

# Real-MFG: A Petri Net based model focusing on the integration of schedulability and fault tolerance

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## Abstract

Developing real-time software controlled systems for safety critical applications and verifying that they meet functional, fault tolerance and timing requirements are inherently complex processes. In order to meet a variety of (usually) conflicting requirements, it is necessary to follow an integrated approach from the early phases of design. In this paper, an integrated platform called Real-Time Multi Flow Graph (*Real-MFG*), is proposed, which provides encapsulation of both function- and priority- driven scheduling, incorporates constructs of powerful task graphs and integrates the Petri Net (*PN*) formalism with schedulability analysis methods. The model addresses fault tolerance requirements by including the promising imprecise computation paradigm in its semantics.

## Keywords

Real-time systems, Petri Net modeling, schedulability analysis, fault-tolerance

## 1 INTRODUCTION

*Petri Net (PN)* theory (Gerogiannis, 1995 and Gerogiannis, 1996a are two recent surveys) is one of the most popular formal methods that graphically models concurrency, nondeterminism and causal relationships between events that occur in a system. The asynchronous nature inherent in *PNs* implies that there is no measure of time or of the flow of time. The introduction of time into the *PN* model is mainly related to the location and type of time delays, the (absolute or relative) time mode and the type of firing rule (strong or weak firing).

Design oriented schedulability analysis and systematic simulation with *PNs* (i.e., reachability analysis) can be used in conjunction: schedulability analysis provides rigorous results using an analytical approach and a worst-case configuration, while *PN* based simulation provides conclusions without guarantees; it depends on the designer to establish the worst-case scenario (initial marking) and then to determine if timing constraints will be met or not (Gerogiannis, 1996b). However, in many cases (e.g., when a system has access to multiple active resources each of which is

scheduled independently), simulation provides real-time designers with a higher confidence level than schedulability analysis. Apart from the fact that almost all existing schedulability analysis tools/techniques are directly related to the specific phase in which they are involved (Gerogiannis, 1996c contains a more analytical justification), the application of different scheduling algorithms to different resources may lead to a complex behaviour that cannot be predicted through existing schedulability tests (Liu, 1993).

As far as fault tolerance is concerned, conventional techniques usually create temporal and/or spatial redundancy without taking into account any schedulability requirements (Stankovic, 1988). A recently proposed paradigm which tries to manage additional redundancy, while preventing timing faults by decreasing (in an acceptable way) the accuracy of the results, is the imprecise computation model (Liu, 1990). According to this paradigm, a task is composed of two parts: a mandatory part followed by an optional part; the first must complete before the corresponding deadline, while the latter simply refines the accuracy of the result produced by the mandatory part.

This paper focuses on the integration of formal design methods based on high-level timed *PNs* with schedulability analysis techniques. The semantics of a high-level timed *PN* called Real-Time Multi Flow Graph (*Real-MFG*) are given (a first model description had been given in (Gerogiannis, 1996c)). *Real-MFG* extends *IMFG*, a high-level *PN* that can be used for specifying user-system interaction (Kameas, 1995), and addresses fault tolerance requirements by including the promising imprecise computation paradigm in its semantics.

## 2 REAL-TIME MULTI FLOW GRAPH

*Real-MFG* is a process-based synchronisation model defined as a high-level Timed *PN*. A real-time application is regarded as a *Real-MFG* that consists of active components called actors (transitions) and passive components called links (places), which accommodate abstract data or control structures (tokens).

Tokens indicate the availability of resources or information, as well as the status of a *Real-MFG* at different phases of its execution. Tokens may indicate also occurrences of certain events which mark the enabling or the completion time of an actor. They can be of several classes; associated with each class there is a corresponding set of arcs. This facilitates tracing the flow of a particular typed token. An actor models a response that must be performed as a consequence of the occurrence of an event (e.g., a resource is available, a timer has expired, an interrupt has occurred). Responses are implemented as tasks and can be decomposed into smaller segments of called actions. Finally, links can model the storage of tokens, their flow among actors, the system conditions, the different events which can occur in the system, the interrelationships between actors, and the type of system resources.

### 2.1 Actors

An actor is described by:

1. Its *name* and a set of *input* and *output* links that make up its interface part.
2. A set of *rules* that make up its behavioural part (the left-hand side of each rule forms a precondition on the actor input links, while the right-hand side part forms a postcondition on its output links).
3. Its *type* that describes the semantics of its firing. The following actor types are provided:
  - *Context*: they represent responses that lead to the achievement of a system goal. They have an internal structure that represents how a response is decomposed into action actors to accomplishing a system goal.
  - *Action*: an action actor corresponds to a direct representation of a single action of a response.
  - *Library*: they are specific system-provided actors that describe the exact way responses are decomposed into actions in order to accomplish a system goal. Library Actors include Chain,

Loop, OR, Select, AND, Parallel-Min and Parallel-Max, Mandatory-Optional actors (characteristics met in AND/OR and imprecise workload models (Gillies, 1990; Liu, 1990) and in data-flow graphs (Papadimitriou, 1992)).

4. A set of *functional parameters* which describe the actor functionality. These include *weight* or *priority* which denotes the importance of actor firing (priority-driven scheduling (Lehoczky, 1991), *importance function* which represents the importance of an actor over time and used to specify multi-level scheduling requirements (function-driven scheduling (Strayer, 1992), *computation function* that represents the internal actor functionality, *preemptability* (the firing of an preemptable actor may be suspended and later resumed), *laxity type* and *laxity function* which indicate the relative cost of exceeding an actor's deadline but still completing firing (Liu, 1990; Liu, 1993), etc.
5. A set of *temporal parameters* which define the timing requirements associated with the actor (Liu, 1990; Tsai, 1995). These include *minimum timing constraint* (or *ready time*) and *maximum timing constraint* (or *deadline*), *maximum execution time* (or *maximum firing duration*), *mandatory and optional execution parts*, *average execution time* (or *average firing duration*), *period* (in case of output actors of a periodic event link), *minimum separation* (in case of output actors of a non periodic event link), *phase*, etc.

The description of a real-time application usually starts with a set of first-level context actors, which represent the basic structure of the application tasks. These are decomposed into action actors, which are used to represent in detail the real-time tasks that constitute the application.

## 2.2 Links

A link is described by:

1. Its *name* and a set of *input* and *output* actors that make up its interface part. These actors provide, consume, destroy or somehow use the tokens it stores.
2. Its *type* that makes up its behavioural part, since it explicitly defines the link role. The following link types are supported: *Context links*, which represent the context of real-time responses/actions, *event links*, which represent abstractions of application events, *resource links*, which represent abstractions of the various objects available for use by the application responses/actions, *condition links*, which represent global system conditions (system condition links) and possible interrelationships between actors (compound condition links), and *data links*, which model the data flow (the input and output data of a computation).
3. A set of *temporal parameters* which define the link timing behaviour and can be used to conduct analysis based on relative time mode. This set includes *maximum (minimum) timing constraint* and *arrival pattern* (only for event links), *maximum (minimum) (de-) acquisition time* and *context switch time* (only for resource links) (Liu, 1993), etc.

A resource link is described by the following parameters: *access type* (*exclusive* or *shared*), *resource type* (*Read only*, *Normal*) and *preemptability*. Event links are categorized according to their origin to (Klein, 1993): *Environmental*, *Internal* and *Timed*. In addition, event links are described by their arrival pattern and categorized to *periodic*, *irregular*, *bounded*, *bursty* and *unbounded*.

It should be noted that not all *Real-MFG* semantics are mandatory; the model formalism incorporates concepts from several paradigms, but it depends on the designer to select which attributes are applicable to his/her application.

## 2.3 State transition

*Real-MFG* uses the *PN* enabling and firing rules to represent state transition, modified as follows:

- An actor is said to be *active* if its input context link contains a token, while an active actor is said to be *enabled* if each of its input links has at least one token.
- An enabled actor is *firable* during the time interval from its *ready time* to its *deadline*, and a firable actor may fire only if its maximum firing duration is less than or equal to the time interval between its deadline and its ready time.
- In general, the firing of a firable actor will consume all tokens from its input links and will fill all its output links with tokens.

A state transition can take place only as a consequence of an event (that is, the appearance of a token on an event link) and is represented as an actor firing. An actor fires according to the *weak firing mode* which does not force any enabled actor to fire. This mode both preserves the same firing mode used by *PN* and can be used to model and analyze conflict structures. In addition, a *Real-MFG* can be analyzed based on *absolute* or *relative time modes*, since timing parameters can be associated with either the actors or links. The model maintains an internal structure with all the actors that are active at any moment (the *actor ready list*). This list forms a representation of a system state, and is modified by any event that causes a state transition, since new actors are added to the list, while others are removed. Therefore, *Real-MFG* constitutes an extension with memory of *PN* models.

### 3 CONCLUSIONS

*Real-MFG* incorporates advantageous characteristics of various *PN* timed versions, powerful task graphs and features found in real-time paradigms (e.g., relative/absolute time mode, typed enabling/firing rules, weak firing mode, average/fixed time intervals). The model supports multi-level scheduling, priority and function-driven design (by using the weight and importance function concept), incorporates fault tolerance semantics (mandatory and optional actor parts), and allows the designer to specify the application characteristics at any level of detail by using primitives of powerful task graphs. In comparison to implementation-oriented schedulability analysis techniques, *Real-MFG* is advantageous in being completely language independent. Other design-oriented approaches lack formal verification, systematic simulation and visualization support, characteristics inherent in the underlying model formalism (i.e., *PN* based specification).

*Real-MFG* provides several design perspectives, such as goal-subgoal structure, task analysis, causation, event flow, data flow, conditions, etc. Analysis can be performed by translating the model to an *ITCPN* (Van der Aalst, 1993) (or to a *TCPN* (Tsai, 1995) and then following reachability analysis. Moreover, *Real-MFG* can be used to represent and analyze complex applications which may include dependent tasks and aperiodic events. In that case, the designer is able to transform the model to a periodic task set in order to apply a schedulability analysis technique, which will determine the feasibility of the timing requirements.

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