

Further Ramanujan's equations applied to various sectors of Particle Physics and Cosmology: some possible new mathematical connections. V


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Abstract

In this research thesis, we have analyzed further Ramanujan formulas and described new possible mathematical connections with some sectors of Particle Physics and Cosmology

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<http://www.giochicreativi.com/2012/01/pazze-formule-ramanujan.html>



1729
 $= 1^3 + 12^3$
 $= 9^3 + 10^3$
 $= 7 \times 13 \times 19$

<https://www.famousscientists.org/srinivasa-ramanujan/>



“It was his insight into algebraical formulae, transformations of infinite series, and so forth that was most amazing. On this side most certainly I have never met his equal, and I can compare him only with Euler or Jacobi.”

G. H. HARDY, 1877 – 1947 (Mathematician)

From:

Manuscript Book Of Srinivasa Ramanujan Volume 1

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$$(((3\sqrt{3}+1)^{1/3}+(3\sqrt{3}-1)^{1/3}))^2 * (13)^{1/6} * 1/(3*(2)^{1/3})$$

Input:

$$\left(\sqrt[3]{3\sqrt{3}+1} + \sqrt[3]{3\sqrt{3}-1}\right)^2 \sqrt[6]{13} \times \frac{1}{3\sqrt[3]{2}}$$

Result:

$$\frac{\sqrt[6]{13} \left(\sqrt[3]{3\sqrt{3}-1} + \sqrt[3]{1+3\sqrt{3}}\right)^2}{3\sqrt[3]{2}}$$

Decimal approximation:

4.827716585669311505850859903413752753840343568084383506637...

4.8277165856693...

Alternate forms:

$$\frac{1}{6} \left(\sqrt[3]{3\sqrt{3}-1} + \sqrt[3]{1+3\sqrt{3}}\right)^2 \sqrt[6]{13} 2^{2/3}$$

root of $x^6 - 26x^4 + 65x^2 - 52$ near $x = 4.82772$

$$\sqrt{\frac{1}{26 + \sqrt[3]{13(821 - 72\sqrt{3})} + \sqrt[3]{13(821 + 72\sqrt{3})}}}$$

Minimal polynomial:

$$x^6 - 26x^4 + 65x^2 - 52$$

$e^{(-13\pi)}$

Input:

$$e^{-13\pi}$$

Decimal approximation:

$$1.8327676056715775684639617650534828603659265496720660... \times 10^{-18}$$

$$1.832767605671... * 10^{-18}$$

Property:

$e^{-13\pi}$ is a transcendental number

Alternative representations:

$$e^{-13\pi} = e^{-2340^\circ}$$

$$e^{-13\pi} = e^{13i \log(-1)}$$

$$e^{-13\pi} = \exp^{-13\pi}(z) \text{ for } z = 1$$

Series representations:

$$e^{-13\pi} = e^{-52 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

$$e^{-13\pi} = \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{-13\pi}$$

$$e^{-13\pi} = \left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}} \right)^{-13\pi}$$

Integral representations:

$$e^{-13\pi} = e^{-52 \int_0^1 \sqrt{1-t^2} dt}$$

$$e^{-13\pi} = e^{-26 \int_0^1 1/\sqrt{1-t^2} dt}$$

$$e^{-13\pi} = e^{-26 \int_0^{\infty} 1/(1+t^2) dt}$$

$$e^{(-13\pi)x} = (((3\sqrt{3}+1)^{1/3}+(3\sqrt{3}-1)^{1/3}))^2 * (13)^{1/6} * 1/(3*(2)^{1/3})$$

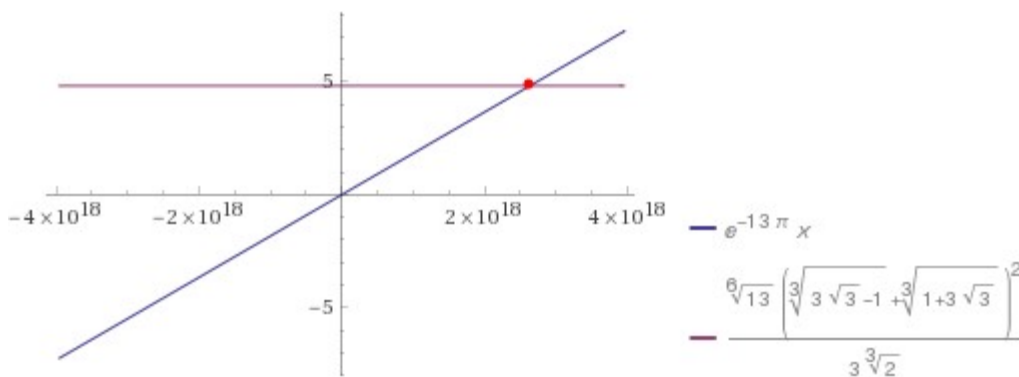
Input:

$$e^{-13\pi x} = \left(\sqrt[3]{3\sqrt{3}+1} + \sqrt[3]{3\sqrt{3}-1} \right)^2 \sqrt[6]{13} \times \frac{1}{3\sqrt[3]{2}}$$

Exact result:

$$e^{-13\pi x} = \frac{\sqrt[6]{13} \left(\sqrt[3]{3\sqrt{3}-1} + \sqrt[3]{1+3\sqrt{3}} \right)^2}{3\sqrt[3]{2}}$$

Plot:



Alternate forms:

$$e^{-13\pi x} = \text{root of } x^6 - 26x^4 + 65x^2 - 52 \text{ near } x = 4.82772$$

$$e^{-13\pi x} = \frac{1}{\sqrt{\frac{3}{26+3\sqrt{13(821-72\sqrt{3})}} + 3\sqrt{13(821+72\sqrt{3})}}}}$$

$$e^{-13\pi x} = \frac{\sqrt[6]{13} (3\sqrt{3}-1)^{2/3}}{3\sqrt[3]{2}} + \frac{\sqrt[6]{13} (1+3\sqrt{3})^{2/3}}{3\sqrt[3]{2}} + \frac{1}{3} \times 2^{2/3} \sqrt[6]{13} \sqrt[3]{(3\sqrt{3}-1)(1+3\sqrt{3})}$$

Solution:

$$x \approx 2634112786983868826$$

$$1/6 13^{(1/6)} (4 13^{(1/3)} + (-2 + 6 \sqrt{3})^{(2/3)} + (2 + 6 \sqrt{3})^{(2/3)}) e^{(13 \pi)}$$

Input:

$$\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3} \right) e^{13\pi}$$

Decimal approximation:

2.6341127869838688278803376180123395006376168896977924... $\times 10^{18}$

2.634112786983... $\times 10^{18}$

Property:

$\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3} \right) e^{13\pi}$ is a transcendental number

Alternate forms:

$e^{13\pi}$ root of $x^6 - 26x^4 + 65x^2 - 52$ near $x = 4.82772$

$$\frac{e^{13\pi}}{\sqrt{\frac{3}{26+3\sqrt{13(821-72\sqrt{3})}+3\sqrt{13(821+72\sqrt{3})}}}}$$

$$\frac{2}{3} \sqrt{13} e^{13\pi} + \frac{1}{6} \sqrt[6]{13} (6\sqrt{3} - 2)^{2/3} e^{13\pi} + \frac{1}{6} \sqrt[6]{13} (2 + 6\sqrt{3})^{2/3} e^{13\pi}$$

Series representations:

$$\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3} \right) e^{13\pi} = \frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{\frac{1}{2}}{k} \right)^{2/3} + 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{\frac{1}{2}}{k} \right)^{2/3} \right)$$

$$\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3} \right) e^{13\pi} = \frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} + 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} \right)$$

$$\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3} \right) e^{13\pi} = \frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3 - z_0)^k z_0^{-k}}{k!} \right)^{2/3} + 2^{2/3} \left(1 + 3\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3 - z_0)^k z_0^{-k}}{k!} \right)^{2/3} \right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$3\ln\left[\frac{1}{6} 13^{1/6} \left(4 13^{1/3} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right]$ -golden ratio

Input:

$$3 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right) - \phi$$

$\log(x)$ is the natural logarithm

ϕ is the golden ratio

Decimal approximation:

125.6272002991209830597038872640022801147662729880795730739...

125.62720029912... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Alternate forms:

$$-\frac{1}{2} - \frac{\sqrt{5}}{2} + 3 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right)$$

$$\frac{1}{2} \left(-1 - \sqrt{5} + 6 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right)\right)$$

$$\frac{1}{2} \left(-1 - \sqrt{5}\right) + 3 \log\left(\frac{e^{13\pi}}{\sqrt{\frac{3}{\sqrt{26+3\sqrt{13}(821-72\sqrt{3})} + \sqrt{13(821+72\sqrt{3})}}}}}\right)$$

Alternative representations:

$$3 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right) - \phi =$$

$$-\phi + 3 \log_e\left(\frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right)\right)$$

$$3 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right) - \phi =$$

$$-\phi + 3 \log(a) \log_a\left(\frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right)\right)$$

$$3 \log\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3}\right) e^{13\pi}\right) - \phi =$$

$$-\phi - 3 \operatorname{Li}_1\left(1 - \frac{1}{6} \sqrt[6]{13} e^{13\pi} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3}\right)\right)$$

$$\left(\left(\left(\frac{1}{6} 13^{1/6} \left(4 13^{1/3} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}\right) e^{13\pi}\right)\right)\right)^{1/88}$$

Input:

$$\sqrt[88]{\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3}\right) e^{13\pi}}$$

Exact result:

$$\frac{\sqrt[528]{13} \sqrt[88]{4 \sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}} e^{(13\pi)/88}}{\sqrt[88]{6}}$$

Decimal approximation:

1.619292821206264086408656253528087560236095639242293147294...

1.61929821206... result that is a good approximation to the value of the golden ratio
1,618033988749...

Property:

$$\frac{\sqrt[528]{13} \sqrt[88]{4 \sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3}} e^{(13\pi)/88}}{\sqrt[88]{6}}$$

is a transcendental number

Alternate form:

$$\frac{\sqrt[528]{13} \sqrt[88]{4 \sqrt[3]{13} + (2(3\sqrt{3} - 1))^{2/3} + (2(1 + 3\sqrt{3}))^{2/3}} e^{(13\pi)/88}}{\sqrt[88]{6}}$$

All 88th roots of $\frac{1}{6} 13^{1/6} (4 13^{1/3} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}) e^{13 \pi}$:

$$\frac{528 \sqrt[13]{13} e^{(13 \pi)/88} e^0}{\sqrt[88]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}}}} \approx 1.6193 \text{ (real, principal root)}$$

$$\frac{528 \sqrt[13]{13} e^{(13 \pi)/88} e^{(i \pi)/44}}{\sqrt[88]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}}}} \approx 1.61517 + 0.11552 i$$

$$\frac{528 \sqrt[13]{13} e^{(13 \pi)/88} e^{(i \pi)/22}}{\sqrt[88]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}}}} \approx 1.60281 + 0.23045 i$$

$$\frac{528 \sqrt[13]{13} e^{(13 \pi)/88} e^{(3 i \pi)/44}}{\sqrt[88]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}}}} \approx 1.58229 + 0.34421 i$$

$$\frac{528 \sqrt[13]{13} e^{(13 \pi)/88} e^{(i \pi)/11}}{\sqrt[88]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}}}} \approx 1.55370 + 0.45621 i$$

Series representations:

$$\sqrt[88]{\frac{1}{6} \sqrt[6]{13} (4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3}) e^{13 \pi}} = \frac{1}{\sqrt[88]{6}} 528 \sqrt[13]{13} \left(e^{13 \pi} \left(4 \sqrt[3]{13} + 2^{2/3} \left(-1 + 3 \sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{1/2}{k} \right)^{2/3} + 2^{2/3} \left(1 + 3 \sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \binom{1/2}{k} \right)^{2/3} \right) \right)^{1/88}$$

$$\sqrt[88]{\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3} \right) e^{13 \pi}} =$$

$$\frac{1}{\sqrt[88]{6}} \sqrt[528]{\sqrt[6]{13} \left(e^{13 \pi} \left(4 \sqrt[3]{13} + 2^{2/3} \left(-1 + 3 \sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} + \right. \right.}$$

$$\left. \left. 2^{2/3} \left(1 + 3 \sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} \right) \right)} \wedge (1/88)$$

$$\sqrt[88]{\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3} \right) e^{13 \pi}} =$$

$$\frac{1}{\sqrt[88]{6}} \sqrt[528]{\sqrt[6]{13} \left(e^{13 \pi} \left(4 \sqrt[3]{13} + \frac{-2 \sqrt{\pi} + 3 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} + \right.}$$

$$\left. \frac{2 \sqrt{\pi} + 3 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} \right)} \wedge (1/88)$$

Integral representation:

$$(1+z)^a = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-a-s)}{z^s} ds}{(2\pi i)\Gamma(-a)} \quad \text{for } (0 < \gamma < -\text{Re}(a) \text{ and } |\arg(z)| < \pi)$$

$$\left(\left(\frac{1}{\left(\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3} \right) e^{13 \pi} \right) \right)^{1/88} \right)^{1/32}$$

Input:

$$\sqrt[32]{\sqrt[88]{\frac{1}{6} \sqrt[6]{13} \left(4 \sqrt[3]{13} + (-2 + 6 \sqrt{3})^{2/3} + (2 + 6 \sqrt{3})^{2/3} \right) e^{13 \pi}}}$$

Exact result:

$$\frac{2816 \sqrt[2816]{\frac{6}{4 \sqrt[3]{13} + (6 \sqrt{3} - 2)^{2/3} + (2 + 6 \sqrt{3})^{2/3}}} e^{-(13 \pi)/2816}}{16 \sqrt[896]{\sqrt[6]{13}}}$$

Decimal approximation:

0.985050694517374407899501325597376070207916059031421967889...

0.98505069451737... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Property:

$$\frac{2816 \sqrt[2816]{\frac{6}{4\sqrt[3]{13} + (-2+6\sqrt{3})^{2/3} + (2+6\sqrt{3})^{2/3}}} e^{-(13\pi)/2816}}{16^{896}\sqrt[13]{13}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{e^{-(13\pi)/2816} \sqrt[2816]{\text{root of } 8x^9 - 25x^6 + 32x^3 - 1 \text{ near } x = 0.317626}}{16^{896}\sqrt[13]{13}}$$

$$\frac{2816 \sqrt[2816]{\frac{6}{4\sqrt[3]{13} + (2(3\sqrt{3}-1))^{2/3} + (2(1+3\sqrt{3}))^{2/3}}} e^{-(13\pi)/2816}}{16^{896}\sqrt[13]{13}}$$

All 32nd roots of $((6/(4 \cdot 13^{1/3}) + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}))^{1/88} e^{-(13\pi)/88} / 13^{1/528}$:

$$\frac{2816 \sqrt[6]{6} e^{-(13\pi)/2816} e^0}{16^{896}\sqrt[13]{13} \sqrt[2816]{4\sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}}} \approx 0.985051 \text{ (real, principal root)}$$

$$\frac{2816\sqrt{6} e^{-(13\pi)/2816} e^{(i\pi)/16}}{16^{896}\sqrt{13} 2816\sqrt{4\sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}}} \approx 0.966123 + 0.192174 i$$

$$\frac{2816\sqrt{6} e^{-(13\pi)/2816} e^{(i\pi)/8}}{16^{896}\sqrt{13} 2816\sqrt{4\sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}}} \approx 0.91007 + 0.37696 i$$

$$\frac{2816\sqrt{6} e^{-(13\pi)/2816} e^{(3i\pi)/16}}{16^{896}\sqrt{13} 2816\sqrt{4\sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}}} \approx 0.81904 + 0.54726 i$$

$$\frac{2816\sqrt{6} e^{-(13\pi)/2816} e^{(i\pi)/4}}{16^{896}\sqrt{13} 2816\sqrt{4\sqrt[3]{13} + (6\sqrt{3} - 2)^{2/3} + (2 + 6\sqrt{3})^{2/3}}} \approx 0.69654 + 0.69654 i$$

Series representations:

$$\sqrt[32]{\frac{1}{88\sqrt{\frac{1}{6}}\sqrt[6]{13} \left(4\sqrt[3]{13} + (-2 + 6\sqrt{3})^{2/3} + (2 + 6\sqrt{3})^{2/3}\right) e^{13\pi}}} =$$

$$\left(2816\sqrt{6} e^{-13\pi} \left(e^{13\pi} \left(4\sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \left(\frac{1}{2}\right)^{2/3}\right) + \right. \right. \right. \right. \\ \left. \left. \left. 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \left(\frac{1}{2}\right)^{2/3}\right) \right) \right)^{2815/2816} \right) / \left(16^{896}\sqrt{13} \right. \\ \left. \left(4\sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \left(\frac{1}{2}\right)^{2/3}\right) + 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} 2^{-k} \left(\frac{1}{2}\right)^{2/3}\right) \right) \right)$$

$$\begin{aligned}
& \sqrt[32]{\frac{1}{88\sqrt{\frac{1}{6}\sqrt[6]{13}\left(4\sqrt[3]{13}+(-2+6\sqrt{3})^{2/3}+(2+6\sqrt{3})^{2/3}\right)e^{13\pi}}}} = \\
& \left(2816\sqrt[6]{6} e^{-13\pi} \left(e^{13\pi} \left(4\sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} + \right. \right. \right. \\
& \quad \left. \left. \left. 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} \right) \right)^{2815/2816} \right) / \\
& \left(16^{896}\sqrt[6]{13} \left(4\sqrt[3]{13} + 2^{2/3} \left(-1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} + \right. \right. \\
& \quad \left. \left. 2^{2/3} \left(1 + 3\sqrt{2} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^{2/3} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt[32]{\frac{1}{88\sqrt{\frac{1}{6}\sqrt[6]{13}\left(4\sqrt[3]{13}+(-2+6\sqrt{3})^{2/3}+(2+6\sqrt{3})^{2/3}\right)e^{13\pi}}}} = \\
& \left(2816\sqrt[6]{6} e^{-13\pi} \left(e^{13\pi} \left(4\sqrt[3]{13} + \frac{-2\sqrt{\pi} + 3\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} + \right. \right. \\
& \quad \left. \left. \left(\frac{2\sqrt{\pi} + 3\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} \right) \right)^{2815/2816} \right) / \\
& \left(16^{896}\sqrt[6]{13} \left(4\sqrt[3]{13} + \frac{-2\sqrt{\pi} + 3\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} + \right. \\
& \quad \left. \left(\frac{2\sqrt{\pi} + 3\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}} \right)^{2/3} \right)
\end{aligned}$$

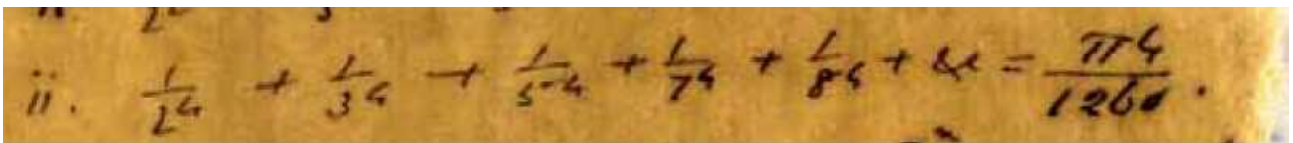
Integral representation:

$$(1+z)^a = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-a-s)}{z^s} ds}{(2\pi i)\Gamma(-a)} \quad \text{for } (0 < \gamma < -\text{Re}(a) \text{ and } |\arg(z)| < \pi)$$

From:

Manuscript Book Of Srinivasa Ramanujan Volume II

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ii. $\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} + \dots = \frac{\pi^4}{1263}$

$$\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}$$

Input:

$$\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}$$

Exact result:

$$\frac{38389024801}{497871360000}$$

Decimal approximation:

0.077106312765209069266406487009013733989438556979859215039...

0.0771063127652...

$(\pi^4)/1263$

Input:

$$\frac{\pi^4}{1263}$$

Decimal approximation:

0.077125171048299633599715227782030966943568951443139684632...

0.077125171...

Property:

$\frac{\pi^4}{1263}$ is a transcendental number

Alternative representations:

$$\frac{\pi^4}{1263} = \frac{(180^\circ)^4}{1263}$$

$$\frac{\pi^4}{1263} = \frac{(-i \log(-1))^4}{1263}$$

$$\frac{\pi^4}{1263} = \frac{\cos^{-1}(-1)^4}{1263}$$

Series representations:

$$\frac{\pi^4}{1263} = \frac{30}{421} \sum_{k=1}^{\infty} \frac{1}{k^4}$$

$$\frac{\pi^4}{1263} = \frac{32}{421} \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}$$

$$\frac{\pi^4}{1263} = \frac{256 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{1263}$$

Integral representations:

$$\frac{\pi^4}{1263} = \frac{256 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{1263}$$

$$\frac{\pi^4}{1263} = \frac{16 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4}{1263}$$

$$\frac{\pi^4}{1263} = \frac{16 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{1263}$$

$$1/2^4 + 1/3^4 + 1/5^4 + 1/7^4 + 1/8^4 = (\pi^4)/x$$

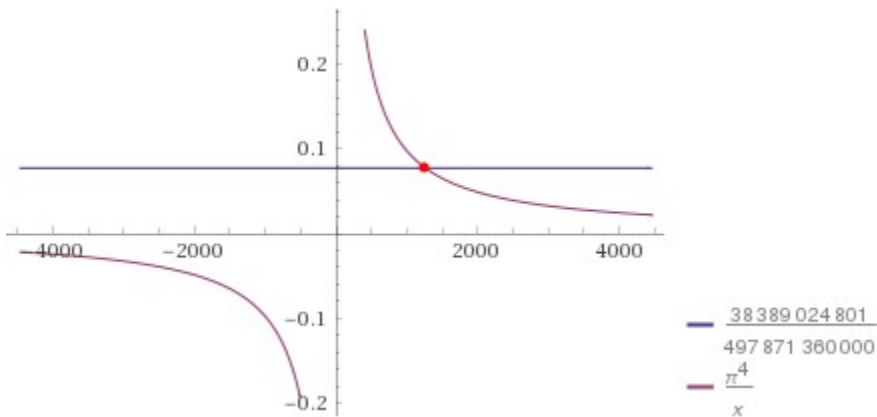
Input:

$$\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} = \frac{\pi^4}{x}$$

Exact result:

$$\frac{38\,389\,024\,801}{497\,871\,360\,000} = \frac{\pi^4}{x}$$

Plot:



Alternate form assuming x is real:

$$\frac{497\,871\,360\,000 \pi^4}{x} = 38\,389\,024\,801$$

Alternate form assuming x is positive:

$$38\,389\,024\,801 x = 497\,871\,360\,000 \pi^4 \quad (\text{for } x \neq 0)$$

Solution:

$$x \approx 1263.30889833386$$

$$1263.30889833386$$

$$(\pi^4)/(1/2^4 + 1/3^4 + 1/5^4 + 1/7^4 + 1/8^4)$$

Input:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

Result:

$$\frac{497871360000 \pi^4}{38389024801}$$

Decimal approximation:

1263.308898333861577329969799525829595372460284872981338792...

1263.3088983386...

Property:

$\frac{497871360000 \pi^4}{38389024801}$ is a transcendental number

Alternative representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{(180^\circ)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{(-i \log(-1))^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{\cos^{-1}(-1)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

Series representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{44808422400000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{38389024801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{47795650560000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{38389024801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{127455068160000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{38389024801}$$

Integral representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{7965\,941\,760\,000 \left(\int_0^\infty \frac{1}{1+t^2} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{7965\,941\,760\,000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} = \frac{127\,455\,068\,160\,000 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{38\,389\,024\,801}$$

$$(\pi^4)/(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}) - 29 - 2$$

Input:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2$$

Result:

$$\frac{497\,871\,360\,000 \pi^4}{38\,389\,024\,801} - 31$$

Decimal approximation:

1232.308898333861577329969799525829595372460284872981338792...

[1232.30889833386....](#) result practically equal to the rest mass of Delta baryon 1232

Property:

$-31 + \frac{497\,871\,360\,000 \pi^4}{38\,389\,024\,801}$ is a transcendental number

Alternate form:

$$\frac{497\,871\,360\,000 \pi^4 - 1\,190\,059\,768\,831}{38\,389\,024\,801}$$

Alternative representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{(180^\circ)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{(-i \log(-1))^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{\cos^{-1}(-1)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

Series representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{44\,808\,422\,400\,000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{47\,795\,650\,560\,000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{127\,455\,068\,160\,000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{38\,389\,024\,801}$$

Integral representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{7\,965\,941\,760\,000 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{7\,965\,941\,760\,000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 29 - 2 = -31 + \frac{127\,455\,068\,160\,000 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{38\,389\,024\,801}$$

$$(\pi^4)/(1/2^4 + 1/3^4 + 1/5^4 + 1/7^4 + 1/8^4) + 29^2 - 322$$

Input:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322$$

Result:

$$519 + \frac{497871360000 \pi^4}{38389024801}$$

Decimal approximation:

1782.308898333861577329969799525829595372460284872981338792...

1782.30889833386... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

Property:

$519 + \frac{497871360000 \pi^4}{38389024801}$ is a transcendental number

Alternate form:

$$\frac{3(6641301290573 + 165957120000 \pi^4)}{38389024801}$$

Alternative representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = -322 + 29^2 + \frac{(180^\circ)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = -322 + 29^2 + \frac{(-i \log(-1))^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = -322 + 29^2 + \frac{\cos^{-1}(-1)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

Series representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{44\,808\,422\,400\,000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{47\,795\,650\,560\,000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{127\,455\,068\,160\,000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{38\,389\,024\,801}$$

Integral representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{7\,965\,941\,760\,000 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{7\,965\,941\,760\,000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 29^2 - 322 = 519 + \frac{127\,455\,068\,160\,000 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{38\,389\,024\,801}$$

$$(\pi^4)/(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4})/11+11$$

Input:

$$\frac{1}{11} \times \frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} + 11$$

Result:

$$11 + \frac{497\,871\,360\,000 \pi^4}{422\,279\,272\,811}$$

Decimal approximation:

125.8462634848965070299972545023481450338600258975437580720...

125.84626348489... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Property:

$11 + \frac{497871360000\pi^4}{422279272811}$ is a transcendental number

Alternate form:

$$\frac{497871360000\pi^4 + 4645072000921}{422279272811}$$

Alternative representations:

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{(180^\circ)^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{(-i \log(-1))^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{\cos^{-1}(-1)^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)}$$

Series representations:

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{44808422400000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{422279272811}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{47795650560000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{422279272811}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{127455068160000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^4}{422279272811}$$

Integral representations:

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{7965941760000 \left(\int_0^\infty \frac{1}{1+t^2} dt\right)^4}{422279272811}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{7965941760000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt\right)^4}{422279272811}$$

$$\frac{\pi^4}{11\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right)} + 11 = 11 + \frac{127455068160000 \left(\int_0^1 \sqrt{1-t^2} dt\right)^4}{422279272811}$$

$$(\pi^4)/\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}\right) - 199 - 47 + 2$$

Input:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2$$

Result:

$$\frac{497871360000 \pi^4}{38389024801} - 244$$

Decimal approximation:

1019.308898333861577329969799525829595372460284872981338792...

[1019.30889833386...](#) result practically equal to the rest mass of Phi meson 1019.445

Property:

$-244 + \frac{497871360000 \pi^4}{38389024801}$ is a transcendental number

Alternate form:

$$\frac{4(124467840000 \pi^4 - 2341730512861)}{38389024801}$$

Alternative representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{(180^\circ)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{(-i \log(-1))^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{\cos^{-1}(-1)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}$$

Series representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{44\,808\,422\,400\,000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{47\,795\,650\,560\,000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{127\,455\,068\,160\,000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{38\,389\,024\,801}$$

Integral representations:

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{7\,965\,941\,760\,000 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4}{38\,389\,024\,801}$$

$$\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = -244 + \frac{7\,965\,941\,760\,000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{38\,389\,024\,801}$$

$$\begin{aligned} \frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} - 199 - 47 + 2 = \\ -244 + \frac{127\,455\,068\,160\,000 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{38\,389\,024\,801} \end{aligned}$$

$(\pi^4) * 1 / (1/2^4 + 1/3^4 + 1/5^4 + 1/7^4 + 1/8^4) * 1/3^2 - 7 + \text{golden ratio}$

Input:

$$\pi^4 \times \frac{1}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}} \times \frac{1}{3^2} - 7 + \phi$$

ϕ is the golden ratio

Result:

$$\phi - 7 + \frac{55\,319\,040\,000 \pi^4}{38\,389\,024\,801}$$

Decimal approximation:

134.9856893591789589959790090039022598257714519434703560612...

134.9856893591... result practically equal to the rest mass of Pion meson 134.9766

Property:

$-7 + \phi + \frac{55\,319\,040\,000 \pi^4}{38\,389\,024\,801}$ is a transcendental number

Alternate forms:

$$\frac{-499\,057\,322\,413 + 38\,389\,024\,801 \sqrt{5} + 110\,638\,080\,000 \pi^4}{76\,778\,049\,602}$$

$$\frac{38\,389\,024\,801 \phi - 268\,723\,173\,607 + 55\,319\,040\,000 \pi^4}{38\,389\,024\,801}$$

$$\frac{38\,389\,024\,801 \phi + 7(7902\,720\,000 \pi^4 - 38\,389\,024\,801)}{38\,389\,024\,801}$$

Alternative representations:

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 - 2 \cos(216^\circ) + \frac{\pi^4}{9 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + 2 \cos\left(\frac{\pi}{5}\right) + \frac{\pi^4}{9 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 - 2 \cos(216^\circ) + \frac{(180^\circ)^4}{9 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)}$$

Series representations:

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{497871360000 \sum_{k=1}^{\infty} \frac{1}{k^4}}{38389024801}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{5310627840000 \sum_{k=0}^{\infty} \frac{1}{(1+2k)^4}}{38389024801}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{14161674240000 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^4}{38389024801}$$

Integral representations:

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{885104640000 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^4}{38389024801}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{885104640000 \left(\int_0^1 \frac{1}{\sqrt{1-t^2}} dt \right)^4}{38389024801}$$

$$\frac{\pi^4}{3^2 \left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} - 7 + \phi = -7 + \phi + \frac{14161674240000 \left(\int_0^1 \sqrt{1-t^2} dt \right)^4}{38389024801}$$

$$\left(\left(\left(\left(\left(\left(\left(\frac{1}{\left(\frac{\pi^4}{\left(\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4} \right)} \right)^{1/15} \right)^{1/64} \right) \right) \right) \right) \right) \right) - \pi / 10^3$$

Input:

$$\sqrt[64]{\sqrt[15]{\sqrt{\frac{1}{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}} - \frac{\pi}{10^3}$$

Exact result:

$$\frac{\sqrt[960]{38\,389\,024\,801}}{\sqrt[80]{2} \sqrt[240]{105\pi}} - \frac{\pi}{1000}$$

Decimal approximation:

0.989446956869959966604428443465641768099347273584635667877...

0.98944695686... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Alternate forms:

$$\frac{100 \times 2^{79/80} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21\pi^{241/240}}{21\,000 \sqrt[240]{\pi}}$$

$$- \frac{\sqrt[80]{2} \sqrt[240]{105} \pi^{241/240} - 1000 \sqrt[960]{38\,389\,024\,801}}{1000 \sqrt[80]{2} \sqrt[240]{105\pi}}$$

Alternative representations:

$$\sqrt[64]{\sqrt[15]{\frac{1}{\sqrt{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}} - \frac{\pi}{10^3} = -\frac{180^\circ}{10^3} + \sqrt[64]{\sqrt[15]{\frac{1}{\sqrt{\frac{(180^\circ)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}}$$

$$\sqrt[64]{\sqrt[15]{\frac{1}{\sqrt{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}} - \frac{\pi}{10^3} = -\frac{\cos^{-1}(-1)}{10^3} + \sqrt[64]{\sqrt[15]{\frac{1}{\sqrt{\frac{\cos^{-1}(-1)^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}}$$

$$\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}} - \frac{\pi}{10^3} = \frac{i \log(-1)}{10^3} + \sqrt[64]{\frac{1}{\sqrt[15]{\frac{(-i \log(-1))^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}}$$

Series representations:

$$\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}} - \frac{\pi}{10^3} = \frac{25 \times 2^{47/48} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^{241/240}}{5250 \sqrt[240]{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}}$$

$$\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}} - \frac{\pi}{10^3} = \left(100 \times 2^{79/80} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\sum_{k=0}^{\infty} \left(-\frac{1}{4} \right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right) \right)^{241/240} \right) / \left(21\,000 \sqrt[240]{\sum_{k=0}^{\infty} \left(-\frac{1}{4} \right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k} \right)} \right)$$

$$\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{\frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{5^4} + \frac{1}{7^4} + \frac{1}{8^4}}}}} - \frac{\pi}{10^3} = \left(100 \times 2^{79/80} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\sum_{k=0}^{\infty} 16^{-k} \left(\frac{1}{-5-8k} - \frac{1}{2+4k} + \frac{4}{1+8k} - \frac{1}{6+8k} \right) \right)^{241/240} \right) / \left(21\,000 \sqrt[240]{\sum_{k=0}^{\infty} 16^{-k} \left(\frac{1}{-5-8k} - \frac{1}{2+4k} + \frac{4}{1+8k} - \frac{1}{6+8k} \right)} \right)$$

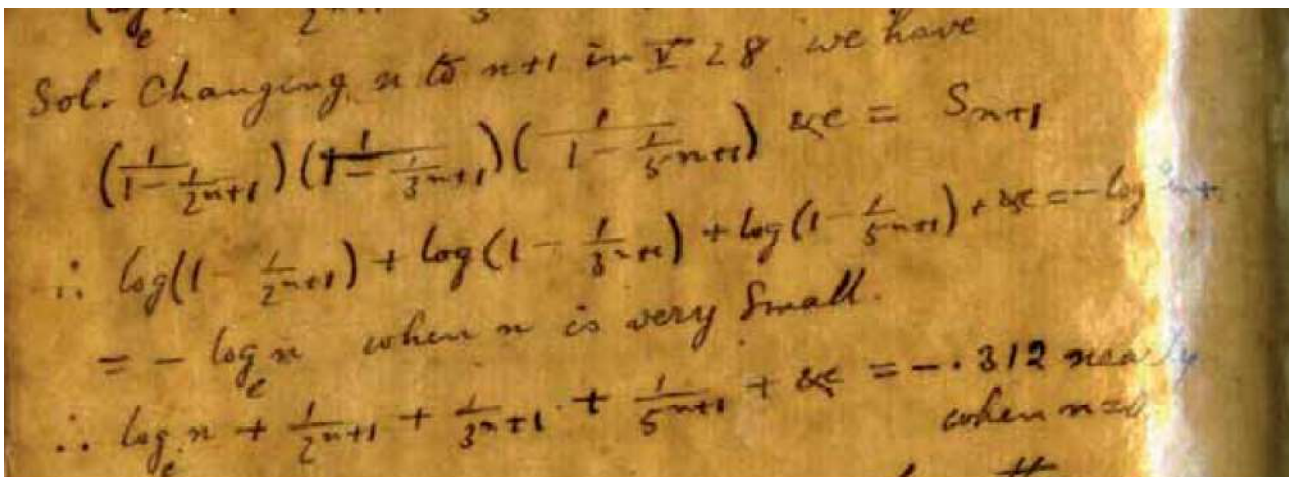
Integral representations:

$$\frac{\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{2^4 + 3^4 + 5^4 + 7^4 + 8^4}}}}} - \frac{\pi}{10^3} = \frac{50 \times 2^{59/60} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\int_0^\infty \frac{1}{1+t^2} dt \right)^{241/240}}{10500 \sqrt[240]{\int_0^\infty \frac{1}{1+t^2} dt}}$$

$$\frac{\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{2^4 + 3^4 + 5^4 + 7^4 + 8^4}}}}} - \frac{\pi}{10^3} = \frac{25 \times 2^{47/48} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\int_0^1 \sqrt{1-t^2} dt \right)^{241/240}}{5250 \sqrt[240]{\int_0^1 \sqrt{1-t^2} dt}}$$

$$\frac{\sqrt[64]{\frac{1}{\sqrt[15]{\frac{\pi^4}{2^4 + 3^4 + 5^4 + 7^4 + 8^4}}}}} - \frac{\pi}{10^3} = \frac{50 \times 2^{59/60} \times 105^{239/240} \sqrt[960]{38\,389\,024\,801} - 21 \left(\int_0^\infty \frac{\sin(t)}{t} dt \right)^{241/240}}{10500 \sqrt[240]{\int_0^\infty \frac{\sin(t)}{t} dt}}$$

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$$\ln 0.352 + 1/(2)^{1.352} + 1/(3)^{1.352} + 1/(5)^{1.352}$$

Input:

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}}$$

$\log(x)$ is the natural logarithm

Result:

-0.312447...

-0.312447...

Alternative representations:

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = \log_e(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}}$$

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = \log(a) \log_a(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}}$$

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = -\text{Li}_1(0.648) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}}$$

Series representations:

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = 0.731677 - \sum_{k=1}^{\infty} \frac{(-1)^k (-0.648)^k}{k}$$

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = 0.731677 + 2i\pi \left[\frac{\arg(0.352 - x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (0.352 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = 0.731677 + \left[\frac{\arg(0.352 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(0.352 - z_0)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (0.352 - z_0)^k z_0^{-k}}{k}$$

Integral representation:

$$\log(0.352) + \frac{1}{2^{1.352}} + \frac{1}{3^{1.352}} + \frac{1}{5^{1.352}} = 0.731677 + \int_1^{0.352} \frac{1}{t} dt$$

From this expression, we obtain also, for $n = 0.0833 = 1/12$:

$$-(((1+34/10^3+\ln 0.0833+ 1/(2)^{1.0833} + 1/(3)^{1.0833}+1/(5)^{1.0833})))$$

Input interpretation:

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right)$$

$\log(x)$ is the natural logarithm

Result:

0.500270...

$$0.500270... \cong 0.5 = 1/2$$

Mathematical connection with Trans-Planckian Censorship and the Swampland (see “Ramanujan mathematics applied to the physics and cosmology”)

$$(((\Gamma(\frac{5}{2}))) * (((2.3e-18)^3)) * 1 / ((2\pi^{4-1/2})) * 1/(((i/ (((\pi^{4-1/2}) * 1/(\Gamma(\frac{5}{2})) * (1/(2.3e-18))^3))))))))))$$

Input interpretation:

$$\Gamma\left(\frac{5}{2}\right)(2.3 \times 10^{-18})^3 \times \frac{1}{2 \pi^{4-1/2}} \times \frac{1}{\frac{i}{\pi^{4-1/2} \times \frac{1}{\Gamma\left(\frac{5}{2}\right)} \left(\frac{1}{2.3 \times 10^{-18}}\right)^3}}$$

$\Gamma(x)$ is the gamma function

i is the imaginary unit

Result:

-0.5 i

Polar coordinates:

$r = 0.5$ (radius), $\theta = -90^\circ$ (angle)

$$0.5 = 1/2$$

Alternative representations:

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1 - \log_e(0.0833) - \frac{1}{2^{1.0833}} - \frac{1}{3^{1.0833}} - \frac{1}{5^{1.0833}} - \frac{34}{10^3}$$

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1 - \log(a) \log_a(0.0833) - \frac{1}{2^{1.0833}} - \frac{1}{3^{1.0833}} - \frac{1}{5^{1.0833}} - \frac{34}{10^3}$$

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1 + \text{Li}_1(0.9167) - \frac{1}{2^{1.0833}} - \frac{1}{3^{1.0833}} - \frac{1}{5^{1.0833}} - \frac{34}{10^3}$$

Series representations:

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1.98504 + \sum_{k=1}^{\infty} \frac{(-1)^k (-0.9167)^k}{k}$$

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1.98504 - 2i\pi \left[\frac{\arg(0.0833 - x)}{2\pi} \right] - \log(x) + \sum_{k=1}^{\infty} \frac{(-1)^k (0.0833 - x)^k x^{-k}}{k} \quad \text{for } x < 0$$

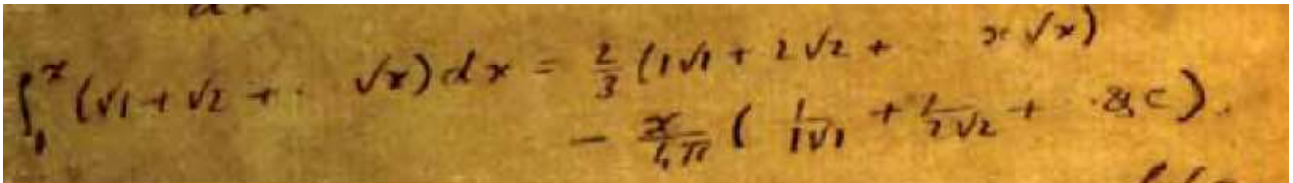
$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) =$$

$$-1.98504 - \left[\frac{\arg(0.0833 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) - \log(z_0) -$$

$$\left[\frac{\arg(0.0833 - z_0)}{2\pi} \right] \log(z_0) + \sum_{k=1}^{\infty} \frac{(-1)^k (0.0833 - z_0)^k z_0^{-k}}{k}$$

Integral representation:

$$-\left(1 + \frac{34}{10^3} + \log(0.0833) + \frac{1}{2^{1.0833}} + \frac{1}{3^{1.0833}} + \frac{1}{5^{1.0833}}\right) = -1.98504 - \int_1^{0.0833} \frac{1}{t} dt$$



$$\frac{2}{3}(1\sqrt{1}+2\sqrt{2}+3\sqrt{3}+x*\sqrt{x})-\frac{x}{(4\pi)}(\frac{1}{(1\sqrt{1})}+\frac{1}{(2\sqrt{2})}+\frac{1}{(3\sqrt{3})})$$

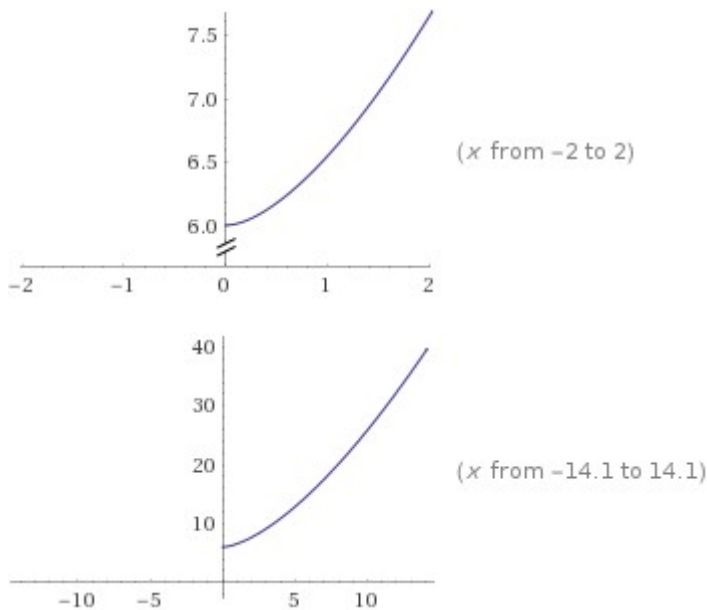
Input:

$$\frac{2}{3} \left(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + x\sqrt{x} \right) - \frac{x}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)$$

Exact result:

$$\frac{2}{3} \left(x^{3/2} + 3\sqrt{3} + 2\sqrt{2} + 1 \right) - \frac{\left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) x}{4\pi}$$

Plots:



Alternate forms:

$$\frac{2}{3} \left(x^{3/2} + 3\sqrt{3} + 2\sqrt{2} + 1 \right) - \frac{(36 + 9\sqrt{2} + 4\sqrt{3})x}{144\pi}$$

$$\frac{96\pi x^{3/2} - 4\sqrt{3}x - 9\sqrt{2}x - 36x + 288\sqrt{3}\pi + 192\sqrt{2}\pi + 96\pi}{144\pi}$$

$$\frac{2}{3} \left(x^{3/2} + \sqrt{35 + 12\sqrt{6}} + 1 \right) + \frac{\left(-6 - \sqrt{\frac{1}{6}(35 + 12\sqrt{6})} \right) x}{24\pi}$$

Expanded form:

$$\frac{2x^{3/2}}{3} - \frac{x}{12\sqrt{3}\pi} - \frac{x}{8\sqrt{2}\pi} - \frac{x}{4\pi} + 2\sqrt{3} + \frac{4\sqrt{2}}{3} + \frac{2}{3}$$

Roots:

$$x = -\frac{-251 - 108\sqrt{2} - 48\sqrt{3} - 12\sqrt{6}}{4608\pi^2} - \frac{(1+i\sqrt{3}) \left(\frac{2}{9216\pi^2} \left(2 \left(82948102 + 56107080\sqrt{2} + 33582240\sqrt{3} + 22348296\sqrt{6} - 27980660736\pi^3 - 18166726656\sqrt{2}\pi^3 - 18933350400\sqrt{3}\pi^3 - 11530321920\sqrt{6}\pi^3 + 3522410053632\pi^6 + 391378894848\sqrt{2}\pi^6 + 587068342272\sqrt{3}\pi^6 + 1174136684544\sqrt{6}\pi^6 + \sqrt{4 \left(147456 \left(108 + 81\sqrt{2} + 112\sqrt{3} + 35\sqrt{6} \right) \pi^3 - \left(-251 - 108\sqrt{2} - 48\sqrt{3} - 12\sqrt{6} \right)^2 \right)^3 + \left(82948102 + 56107080\sqrt{2} + 33582240\sqrt{3} + 22348296\sqrt{6} - 27980660736\pi^3 - 18166726656\sqrt{2}\pi^3 - 18933350400\sqrt{3}\pi^3 - 11530321920\sqrt{6}\pi^3 + 3522410053632\pi^6 + 391378894848\sqrt{2}\pi^6 + 587068342272\sqrt{3}\pi^6 + 1174136684544\sqrt{6}\pi^6 \right)^2} \right) \right)^{1/3} + \left((1-i\sqrt{3}) \left(147456 \left(108 + 81\sqrt{2} + 112\sqrt{3} + 35\sqrt{6} \right) \pi^3 - \left(-251 - 108\sqrt{2} - 48\sqrt{3} - 12\sqrt{6} \right)^2 \right) \right)^{1/3} \right) / \left(4608 \times 2^{2/3} \pi^2 \left(82948102 + 56107080\sqrt{2} + 33582240\sqrt{3} + 22348296\sqrt{6} - 27980660736\pi^3 - 18166726656\sqrt{2}\pi^3 - 18933350400\sqrt{3}\pi^3 - 11530321920\sqrt{6}\pi^3 + 3522410053632\pi^6 + 391378894848\sqrt{2}\pi^6 + 587068342272\sqrt{3}\pi^6 + 1174136684544\sqrt{6}\pi^6 + \sqrt{4 \left(147456 \left(108 + 81\sqrt{2} + 112\sqrt{3} + 35\sqrt{6} \right) \pi^3 - \left(-251 - 108\sqrt{2} - 48\sqrt{3} - 12\sqrt{6} \right)^2 \right)^3 + \left(82948102 + 56107080\sqrt{2} + 33582240\sqrt{3} + 22348296\sqrt{6} - 27980660736\pi^3 - 18166726656\sqrt{2}\pi^3 - 18933350400\sqrt{3}\pi^3 - 11530321920\sqrt{6}\pi^3 + 3522410053632\pi^6 + 391378894848\sqrt{2}\pi^6 + 587068342272\sqrt{3}\pi^6 + 1174136684544\sqrt{6}\pi^6 \right)^2} \right) \right)^{1/3} \right) \approx -2.02771 - 3.97539i$$

Properties as a real function:

Domain

$\{x \in \mathbb{R} : x \geq 0\}$ (all non-negative real numbers)

Range

$\{y \in \mathbb{R} : y \geq 6.01577\}$

\mathbb{R} is the set of real numbers

Derivative:

$$\frac{d}{dx} \left(\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + x\sqrt{x}) - \frac{x \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right) = \sqrt{x} - \frac{36 + 9\sqrt{2} + 4\sqrt{3}}{144\pi}$$

Indefinite integral:

$$\int \left(-\frac{\left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)x}{4\pi} + \frac{2}{3} (1 + 2\sqrt{2} + 3\sqrt{3} + x^{3/2}) \right) dx = \frac{4x^{5/2}}{15} - \frac{(36 + 9\sqrt{2} + 4\sqrt{3})x^2}{288\pi} + \frac{2}{3} (1 + 2\sqrt{2} + 3\sqrt{3})x + \text{constant}$$

Global minimum:

$$\min \left\{ \frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + x\sqrt{x}) - \frac{x \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right\} \approx 6.0158$$

at $x \approx 0.015136$

For $x = 29+4 = 33$, where 29 and 4 are Lucas numbers, we obtain:

Input:

$$\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4}) - \frac{29+4}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) - 3$$

Result:

$$-3 + \frac{2}{3} (1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33}) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}$$

Decimal approximation:

125.3368720059485804490364993979487103187686272298831841702...

125.336872... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Property:

$$-3 + \frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}$$

is a transcendental number

Alternate forms:

$$\frac{-396 - 99\sqrt{2} - 44\sqrt{3} - 112\pi + 64\sqrt{2}\pi + 96\sqrt{3}\pi + 1056\sqrt{33}\pi}{48\pi}$$

$$\frac{1}{3} \left(-7 + 4\sqrt{2} + 6\sqrt{3} + 66\sqrt{33} \right) - \frac{11(36 + 9\sqrt{2} + 4\sqrt{3})}{48\pi}$$

$$-\frac{7}{3} + \frac{4\sqrt{2}}{3} + 2\sqrt{3} + 22\sqrt{33} - \frac{33}{4\pi} - \frac{33}{8\sqrt{2}\pi} - \frac{11}{4\sqrt{3}\pi}$$

$$\frac{2}{3}(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4}) - \frac{(29+4)}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) + 11$$

Where 11 is a Lucas number

Input:

$$\frac{2}{3} \left(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4} \right) - \frac{29+4}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) + 11$$

Result:

$$11 + \frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}$$

Decimal approximation:

139.3368720059485804490364993979487103187686272298831841702...

139.336872... result practically equal to the rest mass of Pion meson 139.57

Property:

$$11 + \frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}$$

is a transcendental number

Alternate forms:

$$\frac{-396 - 99\sqrt{2} - 44\sqrt{3} + 560\pi + 64\sqrt{2}\pi + 96\sqrt{3}\pi + 1056\sqrt{33}\pi}{48\pi}$$

$$\frac{1}{3} \left(35 + 4\sqrt{2} + 6\sqrt{3} + 66\sqrt{33} \right) - \frac{11(36 + 9\sqrt{2} + 4\sqrt{3})}{48\pi}$$

$$\frac{35}{3} + \frac{4\sqrt{2}}{3} + 2\sqrt{3} + 22\sqrt{33} - \frac{33}{4\pi} - \frac{33}{8\sqrt{2}\pi} - \frac{11}{4\sqrt{3}\pi}$$

$$\left[\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4}) - \frac{(29+4)}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right] \times 18 + 123 + 18$$

Where 18, and 123 are Lucas numbers

Input:

$$\left(\frac{2}{3} \left(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4} \right) - \frac{29+4}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right) \times 18 + 123 + 18$$

Result:

$$141 + 18 \left(\frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right)$$

Decimal approximation:

2451.063696107074448082656989163076785737835290137897315063...

[2451.063696...](#) result very near to the rest mass of charmed Sigma baryon 2452.9

Property:

$$141 + 18 \left(\frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right)$$

is a transcendental number

Alternate forms:

$$\frac{3(-396 - 99\sqrt{2} - 44\sqrt{3} + 408\pi + 64\sqrt{2}\pi + 96\sqrt{3}\pi + 1056\sqrt{33}\pi)}{8\pi}$$

$$3(51 + 8\sqrt{2} + 12\sqrt{3} + 132\sqrt{33}) - \frac{33(36 + 9\sqrt{2} + 4\sqrt{3})}{8\pi}$$

$$153 + 24\sqrt{2} + 36\sqrt{3} + 396\sqrt{33} - \frac{297}{2\pi} - \frac{297}{4\sqrt{2}\pi} - \frac{33\sqrt{3}}{2\pi}$$

$$[2/3(1\text{sqrt}1+2\text{sqrt}2+3\text{sqrt}3+(29+4)*\text{sqrt}(29+4))- (29+4)/(4\text{Pi})(1/(1\text{sqrt}1)+1/(2\text{sqrt}2)+1/(3\text{sqrt}3))]*18-521-7$$

Where 521 and 7 are Lucas numbers

Input:

$$\left(\frac{2}{3}(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4}) - \frac{29+4}{4\pi}\left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)\right) \times 18 - 521 - 7$$

Result:

$$18\left(\frac{2}{3}(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33}) - \frac{33\left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)}{4\pi}\right) - 528$$

Decimal approximation:

1782.063696107074448082656989163076785737835290137897315063...

1782.063696... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

Property:

$$-528 + 18\left(\frac{2}{3}(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33}) - \frac{33\left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)}{4\pi}\right)$$

is a transcendental number

Alternate forms:

$$\frac{3(-396 - 99\sqrt{2} - 44\sqrt{3} - 1376\pi + 64\sqrt{2}\pi + 96\sqrt{3}\pi + 1056\sqrt{33}\pi)}{8\pi}$$

$$12(-43 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33}) - \frac{33(36 + 9\sqrt{2} + 4\sqrt{3})}{8\pi}$$

$$-516 + 24\sqrt{2} + 36\sqrt{3} + 396\sqrt{33} - \frac{297}{2\pi} - \frac{297}{4\sqrt{2}\pi} - \frac{33\sqrt{3}}{2\pi}$$

$$[2/3(1\text{sqrt}1+2\text{sqrt}2+3\text{sqrt}3+(29+4)*\text{sqrt}(29+4))- (29+4)/(4\text{Pi})(1/(1\text{sqrt}1)+1/(2\text{sqrt}2)+1/(3\text{sqrt}3))]*18-(521+47+11+2)$$

Where 521, 47, 11 and 2 are Lucas numbers

Input:

$$\left(\frac{2}{3}\left(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4}\right) - \frac{29+4}{4\pi}\left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)\right) \times 18 - (521 + 47 + 11 + 2)$$

Result:

$$18\left(\frac{2}{3}\left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33}\right) - \frac{33\left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}}\right)}{4\pi}\right) - 581$$

Decimal approximation:

1729.063696107074448082656989163076785737835290137897315063...

1729.063696...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Property:

$$-581 + 18 \left(\frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right)$$

is a transcendental number

Alternate forms:

$$\frac{-1188 - 297\sqrt{2} - 132\sqrt{3} - 4552\pi + 192\sqrt{2}\pi + 288\sqrt{3}\pi + 3168\sqrt{33}\pi}{8\pi}$$

$$-569 + 24\sqrt{2} + 36\sqrt{3} + 396\sqrt{33} - \frac{33(36 + 9\sqrt{2} + 4\sqrt{3})}{8\pi}$$

$$-569 + 24\sqrt{2} + 36\sqrt{3} + 396\sqrt{33} - \frac{297}{2\pi} - \frac{297}{4\sqrt{2}\pi} - \frac{33\sqrt{3}}{2\pi}$$

Or:

Input:

$$\left(\frac{2}{3} \left(1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + (29+4)\sqrt{29+4} \right) - \frac{29+4}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right) \\ (21-3) - ((21+3)^2 + 5)$$

Where 3, 5 and 21 are Fibonacci numbers

Result:

$$18 \left(\frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 33\sqrt{33} \right) - \frac{33 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right) - 581$$

Decimal approximation:

1729.063696107074448082656989163076785737835290137897315063...

[1729.063696... as above](#)

$$\frac{1}{\left[\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right]^{1/512}}$$

Input:

$$\frac{1}{\sqrt[512]{\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}}$$

Exact result:

$$\frac{1}{\sqrt[512]{\frac{2}{3} (1 + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}}}}$$

Decimal approximation:

0.995024687328205147621459128813662019348119101347050667697...

0.995024687328... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}}}{1 + \sqrt[5]{\sqrt{\phi^5 \sqrt[4]{5^3}} - 1}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Property:

$$\frac{1}{\sqrt[512]{\frac{2}{3} (1 + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(1 + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}}}}$$
 is a transcendental number

Alternate forms:

$$\frac{1}{\sqrt[512]{\frac{2}{3} \left(1 + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}\right) - \frac{5(36+9\sqrt{2}+4\sqrt{3})}{144\pi}}}$$

$$\frac{1}{\sqrt[128]{2} \sqrt[256]{3} \sqrt[512]{\frac{\pi}{-180 - 45\sqrt{2} - 20\sqrt{3} + 96\pi + 192\sqrt{2}\pi + 288\sqrt{3}\pi + 480\sqrt{5}\pi}}}$$

$$\frac{1}{\sqrt[512]{\frac{1}{6} \left(4 + \sqrt{2 \left(1280 + 240\sqrt{15} + 3\sqrt{\frac{311296}{9} + 20480\sqrt{\frac{5}{3}}}\right)}\right) + \frac{5 \left(-6 - \sqrt{\frac{1}{6}(35+12\sqrt{6})}\right)}{24\pi}}}$$

$1/32 * \log_{0.9950246873282} \left(\frac{1}{\left[\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right]} \right) + 1/\text{golden ratio}$

Input interpretation:

$$\frac{1}{32} \log_{0.9950246873282} \left(\frac{1}{\left(\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5}{4\pi} \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right) \right)} \right) + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

16.618033989...

16.618033989... result very near to the mass of the hypothetical light particle, the boson $m_x = 16.84 \text{ MeV}$

Alternative representation:

$$\frac{1}{32} \log_{0.99502468732820000} \left(\frac{1}{\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}} \right) +$$

$$\frac{1}{\phi} = \frac{1}{\phi} + \frac{\log \left(\frac{1}{-\frac{5 \left(\frac{1}{\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} + \frac{2}{3} (\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5})} \right)}{32 \log(0.99502468732820000)}$$

Series representations:

$$\frac{1}{32} \log_{0.99502468732820000} \left(\frac{1}{\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}} \right) +$$

$$\frac{1}{\phi} = \frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{-\frac{5 \left(\frac{1}{\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} + \frac{2}{3} (\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5})} \right)^k}{k}}{32 \log(0.99502468732820000)}$$

$$\frac{1}{32} \log_{0.99502468732820000} \left(\frac{1}{\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi}} \right) +$$

$$\frac{1}{\phi} = \frac{1.0000000000000000}{\phi} +$$

$$\log \left(\frac{1}{-\frac{5 \left(\frac{1}{\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} + \frac{2}{3} (\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5})} \right)$$

$$\left(-6.2653872823284 - \right.$$

$$\left. 0.0312500000000000 \sum_{k=0}^{\infty} (-0.00497531267180000)^k G(k) \right)$$

for $\left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

$$\frac{1}{32} \log_{0.99502468732820000} \left(\frac{1}{\left(\frac{2}{3} (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) - \frac{5 \left(\frac{1}{1\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} \right)} \right) +$$

$$\frac{1}{\phi} = \frac{1.0000000000000000}{\phi} +$$

$$\log \left(\frac{1}{\left(-\frac{5 \left(\frac{1}{\sqrt{1}} + \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} \right)}{4\pi} + \frac{2}{3} (\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + 5\sqrt{5}) \right)} \right)$$

$$\left(-6.2653872823284 - \right.$$

$$\left. 0.0312500000000000 \sum_{k=0}^{\infty} (-0.00497531267180000)^k G(k) \right)$$

$$\text{for } \left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$$

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Handwritten mathematical derivation on aged paper. The text shows the expansion of a function using partial fractions and the cotangent function. The visible equations are:

$$-\frac{1}{x^2} (1 - 2 + 3 - \dots) + \dots = -\frac{1}{x^2} (1 + 1 + 1 + \dots)$$

$$2 \cdot \frac{1}{1-x^2} + \frac{1}{2-x^2} + \frac{1}{3-x^2} + \dots = -\frac{1}{x^2} (1 + 1 + 1 + \dots)$$

$$-\frac{1}{x^4} (1^4 + 2^4 + 3^4 + \dots) - \frac{1}{x^6} (1^6 + 2^6 + 3^6 + \dots) = \psi(x)$$

$$+\frac{1}{2x^2} = \frac{1}{2x^2} - \frac{\pi \cot \pi x}{2x}$$

For $x = 2$, we obtain:

$$1/(2 \cdot 2^2) - (\pi \cdot \cot 2\pi)/(2 \cdot 2)$$

Input:

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2)\pi}{2 \times 2}$$

$\cot(x)$ is the cotangent function

Exact result:

$$\frac{1}{8} - \frac{1}{4} \pi^2 \cot(2)$$

Decimal approximation:

1.254224753176517190121047578760951314036645305350098136828...

1.2542247531765....

Alternate forms:

$$\frac{1}{8} (1 - 2 \pi^2 \cot(2))$$

$$\frac{1}{8} - \frac{\pi^2 \cos(2)}{4 \sin(2)}$$

$$\frac{1}{8} + \frac{\pi^2 \sin(4)}{4(\cos(4) - 1)}$$

Alternative representations:

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{8} - \frac{\pi^2}{4 \tan(2)}$$

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{4} i \pi^2 \coth(-2 i) + \frac{1}{8}$$

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = -\frac{1}{4} i (\pi^2 \coth(2 i)) + \frac{1}{8}$$

Series representations:

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{8} - \frac{1}{2} \pi^2 \sum_{k=-\infty}^{\infty} \frac{1}{4 - k^2 \pi^2}$$

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{8} + \frac{1}{4} i \pi^2 \sum_{k=-\infty}^{\infty} e^{4 i k} \operatorname{sgn}(k)$$

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{8} - \frac{\pi^2}{8} - \pi^2 \sum_{k=1}^{\infty} \frac{1}{4 - k^2 \pi^2}$$

Integral representation:

$$\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} = \frac{1}{8} + \frac{\pi^2}{4} \int_{\frac{\pi}{2}}^2 \csc^2(t) dt$$

$$0.5\left(\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2\pi)}{2 \times 2}\right)\right)$$

Input:

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right)$$

$\cot(x)$ is the cotangent function

Result:

0.627112376588258595060523789380475657018322652675049068414...

0.62711237658...

Alternative representations:

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.5\left(\frac{1}{8} - \frac{\pi^2}{4 \tan(2)}\right)$$

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.5\left(\frac{1}{4} i \pi^2 \coth(-2i) + \frac{1}{8}\right)$$

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.5\left(-\frac{1}{4} i (\pi^2 \coth(2i)) + \frac{1}{8}\right)$$

Series representations:

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.0625 - 0.25 \pi^2 \sum_{k=-\infty}^{\infty} \frac{1}{4 - k^2 \pi^2}$$

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.0625 + 0.125 i \pi^2 \sum_{k=-\infty}^{\infty} e^{4ik} \operatorname{sgn}(k)$$

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.0625 + 0.125 i \pi^2 + 0.25 i \pi^2 \sum_{k=1}^{\infty} q^{2k} \text{ for } q = e^{2i}$$

Integral representation:

$$0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2}\right) = 0.0625 + 0.125 \pi^2 \int_{\frac{\pi}{2}}^2 \csc^2(t) dt$$

$$\left(\left(\left(\left(0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot 2\pi}{2 \times 2}\right)\right)\right)\right)\right)^{1/64}$$

Input:

$$\sqrt[64]{0.5\left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2)\pi}{2 \times 2}\right)}$$

$\cot(x)$ is the cotangent function

Result:

0.99273543...

0.99273543... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

$2 \cdot \log_{0.99273543} \left(\left(\left(\left(\left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot 2\pi}{2 \times 2} \right) \right) \right) \right) \right) \right) - \pi + 1 / \text{golden ratio}$

Input interpretation:

$$2 \log_{0.99273543} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2)\pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi}$$

Result:

125.476...

125.476... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Alternative representations:

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + 2 \log_{0.992735} \left(0.5 \left(\frac{1}{8} - \frac{\pi^2}{4 \tan(2)} \right) \right) + \frac{1}{\phi}$$

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + 2 \log_{0.992735} \left(0.5 \left(\frac{1}{4} i \pi^2 \coth(-2 i) + \frac{1}{8} \right) \right) + \frac{1}{\phi}$$

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + 2 \log_{0.992735} \left(0.5 \left(-\frac{1}{4} i (\pi^2 \coth(2 i)) + \frac{1}{8} \right) \right) + \frac{1}{\phi}$$

Series representations:

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.992735} \left(0.0625 - 0.25 \pi^2 \sum_{k=-\infty}^{\infty} \frac{1}{4 - k^2 \pi^2} \right)$$

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.992735} \left(0.0625 + 0.125 i \pi^2 \sum_{k=-\infty}^{\infty} e^{4 i k} \operatorname{sgn}(k) \right)$$

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.992735} \left(0.0625 + 0.125 i \pi^2 + 0.25 i \pi^2 \sum_{k=1}^{\infty} q^{2k} \right) \text{ for } q = e^{2i}$$

Integral representation:

$$2 \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.992735} \left(0.0625 + 0.125 \pi^2 \int_{\frac{\pi}{2}}^2 \csc^2(t) dt \right)$$

$1/4 \log$ base 0.99273543 ((((((0.5(((1/(2*2^2) – (Pi*cot 2Pi)/(2*2)))))))))))+1/golden ratio

Input interpretation:

$$\frac{1}{4} \log_{0.99273543} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi}$$

Result:

16.6180...

16.6180... result very near to the mass of the hypothetical light particle, the boson $m_x = 16.84 \text{ MeV}$

Alternative representations:

$$\frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} = \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{8} - \frac{\pi^2}{4 \tan(2)} \right) \right) + \frac{1}{\phi}$$

$$\begin{aligned} \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} = \\ \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{4} i \pi^2 \coth(-2 i) + \frac{1}{8} \right) \right) + \frac{1}{\phi} \end{aligned}$$

$$\begin{aligned} \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} = \\ \frac{1}{4} \log_{0.992735} \left(0.5 \left(-\frac{1}{4} i (\pi^2 \coth(2 i) + \frac{1}{8}) \right) \right) + \frac{1}{\phi} \end{aligned}$$

Series representations:

$$\begin{aligned} \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} = \\ \frac{1}{\phi} + \frac{1}{4} \log_{0.992735} \left(0.0625 - 0.25 \pi^2 \sum_{k=-\infty}^{\infty} \frac{1}{4 - k^2 \pi^2} \right) \end{aligned}$$

$$\begin{aligned} \frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} = \\ \frac{1}{\phi} + \frac{1}{4} \log_{0.992735} \left(0.0625 + 0.125 i \pi^2 \sum_{k=-\infty}^{\infty} e^{4 i k} \operatorname{sgn}(k) \right) \end{aligned}$$

$$\frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{1}{4} \log_{0.992735} \left(0.0625 + 0.125 i \pi^2 + 0.25 i \pi^2 \sum_{k=1}^{\infty} q^{2k} \right) \text{ for } q = e^{2i}$$

Integral representation:

$$\frac{1}{4} \log_{0.992735} \left(0.5 \left(\frac{1}{2 \times 2^2} - \frac{\pi \cot(2) \pi}{2 \times 2} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{1}{4} \log_{0.992735} \left(0.0625 + 0.125 \pi^2 \int_{\frac{\pi}{2}}^2 \csc^2(t) dt \right)$$

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$$3 * (((1/(1+10/9) + 1/(1+(10/9)^2) + 1/(1+(10/9)^3) + 1/(1+(10/9)^4) + 1/(1+(10/9)^5))))$$

Input:

$$3 \left(\frac{1}{1 + \frac{10}{9}} + \frac{1}{1 + \left(\frac{10}{9}\right)^2} + \frac{1}{1 + \left(\frac{10}{9}\right)^3} + \frac{1}{1 + \left(\frac{10}{9}\right)^4} + \frac{1}{1 + \left(\frac{10}{9}\right)^5} \right)$$

Exact result:

$$\frac{274660021421055}{43384786764319}$$

Decimal approximation:

6.330791088431577974847329057763804618029615684913650820416...

6.33079108843...

$$\left(\frac{5}{(21-2)} \right) * 3 * (((1/(1+10/9) + 1/(1+(10/9)^2) + 1/(1+(10/9)^3) + 1/(1+(10/9)^4) + 1/(1+(10/9)^5)))) + 7/10^3$$

Where 7 is a Lucas number

Input:

$$\frac{5}{21-2} \times 3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right) + \frac{7}{10^3}$$

Exact result:

$$\frac{1\ 379\ 070\ 283\ 744\ 929\ 427}{824\ 310\ 948\ 522\ 061\ 000}$$

Decimal approximation:

1.672997654850415256538770804674685425797267285503592321162...

1.672997654... result very near to the proton mass

$$1/ [3(((1/(1+10/9)+1/(1+(10/9)^2) + 1/(1+(10/9)^3) + 1/(1+(10/9)^4)+1/(1+(10/9)^5))))]^{1/256}$$

Input:

$$\frac{1}{\sqrt[256]{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)}}$$

Result:

$$\frac{\sqrt[256]{\frac{43384\ 786\ 764\ 319}{10\ 172\ 593\ 385\ 965}}}{3^{3/256}}$$

Decimal approximation:

0.992817228101858669753657924300494131952884012295137331033...

0.992817228101... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Alternate form:

$$\frac{\sqrt[256]{43\,384\,786\,764\,319} \cdot 3^{253/256} \times 10\,172\,593\,385\,965^{255/256}}{30\,517\,780\,157\,895}$$

1/2*log base 0.9928172281(((1/ [3(((1/(1+10/9)+1/(1+(10/9)^2) + 1/(1+(10/9)^3) + 1/(1+(10/9)^4)+1/(1+(10/9)^5))))])))-Pi+1/golden ratio

Input interpretation:

$$\frac{1}{2} \log_{0.9928172281} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right)^{-\pi + \frac{1}{\phi}}$$

Result:

125.4764413019181575498316994162801404138567605155344181607...

125.4764413... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

Alternative representation:

$$\frac{1}{2} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right)^{-\pi + \frac{1}{\phi}} =$$

$$-\pi + \frac{1}{\phi} + \frac{\log \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right)}{2 \log(0.992817)}$$

Series representations:

$$\frac{1}{2} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{231\ 275\ 234\ 656\ 736}{274\ 660\ 021\ 421\ 055} \right)^k}{k}}{2 \log(0.992817)}$$

$$\frac{1}{2} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - 69.361 \log \left(\frac{43\ 384\ 786\ 764\ 319}{274\ 660\ 021\ 421\ 055} \right) -$$

$$\frac{1}{2} \log \left(\frac{43\ 384\ 786\ 764\ 319}{274\ 660\ 021\ 421\ 055} \right) \sum_{k=0}^{\infty} (-0.00718277)^k G(k)$$

for $\left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

1/16*log base 0.9928172281((((1/ [3(((1/(1+10/9))+1/(1+(10/9)^2) + 1/(1+(10/9)^3) + 1/(1+(10/9)^4)+1/(1+(10/9)^5)))))])))+1/golden ratio

Input interpretation:

$$\frac{1}{16} \log_{0.9928172281} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

16.618034...

16.618034... result very near to the mass of the hypothetical light particle, the boson $m_X = 16.84 \text{ MeV}$

Alternative representation:

$$\frac{1}{16} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{\log \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right)}{16 \log(0.992817)}$$

Series representations:

$$\frac{1}{16} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-\frac{231 \ 275 \ 234 \ 656 \ 736}{274 \ 660 \ 021 \ 421 \ 055} \right)^k}{k}}{16 \log(0.992817)}$$

$$\frac{1}{16} \log_{0.992817} \left(\frac{1}{3 \left(\frac{1}{1+\frac{10}{9}} + \frac{1}{1+(\frac{10}{9})^2} + \frac{1}{1+(\frac{10}{9})^3} + \frac{1}{1+(\frac{10}{9})^4} + \frac{1}{1+(\frac{10}{9})^5} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - 8.67013 \log \left(\frac{43 \ 384 \ 786 \ 764 \ 319}{274 \ 660 \ 021 \ 421 \ 055} \right) -$$

$$0.0625 \log \left(\frac{43 \ 384 \ 786 \ 764 \ 319}{274 \ 660 \ 021 \ 421 \ 055} \right) \sum_{k=0}^{\infty} (-0.00718277)^k G(k)$$

for $\left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

Or, precisely:

$$1/(1+10/9)+1/(1+(10/9)^2) + 1/(1+(10/9)^3) +...$$

Input interpretation:

$$\frac{1}{1 + \frac{10}{\phi}} + \frac{1}{1 + \left(\frac{10}{\phi}\right)^2} + \frac{1}{1 + \left(\frac{10}{\phi}\right)^3} + \dots$$

Infinite sum:

$$\sum_{n=1}^{\infty} \frac{1}{\left(\frac{10}{\phi}\right)^n + 1} = \frac{i \operatorname{Im}\left(\psi\left(\frac{\phi}{10}\right)\left(1 - \frac{i\pi}{\log\left(\frac{10}{\phi}\right)}\right)\right)}{\log\left(\frac{10}{\phi}\right)} + \frac{\operatorname{Re}\left(\psi\left(\frac{\phi}{10}\right)\left(1 - \frac{i\pi}{\log\left(\frac{10}{\phi}\right)}\right)\right)}{\log\left(\frac{10}{\phi}\right)} - \frac{\log(10)}{\log\left(\frac{10}{\phi}\right)}$$

Decimal approximation:

6.331008692864745537718386879838180649341260412564743295777...

6.33100869286... = 2πr, with r = 1.0076113282271...

Note that from 1/r, we obtain:

1/1.0076113282271832

Input interpretation:

$$\frac{1}{1.0076113282271832}$$

Result:

0.992446166479117733848602881177141829359184370297518673158...

0.992446166... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = φ**

this result could mean that the dilaton, obtained by inverting the formula of a circumference of radius 1.0076113282271 ..., is a string having the perimeter of an ellipse

Possible closed forms:

$$\frac{35\,120\,413\,\pi}{111\,173\,820} \approx 0.9924461664791177555958365080$$

$$\frac{1}{8} \pi \tan^2\left(\frac{335\,710}{332\,617}\right) \approx 0.992446166479117919504391902$$

$$\frac{1}{52} (10 e^\pi + 10 \pi + 235 \log(\pi) - 150 \log(2 \pi) - 162 \tan^{-1}(\pi)) \approx 0.99244616647911823295276205$$

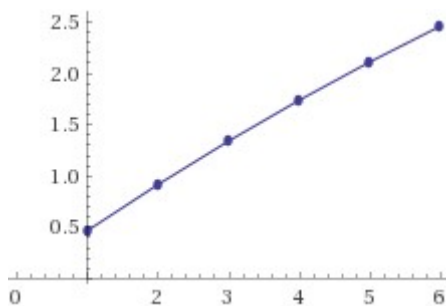
Convergence tests:

By the ratio test, the series converges.

Partial sum formula:

$$\sum_{n=1}^m \frac{1}{1 + \left(\frac{10}{\varrho}\right)^n} = \frac{\psi_{\frac{\varrho}{10}}^{(0)}\left(-\frac{i\pi - \log\left(\frac{10}{\varrho}\right)}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)} - \frac{\psi_{\frac{\varrho}{10}}^{(0)}\left(-\frac{i\pi - (m+1)\log\left(\frac{10}{\varrho}\right)}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)}$$

Partial sums:



Alternate forms:

$$\frac{\log(10) - \psi_{\frac{\varrho}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)}$$

$$-\frac{\log(10)}{\log\left(\frac{10}{\varrho}\right)} + \frac{\psi_{\frac{\varrho}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)}$$

$$\frac{-\log(10) + \psi_{\frac{10}{9}}^{(0)} \left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)} \right)}{\log(10) - 2\log(3)}$$

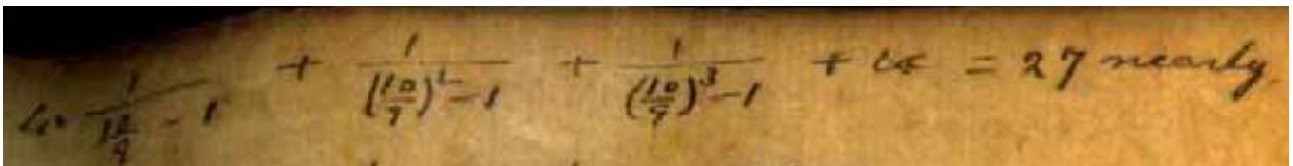
Series representations:

$$\begin{aligned} & \frac{i \operatorname{Im} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} - \frac{\log(10)}{\log\left(\frac{10}{9}\right)} + \frac{\operatorname{Re} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} = \\ & - \left(\left(2\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - \operatorname{Im} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) \right) \right) - \right. \\ & \left. i \log(x) + i \operatorname{Re} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) \right) \right) + \\ & \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) / \\ & \left(2\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) \text{ for } x < 0 \end{aligned}$$

$$\begin{aligned}
& \frac{i \operatorname{Im} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} - \frac{\log(10)}{\log\left(\frac{10}{9}\right)} + \frac{\operatorname{Re} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} = \\
& - \left(\left(2 \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \pi} \right] - \operatorname{Im} \left[\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right) \right] \right) \right. \\
& \quad \left. \frac{i \pi}{2 i \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)} - i \log(z_0) + \right. \\
& \quad \left. i \operatorname{Re} \left[\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i \pi}{2 i \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)} \right] \right) + \\
& \quad \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \\
& \quad \left(2 \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2 \pi} \right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{i \operatorname{Im} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} - \frac{\log(10)}{\log\left(\frac{10}{9}\right)} + \frac{\operatorname{Re} \left(\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log\left(\frac{10}{9}\right)} = \\
& \left(i \operatorname{Im} \left(\psi_{\frac{10}{9}}^{(0)} \left[1 - \frac{i\pi}{\log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right] \right) - \right. \\
& \quad \left. \left\lfloor \frac{\arg(10 - z_0)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) - \log(z_0) - \left\lfloor \frac{\arg(10 - z_0)}{2\pi} \right\rfloor \log(z_0) + \right. \\
& \quad \left. \operatorname{Re} \left(\psi_{\frac{10}{9}}^{(0)} \left[1 - \frac{i\pi}{\log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right] \right) + \right. \\
& \quad \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(\left\lfloor \frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right\rfloor \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right\rfloor \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)
\end{aligned}$$

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(((1/((10/9)^1-1) + 1/((10/9)^2-1) + 1/((10/9)^3-1) + ...)))

Input interpretation:

$$\frac{1}{\left(\frac{10}{9}\right)^1 - 1} + \frac{1}{\left(\frac{10}{9}\right)^2 - 1} + \frac{1}{\left(\frac{10}{9}\right)^3 - 1} + \dots$$

Infinite sum:

$$\sum_{n=1}^{\infty} \frac{1}{\left(\frac{10}{9}\right)^n - 1} = \frac{\log(10) - \frac{\psi_{\frac{10}{9}}^{(0)}(1)}{10}}{\log\left(\frac{10}{9}\right)}$$

$\log(x)$ is the natural logarithm

$\psi_q(z)$ gives the q -digamma function

Decimal approximation:

27.08648503406816780327872576570091022140786017495536508019...

27.08648503... note that the square of result is:

733.6776712804141009 $\approx 729 = 9^3$ (Ramanujan cube $9^3 - 1$)

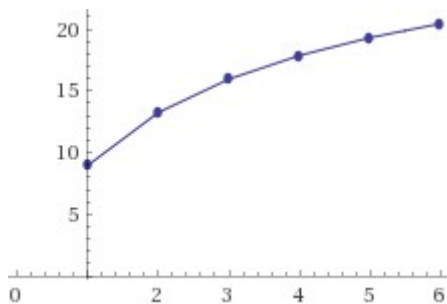
Convergence tests:

By the ratio test, the series converges.

Partial sum formula:

$$\sum_{n=1}^m \frac{1}{-1 + \left(\frac{10}{9}\right)^n} = \frac{\frac{\psi_{\frac{10}{9}}^{(0)}(m+1)}{10}}{\log\left(\frac{10}{9}\right)} - \frac{\frac{\psi_{\frac{10}{9}}^{(0)}(1)}{10}}{\log\left(\frac{10}{9}\right)}$$

Partial sums:



Alternate forms:

$$\frac{\frac{\psi_{\frac{10}{9}}^{(0)}(1) - \log(10)}{10}}{\log(10) - 2 \log(3)}$$

$$\frac{\log(10)}{\log\left(\frac{10}{9}\right)} - \frac{\frac{\psi_{\frac{10}{9}}^{(0)}(1)}{10}}{\log\left(\frac{10}{9}\right)}$$

$$-\frac{\frac{\psi_{\frac{10}{9}}^{(0)}(1)}{10}}{\log(2) - 2 \log(3) + \log(5)} + \frac{\log(2)}{\log(2) - 2 \log(3) + \log(5)} + \frac{\log(5)}{\log(2) - 2 \log(3) + \log(5)}$$

Series representations:

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} = \frac{2\pi \left[\frac{\arg(10-x)}{2\pi} \right] - i \log(x) + i \psi_{\frac{10}{9}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k}}{2\pi \left[\frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right] - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k}} \quad \text{for } x < 0$$

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} = \frac{2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \psi_{\frac{10}{9}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10-z_0)^k z_0^{-k}}{k}}{2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-z_0\right)^k z_0^{-k}}{k}}$$

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} = \frac{\left[\frac{\arg(10-z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(10-z_0)}{2\pi} \right] \log(z_0) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10-z_0)^k z_0^{-k}}{k}}{\left[\frac{\arg\left(\frac{10}{9}-z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg\left(\frac{10}{9}-z_0\right)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-z_0\right)^k z_0^{-k}}{k}}$$

And:

$$\left(\left(\frac{1}{\left(\frac{10}{9}\right)^1 - 1} + \frac{1}{\left(\frac{10}{9}\right)^2 - 1} + \frac{1}{\left(\frac{10}{9}\right)^3 - 1} + \dots \right) \right)^2 + 10^3$$

Input interpretation:

$$\left(\frac{1}{\left(\frac{10}{9}\right)^1 - 1} + \frac{1}{\left(\frac{10}{9}\right)^2 - 1} + \frac{1}{\left(\frac{10}{9}\right)^3 - 1} + \dots \right)^2 + 10^3$$

Result:

$$\frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1) \right)^2}{\log^2\left(\frac{10}{9}\right)} + 1000$$

$\log(x)$ is the natural logarithm

$\psi_q(z)$ gives the q -digamma function

Alternate forms:

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1)^2 - 2\psi_{\frac{9}{10}}^{(0)}(1)\log(10) + 1000\log^2\left(\frac{10}{9}\right) + \log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

$$-\frac{2\psi_{\frac{9}{10}}^{(0)}(1)\log(10)}{\log^2\left(\frac{10}{9}\right)} + \frac{\psi_{\frac{9}{10}}^{(0)}(1)^2}{\log^2\left(\frac{10}{9}\right)} + 1000 + \frac{\log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

$$\frac{1}{(\log(10) - 2\log(3))^2}$$

$$\left(\psi_{\frac{9}{10}}^{(0)}(1)^2 - 2\psi_{\frac{9}{10}}^{(0)}(1)\log(10) + 1001\log^2(2) + 4000\log^2(3) + 1001\log^2(5) - 2\log(2)(2000\log(3) - 1001\log(5)) - 4000\log(3)\log(5)\right)$$

Thence:

$$1000 + (\log(10) - \text{QPolyGamma}(0, 1, 9/10))^2 / (\log^2(10/9)) - 5$$

Input:

$$1000 + \frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5$$

Exact result:

$$\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} + 995$$

Decimal approximation:

1728.677671500798833522624370015899637519935597740039029216...

1728.677671...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–

Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternate forms:

$$\frac{\psi_{\frac{10}{9}}^{(0)}(1)^2 - 2\psi_{\frac{10}{9}}^{(0)}(1)\log(10) + 995\log^2\left(\frac{10}{9}\right) + \log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

$$- \frac{2\psi_{\frac{10}{9}}^{(0)}(1)\log(10)}{\log^2\left(\frac{10}{9}\right)} + \frac{\psi_{\frac{10}{9}}^{(0)}(1)^2}{\log^2\left(\frac{10}{9}\right)} + 995 + \frac{\log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

$$\frac{1}{(\log(10) - 2\log(3))^2}$$

$$\left(\psi_{\frac{10}{9}}^{(0)}(1)^2 - 2\psi_{\frac{10}{9}}^{(0)}(1)\log(10) + 4(249\log^2(2) + 995\log^2(3) + 249\log^2(5) - 995\log(3)\log(5) + \log(2)(498\log(5) - 995\log(3))) \right)$$

Alternative representations:

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 = 995 + \frac{\left(\log_e(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log_e^2\left(\frac{10}{9}\right)}$$

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 = 995 + \frac{\left(\log(a)\log_a(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\left(\log(a)\log_a\left(\frac{10}{9}\right)\right)^2}$$

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 = 995 + \frac{\left(-\text{Li}_1(-9) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\left(-\text{Li}_1\left(1 - \frac{10}{9}\right)\right)^2}$$

Series representations:

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 =$$

$$995 + \frac{\left(2i\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor + \log(x) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right)^2}{\left(2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right)^2} \quad \text{for } x < 0$$

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 =$$

$$995 + \frac{\left(2i\pi \left\lfloor \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right\rfloor + \log(z_0) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10-z_0)^k z_0^{-k}}{k} \right)^2}{\left(2i\pi \left\lfloor \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right\rfloor + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-z_0\right)^k z_0^{-k}}{k} \right)^2}$$

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 =$$

$$995 + \frac{\left(\log(z_0) + \left\lfloor \frac{\arg(10-z_0)}{2\pi} \right\rfloor \right) \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10-z_0)^k z_0^{-k}}{k} \right)^2}{\left(\log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{9}-z_0\right)}{2\pi} \right\rfloor \right) \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-z_0\right)^k z_0^{-k}}{k} \right)^2}$$

Integral representations:

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 =$$

$$\frac{995 \left(\int_1^{\frac{10}{9}} \frac{1}{t} dt \right)^2 + \left(\int_1^{10} \frac{1}{t} dt \right)^2 - 2 \psi_{\frac{10}{9}}^{(0)}(1) \int_1^{10} \frac{1}{t} dt + \psi_{\frac{10}{9}}^{(0)}(1)^2}{\left(\int_1^{\frac{10}{9}} \frac{1}{t} dt \right)^2}$$

$$1000 + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)^2}{\log^2\left(\frac{10}{9}\right)} - 5 =$$

$$\left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds\right)^2 + 995 \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds\right)^2 -$$

$$\left(4i\pi \psi_{\frac{10}{9}}^{(0)}(1) \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 4\pi^2 \psi_{\frac{10}{9}}^{(0)}(1)^2\right) /$$

$$\left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds\right)^2 \text{ for } -1 < \gamma < 0$$

Multiplying the two results, we obtain:

$$(\log(10) - \text{QPolyGamma}(0, 1, 9/10))/\log(10/9) * -(\log(10) - \text{QPolyGamma}(0, 1 - (i\pi)/\log(10/9), 9/10))/\log(10/9)$$

Input:

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} \left(-\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} \right)$$

Exact result:

$$\frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right) \left(-\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)}{\log^2\left(\frac{10}{9}\right)}$$

Decimal approximation:

171.4847722098364035487584754523969975126548558627298626191...

171.4847722098...

Alternate forms:

$$-\frac{\log(10) \left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)}{\log^2\left(\frac{10}{9}\right)} + \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right) \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)}$$

$$\frac{\left(\psi_{\frac{9}{10}}^{(0)}(1) - \log(10)\right) \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)}\right)\right)}{(\log(10) - 2\log(3))^2}$$

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1) \log(10)}{\log^2\left(\frac{10}{9}\right)} + \frac{\log(10) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)} - \frac{\psi_{\frac{9}{10}}^{(0)}(1) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)} - \frac{\log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

Alternative representations:

$$\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} =$$

$$\left(\frac{1}{\log_e\left(\frac{10}{9}\right)}\right)^2 \left(\log_e(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \left(-\log_e(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log_e\left(\frac{10}{9}\right)}\right)\right)$$

$$-\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} = \left(\frac{1}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)^2$$

$$\left(\log(a) \log_a(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \left(-\log(a) \log_a(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)\right)$$

$$-\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} =$$

$$\left(-\frac{1}{\text{Li}_1\left(1 - \frac{10}{9}\right)}\right)^2 \left(-\text{Li}_1(-9) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \left(\text{Li}_1(-9) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\text{Li}_1\left(1 - \frac{10}{9}\right)}\right)\right)$$

Series representations:

$$\begin{aligned}
 & - \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1) \right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} = \\
 & - \left(\left(2\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - i \log(x) + i \psi_{\frac{10}{9}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \right. \\
 & \quad \left(2\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - i \log(x) + \right. \\
 & \quad \left. \left. i \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) + \right. \right. \\
 & \quad \left. \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \right) / \\
 & \quad \left(2\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right)^2 \right) \text{ for } x < 0
 \end{aligned}$$

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{10}{\vartheta}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{\vartheta}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{\vartheta}}^{(0)}(1) \right)}{\log\left(\frac{10}{\vartheta}\right) \log\left(\frac{10}{\vartheta}\right)} = \\
& - \left(\left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \psi_{\frac{10}{\vartheta}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right. \\
& \quad \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + \right. \\
& \quad \left. i \psi_{\frac{10}{\vartheta}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\vartheta} - z_0\right)^k z_0^{-k}}{k}} \right) \right. \\
& \quad \left. \left. + i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right) / \\
& \quad \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\vartheta} - z_0\right)^k z_0^{-k}}{k} \right)^2 \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right)\log\left(\frac{10}{9}\right)} = \\
& - \left(\left(\left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \right. \\
& \quad \left. \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \\
& \left(\left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \psi_{\frac{10}{9}}^{(0)} \left(1 - \right. \right. \\
& \quad \left. \left. \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right) \right. \\
& \quad \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right) / \left(\left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \right. \\
& \quad \left. \log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)^2 \right)
\end{aligned}$$

Integral representations:

$$\begin{aligned}
& \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)\left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right)\log\left(\frac{10}{9}\right)} = \\
& \frac{\left(\int_1^{10} \frac{1}{t} dt - \psi_{\frac{10}{9}}^{(0)}(1)\right)\left(\int_1^{10} \frac{1}{t} dt - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\int_1^{\frac{10}{9}} \frac{1}{t} dt}\right)\right)}{\left(\int_1^{\frac{10}{9}} \frac{1}{t} dt\right)^2}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1) \right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} = \\
& - \left(\left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{9}{10}}^{(0)}(1) \right) \right. \\
& \quad \left. \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{9}{10}}^{(0)} \left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \right) \right) \right) / \\
& \quad \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right)^2 \text{ for } -1 < \gamma < 0
\end{aligned}$$

And:

$$(\log(10) - \text{QPolyGamma}(0, 1, 9/10))/\log(10/9) * -(\log(10) - \text{QPolyGamma}(0, 1 - (i\pi)/\log(10/9), 9/10))/\log(10/9) - 29 - 7$$

Where 29 and 7 are Lucas number

Input:

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} \left(- \frac{\log(10) - \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right)}{\log\left(\frac{10}{9}\right)} \right) - 29 - 7$$

Exact result:

$$-36 + \frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1) \right) \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log^2\left(\frac{10}{9}\right)}$$

Decimal approximation:

135.4847722098364035487584754523969975126548558627298626191...

135.4847722098... result very near to the rest mass of Pion meson 134.9766

Alternate forms:

$$\begin{aligned}
 & -\frac{\psi_{\frac{9}{10}}^{(0)}(1) \log(10) + 36 \log^2\left(\frac{10}{9}\right) + \log^2(10)}{\log^2\left(\frac{10}{9}\right)} + \frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)} \\
 & -\frac{1}{\log^2\left(\frac{10}{9}\right)} \left(-\psi_{\frac{9}{10}}^{(0)}(1) \log(10) - \log(10) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) + \right. \\
 & \quad \left. \psi_{\frac{9}{10}}^{(0)}(1) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) + 36 \log^2\left(\frac{10}{9}\right) + \log^2(10) \right) \\
 & -\frac{1}{(\log(10) - 2 \log(3))^2} \\
 & \left(-\psi_{\frac{9}{10}}^{(0)}(1) \log(10) + \left(\psi_{\frac{9}{10}}^{(0)}(1) - \log(10) \right) \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2 \log(3) + \log(10)}{-2 \log(3) + \log(10)}\right) + 37 \log^2(2) + \right. \\
 & \quad \left. 144 \log^2(3) + 37 \log^2(5) - 2 \log(2) (72 \log(3) - 37 \log(5)) - 144 \log(3) \log(5) \right)
 \end{aligned}$$

Expanded form:

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1) \log(10)}{\log^2\left(\frac{10}{9}\right)} + \frac{\log(10) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)} - \frac{\psi_{\frac{9}{10}}^{(0)}(1) \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log^2\left(\frac{10}{9}\right)} - 36 - \frac{\log^2(10)}{\log^2\left(\frac{10}{9}\right)}$$

Alternative representations:

$$\begin{aligned}
 & -\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} - 29 - 7 = \\
 & -36 + \left(\frac{1}{\log_e\left(\frac{10}{9}\right)}\right)^2 \left(\log_e(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \left(-\log_e(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log_e\left(\frac{10}{9}\right)}\right)\right) \\
 & -\frac{\left(\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} - 29 - 7 = \\
 & -36 + \left(\frac{1}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)^2 \left(\log(a) \log_a(10) - \psi_{\frac{9}{10}}^{(0)}(1)\right) \\
 & \quad \left(-\log(a) \log_a(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)\right)
 \end{aligned}$$

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1) \right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} - 29 - 7 = \\
& -36 + \left(-\frac{1}{\text{Li}_1\left(1 - \frac{10}{9}\right)} \right)^2 \left(-\text{Li}_1(-9) - \psi_{\frac{10}{9}}^{(0)}(1) \right) \left(\text{Li}_1(-9) + \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\text{Li}_1\left(1 - \frac{10}{9}\right)} \right) \right)
\end{aligned}$$

Series representations:

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1) \right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} - 29 - 7 = \\
& -36 + \left(\left(2i\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor + \log(x) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \right. \\
& \left. \left(-2i\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - \log(x) + \right. \right. \\
& \left. \left. \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) \right) + \right. \\
& \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \right) / \\
& \left(2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right)^2 \text{ for } x < 0
\end{aligned}$$

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{10}{\vartheta}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{\vartheta}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{\vartheta}}^{(0)}(1) \right)}{\log\left(\frac{10}{\vartheta}\right) \log\left(\frac{10}{\vartheta}\right)} - 29 - 7 = \\
& -36 + \left(\log(z_0) + \left\lfloor \frac{\arg(10 - z_0)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \psi_{\frac{10}{10}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \\
& \left(-\log(z_0) - \left\lfloor \frac{\arg(10 - z_0)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) + \psi_{\frac{10}{10}}^{(0)} \left(\right. \right. \\
& \left. \left. 1 - \frac{i\pi}{\log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{\vartheta} - z_0\right)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\vartheta} - z_0\right)^k z_0^{-k}}{k} \right) \right) + \\
& \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right) / \\
& \left(\log(z_0) + \left\lfloor \frac{\arg\left(\frac{10}{\vartheta} - z_0\right)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\vartheta} - z_0\right)^k z_0^{-k}}{k} \right)^2
\end{aligned}$$

$$\begin{aligned}
& - \frac{\left(\log(10) - \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \left(\log(10) - \psi_{\frac{10}{9}}^{(0)}(1) \right)}{\log\left(\frac{10}{9}\right) \log\left(\frac{10}{9}\right)} - 29 - 7 = \\
& -36 + \left(2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \\
& \left(-2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - \log(z_0) + \right. \\
& \left. \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right) + \right. \\
& \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)^2
\end{aligned}$$

Dividing the two results, we obtain:

$$\begin{aligned}
& (((1/((10/9)^1-1) + 1/((10/9)^2-1) + 1/((10/9)^3-1) + \dots))) / \\
& (((1/(1+10/9) + 1/(1+(10/9)^2) + 1/(1+(10/9)^3) + \dots)))
\end{aligned}$$

Input interpretation:

$$\frac{\frac{1}{\left(\frac{10}{9}\right)^1-1} + \frac{1}{\left(\frac{10}{9}\right)^2-1} + \frac{1}{\left(\frac{10}{9}\right)^3-1} + \dots}{\frac{1}{1+\frac{10}{9}} + \frac{1}{1+\left(\frac{10}{9}\right)^2} + \frac{1}{1+\left(\frac{10}{9}\right)^3} + \dots}$$

Result:

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

$\log(x)$ is the natural logarithm

$\psi_q(z)$ gives the q -digamma function

Alternate forms:

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1) - \log(10)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)}\right)}$$

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} - \frac{\log(10)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

$(\log(10) - \text{QPolyGamma}(0, 1, 9/10))/(-\log(10) + \text{QPolyGamma}(0, 1 - (i\pi)/\log(10/9), 9/10))$

Input:

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

Decimal approximation:

4.278383800767091807827635053107807949599048192974066311525...

4.2783838007...

Alternate forms:

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1) - \log(10)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)}\right)}$$

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} - \frac{\log(10)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}$$

Alternative representations:

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} = \frac{\log_e(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log_e(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log_e\left(\frac{10}{9}\right)}\right)}$$

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} = \frac{\log(a) \log_a(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(a) \log_a(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)}$$

$$\frac{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}{-\log(10) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} = \frac{-\text{Li}_1(-9) - \psi_{\frac{9}{10}}^{(0)}(1)}{\text{Li}_1(-9) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\text{Li}_1\left(1 - \frac{10}{9}\right)}\right)}$$

Series representations:

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{-\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)} =$$

$$-\left(2\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - i \log(x) + i \psi_{\frac{10}{9}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) /$$

$$\left(2\pi \left\lfloor \frac{\arg(10-x)}{2\pi} \right\rfloor - i \log(x) + \right.$$

$$\left. i \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k}}\right) + \right.$$

$$\left. i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \text{ for } x < 0$$

$$\begin{aligned}
& \frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{10} = \\
& -\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) \\
& - \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \psi_{\frac{10}{9}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + \right. \\
& \left. i \psi_{\frac{10}{9}}^{(0)} \left[1 - \frac{i\pi}{2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right] + \right. \\
& \left. \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{10} = \\
& -\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) \\
& - \left(\left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \right. \\
& \quad \left. \psi_{\frac{10}{9}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(\left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \right. \\
& \quad \left. \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right) - \right. \\
& \quad \left. \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right)
\end{aligned}$$

Integral representations:

$$\begin{aligned}
& \frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{10} = - \frac{\int_1^{10} \frac{1}{t} dt - \psi_{\frac{10}{9}}^{(0)}(1)}{10} \\
& -\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) = \frac{\int_1^{10} \frac{1}{t} dt - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\int_1^{\frac{10}{9}} \frac{1}{t} dt}\right)}{\int_1^{10} \frac{1}{t} dt - \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\int_1^{\frac{10}{9}} \frac{1}{t} dt}\right)} \\
& \frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{10} = \\
& -\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) \\
& - \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\varrho^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{10}{9}}^{(0)}(1)}{10} \quad \text{for } -1 < \gamma < 0 \\
& - \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\varrho^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{10}{9}}^{(0)}\left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\varrho^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}\right)}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\varrho^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{10}{9}}^{(0)}\left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\varrho^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}\right)}
\end{aligned}$$

And:

$$7 * ((((-\log(10) + \text{QPolyGamma}(0, 1 - (i \pi) / \log(10/9), 9/10)) / (\log(10) - \text{QPolyGamma}(0, 1, 9/10)))) - 18/10^3$$

Where 7 and 18 are Lucas numbers

Input:

$$7 \times \frac{-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3}$$

Exact result:

$$-\frac{9}{500} + \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)}$$

Decimal approximation:

1.618131849308361877648675866122824745830417908174497998899...

1.618131849... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Alternate forms:

$$\frac{-9 \psi_{\frac{9}{10}}^{(0)}(1) - 3500 \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right) + 3509 \log(10)}{500 \left(\log(10) - \psi_{\frac{9}{10}}^{(0)}(1) \right)}$$

$$-\frac{7 \log(10)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} + \frac{7 \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i \pi}{\log\left(\frac{10}{9}\right)} \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{9}{500}$$

$$\frac{9 \psi_{\frac{9}{10}}^{(0)}(1) + 3500 \psi_{\frac{9}{10}}^{(0)} \left(\frac{-i \pi - 2 \log(3) + \log(10)}{-2 \log(3) + \log(10)} \right) - 3509 \log(10)}{500 \left(\psi_{\frac{9}{10}}^{(0)}(1) - \log(10) \right)}$$

Alternative representations:

$$\frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(\frac{10}{9})} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = -\frac{18}{10^3} + \frac{7 \left(-\log_e(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log_e(\frac{10}{9})} \right) \right)}{\log_e(10) - \psi_{\frac{9}{10}}^{(0)}(1)}$$

$$\begin{aligned} & \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(\frac{10}{9})} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = \\ & -\frac{18}{10^3} + \frac{7 \left(-\log(a) \log_a(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(a) \log_a(\frac{10}{9})} \right) \right)}{\log(a) \log_a(10) - \psi_{\frac{9}{10}}^{(0)}(1)} \end{aligned}$$

$$\frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(\frac{10}{9})} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = -\frac{18}{10^3} + \frac{7 \left(\text{Li}_1(-9) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\text{Li}_1(1-\frac{10}{9})} \right) \right)}{-\text{Li}_1(-9) - \psi_{\frac{9}{10}}^{(0)}(1)}$$

Series representations:

$$\begin{aligned}
 & \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = \\
 & - \left(\left(7018 \pi \left[\frac{\arg(10-x)}{2\pi} \right] - 3509 i \log(x) + 9 i \psi_{\frac{9}{10}}^{(0)}(1) + \right. \right. \\
 & \quad \left. \left. 3500 i \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{2 i \pi \left[\frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) + \right. \right. \\
 & \quad \left. \left. 3509 i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) / \right. \\
 & \quad \left. \left(500 \left(2 \pi \left[\frac{\arg(10-x)}{2\pi} \right] - i \log(x) + i \psi_{\frac{9}{10}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10-x)^k x^{-k}}{k} \right) \right) \right)
 \end{aligned}$$

for $x < 0$

$$\begin{aligned}
& \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = \\
& - \left(\left(7018 \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - 3509 i \log(z_0) + 9 i \psi_{\frac{9}{10}}^{(0)}(1) + \right. \right. \\
& \left. \left. 3500 i \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{2 i \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right) + \right. \right. \\
& \left. \left. 3509 i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \left(500 \left(2 \pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - \right. \right. \right. \\
& \left. \left. \left. i \log(z_0) + i \psi_{\frac{9}{10}}^{(0)}(1) + i \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = \\
& - \left(\left(3509 \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + 3509 \log(z_0) + 3509 \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \right. \right. \\
& \quad \left. \left. 9 \psi_{\frac{9}{10}}^{(0)}(1) - 3500 \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right)} \right) \right. \\
& \quad \left. 3509 \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) / \left(500 \left(\left[\frac{\arg(10 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \right. \right. \\
& \quad \left. \left. \log(z_0) + \left[\frac{\arg(10 - z_0)}{2\pi} \right] \log(z_0) - \psi_{\frac{9}{10}}^{(0)}(1) - \sum_{k=1}^{\infty} \frac{(-1)^k (10 - z_0)^k z_0^{-k}}{k} \right) \right) \right)
\end{aligned}$$

Integral representations:

$$\begin{aligned}
& \frac{7 \left(-\log(10) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right)}{\log(10) - \psi_{\frac{9}{10}}^{(0)}(1)} - \frac{18}{10^3} = \\
& \frac{3509 \int_1^{10} \frac{1}{t} dt - 9 \psi_{\frac{9}{10}}^{(0)}(1) - 3500 \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\int_1^9 \frac{1}{t} dt} \right)}{500 \left(\int_1^{10} \frac{1}{t} dt - \psi_{\frac{9}{10}}^{(0)}(1) \right)}
\end{aligned}$$

$$\frac{7 \left(-\log(10) + \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log(\frac{10}{9})} \right) \right)}{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)} - \frac{18}{10^3} =$$

$$- \left(\left(3509 i \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds + 18 \pi \psi_{\frac{10}{9}}^{(0)}(1) + \right. \right.$$

$$\left. \left. 7000 \pi \psi_{\frac{10}{9}}^{(0)} \left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right) \right) / \right.$$

$$\left. \left(500 \left(i \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds + 2 \pi \psi_{\frac{10}{9}}^{(0)}(1) \right) \right) \right) \text{ for } -1 < \gamma < 0$$

Subtracting the two results, we obtain:

$$\left(\left(\left(\frac{1}{(10/9)^1 - 1} + \frac{1}{(10/9)^2 - 1} + \frac{1}{(10/9)^3 - 1} + \dots \right) \right) - \left(\frac{1}{1 + (10/9)} + \frac{1}{1 + (10/9)^2} + \frac{1}{1 + (10/9)^3} + \dots \right) \right)$$

Input interpretation:

$$\left(\frac{1}{\left(\frac{10}{9}\right)^1 - 1} + \frac{1}{\left(\frac{10}{9}\right)^2 - 1} + \frac{1}{\left(\frac{10}{9}\right)^3 - 1} + \dots \right) - \left(\frac{1}{1 + \frac{10}{9}} + \frac{1}{1 + \left(\frac{10}{9}\right)^2} + \frac{1}{1 + \left(\frac{10}{9}\right)^3} + \dots \right)$$

Result:

$$\frac{\log(10) - \psi_{\frac{10}{9}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} - \frac{-\log(10) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)}$$

$\log(x)$ is the natural logarithm

$\psi_q(z)$ gives the q -digamma function

Alternate forms:

$$\frac{\psi_{\frac{10}{9}}^{(0)}(1) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) - \log(100)}{\log\left(\frac{10}{9}\right)}$$

$$\frac{-\psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) + 2\log(10)}{\log\left(\frac{10}{9}\right)}$$

$$-\frac{\psi_{\frac{9}{10}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} - \frac{\psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} + \frac{2\log(10)}{\log\left(\frac{10}{9}\right)}$$

$-(\log(100) + \text{QPolyGamma}(0, 1, 9/10) + \text{QPolyGamma}(0, 1 - (i\pi)/\log(10/9), 9/10))/\log(10/9)$

Input:

$$-\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)}$$

Exact result:

$$\frac{-\psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) + \log(100)}{\log\left(\frac{10}{9}\right)}$$

Decimal approximation:

20.75547634120342226556033888586272957206659976239062178441...

20.75547634...

Alternate forms:

$$\frac{\log(100) - \psi_{\frac{9}{10}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} - \frac{\psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)}$$

$$-\frac{\psi_{\frac{9}{10}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} - \frac{\psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} + \frac{\log(100)}{\log\left(\frac{10}{9}\right)}$$

$$\frac{\psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)}\right) - 2\log(10)}{\log(10) - 2\log(3)}$$

Alternative representations:

$$\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} = \frac{\log_e(100) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log_e\left(\frac{10}{9}\right)}\right)}{\log_e\left(\frac{10}{9}\right)}$$

$$\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} = \frac{\log(a) \log_a(100) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(a) \log_a\left(\frac{10}{9}\right)}\right)}{\log(a) \log_a\left(\frac{10}{9}\right)}$$

$$\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} = -\frac{-\text{Li}_1(-99) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\text{Li}_1\left(1 - \frac{10}{9}\right)}\right)}{\text{Li}_1\left(1 - \frac{10}{9}\right)}$$

Series representations:

$$\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} = \left(2\pi \left\lfloor \frac{\arg(100-x)}{2\pi} \right\rfloor - i \log(x) + \right. \\ \left. i \psi_{\frac{9}{10}}^{(0)}(1) + i \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) + \right. \\ \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (100-x)^k x^{-k}}{k} \right) / \\ \left(2\pi \left\lfloor \frac{\arg\left(\frac{10}{9}-x\right)}{2\pi} \right\rfloor - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9}-x\right)^k x^{-k}}{k} \right) \text{ for } x < 0$$

$$\begin{aligned}
& -\frac{-\log(100) + \psi_{\frac{\varrho}{10}}^{(0)}(1) + \psi_{\frac{\varrho}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)} = \\
& \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \psi_{\frac{\varrho}{10}}^{(0)}(1) + \right. \\
& \quad \left. i \psi_{\frac{\varrho}{10}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\varrho} - z_0\right)^k z_0^{-k}}{k}} \right) + \right. \\
& \quad \left. i \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(2\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - i \log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\varrho} - z_0\right)^k z_0^{-k}}{k} \right) \\
& -\frac{-\log(100) + \psi_{\frac{\varrho}{10}}^{(0)}(1) + \psi_{\frac{\varrho}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{\varrho}\right)}\right)}{\log\left(\frac{10}{\varrho}\right)} = \\
& \left(\left[\frac{\arg(100 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg(100 - z_0)}{2\pi} \right] \log(z_0) - \psi_{\frac{\varrho}{10}}^{(0)}(1) - \right. \\
& \quad \left. \psi_{\frac{\varrho}{10}}^{(0)} \left(1 - \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{\varrho} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\varrho} - z_0\right)^k z_0^{-k}}{k}} \right) - \right. \\
& \quad \left. \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} \right) / \\
& \left(\left[\frac{\arg\left(\frac{10}{\varrho} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg\left(\frac{10}{\varrho} - z_0\right)}{2\pi} \right] \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{\varrho} - z_0\right)^k z_0^{-k}}{k} \right)
\end{aligned}$$

Integral representations:

$$\begin{aligned}
 & -\frac{\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(\frac{10}{9})}\right)}{\log(\frac{10}{9})} = \frac{\int_1^{100} \frac{1}{t} dt - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(\frac{10}{9})}\right)}{\int_1^{\frac{10}{9}} \frac{1}{t} dt} \\
 & -\frac{\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(\frac{10}{9})}\right)}{\log(\frac{10}{9})} = \\
 & \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{99^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 2i\pi \psi_{\frac{9}{10}}^{(0)}(1) - 2i\pi \psi_{\frac{9}{10}}^{(0)}\left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}\right)}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \text{ for} \\
 & -1 < \gamma < 0
 \end{aligned}$$

And:

6((((-log(100) + QPolyGamma(0, 1, 9/10) + QPolyGamma(0, 1 - (i pi)/log(10/9), 9/10))/log(10/9))))+1/golden ratio

Input:

$$6 \left(\frac{-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(\frac{10}{9})}\right)}{\log(\frac{10}{9})} \right) + \frac{1}{\phi}$$

Exact result:

$$\frac{1}{\phi} + \frac{6 \left(-\psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(\frac{10}{9})}\right) + \log(100) \right)}{\log(\frac{10}{9})}$$

Decimal approximation:

125.1508920359704284415666201495420155501199077541494935686...

125.150892035... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

Alternate forms:

$$\frac{1}{2}(\sqrt{5}-1) + \frac{6\left(-\psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) + \log(100)\right)}{\log\left(\frac{10}{9}\right)}$$

$$\frac{1}{\phi} - \frac{6\left(\psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(\frac{-i\pi - 2\log(3) + \log(10)}{-2\log(3) + \log(10)}\right) - 2\log(10)\right)}{\log(10) - 2\log(3)}$$

$$-\frac{6\psi_{\frac{9}{10}}^{(0)}(1)}{\log\left(\frac{10}{9}\right)} - \frac{6\psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)}{\log\left(\frac{10}{9}\right)} + \frac{2}{1+\sqrt{5}} + \frac{6\log(100)}{\log\left(\frac{10}{9}\right)}$$

Alternative representations:

$$\frac{6\left(-\left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)\right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{6\left(\log_e(100) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log_e\left(\frac{10}{9}\right)}\right)\right)}{\log_e\left(\frac{10}{9}\right)}$$

$$\frac{6\left(-\left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)\right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{6\left(\log(a)\log_a(100) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log(a)\log_a\left(\frac{10}{9}\right)}\right)\right)}{\log(a)\log_a\left(\frac{10}{9}\right)}$$

$$\frac{6\left(-\left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right)\right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{6\left(-\text{Li}_1(-99) - \psi_{\frac{9}{10}}^{(0)}(1) - \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\text{Li}_1\left(1 - \frac{10}{9}\right)}\right)\right)}{\text{Li}_1\left(1 - \frac{10}{9}\right)}$$

Series representations:

$$\begin{aligned}
 & \frac{6 \left(-\left(-\log(100) + \psi_{\frac{10}{9}}^{(0)}(1) + \psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} = \\
 & \left(2 \left(2\pi \left\lfloor \frac{\arg\left(\frac{10}{9} - x\right)}{2\pi} \right\rfloor + 6\pi \left\lfloor \frac{\arg(100 - x)}{2\pi} \right\rfloor + 6\sqrt{5}\pi \left\lfloor \frac{\arg(100 - x)}{2\pi} \right\rfloor - \right. \right. \\
 & \quad 4i \log(x) - 3i\sqrt{5} \log(x) + 3i\psi_{\frac{10}{9}}^{(0)}(1) + 3i\sqrt{5}\psi_{\frac{10}{9}}^{(0)}(1) + \\
 & \quad \left. 3i\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9} - x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - x\right)^k x^{-k}}{k} \right) + \right. \\
 & \quad \left. 3i\sqrt{5}\psi_{\frac{10}{9}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left\lfloor \frac{\arg\left(\frac{10}{9} - x\right)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - x\right)^k x^{-k}}{k} \right) + \right. \\
 & \quad \left. i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - x\right)^k x^{-k}}{k} + 3i \sum_{k=1}^{\infty} \frac{(-1)^k (100 - x)^k x^{-k}}{k} + \right. \\
 & \quad \left. \left. 3i\sqrt{5} \sum_{k=1}^{\infty} \frac{(-1)^k (100 - x)^k x^{-k}}{k} \right) \right) / \\
 & \left((1 + \sqrt{5}) \left(2\pi \left\lfloor \frac{\arg\left(\frac{10}{9} - x\right)}{2\pi} \right\rfloor - i \log(x) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - x\right)^k x^{-k}}{k} \right) \right) \text{ for } x < \\
 & 0
 \end{aligned}$$

$$\begin{aligned}
& \frac{6 \left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right) \right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} = \\
& \left(\left(2 \left[8\pi \left| \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right| + 6\sqrt{5}\pi \left| \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right| - \right. \right. \right. \\
& \quad \left. \left. \left. 4i\log(z_0) - 3i\sqrt{5}\log(z_0) + 3i\psi_{\frac{9}{10}}^{(0)}(1) + 3i\sqrt{5}\psi_{\frac{9}{10}}^{(0)}(1) + \right. \right. \right. \\
& \quad \left. \left. \left. 3i\psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left| \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right| + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right) \right. \right. \right. \\
& \quad \left. \left. \left. 3i\sqrt{5}\psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{2i\pi \left| \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right| + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right) \right. \right. \right. \\
& \quad \left. \left. \left. i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} + 3i \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} + \right. \right. \right. \\
& \quad \left. \left. \left. 3i\sqrt{5} \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} \right) \right) / \\
& \left((1 + \sqrt{5}) \left(2\pi \left| \frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right| - i\log(z_0) + i \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{6 \left(-\left(-\log(100) + \psi_{\frac{10}{9}}^{(0)}(1) + \psi_{\frac{10}{9}}^{(0)}\left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)}\right)\right) \right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} = \\
& \left(2 \left[\left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + 3 \left[\frac{\arg(100 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \right. \right. \\
& \quad 3\sqrt{5} \left[\frac{\arg(100 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + 4 \log(z_0) + 3\sqrt{5} \log(z_0) + \\
& \quad \left. \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log(z_0) + 3 \left[\frac{\arg(100 - z_0)}{2\pi} \right] \log(z_0) + \right. \\
& \quad \left. 3\sqrt{5} \left[\frac{\arg(100 - z_0)}{2\pi} \right] \log(z_0) - 3 \psi_{\frac{10}{9}}^{(0)}(1) - 3\sqrt{5} \psi_{\frac{10}{9}}^{(0)}(1) - 3 \psi_{\frac{10}{9}}^{(0)} \right. \\
& \quad \left. \left. 1 - \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right. \right. \\
& \quad \left. \left. 3\sqrt{5} \psi_{\frac{10}{9}}^{(0)} \right. \right. \\
& \quad \left. \left. 1 - \frac{i\pi}{\log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k}} \right. \right. \\
& \quad \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} - 3 \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} - \right. \right. \\
& \quad \left. \left. 3\sqrt{5} \sum_{k=1}^{\infty} \frac{(-1)^k (100 - z_0)^k z_0^{-k}}{k} \right) \right) / \\
& \left((1 + \sqrt{5}) \left(\left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left[\frac{\arg\left(\frac{10}{9} - z_0\right)}{2\pi} \right] \log(z_0) - \right. \right. \\
& \quad \left. \left. \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{10}{9} - z_0\right)^k z_0^{-k}}{k} \right) \right)
\end{aligned}$$

Integral representations:

$$\frac{6 \left(-\left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} =$$

$$\frac{1}{1 + \sqrt{5} \int_1^{\frac{10}{9}} \frac{1}{t} dt} 2 \left(\int_1^{\frac{10}{9}} \frac{1}{t} dt + 3 \int_1^{100} \frac{1}{t} dt + 3\sqrt{5} \int_1^{100} \frac{1}{t} dt - 3\psi_{\frac{9}{10}}^{(0)}(1) - \right.$$

$$\left. 3\sqrt{5} \psi_{\frac{9}{10}}^{(0)}(1) - 3\psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\int_1^{\frac{10}{9}} \frac{1}{t} dt} \right) - 3\sqrt{5} \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\int_1^{\frac{10}{9}} \frac{1}{t} dt} \right) \right)$$

$$\frac{6 \left(-\left(-\log(100) + \psi_{\frac{9}{10}}^{(0)}(1) + \psi_{\frac{9}{10}}^{(0)} \left(1 - \frac{i\pi}{\log\left(\frac{10}{9}\right)} \right) \right) \right)}{\log\left(\frac{10}{9}\right)} + \frac{1}{\phi} =$$

$$\left(2 \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds + 3 \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{99^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds + \right. \right.$$

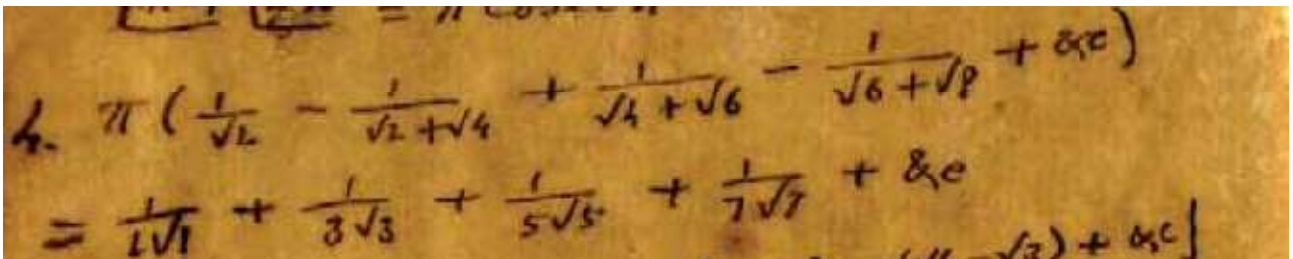
$$\left. 3\sqrt{5} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{99^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds - 6i\pi \psi_{\frac{9}{10}}^{(0)}(1) - \right.$$

$$\left. 6i\sqrt{5} \pi \psi_{\frac{9}{10}}^{(0)}(1) - 6i\pi \psi_{\frac{9}{10}}^{(0)} \left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \right) - \right.$$

$$\left. 6i\sqrt{5} \pi \psi_{\frac{9}{10}}^{(0)} \left(1 + \frac{2\pi^2}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \right) \right) /$$

$$\left(1 + \sqrt{5} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{9^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right) \text{ for } -1 < \gamma < 0$$

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Pi *(1/(sqrt2)-1/(sqrt2+sqrt4)+1/(sqrt4+sqrt6)-1/(sqrt6+sqrt8))

Input:

$$\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2} + \sqrt{4}} + \frac{1}{\sqrt{4} + \sqrt{6}} - \frac{1}{\sqrt{6} + \sqrt{8}} \right)$$

Result:

$$\left(\frac{1}{\sqrt{2}} - \frac{1}{2 + \sqrt{2}} + \frac{1}{2 + \sqrt{6}} - \frac{1}{2\sqrt{2} + \sqrt{6}} \right) \pi$$

Decimal approximation:

1.412113673791598096338931391467032700409225206634342296658...

1.41211367379....

Property:

$$\left(\frac{1}{\sqrt{2}} - \frac{1}{2 + \sqrt{2}} + \frac{1}{2 + \sqrt{6}} - \frac{1}{2\sqrt{2} + \sqrt{6}} \right) \pi \text{ is a transcendental number}$$

Alternate forms:

$$\pi(\sqrt{6} - 2)$$

$$\frac{2\pi}{2 + \sqrt{6}}$$

$$\frac{2\sqrt{2}(1 + \sqrt{2})\pi}{(2 + \sqrt{2})(2 + \sqrt{6})}$$

Series representations:

$$\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2} + \sqrt{4}} + \frac{1}{\sqrt{4} + \sqrt{6}} - \frac{1}{\sqrt{6} + \sqrt{8}} \right) =$$

$$-\frac{\pi}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left((2-z_0)^k + (4-z_0)^k\right) z_0^{-k}}{\pi k!}} + \frac{\pi}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left((4-z_0)^k + (6-z_0)^k\right) z_0^{-k}}{\pi k!}} -$$

$$\frac{\pi}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left((6-z_0)^k + (8-z_0)^k\right) z_0^{-k}}{\pi k!}} + \frac{\pi}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{\pi k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2} + \sqrt{4}} + \frac{1}{\sqrt{4} + \sqrt{6}} - \frac{1}{\sqrt{6} + \sqrt{8}} \right) =$$

$$\frac{\exp\left(i\pi \left[\frac{\arg(2-x)}{2\pi} \right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{\pi k!}}{\sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left((2-x)^k \exp\left(i\pi \left[\frac{\arg(2-x)}{2\pi} \right]\right) + (4-x)^k \exp\left(i\pi \left[\frac{\arg(4-x)}{2\pi} \right]\right) \right) \left(-\frac{1}{2}\right)_k \sqrt{x}}{\pi k!}} +$$

$$\frac{\sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left((4-x)^k \exp\left(i\pi \left[\frac{\arg(4-x)}{2\pi} \right]\right) + (6-x)^k \exp\left(i\pi \left[\frac{\arg(6-x)}{2\pi} \right]\right) \right) \left(-\frac{1}{2}\right)_k \sqrt{x}}{\pi k!}}{\sum_{k=0}^{\infty} \frac{(-1)^k x^{-k} \left((6-x)^k \exp\left(i\pi \left[\frac{\arg(6-x)}{2\pi} \right]\right) + (8-x)^k \exp\left(i\pi \left[\frac{\arg(8-x)}{2\pi} \right]\right) \right) \left(-\frac{1}{2}\right)_k \sqrt{x}}{\pi k!}}$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2} + \sqrt{4}} + \frac{1}{\sqrt{4} + \sqrt{6}} - \frac{1}{\sqrt{6} + \sqrt{8}} \right) =$$

$$\frac{\pi \left(\frac{1}{z_0} \right)^{-1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(2-z_0)/(2\pi) \rfloor)}}{\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}}$$

$$\pi / \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^k \left(-\frac{1}{2}\right)_k z_0^{1/2-k} \left((2-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} + \right. \right.$$

$$\left. \left. (4-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} \right) \right) +$$

$$\pi / \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^k \left(-\frac{1}{2}\right)_k z_0^{1/2-k} \left((4-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} + \right. \right.$$

$$\left. \left. (6-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(6-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(6-z_0)/(2\pi) \rfloor} \right) \right) -$$

$$\pi / \left(\sum_{k=0}^{\infty} \frac{1}{k!} (-1)^k \left(-\frac{1}{2}\right)_k z_0^{1/2-k} \left((6-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(6-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(6-z_0)/(2\pi) \rfloor} + \right. \right.$$

$$\left. \left. (8-z_0)^k \left(\frac{1}{z_0}\right)^{1/2 \lfloor \arg(8-z_0)/(2\pi) \rfloor} z_0^{1/2 \lfloor \arg(8-z_0)/(2\pi) \rfloor} \right) \right)$$

$$1/(\sqrt{1})+1/(\sqrt[3]{3})+1/(\sqrt[5]{5})+1/(\sqrt[7]{7})+\dots$$

$$1/(\sqrt{1})+1/(\sqrt[3]{3})+1/(\sqrt[5]{5})+1/(\sqrt[7]{7})+1/(\sqrt[11]{11})+1/(\sqrt[13]{13})+1/(\sqrt[17]{17})$$

$$+1/(\sqrt[19]{19})$$

Input:

$$\frac{1}{1\sqrt{1}} + \frac{1}{3\sqrt{3}} + \frac{1}{5\sqrt{5}} + \frac{1}{7\sqrt{7}} + \frac{1}{11\sqrt{11}} + \frac{1}{13\sqrt{13}} + \frac{1}{17\sqrt{17}} + \frac{1}{19\sqrt{19}}$$

Result:

$$1 + \frac{1}{3\sqrt{3}} + \frac{1}{5\sqrt{5}} + \frac{1}{7\sqrt{7}} + \frac{1}{11\sqrt{11}} + \frac{1}{13\sqrt{13}} + \frac{1}{17\sqrt{17}} + \frac{1}{19\sqrt{19}}$$

Decimal approximation:

1.410973792493254865502532064755699580693444979832500007456...

1.41097379249...

Alternate forms:

$$\frac{1}{3}\sqrt{3}\frac{1}{3} + \frac{1}{5}\sqrt{5}\frac{1}{5} + \frac{1}{7}\sqrt{7}\frac{1}{7} + \frac{1}{11}\sqrt{11}\frac{1}{11} + \frac{1}{13}\sqrt{13}\frac{1}{13} + \frac{1}{17}\sqrt{17}\frac{1}{17} + \frac{1}{19}\sqrt{19}\frac{1}{19} + 1$$

$$\frac{1}{23520996524025} (23520996524025 + 2613444058225\sqrt{3} + 940839860961\sqrt{5} + 480020337225\sqrt{7} + 194388401025\sqrt{11} + 139177494225\sqrt{13} + 81387531225\sqrt{17} + 65155115025\sqrt{19})$$

$$\frac{1}{19\sqrt{19}} + \frac{1}{65155115025} (65155115025 + 7239457225\sqrt{3} + 2606204601\sqrt{5} + 1329696225\sqrt{7} + 538472025\sqrt{11} + 385533225\sqrt{13} + 225450225\sqrt{17})$$

From the previous expression, we obtain:

$$1/((((Pi * (1/(sqrt2)-1/(sqrt2+sqrt4)+1/(sqrt4+sqrt6)-1/(sqrt6+sqrt8))))))^(1/64$$

Input:

$$\frac{1}{\sqrt[64]{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)}}$$

Exact result:

$$\frac{1}{\sqrt[64]{\left(\frac{1}{\sqrt{2}} - \frac{1}{2+\sqrt{2}} + \frac{1}{2+\sqrt{6}} - \frac{1}{2\sqrt{2}+\sqrt{6}}\right)\pi}}$$

Decimal approximation:

0.994622516313439470387198076716845725808014510743913823288...

0.99462251631343947..... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Property:

$$\frac{1}{\sqrt[64]{\left(\frac{1}{\sqrt{2}} - \frac{1}{2+\sqrt{2}} + \frac{1}{2+\sqrt{6}} - \frac{1}{2\sqrt{2}+\sqrt{6}}\right)\pi}}$$
 is a transcendental number

Alternate forms:

$$\frac{1}{\sqrt[64]{(\sqrt{6} - 2)\pi}}$$

$$\sqrt[64]{\frac{2 + \sqrt{6}}{2\pi}}$$

$$\frac{\sqrt[64]{\frac{7+5\sqrt{2}+4\sqrt{3}+3\sqrt{6}}{(2+\sqrt{3})\pi}}}{\sqrt[128]{\sqrt{2}} \sqrt[64]{1+\sqrt{2}}}$$

2log base 0.994622516313439 (((1/(((Pi *(1/(sqrt2)-1/(sqrt2+sqrt4)+1/(sqrt4+sqrt6)-1/(sqrt6+sqrt8)))))))))-Pi+1/golden ratio

Input interpretation:

$$2 \log_{0.994622516313439} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) - \pi + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

125.4764413351...

125.4764413351... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Alternative representation:

$$2 \log_{0.99462251631343900000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{2 \log \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right)}{\log(0.99462251631343900000)}$$

Series representations:

$$2 \log_{0.99462251631343900000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right)^k}{k}}{\log(0.99462251631343900000)}$$

$$2 \log_{0.99462251631343900000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1.00000000000000000000}{\phi} - 1.00000000000000000000 \pi +$$

$$\log \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) \left(-370.92116546968772 - \right.$$

$$\left. 2.00000000000000000000 \sum_{k=0}^{\infty} (-0.0053774836865610000)^k G(k) \right)$$

$$\text{for } \left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$$

$$2 \log_{0.99462251631343900000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1.00000000000000000000}{\phi} - 1.00000000000000000000 \pi +$$

$$\log \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}+\sqrt{4}} + \frac{1}{\sqrt{4}+\sqrt{6}} - \frac{1}{\sqrt{6}+\sqrt{8}} \right)} \right) \left(-370.92116546968772 - \right.$$

$$\left. 2.00000000000000000000 \sum_{k=0}^{\infty} (-0.0053774836865610000)^k G(k) \right)$$

$$\text{for } \left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$$

1/4 log base 0.994622516313439 (((1/(((Pi * (1/(sqrt2)-1/(sqrt2+sqrt4)+1/(sqrt4+sqrt6)-1/(sqrt6+sqrt8)))))))))+1/golden ratio

Input interpretation:

$$\frac{1}{4} \log_{0.994622516313439} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

16.61803398875...

16.61803398... result very near to the mass of the hypothetical light particle, the boson $m_X = 16.84$ MeV

Alternative representation:

$$\frac{1}{4} \log_{0.9946225163134390000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{\log \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right)}{4 \log(0.9946225163134390000)}$$

Series representations:

$$\frac{1}{4} \log_{0.9946225163134390000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right)^k}{k}}{4 \log(0.9946225163134390000)}$$

$$\frac{1}{4} \log_{0.9946225163134390000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1.000000000000000000}{\phi} +$$

$$\log \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) \left(-46.36514568371096 - \right.$$

$$\left. 0.250000000000000000 \sum_{k=0}^{\infty} (-0.0053774836865610000)^k G(k) \right)$$

for $\left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

$$\frac{1}{4} \log_{0.9946225163134390000} \left(\frac{1}{\pi \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2+\sqrt{4}}} + \frac{1}{\sqrt{4+\sqrt{6}}} - \frac{1}{\sqrt{6+\sqrt{8}}} \right)} \right) + \frac{1}{\phi} =$$

$$\frac{1}{4\phi} \left(4 + \phi \log_{0.9946225163134390000} \left(1 / \left(\pi \left[- \frac{1}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k + (4-z_0)^k z_0^{-k}}{k!}} + \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k + (6-z_0)^k z_0^{-k}}{k!}} - \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (6-z_0)^k + (8-z_0)^k z_0^{-k}}{k!}} + \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}} \right] \right) \right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

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Handwritten mathematical derivation on aged paper:

$$8 \cdot \frac{2}{5} \sqrt{x(x+\frac{1}{2})(x+\frac{1}{2})(x+\frac{2}{4})(x+1) + \frac{5}{768}(x+\frac{1}{2})}$$

$$- (1\sqrt{1} + 2\sqrt{2} + 3\sqrt{3} + \dots + x\sqrt{x})$$

$$= \frac{2}{167\pi} \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} + 2(x) \right)$$

$$3/(16\pi^2)*(((1/(1\sqrt{1})+1/(4\sqrt{2})+1/(9\sqrt{3})+1/(16\sqrt{4}))))$$

Input:

$$\frac{3}{16\pi^2} \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)$$

Result:

$$\frac{3 \left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} \right)}{16\pi^2}$$

Decimal approximation:

0.024168459675030997066368197518608237526403609954799171534...

0.024168459675...

Property:

$$\frac{3 \left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} \right)}{16\pi^2} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{891 + 108\sqrt{2} + 32\sqrt{3}}{4608\pi^2}$$

$$\frac{\frac{99}{512} + \frac{3}{64\sqrt{2}} + \frac{1}{48\sqrt{3}}}{\pi^2}$$

$$\frac{297 + 4\sqrt{\frac{2}{3}(275 + 72\sqrt{6})}}{1536\pi^2}$$

Series representations:

$$\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right) 3}{16\pi^2} = \frac{3}{16\pi^2} \exp\left(i\pi \left\lfloor \frac{\arg(1-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (1-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} +$$

$$\frac{64\pi^2 \exp\left(i\pi \left\lfloor \frac{\arg(2-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}}{1} +$$

$$\frac{48\pi^2 \exp\left(i\pi \left\lfloor \frac{\arg(3-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}}{3} +$$

$$\frac{256\pi^2 \exp\left(i\pi \left\lfloor \frac{\arg(4-x)}{2\pi} \right\rfloor\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (4-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}}{3} \quad \text{for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right) 3}{16\pi^2} = \frac{3 \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(1-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(1-z_0)/(2\pi) \rfloor)}}{16\pi^2 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1-z_0)^k z_0^{-k}}{k!}} +$$

$$\frac{3 \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(2-z_0)/(2\pi) \rfloor)}}{64\pi^2 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}} +$$

$$\frac{\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(3-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(3-z_0)/(2\pi) \rfloor)}}{48\pi^2 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3-z_0)^k z_0^{-k}}{k!}} +$$

$$\frac{3 \left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} z_0^{1/2 (-1 - \lfloor \arg(4-z_0)/(2\pi) \rfloor)}}{256\pi^2 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k z_0^{-k}}{k!}}$$

$$\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right)3}{16\pi^2} =$$

$$\left(9 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-\frac{1}{2}\right)_{k_3} (1-z_0)^{k_1} (2-z_0)^{k_2} (3-z_0)^{k_3} z_0^{-k_1-k_2-k_3} +\right.$$

$$16 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-\frac{1}{2}\right)_{k_3} (1-z_0)^{k_1} (2-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} +$$

$$36 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-\frac{1}{2}\right)_{k_3} (1-z_0)^{k_1} (3-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} +$$

$$144 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-\frac{1}{2}\right)_{k_3} (2-z_0)^{k_1} (3-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} \Bigg/$$

$$\left(768\pi^2 \sqrt{z_0} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1-z_0)^k z_0^{-k}}{k!}\right) \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}\right) \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3-z_0)^k z_0^{-k}}{k!}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k z_0^{-k}}{k!}\right)$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$1/((((3/(16\pi^2)*(((1/(1\sqrt{1})+1/(4\sqrt{2})+1/(9\sqrt{3})+1/(16\sqrt{4})))))))) * 18 + 29$$

Input:

$$\frac{1}{\frac{3}{16\pi^2} \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right)} \times 18 + 29$$

Result:

$$29 + \frac{96\pi^2}{\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}}$$

Decimal approximation:

773.7723289786739064366728621016961412986627748069702160994...

773.772328978... result very near to the rest mass of Charged rho meson 775.4

Property:

$$29 + \frac{96 \pi^2}{\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{1}{65415603433} \left(6302136462336 \pi^2 - 770010624000 \sqrt{2} \pi^2 - 240098770944 \sqrt{3} \pi^2 + 56757583872 \sqrt{6} \pi^2 + 1897052499557 \right)$$

$$29 + \frac{82944 \pi^2}{891 + 108 \sqrt{2} + 32 \sqrt{3}}$$

$$29 + \frac{1}{65415603433} 27648 \left(227941857 - 27850500 \sqrt{2} - 32 \sqrt{3 \left(81877519849 - 34819011216 \sqrt{2} \right)} \right) \pi^2$$

Series representations:

$$\frac{18}{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right) 16\pi^2} + 29 = 29 + (96 \pi^2) / \left(\frac{1}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1-z_0)^k z_0^{-k}}{k!}} + \frac{1}{4 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}} + \frac{1}{9 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3-z_0)^k z_0^{-k}}{k!}} + \frac{1}{16 \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k z_0^{-k}}{k!}} \right)$$

for not ((z₀ ∈ ℝ and -∞ < z₀ ≤ 0))

$$\frac{18}{3\left(\frac{1}{1\sqrt{1}}+\frac{1}{4\sqrt{2}}+\frac{1}{9\sqrt{3}}+\frac{1}{16\sqrt{4}}\right)} + 29 =$$

$$29 + (96\pi^2) \left/ \left(\frac{1}{\exp\left(i\pi\left[\frac{\arg(1-x)}{2\pi}\right]\right)\sqrt{x}\sum_{k=0}^{\infty}\frac{(-1)^k(1-x)^k x^{-k}\left(-\frac{1}{2}\right)_k}{k!}} + \right.$$

$$\frac{4\exp\left(i\pi\left[\frac{\arg(2-x)}{2\pi}\right]\right)\sqrt{x}\sum_{k=0}^{\infty}\frac{(-1)^k(2-x)^k x^{-k}\left(-\frac{1}{2}\right)_k}{k!}}{1} +$$

$$\frac{9\exp\left(i\pi\left[\frac{\arg(3-x)}{2\pi}\right]\right)\sqrt{x}\sum_{k=0}^{\infty}\frac{(-1)^k(3-x)^k x^{-k}\left(-\frac{1}{2}\right)_k}{k!}}{1} +$$

$$\left. \frac{16\exp\left(i\pi\left[\frac{\arg(4-x)}{2\pi}\right]\right)\sqrt{x}\sum_{k=0}^{\infty}\frac{(-1)^k(4-x)^k x^{-k}\left(-\frac{1}{2}\right)_k}{k!}}{1} \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{18}{3\left(\frac{1}{1\sqrt{1}}+\frac{1}{4\sqrt{2}}+\frac{1}{9\sqrt{3}}+\frac{1}{16\sqrt{4}}\right)} + 29 =$$

$$29 + (96\pi^2) \left/ \left(\frac{\left(\frac{1}{z_0}\right)^{-1/2[\arg(1-z_0)/(2\pi)]} z_0^{1/2(-1-[\arg(1-z_0)/(2\pi)])}}{\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k(1-z_0)^k z_0^{-k}}{k!}} + \right.$$

$$\frac{\left(\frac{1}{z_0}\right)^{-1/2[\arg(2-z_0)/(2\pi)]} z_0^{1/2(-1-[\arg(2-z_0)/(2\pi)])}}{4\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k(2-z_0)^k z_0^{-k}}{k!}} +$$

$$\frac{\left(\frac{1}{z_0}\right)^{-1/2[\arg(3-z_0)/(2\pi)]} z_0^{1/2(-1-[\arg(3-z_0)/(2\pi)])}}{9\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k(3-z_0)^k z_0^{-k}}{k!}} +$$

$$\left. \frac{\left(\frac{1}{z_0}\right)^{-1/2[\arg(4-z_0)/(2\pi)]} z_0^{1/2(-1-[\arg(4-z_0)/(2\pi)])}}{16\sum_{k=0}^{\infty}\frac{(-1)^k\left(-\frac{1}{2}\right)_k(4-z_0)^k z_0^{-k}}{k!}} \right)$$

$$\left(\left(\left(\left(\left(\frac{3}{16\pi^2}\right)\left(\left(\frac{1}{\sqrt{1}}+\frac{1}{4\sqrt{2}}+\frac{1}{9\sqrt{3}}+\frac{1}{16\sqrt{4}}\right)\right)\right)\right)\right)\right)^{1/512}$$

Input:

$$\sqrt[512]{\frac{3}{16\pi^2} \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}$$

Exact result:

$$\frac{\sqrt[512]{3 \left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} \right)}}{\sqrt[128]{2} \sqrt[256]{\pi}}$$

Decimal approximation:

0.992755457382685870907518778213089423576732875586435399889...

0.99275545738... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Property:

$$\frac{\sqrt[512]{3 \left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} \right)}}{\sqrt[128]{2} \sqrt[256]{\pi}} \text{ is a transcendental number}$$

Alternate forms:

$$\frac{\sqrt[512]{891 + 108\sqrt{2} + 32\sqrt{3}}}{2^{9/512} \sqrt[256]{3\pi}}$$

$$\frac{\sqrt[512]{72\sqrt{3} + \sqrt{2} (32 + 297\sqrt{3})}}{2^{19/1024} \times 3^{3/1024} \sqrt[256]{\pi}}$$

All 512th roots of $(3(33/32 + 1/(4\sqrt{2}) + 1/(9\sqrt{3}))) / (16\pi^2)$:

$$\frac{\sqrt[512]{3\left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}\right)} e^0}{\sqrt[128]{2} \sqrt[256]{\pi}} \approx 0.992755 \quad (\text{real, principal root})$$

$$\frac{\sqrt[512]{3\left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}\right)} e^{(i\pi)/256}}{\sqrt[128]{2} \sqrt[256]{\pi}} \approx 0.992681 + 0.012183 i$$

$$\frac{\sqrt[512]{3\left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}\right)} e^{(i\pi)/128}}{\sqrt[128]{2} \sqrt[256]{\pi}} \approx 0.992456 + 0.024363 i$$

$$\frac{\sqrt[512]{3\left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}\right)} e^{(3i\pi)/256}}{\sqrt[128]{2} \sqrt[256]{\pi}} \approx 0.992083 + 0.036541 i$$

$$\frac{\sqrt[512]{3\left(\frac{33}{32} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}}\right)} e^{(i\pi)/64}}{\sqrt[128]{2} \sqrt[256]{\pi}} \approx 0.991560 + 0.048712 i$$

Series representations:

$$\sqrt[512]{\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right) 3}{16\pi^2}} =$$

$$\frac{1}{\sqrt[128]{2}} \sqrt[512]{3} \left(\frac{1}{\pi^2} \left(\frac{1}{\exp\left(i\pi \left\lfloor \frac{\text{arg}(1-x)}{2\pi} \right\rfloor\right)} \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (1-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} + \right. \right.$$

$$\frac{4 \exp\left(i\pi \left\lfloor \frac{\text{arg}(2-x)}{2\pi} \right\rfloor\right)}{1} \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} +$$

$$\frac{9 \exp\left(i\pi \left\lfloor \frac{\text{arg}(3-x)}{2\pi} \right\rfloor\right)}{1} \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} +$$

$$\left. \left. \frac{16 \exp\left(i\pi \left\lfloor \frac{\text{arg}(4-x)}{2\pi} \right\rfloor\right)}{1} \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (4-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \right)^{\wedge}$$

(1/512) for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\begin{aligned}
& \sqrt[512]{\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right) 3}{16\pi^2}} = \\
& \frac{1}{128\sqrt{2}} \sqrt[512]{3} \left(\frac{1}{\pi^2} \left(\frac{\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(1-z_0)/(2\pi) \rfloor} z_0^{-1/2-1/2 \lfloor \arg(1-z_0)/(2\pi) \rfloor}}{\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1-z_0)^k z_0^{-k}}{k!}} + \right. \right. \\
& \frac{\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor} z_0^{-1/2-1/2 \lfloor \arg(2-z_0)/(2\pi) \rfloor}}{4 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}} + \\
& \frac{\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(3-z_0)/(2\pi) \rfloor} z_0^{-1/2-1/2 \lfloor \arg(3-z_0)/(2\pi) \rfloor}}{9 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3-z_0)^k z_0^{-k}}{k!}} + \\
& \left. \left. \frac{\left(\frac{1}{z_0}\right)^{-1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor} z_0^{-1/2-1/2 \lfloor \arg(4-z_0)/(2\pi) \rfloor}}{16 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k z_0^{-k}}{k!}} \right) \right) \wedge (1/512)
\end{aligned}$$

$$\begin{aligned}
& \sqrt[512]{\frac{\left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}}\right)3}{16\pi^2}} = \\
& \frac{1}{\sqrt[64]{2}\sqrt[512]{3}} \left(\left(9 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \left(-\frac{1}{2}\right)_{k_3} \right. \right. \\
& \quad (1-z_0)^{k_1} (2-z_0)^{k_2} (3-z_0)^{k_3} z_0^{-k_1-k_2-k_3} + \\
& \quad 16 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \\
& \quad \left(-\frac{1}{2}\right)_{k_3} (1-z_0)^{k_1} (2-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} + \\
& \quad 36 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \\
& \quad \left(-\frac{1}{2}\right)_{k_3} (1-z_0)^{k_1} (3-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} + \\
& \quad \left. 144 \sum_{k_1=0}^{\infty} \sum_{k_2=0}^{\infty} \sum_{k_3=0}^{\infty} \frac{1}{k_1!k_2!k_3!} (-1)^{k_1+k_2+k_3} \left(-\frac{1}{2}\right)_{k_1} \left(-\frac{1}{2}\right)_{k_2} \right. \\
& \quad \left. \left(-\frac{1}{2}\right)_{k_3} (2-z_0)^{k_1} (3-z_0)^{k_2} (4-z_0)^{k_3} z_0^{-k_1-k_2-k_3} \right) / \\
& \left(\pi^2 \sqrt{z_0} \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (1-z_0)^k z_0^{-k}}{k!} \right) \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!} \right) \right. \\
& \quad \left. \left(\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (3-z_0)^k z_0^{-k}}{k!} \right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (4-z_0)^k z_0^{-k}}{k!} \right) \right)^{\wedge} \\
& (1/512) \Big) \text{ for not } ((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))
\end{aligned}$$

Integral representation:

$$(1+z)^a = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-a-s)}{z^s} ds}{(2\pi i)\Gamma(-a)} \text{ for } (0 < \gamma < -\text{Re}(a) \text{ and } |\arg(z)| < \pi)$$

1/4 log base 0.9927554573826

(((((3/(16Pi^2)*(((1/(1sqrt1)+1/(4sqrt2)+1/(9sqrt3)+1/(16sqrt4)))))))))))-Pi+1/golden ratio

Input interpretation:

$$\frac{1}{4} \log_{0.9927554573826} \left(\frac{3}{16 \pi^2} \left(\frac{1}{1 \sqrt{1}} + \frac{1}{4 \sqrt{2}} + \frac{1}{9 \sqrt{3}} + \frac{1}{16 \sqrt{4}} \right) \right) - \pi + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

125.47644133...

125.47644133... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Alternative representation:

$$\frac{1}{4} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1 \sqrt{1}} + \frac{1}{4 \sqrt{2}} + \frac{1}{9 \sqrt{3}} + \frac{1}{16 \sqrt{4}} \right)}{16 \pi^2} \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{\log \left(\frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4 \sqrt{2}} + \frac{1}{9 \sqrt{3}} + \frac{1}{16 \sqrt{4}} \right)}{16 \pi^2} \right)}{4 \log(0.99275545738260000)}$$

Series representations:

$$\frac{1}{4} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1 \sqrt{1}} + \frac{1}{4 \sqrt{2}} + \frac{1}{9 \sqrt{3}} + \frac{1}{16 \sqrt{4}} \right)}{16 \pi^2} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{\frac{144}{\sqrt{1}} + \frac{36}{\sqrt{2}} + \frac{16}{\sqrt{3}} + \frac{9}{\sqrt{4}}}{768 \pi^2} \right)^k}{k}}{4 \log(0.99275545738260000)}$$

$$\frac{1}{4} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right)^k}{k}}{4 \log(0.99275545738260000)}$$

$$\frac{1}{4} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1.0000000000000000}{\phi} - 1.0000000000000000 \pi +$$

$$\log \left(\frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) \left(-34.3837348095031 - \right.$$

$$\left. 0.2500000000000000 \sum_{k=0}^{\infty} (-0.00724454261740000)^k G(k) \right)$$

$$\text{for } \left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$$

1/32 log base 0.9927554573826

(((((3/(16Pi^2))*(((1/(1sqrt1))+1/(4sqrt2))+1/(9sqrt3)+1/(16sqrt4)))))))))+1/golden ratio

Input interpretation:

$$\frac{1}{32} \log_{0.9927554573826} \left(\frac{3}{16\pi^2} \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right) \right) + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

16.618033989...

16.618033989... result very near to the mass of the hypothetical light particle, the boson $m_x = 16.84$ MeV

Alternative representation:

$$\frac{1}{32} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{\log \left(\frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right)}{32 \log(0.99275545738260000)}$$

Series representations:

$$\frac{1}{32} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{\frac{144}{\sqrt{1}} + \frac{36}{\sqrt{2}} + \frac{16}{\sqrt{3}} + \frac{9}{\sqrt{4}}}{768\pi^2} \right)^k}{k}}{32 \log(0.99275545738260000)}$$

$$\frac{1}{32} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right)^k}{k}}{32 \log(0.99275545738260000)}$$

$$\frac{1}{32} \log_{0.99275545738260000} \left(\frac{3 \left(\frac{1}{1\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) + \frac{1}{\phi} =$$

$$\frac{1.0000000000000000}{\phi} + \log \left(\frac{3 \left(\frac{1}{\sqrt{1}} + \frac{1}{4\sqrt{2}} + \frac{1}{9\sqrt{3}} + \frac{1}{16\sqrt{4}} \right)}{16\pi^2} \right) \left(-4.2979668511879 - \right.$$

$$\left. 0.0312500000000000 \sum_{k=0}^{\infty} (-0.00724454261740000)^k G(k) \right)$$

for $\left(G(0) = 0 \text{ and } \frac{(-1)^k k}{2(1+k)(2+k)} + G(k) = \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

i. $\frac{1}{1.2} - \frac{1}{1.2^4} + \frac{1}{1.2^7} - \dots = \frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log 3.$

ii. $\frac{\sqrt{3}-1}{1} - \frac{(\sqrt{3}-1)^4}{4} + \frac{(\sqrt{3}-1)^7}{7} - \dots = \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \frac{1+\sqrt{3}}{\sqrt{3}}.$

iii. $\frac{2-\sqrt{3}}{1} - \frac{(2-\sqrt{3})^3}{5} + \frac{(2-\sqrt{3})^5}{9} - \dots = \frac{\pi}{16} (\sqrt{3}-1) - \frac{\sqrt{3}-1}{2} \log(\sqrt{3}-1).$

$$1/2 - 1/(4*2^4) + 1/(7*2^7)$$

Input:

$$\frac{1}{2} - \frac{1}{4 \times 2^4} + \frac{1}{7 \times 2^7}$$

Exact result:

$$\frac{435}{896}$$

Decimal approximation:

0.485491071428571428571428571428571428571428571428571428571...

0.4854910714....

$$\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \ln 3$$

Input:

$$\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log(3)$$

$\log(x)$ is the natural logarithm

Exact result:

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}$$

Decimal approximation:

0.485401942150387923664887249094113572821926134319248337884...

0.48540194215.....

Alternate forms:

$$\frac{1}{18} \left(\sqrt{3} \pi + \log(27) \right)$$

$$\frac{1}{18} \left(\sqrt{3} \pi + 3 \log(3) \right)$$

$$\frac{\pi + \sqrt{3} \log(3)}{6\sqrt{3}}$$

Alternative representations:

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\log_e(3)}{6} + \frac{\pi}{6\sqrt{3}}$$

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{1}{6} \log(a) \log_a(3) + \frac{\pi}{6\sqrt{3}}$$

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{2}{6} \coth^{-1}(2) + \frac{\pi}{6\sqrt{3}}$$

Series representations:

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\pi}{6\sqrt{3}} + \frac{\log(8)}{18} - \frac{1}{6} \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{2}\right)^k}{k}$$

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\pi}{6\sqrt{3}} + \frac{1}{3} i\pi \left[\frac{\arg(3-x)}{2\pi} \right] + \frac{\log(x)}{6} - \frac{1}{6} \sum_{k=1}^{\infty} \frac{(-1)^k (3-x)^k x^{-k}}{k}$$

for $x < 0$

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\pi}{6\sqrt{3}} + \frac{1}{6} \left[\frac{\arg(3-z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \frac{\log(z_0)}{6} + \frac{1}{6} \left[\frac{\arg(3-z_0)}{2\pi} \right] \log(z_0) - \frac{1}{6} \sum_{k=1}^{\infty} \frac{(-1)^k (3-z_0)^k z_0^{-k}}{k}$$

Integral representations:

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\pi}{6\sqrt{3}} + \frac{1}{6} \int_1^3 \frac{1}{t} dt$$

$$\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6} = \frac{\pi}{6\sqrt{3}} - \frac{i}{12\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{2^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$11/10^3 - 6/((5 \ln((\pi/(6\sqrt{3}) + 1/6 \ln 3))))$$

Where 11 is a Lucas number

Input:

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log(3)\right)}$$

log(x) is the natural logarithm

Exact result:

$$\frac{11}{1000} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)}$$

Decimal approximation:

1.671260862433822004010256676269847702707273749287869588882...

1.67126086243... result practically equal to the value of the formula:

$$m_{p'} = 2 \times \frac{\eta}{R} m_p = 1.6714213 \times 10^{-24} \text{ gm}$$

that is the holographic proton mass (N. Haramein)

Alternate forms:

$$\frac{11}{1000} - \frac{6}{5 \log\left(\frac{1}{18} (\sqrt{3} \pi + \log(27))\right)}$$

$$\frac{11}{1000} - \frac{6}{5 \left(\log\left(\frac{1}{2} (\sqrt{3} \pi + 3 \log(3))\right) - 2 \log(3)\right)}$$

$$\frac{11 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right) - 1200}{1000 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)}$$

Alternative representations:

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = -\frac{6}{5 \log_e\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3}$$

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = -\frac{6}{5 \log(a) \log_a\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3}$$

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = \frac{-6}{-5 \operatorname{Li}_1\left(1 - \frac{\log(3)}{6} - \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3}$$

Series representations:

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = \frac{11}{1000} + \frac{6}{5 \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k (-18 + \sqrt{3} \pi + \log(27))^k}{k}}$$

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = \frac{11}{1000} + \frac{6 i}{10 \pi \left[\frac{\operatorname{arig}(\sqrt{3} \pi - 18 x + \log(27))}{2 \pi} \right] - 5 i \left(\log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k x^{-k} (\sqrt{3} \pi - 18 x + \log(27))^k}{k} \right)}$$

for $x < 0$

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = \frac{11}{1000} - 6 \left/ \left(5 \left[\log(z_0) + \left| \frac{\arg(\sqrt{3} \pi + \log(27) - 18 z_0)}{2 \pi} \right| \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k (\sqrt{3} \pi + \log(27) - 18 z_0)^k z_0^{-k}}{k} \right] \right) \right.$$

Integral representation:

$$\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} = \frac{11}{1000} - \frac{6}{5 \int_1^{\frac{1}{18}(\sqrt{3} \pi + \log(27))} \frac{1}{t} dt}$$

And:

$$10^3 * (((11/10^3 - 6 / (((5 \ln(((\pi / (6 \sqrt{3}) + 1/6 \ln 3)))))))))) + \sqrt{2}$$

Input:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log(3)\right)} \right) + \sqrt{2}$$

$\log(x)$ is the natural logarithm

Exact result:

$$\sqrt{2} + 1000 \left(\frac{11}{1000} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right)$$

Decimal approximation:

1672.675075996195099059058364994057400785843421163246536955...

1672.675075996... result practically equal to the rest mass of Omega baryon 1672.45

Alternate forms:

$$11 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{18} (\sqrt{3} \pi + \log(27))\right)}$$

$$11 + \sqrt{2} - \frac{1200}{\log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)}$$

$$11 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{2}(\sqrt{3}\pi + 3\log(3))\right) - 2\log(3)}$$

Alternative representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} = 10^3 \left(-\frac{6}{5 \log_e\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} =$$

$$10^3 \left(-\frac{6}{5 \log(a) \log_a\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} = 10^3 \left(\frac{-6}{-5 \operatorname{Li}_1\left(1 - \frac{\log(3)}{6} - \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

Series representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} = 11 + \sqrt{2} + \frac{1200}{\sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k \left(-18 + \sqrt{3}\pi + \log(27)\right)^k}{k}}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} = 11 + \sqrt{2} +$$

$$\frac{1200 i}{2\pi \left[\frac{\arg\left(\sqrt{3}\pi - 18x + \log(27)\right)}{2\pi} \right] - i \left(\log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k x^{-k} \left(\sqrt{3}\pi - 18x + \log(27)\right)^k}{k} \right)} \quad \text{for } x < 0$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} =$$

$$11 + \sqrt{2} - 1200 \left/ \left(\log(z_0) + \left[\frac{\arg(\sqrt{3} \pi + \log(27) - 18 z_0)}{2 \pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k (\sqrt{3} \pi + \log(27) - 18 z_0)^k z_0^{-k}}{k} \right) \right.$$

Integral representation:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} = 11 + \sqrt{2} - \frac{1200}{\int_1^{\frac{1}{18}(\sqrt{3} \pi + \log(27))} \frac{1}{t} dt}$$

$$10^3 * (((11/10^3 - 6/((5 \ln(((\pi/(6\sqrt{3}) + 1/6 \ln 3)))))))) + \sqrt{2} + (47+7+2)$$

Where 2, 7 and 47 are Lucas numbers

Input:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log(3)\right)} \right) + \sqrt{2} + (47 + 7 + 2)$$

$\log(x)$ is the natural logarithm

Exact result:

$$56 + \sqrt{2} + 1000 \left(\frac{11}{1000} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right)$$

Decimal approximation:

1728.675075996195099059058364994057400785843421163246536955...

1728.6750759....

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–

Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternate forms:

$$67 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{18} (\sqrt{3} \pi + \log(27))\right)}$$

$$67 + \sqrt{2} - \frac{1200}{\log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)}$$

$$67 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{2} (\sqrt{3} \pi + 3 \log(3))\right) - 2 \log(3)}$$

Alternative representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) =$$

$$56 + 10^3 \left(-\frac{6}{5 \log_e\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) =$$

$$56 + 10^3 \left(-\frac{6}{5 \log(a) \log_a\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) =$$

$$56 + 10^3 \left(\frac{-6}{-5 \operatorname{Li}_1\left(1 - \frac{\log(3)}{6} - \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

Series representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) =$$

$$67 + \sqrt{2} + \frac{1200}{\sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k \left(-18 + \sqrt{3} \pi + \log(27)\right)^k}{k}}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) = 67 + \sqrt{2} +$$

$$\frac{1200 i}{2 \pi \left[\frac{\arg(\sqrt{3} \pi - 18 x + \log(27))}{2 \pi} \right] - i \left(\log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k x^{-k} \left(\sqrt{3} \pi - 18 x + \log(27)\right)^k}{k} \right)}$$

for $x < 0$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) =$$

$$67 + \sqrt{2} - \frac{1200}{\left(\log(z_0) + \left[\frac{\arg(\sqrt{3} \pi + \log(27) - 18 z_0)}{2 \pi} \right] \right) \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) -$$

$$\sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k \left(\sqrt{3} \pi + \log(27) - 18 z_0\right)^k z_0^{-k}}{k}$$

Integral representation:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + (47 + 7 + 2) = 67 + \sqrt{2} - \frac{1200}{\int_1^{\frac{1}{t}} \frac{1}{18} \left(\sqrt{3} \pi + \log(27)\right)^{\frac{1}{t}} dt}$$

$$10^3 * \left(\left(\left(\left(\left(\left(\frac{11}{10^3} - \frac{6}{5 \ln\left(\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \ln 3\right)} \right) \right) \right) \right) \right) \right) + \sqrt{2} + 123 - 11$$

Where 2, 11 and 123 are Lucas numbers

Input:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{1}{6} \log(3)\right)} \right) + \sqrt{2} + 123 - 11$$

$\log(x)$ is the natural logarithm

Exact result:

$$112 + \sqrt{2} + 1000 \left(\frac{11}{1000} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right)$$

Decimal approximation:

1784.675075996195099059058364994057400785843421163246536955...

1784.675075996... result in the range of the hypothetical mass of Gluino (gluino = 1785.16 GeV).

Alternate forms:

$$123 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{18} (\sqrt{3} \pi + \log(27))\right)}$$

$$123 + \sqrt{2} - \frac{1200}{\log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)}$$

$$123 + \sqrt{2} - \frac{1200}{\log\left(\frac{1}{2} (\sqrt{3} \pi + 3 \log(3))\right) - 2 \log(3)}$$

Alternative representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 =$$

$$112 + 10^3 \left(-\frac{6}{5 \log_e\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 =$$

$$112 + 10^3 \left(-\frac{6}{5 \log(a) \log_a\left(\frac{\log(3)}{6} + \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 =$$

$$112 + 10^3 \left(\frac{-6}{-5 \operatorname{Li}_1\left(1 - \frac{\log(3)}{6} - \frac{\pi}{6\sqrt{3}}\right)} + \frac{11}{10^3} \right) + \sqrt{2}$$

Series representations:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 =$$

$$123 + \sqrt{2} + \frac{1200}{\sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k \left(-18 + \sqrt{3} \pi + \log(27)\right)^k}{k}}$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 = 123 + \sqrt{2} +$$

$$\frac{1200 i}{2 \pi \left[\frac{\arg\left(\sqrt{3} \pi - 18 x + \log(27)\right)}{2 \pi} \right] - i \left(\log(x) - \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k x^{-k} \left(\sqrt{3} \pi - 18 x + \log(27)\right)^k}{k} \right)} \quad \text{for } x < 0$$

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 =$$

$$123 + \sqrt{2} - 1200 / \left(\log(z_0) + \left[\frac{\arg\left(\sqrt{3} \pi + \log(27) - 18 z_0\right)}{2 \pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \right.$$

$$\left. \sum_{k=1}^{\infty} \frac{\left(-\frac{1}{18}\right)^k \left(\sqrt{3} \pi + \log(27) - 18 z_0\right)^k z_0^{-k}}{k} \right)$$

Integral representation:

$$10^3 \left(\frac{11}{10^3} - \frac{6}{5 \log\left(\frac{\pi}{6\sqrt{3}} + \frac{\log(3)}{6}\right)} \right) + \sqrt{2} + 123 - 11 = 123 + \sqrt{2} - \frac{1200}{\int_1^{\frac{1}{18}(\sqrt{3} \pi + \log(27))} \frac{1}{t} dt}$$

Now, we have that:

$$(2-\sqrt{3})/1 - ((2-\sqrt{3})^3)/5 + ((2-\sqrt{3})^5)/9$$

Input:

$$\frac{2-\sqrt{3}}{1} - \frac{1}{5}(2-\sqrt{3})^3 + \frac{1}{9}(2-\sqrt{3})^5$$

Result:

$$2-\sqrt{3} - \frac{1}{5}(2-\sqrt{3})^3 + \frac{1}{9}(2-\sqrt{3})^5$$

Decimal approximation:

0.264255083816048548473083196930930879324910724690811115704...

0.264255083...

Alternate forms:

$$\frac{1}{45}(1666 - 955\sqrt{3})$$

$$\frac{1666}{45} - \frac{191}{3\sqrt{3}}$$

$$\frac{1666}{45} - \frac{209}{3\sqrt{3}} + 2\sqrt{3}$$

Minimal polynomial:

$$2025x^2 - 149940x + 39481$$

$$\pi/16 (\sqrt{3}-1) - (\sqrt{3}-1)/4 \ln(\sqrt{3}-1)$$

Input:

$$\frac{\pi}{16}(\sqrt{3}-1) - \left(\frac{1}{4}(\sqrt{3}-1)\right)\log(\sqrt{3}-1)$$

$\log(x)$ is the natural logarithm

Exact result:

$$\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}(\sqrt{3}-1)\log(\sqrt{3}-1)$$

Decimal approximation:

0.200820482280181765362520097697021888150957177245458456769...

0.2008204822...

Alternate forms:

$$\frac{1}{16} (\sqrt{3} - 1) (\pi - 4 \log(\sqrt{3} - 1))$$

$$-\frac{\pi}{16} + \frac{\sqrt{3}\pi}{16} + \frac{1}{4} \log(\sqrt{3} - 1) - \frac{1}{4} \sqrt{3} \log(\sqrt{3} - 1)$$

Alternative representations:

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) =$$

$$-\frac{1}{4} \log_e(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3})$$

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) =$$

$$-\frac{1}{4} \log(a) \log_a(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3})$$

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) =$$

$$\frac{1}{4} \text{Li}_1(2 - \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3})$$

Series representations:

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) = \frac{1}{16} (-1 + \sqrt{3}) \left(\pi + 4 \sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k} \right)$$

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) = \frac{1}{16} (-1 + \sqrt{3})$$

$$\left(\pi - 8i\pi \left[\frac{\arg(-1 + \sqrt{3} - x)}{2\pi} \right] - 4 \log(x) + 4 \sum_{k=1}^{\infty} \frac{(-1)^k (-1 + \sqrt{3} - x)^k x^{-k}}{k} \right) \text{ for } x < 0$$

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) = \frac{1}{16} (-1 + \sqrt{3}) \pi - \frac{1}{4} (-1 + \sqrt{3})$$

$$\left(2i\pi \left[\frac{\arg(-1 + \sqrt{3} - x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (-1 + \sqrt{3} - x)^k x^{-k}}{k} \right) \text{ for } x < 0$$

Integral representation:

$$\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1) = \frac{1}{16} (-1 + \sqrt{3}) \left(\pi - 4 \int_1^{-1+\sqrt{3}} \frac{1}{t} dt \right)$$

$$\text{colog}(((\text{Pi}/16 (\text{sqrt}3-1)-(\text{sqrt}3-1)/4 \ln(\text{sqrt}3-1))))$$

Input:

$$-\log\left(\frac{\pi}{16} (\sqrt{3} - 1) - \left(\frac{1}{4} (\sqrt{3} - 1)\right) \log(\sqrt{3} - 1)\right)$$

$\log(x)$ is the natural logarithm

Exact result:

$$-\log\left(\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1)\right)$$

Decimal approximation:

1.605343892979195304559844988372774680397405899482994315954...

[1.6053438929.... result very near to the elementary charge](#)

Alternate forms:

$$-\log\left(\frac{1}{16} (\sqrt{3} - 1) (\pi - 4 \log(\sqrt{3} - 1))\right)$$

$$\log(16) - \log\left((\sqrt{3} - 1) (\pi - 4 \log(\sqrt{3} - 1))\right)$$

$$4 \log(2) - \log\left((\sqrt{3} - 1) (\pi - 4 \log(\sqrt{3} - 1))\right)$$

Alternative representations:

$$\begin{aligned} &-\log\left(\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1)\right) = \\ &-\log_e\left(-\frac{1}{4} \log(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3})\right) \end{aligned}$$

$$\begin{aligned} &-\log\left(\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} \log(\sqrt{3} - 1) (\sqrt{3} - 1)\right) = \\ &-\log(a) \log_a\left(-\frac{1}{4} \log(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3})\right) \end{aligned}$$

$$-\log\left(\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}\log(\sqrt{3}-1)(\sqrt{3}-1)\right) = \\ \text{Li}_1\left(1 + \frac{1}{4}\log(-1+\sqrt{3})(-1+\sqrt{3}) - \frac{1}{16}\pi(-1+\sqrt{3})\right)$$

Series representations:

$$-\log\left(\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}\log(\sqrt{3}-1)(\sqrt{3}-1)\right) = \\ \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{16}(-1+\sqrt{3})\pi - \frac{1}{4}(-1+\sqrt{3})\log(-1+\sqrt{3})\right)^k}{k}$$

$$-\log\left(\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}\log(\sqrt{3}-1)(\sqrt{3}-1)\right) = \\ -2i\pi \left[\frac{\arg\left(\frac{1}{16}(-1+\sqrt{3})\pi - x - \frac{1}{4}(-1+\sqrt{3})\log(-1+\sqrt{3})\right)}{2\pi} \right] - \log(x) + \\ \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(\frac{1}{16}(-1+\sqrt{3})\pi - x - \frac{1}{4}(-1+\sqrt{3})\log(-1+\sqrt{3})\right)^k}{k} \quad \text{for } x < 0$$

$$-\log\left(\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}\log(\sqrt{3}-1)(\sqrt{3}-1)\right) = -2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - \\ \log(z_0) + \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{1}{16}(-1+\sqrt{3})\pi - \frac{1}{4}(-1+\sqrt{3})\log(-1+\sqrt{3}) - z_0\right)^k z_0^{-k}}{k}$$

Integral representation:

$$-\log\left(\frac{1}{16}(\sqrt{3}-1)\pi - \frac{1}{4}\log(\sqrt{3}-1)(\sqrt{3}-1)\right) = -\int_1^{\frac{1}{16}(-1+\sqrt{3})\pi - 4\log(-1+\sqrt{3})} \frac{1}{t} dt$$

$$\left(\frac{\pi}{16}(\sqrt{3}-1) - \frac{1}{4}\ln(\sqrt{3}-1)\right)^{1/256}$$

Input:

$$\sqrt[256]{\frac{\pi}{16}(\sqrt{3}-1) - \left(\frac{1}{4}(\sqrt{3}-1)\right)\log(\sqrt{3}-1)}$$

$\log(x)$ is the natural logarithm

Exact result:

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1)}$$

Decimal approximation:

0.993748746317238434063829737183982105349884886475838695558...

0.9937487463172... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

$$\frac{1 + \sqrt[5]{\sqrt{\varphi^5 \sqrt[4]{5^3} - 1}}}{\sqrt{5}} - \varphi + 1$$

and to the dilaton value **0.989117352243 = ϕ**

Alternate forms:

$$\frac{\sqrt[256]{(\sqrt{3} - 1) (\pi - 4 \log(\sqrt{3} - 1))}}{\sqrt[64]{2}}$$

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1) \pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)}$$

All 256th roots of $\frac{1}{16} (\sqrt{3} - 1) \pi - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1)$:

$$e^0 \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1) \pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)} \approx 0.993749 \text{ (real, principal root)}$$

$$e^{(i\pi)/128} \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1) \pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)} \approx 0.993449 + 0.024388 i$$

$$e^{(i\pi)/64} \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1) \pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)} \approx 0.992552 + 0.048761 i$$

$$e^{(3i\pi)/128} \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)} \approx 0.991056 + 0.07310i$$

$$e^{(i\pi)/32} \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi + \frac{1}{4} (1 - \sqrt{3}) \log(\sqrt{3} - 1)} \approx 0.988964 + 0.09740i$$

Alternative representations:

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \sqrt[256]{-\frac{1}{4} \log_e(-1 + \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3})}$$

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \sqrt[256]{-\frac{1}{4} \log(a) \log_a(-1 + \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3})}$$

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \sqrt[256]{\frac{1}{4} \text{Li}_1(2 - \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3})}$$

Series representations:

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \frac{\sqrt[256]{-1 + \sqrt{3}} \sqrt[256]{\pi + 4 \sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k}}}{\sqrt[64]{2}}$$

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \left(\frac{1}{16} (-1 + \sqrt{3})\pi - \frac{1}{4} (-1 + \sqrt{3}) \left(2i\pi \left\lfloor \frac{\arg(-1 + \sqrt{3} - x)}{2\pi} \right\rfloor + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (-1 + \sqrt{3} - x)^k x^{-k}}{k} \right) \right)^{(1/256)} \text{ for } x < 0$$

$$\begin{aligned}
& \sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)^\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \frac{1}{\sqrt[64]{2}} \\
& \sqrt[256]{-1 + \sqrt{3}} \left(\pi - 4 \left(\log(z_0) + \left\lfloor \frac{\arg(-1 + \sqrt{3} - z_0)}{2\pi} \right\rfloor \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (-1 + \sqrt{3} - z_0)^k z_0^{-k}}{k} \right) \right)^{\wedge (1/256)}
\end{aligned}$$

Integral representation:

$$\sqrt[256]{\frac{1}{16} (\sqrt{3} - 1)^\pi - \frac{1}{4} \log(\sqrt{3} - 1)(\sqrt{3} - 1)} = \frac{\sqrt[256]{-1 + \sqrt{3}} \sqrt[256]{\pi - 4 \int_1^{-1+\sqrt{3}} \frac{1}{t} dt}}{\sqrt[64]{2}}$$

1/2 * log base 0.9937487463172 ((Pi/16 (sqrt3-1)-(sqrt3-1)/4 ln(sqrt3-1)))-
Pi+1/golden ratio

Input interpretation:

$$\frac{1}{2} \log_{0.9937487463172} \left(\frac{\pi}{16} (\sqrt{3} - 1) - \left(\frac{1}{4} (\sqrt{3} - 1) \right) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi}$$

log(x) is the natural logarithm

log_b(x) is the base- b logarithm

φ is the golden ratio

Result:

125.47644133...

125.47644133... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

Alternative representations:

$$\frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{2} \log_{0.99374874631720000} \left(-\frac{1}{4} \log_e(-1 + \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3}) \right) + \frac{1}{\phi}$$

$$\frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{\log\left(-\frac{1}{4} \log(-1 + \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3})\right)}{2 \log(0.99374874631720000)}$$

$$\frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{2} \log_{0.99374874631720000} \left(-\frac{1}{4} \log(a) \log_a(-1 + \sqrt{3})(-1 + \sqrt{3}) + \frac{1}{16} \pi(-1 + \sqrt{3}) \right) + \frac{1}{\phi}$$

Series representations:

$$\frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{16} \pi(-1 + \sqrt{3}) - \frac{1}{4} \log(-1 + \sqrt{3})(-1 + \sqrt{3})\right)^k}{k}}{2 \log(0.99374874631720000)}$$

$$\frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} =$$

$$-\frac{1}{2\phi} \left(-2 + 2\phi\pi - \phi \log_{0.99374874631720000} \left(\frac{1}{16} \left(-1 + \exp\left(i\pi \left[\frac{\arg(3-x)}{2\pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!} \right) \right. \right.$$

$$\left. \left. \left(\pi + 4 \sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k} \right) \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\begin{aligned} & \frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} = \\ & - \frac{1}{2\phi} \left(-2 + 2\phi\pi - \phi \log_{0.99374874631720000} \left(\frac{1}{16} \pi \left(-1 + \left(\frac{1}{z_0} \right)^{1/2 [\arg(3-z_0)/(2\pi)]} \right. \right. \right. \\ & \left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!} \right) \right) + \right. \\ & \left. \frac{1}{4} \left(\sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k} \right) \left(-1 + \left(\frac{1}{z_0} \right)^{1/2 [\arg(3-z_0)/(2\pi)]} \right. \right. \\ & \left. \left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!} \right) \right) \right) \end{aligned}$$

Integral representation:

$$\begin{aligned} & \frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) - \pi + \frac{1}{\phi} = \\ & \frac{1}{\phi} - \pi + \frac{1}{2} \log_{0.99374874631720000} \left(\frac{1}{16} \left(\pi - 4 \int_1^{-1+\sqrt{3}} \frac{1}{t} dt \right) (-1 + \sqrt{3}) \right) \end{aligned}$$

1/16 * log base 0.9937487463172 ((Pi/16 (sqrt3-1)-(sqrt3-1)/4 ln(sqrt3-1)))+1/golden ratio

Input interpretation:

$$\frac{1}{16} \log_{0.9937487463172} \left(\frac{\pi}{16} (\sqrt{3} - 1) - \left(\frac{1}{4} (\sqrt{3} - 1) \right) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi}$$

Result:

16.618033989...

16.618033989... result very near to the mass of the hypothetical light particle, the boson $m_x = 16.84 \text{ MeV}$

Alternative representations:

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(-\frac{1}{4} \log_e(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3}) \right) + \frac{1}{\phi}$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{\log \left(-\frac{1}{4} \log(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3}) \right)}{16 \log(0.99374874631720000)}$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(-\frac{1}{4} \log(a) \log_a(-1 + \sqrt{3}) (-1 + \sqrt{3}) + \frac{1}{16} \pi (-1 + \sqrt{3}) \right) +$$

$$\frac{1}{\phi}$$

Series representations:

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{16} \pi (-1 + \sqrt{3}) - \frac{1}{4} \log(-1 + \sqrt{3}) (-1 + \sqrt{3}) \right)^k}{k}}{16 \log(0.99374874631720000)}$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{16 \phi} \left(16 + \phi \log_{0.99374874631720000} \left(\frac{1}{16} \left(-1 + \exp \left(i \pi \left[\frac{\arg(3-x)}{2\pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2} \right)_k}{k!} \right) \right. \right.$$

$$\left. \left. \left(\pi + 4 \sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k} \right) \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{16 \phi} \left(16 + \phi \log_{0.99374874631720000} \left(\frac{1}{16} \pi \left(-1 + \left(\frac{1}{z_0} \right)^{1/2 \lfloor \arg(3-z_0)/(2\pi) \rfloor} \right. \right. \right.$$

$$\left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!} \right) + \right.$$

$$\left. \frac{1}{4} \left(\sum_{k=1}^{\infty} \frac{(-1)^k (-2 + \sqrt{3})^k}{k} \right) \left(-1 + \left(\frac{1}{z_0} \right)^{1/2 \lfloor \arg(3-z_0)/(2\pi) \rfloor} \right. \right.$$

$$\left. \left. \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!} \right) \right) \right)$$

Integral representation:

$$\frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \pi (\sqrt{3} - 1) - \frac{1}{4} (\sqrt{3} - 1) \log(\sqrt{3} - 1) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{1}{16} \log_{0.99374874631720000} \left(\frac{1}{16} \left(\pi - 4 \int_1^{-1+\sqrt{3}} \frac{1}{t} dt \right) (-1 + \sqrt{3}) \right)$$

Now, we have:

$$(\sqrt{3}-1)/1 - ((\sqrt{3}-1)^4)/4 + ((\sqrt{3}-1)^7)/7$$

Input:

$$\frac{\sqrt{3}-1}{1} - \frac{1}{4} (\sqrt{3}-1)^4 + \frac{1}{7} (\sqrt{3}-1)^7$$

Result:

$$-1 + \sqrt{3} - \frac{1}{4} (\sqrt{3}-1)^4 + \frac{1}{7} (\sqrt{3}-1)^7$$

Decimal approximation:

0.676349021071779650066145995233095600034043876166881140608...

0.67634902107...

Alternate forms:

$$\frac{3}{7} (121 \sqrt{3} - 208)$$

$$\frac{363\sqrt{3}}{7} - \frac{624}{7}$$

$$\frac{1}{7}(363\sqrt{3} - 624)$$

Minimal polynomial:

$$49x^2 + 8736x - 5931$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \ln\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)$$

Input:

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)$$

$\log(x)$ is the natural logarithm

Decimal approximation:

0.672942823879357247419360622295200340408846890601104557187...

0.672942823879...

Alternate forms:

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{6} \log(2 + \sqrt{3})$$

$$\frac{1}{12} (\sqrt{3} \pi + \log(7 + 4\sqrt{3}))$$

$$\frac{1}{12} (\sqrt{3} \pi - \log(4) + 4 \log(1 + \sqrt{3}))$$

Alternative representations:

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{1}{3} \log_e\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{1}{3} \log(a) \log_a\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = -\frac{1}{3} \operatorname{Li}_1\left(1 - \frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}$$

Series representations:

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{\pi}{4\sqrt{3}} - \frac{1}{3} \sum_{k=1}^{\infty} \frac{\left(1 - \sqrt{\frac{3}{2} - \frac{1}{\sqrt{2}}}\right)^k}{k}$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{\pi}{4\sqrt{3}} + \frac{2}{3} i\pi \left[\frac{\arg\left(\sqrt{\frac{3}{2} + \frac{1}{\sqrt{2}}} - x\right)}{2\pi} \right] +$$

$$\frac{\log(x)}{3} - \frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2} + \frac{1}{\sqrt{2}}} - x\right)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{\pi}{4\sqrt{3}} + \frac{2}{3} i\pi \left[\frac{\arg\left(\frac{1+\sqrt{3}}{\sqrt{2}} - x\right)}{2\pi} \right] +$$

$$\frac{\log(x)}{3} - \frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2} + \frac{1}{\sqrt{2}}} - x\right)^k x^{-k}}{k} \quad \text{for } x < 0$$

Integral representations:

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt$$

$$\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) = \frac{\pi}{4\sqrt{3}} - \frac{i}{6\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}}\right)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds$$

for $-1 < \gamma < 0$

$$1/10^{27} * (((1 + \text{Pi}/(4\sqrt{3})) + 1/3 \ln(((1 + \sqrt{3})/\sqrt{2}))))$$

Input:

$$\frac{1}{10^{27}} \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right)$$

$\log(x)$ is the natural logarithm

Exact result:

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{1\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000}$$

Decimal approximation:

$$1.6729428238793572474193606222952003404088468906011045... \times 10^{-27}$$

1.672942823... * 10⁻²⁷ result practically equal to the proton mass

Alternate forms:

$$\frac{12 + \sqrt{3} \pi + \log(7 + 4\sqrt{3})}{12\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000}$$

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{6} \log(2 + \sqrt{3})}{1\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000}$$

$$\frac{12 + \sqrt{3} \pi + 4 \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{12\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000\ 000}$$

Alternative representations:

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{10^{27}} = \frac{1 + \frac{1}{3} \log_e\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}{10^{27}}$$

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{10^{27}} = \frac{1 + \frac{1}{3} \log(a) \log_a\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}{10^{27}}$$

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{10^{27}} = \frac{1 - \frac{1}{3} \text{Li}_1\left(1 - \frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}{10^{27}}$$

Integral representations:

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{10^{27}} = \frac{1}{\pi \frac{1000000000000000000000000000000}{4000000000000000000000000000000\sqrt{3}}} + \frac{1}{3000000000000000000000000000000} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt$$

$$\frac{1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)}{10^{27}} = \frac{1}{\pi \frac{1000000000000000000000000000000}{4000000000000000000000000000000\sqrt{3}}} - \frac{6000000000000000000000000000000\pi}{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(\frac{2}{-2+\sqrt{2}+\sqrt{6}}\right)^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \text{ for } -1 < \gamma < 0$$

$10^3 * (((1 + \text{Pi}/(4\text{sqrt}3) + 1/3 \ln(((1 + \text{sqrt}3)/\text{sqrt}2))))))$

Input:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right)$$

log(x) is the natural logarithm

Exact result:

$$1000 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right)$$

Decimal approximation:

1672.942823879357247419360622295200340408846890601104557187...

1672.942823879.... result practically equal to the rest mass of Omega baryon

1672.45

Alternate forms:

$$\frac{250}{3} \left(12 + \sqrt{3} \pi + \log(7 + 4\sqrt{3}) \right)$$

$$1000 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{6} \log(2 + \sqrt{3}) \right)$$

$$1000 + \frac{250\pi}{\sqrt{3}} - \frac{500 \log(2)}{3} + \frac{1000}{3} \log(1 + \sqrt{3})$$

Alternative representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 10^3 \left(1 + \frac{1}{3} \log_e\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}} \right)$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 10^3 \left(1 + \frac{1}{3} \log(a) \log_a\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}} \right)$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 10^3 \left(1 - \frac{1}{3} \text{Li}_1\left(1 - \frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}} \right)$$

Series representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 1000 + \frac{250\pi}{\sqrt{3}} - \frac{1000}{3} \sum_{k=1}^{\infty} \frac{\left(1 - \sqrt{\frac{3}{2}} - \frac{1}{\sqrt{2}}\right)^k}{k}$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 1000 + \frac{250\pi}{\sqrt{3}} + \frac{2000}{3} i\pi \left[\frac{\arg\left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x\right)}{2\pi} \right] +$$

$$\frac{1000 \log(x)}{3} - \frac{1000}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x\right)^k x^{-k}}{k} \quad \text{for } x < 0$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 1000 + \frac{250\pi}{\sqrt{3}} + \frac{2000}{3} i\pi \left[\frac{\arg\left(\frac{1+\sqrt{3}}{\sqrt{2}} - x\right)}{2\pi} \right] +$$

$$\frac{1000 \log(x)}{3} - \frac{1000}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x\right)^k x^{-k}}{k} \quad \text{for } x < 0$$

Integral representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) = 1000 + \frac{250\pi}{\sqrt{3}} + \frac{1000}{3} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) = 1000 + \frac{250\pi}{\sqrt{3}} - \frac{500i}{3\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(\frac{2}{-2+\sqrt{2}+\sqrt{6}} \right)^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

$$10^3 * \left(\left(\left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \ln \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) \right) \right) + (47+7+2)$$

Input:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2)$$

$\log(x)$ is the natural logarithm

Exact result:

$$56 + 1000 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right)$$

Decimal approximation:

1728.942823879357247419360622295200340408846890601104557187...

1728.9428238...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Alternate forms:

$$1056 + \frac{250\pi}{\sqrt{3}} + \frac{500}{3} \log(2 + \sqrt{3})$$

$$1056 + \frac{250\pi}{\sqrt{3}} - \frac{500 \log(2)}{3} + \frac{1000}{3} \log(1 + \sqrt{3})$$

$$1056 + \frac{250\pi}{\sqrt{3}} + \frac{1000}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right)$$

Alternative representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$56 + 10^3 \left(1 + \frac{1}{3} \log_e \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$56 + 10^3 \left(1 + \frac{1}{3} \log(a) \log_a \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$56 + 10^3 \left(1 - \frac{1}{3} \text{Li}_1 \left(1 - \frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)$$

Series representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$1056 + \frac{250\pi}{\sqrt{3}} - \frac{1000}{3} \sum_{k=1}^{\infty} \frac{\left(1 - \sqrt{\frac{3}{2}} - \frac{1}{\sqrt{2}} \right)^k}{k}$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$1056 + \frac{250\pi}{\sqrt{3}} + \frac{2000}{3} i\pi \left[\frac{\arg \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x \right)}{2\pi} \right] +$$

$$\frac{1000 \log(x)}{3} - \frac{1000}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x \right)^k}{k} \quad \text{for } x < 0$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$1056 + \frac{250\pi}{\sqrt{3}} + \frac{2000}{3} i\pi \left[\frac{\arg \left(\frac{1+\sqrt{3}}{\sqrt{2}} - x \right)}{2\pi} \right] + \frac{1000 \log(x)}{3} -$$

$$\frac{1000}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x \right)^k x^{-k}}{k} \quad \text{for } x < 0$$

Integral representations:

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) = 1056 + \frac{250\pi}{\sqrt{3}} + \frac{1000}{3} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt$$

$$10^3 \left(1 + \frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + (47+7+2) =$$

$$1056 + \frac{250\pi}{\sqrt{3}} - \frac{500i}{3\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(\frac{2}{-2+\sqrt{2}+\sqrt{6}} \right)^s \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \quad \text{for } -1 < \gamma < 0$$

$$\left(\left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \ln \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) \right)^{1/64}$$

Input:

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right)}$$

$\log(x)$ is the natural logarithm

Decimal approximation:

0.993830129336892848481245596425518566332174439394912164630...

0.9938301293.... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

and to the dilaton value **0.989117352243 = ϕ**

Alternate forms:

$$\frac{64 \sqrt{\frac{1}{3} (\sqrt{3} \pi + \cosh^{-1}(7))}}{32 \sqrt{2}}$$

$$64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{6} \log(2 + \sqrt{3})}$$

$$64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{3} \left(\log(1 + \sqrt{3}) - \frac{\log(2)}{2} \right)}$$

$\cosh^{-1}(x)$ is the inverse hyperbolic cosine function

All 64th roots of $\pi/(4 \text{ sqrt}(3)) + 1/3 \log((1 + \text{sqrt}(3))/\text{sqrt}(2))$:

$$e^0 64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{3} \log\left(\frac{1 + \sqrt{3}}{\sqrt{2}}\right)} \approx 0.993830 \text{ (real, principal root)}$$

$$e^{(i \pi)/32} 64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{3} \log\left(\frac{1 + \sqrt{3}}{\sqrt{2}}\right)} \approx 0.989045 + 0.09741 i$$

$$e^{(i \pi)/16} 64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{3} \log\left(\frac{1 + \sqrt{3}}{\sqrt{2}}\right)} \approx 0.97473 + 0.19389 i$$

$$e^{(3 i \pi)/32} 64 \sqrt{\frac{\pi}{4 \sqrt{3}} + \frac{1}{3} \log\left(\frac{1 + \sqrt{3}}{\sqrt{2}}\right)} \approx 0.95104 + 0.28849 i$$

$$e^{(i\pi)/8} \sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} \approx 0.91818 + 0.38032i$$

Alternative representations:

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \sqrt[64]{\frac{1}{3} \log_e\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}$$

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \sqrt[64]{\frac{1}{3} \log(a) \log_a\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}$$

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \sqrt[64]{-\frac{1}{3} \text{Li}_1\left(1 - \frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}}$$

Series representations:

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \sqrt[64]{\frac{\pi}{4\sqrt{3}} - \frac{1}{3} \sum_{k=1}^{\infty} \frac{\left(1 - \frac{1+\sqrt{3}}{\sqrt{2}}\right)^k}{k}}$$

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \left(2i\pi \left[\frac{\arg\left(\frac{1+\sqrt{3}}{\sqrt{2}} - x\right)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - x\right)^k x^{-k}}{k} \right)} \quad \text{for } x < 0$$

$$\sqrt[64]{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \left(2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\sqrt{\frac{3}{2}} + \frac{1}{\sqrt{2}} - z_0\right)^k z_0^{-k}}{k} \right) \right)^{\wedge (1/64)}$$

Integral representations:

$$64 \sqrt{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = 64 \sqrt{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \int_1^{1+\sqrt{3}} \frac{1}{t} dt}$$

$$64 \sqrt{\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right)} = 64 \sqrt{\frac{\pi}{4\sqrt{3}} - \frac{i}{6\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}}\right)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds}$$

for $-1 < \gamma < 0$

2 log base 0.9938301293368 (((((Pi/(4sqrt3)+1/3 ln (((1+sqrt3)/sqrt2)))))))-
Pi+1/golden ratio

Input interpretation:

$$2 \log_{0.9938301293368} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) - \pi + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

125.47644133...

125.47644133... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

Alternative representations:

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + 2 \log_{0.99383012933680000} \left(\frac{1}{3} \log_e\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}} \right) + \frac{1}{\phi}$$

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + \frac{1}{\phi} + \frac{2 \log\left(\frac{1}{3} \log\left(\frac{1+\sqrt{3}}{\sqrt{2}}\right) + \frac{\pi}{4\sqrt{3}}\right)}{\log(0.99383012933680000)}$$

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} =$$

$$-\pi + 2 \log_{0.99383012933680000} \left(\frac{1}{3} \log(a) \log_a \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right) + \frac{1}{\phi}$$

Series representations:

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)^k}{k}}{\log(0.99383012933680000)}$$

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} = -\frac{1}{\phi} \left(-1 + \phi \pi - \right.$$

$$2 \phi \log_{0.99383012933680000} \left(\frac{\pi}{4 \exp \left(i \pi \left[\frac{\arg(3-x)}{2\pi} \right] \right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2} \right)_k}{k!}} \right. -$$

$$\left. \left. \frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}} \right)^k}{k} \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} =$$

$$-\frac{1}{\phi} \left(-1 + \phi \pi - 2 \phi \log_{0.99383012933680000} \left(-\frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}} \right)^k}{k} + \right.$$

$$\left. \left. \frac{\pi \left(\frac{1}{z_0} \right)^{-1/2 [\arg(3-z_0)/(2\pi)]} z_0^{1/2 (-1 - [\arg(3-z_0)/(2\pi)])}}{4 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!}} \right) \right)$$

Integral representations:

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.99383012933680000} \left(\frac{1}{3} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt + \frac{\pi}{4\sqrt{3}} \right)$$

$$2 \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi + 2 \log_{0.99383012933680000} \left(\frac{1}{6i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}}\right)^{-s}}{\Gamma(1-s)} ds + \frac{\pi}{4\sqrt{3}} \right) \text{ for } -1 < \gamma < 0$$

Note that, this result, the dilaton mass calculated as a type of Higgs boson, is ALWAYS linked to the golden ratio. Indeed, we have that:

$$2 \log \text{ base } 0.9938301293368 \left(\left(\left(\left(\left(\left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \ln \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) \right) \right) \right) \right) \right) - \pi + \frac{1}{x} = 125.47644133$$

Input interpretation:

$$2 \log_{0.9938301293368} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) - \pi + \frac{1}{x} = 125.47644133$$

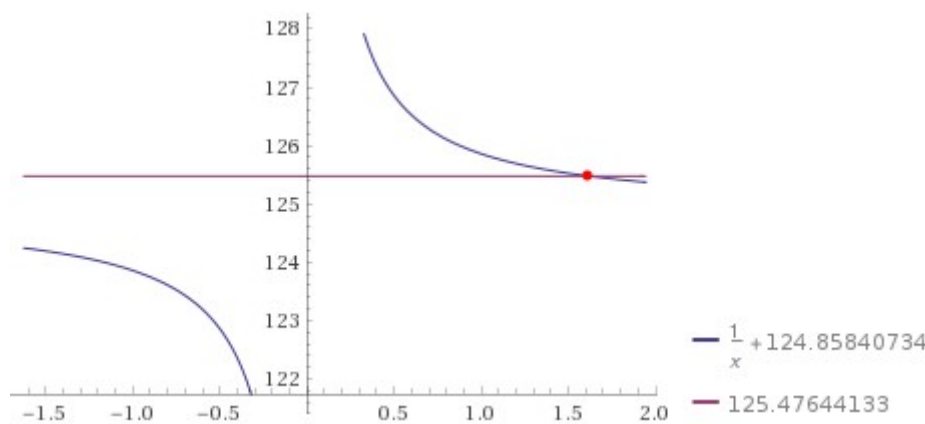
log(x) is the natural logarithm

log_b(x) is the base- b logarithm

Result:

$$\frac{1}{x} + 124.85840734 = 125.47644133$$

Plot:



Alternate form assuming x is real:

$$\frac{1.6180340}{x} = 1.0000000$$

Alternate form:

$$\frac{124.8584073 (1.0000000000 x + 0.008009072206)}{x} = 125.47644133$$

Alternate form assuming x is positive:

$$1.0000000 x = 1.6180340 \text{ (for } x \neq 0)$$

Solution:

$$x \approx 1.6180340$$

1.6180340 = golden ratio

1/4 log base 0.9938301293368 (((((Pi/(4sqrt3))+1/3 ln
(((1+sqrt3)/sqrt2)))))))+1/golden ratio

Input interpretation:

$$\frac{1}{4} \log_{0.9938301293368} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi}$$

φ is the golden ratio

Result:

16.618033989...

16.61803398... result very near to the mass of the hypothetical light particle, the boson m_x = 16.84 MeV

Alternative representations:

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{1}{3} \log_e \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right) + \frac{1}{\phi}$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{\log \left(\frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)}{4 \log(0.99383012933680000)}$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{1}{3} \log(a) \log_a \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right) + \frac{1}{\phi}$$

Series representations:

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \frac{\sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) + \frac{\pi}{4\sqrt{3}} \right)^k}{k}}{4 \log(0.99383012933680000)}$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{4\phi} \left(4 + \phi \log_{0.99383012933680000} \left(\frac{\pi}{4 \exp(i\pi \left[\frac{\arg(3-x)}{2\pi} \right]) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (3-x)^k x^{-k} \left(-\frac{1}{2} \right)_k}{k!}} - \frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}} \right)^k}{k} \right) \right) \text{ for } (x \in \mathbb{R} \text{ and } x < 0)$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{4\phi} \left(4 + \phi \log_{0.99383012933680000} \left(-\frac{1}{3} \sum_{k=1}^{\infty} \frac{(-1)^k \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}} \right)^k}{k} + \frac{\pi \left(\frac{1}{z_0} \right)^{-1/2 [\arg(3-z_0)/(2\pi)]} z_0^{1/2 (-1 - [\arg(3-z_0)/(2\pi)])}}{4 \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2} \right)_k (3-z_0)^k z_0^{-k}}{k!}} \right) \right)$$

Integral representations:

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{1}{4} \log_{0.99383012933680000} \left(\frac{1}{3} \int_1^{\frac{1+\sqrt{3}}{\sqrt{2}}} \frac{1}{t} dt + \frac{\pi}{4\sqrt{3}} \right)$$

$$\frac{1}{4} \log_{0.99383012933680000} \left(\frac{\pi}{4\sqrt{3}} + \frac{1}{3} \log \left(\frac{1+\sqrt{3}}{\sqrt{2}} \right) \right) + \frac{1}{\phi} =$$

$$\frac{1}{\phi} + \frac{1}{4} \log_{0.99383012933680000} \left(\frac{1}{6i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{1+\sqrt{3}}{\sqrt{2}}\right)^{-s}}{\Gamma(1-s)} ds + \frac{\pi}{4\sqrt{3}} \right)$$

for $-1 < \gamma < 0$

Ramanujan mathematics applied to the physics and cosmology

From:

Trans-Planckian Censorship and the Swampland

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points as well, as long as it is sufficiently unstable quantum mechanically. We find that in a meta-stable dS point is compatible with TCC as long as its lifetime T is bounded by

$$T \leq \frac{1}{H} \log \frac{M_p}{H} \quad (1.1)$$

where H is the Hubble parameter and is related to the cosmological constant by $\frac{(d-1)(d-2)}{2} H^2 = V = \Lambda$ in d spacetime dimensions. Also, for unstable critical points, we find a condition similar to the refined dS conjecture which puts a bound on $|V''|/V$ [6]. Moreover, we find that for any expansionary period of the universe for matter with equation of state $w \geq -1$, measurement of H will give an upper bound to the age of the observed universe. The upper bound is the same as the (1.1) with H being the measured value of the Hubble parameter at time T after the expansion started.

where we used the Friedmann equation $(d-1)(d-2)H_i^2/2 = V_{max}$. According to (B.4), the above expression is less than $\Delta\phi$. Therefore, for these initial conditions, $\phi \in [\phi_0, \phi_0 + \Delta\phi]$ for every $t \leq c\sqrt{2/|V''|_{max}}$. If we set $t = c\sqrt{2/|V''|_{max}}$, from (2.4) we find

Now we use the inequality (B.1) that we just proved to obtain a result for quadratic potentials. Suppose the quadratic potential $V(\phi)$ has local maximum $V(\phi_0) = V_0$ and second derivative $-|V''|$ over a field range $[\phi_0, \phi_0 + \sqrt{\frac{2(1-c)V_0}{|V''|}}]$ for some $0 \leq c \leq 1$. This field range corresponds to the potential range $[V_{\min}, V_0]$ where $V_{\min} = cV_0$. Let k be positive number smaller than 1. We can weaken the (B.1) by multiplying the right hand side of the second inequality by k as

$$\Delta\phi < \frac{B_1(d)B_2(d)^{\frac{3}{4}}V_{\max}^{\frac{d-1}{4}}V_{\min}^{\frac{3}{4}}\ln\left(\frac{B_3(d)}{\sqrt{V_{\min}}}\right)^{\frac{1}{2}}}{V_{\min}B_2(d) - |V''|_{\max}\ln\left(\frac{B_3(d)}{\sqrt{V_{\min}}}\right)^2}, \quad \text{or} \quad \frac{|V''|_{\max}}{V_{\min}} \geq kB_2(d)\ln\left(\frac{B_3(d)}{\sqrt{V_{\min}}}\right)^{-2}. \quad (\text{B.18})$$

If

$$H_0 = 71 \frac{\text{km/s}}{\text{Mpc}} = 2.3 \times 10^{-18} \text{ s}^{-1}$$

$$t_H = \frac{1}{2.3 \times 10^{-18} \text{ s}^{-1}} = 13.8 \times 10^9 \text{ years}$$

We have that, for $d = 4$:

$$V_{\max} = (((((4-1)(4-2) (2.3 \times 10^{-18})^2))))/2$$

Input interpretation:

$$\frac{1}{2} ((4-1)(4-2)(2.3 \times 10^{-18})^2)$$

Result:

$$1.587 \times 10^{-35}$$

$$1.587 * 10^{-35} = V_{\max} = V_0$$

For

$0 \leq c \leq 1$. $c = 1/8 = 0.125$, we obtain:

$$V_{\min} = c * V_0 = c * V_{\max} = 1/8 * (((((((4-1)(4-2) (2.3 \times 10^{-18})^2))))))$$

Input interpretation:

$$\frac{1}{8} \left(\frac{1}{2} ((4-1)(4-2)(2.3 \times 10^{-18})^2) \right)$$

Result:

$$1.98375 \times 10^{-36}$$

$$1.98375 * 10^{-36} = V_{\min}$$

Suppose we have a quadratic potential given by

$$V(\phi) = \frac{V''(\phi_0)}{2} (\phi - \phi_0)^2 + V(\phi_0), \quad (4.2)$$

where $V''(\phi_0) < 0$. In [7], for the case of $d = 4$, it was shown that a gaussian probability distribution centered at $\phi = \phi_0$ solves the Fokker-Planck equation describing the evolution of quantum fluctuations. That result could be easily generalized to the following solution for any dimension $d > 2$.

$$Pr[\phi = \phi_c; t] \propto \exp\left[-\frac{\phi_c^2}{2\sigma(t)^2}\right], \quad (4.3)$$

where

$$\sigma(t) = \frac{\sqrt{d-1} H^2 \left(c \frac{2|V''(\phi_0)|t}{(\sigma-1)H} + 1\right)^{1/2}}{2\pi \sqrt{2|V''(\phi_0)|}}. \quad (4.4)$$

Now we use the inequality (B.1) that we just proved to obtain a result for quadratic potentials. Suppose the quadratic potential $V(\phi)$ has local maximum $V(\phi_0) = V_0$ and second derivative $-|V''|$ over a field range $[\phi_0, \phi_0 + \sqrt{\frac{2(1-c)V_0}{|V''|}}]$ for some $0 \leq c \leq 1$. This field range corresponds to the potential range $[V_{\min}, V_0]$ where $V_{\min} = cV_0$. Let k be positive number smaller than 1. We can weaken the (B.1) by multiplying the right hand side of the second inequality by k as

where $V_{\max} = V(\phi_0)$ and $V_{\min} = V(\phi_0 + \Delta\phi)$ are respectively the maximum and the minimum of V over $\phi \in [\phi_0, \Delta\phi]$, and $B_1(d)$, $B_2(d)$, and $B_3(d)$ are $O(1)$ numbers given by

Now, from:

$$B_1(d) = \frac{\Gamma\left(\frac{d+1}{2}\right)^{\frac{1}{2}} 2^{1+\frac{d}{4}}}{\pi^{\frac{d-1}{4}} ((d-1)(d-2))^{\frac{d-1}{4}}},$$

$$B_2(d) = \frac{4}{(d-1)(d-2)},$$

$$B_3(d) = \sqrt{\frac{(d-1)(d-2)}{2}}.$$

We obtain:

$$\left(\frac{\Gamma\left(\frac{5}{2}\right)^{\frac{1}{2}} 2^2}{\pi^{\frac{3}{4}} ((4-1)(4-2))^{\frac{3}{4}}}\right)$$

Input:

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) \times 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}}$$

$\Gamma(x)$ is the gamma function

Exact result:

$$\frac{2 \sqrt[4]{2} \Gamma\left(\sqrt{\frac{5}{2}}\right)}{(3\pi)^{3/4}}$$

Decimal approximation:

0.394203368273179051333918767928334148165287494722133931228...

0.394203368273.... = $B_1(d)$

Alternate form:

$$\frac{2 \left(\frac{2}{3\pi}\right)^{3/4} \sqrt{\frac{5}{2}} !}{\sqrt{5}}$$

$n!$ is the factorial function

Alternative representations:

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{4 e^{-\log G\left(\sqrt{5/2}\right) + \log G\left(1 + \sqrt{5/2}\right)}}{6^{3/4} \pi^{3/4}}$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{4 G\left(1 + \sqrt{\frac{5}{2}}\right)}{G\left(\sqrt{\frac{5}{2}}\right) (6^{3/4} \pi^{3/4})}$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{4 \left(-1 + \sqrt{\frac{5}{2}}\right)!}{6^{3/4} \pi^{3/4}}$$

Series representations:

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2} \sum_{k=0}^{\infty} \frac{\left(\sqrt{\frac{5}{2}} - z_0\right)^k \Gamma^{(k)}(z_0)}{k!}}{(3\pi)^{3/4}} \quad \text{for } (z_0 \notin \mathbb{Z} \text{ or } z_0 > 0)$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2}}{(3\pi)^{3/4} \sum_{k=1}^{\infty} \left(\frac{5}{2}\right)^{k/2} c_k}$$

for $\left(c_1 = 1 \text{ and } c_2 = 1 \text{ and } c_k = \frac{\gamma c_{-1+k} + \sum_{j=1}^{-2+k} (-1)^{1+j+k} c_j \zeta(-j+k)}{-1+k} \right)$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2} \pi}{3^{3/4} \sum_{k=0}^{\infty} \left(\sqrt{\frac{5}{2}} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} \pi (-j+k+2z_0)\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}}$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2} \pi}{3^{3/4} \sum_{k=0}^{\infty} \left(\sqrt{\frac{5}{2}} - z_0\right)^k \sum_{j=0}^k \frac{(-1)^j \pi^{-j+k} \sin\left(\frac{1}{2} (-j+k)\pi + \pi z_0\right) \Gamma^{(j)}(1-z_0)}{j!(-j+k)!}}$$

Integral representations:

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2}}{(3\pi)^{3/4}} \int_0^1 \log^{-1+\sqrt{5/2}}\left(\frac{1}{t}\right) dt$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2}}{(3\pi)^{3/4}} \int_0^{\infty} e^{-t} t^{-1+\sqrt{5/2}} dt$$

$$\frac{\Gamma\left(\sqrt{\frac{5}{2}}\right) 2^2}{\pi^{3/4} ((4-1)(4-2))^{3/4}} = \frac{2 \sqrt[4]{2} \exp\left(\int_0^1 \frac{-1-\sqrt{\frac{5}{2}}(-1+x)+x\sqrt{5/2}}{(-1+x)\log(x)} dx\right)}{(3\pi)^{3/4}}$$

$$B_2(d) = \frac{4}{(d-1)(d-2)},$$

$$4/(4-1)(4-2)$$

$$D(V_0, d) = \frac{c^{\frac{1}{2}} B_2(d)^{\frac{1}{2}} B_1(d)^2 V_0^{\frac{d-2}{2}}}{4(1-c)} \ln \left(\frac{B_3(d)}{\sqrt{cV_0}} \right)^{-1}$$

For $c = 1/8$; $1.587 \times 10^{-35} = V_{\max} = V_0$; $0.394203368273\dots = B_1(d)$;

$0.666666\dots = B_2(d)$; $1.7320508075688\dots = B_3(d)$, we obtain:

$$\sqrt{0.125} * \sqrt{0.666666} * (0.394203368273)^2 * (1.587e-35) * 1/(4(1-0.125)) * \ln \left(\frac{1.7320508075688}{\sqrt{0.125 * 0.394203368273}} \right)^{-1}$$

Input interpretation:

$$\sqrt{0.125} \sqrt{0.666666} \times 0.394203368273^2 \times 1.587 \times 10^{-35} \times \frac{1}{4(1-0.125)} \log \left(\frac{1}{\frac{1.7320508075688}{\sqrt{0.125 \cdot 0.394203368273}}} \right)$$

log(x) is the natural logarithm

Result:

$$-4.17887\dots \times 10^{-37}$$

$$-4.17887\dots * 10^{-37}$$

Now, we have that:

$$[\bar{\phi}, \bar{\phi}] = \frac{i}{\frac{\pi^{d-1/2}}{\Gamma((d+1)/2)} \left(\frac{1}{H}\right)^{d-1}}$$

$$i / \left(\frac{\pi^{4-1/2}}{\Gamma(5/2)} \left(\frac{1}{2.3 \times 10^{-18}} \right)^3 \right)$$

Input interpretation:

$$\frac{i}{\frac{\pi^{4-1/2}}{\Gamma(5/2)} \left(\frac{1}{2.3 \times 10^{-18}} \right)^3}$$

$\Gamma(x)$ is the gamma function

i is the imaginary unit

Result:

$$2.94303\dots \times 10^{-55} i$$

Polar coordinates:

$$r = 2.94303 \times 10^{-55} \text{ (radius), } \theta = 90^\circ \text{ (angle)}$$

$$2.94303... * 10^{-55}$$

And:

$$\delta\phi_i \delta\dot{\phi}_i \geq \frac{\Gamma((d+1)/2) H^{d-1}}{2\pi^{d-1/2}}$$

$$(((\text{gamma}(((5/2)))))) * (((2.3e-18)^3)) * 1 / ((2\text{Pi}^{(4-1/2)}))$$

Input interpretation:

$$\Gamma\left(\frac{5}{2}\right) (2.3 \times 10^{-18})^3 \times \frac{1}{2\pi^{4-1/2}}$$

$\Gamma(x)$ is the gamma function

Result:

$$1.47152... \times 10^{-55}$$

$$1.47152... * 10^{-55}$$

We note that:

$$\left[\frac{1}{\left(\frac{\text{Pi}^{(4-1/2)}}{\left(\text{gamma} \left(\frac{5}{2} \right) \right) * \left(\frac{1}{(2.3e-18)^3} \right)} \right)} \right] * \frac{1}{\left(\text{gamma} \left(\frac{5}{2} \right) \right) * \left((2.3e-18)^3 \right) * \frac{1}{(2\text{Pi}^{(4-1/2)})}}$$

Input interpretation:

$$\frac{1}{\frac{\pi^{4-1/2}}{\Gamma\left(\frac{5}{2}\right)} \left(\frac{1}{2.3 \times 10^{-18}}\right)^3} \times \frac{1}{\Gamma\left(\frac{5}{2}\right) (2.3 \times 10^{-18})^3 \times \frac{1}{2\pi^{4-1/2}}}$$

$\Gamma(x)$ is the gamma function

Result:

2

2 result equal to the graviton spin

Or:

$$(((\text{gamma}(((5/2)))))) * (((2.3e-18)^3)) * 1 / ((2\text{Pi}^{(4-1/2)})) * \frac{1}{\left(\frac{i}{\left(\frac{\text{Pi}^{(4-1/2)}}{\left(\text{gamma} \left(\frac{5}{2} \right) \right) * \left(\frac{1}{(2.3e-18)^3} \right)} \right)} \right)}$$

Input interpretation:

$$\Gamma\left(\frac{5}{2}\right) (2.3 \times 10^{-18})^3 \times \frac{1}{2\pi^{4-1/2}} \times \frac{1}{\frac{i}{\pi^{4-1/2} \times \frac{1}{\Gamma\left(\frac{5}{2}\right)} \left(\frac{1}{2.3 \times 10^{-18}}\right)^3}}$$

$\Gamma(x)$ is the gamma function
 i is the imaginary unit

Result:

$-0.5 i$

Polar coordinates:

$r = 0.5$ (radius), $\theta = -90^\circ$ (angle)

$0.5 = 1/2$ result equal to the electron spin

From:

**EVALUATIONS OF RAMANUJAN-WEBER
 CLASS INVARIANT g_n**

S. Bhargava 1, K. R. Vasuki and B. R. Srivatsa Kumar

2000 Mathematics subject classification: 11F20, 11Y99

Then

$$(i) \quad \lambda_n \lambda_{1/n} = 1, \tag{2.17}$$

$$(ii) \quad \lambda_1 = 1, \tag{2.18}$$

and

$$(iii) \quad \lambda_n = g_{2n}. \tag{2.19}$$

Theorem 3.3. We have

$$(i) \quad g_{28} = 2^{1/8} (3 + \sqrt{7})^{1/4} = g_{1/7}^{-1},$$

and

$$(ii) \quad g_7 = 2^{-3/8} (3 + \sqrt{7})^{1/4} = g_{4/7}^{-1}.$$

$$2^{1/8} (3 + \sqrt{7})^{1/4}$$

Input:

$$\sqrt[8]{2} \sqrt[4]{3 + \sqrt{7}}$$

Decimal approximation:

1.680966991582255116285078686572690826334508255159186986821...

1.6809669915...

Alternate form:

$$\sqrt[4]{2} \sqrt[8]{8 + 3\sqrt{7}}$$

Minimal polynomial:

$$x^{16} - 64x^8 + 16$$

$$\begin{aligned}
 (iv) \quad & 32 \left[(\lambda_n \lambda_{121n})^{10} + \frac{1}{(\lambda_n \lambda_{121n})^{10}} \right] + 352 \left[(\lambda_n \lambda_{121n})^8 + \frac{1}{(\lambda_n \lambda_{121n})^8} \right] \\
 & + 1672 \left[(\lambda_n \lambda_{121n})^6 + \frac{1}{(\lambda_n \lambda_{121n})^6} \right] + 4576 \left[(\lambda_n \lambda_{121n})^4 + \frac{1}{(\lambda_n \lambda_{121n})^4} \right] \\
 & + 8096 \left[(\lambda_n \lambda_{121n})^2 + \frac{1}{(\lambda_n \lambda_{121n})^2} \right] + 9744 = \left(\frac{\lambda_{121n}}{\lambda_n} \right)^{12} + \left(\frac{\lambda_n}{\lambda_{121n}} \right)^{12}, \quad (2.23)
 \end{aligned}$$

$$\begin{aligned}
 & 32*((1.68096699^{10}+1/(1.68096699^{10}))) + 352(((1.68096699^8+1/(1.68096699^8))) \\
 &) + 1672((1.68096699^6+1/(1.68096699^6))) + 4576(((1.68096699^4+1/(1.68096699^4))) \\
 & + 8096(1.68096699^2+1/(1.68096699^2))) + 9744
 \end{aligned}$$

Input interpretation:

$$\begin{aligned}
 & 32 \left(1.68096699^{10} + \frac{1}{1.68096699^{10}} \right) + \\
 & 352 \left(\left(1.68096699^8 + \frac{1}{1.68096699^8} \right) + 1672 \left(1.68096699^6 + \frac{1}{1.68096699^6} \right) + \right. \\
 & \quad \left. 4576 \left(1.68096699^4 + \frac{1}{1.68096699^4} \right) + \right. \\
 & \quad \left. 8096 \left(1.68096699^2 + \frac{1}{1.68096699^2} \right) \right) + 9744
 \end{aligned}$$

Result:

3.54656055435111249952510626904885558099066308363952005... × 10⁷

3.5465605543511124... * 10⁷

$$(1/1.68096699)^{12}+(1.68096699)^{12}$$

Input interpretation:

$$\left(\frac{1}{1.68096699}\right)^{12} + 1.68096699^{12}$$

Result:

508.9931024493161196452074821479830564697428180678055597357...

508.9931024...

$$3.54656055435111249952510626904885558099066308363952005 \times 10^7 /$$

508.9931024493161196452074821479830564697428180678055597357

Input interpretation:

$$\frac{3.54656055435111249952510626904885558099066308363952005 \times 10^7}{508.9931024493161196452074821479830564697428180678055597357}$$

Result:

69677.96886214715420907906626923031642213207440652315556235...

69677.9688621...

$$(69677.9688621471542)*1/128 - 48$$

Input interpretation:

$$69677.9688621471542 \times \frac{1}{128} - 48$$

Result:

496.3591317355246421875

496.3591317... result concerning the dimension of the gauge group of type I string theory that is 496.

$$(69677.9688621471542)+64^2-322+29+11$$

Input interpretation:

$$69\,677.9688621471542 + 64^2 - 322 + 29 + 11$$

Result:

$$73491.9688621471542$$

$$73491.968862\dots$$

Thence, we have the following mathematical connections:

$$(69\,677.9688621471542 + 64^2 - 322 + 29 + 11) = 73491.968\dots \Rightarrow$$

$$\Rightarrow -3927 + 2 \left(\sqrt[13]{N \exp \left[\int d\hat{\sigma} \left(-\frac{1}{4u^2} \mathbf{P}_i D \mathbf{P}_i \right) \right] |Bp\rangle_{\text{NS}} + \int [d\mathbf{X}^\mu] \exp \left\{ \int d\hat{\sigma} \left(-\frac{1}{4v^2} D \mathbf{X}^\mu D^2 \mathbf{X}^\mu \right) \right\} | \mathbf{X}^\mu, \mathbf{X}^i = 0 \rangle_{\text{NS}}} \right) =$$

$$-3927 + 2 \sqrt[13]{2.2983717437 \times 10^{59} + 2.0823329825883 \times 10^{59}}$$

$$= 73490.8437525\dots \Rightarrow$$

$$\Rightarrow \left(A(r) \times \frac{1}{B(r)} \left(-\frac{1}{\phi(r)} \right) \times \frac{1}{e^{\Lambda(r)}} \right) \Rightarrow$$

$$\Rightarrow \left(-0.000029211892 \times \frac{1}{0.0003644621} \left(-\frac{1}{0.0005946833} \right) \times \frac{1}{0.00183393} \right) =$$

$$= 73491.78832548118710549159572042220548025195726563413398700\dots$$

$$= 73491.7883254\dots \Rightarrow$$

$$\left(I_{21} \ll \int_{-\infty}^{+\infty} \exp \left(-\left(\frac{t}{H} \right)^2 \right) \left| \sum_{\lambda \leq p^{1-\varepsilon_2}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)} \right|^2 dt \ll \right.$$

$$\left. \ll H \left\{ \left(\frac{4}{\varepsilon_2 \log T} \right)^{2r} (\log T) (\log X)^{-2\beta} + (\varepsilon_2^{-2r} (\log T)^{-2r} + \varepsilon_2^{-r} h_1^r (\log T)^{-r} \right) T^{-\varepsilon_1} \right\} \right)$$

$$/(26 \times 4)^2 - 24 = \left(\frac{7.9313976505275 \times 10^8}{(26 \times 4)^2 - 24} \right) = 73493.30662\dots$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N D p -branes in the limit of $u \rightarrow \infty$, with the ratio concerning the general asymptotically flat solution of the equations of motion of the p -brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

From:

STRING THEORY VOLUME II - Superstring Theory and Beyond

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11.2 The $SO(32)$ and $E_8 \times E_8$ heterotic strings

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Table 11.2. *Low-lying heterotic string states.*

m^2	NS	R	$\tilde{N}\tilde{S}$	\tilde{R}
$-4/\alpha'$	(1, 1)	-	-	-
0	$(\mathbf{8}_v, \mathbf{1}) + (\mathbf{1}, \mathbf{496})$	-	$\mathbf{8}_v$	$\mathbf{8}$

is the type I supergravity multiplet. The product

$$(\mathbf{1}, \mathbf{496}) \times (\mathbf{8}_v + \mathbf{8}) = (\mathbf{8}_v, \mathbf{496}) + (\mathbf{8}, \mathbf{496}) \quad (11.2.18)$$

is an $N = 1$ gauge multiplet in the adjoint of $SO(32)$. The latter is therefore a gauge symmetry in spacetime.

$$496 * 16 = 8*496 + 8*496 = 7936; 7936/16 = 496$$

The chiral fields of $N = 1$ supergravity with gauge group g are the gravitino $\mathbf{56}$, a neutral fermion $\mathbf{8}'$, and an $\mathbf{8}$ gaugino in the adjoint representation, for total anomaly

$$\begin{aligned}\hat{I}_1 &= \hat{I}_{56}(R_2) - \hat{I}_8(R_2) + \hat{I}_8(F_2, R_2) \\ &= \frac{1}{1440} \left\{ -\text{Tr}_a(F_2^6) + \frac{1}{48} \text{Tr}_a(F_2^2) \text{Tr}_a(F_2^4) - \frac{[\text{Tr}_a(F_2^2)]^3}{14400} \right\} \\ &\quad + (n - 496) \left\{ \frac{\text{tr}(R_2^6)}{725760} + \frac{\text{tr}(R_2^4) \text{tr}(R_2^2)}{552960} + \frac{[\text{tr}(R_2^2)]^3}{1327104} \right\} + \frac{Y_4 X_8}{768}.\end{aligned}\tag{12.2.27}$$

Here

$$Y_4 = \text{tr}(R_2^2) - \frac{1}{30} \text{Tr}_a(F_2^2), \tag{12.2.28a}$$

$$X_8 = \text{tr}(R_2^4) + \frac{[\text{tr}(R_2^2)]^2}{4} - \frac{\text{Tr}_a(F_2^2) \text{tr}(R_2^2)}{30} + \frac{\text{Tr}_a(F_2^4)}{3} - \frac{[\text{Tr}_a(F_2^2)]^2}{900}.\tag{12.2.28b}$$

$$1/1440(-1+1/48-1/14400)+(((1-1/30)*(1+1/4-1/30+1/3-1/900)*1/768))$$

Input:

$$\frac{1}{1440} \left(-1 + \frac{1}{48} - \frac{1}{14400} \right) + \left(1 - \frac{1}{30} \right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900} \right) \times \frac{1}{768}$$

Exact result:

$$\frac{13}{10240}$$

Decimal form:

0.00126953125

0.00126953125

$$1/(((1/1440(-1+1/48-1/14400)+(((1-1/30)*(1+1/4-1/30+1/3-1/900)*1/768))))))$$

Input:

$$\frac{1}{\frac{1}{1440} \left(-1 + \frac{1}{48} - \frac{1}{14400} \right) + \left(1 - \frac{1}{30} \right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900} \right) \times \frac{1}{768}}$$

Exact result:

$$\frac{10\,240}{13}$$

Decimal approximation:

787.6923076923076923076923076923076923076923076923076923076923076...

787.692307... result in the range of the rest mass of Omega meson 782.65

$$1/(2\pi) * 1/(((1/1440(-1+1/48-1/14400))+(((1-1/30)*(1+1/4-1/30+1/3-1/900)*1/768))))))$$

Input:

$$\frac{1}{2\pi} \times \frac{1}{\frac{1}{1440} \left(-1 + \frac{1}{48} - \frac{1}{14400}\right) + \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right) \times \frac{1}{768}}$$

Result:

$$\frac{5120}{13\pi}$$

Decimal approximation:

125.3651244046929414056438259180420820948359055678672334750...

125.3651244... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0

Property:

$\frac{5120}{13\pi}$ is a transcendental number

Alternative representations:

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)}{(360^\circ) \left(\frac{1}{768} \left(1 - \frac{1}{30}\right) \left(\frac{4}{3} + \frac{1}{4} - \frac{1}{30} - \frac{1}{900}\right) + \frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440}\right)}$$

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{1}{(2i \log(-1)) \left(\frac{1}{768} \left(1 - \frac{1}{30}\right) \left(\frac{4}{3} + \frac{1}{4} - \frac{1}{30} - \frac{1}{900}\right) + \frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440}\right)}$$

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{1}{(2 \cos^{-1}(-1)) \left(\frac{1}{768} \left(1 - \frac{1}{30}\right) \left(\frac{4}{3} + \frac{1}{4} - \frac{1}{30} - \frac{1}{900}\right) + \frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440}\right)}$$

Series representations:

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{1280}{13 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{1280}{13 \sum_{k=0}^{\infty} \frac{(-1)^{1+k} 1195^{-1-2k} (5^{1+2k} - 4 \cdot 239^{1+2k})}{1+2k}}$$

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{5120}{13 \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)}$$

Integral representations:

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{1280}{13 \int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{1}{\left(\frac{-1+\frac{1}{48}-\frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{2560}{13 \int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{1}{\left(\frac{-1 + \frac{1}{48} - \frac{1}{14400}}{1440} + \frac{1}{768} \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right)\right) (2\pi)} = \frac{2560}{13 \int_0^1 \frac{1}{\sqrt{1-t^2}} dt}$$

$$\left(\left(\frac{1}{1440}(-1 + \frac{1}{48} - \frac{1}{14400}) + \left(\left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right) \times \frac{1}{768}\right)\right)\right)^{1/4096}$$

Input:

$$\sqrt[4096]{\frac{1}{1440} \left(-1 + \frac{1}{48} - \frac{1}{14400}\right) + \left(1 - \frac{1}{30}\right) \left(1 + \frac{1}{4} - \frac{1}{30} + \frac{1}{3} - \frac{1}{900}\right) \times \frac{1}{768}}$$

Result:

$$\frac{\sqrt[4096]{\frac{13}{5}}}{2^{11/4096}}$$

Decimal approximation:

0.998373124715361463734496936500441896498740668311999305568...

0.9983731247... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

Alternate form:

$$\frac{1}{10} \sqrt[4096]{\frac{13}{5}} 2^{4085/4096} \times 5^{4095/4096}$$

All 4096th roots of 13/10240:

$$\frac{\sqrt[4096]{\frac{13}{5}} e^0}{2^{11/4096}} \approx 0.9983731 \quad (\text{real, principal root})$$

$$\frac{\sqrt[4096]{\frac{13}{5}} e^{(i\pi)/2048}}{2^{11/4096}} \approx 0.9983720 + 0.0015315 i$$

$$\frac{4096 \sqrt{\frac{13}{5}} e^{(i\pi)/1024}}{2^{11/4096}} \approx 0.9983684 + 0.0030630 i$$

$$\frac{4096 \sqrt{\frac{13}{5}} e^{(3i\pi)/2048}}{2^{11/4096}} \approx 0.9983626 + 0.0045944 i$$

$$\frac{4096 \sqrt{\frac{13}{5}} e^{(i\pi)/512}}{2^{11/4096}} \approx 0.9983543 + 0.006126 i$$

From:

ANOMALY CANCELLATIONS IN SUPERSYMMETRIC D = 10 GAUGE THEORY AND SUPERSTRING THEORY

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Received 10 September 1984

Now:

$$\begin{aligned} & -\left[\frac{1}{32} + (n - 496)/13824\right] (\text{tr } R^2)^3 \\ & - \left[\frac{1}{8} + (n - 496)/5760\right] \text{tr } R^2 \text{tr } R^4 \\ & - [(n - 496)/7560] \text{tr } R^6. \end{aligned} \quad (20)$$

In this expression we have included the contributions of one left-handed spin 3/2 gravitino and one right-handed spin 1/2 field from the supergravity sector and n left-handed spin 1/2 fields from the matter sector, which only depends on the dimension of the gauge group.

The last term in eq. (20) corresponds to an anomaly of the form $\int \omega_{10L}^1$, which cannot be cancelled by adding local terms to the action. Therefore 496 left-handed spin 1/2 fields are needed in the matter sector in

order that it vanish. Remarkably, since the dimension of the adjoint representation of $SO(32)$ or $E_8 \times E_8$ is 496, the cancellation occurs for either of these gauge groups. The anomalies associated with the first two terms of eq. (20) can be cancelled (putting $n = 496$) by adding to the effective action for $SO(32)$ or $E_8 \times E_8$

$$S_2 = -c \int \left[\frac{1}{32} B (\text{tr } R^2)^2 + \frac{1}{8} B \text{tr } R^4 + \frac{1}{12} \omega_{3L}^0 \omega_{7L}^0 \right]. \quad (21)$$

For $n = 496$, from (20), we obtain:

$$\begin{aligned} & - \left[\frac{1}{32} + (n - 496)/13824 \right] (\text{tr } R^2)^3 \\ & - \left[\frac{1}{8} + (n - 496)/5760 \right] \text{tr } R^2 \text{tr } R^4 \\ & - \left[(n - 496)/7560 \right] \text{tr } R^6. \end{aligned}$$

$$-(1/32+0)*(\text{trace } R^2)^3 - (1/8+0)*\text{trace } R^2 \text{ trace } R^4 - 0*\text{trace } R^6$$

Input:

$$-\left(\frac{1}{32} + 0\right)(\text{Tr}[R]^2)^3 - \left(\left(\frac{1}{8} + 0\right)\text{Tr}[\text{Tr}[R^2]]\right)R^4 - 0 \text{Tr}[R]^6$$

Result:

$$-\frac{1}{8} R^4 \text{Tr}[\text{Tr}[R^2]] - \frac{1}{32} \text{Tr}[R]^6$$

Without tr, we obtain:

$$-(1/32+0)*(R^2)^3 - (1/8+0)* R^2 R^4 - 0* R^6$$

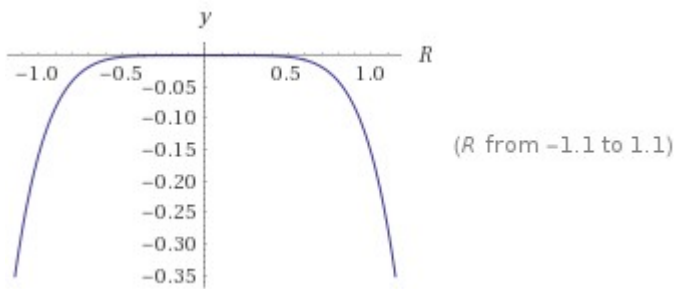
Input:

$$-\left(\frac{1}{32} + 0\right)(R^2)^3 - \left(\left(\frac{1}{8} + 0\right)R^2\right)R^4 - 0 R^6$$

Result:

$$-\frac{5 R^6}{32}$$

Plot:



Geometric figure:

line

Root:

$$R = 0$$

Polynomial discriminant:

$$\Delta = 0$$

Property as a function:

Parity

even

Derivative:

$$\frac{d}{dR} \left(-\left(\frac{1}{32} + 0\right)(R^2)^3 - \left(\left(\frac{1}{8} + 0\right)R^2\right)R^4 - 0R^6 \right) = -\frac{15R^5}{16}$$

Indefinite integral:

$$\int -\frac{5R^6}{32} dR = -\frac{5R^7}{224} + \text{constant}$$

Global maximum:

$$\max \left\{ -\left(\frac{1}{32} + 0\right)(R^2)^3 - \left(\left(\frac{1}{8} + 0\right)R^2\right)R^4 - 0R^6 \right\} = 0 \text{ at } R = 0$$

For $R = 2$, we obtain:

$$-(5 \cdot 2^6)/32$$

Input:

$$-\frac{1}{32} (5 \times 2^6)$$

Result:

$$-10$$

$$-10$$

For $R = -8$, we obtain:

Input:

$$-\frac{1}{32} (5 \times (-1) \times 8^6)$$

Result:

$$40960$$

$$40960 = 64^2 * 10 = 4096 * 10$$

$2\sqrt{((1/10 * -(5 * -8^6)/32)) - \pi} + 1/\text{golden ratio}$

Input:

$$2\sqrt{\frac{1}{10} \left(-\frac{1}{32} (5 \times (-1) \times 8^6) \right)} - \pi + \frac{1}{\phi}$$

ϕ is the golden ratio

Result:

$$\frac{1}{\phi} + 128 - \pi$$

Decimal approximation:

125.4764413351601016097419434510861352335231397804306570411...

125.476441335... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$

Property:

$128 + \frac{1}{\phi} - \pi$ is a transcendental number

Alternate forms:

$$\frac{1}{2} (255 + \sqrt{5} - 2\pi)$$

$$\frac{-128\phi + \pi\phi - 1}{\phi}$$

$$\frac{(128 - \pi)\phi + 1}{\phi}$$

Series representations:

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} - 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} + \sum_{k=0}^{\infty} \frac{4(-1)^k 1195^{-1-2k} (5^{1+2k} - 4 \times 239^{1+2k})}{1+2k}$$

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} - \sum_{k=0}^{\infty} \left(-\frac{1}{4}\right)^k \left(\frac{1}{1+2k} + \frac{2}{1+4k} + \frac{1}{3+4k}\right)$$

Integral representations:

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} - 4 \int_0^1 \sqrt{1-t^2} dt$$

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} - 2 \int_0^1 \frac{1}{\sqrt{1-t^2}} dt$$

$$2\sqrt{-\frac{5(-1)8^6}{32 \times 10}} - \pi + \frac{1}{\phi} = 128 + \frac{1}{\phi} - 2 \int_0^{\infty} \frac{1}{1+t^2} dt$$

And also, we obtain:

$$\left(\left(\left(-1/\left(\left(-\left(5 \times 2^6\right)/32\right)\right)\right)\right)\right)^{1/4096}$$

Input:

$$\sqrt[4096]{\frac{-1}{-\frac{1}{32}(5 \times 2^6)}}$$

Result:

$$\frac{1}{\sqrt[4096]{10}}$$

Decimal approximation:

0.999438003415553196029626790600195415941545113970308718879...

0.999438003... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

Alternate form:

$$\frac{10^{4095/4096}}{10}$$

All 4096th roots of 1/10:

$$\frac{e^0}{\sqrt[4096]{10}} \approx 0.99943800 \text{ (real, principal root)}$$

$$\frac{e^{(i\pi)/2048}}{\sqrt[4096]{10}} \approx 0.99943683 + 0.0015331 i$$

$$\frac{e^{(i\pi)/1024}}{\sqrt[4096]{10}} \approx 0.99943330 + 0.0030662 i$$

$$\frac{e^{(3i\pi)/2048}}{\sqrt[4096]{10}} \approx 0.99942742 + 0.0045993 i$$

$$\frac{e^{(i\pi)/512}}{\sqrt[4096]{10}} \approx 0.99941919 + 0.006132 i$$

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