A STATISTICAL APPROACH TO VIEW SYNTHESIS

by

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ABSTRACT

 View Synthesis is the challenging problem of predicting a new view or pose of an object given an exemplar view or set of views. This thesis presents a novel approach for the problem of view synthesis. The proposed method uses global features rather than local geometry to achieve an effect similar to that of the well known view morphing method **[\[1\]](#page-63-0)**.

 While previous approaches to the view synthesis problem have shown impressive results, they are highly dependent on being able to solve for epipolar geometry and therefore have a very precise correspondence between reference images. In cases where this is not possible such as noisy data, low contrast data, or long wave infrared data an alternative approach is desirable.

 Here two problems will be considered. The proposed view synthesis method will be used to synthesis new views given a set of reference views. Additionally the algorithm will be extended to synthesis new lighting conditions and thermal signatures. Finally the algorithm will be applied toward enhancing the ATR problem by creating additional training data to increase the likelihood of detection and classification.

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I dedicate this work to all of my family and friends that continued to support me throughout the last two years even though I was largely unavailable in many ways while working on my graduate degree.

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LIST OF ACRONYMS

ATR CAD EO IBR IR KL LLS MACH MMSE PCA PSR RANSAC SIFT SNR SVM Automatic Target Recognition Computer Aided Design Electro-Optic Image Based Rendering Infrared Karhunen Loeve Linear Least Squares Maximum Average Correlation Height Minimum Mean Squared Error Principle Component Analysis Peak to Side Lobe Ration Random Sample Consensus Scale Invariant Feature Transform Signal to Noise Ratio Support Vector Machine

CHAPTER ONE: INTRODUCTION

Previous Work

 In many pattern recognition applications, it becomes necessary to predict the shape or appearance of an object from several views. It is imperative to estimate new views of an object under varying imaging conditions, such as when there are changes in lighting and thermal levels, or when the viewing geometry has shifted. Specifically, the goal is to estimate a singular view of the object consistent with any imaging conditions present in the reference view. For example, an object that has already been examined for training data in several ways could potentially yield new data in subsequent observations. In IR, the thermal condition of the new exemplar of an existing object could be drastically different from the training data, requiring views from the new condition to be estimated. Similarly in visible images, conditions in illumination could alter the appearance of the object to such a degree that standard classification algorithms would have difficulty recognizing it. In this case, the new illumination condition would also need to be estimated.

Problem Statement

 Of course many methods have been proposed in attempts to address these types of challenging problems before. In the most general case where prior information about the object is unavailable, conventional approaches may extract edges and employ wire frame

models. These tactics geometrically manipulate the data in a 3D sense. Alternately epipolar geometry could be solved for by first solving precise correspondence between reference images. Once the geometry is known, pre- and post-warping could be used to interpolate synthetic images of a view between the reference views. This is known as view-morphing **[\[1\]](#page-63-0)** and will be further discussed in CHAPTER TWO. This thesis deals with a more bounded problem where is it assumed that the prior knowledge about the object (such as representative views) is available.

 We are concerned with estimating or predicting new views of the same object. This concept is known in general as View Synthesis although specific implementations may take on other names. Previously established methods can work well in many situations. View-morphing for example can create very realistic synthesized views based off of reference images.

 In order to use the traditional approaches, regardless of which implementation is chose, they all seem to require establishing precise correspondence between reference images an initial step. At the time of this thesis the state of the art method of finding this type of accurate correspondence without human interaction was to first use feature point correspondence such as SIFT **[\[11\]](#page-64-0)** followed by a refinement step to remove outlier matches keeping only the most likely correspondences using a method like RANSAC **[\[13\]](#page-64-1)**.

 While this type of technique might be convenient in many types of images, there are several applications where this technique will fail. Such applications would include applications with various amounts of noise present in the data, motion blur present in the

data, low contrast data, and most long wave infrared data. Although manual correspondence could be used to get around this problem, it is not only tedious but in many cases unreliable due to the lack of precision accompanied by manual selection. CHAPTER THREE will examine data types in much detail and show how the ability to accurately discover correspondence in pairs of reference images deteriorates with different types of data.

Overview

 In this thesis we describe a novel approach to the view synthesis problem, one that does not depend at all on image correspondence or epipolar geometry. The approach was motivated by two major considerations. The first consideration is the need for multiview-morphing similar in concept to **[\[18\]](#page-65-0)** for boosting a learning algorithm with the ability to generate high-quality synthesized views which are not stored in the training set. This concept was accomplished using a modified view-morphing technique known as triview-morphing **[\[7\]](#page-63-2)**, however as mentioned prior, it depends on precise correspondence. The IR and noisy data are what is motivating a new approach to that problem. The second consideration is the case where we have images spanning the set of needed views already in the training database. The goal here is to predict views of that object from new thermal or illumination conditions. Therefore looking at the two major considerations for the proposed view-synthesis method, it becomes clear that it would be better suited and more appropriate to restrict the use of this algorithm to applications that are limited by low contrast or damaged data.

 More specifically our approach is able to solve the problem without correspondence and epipolar geometry by treating the problem as a 2-D linear prediction process. As previously mentioned, it is assumed that the representative training views of the desired object are available. The first step is obtaining a basis set representing the training data, which is accomplished in this thesis by computing the Karhunen Loeve (KL) expansion of the data. The training images are represented in terms of their principle components (although other basis representations could be used). Purportedly, using the principle components will constitute a reasonable basis for the unknown views. This assumption implies that there is a certain amount of similarity between the predicted view and the training data. The projections of the training images onto the basis set are treated as features that will be used for estimating the linear predictor. It is well known that the number of principle components may be reduced while still well representing the data. Using fewer principle components allows a predictor to be estimated with less training data. Then given an arbitrary image of the object, its features can be the input for the linear predictor which will estimate the output features of the desired synthesized view. The features can either be reconstructed into an image of this view, or left in feature-space to be classified if the actual image is not required. In addition to creating and using a linear predictor to estimate the appearance of the object from new views, this approach can also effectively estimate new signatures. These signatures can be illuminations or lighting conditions in visible data or could be thermal states in IR data. This effort may be accomplished simply by adding data from multiple signature types and using the new training data to create the basis set and estimate the predictor.

 While the main problem to be solved by this thesis is to synthesize new views and signature types, it is not the only focus. Other literature such as Xiao et al **[\[18\]](#page-65-0)** have used synthesized or morphed views to enhance the performance of Automatic Target Recognition. Since one of the motivations of this thesis was to focus on data that is noisy or low contrast, it seemed natural to try to apply this to the ATR problem; a problem which commonly has IR data or long range-data with noise present. This thesis will use the proposed method of synthesis to enhance completely independent approaches to the ATR problem and show promise.

Organization of the Thesis

 The remainder of the thesis is organized as follows. [CHAPTER TWO:](#page-17-1) will review previous approaches to view synthesis problem along with some intermediate results showing when it can be successfully used as well as when it will not be effective. This will demonstrate the motivation for the proposed method. In addition to reviewing other approaches, it is necessary to review some prerequisite related works that were needed to develop the proposed solution and to run all subsequent experiments. CHAPTER THREE will develop the view-synthesis problem as a prediction process in terms of predicting the principle component-based features. This effect will be evident when a system of linear equations is established by relating the principle component features of different views. A minimum mean square error (MMSE) model can be solved for using well-known regression techniques. This portion will conclude with a demonstration of this model to estimating new views and new signature types.

CHAPTER FOUR contains all of the experiments performed in this thesis. It will show examples of the proposed view-synthesis approach used on data to predict views as well as predict new signature conditions. Additionally there will be an example using the predicted views in an ATR application. Finally CHAPTER FIVE will summarize the thesis making conclusions that compare these experiments performed to other approaches. This section will also discuss future directions and applications for our findings.

CHAPTER TWO: RELATED WORK

 Several disciplines have approaches to solving the Image Based Rendering problem. The two predominant ones are computer graphics and computer science. Each of them has their own associated advantages and disadvantages. It is important to understand the state-of-the-art approaches at some level to better appreciate the work and contribution in this thesis. This chapter will begin by reviewing one of the more popular approaches to View Synthesis, showing some results, and demonstrating the motivation for an alternate solution such as the one proposed. This will be followed by a review of ATR techniques that will be used in later chapters.

View Morphing

View Morphing **[\[1\]](#page-63-0)**, **[\[20\]](#page-65-1)**, **[\[1\]](#page-63-0)** as described by Seitz, is the problem of synthesizing realistic images of a real scene from new virtual camera view points by warping a pair of basis images. The algorithm should be able to produce convincing novel views as long as the constraints are satisfied while being versatile enough to handle change in lighting and non-static scenes. The main constraints being that a reasonable correspondence can be solved for or manually provided such that the epipolar geometry can be recovered. Additionally, only a minimal amount of occlusion may be present or artifacts will be introduced making the synthesized results not very convincing. Finally the object of interest should be rigid between each of the basis images.

The main issues resolved by this method, described in **[\[21\]](#page-65-2)**, are uniqueness, correctness, registration, uncalibrated cameras, and synthesis. *Uniqueness* implies that the each novel viewpoint must be uniquely determined from the basis images. *Correctness* is used to state that the resultant image should be reasonable and convincing as if a real, not virtual camera had seen the object from the new viewpoint. *Registration* of the basis images should be possible as mentioned in the above constraint description. This should be possible without prior knowledge of camera parameters such as position and focal length making them *Uncalibrated Cameras.* Synthesis of images should not only be correct by the above definition of correctness, they should be general enough to work with any object satisfying the aforementioned constraints. Seitz and Dyer describe a generalized 3 step algorithm for solving these issues in **[\[20\]](#page-65-1)**. Below, each of the steps will be described with some intermediate results shown.

Pre-warping

Pre-warping is a term used by Seitz and Dyer to describe the process of finding correspondence between the two basis images, using the correspondence to recover the epipolar geometry, and finally using the epipolar geometry to rectify the images into parallel images with aligned scan lines.

Correspondence

It is important to be able to establish correspondence between the two basis images. Correspondence may either be user provided or automatically recovered. It is

Figure 2-1: **The world coordinate P corresponds to image coordinate p and p'. C and C' represents the camera centers while e and e' represent the epipoles where the epipolar line intersect the baseline.**

ideal to automatically recover the correspondence whenever possible. At the time of this writing, it is widely believed that SIFT **[\[11](#page-64-0)]** provides the state of the art in rotation and illumination invariant feature point detection and description, although other methods such as correlation and Harris-Affine **[\[10\],](#page-64-2) [\[12\],](#page-64-3) [\[23\].](#page-65-3)** The number of accurate correspondences needed to solve for in order to recover the epipolar geometry can be as low as 4 points or higher depending on the algorithm used. Examples of correspondences automatically recovered using SIFT can be seen under various conditions in [Figure 3-5](#page-49-1) and [Figure 3-6.](#page-51-1)

Epipolar Geometry

Epipolar geometry is the geometry of stereo vision. When to different cameras observe the same point in a 3D scene, there are a number of geometric relations that can be made between the 3D point and its projections onto the 2D images. This can be observed in **[Figure 2-1](#page-19-1)**. Corresponding points in the two images can be related by [\(2-1\)](#page-20-1) where p and p' are corresponding points in the basis images, F is the fundamental matrix **[\[24\]](#page-65-4)** which can be computed by several algorithms such as Hartley's 8 point algorithm **[\[14\]](#page-64-4)**. The Fundamental matrix is a 3x3 matrix which represents intrinsic parameters as well as relative translation and rotation. Using the Fundamental matrix, Seitz and Dyer can modify these two basis images such that they become parallel views meaning that their horizontal scan lines are aligned, this process is called rectification.

$$
p^T F p'=0 \tag{2-1}
$$

Rectification

Observing [Figure 2-3](#page-22-1) (a) you can see that middle image is not a realistic view between the outer reference images. This incorrect trajectory exists because when linearly interpolating between two points, interpolation takes place along the most direct

Figure 2-2: **The left image shows a view with the 4 corners of the book indicated with the cross. The right image shows the epipolar lines projected onto a second view from the fundamental matrix between these two images. The points in the left image are mapped to lines in the right image that should intersect the corresponding points.**

points. The solution to this problem is the aforementioned rectification process. Rectification was introduced by Seitz and Dyer **[\[26\]](#page-65-5)**, but has been since been used by Hartley et al **[\[22\]](#page-65-6)**, **[\[27\]](#page-66-0)**. Using rectification, image interpolation can be made to follow gaze direction by aligning the epipolar lines of the two basis images. The resultant rectified images will now have corresponding points located on the same scan lines. This can be observed in [Figure 2-4.](#page-23-1)

Morphing

The effect of rectification is that pairs of conjugate epipolar lines become collinear and parallel to the horizontal axis. This means that corresponding points in the rectified images will be located on the same scan line or some point (\hat{x}, \hat{y}) would have a corresponding point (\hat{x}', \hat{y}) . With the images rectified, linear interpolation along the scan

Figure 2-3: The non-rectified image interpolation problem. (a) Image interpolation without rectification. (b) Image rectification after interpolation.

lines will no produce valid in between views. One possible interpolation method is:

$$
\hat{\Pi}_s = (1 - s)\hat{\Pi}_0 + s\hat{\Pi}_1, \quad 0 < s < 1 \tag{2-2}
$$

where $\hat{\Pi}_0$, $\hat{\Pi}_1$ are rectified basis images, $\hat{\Pi}_s$ is a valid view in between rectified basis images $\hat{\Pi}_0$, $\hat{\Pi}_1$, and s is an interpolation constant defining how far along the gaze path the interpolated image should lie.

Post-warping

The final step of View Morphing is the post warp step. In this step the morphed image is to be transformed back into the original image domain. Sietz and Dyer provide a transform to do this similar the inverse transforms of the rectification transforms used in previous steps, **[\[1\]](#page-63-0)**, **[\[20\]](#page-65-1)**, **[\[26\]](#page-65-5)**. There most likely will not be a point for point transform back to the original image domain leaving holes. These holes can be filled automatically by smoothing and blending or with user interaction.

Figure 2-4: Clockwise starting with upper left image is view 1 with 4 points selected, view 2 with epipolar lines mapped, rectified view 1 showing the same corresponding points, rectified view 2 with horizontal epipolar lines.

Limitations of View Morphing

View Morphing can produce realistic synthetic images from novel view points given a set of basis images as long as the constraints are met. The main limitation of this is that its performance is heavily dependant on a precise epipolar geometry being recovered. The fundamental matrix computation as seen above requires several point correspondence between basis images. When the given basis images have some motion blur or are from a low contrast sensor such as IR, correspondence might be unreliable or

Figure 2-5: Clockwise starting with upper left image is view 1 with 4 points selected, view 2 with epipolar lines mapped, rectified view 1 showing the same corresponding points, rectified view 2 with horizontal epipolar lines.

inaccurate, even with manual correspondence as observed in [Figure 3-5](#page-49-1) and [Figure 3-6.](#page-51-1) With inaccurate correspondence either no solution exists for the fundamental matrix or an unreliable one does. An experiment was run to demonstrate this. [Figure 2-4](#page-23-1) show the projection of point correspondences in one view to epipolar lines in a second view in both the image domain and the rectified domain. Take notice that the epipolar lines intersect where the point correspondences are in the second view. Additionally in the rectified domain, you can observe that corresponding points lie on the same scan line. In [Figure](#page-24-1) [2-5](#page-24-1), some noise and blur was added to the same images from [Figure 2-4.](#page-23-1) A

correspondence procedure was used iteratively with SIFT with RANSAC **[\[13\]](#page-64-1)** to ensure only inlier correspondences were used to solve for the Fundamental matrix. It can be observed that the epipolar lines do not intersect all of the points they were mapped from, and in the rectified domain, not all of the corresponding points occur on the same scan line. This will lead to an incorrect morph since morphing takes place along the scan line in the rectified domain. Due to the impact of blur and noise on the epipolar geometry it should be apparent that an alternate method of creating new views that does not depend on geometry for this type of data. Below [Table 2-1](#page-25-1) shows the impact of deformities on the accuracy of the fundamental matrix. The Samson distance is used to measure accuracy as Gaussian noise and blur are introduced.

Deformity	Sampson Distance
None	0.2735194725
5x5 Gaussian Blur	0.4055758822
10x10 Gaussian Blur	0.6384753291
15x15 Gaussian Blur	2.0534070628
025 Variance Noise	0.5182768764
050 Variance Noise	0.8883337633
.075 Variance Noise	1.1168403824
$5x5$ Blur + .025 Noise	1.2433494125
$5x5$ Blur + .050 Noise	7.2159075410
$5x5$ Blur + .075 Noise	10.1189762729

Table 2-1: Affect of image deformity on accuracy of epipolar geometry

Detection and Classification

While the main focus of this thesis is the proposed View Synthesis algorithm, it is a hope that using this algorithm to create novel observations of an object will improve results from well known ATR frameworks. Two such frameworks were chosen, MACH correlation filters **[\[8\]](#page-63-3)** and Support Vector Machines **[\[28\]](#page-66-1)**. These frameworks will be reviewed and demonstrated below.

Correlation using MACH

The correlation based approach requires no image segmentation as compared to a machine learning classifier due to the fact that it compares the entire image to a template or filter. In general correlation based approached can suffer from the filter deviating even slightly from the target. The maximum average correlation height (MACH) filter used by Mahalanobis et al **[\[8\]](#page-63-3)** is a good choice because it can incorporate a set of images into the filter to allow more variance while maintaining high and sharp peaks. This will give the MACH filter some view and illumination invariance in correlation assuming the right set of images was used in the creation of the filter.

Given a set of training images, the MACH filter is given by:

$$
h = (S + C)^{-1}m
$$
 (2-3)

where *represents the average training image,* $*S*$ *represents the spectral variance of the* data, and *C* is the power spectrum of the background. Performance for the MACH filter is measured in terms of peak to side lobe ratio (PSR) which is defined by:

$$
PSR = \frac{p - \mu}{\sigma} \tag{2-4}
$$

where p represents the maximum value returned from cross correlation between the filter and the test image, and μ and σ represent the mean and standard deviation of the cross correlation respectively. One of the appealing characteristics of the MACH filter was that accounting for some variation between the filter and the test image, cross correlation should still return high sharp peaks. That being the case it is expected that the PSR should be high when an image has qualities similar to the filter and should be low otherwise.

 To demonstrate this, we present an experiment where we will use correlation to detect and classify an alphanumeric character. We will run the experiment twice, once with one exemplar character as the correlation template and a second time using many characters to train a MACH filter. Finally we will compare the resulting correlation maps as well as detection based on the PSR threshold. **[Figure 2-1](#page-19-1)** shows the input for the experiment. Both experiments will share the left image as a test image to try to find all instances of the character 'X". In the first experiment we will use all of the 'X's on the right side to generate a MACH filter, while in the second we will use the single 'X" at the bottom for standard template based correlation.

Figure 2-6: The left side shows a test image. The right hand side is the set of characters to train a MACH filter. The single character will be used for standard template based correlation.

To create the MACH filter the first step was to interpolate all training images to the same size. After that we simply apply the equation seen in [\(2-4\).](#page-27-0) This gives us the MACH filter represented by [Figure 2-7.](#page-28-1) Once we have this filter we can simply use

Figure 2-7: Resultant MACH filter

Figure 2-8: Results for first experiment using MACH filter. The Right shows the correlation map, while the left thresholds PSR to show detection results.

normalized cross correlation as in equation [\(2-5\)](#page-29-1), where *I* is the test image and *h* is the

$$
\frac{1}{n-1}\sum_{x,y}\frac{(I(x,y)-\overline{I})(h(x,y)-\overline{h})}{\sigma_{I}\sigma_{h}}
$$
\n(2-5)

MACH filter. [Figure 2-8](#page-29-2) shows the resulting correlation map on the right. Using equation [\(2-4\)](#page-27-0) on the correlation map we can computer the PSR for every pixel in the correlation map and use this value to threshold detections. The left side shows the detections after applying a threshold. All 'X's were detected. The darker red bounding boxes means that the MACH filter had adjacent pixels with a PSR higher then the threshold. The second part of this experiment was to repeat the process using normalized cross correlation using a single 'X' as the template and compare results. The results for this can be seen in [Figure 2-9](#page-30-1). As expected the filter response was dull compared to the

sharp response in the prior experiment. The same PSR threshold was only able to detect 2 of the $'X$'s.

Figure 2-9: Results for second experiment using a single 'X' as a correlation template. The Right shows the correlation map, while the left thrsholds PSR to show detection results.

Support Vector Machines

In the field of computer vision and machine learning, classification is a challenging and on going problem. In general, classification can be separated into two components, feature extraction and classification. Feature extraction will be taking representative features of an object or class, and using this as an input pattern for a classifier. This overview will focus on just the classifier using raw data as features. At the time of this thesis, one of the most widely used approaches to the classification problem is SVM **[\[28\]](#page-66-1)**. Conceptually SVM can be looked like as a black box that takes in training patterns and outputs a decision surface or model. This process is known as

training. Following training unknown patterns can be presented and compared to this model and assigned a class and confidence based of how it compared to the model. This process is known as testing or classifying.

Theoretically, inside of the black box, SVM is hyperplane classifier which will try to learn a hyperplane that can best separate the input patterns. In the most general case, consider a two class problem that is linearly separable such as in [Figure 2-10.](#page-31-1) In this case an optimal linear boundary can be solved using, for example, the perceptron learning algorithm **[\[31\]](#page-66-2)**.

Two Class Classification Problem

Figure 2-10: Linearly separable two class classification problem.

Figure 2-11: The above figure shows a two class non linearly separable problem in its input space with a decision boundary as an ellipse. The below figure shows the same two class problem mapped two a higher dimensional space where the ellipse decision boundary is now a line.

A kernel, [\(2-6\),](#page-32-1) [\(2-7\),](#page-32-2) is a mapping that will map data into a higher dimensional space or feature space. The lower portion of [Figure 2-11](#page-32-3) demonstrates linear separability in feature space.

$$
\Phi: \mathfrak{R}^N \longrightarrow F \tag{2-6}
$$

$$
k(x, y) = (\Phi(x) \cdot \Phi(y))
$$
\n(2-7)

The specific kernel that is used is application dependent and in some cases must be empirically solved for. Some popular kernels can be seen below

Table 2-2: Types of kernels used in SVM

Polynomial	$k(x, y) = (x \cdot y)^d$	$(2-8)$
Radial Basis Function	$k(x, y) = e^{\frac{- x-y ^2}{2\sigma^2}}$	$(2-9)$
Sigmoid	$k(x, y) = \tanh(k(x \cdot y) + \Theta)$	$(2-10)$

Setting up the decision boundary is very similar to the form of the linear boundary and can be observed in [\(2-11\).](#page-33-1)

.

$$
f(x) = sign(\sum_{i=1}^{e} v_i \cdot k(k, y) + b)
$$
\n(2-11)

For a practical example, we will use SVM to classify handwritten characters 0-9. NIST provides an alphanumeric handwritten database **[**[30](#page-66-3)**]** which contains 7291 16x16 pixel images of characters for benchmarking. A sample of this dataset can be seen in [Figure 2-12](#page-34-1). For this experiment, the total data was divided the data into 2000 characters for training and 5291 characters for testing, with a character histogram as in [Figure 2-13](#page-34-2). The problem was treated as 10 two class problems each with a character as class 1 and the remaining characters as class 2. This results in 10 separate models, one for each character. To run the experiment LibSVM **[\[19\]](#page-65-7)** was chosen due to its being freely available with a well supported Matlab interface. A second degree polynomial kernel was chosen empirically using the grey scale intensity values as features. The results can be observed in [Table 2-3](#page-35-1) and are very reasonable. This well demonstrates the ease and

power of SVM. Features such as PCA could yield better results gray scale were chosen for ease of explanation.

Figure 2-12: A sample of the characters from the NIST handwriting database [\[30\]](#page-66-3)**.**

Figure 2-13: Histogram of characters from training and testing dataset

	Precision	Recall	Accuracy
	0.955828	0.967702	0.995086
	0.978229	0.988270	0.998488
2	0.819521	0.870841	0.987526
3	0.856287	0.842829	0.984880
4	0.850211	0.791749	0.979966
5	0.876993	0.848018	0.986959
6	0.949580	0.907631	0.991306
7	0.929019	0.961123	0.996598
8	0.723150	0.789063	0.984691
9	0.792233	0.857143	0.987148

Table 2-3: Results for SVM character classification

CHAPTER THREE: PROSPOSED VIEW SYNTHESIS METHOD

 One of the main focuses of this thesis is the proposed algorithm for viewsynthesis. This section formulates the algorithm and describes several applications for this method. Since there are other approaches for estimating an object's view from different poses, lighting conditions, or thermal states, we will also discuss when and where it is most appropriate to use the proposed algorithm. Variables such as noise, blur, and the characteristics of imaging sensors will be taken into consideration in the process, and the effect of those variables on the data and resulting prediction will be discussed in detail.

Mathematical Formulation

 It is well known that techniques such as the Karhunen Loeve (KL) decomposition (also known as Principle Component Analysis) can be used to represent data as a linear combination of a set of orthonormal basis functions. The coefficients of linear combinations are readily obtained by projecting the data onto the basis set. We develop a statistical model to characterize the relationship between the coefficients (or features)^{[1](#page-36-1)} associated with different views so that given a new view, the model can estimate the features of other views. We now describe a mathematical formulation for this approach. Basic notation for this section will consist of the following, vectors will have an arrow

¹ The coefficients used for reconstructing the image can be treated as features, as we shall use the term "features" interchangeably with the term "coefficients" in this paper.

above them, for example, vector*b* r . On the other hand, scalars will be italicized but not bold, for example, scalar *s*. Finally, a matrix will be expressed as a capital letter, with an arrow it above such as \vec{M} .

 In the following discussion, we treat images as vectors. Thus, a two dimensional image $\vec{X}(m, n)$ of dimensions $d_1 \times d_2$ is represented by a data vector \vec{x} of dimensions $d = d_1 \cdot d_2$. We express the vector \vec{x} as a linear combination of a set of orthonormal basis vectors \vec{q}_i , $1 \le i \le d$, i.e,

$$
\vec{x} = \sum_{i=1}^{d} a_i \vec{q}_i = \vec{Q}\vec{a}
$$
\n(3-1)

where $\vec{Q} = [\vec{q}_1 \quad \vec{q}_2 \quad \dots \quad \vec{q}_d]$ is a $d \times d$ matrix with basis vectors as its columns. Additionally, the vector $\vec{a} = \begin{bmatrix} a_1 & a_2 & \dots & a_d \end{bmatrix}^T$ is the coefficient (or feature) vector that satisfies:

$$
\vec{a} = \vec{Q}^T \vec{x} \tag{3-2}
$$

It should be noted that we have used the identity stated in [\(3-3\),](#page-38-0) where *I* is the identity matrix, in order to rearrange [\(3-1\)](#page-37-0) as

$$
\vec{Q}^T \vec{Q} = \vec{Q} \vec{Q}^T = I \tag{3-3}
$$

 The KL basis set and other compact representations of the data allow us to approximate \vec{x} using fewer basis sets, i.e, $M \le d$ columns can be included in the definition of *Q* \vec{Q} . It is well known that the KL expansion provides a useful ordering of the basis vectors which minimizes the mean square error for any given choice of *M*.

Let us now consider an image vector \vec{y} that represents another view of the object that differs from the view in \vec{x} . Furthermore, let us assume:

$$
\vec{y} = \sum_{i=1}^{M} b_i \vec{q}_i = \vec{Q}\vec{b}
$$
\n(3-4)

where the vector *b* r is a vector of length M that contains the weights b_i as its elements. The question now becomes, if we are given an image vector \vec{x} (and therefore given \vec{a} from [\(3-2\)](#page-37-1)), can we estimate \vec{b} and hence recover \vec{y} by using [\(3-4\)](#page-38-1)? One simple approach to achieving this would be to postulate that a linear relation exists between \vec{a} and \vec{b} , and that there exists a matrix \vec{A} such that:

Creating a Predictor

 The previous section described a mathematical formulation for estimating the features of one image given the features of another, then recovering the predicted image. It suggested that this is possible by using a linear model or predictor matrix as in [\(3-5\).](#page-39-1) We now describe a method for constructing such a linear model that may be used for relating the images from different viewing angles.

 We begin by assuming that a set of *N* images of the object is available, as in [Figure 3-1](#page-40-1), that can be used to estimate a linear relation between the views that are separated by a fixed increment of Δ° . Let vector \vec{x}_{θ} denote the object at a pose of θ° with respect to the imaging sensor. This image vector would have a corresponding feature vector $\vec{a}_{\theta} = \vec{Q}^T \vec{x}_{\theta}$. Furthermore, let $\vec{x}_{\theta+\Delta}$ represent another view of the object separated by Δ° from \vec{x}_{θ} whose feature vector is given by $\vec{a}_{\theta+\Delta} = \vec{Q}^T \vec{x}_{\theta+\Delta}$.

We now seek a matrix \vec{A}_{Δ} that maps the features of one view to the features of a second view offset from the first view by Δ° , i.e,

$$
\vec{A}_{\Delta}\vec{a}_{\theta} = \vec{a}_{\theta+\Delta} \tag{3-6}
$$

Figure 3-1: Virtual cameras representing multiple views of an object.

Assuming that *M* basis vectors are used to represent the data, it is implied that the linear model A_Δ is a $M \times M$ matrix. It should be observed that by using the features instead of the intensity values of the pixels, the linear model can be represented with dimensions $M \times M$ as opposed to $P \times P$, where P is the total number of pixels in the image. In most cases this results is the linear model being of exponentially lower dimension while still adequately representing the original data. This property will be exploited later in our discussion.

For $N-1$ pairs of images, of which have the same offset by Δ° , we can obtain a system of linear equations given by:

$$
\vec{A}_{\Delta} \begin{bmatrix} \vec{a}_{\theta} & \vec{a}_{\theta+\Delta} & \dots & \vec{a}_{\theta+(N-1)\Delta} \end{bmatrix} = \begin{bmatrix} \vec{a}_{\theta+\Delta} & \vec{a}_{\theta+2\Delta} & \dots & \vec{a}_{\theta+N\Delta} \end{bmatrix}
$$
(3-7)

To simplify the math, each set of feature vectors can be represented in matrix form as shown below:

$$
\vec{F}_x = \begin{bmatrix} \vec{a}_\theta & \vec{a}_{\theta+\Delta} & \dots & \vec{a}_{(N-1)\Delta} \end{bmatrix}
$$
\n
$$
\vec{F}_{x+\Delta} = \begin{bmatrix} \vec{a}_{\theta+\Delta} & \vec{a}_{\theta+2\Delta} & \dots & \vec{a}_{N\Delta} \end{bmatrix}
$$
\n(3-8)

Using the matrix representations in $(3-8)$, a simplified version of $(3-7)$ can be rewritten as seen below:

$$
\vec{A}_{\Delta}\vec{F}_{x} = \vec{F}_{x+\Delta} \tag{3-9}
$$

Looking at the above equation in matrix form, remember that the dimensionality of the linear model \vec{A}_{Δ} is $M \times M$ while the feature matrices \vec{F}_x and $\vec{F}_{x+\Delta}$ are of size $M \times N$ where M is the number of features and N is the number of unique views. For a unique solution to exist for [\(3-9\),](#page-41-1) the condition $N \ge M$ must be true implying that the number of unique views must be larger than the number of features used to represent each individual image. That being the case, it should be apparent and obvious that attempting to solve this system with the intensity values instead of the features obtained from the basis set would be intractable requiring the number of views to be larger than the number of pixels.

 Therefore, by using the features to represent the image, we anticipate that $N \geq M$ is satisfied so that the system may be solved. The minimum mean square error solution for the linear model \vec{A}_{Δ} is given by:

$$
\vec{A}_{\Delta} = \vec{F}_{x+\Delta} \vec{F}_x^T (\vec{F}_x \vec{F}_x^T)^{-1}
$$
\n(3-10)

Novel Views Prediction

 Given a limited amount of two dimensional data from views of an object, consider the problem of estimating new views of the object while maintaining rigidness in a three dimensional space. [Figure 3-2](#page-43-1) helps visualize the problem showing both the set of data as well as predicting a novel view. Although this problem has been previously solved by Seitz et al. **[\[1\]](#page-63-0)** as mentioned earlier, in certain situations (covered more thoroughly in the following sections) the view morphing algorithm will either be impractical to use or will not work. One of the goals of the proposed view synthesis algorithm is to work under such conditions where conventional view morphing is unlikely to succeed.

 In order to predict views using this procedure there are two major steps required, where the first is to construct a linear model. This is fairly straight forward using the technique described in the previous section. Specifically, the data should be arranged as in

Figure 3-2: Estimating a view from an arbitrary image. (a) Displays the set of images used to create a linear model. (b) Displays arbitrary input \vec{x}_{θ} used to predict output view $\vec{x}_{\theta+\Delta}$

[Figure 3-2](#page-43-1) with each view approximately Δ° apart from each other. This data will be used for training to construct the linear model. KL decomposition should be used to construct a basis set representing this data in a significantly lower dimensionality. When choosing dimensionality, it is important to assure that not only the dimensionality be less than or equal to the number of views, but that a sufficient quality of the original image can be recovered from a reduction of that magnitude. [Table 3-1](#page-44-1) shows the type of reduction that can typically be achieved through the described process.

Image Resolution	Number of Pixels	Required Views (no reduction)	\approx Required Views ² (with reduction)
60 80 x	4800	4800	
160 x 120	19200	19200	
320 x 240	76800	76800	13
640 x 480	307200	307200	18

Table 3-1: Comparison of model with principle component reduction vs. no reduction

 With the basis set solved for and the features extracted, a system of equations can be established as in the mathematical formulation which can be used to solve for the linear model. Once the linear model is created it is very simple to estimate a view Δ° apart from any arbitrary view which is the second step. This is observed in [Figure 3-3](#page-45-1) which shows a block diagram that takes an input and yields an estimate of that input rotated by Δ° . Additionally, in the figure we observe that that the prediction can be fed back into the input to generate an estimate of the input rotated by $2\Delta^{\circ}$.

 \overline{a}

 $2²$ The amount of required views were solved for experimentally by compressing an arbitrary number of images of the given resolutions using PCA, and observing the average minimum principle components needed to retain an acceptable representation of the original image.

Figure 3-3: Block diagram of linear prediction with feedback

It should be noted that the prediction process is operated in the feature space. Finally, to get the image back into its original space, the final step is recovery. Recovery is simple and is accomplished by the following: $\vec{x}_{\theta+\Delta} = \vec{Q}^T \vec{a}_{\theta+\Delta}$.

Novel Signature Prediction

 In the previous section, it was discussed how to predict new views. This was possible by arranging the data into a set of linear equations where each image maps to an image offset by an angle of approximately the same amount. Karhunen Loeve decomposition was then used to develop a basis set and restrict the number of principal components such that the number of equations could be reduced and the system could be constrained or over constrained.

 This section extends our concept to estimate not only new views but new signatures as well. We will define signatures as different illumination conditions or the same view in EO sensor data as well as different thermal signatures of the same view in IR sensor data.

[Figure 3-4](#page-47-1) shows an example of what different signatures of the same object at the same view can look like. From these examples it is not difficult to visualize that even if training data exists in a specific object at a specific view, different signatures can make object recognition a challenge. This being the case, it is an interesting problem to predict different views of an object, given a new signature.

 The process for predicting a new signature is very similar to that of predicting a new view with the only difference existing in the creation of the linear model. In order to adequately describe this process a new convention must be established that accounts for signatures. Let the number of apostrophes indicate a signature identifier with a total of 3 signatures in the example. All other notations used will be as described previously. Below we will modify the system described in [\(3-9\)](#page-41-1) to be a more generalized form allowing for a linear model that supports multiple signatures.

Figure 3-4: Comparison of thermal signatures. The columns show 3 different views while the rows represent different thermal states. This figure is intended to illustrate how different the same object at the same view can look from different thermal states.

$$
\vec{A} * \begin{bmatrix} a_1^{1} & a_{1+\Delta}^{1} & a_{1}^{11} & a_{1+\Delta}^{11} & a_{1+\Delta}^{11} & a_{1+\Delta}^{11} & a_{1+\Delta}^{11} \\ a_1^{2} & a_{1+\Delta}^{2} & a_{1}^{2} & a_{1+\Delta}^{2} & a_{1+\Delta}^{2} & a_{1+\Delta}^{2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_1^{P} & a_1^{P} & a_{1+\Delta}^{P} & a_{1+\Delta}^{P}
$$

 The process for creating the general linear predictor that simultaneously handles multiple signatures and views is very similar to the approach described. Once the linear predictor has been solved for which supports multiple signature prediction, it can be used in the same way that the single signature prediction was employed. [Figure 3-2](#page-43-1) shows the views used to create the linear model, and how an arbitrary view is used to predict a new view. Including both signatures and aspect in the estimation process improves (reduces) the condition number of the matrix and leads to a more numerically stable solution.

Sources of Data Degradation

 Previous methods in one way or another are heavily dependent on geometric transformations and perspective principles. In order to adequately achieve this one of the most basic steps is to establish precise correspondence between training images. This is typically done by using a feature point extraction method such as Harris corners **[\[12\]](#page-64-3)** or SIFT interest points **[\[11\]](#page-64-0)**. Following initial correspondence RANSAC **[\[13\]](#page-64-1)** is typically used to remove any outliers and leave the most likely points corresponding in the training images. This correspondence can then be used to solve the fundamental matrix from which geometric transformation will depend on.

 This potentially creates a problem because in order to make convincing geometric transformations, the correspondence must be very precise. This can be difficult depending on that sensor that captured the data, noise present, and several other concerns. The remainder of this chapter will discuss these concerns describing when it would be useful to use an approach to view synthesis that does not depend on establishing correspondence.

Figure 3-5: An example of problem images for automatically finding and refining correspondences. (a) IR image of a truck using SIFT to match correspondences. (b) EO grayscale image of a car using SIFT to match correspondences. (c) IR image with refined correspondences. (d) EO image with refined correspondence.

Sensor Type

 One of the major factors that cause problems for the geometric transform based morphing methods is the sensor type that is used. The two sensor types that are discussed in this thesis are Electro-optic sensors and Infrared sensors. Although there are several types of infrared sensors, we will focus on long wave IR captured at 7-14 microns. Using either of the sensor types can cause registration problems although the difficulty is more likely to occur in IR sensors.

SNR: Its Affect on Synthesis

 In this section, we will focus on noisy data and low contrast data. It is important to understand the limitations of the data to use the best algorithm for the job. [Figure 3-5](#page-49-1) shows an example of two problem images which have difficulty finding correspondences. There are less than 8 correspondences found which is essential for most standard algorithms such as Hartley et al **[\[14\]](#page-64-4)** to compute the fundamental matrix. In order to achieve good geometric transformations, no false positives can be introduced in correspondences, and it is difficult to precisely select additional points by manual techniques.

Noisy Data

 While there are many ways to reduce noise in the data, it is not always convenient to do so. There are several factors that could leave data obtained from both visible and infrared sensors susceptible to noise. One of the most likely candidates for causing noise is having a high exposure index, or simply a legacy digital camera shot without the proper lighting. Of course any digital camera could have noise due to electrical interference.

Figure 3-6: Effects of noise and blur on feature point correspondence. (a) Varying amounts of normally distributed noise and its effect on correspondence. (b) Varying amounts of blur and its effects on correspondence.

Analog imaging sensors are generally less susceptible to noise. The most common source of noise in analog domain is film, whether it is granularity, an accidental exposure, or flaws in the development process. Uncooled long wave IR is particularly susceptible to noise. In [Figure 3-6](#page-51-1) (a), varying amounts of noise is introduced in to two images to show the effect that it can have on finding.

Low Contrast or Blurred Data

 Aside from noise, the blur effect (or low contrast) can also be a problem for image processing. It can have an effect similar to low pass filtering an image, which makes it more difficult to precisely identify edges and other high frequency characteristics in images. There are many factors that introduce blur in images. In electro-optic sensors, factors such as poor focus, camera shake, and motion blur can all create this type of effect In infrared sensors most accept for upper end sensors cannot come close to matching the contrast offered in electro-optic sensors. Similarly to noise present in images, [Figure 3-6](#page-51-1) (b) illustrates the difficulty in finding correspondence with varying amount of blur in the images.

CHAPTER FOUR: EXPERIMENTS & RESULTS

 In order to demonstrate the benefits and affects of the proposed algorithm, several experiments were carried out using multiple datasets. Standard datasets as well as controlled datasets collected in the lab are represented. Experiments were designed to test the functionality of the algorithm on normal data as well as data corrupted by noise and blur. It was also desired to see how varying parameters of the algorithm would affect the learning of the predictor as well as the output of the algorithm. In addition to analysis that test prediction quality, we will attempt to show that synthesis can be used to improve the performance of ATR algorithms. The following section will describe the datasets used throughout this thesis.

Datasets

 Two main datasets were used for the majority of the experiments discussed in this thesis. You can see a subset of the data used for the experiments in [Figure 4-1.](#page-54-1) It was important to have a controlled dataset which could show an object of interest from every possible view for 360 degrees, and hence one of the datasets was collected in the lab. One of the benefits of a controlled dataset is that ground truth is available for every possible experiment, and multiple illumination conditions are available which would not be otherwise.

Figure 4-1: Subsets of the major datasets used in this thesis. (a) Sample of the dataset which was collected in lab. (b) Sample of the well known COIL – 100 dataset. (c) Sample of IR data collected

 Additionally, it is important to show results from a standard database that is publicly available. The COIL – 100 dataset **[\[6\]](#page-63-4)** was chosen for this purpose. It is convenient to use for synthesis because it is comprised of 100 objects divided into categories where each object is shown from 72 different views each having 5 degrees of separation between the views. The only characteristic about the COIL-100 dataset that makes it less than ideal is that the scale of the object varies as the view changes. Unfortunately, this limits the amount of images suitable for our experiments. Additionally, this dataset was used because other view synthesis and morphing publications have used the dataset such as Xiao et al **[\[18\]](#page-65-0)**.

Experiments

Varying the Number of Basis Vectors Used to Create the Predictor

 The purpose of this experiment is to show the affect on prediction quality as a function of the number of basis vectors used to estimate the predictor. The measure of prediction quality is observed by minimizing the mean squared error and maximizing the correlation between the predicted output and the ground truth. Consider equation [\(3-10\)](#page-42-1), where the predictor matrix \vec{A} is a set of coefficients that will predict the principle component features corresponding to the appearance of the input rotated by a constant offset Δ . The number of coefficients in the predictor matrix that need to be estimated is dependent on the number of principle component features chosen to represent the images. This relationship between the number of principle components chosen and the number of coefficients in the predictor is exponential such that if n principle components were chosen, the predictor would be of size n^2 . Intuitively this should imply that since the number of coefficients grow exponentially with the number of principle components chosen, the error in each predicted coefficient should also grow exponentially. This would imply that while choosing too few principle component features might not adequately retain enough of the image to represent it (resulting in poor prediction and appearing heavily smoothed), choosing too many principle component features could cause the error grow exponentially with each coefficient resulting in a noisy prediction.

Figure 4-2: Results from experiment 1. (a) Input image. (b) Ideal output image. (c) Predicted output image using the amount of basis vectors that produced the lowest mean squared error. (d) Predicted output image using the amount of basis vectors producing the highest mean squared error. (g) Plot of the mean squared error as a function of the percentage of available basis vectors used.

 To test this intuition we have chosen an experiment that learns multiple views as well as several illumination conditions. This experiment will vary the number of principle component features used to estimate the predictor. Due to the constraints established in CHAPTER THREE the upper limit for the number of potential principle component features is restricted to the number of views multiplied by the number of signature types or in this case, illumination conditions. [Figure 4-2](#page-56-1) shows the results of this experiment described in this section. Observing the results clearly substantiates the hypothesis that using too few or too many features both result in poor predictions.

Figure 4-3: Results from experiment 2. Column 1 is the input, column 2 is the ideal output, and column 3 is the predicted output. (a) Experiment performed with no corruption. (b) Experiment performed with zero mean and standard deviation of 15 white noise corrupting data. (c) Experiment performed with zero mean and standard deviation of 30 white noise corrupting data. (d) Experiment performed with Gaussian blur with radius of 3 corrupting data. (e) Experiment performed with Gaussian blur with radius of 6 corrupting data.

Prediction Quality as a Function of Added Noise and Blur

 As suggested in previous chapters, one of the primary benefits of using this approach to view-synthesis as compared to previous approaches is in the case of blurry data, noisy data, or data with poor contrast. For this reason it was believed prudent to have an example that could show prediction quality as a function of data corrupted by motion and blur. It should be kept in mind that images with large amounts of this type of corruption cannot have correspondence found by standard methods, making it very

difficult or in some cases impossible to use traditional morphing and synthesis approaches. In this experiment, 4 different synthesis' were performed which included an experiment on data with no corruption, corruption by noise, corruption by blur, and corruption by both noise and blur. The results of this experiment can be seen below in [Figure 4-3](#page-57-1).

Predicting Views from a New Signature Type

 Many computer vision applications use object recognition to compare a new object to some sort of training data in order to classify it for some purpose. In these types of applications, even when a substantial training database exists, it is difficult to adequately capture all possible variations of the object. Changes in signature type for example could alter the appearance of the object in such a way to make it difficult to compare to training data. Of course by signature types this is referring to changes in illumination in visible and changes in thermal state in infrared.

 This experiment is designed to test that the proposed algorithm could effectively learn a model for an object representing its appearance from multiple signatures. Furthermore we will demonstrate that using this learned model, we can predict the appearance of this object from a new signature not present in training data from multiple views.

 For this experiment we use data of the same object from many separate thermal states and used them as training data. We then introduce a new thermal state no in

training and try to predict views from this new thermal state. The setup of the experiment was fairly simple using the training data to construct a basis set. Then, by following equations described in previous chapters such as [\(3-11\)](#page-47-2) an estimate of the predictor is made. With the predictor solved for, any view of the object from the new thermal state can be used as input to estimate views from this new illumination condition. [Figure 4-4](#page-59-1) shows the results for predicting 2 different views. You can see in the predicted outputs that hot spots match for same location as in the ideal output.

Figure 4-4: Results from experiment 3. In each of the two results a view is predicted from a new thermal state. The left column is the input image, the center column is the ideal image, and the right column is the predicted image. (a) Example 1 input is 80 degrees with a predicted output of 20 degrees. (b) Example 2 input is 135 degrees with a predicted output of 75 degrees.

CHAPTER FIVE: CONCLUSION

Summary

 This thesis has introduced a novel approach to view synthesis using linear prediction techniques to estimate the features that represent a synthesized view. We have shown how to use this algorithm to estimate the appearance of new views for an object. Additionally, we have shown how to estimate views of an object in new illumination conditions for visible data and new thermal states for infrared data. All of the constraints are well described indicating when it would be appropriate to use this algorithm for view synthesis and when it a more traditional approach may be better suited.

 In addition to introducing this novel approach and showing results for its synthesis, this thesis also demonstrates how a linear prediction technique can be used to improve the performance of ATR applications. A correlation based approach as well as a machine learning based approach both realized a boost in performance using the proposed algorithm to synthesize images that were not adequately represented by training data.

 While the proposed method for view synthesis is not the only method available, there are several cases where it makes sense to use this approach. It has been well documented that most previous approaches require a solution for the epipolar geometry between the reference images which in turn requires an accurate correspondence between the reference images before it can synthesize new views. We have demonstrated that

when noise, blur, and other corruptions are introduced into data, it is difficult to find accurate correspondences. Additionally, we have shown the difficulties in finding accurate correspondences in the case of most long wave infrared data. Most algorithms use a modified version of the 8-point algorithm to obtain the fundamental matrix required to solve for the epipolar geometry. When the data is corrupted as previously described, it is difficult to find even a few accurate correspondences let alone the eight accurate correspondences can be found. In these cases, the proposed algorithm has demonstrated the ability to synthesize new views and does not depend on correspondences or geometry. Additionally, new signature types can be estimated. Given that this approach works well with noisy blurred data and can estimate new signatures, it seems appropriate for use in the infrared domain where images are commonly low in contrast with some noise present. In these types of images, a change in the thermal condition can drastically change their appearance.

Future Work

 While the results shown in this thesis are promising, further tests need to assess the robustness of this approach and its impact on other ATR algorithms. While using principle components to represent the images in lower dimensions was convenient and worked well, there may exist a different basis set that could offer better predictions. For the case where results are to be inputted directly into a machine learning classifier, basis spaces (that cannot be recovered into their original space or are inconvenient to do so)

may be used alternatively. It is also desired to further show improvements in ATR using the proposed method of View Synthesis. To accomplish this, more time should be spent collecting appropriatedatasets and setting up scenarios for these experiments.

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