 4.55096 \times 10^{11}$$

$$4.55096 \times 10^{11} = \phi_0$$

Thence:

$$S_{\max} = 2S_{\text{BH}} = 2 \left( \phi_0 + \frac{2\pi\phi_r}{\beta} \right) \quad (32)$$

$$2(4.55096e+11 + (2\pi * 6.21921888e+17 / 7198170))$$

**Input interpretation:**

$$2 \left( 4.55096 \times 10^{11} + 2\pi \times \frac{6.21921888 \times 10^{17}}{7198170} \right)$$

**Result:**

$$1.99593... \times 10^{12}$$

1.99593... \* 10<sup>12</sup> that is the maximal entropy

From the two values obtained, performing the division, we have:

$$1.99593e+12 / 5.48515304e+11$$

$$(1.99593e+12) / (5.48515304e+11)$$

**Input interpretation:**

$$\frac{1.99593 \times 10^{12}}{5.48515304 \times 10^{11}}$$

**Result:**

3.638786348247450175063848355268497668024956328292346060047...

3.638786348

$$(1/(2*\text{golden ratio} - 1/5 * \text{golden ratio}))*((1.99593e+12) / (5.48515304e+11))^3$$

**Input interpretation:**

$$\frac{1}{2\phi - \frac{1}{5}\phi} \left( \frac{1.99593 \times 10^{12}}{5.48515304 \times 10^{11}} \right)^3$$

$\phi$  is the golden ratio

**Result:**

16.5428...

16.5428.... result very near to the mass of the hypothetical light particle, the boson  $m_x = 16.84 \text{ MeV}$

Now, we have:

With regard the mathematical constant 0.393625563.... we have that the real solution of  $x + \text{Ci}(x)$  is equal to 0.39362556340804009... The unique real-valued fixed point of  $-\text{Ci}(z)$  (cosine integral – math constant):

$$\sqrt{\frac{1}{798} (6675 - 1558 e - 469 \pi - 1216 \log(2))} \approx 0.3936255634080400909862$$

Adding the golden ratio to this value, and multiplying the result by golden ratio and by the previous expression, we obtain:

$$(0.39362556340804009 + \text{golden ratio}) * (\text{golden ratio}) * (((1.99593e+12) / (5.48515304e+11)))$$

**Input interpretation:**

$$(0.39362556340804009 + \phi) \phi \times \frac{1.99593 \times 10^{12}}{5.48515304 \times 10^{11}}$$

**Result:**

11.8440...

11.8440... result practically equal to the  $S_{BH}$  entropy 11.8477

From (20)

$$\frac{\sinh \frac{\pi(a-b)}{\beta}}{\sinh \frac{\pi(a+b)}{\beta}} = \frac{12\pi\phi_r}{c\beta} \frac{1}{\sinh \frac{2\pi a}{\beta}}$$

For:

$$\beta = 7198170 \quad \phi_r = 6.219218880000000000 * 10^{17}$$

$$c = 54q \quad q \ll 10^{15}; \quad c = 54 * 10^8 \quad a = 7.9824090251193 * 10^6$$

We obtain:

$$(12\pi * 6.21921888e+17) / (54e+8 * 7198170) * 1 / (((\sinh((2\pi * 7.982409025e+6)) / (7198170))))$$

**Input interpretation:**

$$\frac{12\pi * 6.21921888 * 10^{17}}{54 * 10^8 * 7198170} \times \frac{1}{\sinh\left(\frac{2\pi * 7.982409025 * 10^6}{7198170}\right)}$$

$\sinh(x)$  is the hyperbolic sine function

**Result:**

1.13613980...

1.13613980...

$$1 / (((((12\pi * 6.21921888e+17) / (54e+8 * 7198170) * 1 / (((\sinh((2\pi * 7.982409025e+6)) / (7198170))))))))))^{1/16}$$

**Input interpretation:**



$$\sqrt[5]{\frac{1}{\frac{12\pi \times 6.21921888 \times 10^{17}}{54 \times 10^8 \times 7198170} \times \frac{1}{\sinh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)}}}$$

sinh(x) is the hyperbolic sine function

**Result:**

0.9920544607...

0.9920544607.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = φ**

$$\left( \left( \left( \left( \left( \frac{12\pi \times 6.21921888 \times 10^{17}}{54 \times 10^8 \times 7198170} \right) \times \frac{1}{\sinh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} \right) \right) \right) \right) \right)^{5\pi/4}$$

**Input interpretation:**

$$\left( \frac{12\pi \times 6.21921888 \times 10^{17}}{54 \times 10^8 \times 7198170} \times \frac{1}{\sinh\left(\frac{2\pi \times 7.982409025 \times 10^6}{7198170}\right)} \right)^{5\pi/4}$$

sinh(x) is the hyperbolic sine function

**Result:**

1.6507453...

1.6507453.... is very near to the 14th root of the following Ramanujan's class

invariant  $Q = (G_{505}/G_{101/5})^3 = 1164,2696$  i.e. 1,65578...

From:

### Scaling solutions for Dilaton Quantum Gravity

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We have that, from the set of flow equations concerning the large field limit of dilaton gravity, the following expressions:

$$A_V = \frac{1}{192\pi^2} (9\epsilon^3 + 82\epsilon^2 + 612\epsilon + 2760) \quad (5)$$

The simultaneous zero at  $\epsilon = \epsilon_0 = 109.97$ , as well as the pole at  $\epsilon = -6$  are clearly visible.

$$1/(192\pi^2) * (9*(-6)^3 + 82*(-6)^2 + 612*(-6) + 2760)$$

**Input:**

$$\frac{1}{192\pi^2} (9 \times (-1) \times 6^3 + 82 \times (-1) \times 6^2 + 612 \times (-6) + 2760)$$

**Result:**

$$-\frac{121}{4\pi^2}$$

**Decimal approximation:**

-3.06496580518071758617735376209426107685685293383545810257...

-3.06496580518...

**Property:**

$-\frac{121}{4\pi^2}$  is a transcendental number

**Alternative representations:**

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = \frac{-912 - 82 \times 6^2 - 9 \times 6^3}{192(180^\circ)^2}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = \frac{-912 - 82 \times 6^2 - 9 \times 6^3}{1152 \zeta(2)}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = \frac{-912 - 82 \times 6^2 - 9 \times 6^3}{192(-i \log(-1))^2}$$

### Series representations:

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{64 \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^2}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{64 \left( \sum_{k=0}^{\infty} \frac{(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right)^2}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{4 \left( \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left( \frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right) \right)^2}$$

### Integral representations:

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{64 \left( \int_0^1 \sqrt{1-t^2} dt \right)^2}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{16 \left( \int_0^{\infty} \frac{1}{1+t^2} dt \right)^2}$$

$$\frac{9(-1)6^3 + 82(-1)6^2 + 612(-6) + 2760}{192\pi^2} = -\frac{121}{16 \left( \int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^2}$$

$$1/(192 \cdot \pi^2) * (9 \cdot 109.97^3 + 82 \cdot 109.97^2 + 612 \cdot 109.97 + 2760)$$

**Input interpretation:**

$$\frac{1}{192 \pi^2} (9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)$$

**Result:**

6876.61...

6876.61...

**Alternative representations:**

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{70\,061.6 + 82 \times 109.97^2 + 9 \times 109.97^3}{192 (180^\circ)^2}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{70\,061.6 + 82 \times 109.97^2 + 9 \times 109.97^3}{1152 \zeta(2)}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{70\,061.6 + 82 \times 109.97^2 + 9 \times 109.97^3}{192 (-i \log(-1))^2}$$

**Series representations:**

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{4241.84}{\left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^2}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{16\,967.3}{\left( -1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}} \right)^2}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{67\,869.4}{\left( \sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}} \right)^2}$$

**Integral representations:**

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{16\,967.3}{\left(\int_0^\infty \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{4241.84}{\left(\int_0^1 \sqrt{1-t^2} dt\right)^2}$$

$$\frac{9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760}{192 \pi^2} = \frac{16\,967.3}{\left(\int_0^\infty \frac{\sin(t)}{t} dt\right)^2}$$

$$-(6876.606561943517990117 / -3.064965805180717586177) - 64 \times 8 - 2$$

**Input interpretation:**

$$-\left(-\frac{6876.606561943517990117}{3.064965805180717586177}\right) - 64 \times 8 - 2$$

**Result:**

1729.616078952651515151494932879996712804070048427295178814...

1729.616078...

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the  $j$ -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$A_F = \frac{1}{3456\pi^2} (-253\epsilon^3 - 6094\epsilon^2 - 36240\epsilon - 51840) \tag{5}$$

$$1/(3456*\text{Pi}^2)* (-253*-6^3-6094*-6^2-36240*-6-51840)$$

**Input:**

$$\frac{1}{3456 \pi^2} (-253 \times (-1) \times 6^3 - 6094 \times (-1) \times 6^2 - 36\,240 \times (-6) - 51\,840)$$

**Result:**

$$\frac{3053}{24\pi^2}$$

**Decimal approximation:**

12.88889890250238400909016671580410339895863912809869640106...

12.8888989025...

**Property:**

$\frac{3053}{24\pi^2}$  is a transcendental number

**Alternative representations:**

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{3456\pi^2} = \frac{165600 + 6094 \times 6^2 + 253 \times 6^3}{3456(180^\circ)^2}$$

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{3456\pi^2} = \frac{165600 + 6094 \times 6^2 + 253 \times 6^3}{20736\zeta(2)}$$

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{3456\pi^2} = \frac{165600 + 6094 \times 6^2 + 253 \times 6^3}{3456(-i \log(-1))^2}$$

**Series representations:**

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{3456\pi^2} = \frac{3053}{384 \left( \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^2}$$

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{\frac{3456\pi^2}{3053}} = 384 \left( \sum_{k=0}^{\infty} \frac{(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k} \right)^2$$

$$\frac{-253(-1)6^3 - 6094(-1)6^2 - 36240(-6) - 51840}{\frac{3456\pi^2}{3053}} = 24 \left( \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left( \frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right) \right)^2$$

**Integral representations:**

$$\frac{-253(-1)^6 - 6094(-1)^6 - 36240(-6) - 51840}{3456\pi^2} = \frac{3053}{384 \left( \int_0^1 \sqrt{1-t^2} dt \right)^2}$$

$$\frac{-253(-1)^6 - 6094(-1)^6 - 36240(-6) - 51840}{3456\pi^2} = \frac{3053}{96 \left( \int_0^\infty \frac{1}{1+t^2} dt \right)^2}$$

$$\frac{-253(-1)^6 - 6094(-1)^6 - 36240(-6) - 51840}{3456\pi^2} = \frac{3053}{96 \left( \int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^2}$$

$$1/(3456*\text{Pi}^2)*(-253*109.97^3-6094*109.97^2-36240*109.97-51840)$$

**Input interpretation:**

$$\frac{1}{3456\pi^2} (-253 \times 109.97^3 - 6094 \times 109.97^2 + 36240 \times (-109.97) - 51840)$$

**Result:**

-12143.4...

-12143.4...

**Alternative representations:**

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{3456\pi^2} = \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{3456(180^\circ)^2}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{3456\pi^2} = \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{20736 \zeta(2)}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{3456\pi^2} = \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{3456(-i \log(-1))^2}$$

**Series representations:**

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{7490.63}{\left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^2}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{29\,962.5}{\left(-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}\right)^2}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{119\,850.}{\left(\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}\right)^2}$$

**Integral representations:**

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{29\,962.5}{\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{7490.63}{\left(\int_0^1 \sqrt{1-t^2} dt\right)^2}$$

$$\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{3456 \pi^2} = -\frac{29\,962.5}{\left(\int_0^{\infty} \frac{\sin(t)}{t} dt\right)^2}$$

From the ln of the ratio between the two previous results, we obtain:

$$\ln\left(\frac{-\left(\frac{1}{3456\pi^2}(-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840)\right)}{\left(\frac{1}{192\pi^2}(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)\right)}\right)$$

**Input interpretation:**

$$\log\left(-\frac{\frac{1}{3456\pi^2}(-253 \times 109.97^3 - 6094 \times 109.97^2 + 36\,240 \times (-109.97) - 51\,840)}{\frac{1}{192\pi^2}(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right)$$

log(x) is the natural logarithm

**Result:**



0.568657...

0.568657... result practically equal to the value of the following Ramanujan continued fraction:

$$4 \int_0^{\infty} \frac{t dt}{e^{\sqrt{5}t} \cosh t} = \frac{1}{1 + \frac{1^2}{1 + \frac{1^2}{1 + \frac{2^2}{1 + \frac{2^2}{1 + \frac{3^2}{1 + \frac{3^2}{1 + \dots}}}}}}}} \approx 0.5683000031$$

**Alternative representations:**

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)}{192\pi^2}} \right) =$$

$$\log_e \left( \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{\frac{(3456\pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}{192\pi^2}} \right)$$

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)}{192\pi^2}} \right) =$$

$$\log(a) \log_a \left( \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{\frac{(3456\pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}{192\pi^2}} \right)$$

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)}{192\pi^2}} \right) =$$

$$-\text{Li}_1 \left( 1 + \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{\frac{(3456\pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}{192\pi^2}} \right)$$

**Series representations:**

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)} \right) =$$

$$- \sum_{k=1}^{\infty} \frac{(-0.765893)^k}{k}$$

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)} \right) =$$

$$2i\pi \left[ \frac{\arg(1.76589 - x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)} \right) =$$

$$\left[ \frac{\arg(1.76589 - z_0)}{2\pi} \right] \log \left( \frac{1}{z_0} \right) + \log(z_0) +$$

$$\left[ \frac{\arg(1.76589 - z_0)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - z_0)^k z_0^{-k}}{k}$$

### Integral representations:

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)} \right) = \int_1^{1.76589} \frac{1}{t} dt$$

$$\log \left( \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)(3456\pi^2)} \right) =$$

$$\frac{1}{2i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{0.266713s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \quad \text{for } -1 < \gamma < 0$$

$$((288 \cdot 0.988) \cdot 1/10^2) \cdot \ln \left( \frac{-\left( \frac{1}{(3456 \cdot \pi^2)} \cdot (-253 \cdot 109.97^3 - 6094 \cdot 109.97^2 - 36240 \cdot 109.97 - 51840) \right)}{\left( \frac{1}{(192 \cdot \pi^2)} \cdot (9 \cdot 109.97^3 + 82 \cdot 109.97^2 + 612 \cdot 109.97 + 2760) \right)} \right)$$

Where 288 is equal to 233 + 55, that are Fibonacci numbers and 0.988 is very near to the dilaton value

**Input interpretation:**

$$\left( (288 \times 0.988) \times \frac{1}{10^2} \right) \log \left( - \frac{\frac{1}{3456 \pi^2} (-253 \times 109.97^3 - 6094 \times 109.97^2 + 36240 \times (-109.97) - 51840)}{\frac{1}{192 \pi^2} (9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right)$$

log(x) is the natural logarithm

**Result:**

1.618078252589530428708340526797989223967430064790655358180...

1.6180782525...

This result is a very good approximation to the value of the golden ratio 1,618033988749...

**Alternative representations:**

$$\frac{\log \left( - \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right) (288 \times 0.988)}{10^2} =$$

$$\frac{284.544 \log_e \left( - \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{(3456 \pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)} \right)}{10^2}$$

$$\frac{\log \left( - \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right) (288 \times 0.988)}{10^2} =$$

$$\frac{284.544 \log(a) \log_\alpha \left( - \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{(3456 \pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)} \right)}{10^2}$$

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} =$$

$$\frac{10^2}{284.544 \operatorname{Li}_1\left(1 + \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{(3456 \pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}\right)}$$

### Series representations:

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} =$$

$$-2.84544 \sum_{k=1}^{\infty} \frac{(-0.765893)^k}{k}$$

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} =$$

$$5.69088 i \pi \left[ \frac{\arg(1.76589 - x)}{2 \pi} \right] + 2.84544 \log(x) -$$

$$2.84544 \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - x)^k x^{-k}}{k} \text{ for } x < 0$$

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} =$$

$$2.84544 \left[ \frac{\arg(1.76589 - z_0)}{2 \pi} \right] \log\left(\frac{1}{z_0}\right) + 2.84544 \log(z_0) +$$

$$2.84544 \left[ \frac{\arg(1.76589 - z_0)}{2 \pi} \right] \log(z_0) - 2.84544 \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - z_0)^k z_0^{-k}}{k}$$

### Integral representations:

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} =$$

$$2.84544 \int_1^{1.76589} \frac{1}{t} dt$$

$$\frac{\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) (288 \times 0.988)}{192 \pi^2} = \frac{1.42272}{i \pi} \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{e^{0.266713 s} 10^2 \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$((\pi \times 0.937) * \ln((( -(((1/(3456 * \pi^2) * (-253 * 109.97^3 - 6094 * 109.97^2 - 36240 * 109.97 - 51840)))))) / (((1/(192 * \pi^2) * (9 * 109.97^3 + 82 * 109.97^2 + 612 * 109.97 + 2760))))))))))$$

where 0.937 result very near to the spectral index  $n_s$ , to the mesonic Regge slope and to the inflaton value at the end of the inflation 0.9402

### Input interpretation:

$$(\pi \times 0.937) \log\left(-\frac{\frac{1}{3456 \pi^2} (-253 \times 109.97^3 - 6094 \times 109.97^2 + 36240 \times (-109.97) - 51840)}{\frac{1}{192 \pi^2} (9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right)$$

$\log(x)$  is the natural logarithm

### Result:

1.67394...

1.67394... result very near to the neutron mass

### Alternative representations:

$$\log\left(-\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36240 \times 109.97 - 51840}{(3456 \pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}\right) \pi 0.937 = 0.937 \pi \log_e\left(-\frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{(3456 \pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}\right)$$

$$\log \left( -\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}{192\pi^2}} \right) \pi 0.937 =$$

$$0.937 \pi \log(a) \log_a \left( -\frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{\frac{(3456\pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}{192\pi^2}} \right)$$

$$\log \left( -\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}{192\pi^2}} \right) \pi 0.937 =$$

$$-0.937 \pi \operatorname{Li}_1 \left( 1 + \frac{-4.03715 \times 10^6 - 6094 \times 109.97^2 - 253 \times 109.97^3}{\frac{(3456\pi^2)(70061.6 + 82 \times 109.97^2 + 9 \times 109.97^3)}{192\pi^2}} \right)$$

### Series representations:

$$\log \left( -\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}{192\pi^2}} \right) \pi 0.937 =$$

$$-0.937 \pi \sum_{k=1}^{\infty} \frac{(-0.765893)^k}{k}$$

$$\log \left( -\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}{192\pi^2}} \right) \pi 0.937 =$$

$$1.874 i \pi^2 \left[ \frac{\arg(1.76589 - x)}{2\pi} \right] + 0.937 \pi \log(x) -$$

$$0.937 \pi \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\log \left( -\frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{\frac{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)}{192\pi^2}} \right) \pi 0.937 =$$

$$1.874 i \pi^2 \left[ -\frac{-\pi + \arg\left(\frac{1.76589}{z_0}\right) + \arg(z_0)}{2\pi} \right] +$$

$$0.937 \pi \log(z_0) - 0.937 \pi \sum_{k=1}^{\infty} \frac{(-1)^k (1.76589 - z_0)^k z_0^{-k}}{k}$$

### Integral representations:

$$\log \left[ \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right] \pi^{0.937} =$$

$$0.937 \pi \int_1^{1.76589} \frac{1}{t} dt$$

$$\log \left[ \frac{-253 \times 109.97^3 - 6094 \times 109.97^2 - 36\,240 \times 109.97 - 51\,840}{(3456\pi^2)(9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right] \pi^{0.937} =$$

$$\frac{0.4685}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{0.266713s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$\Gamma(x)$  is the gamma function

$$((\pi \cdot x) \cdot \ln \left( \frac{-\left( \frac{1}{3456\pi^2} (-253 \cdot 109.97^3 - 6094 \cdot 109.97^2 - 36240 \cdot 109.97 - 51840) \right)}{\left( \frac{1}{192\pi^2} (9 \cdot 109.97^3 + 82 \cdot 109.97^2 + 612 \cdot 109.97 + 2760) \right)} \right)) = 1.674927$$

Where 1.674927 is the neutron mass

### Input interpretation:

$$(\pi x) \log \left( \frac{\frac{1}{3456\pi^2} (-253 \times 109.97^3 - 6094 \times 109.97^2 + 36\,240 \times (-109.97) - 51\,840)}{\frac{1}{192\pi^2} (9 \times 109.97^3 + 82 \times 109.97^2 + 612 \times 109.97 + 2760)} \right) =$$

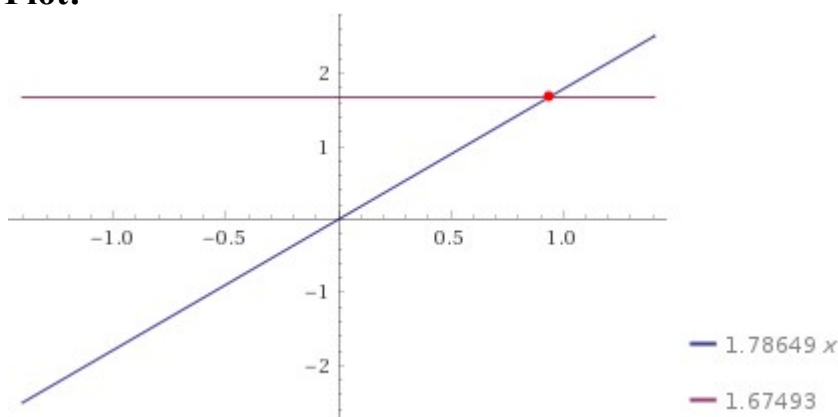
$$1.674927$$

$\log(x)$  is the natural logarithm

### Result:

$$1.78649 x = 1.67493$$

### Plot:



### Alternate form:

$$1.78649x - 1.67493 = 0$$

**Alternate form assuming x is real:**

$$1.78649x + 0 = 1.67493$$

**Solution:**

$$x \approx 0.937553$$

$x = 0.937553$  result very near to the spectral index  $n_s$ , to the mesonic Regge slope and to the inflaton value at the end of the inflation 0.9402

Now, we have

$$C_K = \frac{1}{36\pi^2} (-\epsilon^4 + 90\epsilon^3 + 2079\epsilon^2 + 12636\epsilon + 26244) \quad (5)$$

$$1/(36\pi^2) * (-(-6)^4 + 90 * (-6)^3 + 2079 * (-6)^2 + 12636 * (-6) + 26244)$$

**Input:**

$$\frac{1}{36\pi^2} (-(-6)^4 + 90 \times (-1) \times 6^3 + 2079 \times (-1) \times 6^2 + 12636 \times (-6) + 26244)$$

**Result:**

$$-\frac{4032}{\pi^2}$$

**Decimal approximation:**

$$-408.527012445905894461721995661621840062374579478498084945\dots$$

$$-408.52701244$$

**Property:**

$$-\frac{4032}{\pi^2} \text{ is a transcendental number}$$

**Alternative representations:**

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{36(180^\circ)^2} = \frac{-49572 - (-6)^4 - 2079 \times 6^2 - 90 \times 6^3}{36(180^\circ)^2}$$



$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{-49572 - (-6)^4 - 2079 \times 6^2 - 90 \times 6^3} = \frac{36\pi^2}{216\zeta(2)}$$

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{-49572 - (-6)^4 - 2079 \times 6^2 - 90 \times 6^3} = \frac{36\pi^2}{36(-i \log(-1))^2}$$

### Series representations:

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{36\pi^2} = -\frac{252}{\left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^2}$$

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{252} = -\frac{36\pi^2}{\left(\sum_{k=0}^{\infty} \frac{(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}\right)^2}$$

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{4032} = -\frac{36\pi^2}{\left(\sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)\right)^2}$$

### Integral representations:

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{36\pi^2} = -\frac{252}{\left(\int_0^1 \sqrt{1-t^2} dt\right)^2}$$

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{36\pi^2} = -\frac{1008}{\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{-(-6)^4 + 90(-1)6^3 + 2079(-1)6^2 + 12636(-6) + 26244}{36\pi^2} = -\frac{1008}{\left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt\right)^2}$$

$$1/(36\pi^2)*(-109.97^4+90*109.97^3+2079*109.97^2+12636*109.97+26244)$$

**Input interpretation:**

$$\frac{1}{36\pi^2} (-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244)$$

**Result:**

-0.909666...

-0.909666...

**Alternative representations:**

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36\pi^2} = \frac{1.41582 \times 10^6 + 2079 \times 109.97^2 + 90 \times 109.97^3 - 109.97^4}{36(180^\circ)^2}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36\pi^2} = \frac{1.41582 \times 10^6 + 2079 \times 109.97^2 + 90 \times 109.97^3 - 109.97^4}{216\zeta(2)}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36\pi^2} = \frac{1.41582 \times 10^6 + 2079 \times 109.97^2 + 90 \times 109.97^3 - 109.97^4}{36(-i \log(-1))^2}$$

**Series representations:**

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36\pi^2} = \frac{0.561128}{\left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^2}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36\pi^2} = \frac{2.24451}{\left(-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}\right)^2}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36 \pi^2} =$$

$$-\frac{8.97804}{\left(\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}\right)^2}$$

**Integral representations:**

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36 \pi^2} =$$

$$-\frac{2.24451}{\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36 \pi^2} =$$

$$-\frac{0.561128}{\left(\int_0^1 \sqrt{1-t^2} dt\right)^2}$$

$$\frac{-109.97^4 + 90 \times 109.97^3 + 2079 \times 109.97^2 + 12\,636 \times 109.97 + 26\,244}{36 \pi^2} =$$

$$-\frac{2.24451}{\left(\int_0^{\infty} \frac{\sin(t)}{t} dt\right)^2}$$

Now from the following results 6876.61 -12143.4 and -0.909666, we obtain:

$$\sqrt{144} - (6876.61 - 12143.4 - 0.909666)$$

where 144 is a Fibonacci number

**Input interpretation:**

$$\sqrt{144} - (6876.61 - 12143.4 - 0.909666)$$

**Result:**

5279.699666

5279.699666 result practically equal to the rest mass of B meson 5279.53

And:

$$(((\sqrt{144})-(6876.61 -12143.4 -0.909666)))) /48 +29 +(\sqrt{5}-1)/2$$

**Input interpretation:**

$$\frac{1}{48} \left( \sqrt{144} - (6876.61 - 12143.4 - 0.909666) \right) + 29 + \frac{1}{2} (\sqrt{5} - 1)$$

**Result:**

139.612...

139.612...

Or:

$$5279.699666 /48 +29 +(\sqrt{5}-1)/2$$

**Input interpretation:**

$$\frac{5279.699666}{48} + 29 + \frac{1}{2} (\sqrt{5} - 1)$$

**Result:**

139.6117770...

139.611777... result practically equal to the rest mass of Pion meson 139.57

From:

## INTEGRALS ASSOCIATED WITH RAMANUJAN AND ELLIPTIC FUNCTIONS

*BRUCE C. BERNDT*

From:

$$\begin{aligned} \int_{-\infty}^{\infty} \frac{dx}{\cos \sqrt{x} + \cosh \sqrt{x}} &= 2\pi^2 \cdot \frac{1}{2} \left( \frac{\sqrt{\pi}}{\Gamma^2(\frac{3}{4})} \right)^2 \sqrt{\frac{1}{2} \cdot \frac{1}{2}} \\ &= \frac{\pi^3}{2\Gamma^4(\frac{3}{4})} = \frac{\pi^3}{2\Gamma^2(\frac{3}{4})} \cdot \frac{\Gamma^2(\frac{1}{4})}{2\pi^2} = \frac{\pi \Gamma^2(\frac{1}{4})}{4 \Gamma^2(\frac{3}{4})}, \end{aligned} \tag{2.14}$$

We obtain:

$$\frac{\pi}{4} \frac{\Gamma^2(\frac{1}{4})}{\Gamma^2(\frac{3}{4})}$$

**Input:**

$$\frac{\pi}{4} \times \frac{\Gamma\left(\frac{1}{4}\right)^2}{\Gamma\left(\frac{3}{4}\right)^2}$$

$\Gamma(x)$  is the gamma function

**Exact result:**

$$\frac{\pi \Gamma\left(\frac{1}{4}\right)^2}{4 \Gamma\left(\frac{3}{4}\right)^2}$$

**Decimal approximation:**

6.875185818020372827490095779810557197900856451819160896274...

6.87518581802.....

**Alternate forms:**

$$\frac{\Gamma\left(\frac{1}{4}\right)^4}{8 \pi}$$

$$\frac{4 \pi \Gamma\left(\frac{5}{4}\right)^2}{\Gamma\left(\frac{3}{4}\right)^2}$$

$$\frac{9 \pi \left(\frac{1}{4}!\right)^2}{4 \left(\frac{3}{4}!\right)^2}$$

$n!$  is the factorial function

**Alternative representations:**

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left(-1 + \frac{1}{4}\right)!^2}{4 \left(-1 + \frac{3}{4}\right)!^2}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \Gamma\left(\frac{1}{4}, 0\right)^2}{4 \Gamma\left(\frac{3}{4}, 0\right)^2}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left(\frac{G\left(1+\frac{1}{4}\right)}{G\left(\frac{1}{4}\right)}\right)^2}{4 \left(\frac{G\left(1+\frac{3}{4}\right)}{G\left(\frac{3}{4}\right)}\right)^2}$$

### Series representations:

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left(\sum_{k=1}^{\infty} \left(\frac{3}{4}\right)^k c_k\right)^2}{4 \left(\sum_{k=1}^{\infty} 4^{-k} c_k\right)^2}$$

for  $\left( c_1 = 1 \text{ and } c_2 = 1 \text{ and } c_k = \frac{\gamma c_{-1+k} + \sum_{j=1}^{-2+k} (-1)^{1+j+k} c_j \zeta(-j+k)}{-1+k} \right)$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{9 \pi \left(\sum_{k=0}^{\infty} \frac{4^{-k} \Gamma^{(k)}(1)}{k!}\right)^2}{4 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}\right)^k \Gamma^{(k)}(1)}{k!}\right)^2}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left(\sum_{k=0}^{\infty} \frac{\left(\frac{1}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^2}{4 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^2} \text{ for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left(\sum_{k=0}^{\infty} \left(\frac{3}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^2}{4 \left(\sum_{k=0}^{\infty} \left(\frac{1}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^2}$$

### Integral representations:

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{1}{4} \exp\left(\gamma + \int_0^1 \frac{2 \sqrt[4]{x} - 2 x^{3/4} + \log(x)}{(-1+x) \log(x)} dx\right) \pi$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{1}{4} e^{\int_0^1 \frac{(-1+\sqrt[4]{x})^2}{(1+\sqrt{x}) \log(x)} dx} \pi$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^2 \pi}{\Gamma\left(\frac{3}{4}\right)^2 4} = \frac{\pi \left( \int_0^1 \frac{1}{\log^{3/4}\left(\frac{1}{t}\right)} dt \right)^2}{4 \left( \int_0^1 \frac{1}{\sqrt[4]{\log\left(\frac{1}{t}\right)}} dt \right)^2}$$

Now:

**Corollary 3.3.** *If  $r$  is any non-negative integer, then*

$$\int_0^\infty \frac{x^{4r+1} dx}{\cos x + \cosh x} = \frac{(-1)^r \pi^{4r+2}}{2^{2r+1}} \sum_{m=0}^\infty \frac{(-1)^m (2m+1)^{4r+1}}{\cosh\left\{\frac{1}{2}(2m+1)\pi\right\}}. \quad (3.6)$$

*Proof.* Let  $a$  be even, say,  $a = 2r$ , in (3.1). The evaluation (3.6) follows immediately.  $\square$

Let  $r = 1$  in (3.6). We use Entry 16(iii) in Chapter 17 of Ramanujan's second notebook [15], [3, p. 134]. In the notation (2.11),

$$\sum_{m=0}^\infty \frac{(-1)^m (2m+1)^5}{\cosh\left\{\frac{1}{2}(2m+1)y\right\}} = \frac{1}{2} z^6 \{1 - 16x(1-x)\} \sqrt{x(1-x)}. \quad (3.7)$$

Using also (2.13), we see that (3.6) and (3.7) yield

$$\begin{aligned} \int_0^\infty \frac{x^5 dx}{\cos x + \cosh x} &= -\frac{\pi^6}{16} \left( \frac{\sqrt{\pi}}{\Gamma^2\left(\frac{3}{4}\right)} \right)^6 \left\{ 1 - \frac{16}{4} \right\} \frac{1}{2} \\ &= \frac{3\pi^9}{32\Gamma^{12}\left(\frac{3}{4}\right)} = \frac{3\pi^3 \Gamma^6\left(\frac{1}{4}\right)}{256 \Gamma^6\left(\frac{3}{4}\right)}, \end{aligned}$$

$$\left( \left( \frac{3\pi^3}{256} \right) \left( \frac{\Gamma^6\left(\frac{1}{4}\right)}{\Gamma^6\left(\frac{3}{4}\right)} \right) \right)$$

**Input:**

$$\left( 3 \times \frac{\pi^3}{256} \right) \times \frac{\Gamma\left(\frac{1}{4}\right)^6}{\Gamma\left(\frac{3}{4}\right)^6}$$

$\Gamma(x)$  is the gamma function

**Exact result:**

$$\frac{3 \pi^3 \Gamma\left(\frac{1}{4}\right)^6}{256 \Gamma\left(\frac{3}{4}\right)^6}$$

**Decimal approximation:**

243.7331407513206852001947251977716653431983226563734391776...

243.73314075132....

**Alternate forms:**

$$\frac{3 \Gamma\left(\frac{1}{4}\right)^{12}}{2048 \pi^3}$$

$$\frac{48 \pi^3 \Gamma\left(\frac{5}{4}\right)^6}{\Gamma\left(\frac{3}{4}\right)^6}$$

$$\frac{2187 \pi^3 \left(\frac{1}{4}!\right)^6}{256 \left(\frac{3}{4}!\right)^6}$$

$n!$  is the factorial function

**Alternative representations:**

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left(-1 + \frac{1}{4}\right)!^6}{256 \left(-1 + \frac{3}{4}\right)!^6}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \Gamma\left(\frac{1}{4}, 0\right)^6}{256 \Gamma\left(\frac{3}{4}, 0\right)^6}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left(\frac{G\left(1+\frac{1}{4}\right)}{G\left(\frac{1}{4}\right)}\right)^6}{256 \left(\frac{G\left(1+\frac{3}{4}\right)}{G\left(\frac{3}{4}\right)}\right)^6}$$



### Series representations:

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left(\sum_{k=1}^{\infty} \left(\frac{3}{4}\right)^k c_k\right)^6}{256 \left(\sum_{k=1}^{\infty} 4^{-k} c_k\right)^6}$$

for  $\left( c_1 = 1 \text{ and } c_2 = 1 \text{ and } c_k = \frac{\gamma c_{-1+k} + \sum_{j=1}^{-2+k} (-1)^{1+j+k} c_j \zeta(-j+k)}{-1+k} \right)$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{2187 \pi^3 \left(\sum_{k=0}^{\infty} \frac{4^{-k} \Gamma^{(k)}(1)}{k!}\right)^6}{256 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}\right)^k \Gamma^{(k)}(1)}{k!}\right)^6}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{1}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^6}{256 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^6} \text{ for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left(\sum_{k=0}^{\infty} \left(\frac{3}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^6}{256 \left(\sum_{k=0}^{\infty} \left(\frac{1}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^6}$$

### Integral representations:

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3}{256} \exp\left(3 \left(\gamma + \int_0^1 \frac{2 \sqrt[4]{x} - 2 x^{3/4} + \log(x)}{(-1+x) \log(x)} dx\right)\right) \pi^3$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3}{256} \exp\left(\int_0^1 \frac{3(-1+\sqrt[4]{x})^2}{(1+\sqrt{x}) \log(x)} dx\right) \pi^3$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^6 3 \pi^3}{\Gamma\left(\frac{3}{4}\right)^6 256} = \frac{3 \pi^3 \left( \int_0^1 \frac{1}{\log^{3/4}\left(\frac{1}{t}\right)} dt \right)^6}{256 \left( \int_0^1 \frac{1}{\sqrt[4]{\log\left(\frac{1}{t}\right)}} dt \right)^6}$$

Now:

Again, we set  $x = \frac{1}{2}$ , which implies that  $y = \pi$ . Hence, (3.6) and (3.8) give us

$$\begin{aligned} \int_0^\infty \frac{x^9 dx}{\cos x + \cosh x} &= \frac{\pi^{10}}{2^6} \left( \frac{\sqrt{\pi}}{\Gamma^2\left(\frac{3}{4}\right)} \right)^{10} \left\{ 1 - \frac{1232}{4} + \frac{7936}{16} \right\} \frac{1}{2} \\ &= \frac{189\pi^{15}}{2^7\Gamma^{20}\left(\frac{3}{4}\right)} = \frac{189\pi^{15}}{2^7\Gamma^{10}\left(\frac{3}{4}\right)} \cdot \frac{\Gamma^{10}\left(\frac{1}{4}\right)}{(\pi\sqrt{2})^{10}} = \frac{3^3 \cdot 7\pi^5 \Gamma^{10}\left(\frac{1}{4}\right)}{2^{12} \Gamma^{10}\left(\frac{3}{4}\right)}. \end{aligned}$$

$((3^3 \cdot 7 \cdot \pi^5) / (2^{12})) \cdot (((\text{gamma}^{10}(1/4) / (\text{gamma}^{10}(3/4))))))$

**Input:**

$$\frac{3^3 \times 7 \pi^5}{2^{12}} \times \frac{\Gamma\left(\frac{1}{4}\right)^{10}}{\Gamma\left(\frac{3}{4}\right)^{10}}$$

$\Gamma(x)$  is the gamma function

**Exact result:**

$$\frac{189 \pi^5 \Gamma\left(\frac{1}{4}\right)^{10}}{4096 \Gamma\left(\frac{3}{4}\right)^{10}}$$

**Decimal approximation:**

725811.7845430244874980537425854957142684872912626410861573...

725811.784543024....

**Alternate forms:**

$$\frac{189 \Gamma\left(\frac{1}{4}\right)^{20}}{131072 \pi^5}$$

$$\frac{48384 \pi^5 \Gamma\left(\frac{5}{4}\right)^{10}}{\Gamma\left(\frac{3}{4}\right)^{10}}$$

$$\frac{11160261 \pi^5 \left(\frac{1}{4}!\right)^{10}}{4096 \left(\frac{3}{4}!\right)^{10}}$$

$n!$  is the factorial function

**Alternative representations:**

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\left(-1 + \frac{1}{4}\right)!\right)^{10}}{2^{12} \left(\left(-1 + \frac{3}{4}\right)!\right)^{10}}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \Gamma\left(\frac{1}{4}, 0\right)^{10}}{2^{12} \Gamma\left(\frac{3}{4}, 0\right)^{10}}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\frac{G\left(1+\frac{1}{4}\right)}{G\left(\frac{1}{4}\right)}\right)^{10}}{2^{12} \left(\frac{G\left(1+\frac{3}{4}\right)}{G\left(\frac{3}{4}\right)}\right)^{10}}$$

**Series representations:**

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\sum_{k=1}^{\infty} \left(\frac{3}{4}\right)^k c_k\right)^{10}}{4096 \left(\sum_{k=1}^{\infty} 4^{-k} c_k\right)^{10}}$$

$$\text{for } \left( c_1 = 1 \text{ and } c_2 = 1 \text{ and } c_k = \frac{\gamma c_{-1+k} + \sum_{j=1}^{-2+k} (-1)^{1+j+k} c_j \zeta(-j+k)}{-1+k} \right)$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{11160261 \pi^5 \left(\sum_{k=0}^{\infty} \frac{4^{-k} \Gamma^{(k)}(1)}{k!}\right)^{10}}{4096 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}\right)^k \Gamma^{(k)}(1)}{k!}\right)^{10}}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{1}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^{10}}{4096 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^{10}} \text{ for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\sum_{k=0}^{\infty} \left(\frac{3}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^{10}}{4096 \left(\sum_{k=0}^{\infty} \left(\frac{1}{4}-z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2}(-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^{10}}$$

### Integral representations:

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \exp\left(5 \gamma + \int_0^1 \frac{5\left(2\sqrt[4]{x} - 2x^{3/4} + \log(x)\right)}{(-1+x)\log(x)} dx\right) \pi^5}{4096}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \exp\left(10 \int_0^1 \frac{\left(-1+\sqrt[4]{x}\right)^2}{2(1+\sqrt{x})\log(x)} dx\right) \pi^5}{4096}$$

$$\frac{\Gamma\left(\frac{1}{4}\right)^{10} (3^3 \times 7 \pi^5)}{\Gamma\left(\frac{3}{4}\right)^{10} 2^{12}} = \frac{189 \pi^5 \left(\int_0^1 \frac{1}{\log^{3/4}\left(\frac{1}{t}\right)} dt\right)^{10}}{4096 \left(\int_0^1 \frac{1}{\sqrt[4]{\log\left(\frac{1}{t}\right)}} dt\right)^{10}}$$

From the ratio of the two results, we obtain:

$$(725811.7845430244 / 243.7331407513)$$

**Input interpretation:**

$$\frac{725811.7845430244}{243.7331407513}$$

**Result:**

2977.895342035685543330666692660957446344073975995620545628...

2977.8953420

And multiplying by  $1/\pi$  this result, divided by the previous obtained value, we obtain:

$$1/\pi(2977.8953420356 / 6.8751858180)$$

**Input interpretation:**

$$\frac{1}{\pi} \times \frac{2977.8953420356}{6.8751858180}$$

**Result:**

137.87169576...

137.87169576 result very near to the rest mass of Pion meson 139.57

**Alternative representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{2977.89534203560000}{6.87518581800000 (180^\circ)}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{2977.89534203560000}{6.87518581800000 (-i \log(-1))}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{2977.89534203560000}{6.87518581800000 \cos^{-1}(-1)}$$

**Series representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{108.284176634148}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{216.568353268296}{-1.0000000000000000 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{433.136706536591}{\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}}$$

**Integral representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{216.568353268296}{\int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{108.284176634148}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} = \frac{216.568353268296}{\int_0^{\infty} \frac{\sin(t)}{t} dt}$$

Or:

golden ratio+1/Pi(2977.8953420356 / 6.8751858180)

**Input interpretation:**

$$\phi + \frac{1}{\pi} \times \frac{2977.8953420356}{6.8751858180}$$

$\phi$  is the golden ratio

**Result:**

139.48972975...

139.48972975.... result very near to the rest mass of Pion meson 139.57

**Alternative representations:**

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = -2 \cos(216^\circ) + \frac{2977.89534203560000}{6.87518581800000 \pi}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = 2 \cos\left(\frac{\pi}{5}\right) + \frac{2977.89534203560000}{6.87518581800000 \pi}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = -2 \cos(216^\circ) + \frac{2977.89534203560000}{6.87518581800000 (180^\circ)}$$

**Series representations:**

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{108.284176634148}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{216.568353268296}{-1.0000000000000000 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{433.136706536591}{\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}}$$

**Integral representations:**

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{216.568353268296}{\int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{108.284176634148}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\phi + \frac{2977.89534203560000}{6.87518581800000 \pi} = \phi + \frac{216.568353268296}{\int_0^{\infty} \frac{\sin(t)}{t} dt}$$

And:

$$1/\text{Pi}(2977.8953420356 / 6.8751858180) - 13$$

**Input interpretation:**

$$\frac{1}{\pi} \times \frac{2977.8953420356}{6.8751858180} - 13$$

**Result:**

124.87169576...

124.87169576.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

**Alternative representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{2977.89534203560000}{6.87518581800000 (180^\circ)}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{2977.89534203560000}{6.87518581800000 (-i \log(-1))}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{2977.89534203560000}{6.87518581800000 \cos^{-1}(-1)}$$

**Series representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{108.284176634148}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{216.568353268296}{-1.000000000000000 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{433.136706536591}{\sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}}}$$



**Integral representations:**

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{216.568353268296}{\int_0^\infty \frac{1}{1+t^2} dt}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{108.284176634148}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{2977.89534203560000}{6.87518581800000 \pi} - 13 = -13 + \frac{216.568353268296}{\int_0^\infty \frac{\sin(t)}{t} dt}$$

We note that from the result of previous expression,

$$\frac{725811.7845430244}{243.7331407513}$$

we obtain also:

$$1/2(725811.7845430244 / 243.7331407513)+199+47-7$$

where 7, 47 and 199 are Lucas numbers

**Input interpretation:**

$$\frac{1}{2} \times \frac{725811.7845430244}{243.7331407513} + 199 + 47 - 7$$

**Result:**

1727.947671017842771665333346330478723172036987997810272814...

1727.9476710...

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

And:

$$2\sqrt{(725811.7845430244 / 243.7331407513)+11+5}$$

Where 5 is a Fibonacci number and 11 is a Lucas number

**Input interpretation:**

$$2\sqrt{\frac{725811.7845430244}{243.7331407513} + 11 + 5}$$

**Result:**

125.1401913510...

125.1401913510... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

We obtain also:

$$(((1/\sqrt{(725811.7845430244 / 243.7331407513)})))^{1/1024}$$

**Input interpretation:**

$$1024\sqrt{\sqrt{\frac{1}{\sqrt{\frac{725811.7845430244}{243.7331407513}}}}}$$

**Result:**

0.9961018694329181...

0.9961018694329181.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

$$(754+1.7168646644) \times 10^3 * (((3^3 * 7 * \pi^5) / (2^{12}))) (((\Gamma(1/4) / (\Gamma(3/4))))))$$

**Input interpretation:**

$$(754 + 1.7168646644) \times 10^3 \times \frac{3^3 \times 7 \pi^5}{2^{12}} \times \frac{\Gamma\left(\frac{1}{4}\right)^{10}}{\Gamma\left(\frac{3}{4}\right)^{10}}$$

$\Gamma(x)$  is the gamma function

**Result:**

$$5.4850820615133... \times 10^{11}$$

$$5.4850820615133 * 10^{11}$$

**Alternative representations:**

$$\frac{(754 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} = \frac{142830.487421571600 \times 10^3 \pi^5 \left(-1 + \frac{1}{4}\right)!^{10}}{2^{12} \left(-1 + \frac{3}{4}\right)!^{10}}$$

$$\frac{(754 + 1.716864664400000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{142830.487421571600 \times 10^3 \pi^5 \Gamma\left(\frac{1}{4}, 0\right)^{10}}{2^{12} \Gamma\left(\frac{3}{4}, 0\right)^{10}}$$

$$\frac{(754 + 1.716864664400000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{142830.487421571600 \times 10^3 \pi^5 \left(\frac{G\left(1+\frac{1}{4}\right)}{G\left(\frac{1}{4}\right)}\right)^{10}}{2^{12} \left(\frac{G\left(1+\frac{3}{4}\right)}{G\left(\frac{3}{4}\right)}\right)^{10}}$$

### Series representations:

$$\frac{(754 + 1.716864664400000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{2.05908140912021030 \times 10^9 \pi^5 \left(\sum_{k=0}^{\infty} \frac{4^{-k} \Gamma^{(k)}(1)}{k!}\right)^{10}}{\left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}\right)^k \Gamma^{(k)}(1)}{k!}\right)^{10}}$$

$$\frac{(754 + 1.716864664400000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left(\sum_{k=0}^{\infty} \frac{\left(\frac{1}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^{10}}{\left(\sum_{k=0}^{\infty} \frac{\left(\frac{3}{4}-z_0\right)^k \Gamma^{(k)}(z_0)}{k!}\right)^{10}} \quad \text{for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{(754 + 1.716864664400000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left(\sum_{k=0}^{\infty} \left(\frac{3}{4} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} \pi (-j+k+2 z_0)\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^{10}}{\left(\sum_{k=0}^{\infty} \left(\frac{1}{4} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} \pi (-j+k+2 z_0)\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}\right)^{10}}$$

**Integral representations:**

$$\frac{(754 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} = \frac{34870.7244681571289 \pi^5 \left(\int_0^1 \frac{1}{\log^{3/4}\left(\frac{1}{t}\right)} dt\right)^{10}}{\left(\int_0^1 \frac{1}{\sqrt[4]{\log\left(\frac{1}{t}\right)}} dt\right)^{10}}$$

$$\frac{(754 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} = \frac{34870.7244681571289 \pi^5 \left(\int_0^\infty \frac{e^{-t}}{t^{3/4}} dt\right)^{10}}{\left(\int_0^\infty \frac{e^{-t}}{\sqrt[4]{t}} dt\right)^{10}}$$

$$\frac{(754 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} = \frac{34870.7244681571289 \pi^5 \csc^{10}\left(\frac{\pi}{8}\right) \left(\int_0^\infty \frac{\sin(t)}{t^{3/4}} dt\right)^{10}}{\csc^{10}\left(\frac{3\pi}{8}\right) \left(\int_0^\infty \frac{\sin(t)}{\sqrt[4]{t}} dt\right)^{10}}$$

Or:

$$(775-21+1.7168646644)*10^3 * (((3^3*7*\pi^5)/(2^12))) (((\gamma^{10}(1/4)/(\gamma^{10}(3/4))))))$$

Where 775 is very near to the rest mass of Charged rho meson 775.11 and 1.7168646644 is a Ramanujan mock theta function

**Input interpretation:**

$$(775 - 21 + 1.7168646644) \times 10^3 \times \frac{3^3 \times 7 \pi^5}{2^{12}} \times \frac{\Gamma\left(\frac{1}{4}\right)^{10}}{\Gamma\left(\frac{3}{4}\right)^{10}}$$

$\Gamma(x)$  is the gamma function

**Result:**

$$5.4850820615133... \times 10^{11}$$

$$5.485082.... * 10^{11}$$

The two results are very near to the value  $5.48515304... * 10^{11}$  that is the generalized black hole entropy (see previous analyzed formula (19))

**Alternative representations:**

$$\frac{((775 - 21 + 1.71686466440000) 10^3 \Gamma(\frac{1}{4})^{10}) 3^3 (7 \pi^5)}{2^{12} \Gamma(\frac{3}{4})^{10}} =$$

$$\frac{142830.487421571600 \times 10^3 \pi^5 \left((-1 + \frac{1}{4})!\right)^{10}}{2^{12} \left((-1 + \frac{3}{4})!\right)^{10}}$$

$$\frac{((775 - 21 + 1.71686466440000) 10^3 \Gamma(\frac{1}{4})^{10}) 3^3 (7 \pi^5)}{2^{12} \Gamma(\frac{3}{4})^{10}} =$$

$$\frac{142830.487421571600 \times 10^3 \pi^5 \Gamma(\frac{1}{4}, 0)^{10}}{2^{12} \Gamma(\frac{3}{4}, 0)^{10}}$$

$$\frac{((775 - 21 + 1.71686466440000) 10^3 \Gamma(\frac{1}{4})^{10}) 3^3 (7 \pi^5)}{2^{12} \Gamma(\frac{3}{4})^{10}} =$$

$$\frac{142830.487421571600 \times 10^3 \pi^5 \left(\frac{G(1+\frac{1}{4})}{G(\frac{1}{4})}\right)^{10}}{2^{12} \left(\frac{G(1+\frac{3}{4})}{G(\frac{3}{4})}\right)^{10}}$$

**Series representations:**

$$\frac{((775 - 21 + 1.71686466440000) 10^3 \Gamma(\frac{1}{4})^{10}) 3^3 (7 \pi^5)}{2^{12} \Gamma(\frac{3}{4})^{10}} =$$

$$\frac{2.05908140912021030 \times 10^9 \pi^5 \left(\sum_{k=0}^{\infty} \frac{4^{-k} \Gamma^{(k)}(1)}{k!}\right)^{10}}{\left(\sum_{k=0}^{\infty} \frac{(\frac{3}{4})^k \Gamma^{(k)}(1)}{k!}\right)^{10}}$$

$$\frac{(775 - 21 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left( \sum_{k=0}^{\infty} \frac{\left(\frac{1}{4} - z_0\right)^k \Gamma^{(k)}(z_0)}{k!} \right)^{10}}{\left( \sum_{k=0}^{\infty} \frac{\left(\frac{3}{4} - z_0\right)^k \Gamma^{(k)}(z_0)}{k!} \right)^{10}} \quad \text{for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{(775 - 21 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left( \sum_{k=0}^{\infty} \left(\frac{3}{4} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} \pi (-j+k+2 z_0)\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!} \right)^{10}}{\left( \sum_{k=0}^{\infty} \left(\frac{1}{4} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} \pi (-j+k+2 z_0)\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!} \right)^{10}}$$

### Integral representations:

$$\frac{(775 - 21 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left( \int_0^1 \frac{1}{\log^{3/4}\left(\frac{1}{t}\right)} dt \right)^{10}}{\left( \int_0^1 \frac{1}{\sqrt[4]{\log\left(\frac{1}{t}\right)}} dt \right)^{10}}$$

$$\frac{(775 - 21 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \left( \int_0^{\infty} \frac{e^{-t}}{t^{3/4}} dt \right)^{10}}{\left( \int_0^{\infty} \frac{e^{-t}}{\sqrt[4]{t}} dt \right)^{10}}$$

$$\frac{(775 - 21 + 1.71686466440000) 10^3 \Gamma\left(\frac{1}{4}\right)^{10} 3^3 (7 \pi^5)}{2^{12} \Gamma\left(\frac{3}{4}\right)^{10}} =$$

$$\frac{34870.7244681571289 \pi^5 \csc^{10}\left(\frac{\pi}{8}\right) \left( \int_0^{\infty} \frac{\sin(t)}{t^{3/4}} dt \right)^{10}}{\csc^{10}\left(\frac{3\pi}{8}\right) \left( \int_0^{\infty} \frac{\sin(t)}{\sqrt[4]{t}} dt \right)^{10}}$$

From:

## Anomalies in the Space of Coupling Constants and Their Dynamical Applications I

Clay Cordova, Daniel S. Freed, Ho Tat Lam, and Nathan Seiberg

arXiv:1905.09315v3 [hep-th] 30 Oct 2019

<sup>24</sup>As usual, it is convenient to define this term by an extension to a spin four-manifold  $Y$ . Then for any integer  $k$  we have

$$\exp\left(ik \int_X CS_{\text{grav}}\right) = \exp\left(2\pi ik \int_Y \frac{p_1(Y)}{48}\right) = \exp\left(\frac{ik}{192\pi} \int_Y \text{Tr}(R \wedge R)\right), \quad (3.14)$$

where  $p_1(Y)$  is the Pontrjagin class and we have used  $\int_Y p_1(Y) \in 48\mathbb{Z}$  for any closed spin manifold  $Y$ . Although this term is called a gravitational ‘Chern-Simons term’ in the physics literature, it is not covered by the work of Chern-Simons [56]. Rather, it is an exponentiated  $\eta$ -invariant; see Remark 6.25.

In particular we can use this to recover the  $\mathbb{T}$  anomaly of the theory at  $m = 0$ : using  $\rho(0) = 1/2$ , the anomaly becomes a familiar gravitational  $\theta_g$ -angle at the non-trivial  $\mathbb{T}$ -invariant value of  $\theta_g = \pi$ .

$$\tilde{Z}[m, g] = Z[m, g] \exp\left(-i \int_Y \rho(m) dCS_{\text{grav}}\right) = Z[m, g] \exp\left(-\frac{i}{192\pi} \int_Y \rho(m) \text{Tr}(R \wedge R)\right), \quad (3.15)$$

where we have considered  $\rho(m) = 1/2$  and  $\text{Tr}(R \wedge R) = -5$ .

We obtain:

$$\exp\left(\left(\left(-i/(192\pi)\right) \int \left[1/2 \cdot (-5)\right] dx\right)\right)$$

**Input:**

$$\exp\left(-\frac{i}{192\pi} \int \left(\frac{1}{2} \times (-5)\right) x dx\right)$$

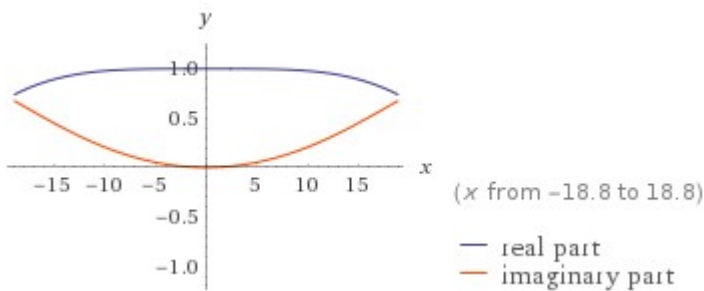
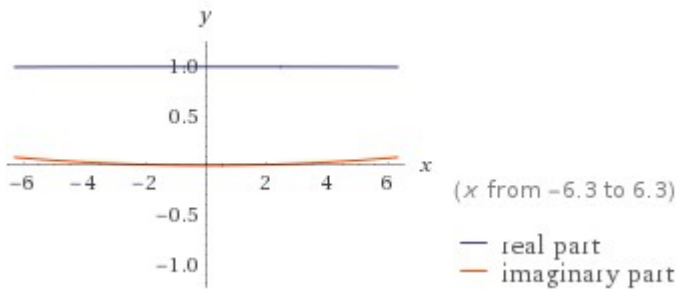
$i$  is the imaginary unit

**Exact result:**

$$e^{(5ix^2)/(768\pi)}$$

**Plots:**





**Alternate form assuming x is real:**

$$\cos\left(\frac{5x^2}{768\pi}\right) + i \sin\left(\frac{5x^2}{768\pi}\right)$$

**Series expansion of the integral at x = 0:**

$$1 + \frac{5ix^2}{768\pi} - \frac{25x^4}{1179648\pi^2} + O(x^5)$$

(Taylor series)

**Indefinite integral:**

$$\exp\left(-\frac{i \int -\frac{5x}{2} dx}{192\pi}\right) = e^{\frac{5ix^2}{768\pi} + \text{constant}}$$

From

$$\cos\left(\frac{5x^2}{768\pi}\right) + i \sin\left(\frac{5x^2}{768\pi}\right)$$

For x = 10 and changing the sign, we obtain:

$$\cos\left(\frac{5 \cdot 10^2}{768\pi}\right) - \sin\left(\frac{5 \cdot 10^2}{768\pi}\right)$$

**Input:**

$$\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)$$

**Exact result:**

$$\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)$$

**Decimal approximation:**

0.772851086145922732558991065986292895441132242434402113431...

0.7728510861459....

**Alternate forms:**

$$\left(\frac{1}{2} - \frac{i}{2}\right) e^{-(125 i)/(192 \pi)} + \left(\frac{1}{2} + \frac{i}{2}\right) e^{(125 i)/(192 \pi)}$$

$$\left(\cos\left(\frac{1}{192 \pi}\right) - \sin\left(\frac{1}{192 \pi}\right)\right) \left(-1 - 2 \sin\left(\frac{1}{96 \pi}\right) + 2 \cos\left(\frac{1}{48 \pi}\right)\right) \\ \left(-1 - 2 \sin\left(\frac{5}{96 \pi}\right) + 2 \cos\left(\frac{5}{48 \pi}\right)\right) \left(-1 - 2 \sin\left(\frac{25}{96 \pi}\right) + 2 \cos\left(\frac{25}{48 \pi}\right)\right)$$

**Alternative representations:**

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \cosh\left(-\frac{5 i 10^2}{768 \pi}\right) + \cos\left(\frac{\pi}{2} + \frac{5 \times 10^2}{768 \pi}\right)$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \cosh\left(-\frac{5 i 10^2}{768 \pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768 \pi}\right)$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \cosh\left(\frac{5 i 10^2}{768 \pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768 \pi}\right)$$

**Series representations:**

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \sum_{k=0}^{\infty} \frac{(192 \pi)^{-2k} \left((-15 625)^k + (-1)^{1+k} (125 - 96 \pi^2)^{2k}\right)}{(2k)!}$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \sum_{k=0}^{\infty} \left( \frac{(-15 625)^k (192 \pi)^{-2k}}{(2k)!} - \frac{e^{i k \pi} \left(\frac{192 \pi}{125}\right)^{-1-2k}}{(1+2k)!} \right)$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \sum_{k=0}^{\infty} \left( \frac{(-1)^{1+k} \left(\frac{125}{192 \pi} - \frac{\pi}{2}\right)^{1+2k}}{(1+2k)!} - \frac{e^{i k \pi} \left(\frac{192 \pi}{125}\right)^{-1-2k}}{(1+2k)!} \right)$$

**Integral representations:**

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \int_{-i \infty + \gamma}^{i \infty + \gamma} -\frac{i e^{-15625/(147456 \pi^2 s) + s} (-125 + 384 \pi s)}{768 \pi^{3/2} s^{3/2}} ds \quad \text{for } \gamma > 0$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \frac{-125 i \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{e^{-15625/(147456 \pi^2 s) + s}}{s^{3/2}} ds + 768 \pi^{3/2} \int_{\frac{\pi}{2}}^{\frac{192 \pi}{2}} \sin(t) dt}{768 \pi^{3/2}} \quad \text{for } \gamma > 0$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = \frac{i \left( 96 \sqrt{\pi} \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{e^{-15625/(147456 \pi^2 s) + s}}{\sqrt{s}} ds - 125 i \int_0^1 \cos\left(\frac{125 t}{192 \pi}\right) dt \right)}{192 \pi} \quad \text{for } \gamma > 0$$

### Multiple-argument formulas:

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = -1 + 2 \cos^2\left(\frac{125}{384 \pi}\right) - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right)$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = 1 - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right) - 2 \sin^2\left(\frac{125}{384 \pi}\right)$$

$$\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right) = T_{\frac{125}{192}}\left(\cos\left(\frac{1}{\pi}\right)\right) - \sin\left(\frac{125}{192 \pi}\right)$$

From the result, we obtain:

$$1/\left(\left(\left(\left(\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)\right)\right)\right)\right)^{19}$$

where the exponent 19 is equal to 11 + 8, where 11 is a Lucas number and 8 is a Fibonacci number

**Input:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}}$$

**Exact result:**

$$\frac{1}{\left(\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)\right)^{19}}$$

**Decimal approximation:**

133.7147723975021853100107295880967019756047198495828154313...

133.7147723... result near to the rest mass of Pion meson 134.9766

**Alternate forms:**

$$-\frac{1}{\left(\sin\left(\frac{125}{192\pi}\right) - \cos\left(\frac{125}{192\pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\frac{1}{2}\left(e^{-i(125)/(192\pi)} + e^{i(125)/(192\pi)}\right) - \frac{1}{2}i\left(e^{-i(125)/(192\pi)} - e^{i(125)/(192\pi)}\right)\right)^{19}}$$

$$\frac{1}{\left(\left(\cos\left(\frac{1}{192\pi}\right) - \sin\left(\frac{1}{192\pi}\right)\right)^{19} \left(-1 - 2\sin\left(\frac{1}{96\pi}\right) + 2\cos\left(\frac{1}{48\pi}\right)\right)^{19} \right. \\ \left. \left(-1 - 2\sin\left(\frac{5}{96\pi}\right) + 2\cos\left(\frac{5}{48\pi}\right)\right)^{19} \left(-1 - 2\sin\left(\frac{25}{96\pi}\right) + 2\cos\left(\frac{25}{48\pi}\right)\right)^{19}\right)}$$

**Alternative representations:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} = \frac{1}{\left(\cosh\left(-\frac{5i \cdot 10^2}{768\pi}\right) + \cos\left(\frac{\pi}{2} + \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} = \frac{1}{\left(\cosh\left(-\frac{5i \cdot 10^2}{768\pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} = \frac{1}{\left(\cosh\left(\frac{5i \cdot 10^2}{768\pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

**Series representations:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} = \frac{1}{\left(\sum_{k=0}^{\infty} \frac{(192\pi)^{-2k} (-15 \cdot 625)^k + (-1)^{1+k} (125 - 96\pi^2)^{2k}}{(2k)!}\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} = \frac{1}{\left(\sum_{k=0}^{\infty} \left(\frac{(-15 \cdot 625)^k (192\pi)^{-2k}}{(2k)!} - \frac{e^{i k \pi} \left(\frac{192\pi}{125}\right)^{-1-2k}}{(1+2k)!}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} = \frac{1}{\left(\sum_{k=0}^{\infty} \left(\frac{(-1)^{1+k} \left(\frac{125}{192 \pi} - \frac{\pi}{2}\right)^{1+2k}}{(1+2k)!} - \frac{e^{i k \pi} \left(\frac{192 \pi}{125}\right)^{-1-2k}}{(1+2k)!}\right)\right)^{19}}$$

**Multiple-argument formulas:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} = - \frac{1}{\left(1 - 2 \cos^2\left(\frac{125}{384 \pi}\right) + \sin\left(\frac{125}{192 \pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} = - \frac{1}{\left(-1 + 2 \sin^2\left(\frac{125}{384 \pi}\right) + \sin\left(\frac{125}{192 \pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} = \frac{1}{\left(T_{\frac{125}{192}}\left(\cos\left(\frac{1}{\pi}\right)\right) - \sin\left(\frac{125}{192 \pi}\right)\right)^{19}}$$

And:

$$1/\left(\left(\left(\left(\left(\cos\left(\frac{5 * 10^2}{768 \pi}\right) - \sin\left(\frac{5 * 10^2}{768 \pi}\right)\right)\right)\right)\right)\right)^{19} - 8$$

where 8 is a Fibonacci number

**Input:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8$$

**Exact result:**

$$\frac{1}{\left(\cos\left(\frac{125}{192 \pi}\right) - \sin\left(\frac{125}{192 \pi}\right)\right)^{19}} - 8$$

**Decimal approximation:**

125.7147723975021853100107295880967019756047198495828154313...

125.7147723975.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

**Alternate forms:**

$$-8 - \frac{1}{\left(\sin\left(\frac{125}{192\pi}\right) - \cos\left(\frac{125}{192\pi}\right)\right)^{19}}$$

$$-8 + \frac{1}{\left(\frac{1}{2}\left(e^{-(125i)/(192\pi)} + e^{(125i)/(192\pi)}\right) - \frac{1}{2}i\left(e^{-(125i)/(192\pi)} - e^{(125i)/(192\pi)}\right)\right)^{19}}$$

$$\begin{aligned} & \left(1 + 8 \sin^{17}\left(\frac{125}{192\pi}\right) - 8 \cos^{19}\left(\frac{125}{192\pi}\right) + 152 \sin\left(\frac{125}{192\pi}\right) \cos^{18}\left(\frac{125}{192\pi}\right) - \right. \\ & 1368 \sin^2\left(\frac{125}{192\pi}\right) \cos^{17}\left(\frac{125}{192\pi}\right) + 7752 \sin^3\left(\frac{125}{192\pi}\right) \cos^{16}\left(\frac{125}{192\pi}\right) - \\ & 31008 \sin^4\left(\frac{125}{192\pi}\right) \cos^{15}\left(\frac{125}{192\pi}\right) + 93024 \sin^5\left(\frac{125}{192\pi}\right) \cos^{14}\left(\frac{125}{192\pi}\right) - \\ & 217056 \sin^6\left(\frac{125}{192\pi}\right) \cos^{13}\left(\frac{125}{192\pi}\right) + 403104 \sin^7\left(\frac{125}{192\pi}\right) \cos^{12}\left(\frac{125}{192\pi}\right) - \\ & 604656 \sin^8\left(\frac{125}{192\pi}\right) \cos^{11}\left(\frac{125}{192\pi}\right) + 739024 \sin^9\left(\frac{125}{192\pi}\right) \cos^{10}\left(\frac{125}{192\pi}\right) - \\ & 739024 \sin^{10}\left(\frac{125}{192\pi}\right) \cos^9\left(\frac{125}{192\pi}\right) + 604656 \sin^{11}\left(\frac{125}{192\pi}\right) \cos^8\left(\frac{125}{192\pi}\right) - \\ & 403104 \sin^{12}\left(\frac{125}{192\pi}\right) \cos^7\left(\frac{125}{192\pi}\right) + 217056 \sin^{13}\left(\frac{125}{192\pi}\right) \cos^6\left(\frac{125}{192\pi}\right) - \\ & 93024 \sin^{14}\left(\frac{125}{192\pi}\right) \cos^5\left(\frac{125}{192\pi}\right) + 31008 \sin^{15}\left(\frac{125}{192\pi}\right) \cos^4\left(\frac{125}{192\pi}\right) - \\ & 7752 \sin^{16}\left(\frac{125}{192\pi}\right) \cos^3\left(\frac{125}{192\pi}\right) + 1360 \sin^{17}\left(\frac{125}{192\pi}\right) \cos^2\left(\frac{125}{192\pi}\right) - \\ & \left. 152 \sin^{18}\left(\frac{125}{192\pi}\right) \cos\left(\frac{125}{192\pi}\right)\right) / \left(\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)\right)^{19} \end{aligned}$$

**Alternative representations:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\cosh\left(-\frac{5i \cdot 10^2}{768\pi}\right) + \cos\left(\frac{\pi}{2} + \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\cosh\left(-\frac{5i \cdot 10^2}{768\pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\cosh\left(\frac{5i \cdot 10^2}{768\pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768\pi}\right)\right)^{19}}$$

**Series representations:**

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768\pi}\right) - \sin\left(\frac{5 \times 10^2}{768\pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\sum_{k=0}^{\infty} \frac{(192\pi)^{-2k} \left((-15 \cdot 625)^k + (-1)^{1+k} (125 - 96\pi^2)^{2k}\right)}{(2k)!}\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\sum_{k=0}^{\infty} \frac{(-15625)^k (192 \pi)^{-1-2k} (-125(2k)! + 192 \pi (1+2k)!)}{(2k)!(1+2k)!}\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(\sum_{k=0}^{\infty} \left(\frac{(-1)^{-1+k} \left(\frac{125}{192 \pi} - \frac{\pi}{2}\right)^{1+2k}}{(1+2k)!} + \frac{(-1)^{1+k} 125^{1+2k} (192 \pi)^{-1-2k}}{(1+2k)!}\right)\right)^{19}}$$

### Multiple-argument formulas:

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(T_{\frac{125}{192}}\left(\cos\left(\frac{1}{\pi}\right)\right) - \sin\left(\frac{125}{192 \pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(-1 + 2 \cos^2\left(\frac{125}{384 \pi}\right) - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right)\right)^{19}}$$

$$\frac{1}{\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)^{19}} - 8 = -8 + \frac{1}{\left(1 - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right) - 2 \sin^2\left(\frac{125}{384 \pi}\right)\right)^{19}}$$

$T_n(x)$  is the Chebyshev polynomial of the first kind

In conclusion, performing the 64th root:

$$\left(\left(\left(\left(\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)\right)\right)\right)\right)^{1/64}$$

### Input:

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)}$$

### Exact result:

$$\sqrt[64]{\cos\left(\frac{125}{192 \pi}\right) - \sin\left(\frac{125}{192 \pi}\right)}$$

### Decimal approximation:

0.995982017326860600787685769715711218867654510292850800244...

0.99598201732.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Alternate form:**

$$64 \sqrt[64]{\frac{1}{2} \left( e^{-(125i)/(192\pi)} + e^{(125i)/(192\pi)} \right) - \frac{1}{2} i \left( e^{-(125i)/(192\pi)} - e^{(125i)/(192\pi)} \right)}$$

**All 64th roots of  $\cos(125/(192\pi)) - \sin(125/(192\pi))$ :**

$$e^0 \sqrt[64]{\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)} \approx 0.995982 \text{ (real, principal root)}$$

$$e^{(i\pi)/32} \sqrt[64]{\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)} \approx 0.991186 + 0.09762 i$$

$$e^{(i\pi)/16} \sqrt[64]{\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)} \approx 0.976845 + 0.19431 i$$

$$e^{(3i\pi)/32} \sqrt[64]{\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)} \approx 0.95310 + 0.28912 i$$

$$e^{(i\pi)/8} \sqrt[64]{\cos\left(\frac{125}{192\pi}\right) - \sin\left(\frac{125}{192\pi}\right)} \approx 0.92017 + 0.38115 i$$

**Alternative representations:**



$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\cosh\left(-\frac{5 i 10^2}{768 \pi}\right) + \cos\left(\frac{\pi}{2} + \frac{5 \times 10^2}{768 \pi}\right)}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\cosh\left(-\frac{5 i 10^2}{768 \pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768 \pi}\right)}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\cosh\left(\frac{5 i 10^2}{768 \pi}\right) - \cos\left(\frac{\pi}{2} - \frac{5 \times 10^2}{768 \pi}\right)}$$

### Series representations:

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\sum_{k=0}^{\infty} \frac{(192 \pi)^{-2k} \left((-15 625)^k + (-1)^{1+k} (125 - 96 \pi^2)^{2k}\right)}{(2k)!}}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\sum_{k=0}^{\infty} \left( \frac{(-15 625)^k (192 \pi)^{-2k}}{(2k)!} - \frac{e^{i k \pi} \left(\frac{192 \pi}{125}\right)^{-1-2k}}{(1+2k)!} \right)}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\sum_{k=0}^{\infty} \left( \frac{(-1)^{1+k} \left(\frac{125}{192 \pi} - \frac{\pi}{2}\right)^{1+2k}}{(1+2k)!} - \frac{e^{i k \pi} \left(\frac{192 \pi}{125}\right)^{-1-2k}}{(1+2k)!} \right)}$$

### Integral representations:

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{\int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{i e^{-15 625 / (147 456 \pi^2 s) + s} (-125 + 384 \pi s)}{768 \pi^{3/2} s^{3/2}} ds \quad \text{for } \gamma > 0}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \frac{\sqrt[64]{-96 i \sqrt{\pi} \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{e^{-15625 / (147456 \pi^2 s) + s}}{\sqrt{s}} ds - 125 \int_0^1 \cos\left(\frac{125 t}{192 \pi}\right) dt}}{2^{3/32} \sqrt[64]{3 \pi}} \quad \text{for } \gamma > 0$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \frac{\sqrt[64]{125 i \int_{-i \infty + \gamma}^{i \infty + \gamma} \frac{e^{-15625/(147456 \pi^2 s) + s}}{s^{3/2}} ds - 768 \pi^{3/2} \int_{\frac{\pi}{2}}^{\frac{192 \pi}{2}} \sin(t) dt}}{\sqrt[8]{2} \sqrt[64]{3} \pi^{3/128}} \quad \text{for } \gamma > 0$$

### Multiple-argument formulas:

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{T_{\frac{125}{192}}\left(\cos\left(\frac{1}{\pi}\right)\right) - \sin\left(\frac{125}{192 \pi}\right)}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{-1 + 2 \cos^2\left(\frac{125}{384 \pi}\right) - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right)}$$

$$\sqrt[64]{\cos\left(\frac{5 \times 10^2}{768 \pi}\right) - \sin\left(\frac{5 \times 10^2}{768 \pi}\right)} = \sqrt[64]{1 - 2 \cos\left(\frac{125}{384 \pi}\right) \sin\left(\frac{125}{384 \pi}\right) - 2 \sin^2\left(\frac{125}{384 \pi}\right)}$$

Now, we have:

$$\tilde{Z}[m, g] = Z[m, g] \exp\left(2\pi i \int_Y \lambda(m) \wedge \frac{p_1(Y)}{48}\right), \quad (3.22)$$

Utilizing always the same previous values, we obtain:

$$\exp(((2\pi i) \int [1/2 * (-5)]x))$$

**Input:**

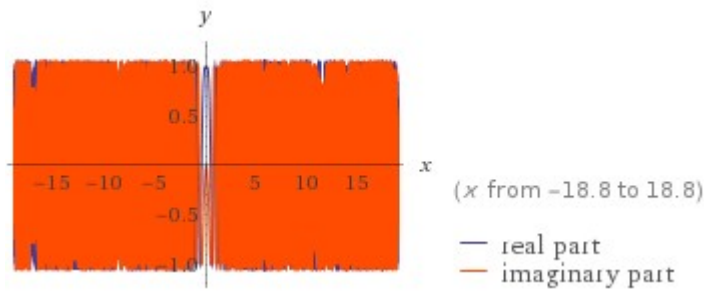
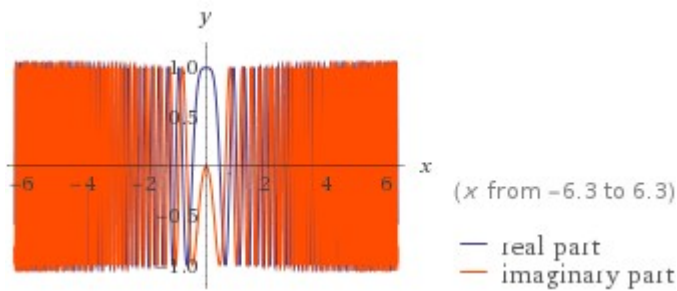
$$\exp\left(2\pi i \int \left(\frac{1}{2} \times (-5)\right) x dx\right)$$

$i$  is the imaginary unit

**Exact result:**

$$e^{-5/2 i \pi x^2}$$

**Plots:**



**Alternate form assuming x is real:**

$$\cos\left(\frac{5\pi x^2}{2}\right) - i \sin\left(\frac{5\pi x^2}{2}\right)$$

**Series expansion of the integral at x = 0:**

$$1 - \frac{5}{2} i \pi x^2 - \frac{25 \pi^2 x^4}{8} + O(x^5)$$

(Taylor series)

**Indefinite integral:**

$$\exp\left(2\pi i \int -\frac{5x}{2} dx\right) = e^{-\frac{5}{2} i \pi x^2 + \text{constant}}$$

From the solution

$$\cos\left(\frac{5\pi x^2}{2}\right) - i \sin\left(\frac{5\pi x^2}{2}\right)$$

for x = 5, (where 5 is a Fibonacci number) we obtain:

$$\cos\left(\frac{5\pi \cdot 5^2}{2}\right) - i \sin\left(\frac{5\pi \cdot 5^2}{2}\right)$$

**Input:**

$$\cos\left(\frac{1}{2} (5\pi \times 5^2)\right) - i \sin\left(\frac{1}{2} (5\pi \times 5^2)\right)$$

$i$  is the imaginary unit

**Result:**

$-i$

**Polar coordinates:**

$r = 1$  (radius),  $\theta = -90^\circ$  (angle)

**Alternative representations:**

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \cosh\left(\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5 \pi 5^2}{2}\right)$$

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \cosh\left(-\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5 \pi 5^2}{2}\right)$$

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \cosh\left(-\frac{5}{2} i \pi 5^2\right) + i \cos\left(\frac{\pi}{2} + \frac{5 \pi 5^2}{2}\right)$$

**Series representations:**

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \sum_{k=0}^{\infty} \left( -2(-1)^k i J_{1+2k}\left(\frac{125 \pi}{2}\right) + \frac{(-1)^{1+k} 62^{1+2k} \pi^{1+2k}}{(1+2k)!} \right)$$

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \sum_{k=0}^{\infty} \left( -2(-1)^k i J_{1+2k}\left(\frac{125 \pi}{2}\right) + \frac{\left(-\frac{15 \cdot 625}{4}\right)^k \pi^{2k}}{(2k)!} \right)$$

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \sum_{k=0}^{\infty} \left( \frac{\left(-\frac{15 \cdot 625}{4}\right)^k \pi^{2k}}{(2k)!} - \frac{i \left(\left(\frac{2}{125}\right)^{-1-2k} e^{i k \pi} \pi^{1+2k}\right)}{(1+2k)!} \right)$$

**Integral representations:**

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = 1 + \int_0^1 -\frac{125}{2} \pi \left( i \cos\left(\frac{125 \pi t}{2}\right) + \sin\left(\frac{125 \pi t}{2}\right) \right) dt$$

$$\cos\left(\frac{5}{2}(\pi 5^2)\right) - i \sin\left(\frac{5}{2}(\pi 5^2)\right) = \int_0^1 \left( -\frac{125}{2} i \pi \cos\left(\frac{125 \pi t}{2}\right) - 62 \pi \sin\left(\pi \left(\frac{1}{2} + 62 t\right)\right) \right) dt$$



1.00179831923214082196718018992585437697004399881740171... +  
 0.00409799452422547796373385507184309419682441399448918422... *i*

**Polar coordinates:**

$r \approx 1.00181$  (radius),  $\theta \approx 0.234375^\circ$  (angle)

1.00181 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{\frac{2\pi}{5}}}{\sqrt{\varphi\sqrt{5} - \varphi}} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}}$$

$\approx 1.0018674362$

**Alternate forms:**

$${}^{384}\sqrt{2} \cos\left(\frac{\pi}{768}\right) + i {}^{384}\sqrt{2} \sin\left(\frac{\pi}{768}\right)$$

$${}^{384}\sqrt{2} e^{(i\pi)/768}$$

**Alternative representations:**

$$\frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cosh\left(\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5\pi 5^2}{2}\right) \right)}}$$

$$\frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cosh\left(-\frac{5}{2} i \pi 5^2\right) + i \cos\left(\frac{\pi}{2} + \frac{5\pi 5^2}{2}\right) \right)}}$$

$$\frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cosh\left(-\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5\pi 5^2}{2}\right) \right)}}$$

**Series representations:**

$$\frac{1}{{}^{384}\sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{{}^{384}\sqrt{2}}{{}^{384}\sqrt{\sum_{k=0}^{\infty} \left( -2 (-1)^k i J_{1+2k}\left(\frac{125\pi}{2}\right) + \frac{\left(-\frac{15625}{4}\right)^k \pi^{2k}}{(2k)!} \right)}}$$

$$\frac{1}{\sqrt[384]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{\sqrt[384]{2}}$$

$$\frac{1}{\sqrt[384]{\sum_{k=0}^{\infty} \left( -2 (-1)^k i J_{1+2k}\left(\frac{125\pi}{2}\right) + \frac{(-1)^{1+k} 62^{1+2k} \pi^{1+2k}}{(1+2k)!} \right)}} = \frac{\sqrt[384]{2}}{\sqrt[384]{\sum_{k=0}^{\infty} \left( \frac{\left(-\frac{15625}{4}\right)^k \pi^{2k}}{(2k)!} - \frac{i \left(\frac{2}{125}\right)^{-1-2k} e^{i k \pi} \pi^{1+2k}}{(1+2k)!} \right)}}$$

**Integral representations:**

$$\frac{1}{\sqrt[384]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{\sqrt[192]{2}}{\sqrt[384]{2 + \int_0^1 -125\pi \left( i \cos\left(\frac{125\pi t}{2}\right) + \sin\left(\frac{125\pi t}{2}\right) \right) dt}}$$

$$\frac{1}{\sqrt[384]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{\sqrt[192]{2}}{\sqrt[384]{\int_0^{1-\pi} \left( 125 i \cos\left(\frac{125\pi t}{2}\right) + 124 \sin\left(\pi\left(\frac{1}{2} + 62 t\right)\right) \right) dt}}$$

$$\frac{1}{\sqrt[384]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{\sqrt[384]{2}}{\sqrt[384]{\int_{-\mathcal{A}\infty+\gamma}^{\mathcal{A}\infty+\gamma} \frac{e^{-(15625\pi^2)/(16s)+s(-125i\pi+4s)\sqrt{\pi}}}{8\pi s^{3/2}\mathcal{A}} ds}} \quad \text{for } \gamma > 0$$

**Half-argument formula:**

$$\frac{1}{\sqrt[384]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \left( \sqrt[384]{2} \right) /$$

$$\left( \left( (-1)^{1+[\text{Re}(125\pi)/(2\pi)]} i \sqrt{\frac{1}{2} (1 - \cos(125\pi))} \left( 1 - \left( 1 + (-1)^{[-\text{Re}(125\pi)/(2\pi)] + [\text{Re}(125\pi)/(2\pi)]} \right) \right) \right. \right.$$

$$\left. \left. \theta(-\text{Im}(125\pi)) + (-1)^{[\pi + \text{Re}(125\pi)/(2\pi)]} \sqrt{\frac{1}{2} (1 + \cos(125\pi))} \right. \right.$$

$$\left. \left. \left( 1 - \left( 1 + (-1)^{[-\pi + \text{Re}(125\pi)/(2\pi)] + [\pi + \text{Re}(125\pi)/(2\pi)]} \right) \theta(-\text{Im}(125\pi)) \right) \right)^{\wedge} (1/384)$$





$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Alternate forms:**

$$\sqrt[32]{\frac{1}{2} - \frac{i}{2}}$$

$$\frac{\cos\left(\frac{\pi}{128}\right)}{\sqrt[64]{2}} - \frac{i \sin\left(\frac{\pi}{128}\right)}{\sqrt[64]{2}}$$

$$- \frac{e^{(127i\pi)/128}}{\sqrt[64]{2}}$$

**Minimal polynomial:**

$$2x^{64} - 2x^{32} + 1$$

**Alternative representations:**

$$\frac{1}{\sqrt[64]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{\sqrt[64]{\frac{1}{2} \left( \cosh\left(\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5\pi 5^2}{2}\right) \right)}}$$

$$\frac{1}{\sqrt[64]{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}} = \frac{1}{\sqrt[64]{\frac{1}{2} \left( \cosh\left(-\frac{5}{2} i \pi 5^2\right) + i \cos\left(\frac{\pi}{2} + \frac{5\pi 5^2}{2}\right) \right)}}$$

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cosh\left(-\frac{5}{2} i \pi 5^2\right) - i \cos\left(\frac{\pi}{2} - \frac{5\pi 5^2}{2}\right) \right)}}}$$

### Series representations:

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{64 \sqrt{\sum_{k=0}^{\infty} \left( -2 (-1)^k i J_{1+2k}\left(\frac{125\pi}{2}\right) + \frac{\left(-\frac{15625}{4}\right)^k \pi^{2k}}{(2k)!} \right)}}{64 \sqrt{2}}$$

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{64 \sqrt{\sum_{k=0}^{\infty} \left( -2 (-1)^k i J_{1+2k}\left(\frac{125\pi}{2}\right) + \frac{(-1)^{1+k} 62^{1+2k} \pi^{1+2k}}{(1+2k)!} \right)}}{64 \sqrt{2}}$$

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{64 \sqrt{\sum_{k=0}^{\infty} \left( \frac{\left(-\frac{15625}{4}\right)^k \pi^{2k}}{(2k)!} - \frac{i \left(\left(\frac{2}{125}\right)^{-1-2k} e^{i k \pi} \pi^{1+2k}\right)}{(1+2k)!} \right)}}{64 \sqrt{2}}$$

### Integral representations:

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{64 \sqrt{2 + \int_0^1 -125 \pi \left( i \cos\left(\frac{125\pi t}{2}\right) + \sin\left(\frac{125\pi t}{2}\right) \right) dt}}{32 \sqrt{2}}$$

$$\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right) \right)}}} = \frac{64 \sqrt{\int_0^1 -\pi \left( 125 i \cos\left(\frac{125\pi t}{2}\right) + 124 \sin\left(\pi \left(\frac{1}{2} + 62 t\right)\right) \right) dt}}{32 \sqrt{2}}$$

$$\frac{\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right)\right)}}}}{1} = \frac{64 \sqrt{\frac{\sqrt{\pi}}{\pi \mathcal{A}} \int_{-\mathcal{A} \infty + \gamma}^{\mathcal{A} \infty + \gamma} \frac{e^{-(15625 \pi^2)/(16s) + s(-125i\pi + 4s)}}{s^{3/2}} ds}}{16\sqrt{2}} \quad \text{for } \gamma > 0$$

### Half-argument formula:

$$\frac{\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right)\right)}}}}{1} = \frac{1}{64\sqrt{2}}$$

$$\left( (-1)^{1 + [\text{Re}(125\pi)/(2\pi)]} i \sqrt{\frac{1}{2} (1 - \cos(125\pi))} \left( 1 - \left( 1 + (-1)^{[-\text{Re}(125\pi)/(2\pi)] + [\text{Re}(125\pi)/(2\pi)]} \right) \theta(-\text{Im}(125\pi)) \right) + (-1)^{[\pi + \text{Re}(125\pi)/(2\pi)]} \sqrt{\frac{1}{2} (1 + \cos(125\pi))} \left( 1 - \left( 1 + (-1)^{[-\pi + \text{Re}(125\pi)/(2\pi)] + [\pi + \text{Re}(125\pi)/(2\pi)]} \right) \theta(-\text{Im}(125\pi)) \right) \right)^{\wedge} (1/64)$$

### Multiple-argument formulas:

$$\frac{\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right)\right)}}}}{1} = 64 \sqrt{-\frac{1}{2} + \cos^2\left(\frac{125\pi}{4}\right) - i \left( \cos\left(\frac{125\pi}{4}\right) \sin\left(\frac{125\pi}{4}\right) \right)}$$

$$\frac{\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right)\right)}}}}{1} = 64 \sqrt{\frac{1}{2} - i \left( \cos\left(\frac{125\pi}{4}\right) \sin\left(\frac{125\pi}{4}\right) \right) - \sin^2\left(\frac{125\pi}{4}\right)}$$

$$\frac{\frac{1}{\frac{1}{64 \sqrt{\frac{1}{2} \left( \cos\left(\frac{5\pi 5^2}{2}\right) - i \sin\left(\frac{5\pi 5^2}{2}\right)\right)}}}}{1} = 64 \sqrt{-\frac{1}{2} + \cos^2\left(\frac{125\pi}{4}\right) - \frac{3}{2} i \sin\left(\frac{125\pi}{6}\right) + 2 i \sin^3\left(\frac{125\pi}{6}\right)}$$

Now, we have that:

For odd  $p$ , the condition (4.27) can be solved by  $k = \frac{p+1}{2}$

$$Z[\pi, K] \rightarrow Z[\pi, K] \exp\left(2\pi i \frac{1-2k}{p} \int K\right).$$

For  $p = 5$ ,  $k = 3$  and  $K = 8$ , (where 8 is a Fibonacci numbers), from

$\exp(2\pi i \cdot i \cdot ((1-6)/5) \int 8x dx)$  from which

$\exp(-((2\pi i \cdot i \cdot (1-6)/5) \int 8x dx))$

we obtain:

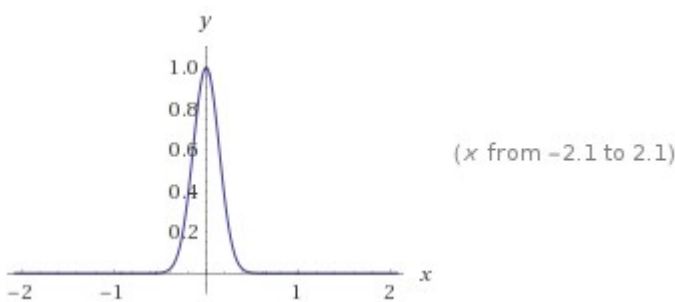
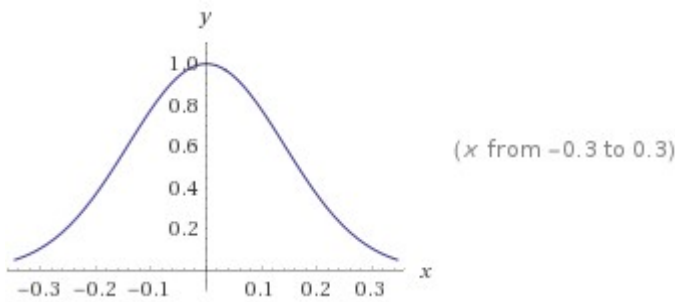
**Input:**

$$\exp\left(-\left(-2\pi \times \frac{1-6}{5} \int 8x dx\right)\right)$$

**Exact result:**

$$e^{-8\pi x^2}$$

**Plots:**



**Series expansion of the integral at  $x = 0$ :**

$$1 - 8\pi x^2 + 32\pi^2 x^4 + O(x^5)$$

(Taylor series)

**Indefinite integral:**

$$\exp\left(-\frac{1}{5} \left(-2\pi(1-6) \int 8x dx\right)\right) = e^{-8\pi x^2 + \text{constant}}$$

From the solution

$$e^{-8\pi x^2}$$

For  $x = 1$ , we obtain:

$$e^{(-8\pi \cdot 1^2)}$$

**Input:**

$$e^{-8\pi \times 1^2}$$

**Exact result:**

$$e^{-8\pi}$$

**Decimal approximation:**

$$1.2161556709409308397405550475258851771631170167577743... \times 10^{-11}$$

$$1.21615567094093... * 10^{-11}$$

**Property:**

$e^{-8\pi}$  is a transcendental number

**Alternative representations:**

$$e^{-8\pi \cdot 1^2} = e^{-1440^\circ}$$

$$e^{-8\pi \cdot 1^2} = e^{8i \log(-1)}$$

$$e^{-8\pi \cdot 1^2} = \exp^{-8\pi \cdot 1^2}(z) \text{ for } z = 1$$

**Series representations:**

$$e^{-8\pi \cdot 1^2} = e^{-32 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

$$e^{-8\pi \cdot 1^2} = \left( \sum_{k=0}^{\infty} \frac{1}{k!} \right)^{-8\pi}$$

$$e^{-8\pi \cdot 1^2} = \left( \frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}} \right)^{-8\pi}$$

**Integral representations:**

$$e^{-8\pi 1^2} = e^{-32 \int_0^1 \sqrt{1-t^2} dt}$$

$$e^{-8\pi 1^2} = e^{-16 \int_0^1 1/\sqrt{1-t^2} dt}$$

$$e^{-8\pi 1^2} = e^{-16 \int_0^\infty 1/(1+t^2) dt}$$

$$(89 \cdot 10^{-8}) / (e^{-8\pi 1^2}) + 322 - 11$$

Where 89 is a Fibonacci number, while 11 and 322 are Lucas numbers

**Input interpretation:**

$$\frac{89 \times 10^{-8}}{e^{-8\pi \times 1^2}} + 322 - 11$$

**Result:**

$$311 + \frac{89 e^{8\pi}}{100\,000\,000}$$

**Decimal approximation:**

73492.42087117954579472054629689511758061969378596316393666...

73492.42087

**Property:**

$311 + \frac{89 e^{8\pi}}{100\,000\,000}$  is a transcendental number

**Alternate form:**

$$\frac{31\,100\,000\,000 + 89 e^{8\pi}}{100\,000\,000}$$

Thence, we have the following mathematical connection:

$$\begin{aligned} & \left( 311 + \frac{89 e^{8\pi}}{100\,000\,000} \right) = 73492.42087 \Rightarrow \\ \Rightarrow & -3927 + 2 \left( \sqrt[13]{ N \exp \left[ \int d\hat{\sigma} \left( -\frac{1}{4u^2} \mathbf{P}_i D \mathbf{P}_i \right) \right] |Bp\rangle_{\text{NS}} + \int [d\mathbf{X}^\mu] \exp \left\{ \int d\hat{\sigma} \left( -\frac{1}{4v^2} D \mathbf{X}^\mu D^2 \mathbf{X}^\mu \right) \right\} |X^\mu, \mathbf{X}^i = 0\rangle_{\text{NS}} } \right) = \\ & -3927 + 2 \sqrt[13]{ 2.2983717437 \times 10^{59} + 2.0823329825883 \times 10^{59} } \\ & = 73490.8437525 \dots \Rightarrow \end{aligned}$$

$$\begin{aligned} & \Rightarrow \left( A(r) \times \frac{1}{B(r)} \left( -\frac{1}{\phi(r)} \right) \times \frac{1}{e^{\Lambda(r)}} \right) \Rightarrow \\ \Rightarrow & \left( -0.000029211892 \times \frac{1}{0.0003644621} \left( -\frac{1}{0.0005946833} \right) \times \frac{1}{0.00183393} \right) = \\ = & 73491.78832548118710549159572042220548025195726563413398700 \dots \\ = & 73491.7883254 \dots \Rightarrow \end{aligned}$$

$$\begin{aligned} & \left( I_{21} \ll \int_{-\infty}^{+\infty} \exp \left( -\left( \frac{t}{H} \right)^2 \right) \left| \sum_{\lambda \leq p^{1-\varepsilon_2}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)} \right|^2 dt \ll \right. \\ & \left. \ll H \left\{ \left( \frac{4}{\varepsilon_2 \log T} \right)^{2r} (\log T) (\log X)^{-2\beta} + (\varepsilon_2^{-2r} (\log T)^{-2r} + \varepsilon_2^{-r} h_1^r (\log T)^{-r} \right) T^{-\varepsilon_1} \right\} \right) \\ & / (26 \times 4)^2 - 24 = \left( \frac{7.9313976505275 \times 10^8}{(26 \times 4)^2 - 24} \right) = 73493.30662 \dots \end{aligned}$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of  $u \rightarrow \infty$ , with the ratio concerning the general asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

Now, we have also that:

$$(((e^{(-8 \pi^2)})))^{1/4096}$$

**Input:**

$$\sqrt[4096]{e^{-8 \pi^2}}$$

**Exact result:**

$$e^{-\pi/512}$$

**Decimal approximation:**

$$0.993882863181447312422244929104462434670072979619464140596\dots$$

0.993882863181... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

$$\frac{1 + \sqrt[5]{\sqrt{\varphi^5 \sqrt[4]{5^3} - 1}}}{\sqrt{5}} - \varphi + 1$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Property:**

$e^{-\pi/512}$  is a transcendental number

$$e^{-\pi/512} e^0 \approx 0.993883 \text{ (real, principal root)}$$

$$e^{-\pi/512} e^{(i \pi)/2048} \approx 0.9938817 + 0.0015246 i$$

$$e^{-\pi/512} e^{(i \pi)/1024} \approx 0.9938782 + 0.0030492 i$$



$$e^{-\pi/512} e^{(3i\pi)/2048} \approx 0.9938723 + 0.0045738 i$$

$$e^{-\pi/512} e^{(i\pi)/512} \approx 0.9938642 + 0.0060984 i$$

### Alternative representations:

$$4096\sqrt[4096]{e^{-8\pi^2}} = 4096\sqrt[4096]{e^{-1440^\circ}}$$

$$4096\sqrt[4096]{e^{-8\pi^2}} = 4096\sqrt[4096]{e^{8i \log(-1)}}$$

$$4096\sqrt[4096]{e^{-8\pi^2}} = 4096\sqrt[4096]{\exp^{-8\pi^2}(z)} \text{ for } z = 1$$

### Series representations:

$$4096\sqrt[4096]{e^{-8\pi^2}} = e^{-1/128 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

$$4096\sqrt[4096]{e^{-8\pi^2}} = \left( \sum_{k=0}^{\infty} \frac{1}{k!} \right)^{-\pi/512}$$

$$4096\sqrt[4096]{e^{-8\pi^2}} = \left( \frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}} \right)^{-\pi/512}$$

### Integral representations:

$$4096\sqrt[4096]{e^{-8\pi^2}} = e^{-1/128 \int_0^1 \sqrt{1-t^2} dt}$$

$$4096\sqrt[4096]{e^{-8\pi^2}} = e^{-1/256 \int_0^1 1/\sqrt{1-t^2} dt}$$

$$4096 \sqrt{e^{-8\pi^2}} = e^{-1/256 \int_0^\infty 1/(1+t^2) dt}$$

From which, we obtain:

$$2 * (((\log \text{base } 0.993882863181447 (((e^{(-8\pi^2)}))))))^{1/2} - 3$$

where 3 is a Fibonacci number

**Input interpretation:**

$$2 \sqrt{\log_{0.993882863181447}(e^{-8\pi^2})} - 3$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

125.0000000000...

125 result equal to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$2 \sqrt{\log_{0.9938828631814470000}(e^{-8\pi^2})} - 3 = -3 + 2 \sqrt{\frac{\log(e^{-8\pi})}{\log(0.9938828631814470000)}}$$

**Series representations:**

$$2 \sqrt{\log_{0.9938828631814470000}(e^{-8\pi^2})} - 3 = -3 + 2 \sqrt{-\frac{\sum_{k=1}^{\infty} \frac{(-1)^k (-1+e^{-8\pi})^k}{k}}{\log(0.9938828631814470000)}}$$

$$2 \sqrt{\log_{0.9938828631814470000}(e^{-8\pi^2})} - 3 = -3 + 2 \sqrt{\left( -1.0000000000000000 \log(e^{-8\pi}) \right. \\ \left. \left( 162.97517305270092 + \sum_{k=0}^{\infty} (-0.0061171368185530000)^k G(k) \right) \right)}$$

for  $\left( G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

$$2\sqrt{\log_{0.9938828631814470000}(e^{-8\pi^2})} - 3 = -3 + 2\sqrt{\left(-1.0000000000000000 \log(e^{-8\pi})\right. \\ \left. \left(162.97517305270092 + \sum_{k=0}^{\infty} (-0.0061171368185530000)^k G(k)\right)\right)} \\ \text{for } \left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j}\right)$$

Now, we have that:

$$\theta = \pi$$

Considering

$$q^*A \in \Omega^1(X).$$

equal to 64, we obtain, from the following expression:

$$\exp\left(\frac{1}{2\pi\sqrt{-1}} \int_X \theta q^*A\right), \quad (7.2)$$

$\exp(\frac{1}{2\pi\sqrt{-1}} \int (64\pi)x dx)$

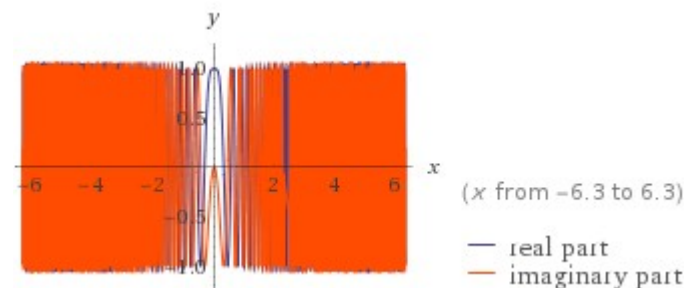
**Input:**

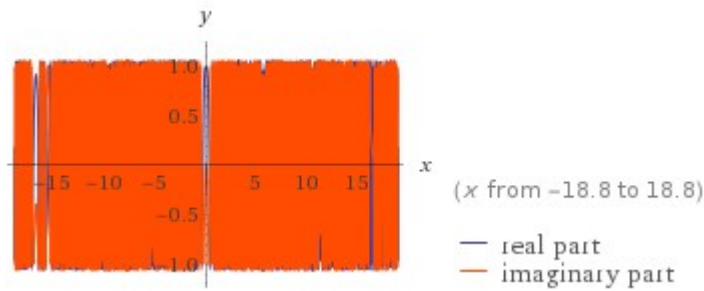
$$\exp\left(\frac{1}{2\pi\sqrt{-1}} \int (64\pi)x dx\right)$$

**Exact result:**

$$e^{-16ix^2}$$

**Plots:**





**Alternate form assuming x is real:**

$$\cos(16x^2) - i \sin(16x^2)$$

**Series expansion of the integral at x = 0:**

$$1 - 16ix^2 - 128x^4 + O(x^5)$$

(Taylor series)

**Indefinite integral:**

$$\exp\left(\frac{1}{2\pi\sqrt{-1}} \int (64\pi)x dx\right) = e^{-16ix^2 + \text{constant}}$$

From  $e^{-16ix^2}$ , for  $x = 2$  and multiplying by  $-1$ , we obtain:

$$e^{(-16 * -2^2)}$$

**Input:**

$$e^{-16 \times (-1) \times 2^2}$$

**Exact result:**

$$e^{64}$$

**Decimal approximation:**

$$6.2351490808116168829092387089284697448313918462357999... \times 10^{27}$$

$$6.23514908081... * 10^{27}$$

**Property:**

$e^{64}$  is a transcendental number

**Alternative representation:**

$$e^{-16(-1)2^2} = \exp^{-16(-1)2^2}(z) \text{ for } z = 1$$

**Series representations:**

$$e^{-16(-1)2^2} = \sum_{k=0}^{\infty} \frac{64^k}{k!}$$

$$e^{-16(-1)2^2} = \left( \sum_{k=0}^{\infty} \frac{1}{k!} \right)^{64}$$

$$e^{-16(-1)2^2} = \frac{1}{\left( \sum_{k=0}^{\infty} \frac{(-1)^k}{k!} \right)^{64}}$$

### Integral representation:

$$(1+z)^{\alpha} = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-\alpha-s)}{z^s} ds}{(2\pi i)\Gamma(-\alpha)} \quad \text{for } (0 < \gamma < -\text{Re}(\alpha) \text{ and } |\arg(z)| < \pi)$$

From which:

$$1/((e^{(-16 * -2^2)}))^{1/4096}$$

**Input:**

$$\frac{1}{\sqrt[4096]{e^{-16 \times (-1) \times 2^2}}}$$

**Exact result:**

$$\frac{1}{\sqrt[64]{e}}$$

**Decimal approximation:**

0.984496437005408405986988829697020369707861003180350567476...

0.984496437.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Property:**

$\frac{1}{\sqrt[64]{e}}$  is a transcendental number

**Alternative representation:**

$$\frac{1}{\sqrt[4096]{e^{-16(-1)2^2}}} = \frac{1}{\sqrt[4096]{\exp^{-16(-1)2^2}(z)}} \text{ for } z = 1$$

**Series representations:**

$$\frac{1}{\sqrt[4096]{e^{-16(-1)2^2}}} = \frac{1}{\sqrt[64]{\sum_{k=0}^{\infty} \frac{1}{k!}}}$$

$$\frac{1}{\sqrt[4096]{e^{-16(-1)2^2}}} = \frac{1}{\sqrt[64]{\sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!}}}$$

$$\frac{1}{\sqrt[4096]{e^{-16(-1)2^2}}} = \frac{\sqrt[64]{2}}{\sqrt[64]{\sum_{k=0}^{\infty} \frac{1+k}{k!}}}$$

and again:

$$2 * \sqrt{\left( \left( \left( \left( \left( \log \text{base } 0.984496437 \left( \left( \left( \left( \left( \left( \frac{1}{\left( e^{-16 * -2^2} \right)} \right)} \right)} \right)} \right)} \right)} \right)} \right)} \right)} \right)} \right)} - 3$$

where 3 is a Fibonacci number

**Input interpretation:**

$$2 \sqrt{\log_{0.984496437} \left( \frac{1}{e^{-16 \cdot (-1) \cdot 2^2}} \right)} - 3$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

125.0000...

125 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$2 \sqrt{\log_{0.984496} \left( \frac{1}{e^{-16(-1)2^2}} \right)} - 3 = -3 + 2 \sqrt{\frac{\log\left(\frac{1}{e^{64}}\right)}{\log(0.984496)}}$$

**Series representations:**

$$2 \sqrt{\log_{0.984496} \left( \frac{1}{e^{-16(-1)2^2}} \right)} - 3 = -3 + 2 \sqrt{\frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{e^{64}}\right)^k}{k}}{\log(0.984496)}}$$

$$2 \sqrt{\log_{0.984496} \left( \frac{1}{e^{-16(-1)2^2}} \right)} - 3 = -3 + 2 \sqrt{-1 + \log_{0.984496} \left( \frac{1}{e^{64}} \right) \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left(-1 + \log_{0.984496} \left( \frac{1}{e^{64}} \right)\right)^{-k}}$$

$$2 \sqrt{\log_{0.984496} \left( \frac{1}{e^{-16(-1)2^2}} \right)} - 3 = -3 + 2 \sqrt{-1 + \log_{0.984496} \left( \frac{1}{e^{64}} \right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-1 + \log_{0.984496} \left( \frac{1}{e^{64}} \right)\right)^{-k} \left(-\frac{1}{2}\right)_k}{k!}}$$

We have also:

$$((e^{(-16 * -2^2)})^{1/13})$$

**Input:**

$$\sqrt[13]{e^{-16 \times (-1) \times 2^2}}$$

**Exact result:**

$$e^{64/13}$$

**Decimal approximation:**

137.4248088873354879354828828258476149244161631868758634725...

137.42480888... result very near to the average rest mass of the two Pion mesons that is 137.2733

**Property:**

$e^{64/13}$  is a transcendental number

**All 13th roots of  $e^{64}$ :**

$$e^{64/13} e^{0} \approx 137.42 \text{ (real, principal root)}$$

$$e^{64/13} e^{(2i\pi)/13} \approx 121.68 + 63.86i$$

$$e^{64/13} e^{(4i\pi)/13} \approx 78.07 + 113.10i$$

$$e^{64/13} e^{(6i\pi)/13} \approx 16.56 + 136.42i$$

$$e^{64/13} e^{(8i\pi)/13} \approx -48.73 + 128.49i$$

**Alternative representation:**

$$\sqrt[13]{e^{-16(-1)2^2}} = \sqrt[13]{\exp^{-16(-1)2^2}(z)} \text{ for } z = 1$$

**Series representations:**

$$\sqrt[13]{e^{-16(-1)2^2}} = \left( \sum_{k=0}^{\infty} \frac{1}{k!} \right)^{64/13}$$



$$\sqrt[13]{e^{-16(-1)2^2}} = \left( \sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{64/13}$$

$$\sqrt[13]{e^{-16(-1)2^2}} = \left( \frac{\sum_{k=0}^{\infty} \frac{-1+k+z}{k!}}{z} \right)^{64/13}$$

**Integral representation:**

$$(1+z)^\alpha = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-\alpha-s)}{z^s} ds}{(2\pi i)\Gamma(-\alpha)} \text{ for } (0 < \gamma < -\text{Re}(\alpha) \text{ and } |\arg(z)| < \pi)$$

We can to obtain 125 also as follows:

$$((e^{(-16 * -2^2)})^{1/13} - 12$$

**Input:**

$$\sqrt[13]{e^{-16 \times (-1) \times 2^2}} - 12$$

**Exact result:**

$$e^{64/13} - 12$$

**Decimal approximation:**

125.4248088873354879354828828258476149244161631868758634725...

125.42480888... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

**Property:**

$-12 + e^{64/13}$  is a transcendental number

**Alternative representation:**

$$\sqrt[13]{e^{-16(-1)2^2}} - 12 = \sqrt[13]{\exp^{-16(-1)2^2}(z)} - 12 \text{ for } z = 1$$

**Series representations:**

$$\sqrt[13]{e^{-16(-1)2^2}} - 12 = -12 + \left( \sum_{k=0}^{\infty} \frac{1}{k!} \right)^{64/13}$$

$$\sqrt[13]{e^{-16(-1)2^2}} - 12 = -12 + \left( \sum_{k=0}^{\infty} \frac{(-1+k)^2}{k!} \right)^{64/13}$$

$$\sqrt[13]{e^{-16(-1)2^2}} - 12 = -12 + \left( \frac{\sum_{k=0}^{\infty} \frac{-1+k+z}{k!}}{z} \right)^{64/13}$$

Now, we have this further interpretation of the previous formulas.

We would now like to reinterpret the jump (3.13) in terms of an anomaly involving the fermion mass viewed now as a background field. Analogous to our examples in quantum mechanics, we introduce a new partition function  $\tilde{Z}[m, g]$ , which depends on an extension of the mass  $m$  and metric  $g$  into a four-manifold  $Y$  with boundary  $X$ :

$$\tilde{Z}[m, g] = Z[m, g] \exp \left( -i \int_Y \rho(m) dC S_{\text{grav}} \right) = Z[m, g] \exp \left( -\frac{i}{192\pi} \int_Y \rho(m) \text{Tr}(R \wedge R) \right), \tag{3.15}$$

where above  $\rho(m)$  satisfies the same criteria as in the anomaly in the fermion quantum mechanics theory (3.7). (And as in the discussion there, in the free fermion theory it is natural to take  $\rho(m)$  a Heaviside theta-function.) This partition function now retains the

From eq. (3.15), converting the value of the electron mass to temperature (Kelvin), bearing in mind that the electron is a fermion, we obtain:

$$0.5109989500015 \text{ MeV}/c^2$$

convert

0.5109989500015 MeV/ $k_B$  (megaelectronvolts per Boltzmann constant) to kelvins

$$5.92989657539 \times 10^9 \text{ K (kelvins)}$$

and the formula:

$$Z = \text{tr}(e^{-\beta \hat{H}})$$



**Input interpretation:**

$$\exp\left(-\left(\frac{1}{1.38064852 \times 10^{-23} \times 5.92989657539 \times 10^9} \times 4.4 \times 10^{-18}\right)\right)$$

**Result:**

0.9999462584...

$$0.9999462584... = H \approx 1$$

$$\exp(\frac{-i}{192\pi} \text{Tr}(\int \frac{1}{2} \times 5.92989657539 \times 10^9 x dx))$$

**Input interpretation:**

$$\exp\left(-\frac{i}{192\pi} \text{Tr}\left[\int\left(\frac{1}{2} \times 5.92989657539 \times 10^9\right) x dx\right]\right)$$

*i* is the imaginary unit

**Result:**

$$e^{-i \text{Tr}[1.48247414385 \times 10^9 x^2]/(192\pi)}$$

**Series expansion of the integral at x = 0:**

$$e^{-i \text{Tr}[0]/(192\pi)} - 2.45774049999 \times 10^6 i x^2 e^{-i \text{Tr}[0]/(192\pi)} \text{Tr}'(0) + x^4 e^{-i \text{Tr}[0]/(192\pi)} (-3.02024418265 \times 10^{12} \text{Tr}'(0)^2 - 1.82176837176 \times 10^{15} i \text{Tr}''(0)) + O(x^5)$$

(Taylor series)

$$\exp(-i*(1.48247414385e+9)/(192\pi))$$

**Input interpretation:**

$$\exp\left(-i \times \frac{1.48247414385 \times 10^9}{192\pi}\right)$$

*i* is the imaginary unit

**Result:**

-0.952193... +

0.305499... *i*

**Polar coordinates:**

*r* = 1.00000 (radius), *θ* = 162.212° (angle)

$$(-0.952193+0.305499)i$$

**Input interpretation:**

$$(-0.952193 + 0.305499) i$$

$i$  is the imaginary unit

**Result:**

$$-0.646694 i$$

**Polar coordinates:**

$$r = 0.646694 \text{ (radius), } \theta = -90^\circ \text{ (angle)}$$

$$0.646694$$

Note that inserting the Trace within the integral, we obtain the same result. Indeed:

$$\exp(\frac{-i}{192\pi} \int (\frac{1}{2} \text{Tr}[5.92989657539 \times 10^9] x) dx)$$

**Input interpretation:**

$$\exp\left(-\frac{i}{192\pi} \int \left(\frac{1}{2} \text{Tr}[5.92989657539 \times 10^9]\right) x dx\right)$$

$i$  is the imaginary unit

**Result:**

$$e^{-\frac{i x^2 \text{Tr}[5.92989657539 \times 10^9]}{768\pi}}$$

**Series expansion of the integral at  $x = 0$ :**

$$1 - \frac{i x^2 \text{Tr}[5.92989657539 \times 10^9]}{768\pi} - \frac{x^4 \text{Tr}[5.92989657539 \times 10^9]^2}{1179648\pi^2} + O(x^5)$$

(Taylor series)

**Indefinite integral assuming all variables are real:**

$$\frac{(4 - 4i) \sqrt{6} \pi \operatorname{erf}\left(\frac{\left(\frac{1}{16} + \frac{i}{16}\right)x \sqrt{\text{Tr}[5.92989657539 \times 10^9]}}{\sqrt{6\pi}}\right)}{\sqrt{\text{Tr}[5.92989657539 \times 10^9]}} + \text{constant}$$

$$\exp(\frac{-i(5.92989657539e+9)}{768\pi})$$

**Input interpretation:**

$$\exp\left(-\frac{i \times 5.92989657539 \times 10^9}{768\pi}\right)$$

$i$  is the imaginary unit

**Result:**

$$-0.952194... + 0.305495... i$$

**Polar coordinates:**

$$r = 1.00000 \text{ (radius)}, \theta = 162.212^\circ \text{ (angle)}$$

$$(-0.952194 + 0.305495)i$$

**Input interpretation:**

$$(-0.952194 + 0.305495) i$$

$i$  is the imaginary unit

**Result:**

$$-0.646699 i$$

**Polar coordinates:**

$$r = 0.646699 \text{ (radius)}, \theta = -90^\circ \text{ (angle)}$$

$$0.646699 \text{ (or } 0.646665 \text{ multiplying the equation by } 0.9999462584... = H)$$

From which, we obtain:

$$((( -0.952194 + 0.305495)i ))^{1/64}$$

**Input interpretation:**

$$\sqrt[64]{(-0.952194 + 0.305495) i}$$

$i$  is the imaginary unit

**Result:**

$$0.99291347... - 0.024374657... i$$

**Polar coordinates:**

$$r = 0.993213 \text{ (radius)}, \theta = -1.40625^\circ \text{ (angle)}$$

$$0.993213$$

result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

We have also the following result:

**Input interpretation:**

$$-\pi i + 2 i \log_{0.993213}(-(-0.952194 + 0.305495))$$

$\log_b(x)$  is the base-  $b$  logarithm

$i$  is the imaginary unit

**Result:**

$$124.866... i$$

**Polar coordinates:**

$$r = 124.866 \text{ (radius), } \theta = 90^\circ \text{ (angle)}$$

124.866 result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$-i\pi + 2 i \log_{0.993213}(-(-0.952194 + 0.305495)) = -i\pi + \frac{2 i \log(0.646699)}{\log(0.993213)}$$

**Series representations:**

$$-i\pi + 2 i \log_{0.993213}(-(-0.952194 + 0.305495)) = -i\pi - \frac{2 i \sum_{k=1}^{\infty} \frac{(-1)^k (-0.353301)^k}{k}}{\log(0.993213)}$$

$$\begin{aligned}
& -i\pi + 2i \log_{0.993213}(-(-0.952194 + 0.305495)) = \\
& -i\pi - 293.681i \log(0.646699) - 2i \log(0.646699) \sum_{k=0}^{\infty} (-0.006787)^k G(k) \\
& \text{for } \left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)
\end{aligned}$$

From:

[https://www.wired.it/scienza/lab/2019/11/20/quinta-forza-universo-bosone/?refresh\\_ce=](https://www.wired.it/scienza/lab/2019/11/20/quinta-forza-universo-bosone/?refresh_ce=)

*In recent years Hungarian researchers have sought further evidence of the new particle. And now - in an article published in arXiv and not yet subjected to peer review - they claim to have found them, this time observing the change of state of an excited helium nucleus: pairs of electrons and positrons separate at an angle different from that which theoretical models predict, around 115°. According to the authors the anomaly could be explained by the production by the helium atom of a different boson from all those we know, of short duration and with a mass of slightly less than 17 megaelectronvolts. Hence the name of X17. Of course it is very suggestive that several experiments aimed at finding out more about dark matter focused precisely on the existence of a hypothetical 17 megaelectronvolts (precisely 16.84 MeV - author's note) particle.*

From:

**New evidence supporting the existence of the hypothetic X17 particle**

*A.J. Krasznahorkay, M. Csatos, L. Csige, J. Gulyas, M. Koszta, B. Szihalmi, and J. Timar*

Institute of Nuclear Research (Atomki), P.O. Box 51, H-4001 Debrecen, Hungary

*D.S. Firak, A. Nagy, and N.J. Sas*

University of Debrecen, 4010 Debrecen, PO Box 105, Hungary

*A. Krasznahorkay*

CERN, Geneva, Switzerland and

Institute of Nuclear Research, (Atomki), P.O. Box 51, H-4001 Debrecen, Hungary

<https://arxiv.org/abs/1910.10459v1>

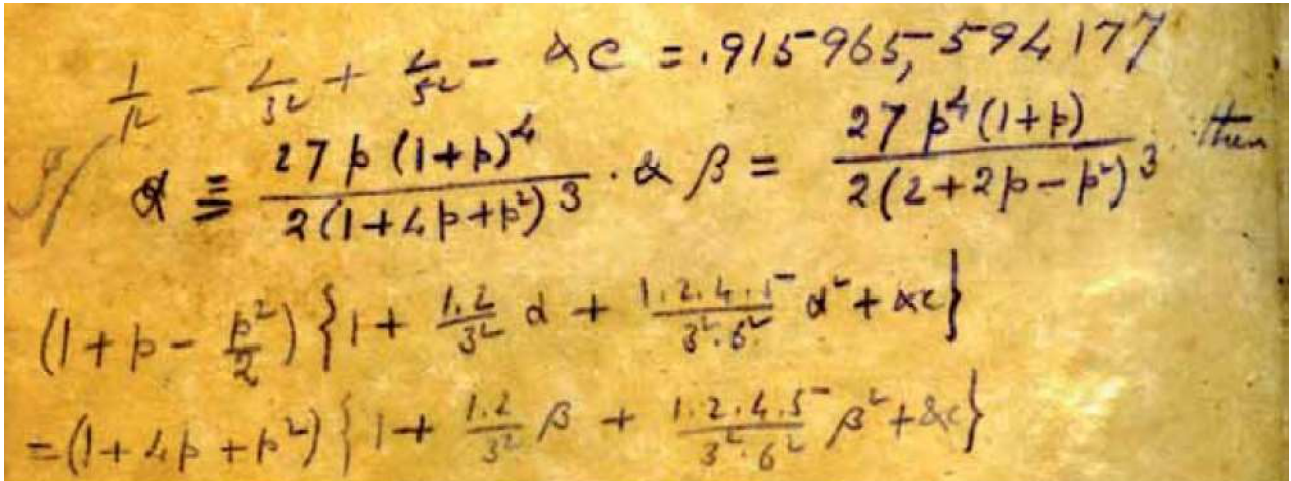
We observed electron-positron pairs from the electro-magnetically forbidden M0 transition depopulating the 21.01 MeV  $0^-$  state in  $^4\text{He}$ . A peak was observed in their  $e^+e^-$  angular correlations at  $115^\circ$  with  $7.2\sigma$  significance, and could be described by assuming the creation and subsequent decay of a light particle with mass of  $m_{\text{X}}c^2 = 16.84 \pm 0.16(\text{stat}) \pm 0.20(\text{syst})$  MeV and  $\Gamma_{\text{X}} = 3.9 \times 10^{-5}$  eV. According to the mass, it is likely the same X17 particle, which we recently suggested [Phys. Rev. Lett. 116, 052501 (2016)] for describing the anomaly observed in  $^8\text{Be}$ .



From:

**MANUSCRIPT BOOK I OF *SRINIVASA RAMANUJAN***

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Now, we have that, for  $p = 2$

$$((27 \cdot 2 \cdot (1+2)^4)) / ((2 \cdot (1+4 \cdot 2+2^2)^3)) = \alpha$$

**Input:**

$$\frac{27 \times 2 \cdot (1+2)^4}{2 \cdot (1+4 \times 2+2^2)^3}$$

**Exact result:**

$$\frac{2187}{2197}$$

**Decimal approximation:**

0.995448338643604915794264906690942193900773782430587164314...

0.995448338643.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

$$((27 \cdot 2^4 (1+2))) / ((2(2+2 \cdot 2 - 2^2)^3)) = \beta$$

**Input:**

$$\frac{27 \times 2^4 (1+2)}{2(2+2 \times 2 - 2^2)^3}$$

**Result:**

81  
81

$$(1+4 \cdot 2+2^2) [1+((1 \cdot 2 \cdot 81))/((3^2))+(((1 \cdot 2 \cdot 4 \cdot 5) \cdot 81^2))/((3^2 \cdot 6^2))]$$

**Input:**

$$(1+4 \times 2 + 2^2) \left( 1 + \frac{2 \times 81}{3^2} + \frac{(2 \times 4 \times 5) \times 81^2}{3^2 \times 6^2} \right)$$

**Result:**

10777  
10777

$$(1+2-2^{2/2})$$

$$[1+((1 \cdot 2 \cdot 0.995448338643))/((3^2))+(((1 \cdot 2 \cdot 4 \cdot 5) \cdot 0.995448338643^2))/((3^2 \cdot 6^2))]$$

**Input interpretation:**

$$\left( 1 + 2 - \frac{2^2}{2} \right) \left( 1 + \frac{2 \times 0.995448338643}{3^2} + \frac{(2 \times 4 \times 5) \times 0.995448338643^2}{3^2 \times 6^2} \right)$$

**Result:**

1.34354622277339614902240111...

**Repeating decimal:**

1.343546222773396149022401̄ (period 1)

1.34354622277396.....

Now, dividing the two results, performing the 3th root and subtracting by  $\pi$ , we obtain:

$$[10777 / (((((1+2-2^2/2) ((1+((1*2*0.995448338643))/((3^2))+((1*2*4*5)*0.995448338643^2))/((3^2*6^2) ))))))))]^{1/3} - \pi$$

**Input interpretation:**

$$\sqrt[3]{\frac{10777}{(1+2-\frac{2^2}{2})\left(1+\frac{2 \times 0.995448338643}{3^2} + \frac{(2 \times 4 \times 5) \times 0.995448338643^2}{3^2 \times 6^2}\right)}} - \pi$$

**Result:**

16.87614946940...

16.87614946940... result practically equal to the black hole entropy 16.8741 and to the mass of the light particle  $m_X = 16.84$  MeV

**Alternative representations:**

$$\sqrt[3]{\frac{10777}{(1+2-\frac{2^2}{2})\left(1+\frac{2 \times 0.9954483386430000}{3^2} + \frac{(2 \times 4 \times 5) \times 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$-180^\circ + \sqrt[3]{1 + \frac{1.990896677286000}{9} + \frac{40 \times 0.9954483386430000^2}{9 \times 6^2}}$$

$$\sqrt[3]{\frac{10777}{(1+2-\frac{2^2}{2})\left(1+\frac{2 \times 0.9954483386430000}{3^2} + \frac{(2 \times 4 \times 5) \times 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$i \log(-1) + \sqrt[3]{1 + \frac{1.990896677286000}{9} + \frac{40 \times 0.9954483386430000^2}{9 \times 6^2}}$$

$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$-\cos^{-1}(-1) + \sqrt[3]{\frac{10777}{1+\frac{1.990896677286000}{9}+\frac{40 \times 0.9954483386430000^2}{9 \times 6^2}}}$$

### Series representations:

$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$20.017742122984893 - 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$22.017742122984893 - 2 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$20.017742122984893 - \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}$$

### Integral representations:

$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$20.017742122984893 - 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

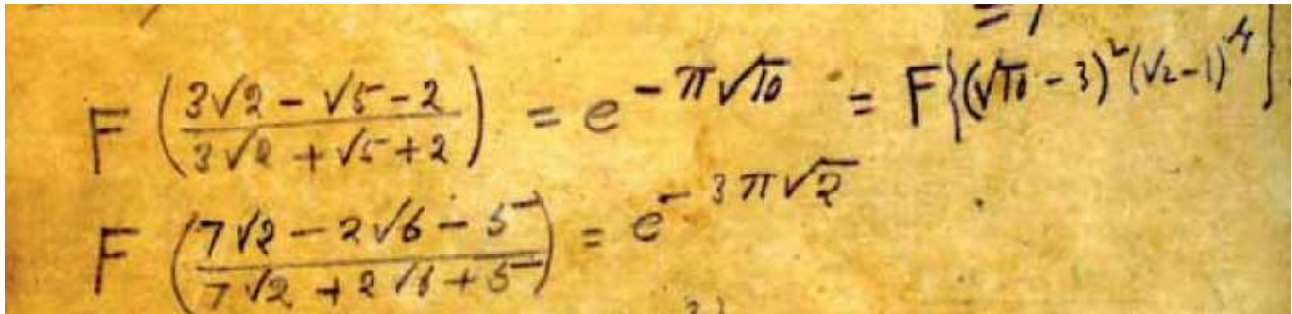
$$\sqrt[3]{\frac{10777}{\left(1+2-\frac{2^2}{2}\right)\left(1+\frac{2 \times 0.9954483386430000}{3^2}+\frac{(2 \times 4 \times 5) 0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$20.017742122984893 - 4 \int_0^1 \sqrt{1-t^2} dt$$

$$\sqrt[3]{\frac{10777}{\left(1 + 2 - \frac{2^2}{2}\right)\left(1 + \frac{2 \times 0.9954483386430000}{3^2} + \frac{(2 \times 4 \times 5)0.9954483386430000^2}{3^2 \times 6^2}\right)}} - \pi =$$

$$20.017742122984893 - 2 \int_0^\infty \frac{\sin(t)}{t} dt$$

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(( exp-(Pi\*sqrt10))

**Input:**

$$\exp\left(-\left(\pi \sqrt{10}\right)\right)$$

**Exact result:**

$$e^{-\sqrt{10} \pi}$$

**Decimal approximation:**

0.000048468896947360265569918689569543669060373746607227063...

0.00004846889...

**Property:**

$e^{-\sqrt{10} \pi}$  is a transcendental number

**Series representations:**

$$e^{-\pi \sqrt{10}} = e^{-\pi \sqrt{10} \sum_{k=0}^{\infty} \binom{1/2}{k} \frac{10^k}{k!}}$$

$$e^{-\pi\sqrt{10}} = \exp\left(-\pi\sqrt{9} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{9}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)$$

$$e^{-\pi\sqrt{10}} = \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 9^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)$$

(exp-(3Pi\*sqrt2))

**Input:**

$$\exp\left(-\left(3\pi\sqrt{2}\right)\right)$$

**Exact result:**

$$e^{-3\sqrt{2}\pi}$$

**Decimal approximation:**

$$1.6272016226072509292942156739117979541838581136954016... \times 10^{-6}$$

$$1.627201622... * 10^{-6}$$

**Property:**

$e^{-3\sqrt{2}\pi}$  is a transcendental number

**Series representations:**

$$e^{-3(\pi\sqrt{2})} = \exp\left(-3\pi\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right)$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$e^{-3(\pi\sqrt{2})} = \exp\left(-3\pi \exp\left(i\pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right)$$

for  $(x \in \mathbb{R} \text{ and } x < 0)$

$$e^{-3(\pi\sqrt{2})} =$$

$$\exp\left(-3\pi \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} z_0^{1/2(1+\lfloor \arg(2-z_0)/(2\pi) \rfloor)} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right)$$

From which, we obtain:

$$1/(\text{golden ratio} \cdot \pi^2) + (((1/(((\exp(-3\pi \cdot \sqrt{2}) \cdot 1 / \exp(-\pi \cdot \sqrt{10})))) - 13))))$$

**Input:**

$$\frac{1}{\phi \pi^2} + \left( \frac{1}{\exp(-3\pi \sqrt{2}) \times \frac{1}{\exp(-\pi \sqrt{10})}} - 13 \right)$$

$\phi$  is the golden ratio

**Exact result:**

$$\frac{1}{\pi^2 \phi} - 13 + e^{3\sqrt{2} \pi - \sqrt{10} \pi}$$

**Decimal approximation:**

16.84927714723931180323495401189575055784023282959459012956...

16.84927714... result very near to the mass of the hypothetical light particle, the boson  $m_X = 16.84 \text{ MeV}$

**Alternate forms:**

$$\frac{1}{\pi^2 \phi} - 13 + e^{-\sqrt{2} (\sqrt{5} - 3) \pi}$$

$$\frac{1}{\pi^2 \phi} - 13 + e^{2\sqrt{7-3\sqrt{5}} \pi}$$

$$\frac{1}{\pi^2 \phi} - 13 + e^{(3\sqrt{2} - \sqrt{10}) \pi}$$

**Series representations:**

$$\frac{1}{\phi \pi^2} + \left( \frac{1}{\frac{\exp(-3\pi\sqrt{2})}{\exp(-\pi\sqrt{10})}} - 13 \right) = - \left( \left( -\exp\left(-3\pi\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right) \right) + \right. \\ \left. 13 \phi \pi^2 \exp\left(-3\pi\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right) - \right. \\ \left. \phi \pi^2 \exp\left(-\pi\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (10-z_0)^k z_0^{-k}}{k!}\right) \right) / \\ \left( \phi \pi^2 \exp\left(-3\pi\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right) \right)$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{1}{\phi \pi^2} + \left( \frac{1}{\frac{\exp(-3\pi\sqrt{2})}{\exp(-\pi\sqrt{10})}} - 13 \right) = \\ - \left( \left( -\exp\left(-3\pi \exp\left(i\pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right) + \right. \\ \left. 13 \phi \pi^2 \exp\left(-3\pi \exp\left(i\pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) - \right. \\ \left. \phi \pi^2 \exp\left(-\pi \exp\left(i\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (10-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right) / \\ \left( \phi \pi^2 \exp\left(-3\pi \exp\left(i\pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}\right) \right)$$

for  $(x \in \mathbb{R} \text{ and } x < 0)$



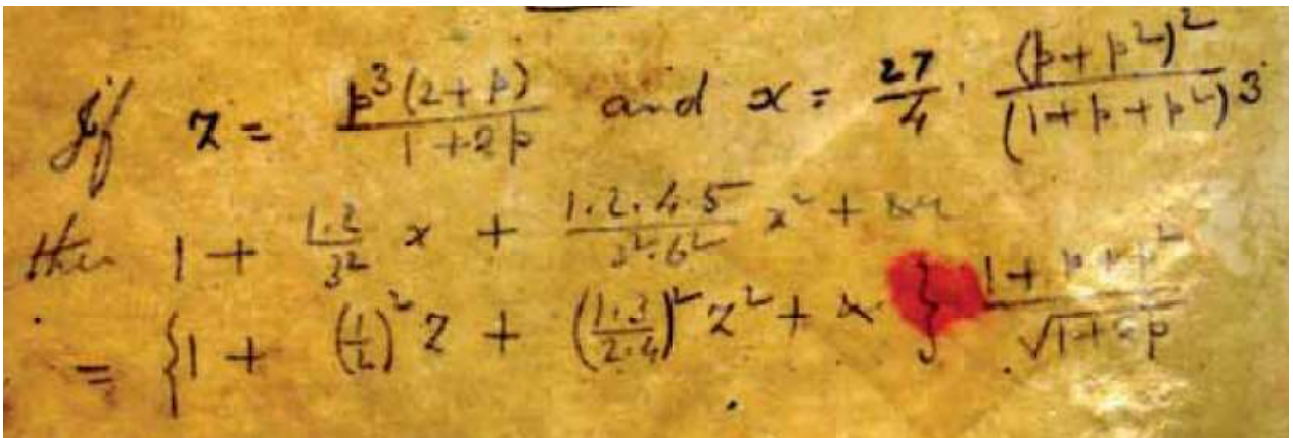
$$\frac{1}{\phi \pi^2} + \left( \frac{1}{\frac{\exp(-3\pi\sqrt{2})}{\exp(-\pi\sqrt{10})}} - 13 \right) =$$

$$- \left( \left( -\exp \left( -3\pi \left( \frac{1}{z_0} \right)^{1/2 [\arg(2-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(2-z_0)/(2\pi)])} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!} \right) + \right.$$

$$13 \phi \pi^2 \exp \left( -3\pi \left( \frac{1}{z_0} \right)^{1/2 [\arg(2-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(2-z_0)/(2\pi)])} \right.$$

$$\left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!} \right) - \phi \pi^2 \exp \left( -\pi \left( \frac{1}{z_0} \right)^{1/2 [\arg(10-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(10-z_0)/(2\pi)])} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (10-z_0)^k z_0^{-k}}{k!} \right) \Bigg) /$$

$$\left( \phi \pi^2 \exp \left( -3\pi \left( \frac{1}{z_0} \right)^{1/2 [\arg(2-z_0)/(2\pi)]} z_0^{1/2 (1+[\arg(2-z_0)/(2\pi)])} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!} \right) \right)$$



For p = 2

$$((2^3(2+2)))/(1+2*2)$$

**Input:**

$$\frac{2^3(2+2)}{1+2 \times 2}$$

**Exact result:**

$$\frac{32}{5}$$

**Decimal form:**

$$6.4$$

$$6.4 = z$$

$$27/4 * (((2+2^2)^2)) / (((1+2+2^2)^3))$$

**Input:**

$$\frac{27}{4} \times \frac{(2+2^2)^2}{(1+2+2^2)^3}$$

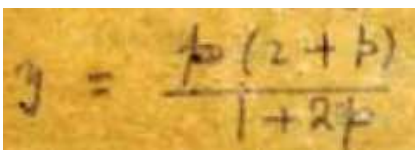
**Exact result:**

$$\frac{243}{343}$$

**Decimal approximation:**

$$0.708454810495626822157434402332361516034985422740524781341\dots$$

$$0.70845481049\dots = x$$



A photograph of a piece of aged, yellowish paper with a handwritten mathematical equation in dark ink. The equation is  $y = \frac{2 + 2}{1 + 2 \times 2}$ . The handwriting is somewhat cursive and the paper shows signs of wear and discoloration.

$$((2(2+2)))/(1+2*2)$$

**Input:**

$$\frac{2(2+2)}{1+2 \times 2}$$

**Exact result:**

$$\frac{8}{5}$$

**Decimal form:**

1.6

$$1.6 = y$$

From the sum of the three results and multiplying by the square root of 3.6180339887498..., we obtain:

$$\sqrt{\left(\frac{5+\sqrt{5}}{2}\right) \left( \frac{2^3(2+2)}{1+2 \times 2} + \frac{27}{4} \frac{(2+2^2)^2}{(1+2+2^2)^3} + \frac{2(2+2)}{1+2 \times 2} \right) + \left( \frac{2(2+2)}{1+2 \times 2} \right)}$$

**Input:**

$$\sqrt{\frac{1}{2} (5 + \sqrt{5}) \left( \frac{2^3 (2+2)}{1+2 \times 2} + \frac{27}{4} \times \frac{(2+2^2)^2}{(1+2+2^2)^3} + \frac{2(2+2)}{1+2 \times 2} \right)}$$

**Result:**

$$\frac{2987}{343} \sqrt{\frac{1}{2} (5 + \sqrt{5})}$$

**Decimal approximation:**

16.56446538876748524729915037203623593208642460719309571107...

16.56446538... result very near to the mass of the hypothetical light particle, the boson  $m_x = 16.84 \text{ MeV}$

**Alternate form:**

$$\frac{2987}{686} \sqrt{(5 + \sqrt{5})^2}$$

**Minimal polynomial:**

$$13841287201 x^4 - 5248421303405 x^2 + 398025498322805$$

Further, we obtain:

$$\frac{1}{\left( \frac{2^3(2+2)}{1+2 \times 2} + \frac{27}{4} \frac{(2+2^2)^2}{(1+2+2^2)^3} + \frac{2(2+2)}{1+2 \times 2} \right) + \left( \frac{2(2+2)}{1+2 \times 2} \right)}^{1/256}$$

**Input:**

$$\sqrt[256]{\frac{1}{\left( \frac{2^3 (2+2)}{1+2 \times 2} + \frac{27}{4} \times \frac{(2+2^2)^2}{(1+2+2^2)^3} + \frac{2(2+2)}{1+2 \times 2} \right) + \left( \frac{2(2+2)}{1+2 \times 2} \right)}}$$

**Result:**

$$\frac{7^{3/256}}{\sqrt[256]{2987}}$$

**Decimal approximation:**

0.991581361996300838042539064353388810605545171886910858324...

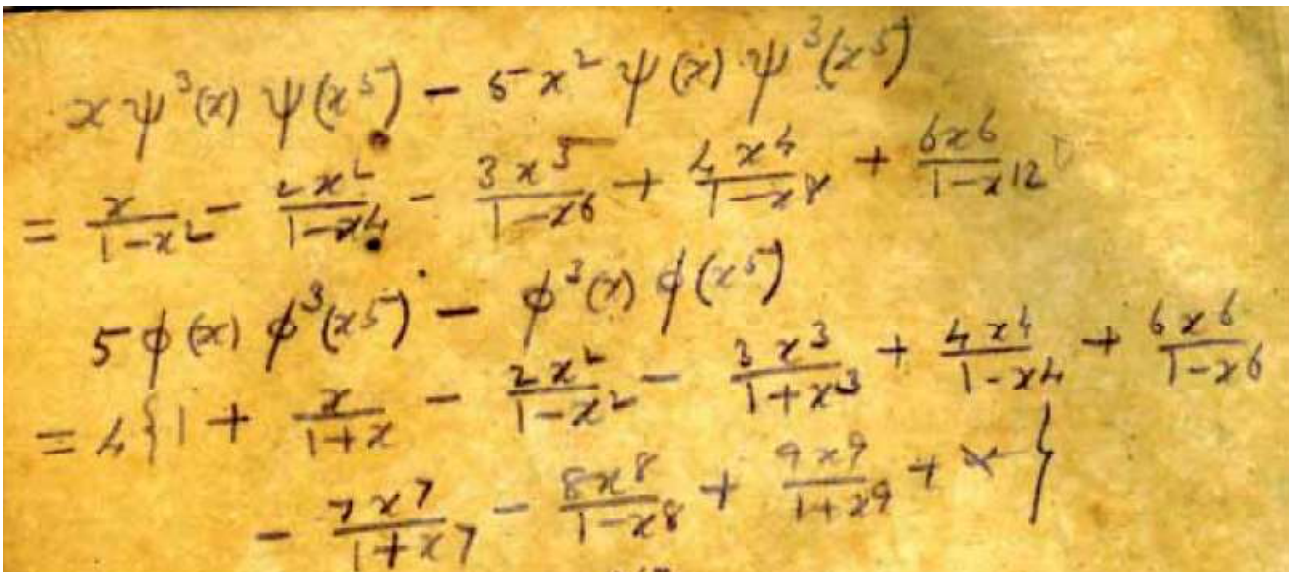
0.991581361... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Alternate form:**

$$\frac{7^{3/256} \times 2987^{255/256}}{2987}$$



For x = 2:

$$2/(1-2^2)-(2*4)/(1-2^4)-(3*8)/(1-2^6)+(4*16)/(1-2^8)+(6*2^6)/(1-2^{12})$$

**Input:**

$$\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}$$

**Exact result:**

$$-\frac{322}{3315}$$

**Decimal approximation:**

-0.09713423831070889894419306184012066365007541478129713423...  
 -0.0971342383...

$$2\pi - 1/((((2/(1-2^2)-(2*4)/(1-2^4)-(3*8)/(1-2^6)+(4*16)/(1-2^8)+(6*2^6)/(1-2^{12}))))))$$

**Input:**

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}}$$

**Result:**

$$\frac{3315}{322} + 2\pi$$

**Decimal approximation:**

16.57821636308020759493770912680745297336328289812909362952...

16.578216363..... result very near to the mass of the hypothetical light particle, the boson  $m_X = 16.84 \text{ MeV}$

**Property:**

$\frac{3315}{322} + 2\pi$  is a transcendental number

**Alternate form:**

$$\frac{1}{322} (644\pi + 3315)$$

**Alternative representations:**

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = 360^\circ - \frac{1}{-\frac{2}{3} - \frac{8}{1-2^4} - \frac{24}{1-2^6} + \frac{64}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}}$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = -2i \log(-1) - \frac{1}{-\frac{2}{3} - \frac{8}{1-2^4} - \frac{24}{1-2^6} + \frac{64}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}}$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = 2 \cos^{-1}(-1) - \frac{1}{-\frac{2}{3} - \frac{8}{1-2^4} - \frac{24}{1-2^6} + \frac{64}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}}$$

**Series representations:**

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + 8 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + \sum_{k=0}^{\infty} \frac{8(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + 2 \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)$$

**Integral representations:**

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + 8 \int_0^1 \sqrt{1-t^2} dt$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + 4 \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$2\pi - \frac{1}{\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}} = \frac{3315}{322} + 4 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\left(\left(\left(\left(\left(\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}\right)\right)\right)\right)\right)^{1/256}$$

**Input:**

$$\sqrt[256]{-\left(\frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}}\right)}$$

**Result:**

$$\sqrt[256]{\frac{322}{3315}}$$

**Decimal approximation:**

0.990933300488502686816572576977892871181315411622053821237...

0.9909333004885.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value  $0.989117352243 = \phi$

**Alternate form:**

$$\frac{\sqrt[256]{322 \cdot 3315^{255/256}}}{3315}$$

$$8\sqrt{\log_{0.9909333004885} \left( \frac{-2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right)} - \pi$$

**Input interpretation:**

$$8 \sqrt{\log_{0.9909333004885} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

124.85840735...

124.85840735.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi =$$

$$-\pi + 8 \sqrt{\frac{\log \left( \frac{-2}{-3} + \frac{8}{1-2^4} + \frac{24}{1-2^6} - \frac{64}{1-2^8} - \frac{6 \times 2^6}{1-2^{12}} \right)}{\log(0.99093330048850000)}}$$

**Series representations:**



$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi =$$

$$- \pi + 8 \sqrt{- \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( \frac{-2993}{3315} \right)^k}{k}}{\log(0.99093330048850000)}}$$

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi =$$

$$- \pi + 8 \sqrt{-1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right)}$$

$$\sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left( -1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right) \right)^k$$

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi =$$

$$- \pi + 8 \sqrt{-1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right)}$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left( -1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right) \right)^k \left( -\frac{1}{2} \right)_k}{k!}$$

$$4 \left( \left( \left( \left( \left( \left( \frac{1+2/3-2 \cdot 4/(1-4)-3 \cdot 8/(1+8)+4 \cdot 16/(1-16)+(6 \cdot 2^6)/(1-2^6)-(7 \cdot 2^7)/(1+2^7)-(8 \cdot 2^8)/(1-2^8)+(9 \cdot 2^9)/(1+2^9) \right) \right) \right) \right) \right) \right)$$

**Input:**

$$4 \left( 1 + \frac{2}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)$$

**Exact result:**

$$\frac{533892}{97223}$$

**Decimal approximation:**

5.491416640095450664966108842557830965923701181819116875636...  
5.49141664009...

$$12 \left( \left( \left( \left( \left( \left( \frac{1+2/3-2 \cdot 4/(1-4)-3 \cdot 8/(1+8)+4 \cdot 16/(1-16)+(6 \cdot 2^6)/(1-2^6)-(7 \cdot 2^7)/(1+2^7)-(8 \cdot 2^8)/(1-2^8)+(9 \cdot 2^9)/(1+2^9) \right) \right) \right) \right) \right) \right)$$

**Input:**

$$12 \left( 1 + \frac{2}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)$$

**Exact result:**

$$\frac{1601676}{97223}$$

**Decimal approximation:**

16.47424992028635199489832652767349289777110354545735062690...

16.47424992.... result very near to the mass of the hypothetical light particle, the boson  $m_X = 16.84$  MeV

$$1/[4(((1+2/3-2*4/(1-4)-3*8/(1+8)+4*16/(1-16)+(6*2^6)/(1-2^6)-(7*2^7)/(1+2^7)-(8*2^8)/(1-2^8)+(9*2^9)/(1+2^9)))))]^{1/256}$$

**Input:**

$$\frac{1}{\sqrt[256]{4 \left( 1 + \frac{2}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)}}$$

**Result:**

$$\frac{\sqrt[256]{\frac{97223}{133473}}}{\sqrt[128]{2}}$$

**Decimal approximation:**

0.993369011342215081271900694747689088058725146793831390260...

0.993369011342215.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

$$\frac{1}{1 + \sqrt[5]{\sqrt{\varphi^5 \sqrt[4]{5^3}} - 1}} - \varphi + 1$$

and to the dilaton value  $0.989117352243 = \phi$

**Alternate form:**

$$\frac{\sqrt[256]{97223} 2^{127/128} \times 133473^{255/256}}{266946}$$

$$1/2 * \log_{\text{base } 0.993369011342215} \left( \left( \frac{1}{4 \left( \frac{1}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) \right) - \pi$$

**Input interpretation:**

$$\frac{1}{2} \log_{0.993369011342215} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

124.8584073464...

124.858407.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi =$$

$$-\pi + \frac{\log \left( \frac{1}{4 \left( \frac{13}{3} + \frac{64}{15} - \frac{24}{9} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right)}{2 \log(0.9933690113422150000)}$$

**Series representations:**

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right)^{-\pi} =$$

$$-\pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{436669}{533892} \right)^k}{k}}{2 \log(0.9933690113422150000)}$$
  

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right)^{-\pi} =$$

$$-1.00000000000000000000 \pi - 75.15353721054604 \log \left( \frac{97223}{533892} \right) -$$

$$0.50000000000000000000 \log \left( \frac{97223}{533892} \right) \sum_{k=0}^{\infty} (-0.0066309886577850000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

$$25 - \phi(x) \phi^3(x^5) - \frac{\phi^5(x)}{\phi(x^5)}$$

$$= 24 + 40 \left( \frac{x}{1+x} - \frac{3x^3}{1+x^3} - \frac{7x^7}{1+x^7} + \frac{9x^9}{1+x^9} \dots \right)$$

$$\frac{\psi^5(x)}{\psi(x^5)} - 25x^2 - \psi(x) \psi^3(x^5)$$

$$= 1 + 5 \left( \frac{x}{1+x} - \frac{2x^2}{1+x^2} - \frac{3x^3}{1+x^3} + \frac{4x^4}{1+x^4} + \dots \right)$$

$$24+40\left(\left(\frac{2}{3}-\frac{24}{9}-\frac{7*2^7}{1+2^7}\right)/\left(1+2^7\right)+\left(\frac{9*2^9}{1+2^9}\right)/\left(1+2^9\right)\right)$$

**Input:**

$$24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1 + 2^7} + \frac{9 \times 2^9}{1 + 2^9} \right)$$

**Exact result:**

$$\frac{20808}{817}$$

**Decimal approximation:**

25.46878824969400244798041615667074663402692778457772337821...

25.468788249...

$$\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\left(\frac{24+40\left(\left(\frac{2}{3}-\frac{24}{9}-\frac{7*2^7}{1+2^7}\right)/\left(1+2^7\right)+\left(\frac{9*2^9}{1+2^9}\right)/\left(1+2^9\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)\right)-3^2$$

**Input:**

$$\left(24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1 + 2^7} + \frac{9 \times 2^9}{1 + 2^9} \right) \right) - 3^2$$

**Exact result:**

$$\frac{13455}{817}$$

**Decimal approximation:**

16.46878824969400244798041615667074663402692778457772337821...

16.468788249.... result very near to the mass of the hypothetical light particle, the boson  $m_x = 16.84 \text{ MeV}$



**Input interpretation:**

$$\frac{1}{4} \log_{0.993696797273339} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

124.8584073464...

124.858407.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi =$$

$$-\pi + \frac{\log \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right)}{4 \log(0.9936967972733390000)}$$

**Series representations:**

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi =$$

$$-\pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{19991}{20808} \right)^k}{k}}{4 \log(0.9936967972733390000)}$$

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi =$$

$$-1.00000000000000000000 \pi - 39.537376547490909 \log \left( \frac{817}{20808} \right) -$$

$$0.25000000000000000000 \log \left( \frac{817}{20808} \right) \sum_{k=0}^{\infty} (-0.0063032027266610000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

$$1+5(2/3-8/5-24/9+64/17)$$

**Input:**

$$1+5\left(\frac{2}{3}-\frac{8}{5}-\frac{24}{9}+\frac{64}{17}\right)$$

**Exact result:**

$$\frac{31}{17}$$

**Decimal approximation:**

1.823529411764705882352941176470588235294117647058823529411...

1.82352941176...

$$(((1+5(2/3-8/5-24/9+64/17))))*3^2$$

**Input:**

$$\left(1+5\left(\frac{2}{3}-\frac{8}{5}-\frac{24}{9}+\frac{64}{17}\right)\right)\times 3^2$$

**Exact result:**

$$\frac{279}{17}$$

**Decimal approximation:**

16.41176470588235294117647058823529411764705882352941176470...

16.411764705.... result very near to the mass of the hypothetical light particle, the boson  $m_x = 16.84$  MeV

$$1/(((1+5(2/3-8/5-24/9+64/17))))^1/64$$

**Input:**

$$\frac{1}{\sqrt[64]{1+5\left(\frac{2}{3}-\frac{8}{5}-\frac{24}{9}+\frac{64}{17}\right)}}$$

**Result:**

$$\sqrt[64]{\frac{17}{31}}$$

**Decimal approximation:**

0.990656829636629644428697934707978356729510518855688643804...

0.99065682963.... result very near to the value of the following Rogers-Ramanujan continued fraction:



$$\frac{\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}}}{1 + \sqrt[5]{\sqrt{\varphi^5 \sqrt[4]{5^3}} - 1}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Alternate form:**

$$\frac{1}{31} \sqrt[64]{17} 31^{63/64}$$

2\*log base 0.9906568296366 ((1/(((1+5(2/3-8/5-24/9+64/17))))))-Pi

**Input interpretation:**

$$2 \log_{0.9906568296366} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi$$

$\log_b(x)$  is the base- $b$  logarithm

**Result:**

124.85840735...

124.858407.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi = -\pi + \frac{2 \log \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right)}{\log(0.99065682963660000)}$$

**Series representations:**

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi = -\pi - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{14}{31} \right)^k}{k}}{\log(0.99065682963660000)}$$

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi =$$

$$-1.0000000000000000 \pi - 213.060101893743 \log\left(\frac{17}{31}\right) -$$

$$2.0000000000000000 \log\left(\frac{17}{31}\right) \sum_{k=0}^{\infty} (-0.00934317036340000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

Note that all the four results concerning the value very near to the like-Higgs boson dilaton mass, are perfectly equals. These Ramanujan expressions, for  $x = 2$ , subtracting  $\pi$  and adding  $1/\phi$  to them, provides ALWAYS the same result: 125.47644... Indeed :

$$8 \sqrt{\log_{0.9909333004885} \left( \left( \left( \left( \left( \left( \left( \frac{-2}{1-2^2} - \frac{2 \cdot 4}{1-2^4} - \frac{3 \cdot 8}{1-2^6} + \frac{4 \cdot 16}{1-2^8} + \frac{6 \cdot 2^6}{1-2^{12}} \right) \right) - (3 \cdot 8) / (1-2^6) + (4 \cdot 16) / (1-2^8) + (6 \cdot 2^6) / (1-2^{12}) \right) \right) \right) \right) \right) \right) - \pi + 1/\phi}$$

**Input interpretation:**

$$8 \sqrt{\log_{0.9909333004885} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right) - \pi + \frac{1}{\phi}}$$

$\log_b(x)$  is the base- $b$  logarithm

$\phi$  is the golden ratio

**Result:**

125.47644134...

125.47644... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$

**Alternative representation:**

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi + \frac{1}{\phi} =$$

$$- \pi + \frac{1}{\phi} + 8 \sqrt{\frac{\log \left( \frac{-2}{-3} + \frac{8}{1-2^4} + \frac{24}{1-2^6} - \frac{64}{1-2^8} - \frac{6 \times 2^6}{1-2^{12}} \right)}{\log(0.99093330048850000)}}$$

**Series representations:**

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 8 \sqrt{- \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( \frac{-2993}{3315} \right)^k}{k}}{\log(0.99093330048850000)}}$$

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 8 \sqrt{-1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right)}$$

$$\sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} \left( -1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right) \right)^k$$

$$8 \sqrt{\log_{0.99093330048850000} \left( - \left( \frac{2}{1-2^2} - \frac{2 \times 4}{1-2^4} - \frac{3 \times 8}{1-2^6} + \frac{4 \times 16}{1-2^8} + \frac{6 \times 2^6}{1-2^{12}} \right) \right)} - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 8 \sqrt{-1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right)}$$

$$\sum_{k=0}^{\infty} \frac{(-1)^k \left( -1 + \log_{0.99093330048850000} \left( \frac{322}{3315} \right) \right)^k \left( -\frac{1}{2} \right)_k}{k!}$$

1/2\*log base 0.993369011342215 (((1/[4(((1+2/3-2\*4/(1-4)-3\*8/(1+8)+4\*16/(1-16)+(6\*2^6)/(1-2^6)-(7\*2^7)/(1+2^7)-(8\*2^8)/(1-2^8)+(9\*2^9)/(1+2^9)))))))-Pi+1/golden ratio

**Input interpretation:**

$$\frac{1}{2} \log_{0.993369011342215} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - 2 \times \frac{4}{1-4} - 3 \times \frac{8}{1+8} + 4 \times \frac{16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi}$$

$\log_b(x)$  is the base- $b$  logarithm

$\phi$  is the golden ratio

### Result:

125.4764413352...

125.47644... result very near to the dilaton mass calculated as a type of Higgs boson:  
125 GeV for  $T = 0$

### Alternative representation:

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{\log \left( \frac{1}{4 \left( \frac{13}{3} + \frac{64}{15} - \frac{24}{9} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right)}{2 \log(0.9933690113422150000)}$$

### Series representations:

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{436669}{533892} \right)^k}{k}}{2 \log(0.9933690113422150000)}$$

$$\frac{1}{2} \log_{0.9933690113422150000} \left( \frac{1}{4 \left( 1 + \frac{2}{3} - \frac{2 \times 4}{1-4} - \frac{3 \times 8}{1+8} + \frac{4 \times 16}{1-16} + \frac{6 \times 2^6}{1-2^6} - \frac{7 \times 2^7}{1+2^7} - \frac{8 \times 2^8}{1-2^8} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - 1.00000000000000000000 \pi - 75.15353721054604 \log \left( \frac{97223}{533892} \right) -$$

$$\frac{1}{2} \log \left( \frac{97223}{533892} \right) \sum_{k=0}^{\infty} (-0.0066309886577850000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

1/4\*log base 0.993696797273339 (((1/((((24+40(((2/3-24/9-(7\*2^7)/(1+2^7)+(9\*2^9)/(1+2^9)))))))))))-Pi+1/golden ratio

**Input interpretation:**

$$\frac{1}{4} \log_{0.993696797273339} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi}$$

log<sub>b</sub>(x) is the base- b logarithm

φ is the golden ratio

**Result:**

125.4764413352...

125.47644... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

**Alternative representation:**

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{\log \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right)}{4 \log(0.9936967972733390000)}$$

**Series representations:**

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{19991}{20808} \right)^k}{k}}{4 \log(0.9936967972733390000)}$$

$$\frac{1}{4} \log_{0.9936967972733390000} \left( \frac{1}{24 + 40 \left( \frac{2}{3} - \frac{24}{9} - \frac{7 \times 2^7}{1+2^7} + \frac{9 \times 2^9}{1+2^9} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - 1.00000000000000000000 \pi - 39.537376547490909 \log\left(\frac{817}{20808}\right) -$$

$$\frac{1}{4} \log\left(\frac{817}{20808}\right) \sum_{k=0}^{\infty} (-0.0063032027266610000)^k G(k)$$

for  $G(0) = 0$  and  $G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j}$

2\*log base 0.9906568296366 ((1/(((1+5(2/3-8/5-24/9+64/17)))))))-Pi+1/golden ratio

**Input interpretation:**

$$2 \log_{0.9906568296366} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi + \frac{1}{\phi}$$

$\log_b(x)$  is the base- $b$  logarithm

$\phi$  is the golden ratio

**Result:**

125.47644133...

125.47644... result very near to the dilaton mass calculated as a type of Higgs boson:  
125 GeV for  $T = 0$

**Alternative representation:**

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{2 \log \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right)}{\log(0.99065682963660000)}$$

**Series representations:**

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{14}{31} \right)^k}{k}}{\log(0.99065682963660000)}$$

$$2 \log_{0.99065682963660000} \left( \frac{1}{1 + 5 \left( \frac{2}{3} - \frac{8}{5} - \frac{24}{9} + \frac{64}{17} \right)} \right) - \pi + \frac{1}{\phi} = \frac{1}{\phi} - 1.0000000000000000 \pi -$$

$$213.060101893743 \log \left( \frac{17}{31} \right) - 2 \log \left( \frac{17}{31} \right) \sum_{k=0}^{\infty} (-0.00934317036340000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

## Appendix

From:

### Modular equations and approximations to $\pi$

*Srinivasa Ramanujan* - Quarterly Journal of Mathematics, XLV, 1914, 350 – 372

We note that:

$$g_{22} = \sqrt{(1 + \sqrt{2})}.$$

Hence

$$\begin{aligned} 64g_{22}^{24} &= e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots, \\ 64g_{22}^{-24} &= 4096e^{-\pi\sqrt{22}} + \dots, \end{aligned}$$

so that

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}.$$

Hence

$$e^{\pi\sqrt{22}} = 2508951.9982\dots$$

Thence:

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \dots$$

And

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}$$

That are connected with 64 and  $4096 = 64^2$



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