

Binocular Rivalry Oriented Predictive Auto-Encoding Network for Blind Stereoscopic Image Quality Assessment

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Abstract—Stereoscopic image quality assessment (SIQA) has encountered non-trivial challenges due to the fast proliferation of 3D contents. In the past years, deep learning oriented SIQA methods have emerged and achieved spectacular performance compared to conventional algorithms which are only relied on extracting hand-crafted features. However, most existing deep SIQA evaluators are not specifically built for stereoscopic content and consider little prior domain knowledge of the 3D human visual system (HVS) in network design. In this paper, to better simulate the binocular rivalry phenomenon, we propose a Predictive Auto-encoDing Network (PAD-Net) for blind/No-Reference stereoscopic image quality assessment (NR-SIQA). The proposed encoder-decoder architecture is inspired by the predictive coding theory that the cognition system tries to match bottom-up visual signal with top-down predictions. Besides, we design the Siamese framework to mimic the binocular rivalry in the 3D HVS based on the likelihood and prior maps generated from the predictive coding process. Extensive experimental results on three publicly available stereoscopic image quality databases demonstrate that the devised approach outperforms state-of-the-art algorithms for predicting the perceptual quality of both symmetrically and asymmetrically distorted stereoscopic images with various distortion types.

Index Terms—Siamese encoder-decoder, stereoscopic image quality, 3D human vision, predictive auto-encoding, quality regression.

I. INTRODUCTION

IMAGE quality assessment (IQA) plays an essential role in various image processing and visual communication systems. In the literature, many traditional 2D IQA metrics have been proposed [1]–[7]. Due to the unprecedented development of 3D/stereoscopic technologies, quality issues for 3D media are becoming more and more attracted in both academy and industry [8]. Through the process of acquisition, compression, transmission, display, etc. original reference stereoscopic images usually suffer from perceptual quality degradation

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caused by diverse distortion types and degrees. As a result, the demands for effectively assessing the perceptual quality of stereoscopic images are urgent.

Compared with the previous 2D IQA case, stereoscopic image quality assessment (SIQA) is more challenging owing to a wide variety of 2D and 3D influential factors, such as image spatial artifacts, depth perception, visual comfort, and so on [9]. These factors have different effects on evaluating the quality of experience (QoE) for stereoscopic images. Except for [10] that considers image distortion and depth perception quality simultaneously, existing research works mainly focus on modeling each individual factor for 3D QoE [11]–[14]. In this paper, we aim to study the visually perceptual quality assessment of stereoscopic images.

Similar to 2D IQA, according to the availability of original reference stereoscopic images, SIQA models are typically divided into three categories: full-reference (FR) [15]–[21], reduced-reference (RR) [22]–[24], and blind/no-reference (NR) [25]–[31] SIQA metrics.

For FR SIQA algorithms, full information of the reference image is assumed to be exploited. The earliest FR IQA model investigated some off-the-shelf 2D IQA metrics, such as structural similarity index (SSIM) [1], universal quality index (UQI) [2], C4 [3] and so on [4], to assess stereoscopic image quality [15]. Further, disparity information was integrated into the 2D IQA metrics to predict the 3D image quality [16], [17]. Apart from incorporating depth clues, the binocular vision characteristics of the human visual system (HVS) were combined with 2D IQA algorithms. For example, Gorley and Holliman proposed a new stereo band limited contrast (SBLC) metric based on the HVS sensitivity to contrast changes in high frequency regions [18]. Moreover, Chen *et al.* [19] proposed cyclopean images according to the binocular rivalry in the human eyes. In addition, Lin and Wu developed a binocular integration based computational model for evaluating the perceptual quality of stereoscopic images [20].

As for RR SIQA approaches, only part of original non-distorted image data is available. Qi *et al.* utilized binocular perceptual information (BPI) to perform RR SIQA [22]. By characterizing the statistical properties of stereoscopic images in the reorganized discrete cosine transform (RDCT) domain, Ma *et al.* presented the RR SIQA method [23]. Furthermore, a new RR-SIQA metric based on natural scene statistics (NSS) and structural degradation was proposed [24].

However, in most practical applications, the original pristine

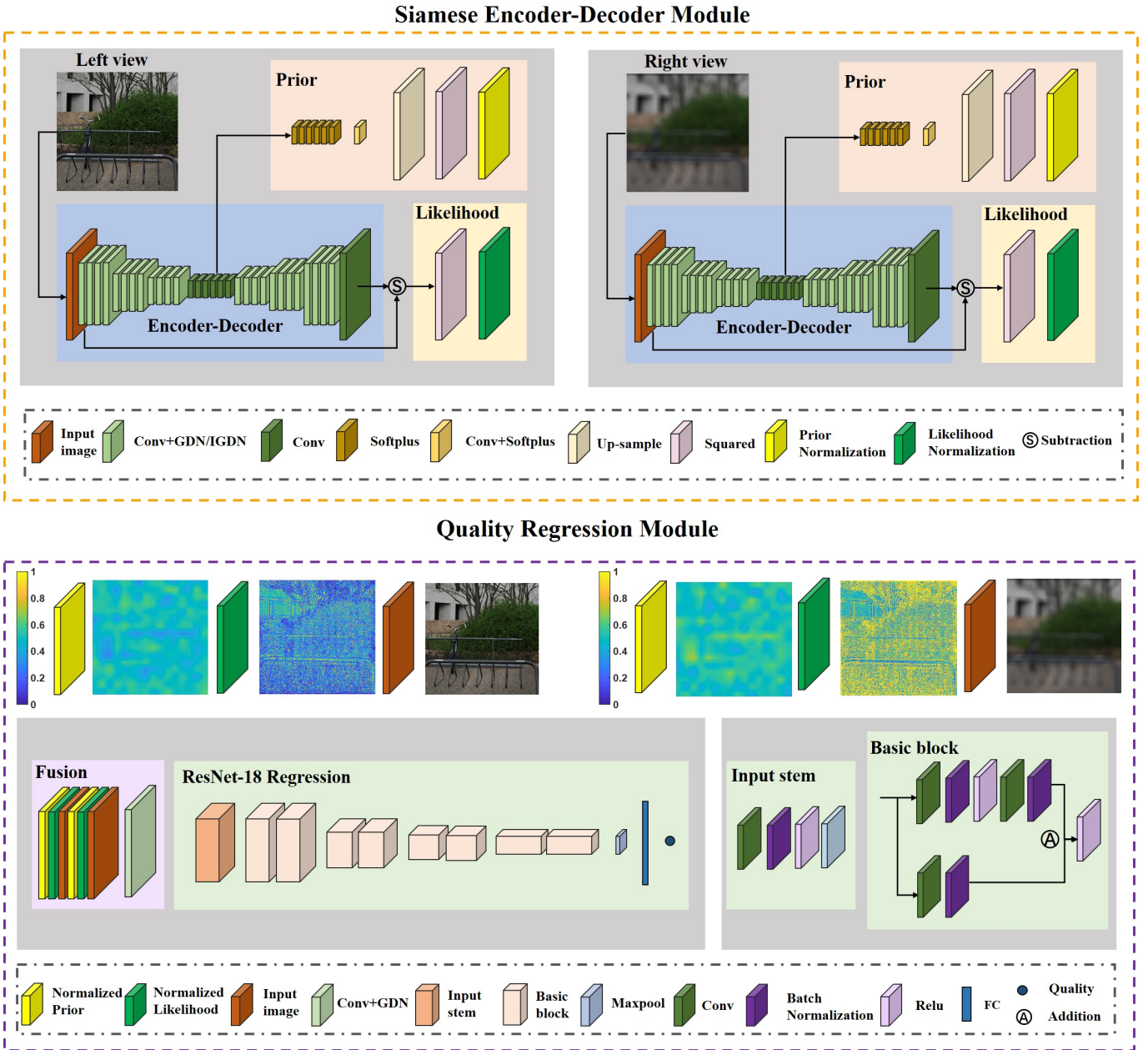


Fig. 1: The architecture of our proposed PAD-Net. It consists of a Siamese encoder-decoder module and a quality regression module. For the entire network, given paired distorted stereoscopic images and it will predict the perceptual quality score. In the Siamese encoder-decoder module, we calculate the prior and likelihood probability for each view image. Then, the left and right view images as well as their likelihood and prior probability maps are feed into the quality regression network for final score computation.

image cannot be accessible. Therefore, NR SIQA is inevitably required. Some research works have been studied about NR SIQA. Akhter *et al.* extracted the local features of artifacts and disparity to evaluate the perceptual quality of stereoscopic images [25]. Sazzad *et al.* also exploited perceptual differences of local features for NR SIQA [26]. However, these methods are distortion-specific NR SIQA approaches, which are only suitable for JPEG coded stereoscopic image pairs. Thus, several general-purpose NR SIQA metrics have emerged. Chen *et al.* [27] extracted 2D and 3D NSS features from

stereoscopic image pairs. The shape-parameter features were regressed onto subjective quality scores by using the well-known support vector regression (SVR). Su *et al.* proposed the stereoscopic/3D blind image naturalness quality (S3D-BLINQ) index by constructing a convergent cyclopean image and extracting bivariate and correlation NSS features in spatial and wavelet domains [28].

With the development of deep learning techniques, deep neural networks (DNN) have achieved remarkable advantages for many image processing and computer vision tasks [32]–

[34]. It also brings improvement for the study on NR SIQA. Specifically, Shao *et al.* proposed a blind deep quality evaluator for assessing stereoscopic image quality with monocular and binocular interactions based on deep belief network (DBN) [11]. The deep NR stereoscopic/3D image quality evaluator (DNR-S3DIQE) was proposed, which extracted local abstractions and then aggregated them into global features by employing the aggregation layer [29]. In addition, Yang *et al.* took into account the deep perception map and binocular weight model along with the DBN to predict perceived stereoscopic image quality [30]. In [35], a deep edge and color signal integrity evaluator (DECOSINE) was proposed based on the whole visual perception route from eyes to the frontal lobe. Besides, Zhou *et al.* proposed a dual-stream interactive network called stereoscopic image quality assessment network (StereoQA-Net) for NR SIQA [31]. However, the above-mentioned algorithms consider little prior domain knowledge of the 3D HVS, and thus having difficulty in accurately predicting the perceptual quality of stereoscopic images with various distortion types and levels.

Binocular vision is crucial to quality assessment for stereoscopic images, and can be mainly classified into three categories, namely binocular fusion, rivalry and suppression [10]. Firstly, if the retina regions of left and right eyes receive the same or similar visual contents, binocular fusion happens and the two views are integrated into one single and stable binocular perception [36]. Secondly, binocular rivalry is a phenomenon in 3D vision, in which perception alternates between different views when two eyes see different scenes [37]. Thirdly, binocular suppression occurs since the HVS cannot tolerate binocular rivalry for a long time. During binocular suppression, one view may be inhibited by the other entirely [10]. Existing researches consider either one or multiple binocular vision mechanisms to assist SIQA and in this paper, we primarily focus on modeling binocular rivalry for SIQA. In conventional perspective, binocular rivalry is simulated by low-level competition between the input stimulus and it is related to the energy of the stimulus [38]–[40]. Recently, more literatures try to explain binocular rivalry by the predictive coding theory [41], [42]. It is a popular theory about how brain process sensing visual stimuli. According to predictive coding theory, the cognition system tries to match bottom-up visual signal with top-down predictions [43]. Different from the traditional statements that binocular rivalry is low-level inter-ocular competition in early visual cortex, binocular rivalry mechanism based on predictive coding theory (BRM-PC) stress more on the high-level competition [41]. Moreover, the BRM-PC is the HVS guided and more inline with human cognition system [42]. Therefore, we believe that introducing BRM-PC will be beneficial to SIQA.

In this paper, we propose a generic architecture called Predictive Auto-encoDing Network (PAD-Net), which is an end-to-end network for general-purpose NR SIQA. Our contributions of the proposed method are summarized as follows:

- We propose a biologically plausible and explicable predictive auto-encoding network through combining the network design with the binocular rivalry mechanism based on predictive coding theory [42] which helps to

explain the binocular rivalry phenomenon in 3D vision. The source code of PAD-Net is available online for public research usage¹.

- According to the predictive coding theory in human brain, we adopt the encoder-decoder architecture to reconstruct the sensory input and further exploit the Siamese network to generate the corresponding likelihood as well as prior maps for modeling binocular rivalry in the cognition system.
- We demonstrate that we can obtain the fusion information to reflect the perceived differences for symmetrically and asymmetrically distorted stereoscopic image pairs under various distortion types and levels.
- Compared with state-of-the-art SIQA metrics, the proposed PAD-Net provides more precise quality estimation, especially for those stereopairs under asymmetric distortions thanks to the well consideration of binocular rivalry based on predictive coding theory.

The remainder sections of this paper are organized as follows. Section II explains the proposed Predictive Auto-encoDing Network (PAD-Net) for NR SIQA in details. Section III presents the experimental results and analysis. In Section IV, we conclude the paper with an outlook on the future work.

II. BINOCULAR RIVALRY MECHANISM BASED ON PREDICTIVE CODING THEORY

In this section, we will first describe the predictive coding theory and then introduce the binocular rivalry mechanism based on predictive coding theory (BRM-PC) in details.

A. Predictive Coding Theory

According to [44], the core task of brain is to represent the environmental causes of its sensory input. In other words, given a sensory input, the cognition system of human brain will predict the environmental cause, and gives a hypothesis. The final perceptual content is determined by the hypothesis that generates the best prediction [42].

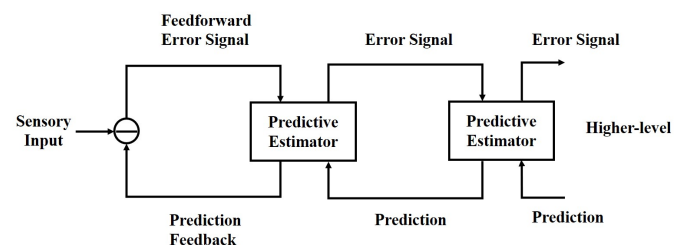


Fig. 2: Predictive coding theory based hierarchical representation of the sensory input [45]. In this model, the feedback pathways carry the prediction from higher-level. In addition, the feedforward pathways return the prediction errors between the prediction and sensory input to update the prediction and get the best hypothesis.

Numerous predictive coding models have been proposed, and the simplest is the linear predictive coding (LPC) in digital

¹<http://staff.ustc.edu.cn/~chenzhibo/resources.html>

signal processing [46]. Then, the predictive coding theory has been applied to efficient encoding in the retina. Rao *et al.* [45] proposed a hierarchical model to represent the principle of human brain in Fig. 2. The feedback pathways carry the prediction from higher-level and the feedforward pathways return the prediction errors between the prediction and sensory input to update the prediction and get the best hypothesis. The model mentioned here is for monocular vision, and it is the basis of binocular rivalry model. In Rao's model, consider an image \mathbf{I} , it is represented by a vector \mathbf{r} (lower-level cause) using the activation function f and the dictionary \mathbf{U} :

$$\mathbf{I} = f(\mathbf{U}\mathbf{r}) + \mathbf{n} = f\left(\sum_{j=1}^k \mathbf{U}_j r_j\right) + \mathbf{n}, \quad (1)$$

where \mathbf{n} is the stochastic noise and \mathbf{U}_j denotes the basis vector. Then the vector \mathbf{r} can be further represented as:

$$\mathbf{r} = f(\mathbf{U}^h \mathbf{r}^h) + \mathbf{n}^{td} = \mathbf{r}^{td} + \mathbf{n}^{td}, \quad (2)$$

where \mathbf{U}^h and \mathbf{r}^h are higher-level dictionary and causes. \mathbf{r}^{td} is the 'top-down' prediction of \mathbf{r} . Then $E = \frac{1}{\sigma^2}(\mathbf{I} - f(\mathbf{U}\mathbf{r}))^T(\mathbf{I} - f(\mathbf{U}\mathbf{r}))$ can be applied as the optimization function since the goal of the predictive coding model is to estimate suitable causes for generating the best prediction.

B. Binocular Rivalry Mechanism Based on Predictive Coding Theory

According to [37], binocular rivalry appears when left and right views are given different images, and the perception alternates between the two views. It is an important phenomenon when evaluating the quality of stereoscopic images due to the existence of asymmetrical distortion which means left and right views may suffer from different levels of distortion. Thus, employing binocular rivalry mechanism is beneficial to the improvement of stereoscopic image quality assessment.

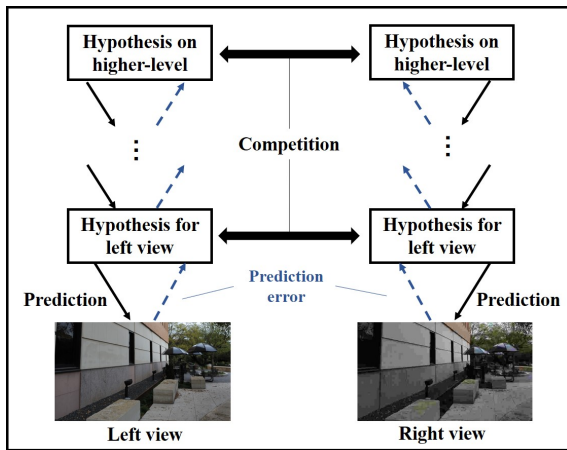


Fig. 3: Simplified schematic of the binocular rivalry mechanism based on predictive coding theory [42]. The black solid arrow is the top-down prediction from higher-level and the blue dotted arrow is the bottom-up error signals. The hypothesis for left and right view will compete with each other to generate the final perceptual content.

Introducing predictive coding theory to explain binocular rivalry phenomenon has attracted greater attention from the community in recent years [42]. Compared with the conventional perspective that believes binocular rivalry is low-level inter-ocular competition in early visual cortex, BRM-PC stress more on the high-level competition [47]. In this paper, we adopt the general theoretical framework in [42], [48] for SIQA. On the basis of BRM-PC, we perceive the content since the corresponding hypothesis has the highest posterior probability from the Bayesian perspective [49], [50]. As shown in Fig. 3, given a stereoscopic image, our brain normally first determines a hypothesis that can best explain the corresponding stimulus. The perceptual inference depends on the likelihood as well as the prior probability of the hypotheses. **The likelihood $p(\mathbf{I}|\mathbf{H})$ is about how well the hypothesis \mathbf{H} predicts the input \mathbf{I} . The prior $p(\mathbf{H})$ is related to empirical knowledge (shape, material, lighting) which comes from hypothesis on higher-level [50], [51] and is about how probable the hypothesis is.** Then, the hypotheses for left and right views will compete with each other according to the posterior probability $p(\mathbf{H}|\mathbf{I})$ computing from prior and likelihood.

According to the above analysis, we can conclude that the likelihood and prior are important to obtain perceptual inference during binocular rivalry. And they can be designed based on the high-level causes and the error map in the predictive coding model introduced in Section II A.

III. PROPOSED METHOD

Inspired by the BRM-PC [42], we design the no-reference PAD-Net to automatically predict the perceptual quality of stereoscopic images. The proposed PAD-Net is a Siamese based end-to-end network, including auto predictive coding and quality regression modules. Given paired distorted 3D images, they are divided into sub-images with size 256x256 first, then the quality scores of these sub-images are estimated through PAD-Net and aggregated as a final one as done in [52]. We pre-train the proposed auto-encoder and quality regression module on Waterloo Exploration Database [53] and LIVE 2D Database [54], respectively. After that, the entire network is jointly optimized using 3D IQA databases [19], [55] to generate more accurate predictions.

In this section, the architecture of our proposed PAD-Net is described first as shown in Fig. 1. Then, we introduce the Siamese encoder-decoder module and quality regression module in details. Finally, the training and testing methods of our PAD-Net are presented.

A. Overview

The architecture of the PAD-Net is depicted in Fig. 1, which contains a Siamese encoder-decoder module and a quality regression module. The Siamese encoder-decoder module represents the processing procedure of left and right view images. It is inspired by the predictive coding theory that the human brain tries to match bottom-up visual stimuli with top-down predictions [43]. In Section II, an empirical Bayesian framework based on BRM-PC is introduced and the rivalry dominance is calculated from the likelihood and prior

probability [56]. Correspondingly, the likelihood and prior are inferred through the Siamese encoder-decoder in our proposed PAD-Net. *Note that we are not going to calculate real probabilities in the proposed method, but just try to model the likelihood and prior with a quantity that has similar physical meaning in the BRM-PC described in [42].*

For each branch of the Siamese encoder-decoder, four times down convolution and up convolution with a stride of 2 pixels are performed to reconstruct the distorted images. Non-linear activation function layers follow the first three down convolution and up convolution layers to enhance the representation ability of our neural network. We square the error between the input and reconstructed image as the residual map and utilize this map for likelihood calculation. Moreover, the high-level features are convolved with a stride of one pixel to change the channel size and upsampled to the same resolution as the input image. In the PAD-Net, we use the reconstruction error to obtain likelihood probability map and the high-level representation after four times down convolution to generate prior probability map. The reasons will be given in Section III B.

Once we get the left and right view images as well as their likelihood and prior probability maps, we can put them into the quality regression module and compute the final quality score. It can be seen from the bottom of Fig. 1 that the quality regression module is composed of 1) fusion for input images and probability maps, 2) ResNet-18 without last two layers as feature extractor and 3) the final max pooling and fully connected layer. Note that fusion in Fig. 1 includes a one stride convolution layer and activation function layer to match the input size with ResNet-18. The output of the proposed PAD-Net is the predicted quality score of the input stereoscopic image.

B. Siamese Encoder-Decoder Module

The Siamese encoder-decoder module is inspired by the BRM-PC, which is the HVS guided and able to generate more reliable and interpretable results. To simulate the predictive coding process in BRM-PC, we adopt the encoder-decoder network structure for image compression from [57], [58], which is a hierarchical structure. In Fig. 2, prediction is adjusted with residual errors to obtain better hypothesis, thus, we employ the squared error between predicted (decoded) image and input image [45] as our loss function l_1 to pre-train the encoder-decoder network as follows:

$$l_1 = \frac{1}{M \times N \times C \times K} \sum_{x,y,c,k} (\mathbf{I}^{(k)}(x, y, c) - \hat{\mathbf{I}}^{(k)}(x, y, c))^2, \quad (3)$$

$$\hat{\mathbf{I}}^{(k)} = f_1(\mathbf{I}^{(k)}; \mathbf{w}_1), \quad (4)$$

$$\mathbf{w}'_1 = \arg \min_{\mathbf{w}_1} l_1, \quad (5)$$

where $\mathbf{I}^{(k)}$ and $\hat{\mathbf{I}}^{(k)}$ represent the k -th input and predicted image. M , N and C are the width, height and channel of $\mathbf{I}^{(k)}$ and $\hat{\mathbf{I}}^{(k)}$. K is the batch size of a mini-batch training data. $\hat{\mathbf{I}}^{(k)}$ is estimated via the encoder-decoder network f_1 with weight

\mathbf{w}_1 . \mathbf{w}'_1 is the weight for encoder-decoder after loss minimization. During the training stage, the loss is defined as the prediction error between distorted and reconstructed images which can be assumed as the feedforward error signal in Fig. 2. Then, we use the gradient descent algorithm to update \mathbf{w}_1 and generate better prediction. Finally, the prediction error will converge and reach a stable value. The decoded image would not change greatly. Thus, the updating policy of the encoder-decoder network is similar to the prediction coding theory of human brain. Note that the encoder-decoder network is pre-trained on the Waterloo Exploration Database [53], therefore the training data includes both reference and distorted images.

TABLE I: DETAILED CONFIGURATIONS OF THE ENCODER-DECODER NETWORK.

	Layer	Input Shape $C \times H \times W$	Output Shape $C \times H \times W$	Kernel size/ Stride/Padding
Encoder	Conv1+GDN1	3, 256, 256	128, 128, 128	5x5/2/2
	Conv2+GDN2	128, 128, 128	128, 64, 64	5x5/2/2
	Conv3+GDN3	128, 64, 64	128, 32, 32	5x5/2/2
	Conv4	128, 32, 32	192, 16, 16	5x5/2/2
Decoder	Unconv1+IGDN1	192, 16, 16	128, 32, 32	5x5/2/2
	Unconv2+IGDN2	128, 32, 32	128, 64, 64	5x5/2/2
	Unconv3+IGDN3	128, 64, 64	128, 128, 128	5x5/2/2
	Unconv4	128, 128, 128	3, 256, 256	5x5/2/2

¹ Conv: Convolution

² Unconv: Fractionally-strided convolution

³ GDN: Generalized divisive normalization

⁴ IGDN: Inverse generalized divisive normalization

⁵ $C \times H \times W$: Channel \times Height \times Width

The structure of the encoder-decoder network is listed in Table I. It is composed of convolution and fractionally-strided convolution layers [59], generalized divisive normalization (GDN) transform and inverse generalized divisive normalization (IGDN). GDN is inspired by the neuron models in biological visual system and proves to be effective in density estimation [60], image compression [58] and image quality assessment [52]. The GDN and IGDN operations are given by:

$$\mathbf{y}_i(m, n) = \frac{\mathbf{x}_i(m, n)}{(\beta_i + \sum_j \gamma_{ij} \mathbf{x}_j(m, n)^2)^{\frac{1}{2}}}, \quad (6)$$

$$\hat{\mathbf{x}}_i(m, n) = \hat{\mathbf{y}}_i(m, n) \cdot (\hat{\beta}_i + \sum_j \hat{\gamma}_{ij} \mathbf{x}_j(m, n)^2)^{\frac{1}{2}}, \quad (7)$$

where \mathbf{x}_i means the i -th channel of \mathbf{x} and it is the input of GDN transform. \mathbf{y}_i is the i -th channel of normalized activation feature map and it is the output of GDN operation. Moreover, β and γ are the parameters to be updated in GDN function. Likewise, $\hat{\mathbf{x}}_i$, $\hat{\mathbf{y}}_i$, $\hat{\beta}$ and $\hat{\gamma}$ share the same meaning as \mathbf{x}_i , \mathbf{y}_i , β and γ for IGDN transform. The goal of our encoder-decoder module is to reconstruct the input sensory instead of compressing it. Therefore, we remove the quantization step in [58] for better reconstruction.

By now, we can get the high-level causes (high-level features) and reconstructed image from the input sensory in the proposed Siamese encoder-decoder module. Then, according to the BRM-PC [42], the left and right views will compete with each other to obtain the best hypothesis which is related to prior and likelihood. To be specific, the likelihood is about how well the hypothesis predicts the input and the prior is about

how probable the hypothesis is and concern with empirical knowledge [50]. Corresponding to the physical meaning of likelihood and prior, we first obtain the k -th squared residual error map $\mathbf{E}^{(k)}$ in the mini-batch of a size of K to calculate likelihood as follows:

$$\mathbf{E}^{(k)} = \frac{1}{C} \sum_c (\mathbf{I}_c^{(k)} - \widehat{\mathbf{I}}_c^{(k)})^2, \quad (8)$$

where $\mathbf{I}_c^{(k)}$ and $\widehat{\mathbf{I}}_c^{(k)}$ denote the c -th channel of the input and predicted image. C equals 3 in Eq. 8. The likelihood is used to measure the similarity between $\mathbf{I}_c^{(k)}$ and $\widehat{\mathbf{I}}_c^{(k)}$ and it is inversely proportional to errors. The training stage of encoder-decoder network can be regarded as the procedure of prediction error minimization.

In the Siamese encoder-decoder module, the prior is modeled with the high-level representation of the sensory input [51] since the prior comes from high-levels in the cognition system, as assumed in empirical Bayes [42], [61]. Thus, the high-level features are utilized to generate the k -th prior map $\mathbf{P}^{(k)}$. Before being fed into the quality regression module, the squared error map $\mathbf{E}^{(k)}$ and the prior map $\mathbf{P}^{(k)}$ are normalized between left and right view as follows:

$$\mathbf{P}_{nl}^{(k)} = \frac{\mathbf{P}_l^{(k)}}{\mathbf{P}_l^{(k)} + \mathbf{P}_r^{(k)}} \quad \text{and} \quad \mathbf{P}_{nr}^{(k)} = \frac{\mathbf{P}_r^{(k)}}{\mathbf{P}_l^{(k)} + \mathbf{P}_r^{(k)}}, \quad (9)$$

$$\mathbf{L}_{nl}^{(k)} = \frac{\mathbf{E}_r^{(k)}}{\mathbf{E}_l^{(k)} + \mathbf{E}_r^{(k)}} \quad \text{and} \quad \mathbf{L}_{nr}^{(k)} = \frac{\mathbf{E}_l^{(k)}}{\mathbf{E}_l^{(k)} + \mathbf{E}_r^{(k)}}, \quad (10)$$

where $\mathbf{P}_l^{(k)}$, $\mathbf{P}_r^{(k)}$, $\mathbf{E}_l^{(k)}$ and $\mathbf{E}_r^{(k)}$ are the prior and error maps for the k -th left view and right view images in a mini-batch. $\mathbf{P}_{nl}^{(k)}$, $\mathbf{P}_{nr}^{(k)}$, $\mathbf{L}_{nl}^{(k)}$ and $\mathbf{L}_{nr}^{(k)}$ indicate the normalized prior and likelihood probability maps. Note that the error is opposite to the likelihood, that is to say, if the error is large, the likelihood will be small. For example, when computing the likelihood map for left view, the error map of right view is adopted and vice versa.

TABLE II: DETAILED CONFIGURATIONS OF THE PRIOR AND LIKELIHOOD GENERATION NETWORK.

	Layer	Input Shape $C \times H \times W$	Output Shape $C \times H \times W$	Kernel size/ Stride/Padding
Prior	Softplus4	192, 16, 16	192, 16, 16	-
	Conv5+Softplus5	192, 16, 16	1, 16, 16	1x1/1/0
	Up-sample6	1, 16, 16	1, 256, 256	-
	Square7a	1, 256, 256	1, 256, 256	-
	Normlization8a	1, 256, 256	1, 256, 256	-
Likelihood	Square7b	1, 256, 256	1, 256, 256	-
	Normlization8b	1, 256, 256	1, 256, 256	-

¹ Conv: Convolution

² Normlization: Normalization between left view and right view

³ $C \times H \times W$: Channel \times Height \times Width

The detailed structure of prior and likelihood creation is given in Table II. We employ the Softplus activation function [62] in prior generation to avoid square negative values to positive values. It is defined as:

$$s(x) = \log(1 + e^x). \quad (11)$$

The Softplus function can be regarded as the smoothing version of ReLU function which is similar to the way cerebral neurons being activated [63].

C. Quality Regression Module

Based on the distorted stereoscopic images as well as the obtained prior and likelihood probability maps from the Siamese encoder-decoder module, we fuse them as a 3-channel feature map and further feed the 3-channel feature map into the ResNet-18 quality regression network to extract discriminative features for quality estimation. ResNet-18 is chosen for its excellent ability of feature extraction [34], [64]. The last two layers including average pooling and fully connected layer are removed for regressing the feature map into a quality score. Table III illustrates the architecture of quality regression network. The input stem and basic block of the ResNet-18 structure are shown in Fig. 1.

TABLE III: DETAILED CONFIGURATIONS OF THE QUALITY REGRESSION NETWORK.

	Layer	Input Shape $C \times H \times W$	Output Shape $C \times H \times W$	Kernel size /Stride/Padding
Fusion	Conv9+GDN9	10, 256, 256	3, 256, 256	1x1/1/0
ResNet18 Regression	ResNet-18	3, 256, 256	512,8,8	-
	Maxpool10	512,8,8	512,1,1	8x8/8/0
	Fc11	512	1	-

¹ Conv: Convolution

² GDN: Generalized divisive normalization

³ Fc: Fully connected layer

⁴ $C \times H \times W$: Channel \times Height \times Width

D. Training and Testing

Owing to the limited size of available 3D image quality assessment database, we train the PAD-Net on the sub-image pairs with the resolution of 256×256 , the MOS value for the entire image is assumed as the quality scores for several sub-images as done in [52]. Thus, sub-images coming from the same test image share the same labels. Moreover, transfer learning is adopted to solve the problem of lacking labeled data and enhance the prediction accuracy of the network [65], [66].

In blind stereoscopic image quality assessment, it is difficult to predict the MOS value precisely [52]. Therefore, we divide the training stage into three steps: 1) pre-training of encoder-decoder on the pristine and distorted 2D images; 2) pre-training ResNet-18 regression on the pristine and distorted 2D images; 3) joint optimization on the 3D IQA database.

Firstly, encoder-decoder is trained to minimize the difference between predicted and input images which is described in Section II B. Secondly, we utilize the original and distorted 2D images along with the associated MOS scores to pre-train the ResNet-18 regression network. It is aimed to map the 2D image into a quality score. In addition, ResNet-18 with pre-trained weight on ImageNet is adopted for better initialization.

Finally, the Siamese encoder-decoder and quality regression module are jointly optimized using stereo image pairs. Since the ultimate purpose of PAD-Net is to estimate the perceptual

quality of 3D images, we adopt the l_2 -norm between the subjective MOS value q_{3d} and predicted score \hat{q}_{3d} as loss function:

$$l = \frac{1}{K} \sum_k (q_{3d}^{(k)} - \hat{q}_{3d}^{(k)})^2, \quad (12)$$

$$\hat{q}_{3d}^{(k)} = f(\mathbf{I}_l^{(k)}, \mathbf{I}_r^{(k)}; \mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3), \quad (13)$$

where $\mathbf{I}_l^{(k)}$ and $\mathbf{I}_r^{(k)}$ represent the input 3D sub-image pairs. f indicates the PAD-Net with encoder-decoder weight \mathbf{w}_1 , ResNet-18 regression weight \mathbf{w}_2 and weight \mathbf{w}_3 training from scratch. At the joint optimization step, $(\mathbf{w}_1, \mathbf{w}_2)$ are initialized with pre-trained weight $(\mathbf{w}'_1, \mathbf{w}'_2)$ and updated with \mathbf{w}_3 through final loss minimization:

$$\mathbf{w}_1^*, \mathbf{w}_2^*, \mathbf{w}_3^* = \arg \min_{\mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3} l_3. \quad (14)$$

In the testing stage, the stereo image is divided into sub-image pairs with a stride of U to cover the whole content. The predicted qualities of all sub-image pairs are averaged to compute the final perceptual quality score.

IV. EXPERIMENTAL RESULTS AND ANALYSIS

In this section, we first introduce the databases and performance measures used in our experiment. Then, the experimental results of the proposed PAD-Net on the entire LIVE databases and individual distortion type are illustrated. Meanwhile, the visualization results are provided for better explanation. Finally, we conduct the ablation study to verify the effectiveness of each component in our model and measure the computation complexity.

A. Databases and Performance Measures

Three benchmark stereoscopic image quality assessment databases are used in our experiment including LIVE Phase I [55], LIVE Phase II [19], [27] and Waterloo IVC Phase I [37].

LIVE Phase I [55]: This database contains 20 original and 365 symmetrically distorted stereo image pairs. Five distortion types are included in this database, namely JPEG2000 compression (JP2K), JPEG compression (JPEG), additive white noise (WN), Gaussian blur (BLUR) and Raleigh fast fading channel distortion (FF). Subjective differential mean opinion score (DMOS) is provided for each degraded stereo image. Higher DMOS value means lower visual quality.

LIVE Phase II [19], [27]: It includes 120 symmetrically and 240 asymmetrically distorted stereopairs derived from 8 reference images. This database contains the same distortion types as LIVE Phase I. For each distortion type, the pristine image pair is degraded to 3 symmetrically and 6 asymmetrically image pairs. Subjective scores are also recorded in the form of DMOS.

Waterloo IVC Phase I [37]: This database originates from 6 pristine stereoscopic image pairs. The reference image is altered by three types of distortions, namely WN, BLUR, and JPEG. Altogether, there are totally 78 symmetrically and 252 asymmetrically distorted stereopairs. Subjective mean opinion score (MOS) and individual scores are provided for each

stereoscopic image in this database, while higher MOS value means better visual quality.

Performance Measure: Three commonly used criteria [67] are utilized in our experiment for performance evaluation, including Spearman's rank order correlation coefficient (SROCC), Pearson's linear correlation coefficient (PLCC) and root mean squared error (RMSE). SROCC is a non-parametric measure and independent of monotonic mapping. PLCC and RMSE evaluate the prediction accuracy. Higher SROCC, PLCC and lower RMSE indicate better correlation with human judgements. Before calculating PLCC and RMSE, a five-parameter logistic function [54] is applied to maximize the correlation between subjective ratings and objective metrics.

One of the main issues of PLCC and SROCC is that they neglect the uncertainty of the subjective scores [68]. Thus, we also employ the Krasula methodology [68], which could be used to better assess the capabilities of objective metrics by considering the statistical significance of the subjective scores and getting rid of the mapping functions.

The basic idea of this model is to determine the reliability of objective models by checking whether they are capable of well 1) distinguishing the significantly different stimuli from the similar ones, and 2) indicating whether one stimulus are of better/worse quality than the other. To this end, in the Krasula framework, pairs of stimuli are selected from the database to compute the area under ROC curve of the Different vs. Similar category (AUC-DS), area under ROC curve of the Better vs. Worse category (AUC-BW), and percentage of correct classification (CC). Higher AUC-DS and AUC-BW mean more capability to indicate different/similar and better/worse pairs. Higher CC represents better prediction accuracy. Please refer to [68] for more details.

B. Performance Evaluation

In the experiment, the distorted stereo pairs are randomly split into 80% training set and 20% testing set according to [31]. We adopt the Adam algorithm in the pre-training and joint optimization step. During pre-training, the learning rate α is set as 10^{-4} and lowered by a factor of 10 every 50 epochs. The pre-trained weights are obtained after 100 epochs. Since encoder-decoder should retain its function, the learning rate α_1 for encoder-decoder weight \mathbf{w}_1 is set as 10^{-5} to avoid drastic change when conducting joint optimization. Moreover, the learning rate α_2 for ResNet-18 regression \mathbf{w}_2 is set as half of α_3 for \mathbf{w}_3 . α_3 is initialized as 10^{-3} and scaled by 0.25 every 50 epochs. The learning rate remains unchanged after 200 epochs. We apply data augmentation by randomly cropping, horizontal and vertical flipping in the training stage [69]. The results are obtained after 300 epochs. During testing, the stride U is set as 192 for width and 104 for height in a slight overlapping manner to cover the whole resolution in LIVE databases as shown in Fig. 4.

We compare the proposed PAD-Net with several classic FR, RR and NR SIQA metrics on the LIVE Phase I and II database. The competing FR and RR models include Gorley's method [18], You's method [17], Benoit's method [16], Lin's method [20], Cyclopean MS-SSIM [19], RR-BPI [22], RR-RDCT



Fig. 4: Crop in a slight overlapping manner during the testing stage.

TABLE IV: OVERALL PERFORMANCE COMPARISON ON LIVE PHASE I AND PHASE II DATABASES. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Type	Metrics	LIVE Phase I			LIVE Phase II		
		SROCC	PLCC	RMSE	SROCC	PLCC	RMSE
FR	Gorley [18]	0.142	0.451	14.635	0.146	0.515	9.675
	You [17]	0.878	0.881	7.746	0.786	0.800	6.772
	Benoit [16]	0.899	0.902	7.061	0.728	0.748	7.490
	Lin [20]	0.856	0.784	-	0.638	0.642	-
	Cyclopean MS-SSIM [19]	0.916	0.917	6.533	0.889	0.900	4.987
RR	RR-BPI [22]	-	-	-	0.867	0.915	4.409
	RR-RDCT [23]	0.905	0.906	6.954	0.809	0.843	6.069
	Ma [24]	0.929	0.930	6.024	0.918	0.921	4.390
NR	Akhter [25]	0.383	0.626	14.827	0.543	0.568	9.294
	Sazzad [26]	0.624	0.624	-	0.648	0.669	-
	Chen [27]	0.891	0.895	7.247	0.880	0.895	5.102
	S3D-BLINQ [28]	-	-	-	0.905	0.913	4.657
	Shao [11]	0.945	0.957	-	0.911	0.927	-
	CNN [70]	0.896	0.933	5.948	0.633	0.634	8.632
	DNR-S3DIQE [29]	0.935	0.943	-	0.871	0.863	-
	DBN [30]	0.944	0.956	4.917	0.921	0.934	4.005
	DECOSINE [35]	0.953	0.962	-	0.941	0.950	-
	StereoQA-Net [31]	0.965	0.973	4.711	0.947	0.957	3.270
	Proposed PAD-Net	0.973	0.975	3.514	0.967	0.975	2.446

[23] and Ma’s method [24]. For NR metrics, some hand-crafted features based algorithms including Akhter’s method [25], Sazzad’s method [26], Chen’s method [27], S3D-BLINQ [28], DECOSINE [35] and deep neural network based models including Shao’s method [11], CNN [70], DNR-S3DIQE [29], DBN [30], StereoQA-Net [31] are considered in the performance comparison. Note that CNN [70] is computed for left and right view images separately and then average the scores for both views. The SROCC, PLCC and RMSE performance for the above metrics and proposed PAD-Net are listed in Table IV where the best results are highlighted in bold. It could be observed from the table that the proposed method outperforms state-of-the-art SIQA metrics, especially on LIVE Phase II database. Since there are more asymmetrically distorted images in LIVE II, the proposed PAD-Net is more effective for the challenging asymmetric distortion which will be explained in Section III C.

To employ the Krasula methodology [68], significance analysis of the subjective scores are required. Among the three considered 3D IQA databases [19], [27], [37], [55], only the Waterloo IVC Phase I [37] is equipped with individual scores. Furthermore, the excusable/source code of most of the state-of-the-art NR 3D metrics are not released. Therefore, we could only conduct the Krasula analysis on the Waterloo IVC Phase I dataset and compare the proposed PAD-Net with StereoQA-Net [31], which obtains the best performance on both LIVE Phase I [55] and LIVE Phase II [19], [27] databases. Table V lists the results of SROCC, PLCC, RMSE and Krasula performance evaluation, it can be observed from the table

TABLE V: SROCC, PLCC, RMSE AND KRASULA PERFORMANCE EVALUATION ON THE WATERLOO IVC PHASE I DATABASE. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Metrics	SROCC	PLCC	RMSE
StereoQA-Net	0.955	0.970	4.350
Proposed PAD-Net	0.974	0.979	3.696
Metrics	AUC_DS	AUC_BW	CC
StereoQA-Net	0.894	0.998	0.979
Proposed PAD-Net	0.925	0.999	0.993

that the proposed PAD-Net achieve the best performance in terms of SROCC, PLCC, RMSE, AUC-DS, AUC-BW and CC. The results of Krasula performance criteria demonstrate that PAD-Net is the most promising metric in distinguishing stereo images with different qualities.

TABLE VI: RESULTS OF THE T-TEST ON THE LIVE PHASE I AND PHASE II DATABASE.

LIVE Phase I / II	Cyclopean MS-SSIM [19]	CNN [70]	StereoQA-Net [31]	Proposed PAD-Net
Cyclopean MS-SSIM [19]	0 / 0	-1 / 1	-1 / -1	-1 / -1
CNN [70]	1 / -1	0 / 0	-1 / -1	-1 / -1
StereoQA-Net [31]	1 / 1	1 / 1	0 / 0	-1 / -1
Proposed PAD-Net	1 / 1	1 / 1	1 / 1	0 / 0

Moreover, we conduct significance t-tests using the PLCC values of 10 runs [29] to verify whether our proposed model is statistically better than other metrics. Table VI list the results of t-tests on LIVE Phase I and II where 1 or -1 indicate that the metric in the row is statistically superior or worse than the competitive metric in the column. The number 0 means that the two metrics are statistically indistinguishable. From Table VI, we can see that our proposed metric is statistically better than other metrics both on LIVE Phase I and II.

C. Performance Evaluation for Symmetric/Asymmetric Distortion

Our proposed PAD-Net is based on the predictive coding theory and applies deep neural networks to model binocular rivalry mechanism for better prediction of the stereo image quality. Binocular rivalry seldom happens in symmetrical distortion but plays an important role in asymmetrically distorted

TABLE VII: SROCC PERFORMANCE FOR SYMMETRICALLY AND ASYMMETRICALLY DISTORTED IMAGE PAIRS ON LIVE PHASE II AND WATERLOO IVC PHASE I DATABASES.

Type	Metrics	LIVE Phase II		Waterloo IVC Phase I	
		Symmetric	Asymmetric	Symmetric	Asymmetric
FR	Gorley [18]	0.383	0.056	0.566	0.475
	You [17]	0.914	0.701	0.752	0.571
	Benoit [16]	0.860	0.671	0.728	0.577
	Lin [20]	0.605	0.668	0.688	0.592
	Cyclopean MS-SSIM [19]	0.923	0.842	0.924	0.643
NR	Akhter [25]	0.420	0.517	-	-
	Chen [27]	0.918	0.834	0.934	0.907
	CNN [70]	0.590	0.633	-	-
	S3D-BLINQ [28]	0.937	0.849	-	-
	StereoQA-Net [31]	0.979	0.927	0.957	0.940
	Proposed PAD-Net	0.982	0.954	0.985	0.978

image quality assessment. Table VII presents the SROCC performance for symmetrically and asymmetrically distorted images in LIVE Phase II and Waterloo IVC Phase I databases. PAD-Net demonstrates the extraordinary ability to predict the perceived quality of asymmetrically distorted stereo pairs by well mimicking the visual mechanism in binocular rivalry.

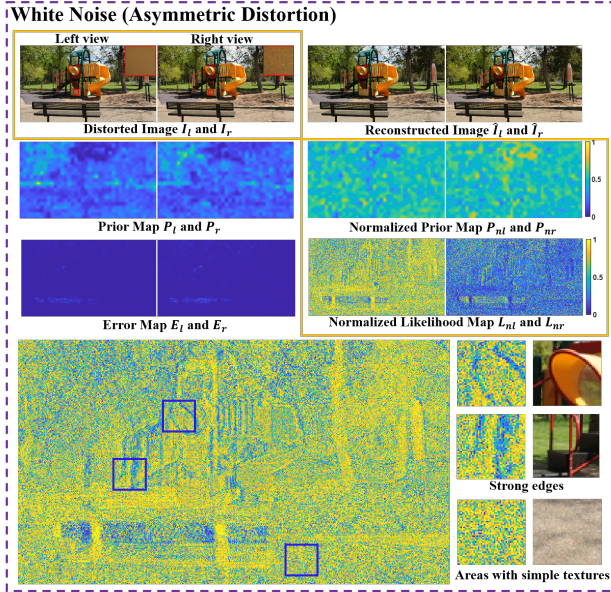
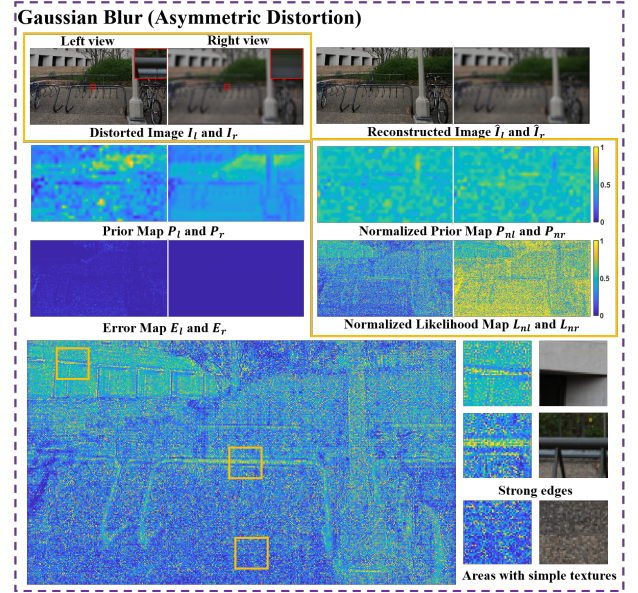


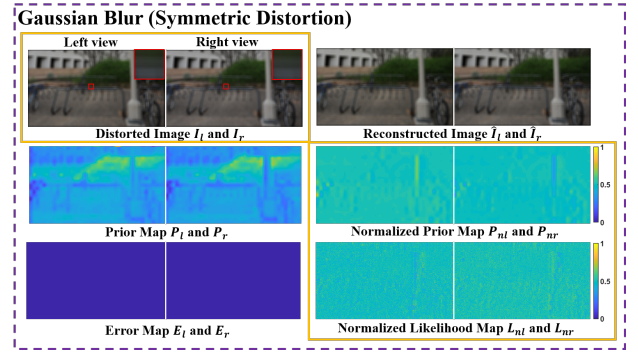
Fig. 5: Visualization results for asymmetrically distorted image in LIVE II database. The left view is undamaged and the right view is distorted with white noise. The bottom is the magnified likelihood map for left view. The higher the value (from blue to yellow) is, the larger the probability. Images inside yellow boxes are fed into the quality regression network.

We provide some visualization results of the PAD-Net for better explanation. In Fig. 5, the left view is undamaged while the right view is degraded with white noise. The reconstructed stereo pairs are similar to the inputs. In the normalized prior and likelihood map, lighter color indicates higher probability. For asymmetrically noised image, the view with heavier noise is harder to be reconstructed thus having lower likelihood probability globally. *However, at the strong edges that indicate structural information, the undamaged view may be allocated smaller probability as shown in the magnified likelihood map of Fig. 5.* Moreover, the discrepancy between normalized left and right view prior maps is not significant since we can still recognize the scene for both views. *According to [37], 3D image quality is more affected by the poor-quality view for noise contamination, as reflected by the magnified likelihood map of Fig. 5, this tendency appears around regions containing obvious edges which means subjective rating is more affected by structural information [1], [19].*

Fig. 6(a) presents the asymmetrically blurred image, the left view is undamaged while the right view is blurred. Contrary to white noise, the view with heavier blurring effect is easier to reconstruct thus having larger likelihood probability. *In addition, strong edges in the undistorted view tend to gain more probability in binocular rivalry as indicated in the*



(a) The left view is undamaged and the right view is blurred. The bottom is the magnified likelihood map for left view.



(b) The left and right view images are symmetrically blurred.

Fig. 6: Visualization results for asymmetrically/symmetrically distorted images in LIVE II database. The higher the value (from blue to yellow) is, the larger the probability. Images inside yellow boxes are fed into the quality regression network.

magnified likelihood map of Fig. 6(b). For the same reason that both views are comprehensible, the normalized prior maps do not show significant differences. *For image blur, it is reported in [37], [71] that 3D image quality is more affected by the high-quality view. In the magnified likelihood map of Fig. 6(b), strong edges in high-quality view have higher probability, which again demonstrates that subjective judgments are more affected by structural information. [1], [19]* In Fig. 6(b), the stereo pairs are symmetrically distorted. As a result, the normalized prior and likelihood maps for both views share similar probability.

Besides, the fusion maps of distorted images, normalized prior and likelihood from left and right views are depicted in Fig. 7. The colors of fusion map for symmetrically and asymmetrically distorted images are easy to be distinguished. The color of the fusion maps for symmetrically distorted image is gray tone, while asymmetrically distorted images

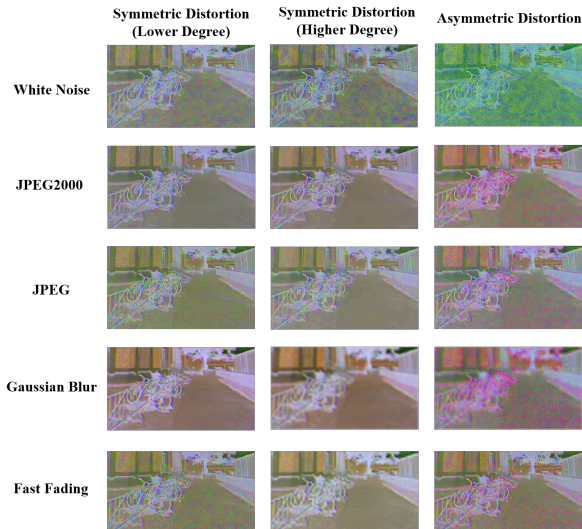


Fig. 7: Fusion maps for symmetrically and asymmetrically degraded stereo images under various distortion types.

appear green or pink. It is caused by the different probability for left and right view images during fusion. Moreover, for asymmetrically distorted images, white noise is different from the other four distortion types since noise tends to introduce high-frequency information while the other four distortion types are apt to remove details that correspond to high-frequency information.

D. Performance Evaluation on Individual Distortion Type

We further investigate the capacity of our proposed PAD-Net for each distortion type, the SROCC and PLCC performance are illustrated in Table VIII and IX. The best performing results across listed metrics are highlighted in boldface. As shown in Table VIII and IX, our proposed model achieves competitive performance for most of the distortion

types. In addition, the scatter plots of DMOS values versus objective scores predicted by PAD-Net for each distortion type on LIVE Phase I and II are presented in Fig. 8(a) and 8(b). The linear correlation between DMOS values and predicted scores demonstrates the great monotonicity and accuracy of PAD-Net. DMOS value range of JPEG compressed images is roughly narrower than those of other distortion types, making it more difficult to estimate the perceptual image quality. Thus, the PLCC and SROCC performance for JPEG distortion is generally lower than the other four.

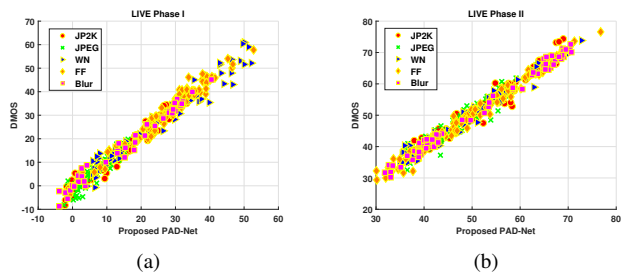


Fig. 8: Scatter plots of DMOS values against predictions by PAD-Net for individual distortion type on (a) LIVE Phase I and (b) LIVE Phase II.

E. Cross Database Tests

We conduct cross database tests to verify the generalization ability of our proposed PAD-Net. Models to be compared are trained on one database and tested on another. Table X presents the PLCC performance for cross database validation. Although PAD-Net does not show the best performance when trained on LIVE Phase II and tested on LIVE Phase I, it outperforms other metrics in the second round which is a more challenging task. Since LIVE Phase I only consists of symmetrical distortion while more than half of the 3D pairs in LIVE Phase II are asymmetrically distorted. PAD-Net trained

TABLE VIII: SROCC PERFORMANCE COMPARISON FOR INDIVIDUAL DISTORTION TYPE ON LIVE PHASE I AND PHASE II DATABASES. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Type	Metrics	LIVE Phase I					LIVE Phase II				
		JP2K	JPEG	WN	BLUR	FF	JP2K	JPEG	WN	BLUR	FF
FR	Gorley [18]	0.015	0.569	0.741	0.750	0.366	0.110	0.027	0.875	0.770	0.601
	You [17]	0.860	0.439	0.940	0.882	0.588	0.894	0.795	0.909	0.813	0.891
	Benoit [16]	0.910	0.603	0.930	0.931	0.699	0.751	0.867	0.923	0.455	0.773
	Lin [20]	0.839	0.207	0.928	0.935	0.658	0.718	0.613	0.907	0.711	0.701
	Cyclopean MS-SSIM [19]	0.888	0.530	0.948	0.925	0.707	0.814	0.843	0.940	0.908	0.884
RR	RR-BPI [22]	-	-	-	-	-	0.776	0.736	0.904	0.871	0.854
	RR-RDCT [23]	0.887	0.616	0.912	0.879	0.696	0.879	0.737	0.732	0.876	0.895
	Ma [24]	0.907	0.660	0.928	0.921	0.792	0.868	0.791	0.954	0.923	0.944
NR	Akhter [25]	0.866	0.675	0.914	0.555	0.640	0.724	0.649	0.714	0.682	0.559
	Sazzad [26]	0.721	0.526	0.807	0.597	0.705	0.625	0.479	0.647	0.775	0.725
	Chen [27]	0.863	0.617	0.919	0.878	0.652	0.867	0.867	0.950	0.900	0.933
	S3D-BLINQ [28]	-	-	-	-	-	0.845	0.818	0.946	0.903	0.899
	CNN [70]	0.857	0.477	0.874	0.782	0.670	0.660	0.598	0.769	0.317	0.476
	DNR-S3DIQE [29]	0.885	0.765	0.921	0.930	0.944	0.853	0.822	0.833	0.889	0.878
	DBN [30]	0.897	0.768	0.929	0.917	0.685	0.859	0.806	0.864	0.834	0.877
	StereoQA-Net [31]	0.961	0.912	0.965	0.855	0.917	0.874	0.747	0.942	0.600	0.951
	Proposed PAD-Net	0.969	0.889	0.968	0.917	0.996	0.959	0.882	0.962	0.867	0.945

TABLE IX: PLCC PERFORMANCE COMPARISON FOR INDIVIDUAL DISTORTION TYPE ON LIVE PHASE I AND PHASE II DATABASES. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Type	Metrics	LIVE Phase I					LIVE Phase II				
		JP2K	JPEG	WN	BLUR	FF	JP2K	JPEG	WN	BLUR	FF
FR	Gorley [18]	0.485	0.312	0.796	0.852	0.364	0.372	0.322	0.874	0.934	0.706
	You [17]	0.877	0.487	0.941	0.919	0.730	0.905	0.830	0.912	0.784	0.915
	Benoit [16]	0.939	0.640	0.925	0.948	0.747	0.784	0.853	0.926	0.535	0.807
	Lin [20]	0.799	0.196	0.925	0.811	0.700	0.744	0.583	0.909	0.671	0.699
	Cyclopean MS-SSIM [19]	0.912	0.603	0.942	0.942	0.776	0.834	0.862	0.957	0.963	0.901
RR	RR-BPI [22]	-	-	-	-	-	0.858	0.871	0.891	0.981	0.925
	RR-RDCT [23]	0.918	0.722	0.913	0.925	0.807	0.897	0.748	0.810	0.969	0.910
	Ma [24]	0.940	0.720	0.935	0.936	0.843	0.880	0.765	0.932	0.913	0.906
NR	Akhter [25]	0.905	0.729	0.904	0.617	0.503	0.776	0.786	0.722	0.795	0.674
	Sazzad [26]	0.774	0.565	0.803	0.628	0.694	0.645	0.531	0.657	0.721	0.727
	Chen [27]	0.907	0.695	0.917	0.917	0.735	0.899	0.901	0.947	0.941	0.932
	S3D-BLINQ [28]	-	-	-	-	-	0.847	0.888	0.953	0.968	0.944
	CNN [70]	0.956	0.630	0.983	0.862	0.846	0.685	0.567	0.855	0.455	0.662
	DNR-S3DIQE [29]	0.913	0.767	0.910	0.950	0.954	0.865	0.821	0.836	0.934	0.915
	DBN [30]	0.942	0.824	0.954	0.963	0.789	0.886	0.867	0.887	0.988	0.916
	StereoQA-Net [31]	0.988	0.916	0.988	0.974	0.965	0.905	0.933	0.972	0.955	0.994
	Proposed PAD-Net	0.982	0.919	0.978	0.985	0.994	0.981	0.898	0.973	0.997	0.986

on LIVE Phase I is able to handle the asymmetrical distortion in LIVE Phase II never met before. The PLCC performance on LIVE Phase II not only proves the generalization and robustness of PAD-Net but also demonstrates the effectiveness of the binocular rivalry mechanism based on predictive coding theory for asymmetric distortion in the proposed method.

TABLE X: PLCC PERFORMANCE OF CROSS DATABASE RESULTS. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Metrics	Train LIVE II/Test LIVE I	Train LIVE I/Test LIVE II
Shao [11]	0.894	0.779
Chen [27]	0.865	-
CNN [70]	0.713	0.656
DBN [30]	0.869	0.852
DECOSINE [35]	0.916	0.846
StereoQA-Net [31]	0.932	0.710
Proposed PAD-Net	0.915	0.854

F. Effects of Network Structure

To explore the influence of different network structures as quality regression network, VGG-16 [33], ResNet-18, 34 and 50 [34] are adopted to make comparisons. The SROCC, PLCC and RMSE performance on LIVE Phase I and II are reported in Table XI. Firstly, ResNet has superior capability to extract discriminative features for quality prediction than VGG structure. Moreover, with the increased depth of ResNet, the performance does not improve. The possible explanation is that the limited training data requires shallow architecture. Generally, very deep networks need a huge amount of training data to achieve high performance. However, there are only hundreds of distorted images in LIVE Phase I and II, even with data augmentation, it is far from enough for deeper networks. Lack of training data may cause over-fitting problems for deeper neural networks. As a result, ResNet-18 is chosen in this paper to reach better tradeoff.

TABLE XI: PERFORMANCE EVALUATION OF DIFFERENT STRUCTURE AS QUALITY REGRESSION NETWORK. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Regression Structure	LIVE Phase I			LIVE Phase II		
	SROCC	PLCC	RMSE	SROCC	PLCC	RMSE
VGG-16	0.913	0.924	5.945	0.858	0.869	5.506
ResNet-18	0.973	0.975	3.514	0.967	0.975	2.446
ResNet-34	0.970	0.974	3.537	0.960	0.961	2.871
ResNet-50	0.968	0.974	3.588	0.963	0.965	2.727

G. Ablation Study

Furthermore, ablation study is conducted to verify the effectiveness of each component in PAD-Net. We first feed the distorted left and right view images into quality regression module as the baseline. Then, normalized likelihood and prior maps are introduced to provide additive information for computing rivalry dominance of both views. Moreover, we compare different fusion methods.

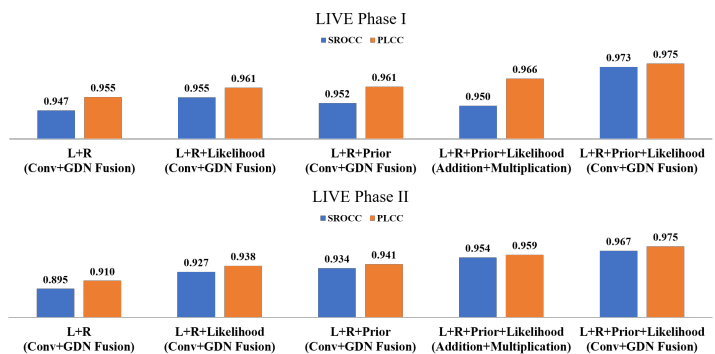


Fig. 9: Ablation Study on LIVE Phase I and Phase II Databases.

As shown in Fig. 9, simply fusing left and right views can achieve promising performance on LIVE Phase I which

only consists of symmetrically distorted pairs. However, the performance degrades seriously on LIVE Phase II owing to the existence of asymmetric distortion. According to the BRM-PC, prior and likelihood probability maps are necessary for 3D image quality estimation. The performance improvement on LIVE Phase II verify the effectiveness of prior and likelihood probability maps obtained through Siamese Encoder-decoder network and further demonstrate the superiority of the HVS guided binocular rivalry mechanism based on predictive coding theory. In addition, we compare the Conv+GDN fusion method with the intuitive addition+multiplication method which denotes we obtain the posterior probability by multiplying prior and likelihood probabilities. Note that Conv+GDN fusion means $GDN(Conv(Concat(\mathbf{P}_{nl}, \mathbf{L}_{nl}, \mathbf{I}_l, \mathbf{P}_{nr}, \mathbf{L}_{nr}, \mathbf{I}_r)))$ and Addition+Multiplication represents $\mathbf{P}_{nl} \times \mathbf{L}_{nl} \times \mathbf{I}_l + \mathbf{P}_{nr} \times \mathbf{L}_{nr} \times \mathbf{I}_r$. It is shown in Fig. 9 that our proposed method benefits a lot from the Conv+GDN fusion method since the parameters of fusion operation are updated during the training stage to generate the most discriminative feature maps for quality prediction. Therefore, the HVS guided Siamese encoder-decoder module to generate prior and likelihood map and the Conv+GDN fusion method are keys to the success of PAD-Net.

H. Computation Complexity

A good metric for blind SIQA should have high prediction accuracy as well as low computational cost. In the experiment, the models are tested on the NVIDIA GTX 1080ti GPU with 11GB memory. The running time for our proposed PAD-Net and other metrics are listed in Table XII. Note that we record the time for predicting quality scores of 50 stereo images with the resolution of 360×640 and then average to obtain the time for each 3D image. The results in Table XII show that PAD-Net only needs around 0.906 seconds per image which is significantly lower than other metrics.

TABLE XII: THE COMPUTATION TIME ON NVIDIA GTX 1080TI GPU. THE BEST PERFORMING RESULTS ARE HIGHLIGHTED IN BOLD.

Metrics	CNN [70]	StereoQA-Net [31]	Proposed PAD-Net
Time(sec)	8.308	2.377	0.906

V. CONCLUSIONS

In this paper, we explore a novel deep learning approach for blind stereoscopic image quality assessment according to the binocular rivalry mechanism based on predictive coding theory. Our proposed predictive auto-encoding network is an end-to-end architecture inspired by the human brain cognition process. Specifically, we adopt the Siamese encoder-decoder module to reconstruct binocular counterparts and generate the corresponding likelihood as well as prior maps. Moreover, we incorporate the quality regression module to obtain the final estimated perceptual quality score. The experimental results demonstrate that our proposed PAD-Net correlates well

with subjective ratings. In addition, the proposed method outperforms state-of-the-art algorithms for distorted stereoscopic images under a variety of distortion types, especially for those with asymmetric distortions. Furthermore, we also show that the proposed PAD-Net has a promising generalization ability and can achieve lower time complexity. In future work, we intend to extend the method to blind stereoscopic video quality assessment. Except for image visual quality, we plan to investigate other 3D quality dimensions such as depth perception and visual comfort.

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