

# EXTENDED EINSTEIN FIELD EQUATIONS FOR COMPLEX SPACETIME

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ABSTRACT. Goal of physics is to arrive at new theory still rooted in old theory. From Newtonian physics to Einstein and most probably to quantum gravity and then to unified field theory that is most accepted view on how physics theories should progress. But what if this assumption is not true? What if from Newton to Einstein and then to Extended Einstein? What if final step does not take into account quantum physics? This seems absurd at first but I will explore this possibility. First question that arises is that basics or fundamental physics should stay at basic level same, basic physics is classical physics and then from it Relativity emerges as result of Maxwell equations. Then a new physic is born, quantum physics that changes the view of classical physics into probability theory with no way to say what will happen exactly. This approach was most successful theory of twenty century and to this day proves itself with amazing accuracy. On the other side of physics there is another successful theory that is general relativity, that proves itself with any experiment. But both theories are incomplete, quantum physics lacks gravity, relativity breaks down at singularities that emerge from it in crucial of universe evolution moment that is the moment of big bang itself. Most physics community effort goes into trying to quantize gravity one way or another, or in general unify quantum physics with gravity and extensions of standard model. But there should be equal amount of tries to do the opposite, try to make quantum physics consistent with gravity first. By that I mean that quantum should be relativized same way theory of relativity needs to be quantized. My approach will be even another one, I will assume that only step forward is to extend relativity into more general theory without need to quantize it at all. And that its generalization will be good enough to explain quantum effects. This may seem absurd at first but as I will show it gives pretty good results and in general is a good but very complicated model of spacetime curvature. Field a physical field should be treat as field a continuous one with no gaps with empty parts of that field. Same should apply to matter field, matter should be threat as one field that is continuous in all space and that is goal of this work. Where in the end I use complex spacetime as final model that integrates quantum effects into whole picture. Final conclusion is that field theory allows for something new that follows from Einstein Field Equations.

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## 1. BASIC DEFINITIONS

**1.1. Description of the inertial system.** According to Newton's laws of motion, motion with constant velocity or lack of it gives an inertial frame of reference. This definition can be simplified even more that it is a system in which there are no forces associated with the motion of this system. Such a system does not feel the forces associated with its movement. The key question is whether an observer under the influence of a gravitational field can be treated as an inertial observer? According to the equivalence principle, the gravitational field cannot be locally distinguished from the acceleration, on the other hand, omitting the tidal forces, one can look at the inertial system as the system of any falling observer in the gravitational field. This observer locally has no weight, no force acts on him. There are two possibilities, either the observer is in uniform motion or the observer is at rest. The first possibility can be ruled out for obvious reasons only the second possibility remains, the observer in the gravitational field is motionless. This means that every observer in the gravitational field that is not subjected to any kind of apparent force related to e.g. standing on the surface of the gravitational field source or any other force is treated as an inertial system. And according to this observer's perspective, this gravitational field needs to be described. This means that any non-inertial observer cannot see the true cause of motion because there are forces in his system, so they exclude him from being an inertial system. The description of the laws of physics and thus motion must always be seen from the perspective of an inertial observer as only he perceives the true cause of motion, which also applies to the gravitational field. An inertial frame of reference is defined as one which, under the influence of a physical field, remains completely motionless from its own perspective, where this motionlessness is only locally defined. This locality makes us ignore the tidal forces that will naturally accompany the gravitational field, and thus the physical field that is the source of motion. However, the definition of the physical field itself, i.e. the gravitational field, the field that causes motion, is more delicate. It results from the definition of the inertial system itself, physical fields are a field from the perspective of which no inertial observer can be described as an inertial observer, so he must be in motion relative to this field. This means that the field itself cannot give us the whole picture of how motion physically occurs. Only the perspective of a field that is the source of motion and an inertial observer that is able to detect true non-relative motion as a combination gives us a description of physical reality. Any motion that is relative depends on the system in which it is measured, the physical field or simply the gravitational field cannot be dependent on the system in which it is measured, it must be a source of motion for every inertial observer.

**1.2. Observer Definition.** Observer definition. The observer is understood as a frame of reference capable of measuring time (clock) and distance (ruler). The units of measurement must always be chosen to express distance in time or space. This means that if I measure distance in meters and seconds I have to express both units in meters or seconds, which is achieved by multiplying time by the speed of light (meters) or dividing distance by the speed of light (seconds). This is a fairly basic assumption in the Theory of Relativity. What is crucial for extending the field equations is the exact physical definition of the phenomenon for a given observer. A physical phenomenon is simply such a phenomenon that meets the previous assumption, the observer is completely at rest relative to the event, which means that it is defined as an inertial frame of reference. The previous definition, of course, only makes sense in the case of flat space-time, so it is not a general case. To go to the general case, it is necessary to define an observer in a gravitational field as still an observer motionless relative to an event in which a gravitational field is present. Before discussing free fall from the perspective of an inertial observer, one key point needs to be addressed. Space-time in the mathematical description must adhere to the principle according to which the observer remains inertial to the event, this means that locally, as in the Theory of Relativity, the observer locally measures flat spacetime, which is not true globally. The whole point of this paper is to show that there are other field equations that reproduce this principle but with an additional condition. This condition is that the gravitational field is fully dependent on the existence of a field of matter and/or energy at every point in space-time. In the absence of matter at any point in space-time, these equations become equations for flat space-time, which means that literally the source of deviations from flat space-time must be the presence of matter at the point where this space-time deviates from it, otherwise we get flat Minkowski space. There is an additional principle that is central to this whole model and its assumptions, the equivalence of gravity and the field of matter. Which I will discuss in more detail later in the section on the non-zero momentum energy tensor requirement.

**1.3. Light Clock.** In the Theory of Relativity, time is measured using a theoretical light clock that measures the time between successive reflections of a light ray. Such a hypothetical clock has quite important implications for how distance and the passage of time are defined. Since the speed of light is constant in a vacuum for any observer, it is a contentious but important question as to what the speed of light really remains constant. Let's consider three possible scenarios:

1. Relative to some field - a medium once called ether.
2. Relative to an inertial observer.
3. It's just a constant relative to nothing.

Thanks to the light clock, you can answer the question. If there is a field with respect to which light always has a constant speed - that field is an event, the inertial observer perceives that for each event the speed of light is constant, so this does not contradict the second point of this assumption. This also explains why the speed of light is the speed of causality in a simple way, events propagate at the speed of light and any observer who is not moving at the speed of light and therefore not an event stays still relative to the event which makes the speed of light remain constant and the information moves exactly at the speed of light (only in the sense of a physical event). Now a thought experiment using a light clock that can rule out the third option is as follows, I have two observers A and B both of whom use a light clock to measure time, but you don't know which is moving and which is not. These observers at some point in time  $t$  meet and compare their clocks, always the clock of the moving observer will have fewer ticks. It is impossible to define whether the observer A was in motion or the observer B was in motion, because without the top-down assumption that this particular observer is in motion and the other one, it is not possible to perform an experiment using light signals that will distinguish which one is truly in motion. However, what makes it possible to distinguish which is in motion is the indication of the first clock relative to the second, if the observer A was in motion, his light clock has a smaller clock indication. This means that both the clock and the observer A were physically in motion relative to an event that lasted a certain amount of time. The difference is that the light in the clock seems to tick normally for observer A and slower for observer B, but observer B will say the same about observer A. This means that since A's clock is in true motion, observer B is right and observer A's perspective is wrong. A's clock is ticking slower objectively because fewer events occur physically for this observer - and since the speed of light is constant relative to events as their number decreases relative to observer B for whom more events occur, it will find that fewer events occur for observer A which is a physical fact. So this paradox clearly shows that the speed of light is constant only and exclusively with respect to the event.

## 2. EXPANDING EINSTEIN

**2.1. EFE- Einstein field equations.** Einstein field equations are basics theory of gravitation. They relate spacetime curvature with matter-energy content of universe. But problem with field equations is that they break at edge of a black hole, where all geodesic end. This geodesic incompleteness is a crucial problem that breaks down whole model in ultimate sense. Model works perfect till there is a singularity of a black hole or begin of universe. Another problem with that theory that is not a real problem but seems there could be something wrong is dark matter, as long as dark energy can be thought just as cosmological constant, problem with dark matter is that i could be new type of particle or something is missing in gravity theory.

EFE can be written as ten equations where key is Einstein tensor [1][2][3][4] that is derived from Banachi identity. This makes conservation of energy possible and energy momentum tensor zero covariant derivative, equation can be written:

$$G_{ab} = \kappa T_{ab} \quad (2.1)$$

$$R_{ab} - \frac{1}{2}Rg_{ab} = \kappa T_{ab} \quad (2.2)$$

Where both parts of equation give zero covariant derivative that can be written, whee I will use covariant derivative with index up so it's multiply by metric tensor:

$$g^{bk}\nabla_k = \nabla^b \quad (2.3)$$

$$\nabla^b G_{ab} = \nabla^b \kappa T_{ab} = 0 \quad (2.4)$$

$$\nabla^b \left( R_{ab} - \frac{1}{2}Rg_{ab} \right) = \kappa \nabla^b T_{ab} = 0 \quad (2.5)$$

Vacuum solutions are arrived at when energy momentum tensor [5] is equal to zero so when there is no matter present that is equal for vanishing of Einstein tensor to be equal to zero  $G_{ab} = 0$ . But it does not mean that spacetime is flat when Einstein tensor vanishes. So it means that matter field is not a continuous field and this will be key hint for extending that equation.

Where i did use normal letters for spacetime indexes, not Greek ones as it is written most of the time. But still convention I will be using here is that Latin letters have indexes ranging from zero to three. So they both represent space and time coordinates.

**2.2. EEFE- Extended Einstein field equations.** Now why does matter field should not vanish in any point? It seems absurd but its only way to arrive at extension of Einstein field equations. And it has one big advantage it can explain in principle dark matter. Matter will extend as a field in whole space, that could explain why there is missing matter in the universe, it's stored in field itself.

But where to start? That is key question, let first write EFE but expand all elements to curvature tensor:

$$R_{bcd}^c - \frac{1}{2}R_{ncm}^c g^{nm} g_{bd} = \kappa T_{bd} \quad (2.6)$$

Where I did use  $bd$  index as base one. Now we can see a reaping pattern here, there is curvature tensor then it's contractions. Only thing that does not follow this rule is energy momentum tensor that does not have any contractions. What if this symmetry of contraction is preserve so let me rewrite this equation:

$$R_{bcd}^c - \frac{1}{2}R_{ncm}^c g^{nm} g_{bd} = \kappa T_{bcd}^c \quad (2.7)$$

Now there is a clear pattern, in truth we are acting on four rank tensors in whole equation. On one side of equation there is curvature tensor and it's contractions that are a bit complex on left side there is some unknown tensor that reduces to energy momentum tensor by contraction. So EFE are not a final word as it can be seen we can calculate curvature tensor directly by using one metric tensor that will contraction cancel one contraction, and this will lead to:

$$g^{kc} R_{bcd}^c - \frac{1}{2}g^{kc} R_{ncm}^c g^{nm} g_{bd} = \kappa g^{kc} T_{bcd}^c \quad (2.8)$$

$$R_{bkd}^c - \frac{1}{2}R_{nkm}^c g^{nm} g_{bd} = \kappa T_{bkd}^c \quad (2.9)$$

$$R_{bkd}^c - \frac{1}{2}R_k^c g_{bd} = \kappa T_{bkd}^c \quad (2.10)$$

$$g_{pc} R_{bkd}^c - \frac{1}{2}g_{pc} R_k^c g_{bd} = g_{pc} \kappa T_{bkd}^c \quad (2.11)$$

$$R_{pbkd} - \frac{1}{2}R_{pk} g_{bd} = \kappa T_{pbkd} \quad (2.12)$$

EEFE can be written in two forms as seen here mixed and fully covariant, I will use fully covariant one for all calculations presented here but they are both equal from fact it's a tensor equation.

## 3. PROPERTIES OF EEFE

**3.1. Conservation.** I can easily prove that indeed this new tensor has covariant derivative equal to zero on both sides of equation [6], it's pretty simple task from fact how this tensor is derived. I will write EFE and I know that its covariant derivative is zero so I can just multiply both sides of equation by same metric tensor that will give me, where I use fact that covariant derivative of metric tensor is equal to zero so I treat it as a constant:

$$\nabla^d \left( R_{bcd}^c - \frac{1}{2} R_{ncm}^c g^{nm} g_{bd} \right) = \kappa \nabla^d T_{bcd}^c = 0 \quad (3.1)$$

$$\nabla^d g^{kc} \left( R_{bcd}^c - \frac{1}{2} R_{ncm}^c g^{nm} g_{bd} \right) = \kappa \nabla^d g^{kc} T_{bcd}^c = 0 \quad (3.2)$$

$$\nabla^d \left( R_{bkd}^c - \frac{1}{2} R_{nkm}^c g^{nm} g_{bd} \right) = \kappa \nabla^d T_{bkd}^c = 0 \quad (3.3)$$

Now contraction of those equations will naturally lead to EFE that is obvious fact from previous equations, but will write it:

$$g^{kp} R_{pbkd} - \frac{1}{2} g^{kp} R_{pk} g_{bd} = \kappa g^{kp} T_{pbkd} \quad (3.4)$$

$$R_{bd} - \frac{1}{2} R g_{bd} = \kappa T_{bd} \quad (3.5)$$



**3.2. Non vanishing energy momentum tensor and dimensions.** This new extended Einstein tensor has one key property, when matter field vanishes it gives a flat spacetime. I can prove it by writing that tensor and setting it zero:

$$R_{pbkd} - \frac{1}{2}R_{pk}g_{bd} = 0 \quad (3.6)$$

Now set indexes so Riemann tensor vanishes:

$$R_{pkkk} - \frac{1}{2}R_{pk}g_{kk} = 0 \quad (3.7)$$

$$-\frac{1}{2}R_{pk}g_{kk} = 0 \quad (3.8)$$

$$R_{pk} = 0 \quad (3.9)$$

Now plug it into equation gives that Riemann tensor is always zero:

$$R_{pbkd} = 0 \quad (3.10)$$

It means that energy momentum extended tensor has to not vanish at every point of space to not give flat spacetime. Finally last property is that there is only equal amount of unknowns in four dimensional spacetime. This can be easy seen from fact that Ricci tensor with metric tensor has total twenty components that are independent. And Riemann tensor gives twenty independent components in four dimensional spacetime. And to prove it's only case I can take number of independent Riemann components and set it equal to two times second order symmetric tensor components that gives:

$$\frac{n^2(n^2 - 1)}{12} = n(n + 1) \quad (3.11)$$

$$\frac{n^4 - n^2}{12} = n^2 + n \quad (3.12)$$

$$\frac{n^3 - n}{12} = 1 + n \quad (3.13)$$

$$\frac{n^3 - n}{12} - n - 1 = 0 \quad (3.14)$$

Solution to this equation [7] is 4, -1, -3 so from fact that number of dimensions is always a positive number there is only four left.

**3.3. Quantum like effects and rest mass.** Real question is can this model explain quantum effects? First I do write two possible way of writing spacetime interval that means distance in complex spacetime, then I will combine then into one single real interval:

$$ds^2 = g_{ab}dz^a dz^b \quad (3.15)$$

$$d\bar{s}^2 = \bar{g}_{ab}d\bar{z}^a d\bar{z}^b \quad (3.16)$$

$$d\bar{s}ds = \sqrt{d\bar{s}^2 ds^2} = \sqrt{g_{ab}\bar{g}_{ab}dz^a dz^b d\bar{z}^a d\bar{z}^b} = ds^2 \quad (3.17)$$

Now what is left is to define metric tensor and in general a complex field:

$$g_{ab} = \frac{\partial\chi^i}{\partial z^a} \frac{\partial\chi^j}{\partial z^b} \eta_{ij} \quad (3.18)$$

$$\bar{g}_{ab} = \frac{\partial\bar{\chi}^i}{\partial \bar{z}^a} \frac{\partial\bar{\chi}^j}{\partial \bar{z}^b} \eta_{ij} \quad (3.19)$$

$$\chi^k = a^k(\mathbf{x}) e_k + ib^k(\mathbf{x}) \epsilon_k \quad (3.20)$$

$$\bar{\chi}^k = a^k(\mathbf{x}) e_k - ib^k(\mathbf{x}) \epsilon_k \quad (3.21)$$

$$\chi^k (\chi^k)^\dagger = \chi^k \bar{\chi}_k = a^k(\mathbf{x}) a_k(\mathbf{x}) + b^k(\mathbf{x}) b_k(\mathbf{x}) \quad (3.22)$$

Now when i have all fields defined I can move to most used field that is scalar field. Let me state that there is a scalar field that integral is equal to some real number  $N$  that will be normalization constant of that field. I will write that scalar field just as  $\psi$ , all information about it can be written:

$$\int_{\mathbf{M}^4} \sqrt{\sqrt{\det(g_{ab}\bar{g}_{ab})}} \psi d^4\mathbf{x} = N \quad (3.23)$$

$$\frac{1}{N} \int_{\mathbf{M}^4} \sqrt{\sqrt{\det(g_{ab}\bar{g}_{ab})}} \psi d^4\mathbf{x} = 1 \quad (3.24)$$

$$\frac{1}{N} \int_{x^a(\mathbf{x}) \in \mathbf{M}^4} \sqrt{\sqrt{\det(g_{ab}\bar{g}_{ab})}} \psi d^4\mathbf{x} = \varphi(x^a(\mathbf{x})) \quad (3.25)$$

To construct field equation I need only set Riemann tensor to a complex tensor instead of real one that is just done by changing metric tensors. I will define probability function with field equation:

$$R_{abcd}^\dagger = \bar{R}^{abcd} \quad (3.26)$$

$$R_{abcd}^\dagger R_{abcd} = \psi \quad (3.27)$$

$$R_{abcd}^\dagger R_{abcd} = R_{abcd}^\dagger \left( \kappa T_{abcd} + \frac{1}{2} R_{ac} g_{bd} \right) \quad (3.28)$$

$$\psi = R_{abcd}^\dagger \left( \kappa T_{abcd} + \frac{1}{2} R_{ac} g_{bd} \right) \quad (3.29)$$

$$\frac{1}{N} \int_{x^a(\mathbf{x}) \in \mathbf{M}^4} \sqrt{\sqrt{\det(g_{ab}\bar{g}_{ab})}} R_{abcd}^\dagger \left( \kappa T_{abcd} + \frac{1}{2} R_{ac} g_{bd} \right) d^4\mathbf{x} = \varphi(x^a(\mathbf{x})) \quad (3.30)$$

## 4. PREDICTIONS

4.1. **Dark Matter.** Dark matter is in this EEFE not a new type of particle but field of matter itself that extends in space. I will do simplest possible approximation of value of this field by using simple integral. First i start off by writing density with function of mass  $M(R)$ . Then will assume that in units of radius that gives surface of matter  $r_0$  i will get rest mass contained in that radius. And finally write density dived by rest mass that will be close to one over radius to third. From it its straight forward to calculate integral that gives total mass change from surface to infinity [8]:

$$\rho = \frac{M(R)}{\frac{4}{3}\pi R^3} \quad (4.1)$$

$$\int_0^{r_0} \frac{M(R)}{\frac{4}{3}\pi} dr = M_0 \quad (4.2)$$

$$\frac{\rho}{\int_0^{r_0} M(R) dr} \approx \frac{1}{R^3} \quad (4.3)$$

$$\int_1^\infty \int_0^\pi \int_0^{2\pi} \frac{1}{R^3} dr d\theta d\varphi = \pi^2 \quad (4.4)$$

This is simplest calculation for dark matter that is just extend matter field. I assumed spherical coordinate system. In more general case, mass density function decreases proportional to radius cubed. From it I can calculate how much there is dark matter compared to normal matter:

$$\frac{\pi^2 - 1}{\pi^2} \approx 90\% \quad (4.5)$$

This whole dark matter calculation is a approximation but a good enough one.

**4.2. Universe expansion.** Good test of this theory is predicting the cosmological constant. From previous subsection approximation of amount of dark matter is equal to  $\pi^2$  now I will use perfect fluid model but with pressure calculation that will be equal to one third escape velocity of universe squared dived by speed of light squared. I can write energy momentum tensor for perfect fluid as:

$$T_{00} = \rho_0 \pi^2 \quad (4.6)$$

$$T_{aa} = \frac{1}{3} \frac{2GM_0}{c^2 r} \rho_0 \pi^2 \quad (4.7)$$

Now lets go back to field equation, I will assume only diagonal elements of both metric tensor and Ricci tensor and energy momentum extended tensor, so field equation in this case turns into:

$$R_{pbpb} - \frac{1}{2} R_{pp} g_{bb} = \kappa T_{pbpb} \quad (4.8)$$

Now I want to calculate zero-zero component of Ricci tensor that will be equal to:

$$R_{0b0b} - \frac{1}{2} R_{00} g_{bb} = \kappa T_{pbpb} \quad (4.9)$$

$$g^{bb} R_{0b0b} - 2R_{00} = \kappa g^{bb} T_{0b0b} \quad (4.10)$$

$$R_{00} = -\kappa T_{00} \quad (4.11)$$

Rest of components I can calculate in same way so I will finally get [9]:

$$g^{bb} R_{pbpb} - \frac{1}{2} g^{bb} R_{pp} g_{bb} = \kappa g^{bb} T_{pbpb} \quad (4.12)$$

$$R_{pp} = -\kappa T_{pp} \quad (4.13)$$

Now I can divide Ricci tensor by Einstein constant to arrive at energy momentum part and i will sum elements of space part of energy momentum tensor [9]:

$$\frac{1}{\kappa} g^{ii} R_{ii} = -g^{ii} T_{ii} \quad (4.14)$$

$$\frac{1}{\kappa} R = - \left( \frac{2GM_0}{c^2 r} \right) \rho_0 \pi^2 \quad (4.15)$$

$$\frac{1}{\kappa} R = -2.1008 \cdot 10^{-27} [kg/m^3] \quad (4.16)$$

Now from previous equations I can calculate Ricci scalar as equal to:

$$R = -\kappa T \quad (4.17)$$

Now plug in all the numbers and i finally get [10] :

$$R = -\kappa \rho_0 \pi^2 \left( 1 + \frac{2GM_0}{c^2 r} \right) \quad (4.18)$$

$$R = -1.166 \cdot 10^{-52} [m^{-2}] \quad (4.19)$$

**4.3. Black holes.** Black holes are the ultimate test of gravity. Simplest case of black holes are static non rotating ones. I will start by solving field equation in simplest case, that is only diagonal elements of Ricci tensor and Energy momentum tensor for perfect fluid. I will write all calculations in one line then will discuss them:

$$R_{aa} = -2\kappa T_{aa} \quad (4.20)$$

$$g^{aa} R_{aa} = -2\kappa g^{aa} T_{aa} \quad (4.21)$$

$$R = -2\kappa T \quad (4.22)$$

$$R = -2\kappa\rho_0\pi^2 \left(1 + \frac{2GM}{rc^2}\right) \quad (4.23)$$

$$\lim_{r \rightarrow 0^\pm} -2\kappa\rho_0\pi^2 \left(1 + \frac{2GM}{rc^2}\right) = \pm\infty \quad (4.24)$$

$$R(0^+) = +\infty \quad (4.25)$$

$$R(0^-) = -\infty \quad (4.26)$$

$$R(0^+) + R(0^-) = 0 \quad (4.27)$$

From equation follows that there is no singularity at  $r = 0$  as one side there is plus infinity on another side there is minus infinity so they cancel out. It means that black holes connect two possible universes in one point of spacetime from each universe perspective all spacetime stays in one universe till singularity point where those two connect. It shows clear that EEFE are singularity free. Compared to EFE that generated a point that can't be removed and where all geodesic end. Here central point is where all geodesic connect. It means that this point represents a flow of all information from two connected universes. And non moving observer can stay in that point for any amount of proper time measured by its clock. From point of view of any other observer that is not at that point, that observer is both in all possible future and in all possible past. If observer inside does move it will go to any possible location in time, where that location itself is random and cant be determined as all spacetime paths are solutions. This can be written as:

$$R(\mathbf{x}^+) + R(\mathbf{x}^-) = 0 \quad (4.28)$$

It means that black holes act as a bridge between two spacetimes. That bridge has only one point where it can be seen. But when getting out of that point all points of spacetime act as solution afterwards observer is split to one universe that means that it can have positive or negative value in frame of reference of singularity but in its frame it's just:

$$R(\mathbf{x}) + R(\mathbf{x}) = 2R(\mathbf{x}) \quad (4.29)$$

It means that I can re-write field equation :

$$2R = -2\kappa T \quad (4.30)$$

$$R = -\kappa T \quad (4.31)$$

4.4. **Quantum black holes for empty spacetime.** I can solve equation for flat complex spacetime that will give a black hole in quantum point of view. I will start with empty complex spacetime:

$$ds^2 = \sqrt{\eta_{ab}\eta_{ab}dz^a dz^b d\bar{z}^a d\bar{z}^b} = \sqrt{dz_b dz_b d\bar{z}^b d\bar{z}^b} \quad (4.32)$$

$$= dx^b(\mathbf{x}) dx_b(\mathbf{x}) + d\chi^b(\mathbf{x}) d\chi_b(\mathbf{x}) = \eta_{ab} dx^a(\mathbf{x}) dx^b(\mathbf{x}) + \eta_{ab} d\chi^a(\mathbf{x}) d\chi^b(\mathbf{x}) \quad (4.33)$$

$$= dx^0(\mathbf{x}) dx^0(\mathbf{x}) - \sum_{i=1}^3 dx^i(\mathbf{x}) dx^i(\mathbf{x}) + d\chi^0(\mathbf{x}) d\chi^0(\mathbf{x}) - \sum_{i=1}^3 d\chi^i(\mathbf{x}) d\chi^i(\mathbf{x}) \quad (4.34)$$

$$= dx^0(\mathbf{x}) dx^0(\mathbf{x}) + d\chi^0(\mathbf{x}) d\chi^0(\mathbf{x}) - \left( \sum_{i=1}^3 dx^i(\mathbf{x}) dx^i(\mathbf{x}) + d\chi^i(\mathbf{x}) d\chi^i(\mathbf{x}) \right) \quad (4.35)$$

Now i got a eight dimensional flat spacetime. I will represent it as complex four dimensional spacetime. I will use Euler identity so I can write it as:

$$ds^2 = \eta_{ab} dz^a dz^b = \pm C_1 i \eta_{ab}^{\mp} dk^a dk^b \exp(C_1 i \eta_{ab}^{\mp} dk^a dk^b) \quad (4.36)$$

$$ds^2 = \pm i C_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \exp \left( i C_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \right) \quad (4.37)$$

$$d\bar{s}^2 = \pm i C_1 \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \exp \left( -i C_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \right) \quad (4.38)$$

$$ds^2 = \pm 4i\pi^2 \sum_n \left( \frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} - \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right) \exp \left( 4i\pi^2 \left( \frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} - \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right) \right) \quad (4.39)$$

$$d\bar{s}^2 = \pm 4i\pi^2 \sum_n \left( -\frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} + \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right) \exp \left( 4i\pi^2 \left( -\frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} + \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right) \right) \quad (4.40)$$

$$ds^2 = ds d\bar{s} = \sqrt{-16\pi^4 \sum_n \left( -\frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} + \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right) \left( \frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} - \frac{4m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \right)} \quad (4.41)$$

$$ds^2 = 4\pi^2 \sum_n \sqrt{\left( \frac{\hbar^4 \omega_n^4 c^4 dt^4}{E_P^4} - 8 \frac{m_n^2 l_P^2 dr^2}{r_0^2 m_P^2} \frac{\hbar^2 \omega_n^2 c^2 dt^2}{E_P^2} + \frac{16m_n^4 l_P^4 dr^4}{r_0^4 m_P^4} \right)} \quad (4.42)$$

Where  $r_0$  is surface of object that is calculated than can't be less than one Planck length.

**4.5. Elementary Particles.** From symmetry of field I can deduce elementary particles model that follows from this theory. I will start by symmetry this theory uses, this symmetry will be  $SU(1, 3)$  that gives quark symmetry plus Lorentz transformation I can write for flat spacetime condition that when I transform from one frame of reference to another:

$$ds^2 = ds'^2 \quad (4.43)$$

$$\eta_{ab}dz^a dz^b = \eta_{ab}dz'^a dz'^b \quad (4.44)$$

But is it quark symmetry or a graviton symmetry? I will use formula that i used for quantum black holes that will show that in truth it's symmetry of complex field of spin two:

$$ds^2 = \sqrt{\eta_{ab}\eta_{ab}dz^a dz^b d\bar{z}^a d\bar{z}^b} = \sqrt{dz_b dz_b d\bar{z}^b d\bar{z}^b} \quad (4.45)$$

$$ds^2 = \pm iC_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \exp \left( iC_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \right) \quad (4.46)$$

$$d\bar{s}^2 = \pm iC_1 \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \exp \left( -iC_1 \left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \right) \quad (4.47)$$

$$dsd\bar{s} = -C_1 \sqrt{\left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right)} \quad (4.48)$$

Now how to prove it's spin two complex field? I can write field as solution to field equation where  $\psi = 0$ , field will have four possible states that will give spin two:

$$\psi_{\pm\pm, \pm\mp} = \int \pm iC_1 \left( \pm dk^0 dk^0 \mp \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \exp \left( iC_1 \left( \pm dk^0 dk^0 \mp \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \right) d^4\mathbf{x} \quad (4.49)$$

It means that it has four possible states, but in contradiction to quantum physics they all represent same energy level, one solution is massive field and massive tachyon field plus antimatter parts. It means that clear in this model graviton has mass. That may seem as contradiction to LIGO experiment but is not. Pure graviton field is massless so that:

$$\pm dk^0 dk^0 \mp \left( \sum_{j=1}^3 dk^j dk^j \right) = 0 \quad (4.50)$$

Otherwise its dark matter field created by massive particles.

## 5. PHYSICAL PRINCIPLES

**5.1. Meaning of field equations.** EEFE are pretty complex equations. They leave one object undefined properly. That is extended energy momentum tensor. First property of it is it's contraction leads to normal energy momentum tensor:

$$g^{ac}T_{abcd} = T_{bd} \quad (5.1)$$

Another property is conservation of energy:

$$\nabla^b g^{ac}T_{abcd} = \nabla^d g^{ac}T_{abcd} = \nabla^b T_{bd} = \nabla^d T_{bd} = 0 \quad (5.2)$$

Now I have properties of energy momentum tensor that will have to have twenty independent components I can move to field equation itself. Field equation says that physical field thus gravity field is always measured from free-falling observer point of view. It means that if I do not reverse time flow gravity is always an expansive force. From that fact it comes counter intuitive idea about gravity field- gravity is equal motion itself. This is physical meaning behind this equation, on left side of equation there is motion of spacetime and on right side of equation there is energy field or just matter field.



**5.2. Motion and spacetime expansion.** Negative Ricci tensor for positive matter field may seem like contradiction. But logic goes like this, when spacetime around earth expands volume of earth increases but earth moves with exactly rate of expansion of spacetime so those two effects cancel out and I am left with just static earth that causes object to fall onto it. In subsection about black holes i mention two universes that connect each other one universe is expanding another one is collapsing. It means that they are opposites of each other. From it follows that in one time goes forward in another it goes backwards compared to first one. It could be explanation for missing antimatter. At moment of big bang universe splits into two, one expands one collapses, I will make it formal:

$$R = -2\kappa\rho_0\pi^2 \left( 1 + \frac{2GM}{rc^2} \right) \quad (5.3)$$

$$R(0^\pm) = -2\kappa\rho_0\pi^2 \left( \pm 1 + \frac{2GM}{\pm 0c^2} \right) \quad (5.4)$$

$$R(\mathbf{x}^\pm) = -2\kappa\rho_0\pi^2 \left( \pm 1 + \frac{2GM}{\pm rc^2} \right) \quad (5.5)$$

Those equation seem time independent but they are not. Now i will split this equations into two and split time and space coordinate:

$$R(r, ct) = -2\kappa\rho_0\pi^2 \left( 1 + \frac{2GM}{+rc^2} \right) \quad (5.6)$$

$$R(-r, -ct) = -2\kappa\rho_0\pi^2 \left( -1 + \frac{2GM}{-rc^2} \right) \quad (5.7)$$

It's now obvious that if I add those two functions I will get zero:

$$R(r, ct) + R(-r, -ct) = 0 \quad (5.8)$$

$$R(r, ct) = -R(-r, -ct) \quad (5.9)$$

But observer that is not in singularity so point of  $r = 0$  will observe it another way, it will see that time goes forward in both universes so it will lead to equation:

$$R(r, ct) - R(-r, -ct) = 2R(r, ct) \quad (5.10)$$

$$2R(r, ct) = -2\kappa\rho_0\pi^2 \left( 1 + \frac{2GM}{+rc^2} \right) \quad (5.11)$$

$$R(r, ct) = -\kappa\rho_0\pi^2 \left( 1 + \frac{2GM}{+rc^2} \right) \quad (5.12)$$

$$R = -\kappa T \quad (5.13)$$

And that result is consistent with previous subsections.

**5.3. Free fall as case for field equation.** Free fall is base and simplest gravity phenomenon. In this model it has very simple interpretation that can be reduced to one equation:

$$R_{aa} = -2\kappa T_{aa} \quad (5.14)$$

Where as i did show in chapter about black holes, those two can be reduced by chose of a reference frame that is not singularity rooted. This mean that proper equation is just:

$$R_{aa} = -\kappa T_{aa} \quad (5.15)$$

It is seen from observer that is falling, its past and future will have to be same in time but opposite in space direction, for example falling observer towards some surface will see both expansion of past light cone and future light cone, so that two will just mean for each part of light cone. From fact that Ricci tensor has negative sign, spacetime past and future will both expand. For antiuniverse observer it will be same but with opposite way of time flowing, so it will make spacetime contract so it will get further away from gravity field. It means that from our perspective antimatter falls in gravity field just like normal matter, but from its perspective it falls in opposite direction of time and space, that create a mirror universe. When they collide they form a singularity that turns matter into energy, it's same singularity that formed a big bang. Still one particle has to move forward in time one backwards. If for example from two particles , where one is antiparticle of first one I do form a photon field one photon moves forward in time one backwards but its impossible to see any change between those two as photon moving backwards in time will have same properties from our perspective only change is that it spins in opposite direction. That means that I need to define energy in invariant way that will be just energy momentum tensor trace. It's best candidate as it's a scalar and its responsible for expanding or contracting spacetime. So conservation of energy for energy momentum tensor was told before, but i want to look at it more precise using quantum properties:

$$\psi_{\pm\pm,\pm\mp} = \pm C_1 i \eta_{ab}^{\mp} dk^a dk^b \exp(C_1 i \eta_{ab}^{\mp} dk^a dk^b) \quad (5.16)$$

$$\int_{\mathbf{x}}^{\mathbf{x}+d\mathbf{x}} \eta_{ab}^{\mp} dk^a dk^b d^4\mathbf{x} = m^2 \quad (5.17)$$

So conservation law is just rest mass doses not change over time so:

$$\frac{1}{c} \partial_0 \sqrt{\int_{\mathbf{x}}^{\mathbf{x}+d\mathbf{x}} \eta_{ab}^{\mp} dk^a dk^b d^4\mathbf{x}} = 0 \quad (5.18)$$

And that example shows how rest mass is defined in quantum spacetime. But in truth i need to add motion in space to get full conservation law so I will get four gradient of that integral  $\partial_k = (\frac{1}{c}\partial_0, \partial_1, \partial_2, \partial_3)$ :

$$\partial_k \sqrt{\int_{\mathbf{x}}^{\mathbf{x}+d\mathbf{x}} \eta_{ab}^{\mp} dk^a dk^b d^4\mathbf{x}} = 0 \quad (5.19)$$

5.4. **Four types of particles in field theory.** From previous subsection I can extract four types of particles that are key to gravity effects. Those types of particles are particles with mass, antiparticles with mass, mass-less particles and tachyon parts of those. So there are massive tachyon , anti-tachyon massive and finally mass-less tachyon. I can write spacetime relation for them:

$$\int_{\mathbf{x}}^{\mathbf{x}+d\mathbf{x}} \eta_{ab}^{\mp} dk^a dk^b d^4\mathbf{x} = \pm m^2 \quad (5.20)$$

$$\int_{\mathbf{x}}^{\mathbf{x}+d\mathbf{x}} \eta_{ab}^{\mp} dk^a dk^b d^4\mathbf{x} = \pm 0 \quad (5.21)$$

Where Minkowski tensor can be written for normal field that will be mostly minus notation and for tachyon field it will be mostly plus notation- but it has direct interpretation first one represents normal particles and second one antiparticles that will be just tachyon particles. It means that there can't be chosen mostly plus notation for normal not tachyon fields. Mass-less particles can be both normal and tachyon ones. In practical point of view tachyon time axis is rotated by more than  $\frac{\pi}{4}$  radians compared to normal time axis of non tachyon particles. So antimatter in this model is literally tachyon particle. And even mass-less particles have tachyon part. Still even in curved spacetime equality holds. Proper time for a clock of antimatter is always negative it means that time flows backwards, for matter particles it flows forward:

$$\int \sqrt{\frac{dsd\bar{s}}{c^2}} = \pm \int \sqrt{-\frac{C_1}{c^2} \sqrt{\left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right)}} \quad (5.22)$$

So it can be split into two parts, positive clock with matter and negative with antimatter that is equal to tachyon part:

$$\int \sqrt{\frac{dsd\bar{s}}{c^2}} = + \int \sqrt{-\frac{C_1}{c^2} \sqrt{\left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right)}} \quad (5.23)$$

$$\int \sqrt{\frac{dsd\bar{s}}{c^2}} = - \int \sqrt{-\frac{C_1}{c^2} \sqrt{\left( dk^0 dk^0 - \left( \sum_{j=1}^3 dk^j dk^j \right) \right) \left( -dk^0 dk^0 + \left( \sum_{j=1}^3 dk^j dk^j \right) \right)}} \quad (5.24)$$

Field of possible metric is always solution to field equation so it can't be any metric. General solution can be written as:

$$dsd\bar{s} = \sqrt{g_{ab}^{\mp} \bar{g}_{ab}^{\mp} dz^a dz^b d\bar{z}^a d\bar{z}^b} \quad (5.25)$$

$$\int \sqrt{\frac{1}{c^2} dsd\bar{s}} = \pm \sqrt{\frac{1}{c^2} \sqrt{g_{ab}^{\mp} \bar{g}_{ab}^{\mp} dz^a dz^b d\bar{z}^a d\bar{z}^b}} \quad (5.26)$$

## 6. SUMMARY

In this paper is showed clear that EFE are not final world in gravitation theory. Set of new equations emerges from EFE that leads to EEFE. Simple calculations did lead to consistent result , it means that model has a big potential in becoming next theory of gravity and replacing Theory Of Relativity. Model is singularity free but i did not show for specific metric tensor as solutions I did show work for any possible simplest case black hole.

Model itself is very complex and could be easy miss-leading when dealing with physical field itself. Another problem with complexity of that model is how hard it is to solve field equation directly. Still predictions about early universe, black holes and quantum effects are a solid proof this model is a good agreement with observation.

One thing that was left is general way to get a real field from scalar field, and method is pretty simple for scalar field or turning tensor field into scalar field by using  $\dagger$  operator. But another way of doing it is just multiply field by it's complex conjugate formally its Hadamard product of two tensor fields that gives another tensor field:

$$Z_{ab\dots n}\bar{Z}_{ab\dots n} = \sqrt{X_{ab\dots n} \odot X_{ab\dots n} + Y_{ab\dots n} \odot Y_{ab\dots n}} \quad (6.1)$$

Where  $Z$  is complex tensor field and  $X$  is real part of that field  $Y$  is imaginary part but without a imaginary unit. This definition of product is very important for whole idea to work when taking into account complex fields. Geodesic equation takes form of:

$$\delta \int \sqrt{dsd\bar{s}} = 0 \quad (6.2)$$

This definition of geodesic works both for complex spacetime and real spacetime where for for real it gives just real spacetime integral:

$$\delta \int ds = 0 \quad (6.3)$$

It's good to remember that complex spacetime turns into real spacetime but it has twice the dimensions so it truth eight dimensions. It means that final product has two bases not one tensor basis and the are not equal:

$$Z_{ab\dots n}\bar{Z}_{ab\dots n} = \sqrt{X_{ab\dots n}e^{ab\dots n} \odot X_{ab\dots n}e^{ab\dots n} + Y_{ab\dots n}\epsilon^{ab\dots n} \odot Y_{ab\dots n}\epsilon^{ab\dots n}} \quad (6.4)$$

$$Z_{ab\dots n}\bar{Z}_{ab\dots n} = \sqrt{X_{ab\dots n} \odot X_{ab\dots n}e^{ab\dots n} \odot e^{ab\dots n} + Y_{ab\dots n} \odot Y_{ab\dots n}\epsilon^{ab\dots n} \odot \epsilon^{ab\dots n}} \quad (6.5)$$

