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Leakage Squeezing Countermeasure
Against High-Order Attacks

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Abstract. In the recent years, side channel attacks have been widely investigated. In particular, second order attacks (2O-attacks) have been improved and successfully applied to break many masked implementations. In this context we propose a new concept to hinder attacks of all order: instead of injecting more entropy, we make the most of a single-mask entropy. With specially crafted bijections instantiated on the mask path, we manage to reduce the inter-class variance (method we call "leakage squeezing") so that the leakage distributions become almost independent from the processed data. We present two options for this countermeasure. The first one is based on a recoded memory with a size squared w.r.t. the unprotected requirement, whilst the second one is an enhancement alleviating the requirement for a large memory. We theoretically prove the robustness of those implementations and practically evaluate their security improvements. This is attested by a robustness evaluation based on an information theoretic framework and by a 2O-DPA, an EPA and a multi-variate mutual information analysis (MMIA) attack metric. As opposed to software-oriented 3O-DPA-proof countermeasures that seriously impact the performances, our is hardware-oriented and keeps a complexity similar to that of a standard 2O-attack countermeasure with an almost untouched throughput, which is a predominant feature in computing-intensive applications.

Keywords: Higher-Order Differential Power Analysis, Variance-based Power Attack (VPA), Multi-variate Mutual Information Analysis (MMIA), Masking Countermeasure, Leakage Squeezing, FPGA.

1 Introduction

During the last ten years, a lot of effort has been dedicated towards the research about side-channel attacks [1, 10] and the development of corresponding countermeasures. In particular, there have been many endeavors to develop effective countermeasures against differential power analysis (DPA) [11] attacks.

Amongst the two major countermeasures against DPA, hiding and masking, the latter is certainly the least complex to implement when applied at the algorithmic level. The idea of masking the intermediate values inside a cryptographic algorithm has been suggested in several papers [2, 4, 12] as a possible countermeasure to power analysis attacks. Masking ensures that every single variable

is masked with at least one random value so that a classical (first order) DPA attack cannot be successfully carried out anymore. However other attacks, such as the Higher Order DPA attacks [19, 20, 24], exist that can defeat masking.

In fact, masking can be defeated if the attacker knows how to combine the leakages corresponding to the masked data and its mask. This is known as second-order, or more generally higher-order, power analysis (abridged 2O-DPA and HO-DPA) and was originally suggested by Thomas S. Messerges in [19]. Investigating 2O-DPA, however, is of major importance for practitioners as it remains a good alternative that is powerful enough to break real-life, DPA-protected security products.

The attacker is allowed to profile the leakage in order to exhibit a relationship between the statistical distribution of the leakage and the value of a sensitive variable. Once this relationship is determined, the likelihood of key guesses is estimated given the distribution of the leakage. Such attacks are based on the same principle as the template attacks introduced by Suresh Chari *et al.* in [5]. These attacks have been successfully applied by Éric Peeters *et al.* in [20] to break some masked implementations more efficiently than any combining 2O-DPA. Moreover, Houssem Maghrebi *et al.* in [14] proposed a 2O-DPA based on variance analysis, called Variance Power Analysis (VPA), which is powerful enough to practically break a masked DES implemented in an FPGA. More recently, a generic multi-variate attack called MMIA has been introduced by Benedikt Gierlichs *et al.* [8] to attack high-order countermeasures. Therefore, there is a need for countermeasures thwarting 2O-DPA in particular and HO-DPA in general. We describe in the present paper a methodology to squeeze the leakage distributions so that any partitioning becomes almost indistinguishable.

The paper is organized as follows. Section 2 presents the state-of-the-art of first order masking and describes its weaknesses against 2O-DPA. The description of the concept of leakage squeezing is provided in section 3. The section 4 presents two variants of implementations and includes the experimental results about the complexity and robustness evaluation. Finally, section 5 concludes the paper and opens some perspectives.

2   State of the art

2.1   First Order Masking Overview

Let us consider the masked DES studied at UCL [23], whose principle is illustrated in Fig. 1. This algorithmic masking associates a mask ML, MR to the plaintext L, R.

At each round $i \in [1:16]$ an intermediate mask ML_i, MR_i is calculated in parallel with the intermediate cipher word L_i, R_i. If we let apart the expansion E and the permutation P, the DES round function f is implemented in a masked way by using a set of functions S and a set of functions S':

$$\begin{cases} \text{masked data: } S(x_m \oplus k) = S(x \oplus m \oplus k) = S(x \oplus k) \oplus m', \\ \text{mask} \qquad\quad m' = S'(x_m \oplus k, m) = S'(x \oplus m \oplus k, m). \end{cases} \quad (1)$$
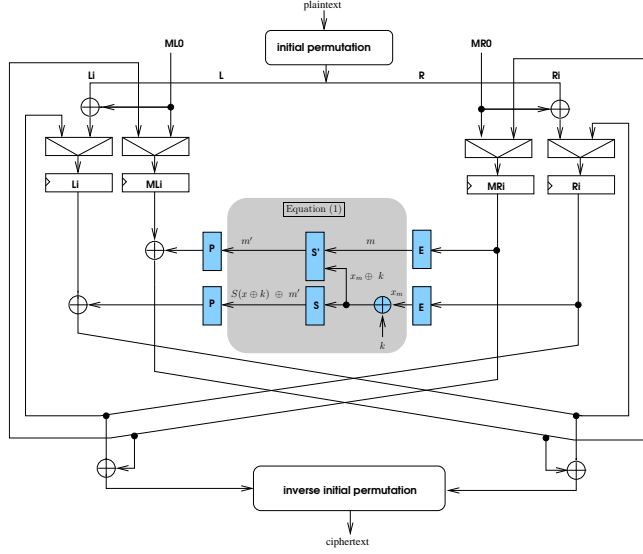
Fig. 1. ROM Masked DES.

The variable m' is a new mask reusable for the next round. The set of functions S contains the traditional S-boxes applied on masked intermediate words. The size of each S is 64 words of 4 bits when implemented with a ROM. S' is a new table which has a much greater ROM size of $4K$ words of 4 bits, as there are two input words of 6 bits.

The two operations of Eq. (1) can be executed sequentially, as in software. In hardware, they can be executed simultaneously. We call it "zero-offset" masking, and it will be our case of study in the rest of this article.

2.2 Vulnerability of the Masking against 1O-Attacks

It has been reported in [17] that first order DPA could be conducted on masked circuits. As investigated in [18], it happens that the leakage does not come from the registers, but from the combinational parts of the design. This logic is susceptible to produce glitches, whose appearance can be correlated with unmasked data during the internal demasking of the variables.

In this article, we reduce the number of glitches by confining the sensitive combinational logic in ROMs. The same approach has already been suggested in other papers, such as [9, §IV.1] Although this is not formally a guarantee that sensitive glitches disappear, we benefit all the same from the low-power design of the memory blocks that suppresses most of the non-functional activity.

For the proposed countermeasure to be evaluated clearly, we focus the rest of the article on the protection of registers: we assume a toggle count leakage

model (*aka* Hamming distance model), and we consider only attacks targeting this model.

2.3   Vulnerability of the Masking against 2O-Attacks

Implementations were studied to thwart attacks of high order, as that of Mehdi-Laurent Akkar [3] which uses constant masks. However to obtain an important robustness the price to be paid is a strong increase of the complexity. As illustration, it has been demonstrated by Jiqiang Lv in [13] that the DES algorithm requires at least three different masks and six additional S-boxes for every S-box to be resistant against high order attacks using this method. Another method, such as that used by François-Xavier Standaert *et al.* [23], consists in recomputing a new mask in every iteration at the same time as S-box, as Fig. 1 shows for the DES algorithm. The masked variable $x \oplus m$ of the register R is associated in every round with a new mask m stemming from the register M. So at the end of a round the variable $x \oplus m$ is transformed in $S'(x) \oplus m$ and the new mask m' which is calculated according to m and $x \oplus m$ by means of new S-box S'. This method offers a good compromise of complexity because it associates only a new S-box S' with every existing S-box S.

   This implementation remains subject to the 2O-DPA of Éric Peeters [20]. The figure 2 represents the S-box implementation S' in ROM. For reasons of simplicity the figure disregards the expansion and permutation functions appropriate for the DES algorithm. The so-called "zero-offset" HO-DPA attack of
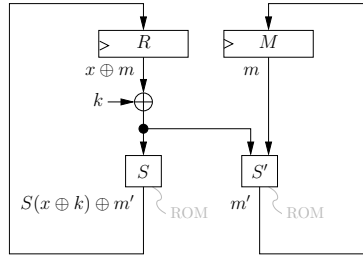

Fig. 2. Masked DES using two paths, implemented with ROM.

Éric Peeters [20] concerns variables $x \oplus m$ and m which are stored in R and M registers. The principle consists in studying the distributions of the activity at the register outputs for various values of x. In CMOS logic, a model of activity, noted A, can be the Hamming distance, noted HD, between two consecutive words:

$$\begin{aligned} A(x \oplus m, m) &\doteq HD(x \oplus m, S(x \oplus k) \oplus m') + HD(m, m') \\ &= HW(x \oplus S(x \oplus k) \oplus m \oplus m') + HW(m \oplus m') \\ &= HW(\Delta(x) \oplus \Delta(m)) + HW(\Delta(m)), \end{aligned}$$

where HW corresponds to the Hamming Weight and Δ is the difference between two consecutive values of a register output:

$$\Delta(x) \doteq x \oplus S(x \oplus k) \text{ and } \Delta(m) \doteq m \oplus m'. \tag{2}$$

If x and m fit on a single bit, the corresponding activity is $2 \cdot HW(\Delta(m))$ if $HW(\Delta(x)) = 0$, whereas if $HW(\Delta(x)) = 1$, the corresponding activity is $\overline{HW(\Delta(m))} + HW(\Delta(m))$ and is thus constantly equal to 1. The knowledge of the consumption distributions for every $HW(\Delta(x))$ values allows to build the HO-DPA attack by observing the consumption distributions and by comparing them with the predicted activity for a key hypothesis included in x.
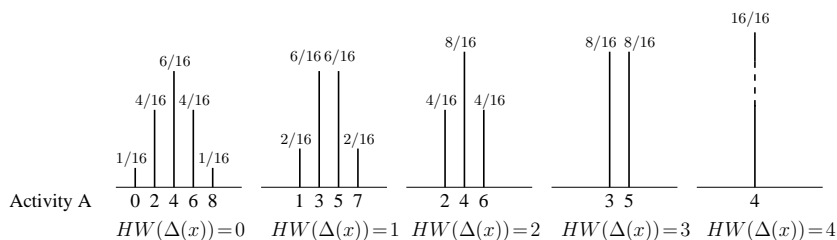

Fig. 3. Ideal (*i.e.* noise-free) probability density functions (pdf) corresponding to the five possible values of $HW(\Delta(x))$ without 2O-DPA protection [14].

Considering 4-bit registers, there are five possible distributions depending on the $HW(\Delta(x))$ values. They are shown in Fig. 3. It appears a clear difference between the five distributions, which could be exploited by a HO-DPA attack.

In [20], Éric Peeters proposed an improved higher-order technique to bypass the masking countermeasure. It is based on the efficient use of the statistical distributions of the power consumption described in figure 3 and it consists in computing the maximum likelihood of key guesses. Another alternative is to take advantage of the fact that the distributions showed in figure 3 all have the same mean value and only differ in their variances. This fact allows to understand the origin of previous attacks, as the one in [14], so-called Variance-based Power Attack where it is proposed to compute the difference of variance between the five possible distributions depending on the secret state of the implementation $HW(\Delta(x))$ values. This attack is quite efficient on "zero-offset" implementation and requires a reasonable number of traces (200K) [14]. Moreover, in [15] a novel approach to information-theoretic HO attacks, called the Entropy-based Power Analysis (EPA) was introduced using a weighted sum of conditional entropies as a distinguisher. It is designed to ease the distinguisability between hypotheses on candidate keys by computing the difference of conditional entropies between the distributions. Moreover, a novel approach, Multivariate Mutual Information Analysis MMIA, was proposed in [8]. This attack works in software masking but has never been applied on zero-offset implementations.

A simple approach consists in modifying the mask m by using a bijective transformation B before storing $B(m)$ in the mask register M. It is shown in Fig. 4. Indeed, the presence of $\Delta(m)$ twice in the leakage function, (Eqn. (2)), tends to reduce the effect of the masking countermeasure as the two terms compensate partially so that there remains a residual dependency in $HW(\Delta(x))$. To decorrelate those two terms, we need a Boolean function that implements good confusion, namely an S-box B. The activity of the variables $x \oplus m$ and $B(m)$ should be ideally decorrelated. This activity of the registers R and M is expressed by:

$$A_B = HW(x \oplus S(x \oplus k) \oplus m \oplus m') + HW(B(m) \oplus B(m'))$$
$$= HW[\Delta(x) \oplus \Delta(m)] + HW[\Delta B(m)] . \tag{3}$$

With the bijection, the leakage (Eqn. (3)) is squeezed because $\Delta(m)$ and $\Delta(B(m))$ do not cancel as easily as previously.

The bijection and its inverse can be implemented as internal encodings in a table. The figure 4 describes a hardware architecture, where the registers R and M are protected against Hamming distance attack via a squeezing of their leakage. The rest of the schematic is combinational logic : either gates or memory blocks.
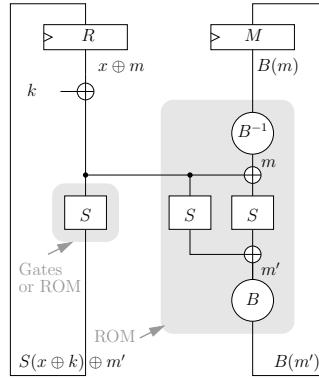
Fig. 4. Mask path with bijections for "Leakage squeezing".

By choosing the appropriate bijection B we can obtain very close distributions which should not allow the adversary to take advantage of the residual mismatches.

3.2 Formal Security Assessment and Motivation for some Bijections

In order to evaluate the information revealed by the squeezing countermeasure, we follow the information theoretic approach suggested in [22]. Namely we com-

pute the mutual information between the sensitive variable k and the leakage function A_B of Eqn. (3).

In our experiments, we will consequently assume that the leakage is affected by some Gaussian noise. Thus, the physical observations are represented by a variable : $O = A_B + \mathcal{N}(0, \sigma^2)$.

For comparison purposes, we compute the mutual information value ($I(k; O)$) as proposed in [22] for several bijection functions. The lower the mutual information, the better the countermeasure.

The mutual information is represented in figure 5 for the different bijections, in function of the signal-to-noise ratio ($SNR = 10 \cdot \log_{10} \frac{\epsilon^2}{\sigma^2}$), where ϵ and σ respectively denote the standard deviation of the signal and the noise emanated from the implementation.
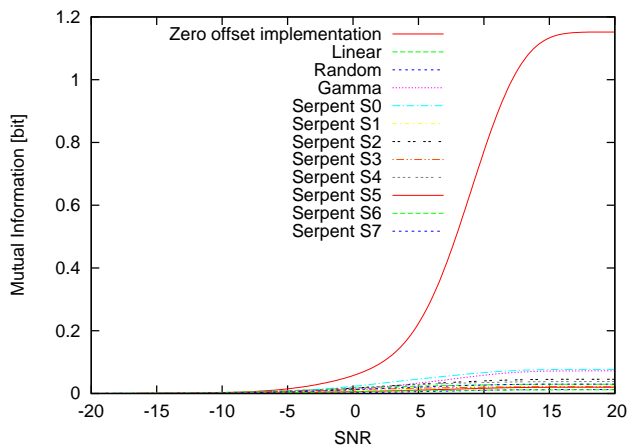
Fig. 5. Mutual information for some bijections.

These results demonstrate the information leakage reduction implied by the use of bijections functions. The linear function already decreases significantly the mutual information. Then, the non-linear functions still achieve a better improvement. It appears that Serpent S-boxes are leaking less than the randomly generated bijection or than the Gamma function of Noekeon. This justifies the use of the S-boxes crafted for strong symmetric algorithms.

This first analysis allows us to observe that the gain is high when the leakage squeezing is applied, because the mutual information is almost zero whatever the SNR. On the other hand, these results justify the best choice of the bijection to be used in our implementation. Indeed, the knowledge of this bijection (that can even be made public) is of no help for the attacker since the mask is unknown. Therefore, in all the cases, we assume a partitioning according to $HW(\Delta(x))$, that is independent of B.

4   Experiments on Masked DES Implementations

In this section, we apply the principle of leakage squeezing introduced in section 3.1 to DES. It requires an adaptation since its round function is more elaborate than $x \mapsto S(x \oplus k)$. Also, it is unrealistic to use 32-bits bijections. Therefore, we show how to split the bijection B (refer to Fig. 4) into smaller bijections. Two implementations are proposed: a ROM based architecture and a simpler structure called "Universal S-box Masking" (USM).

4.1   ROM Implementation

For DES we can use eight different bijections[1], denoted B_1, one for each S-box. To further protect the new mask m', we compose the DES parts by using external encodings with bijections B_2, for instance:

$$\underbrace{B_1^{-1} \circ E \circ S \circ P \circ \texttt{XOR}(L) \circ B_1}_{\text{ROM}} = \underbrace{B_1^{-1} \circ E \circ S \circ B_2}_{\text{ROM}} \circ P \circ \underbrace{B_2^{-1} \circ \texttt{XOR}(L) \circ B_1}_{\text{LUT network}},$$

(4)

where B_1 and B_2 are 4-bit bijections, E, S, P and $\texttt{XOR}(L)$, respectively the Expansion, S-Box, Permutation and Left part recombination of the DES algorithm. As the expansion E needs 6 bits, specific care has to be taken for the 4-bit bijections. This point is discussed further.

This principle of internal encodings has already been proposed by Chow *et al.* in [6] in the context of white box cryptography. This protection method has already been attacked for the DES and for the AES. However these attacks should not apply for the mask path as it is random and consequently no values can be imposed at the table inputs.

The general ROM implementation is given in figure 6. With respect to figure 4, the intermediate data (*e.g.* Sboxes output) have been protected by the same strategy, so as to provide a seamless "squeezing" throughout the combinational logic.

The bijection B_2 is constrained to be a *xor* operation with a constant, as the permutation P on 32 bits causes the ROM output bits to be split for the next round. The implementation of the mixing L with the left part can be done by a Look Up Table (LUT) network in FPGAs rather than a ROM in order to reduce the complexity. This requires that the bijections are a set of three 2-bit bijections to take advantage of LUT having 4 inputs (LUT4) in FPGAs, or two 3-bit bijections if LUT6 are available.

If we compare this implementation to the one proposed in [23] and described in figure 1, we have the same ROM complexity which is of eight 2^{12} words of four bits.

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[1] The same bijection can be reused eight times without compromising the security.
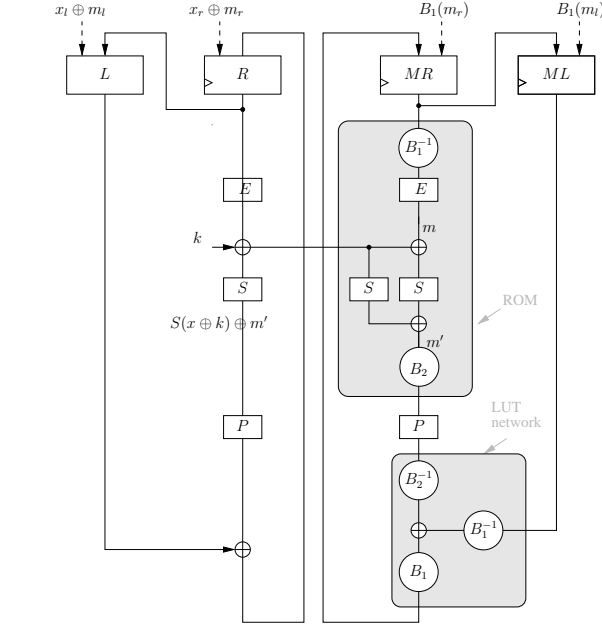
Fig. 6. Leakage squeezing of DES with a masked ROM implementation.

4.2   USM Implementation

The ROM implementation can be replaced by a more simple structure which is the Universal S-box Masking (USM) studied in [14]. This implementation presents some security weaknesses as discussed in [14]; the weakness can be exploited successfully by a classical CPA. If we apply function compositions as for Eq. (4) with new bijection encodings, the CPA and second order DPA attacks could be thwarted. Figure 7 illustrates the mask path of DES with USM implementation taking advantage of the "leakage squeezing" method. It is made up four stages which can be protected by using bijections B_1, B_2, B_3 and B_4. All the bijection are on four bits except B_2 which is on six bits.

Every stage can be implemented by a set of LUT networks or a ROM.

The bijection B_4 is constrained to be a *xor* operation with a constant, as the permutation P on 32 bits causes the output bits to be split.

All the stages can be implemented with a LUT network based on sets of 2-bit bijections. The second stage with the S-box could also be implemented in a small 64×4 ROM.

In this stage the mask m is xored with the masked data $x \oplus k \oplus m$ and the expansion E is performed as 6 bits of masks are considered.
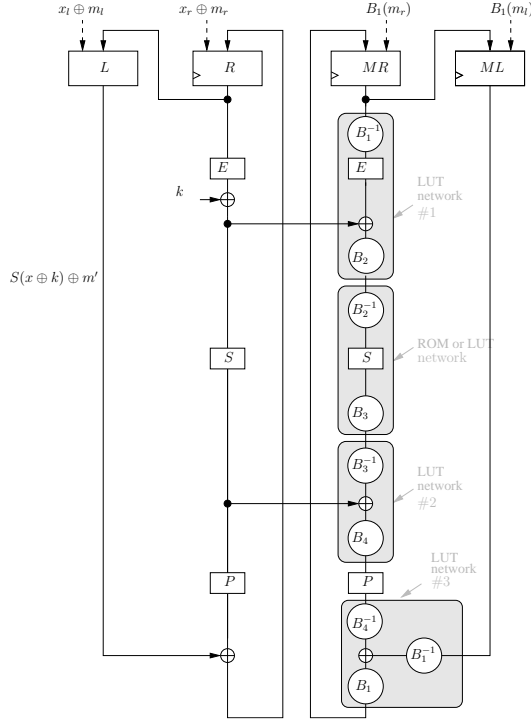
Fig. 7. Leakage squeezing of DES with a masked USM implementation.

4.3   Complexity and Throughput Results

The proposed implementations have been tested in a STRATIXII FPGA which is based on Adaptative LUT Module (ALM) cell. They have been compared with non protected DES, masked ROM and masked USM implementations without any leakage squeezing.

The table 1 summarizes the memories needed for each implementation and the estimated throughput.

These results show that the leakage squeezing method on hardware implementations has little impact on complexity and speed compared with software implementation against HO-DPA [21]. Moreover the USM implementation is particularly efficient as it avoids the use of large ROMs while keeping a high throughput.

In order to validate our implementations, we conduct in the next sections an evaluation of the leakages resulting from the leakage squeezing implementation. In [22], a theoretical framework was consequently introduced and suggests analyzing side-channel attacks with a combination of information theoretic and security metrics. These metrics respectively aim at evaluating the amount of in-

Table 1. Complexity and speed results. "l. s." denotes the "leakage squeezing" countermeasure.

Implementation	ALMs	Block mem-ory [bit]	M4Ks	Throughput [Mbit/s]
Unprotected DES (*reference*)	276	0	0	929.4
DES masked USM	447	0	0	689.1
DES masked ROM	366	131072	32	398.4
DES masked ROM with l. s.	408	131072	32	320.8
DES masked USM with l. s.	488	0	0	582.8

formation provided by a leaking implementation and the possibility to turn this information into a successful key recovery.

4.4   Information-Theoretic Evaluation of the Proposed Solutions

As it was suggested in [22], we computed the mutual information between the secret state k and the leakage function in the Hamming weight model with Gaussian noise for our two implementations and the others for comparison purposes.

Figure 8 (a) shows the mutual information values obtained for each kind of leakage with respect to an increasing noise standard deviation over [0.1, 10] (*i.e.* an increasing SNR over [-20 , 20])

(a) Comparison   (b) Zoom
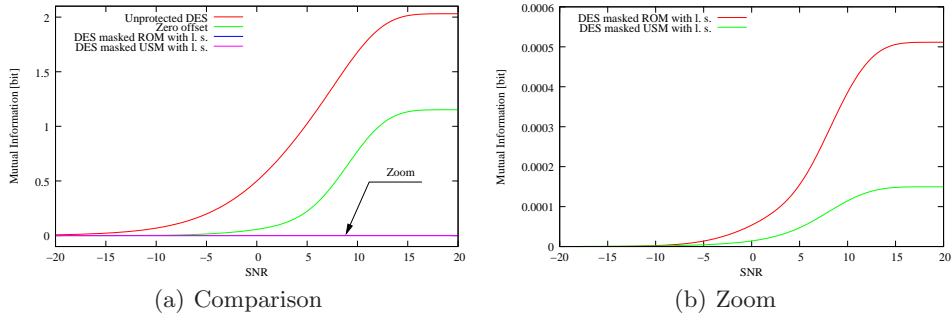
Fig. 8. Mutual information metric computed on several DES implementations.

These results demonstrate the information leakage reduction implied by the use of the leakage squeezing technique. As expected, the two implementations based on leakage squeezing leak less information than the zero offset implementation and the unprotected DES for all SNRs. The somewhat surprising conclusion of our experiments is that the mutual information is almost zero which proves the robustness of this technique. In figure 8 (b), we zoom on the evolution of

the mutual information in the case of the implementations based on the leakage squeezing technique in order to make a comparison between them.

We clearly see that when the SNR increases the mutual information for the USM implementation tend asymptotically to the value $1e^{-4}$ bit and remains below the mutual information leaked in the case of the ROM implementation (*i.e.* $5e^{-4}$) and then is the most robust implementation.

We can explain this results by the fact that the leakage squeezing techniques, (*i.e.* by applying bijection), aim at balancing the leakage distributions described in figure 3 so that any partitioning becomes almost distinguishable whatever the secret state $HW(\Delta(x))$ and as a consequence the information leakage is reduced. We showed in figure 9 the five possible values of $HW(\Delta(x))$ for the USM implementation with the squeezing leakage technique using the sixteenth serpent S-Box (*i.e.* proved to be the most appropriate bijection, see subsection 3.2). These distributions are clearly identical.
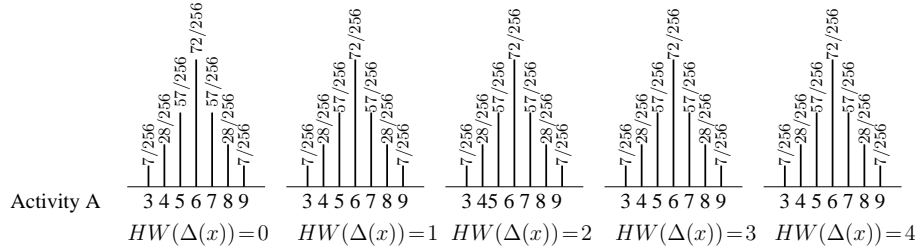

Fig. 9. Probability density functions (pdf) corresponding to the five possible values of $HW(\Delta(x))$ with Leakage Squeezing protection.

4.5 Evaluation of the Implementations against 2O-Attacks

After the information theoretic evaluation, the second step to evaluate the robustness of a leaking device is the security evaluation using various distinguishers to see how the information leakages translate into success rate under different assumptions.

First, we applied several side-channel distinguishers to leakage measurements simulated in the Hamming weight model with Gaussian noise. We not only applied (HO)-DPA, but also other kinds of attacks, namely MMIA. We chose to test these three side channel distinguishers against different kinds of masking, firstly because they are the most widely used in the literature, and secondly because they represent a brand spectrum of adversary capabilities.

Afterward, we performed these attacks against real power consumption measurements of our FPGA implementations in order to check them in a real-world context.

For each scenario, we acquired a set of $25,000$ power consumption traces using random masks and plaintexts. We performed the first order success rate as in [22].

We showed in figure 10 our experimental results also for these attacks on the "zero offset" hardware implementation used here for comparison purposes with our hardware solution based on the leakage squeezing technique.
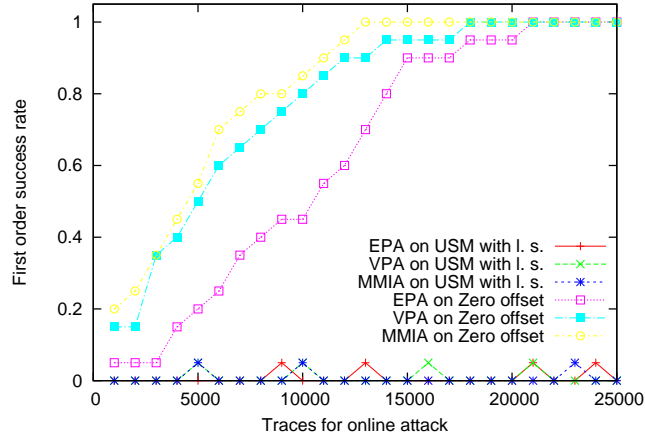

Fig. 10. First order success rate of 3 distinguishers, FPGA implementation.

We can see that the attacks based on various distinguishers perform well in the case of the "zero offset" implementation. About $5,000$ traces suffice to achieve a success rate of 50% and starting from about $13,000$ traces the MMIA attack reveals the correct key with success rate of 100%. The VPA and EPA attack perform well also. For the EPA, the success rates stay well above 50% even when using $11,000$ measurements, but eventually reaches success rate of 95% using $18,000$ traces.

For our proposed countermeasure, the attacks perform worse. The success rates stay under 10% even when using $25,000$ measurements.

We conclude that the experiments on a real circuit shows the evidence of benefit of our countermeasure since it leaks little information which are not exploited by the adversary to mount a successful attack.

5   Conclusion and Perspectives

Second order DPA attacks not only allow to theoretically invalidate some countermeasures, but can break them in practice. We presented in this paper a method called "leakage squeezing" which aims at balancing the power consumption distribution on hardware masked implementations. This method consists in

using bijective encodings composed of functional operations and implemented in ROMs or LUT networks. Two implementations have been proposed and evaluated. They provide a great robustness against 2O-DPA (VPA, EPA) and MMIA as none of the subkeys have been guessed using 25k traces. The robustness is corroborated by an information theoretic analysis of the leakage. Moreover the performances decrease in terms of complexity and speed are very limited, which is particularly true for the USM implementation which does not require large memories.

The main perspective of this work is to compare our countermeasure based fundamentally on Boolean masking with others solutions such the affine masking [7] scheme which also provides good performance-security against HO attacks.

Acknowledgment

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