

# Computational Thinking and Thinking About Computing

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# Outline

- Computational Thinking
  - A Vision for our Field
- Thinking about Computing
  - Drivers of our Field
  - 5 Deep Questions in Computing

# Computational Thinking

# My Grand Vision for the Field

- **Computational thinking** will be a fundamental skill used by everyone in the world by the middle of the 21<sup>st</sup> Century.
  - Just like reading, writing, and arithmetic.
  - Imagine every child knowing how to think like a computer scientist!
  - Incestuous: Computing and computers will enable the spread of computational thinking.
  - **In research:** scientists, engineers, ..., historians, artists
  - **In education:** K-12 students and teachers, undergrads, ...

J.M. Wing, "Computational Thinking," *CACM Viewpoint*, March 2006, pp. 33-35.  
Paper off CISE AC website; paper and talks off <http://www.cs.cmu.edu/~wing/>

# Examples of Computational Thinking

- How difficult is this problem and how best can I solve it?
  - Theoretical computer science gives precise meaning to these and related questions and their answers.
- C.T. is thinking recursively.
- C.T. is reformulating a seemingly difficult problem into one which we know how to solve.
  - Reduction, embedding, transformation, simulation
- C.T. is choosing an appropriate representation or modeling the relevant aspects of a problem to make it tractable.
- C.T. is interpreting code as data and data as code.
- C.T. is using abstraction and decomposition in tackling a large complex task.
- C.T. is judging a system's design for its simplicity and elegance.
- C.T. is type checking, as a generalization of dimensional analysis.
- C.T. is prevention, detection, and recovery from worst-case scenarios through redundancy, damage containment, and error correction.
- C.T. is modularizing something in anticipation of multiple users and prefetching and caching in anticipation of future use.
- C.T. is calling gridlock deadlock and avoiding race conditions when synchronizing meetings.
- C.T. is using the difficulty of solving hard AI problems to foil computing agents.
- C.T. is taking an approach to solving problems, designing systems, and understanding human behavior that draws on concepts fundamental to computer science.

Please tell me your favorite examples of computational thinking!

# Simple Daily Examples

- Looking up a name in an alphabetically sorted list
  - Linear: start at the top
  - Binary search: start in the middle
- Standing in line at a bank, supermarket, customs & immigration
  - Performance analysis of task scheduling
- Putting things in your child's knapsack for the day
  - Pre-fetching and caching
- Taking your kids to soccer, gymnastics, and swim practice
  - Traveling salesman (with more constraints)
- Cooking a gourmet meal
  - Parallel processing: You don't want the meat to get cold while you're cooking the vegetables.
- Cleaning out your garage
  - Keeping only what you need vs. throwing out stuff when you run out of space.
- Storing away your child's Lego pieces scattered on the LR floor
  - Using hashing (e.g., by shape, by color)
- Doing laundry, getting food at a buffet
  - Pipelining the wash, dry, and iron stages; plates, salad, entrée, dessert stations
- Even in grade school, we learn algorithms (long division, factoring, GCD, ...) and abstract data types (sets, tables, ...).

# The First A to Computational Thinking

- **Abstractions** are our “mental” tools
- The abstraction process includes
  - Choosing the right abstractions
  - Operating simultaneously at multiple layers of abstraction
  - Defining the relationships the between layers

# The Second **A** to Computational Thinking

- The power of our “mental” tools is amplified by our “metal” tools.
- **Automation** is mechanizing our abstractions, abstraction layers, and their relationships
  - Mechanization is possible due to precise and exacting notations and models
  - There is some “computer” below (human or machine, virtual or physical)



# Two A's to C.T. Combined

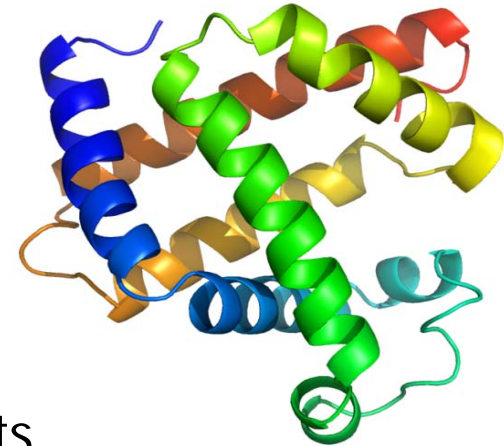
- Computing is the **automation** of our **abstractions**
  - They give us the audacity and ability to scale.
- Computational thinking
  - choosing the right abstractions, etc.
  - choosing the right "computer" for the task

# Research Implications

# CT in Other Sciences, Math, and Engineering

## Biology

- Shotgun algorithm expedites sequencing of human genome
- DNA sequences are strings in a language
- Protein structures can be modeled as knots
- Protein kinetics can be modeled as computational processes
- Cells as a self-regulatory system are like electronic circuits



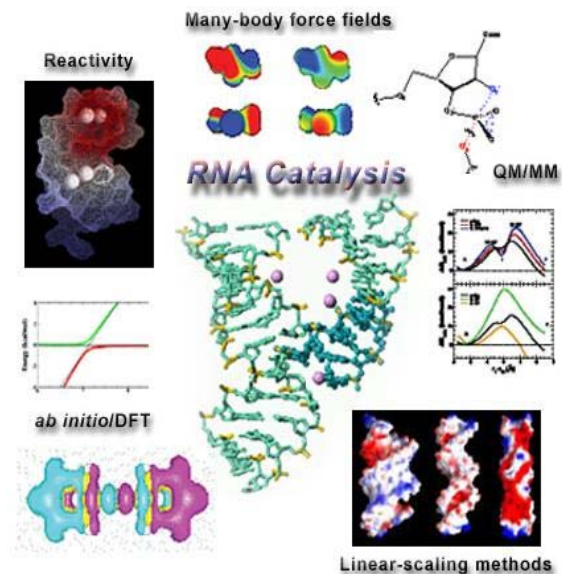
## Brain Science

- Modeling the brain as a computer
- Vision as a feedback loop
- Analyzing fMRI data with machine learning

# CT in Other Sciences, Math, and Engineering

## Chemistry [Madden, Fellow of Royal Society of Edinburgh]

- Atomistic calculations are used to explore chemical phenomena
- Optimization and searching algorithms identify best chemicals for improving reaction conditions to improve yields



[York, Minnesota]



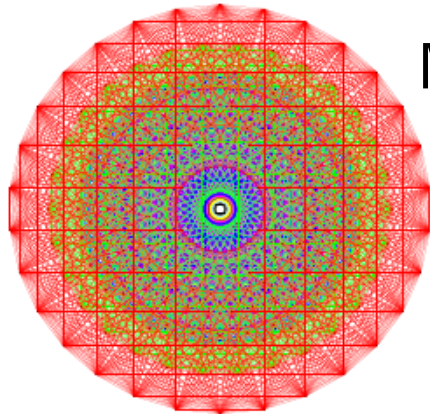
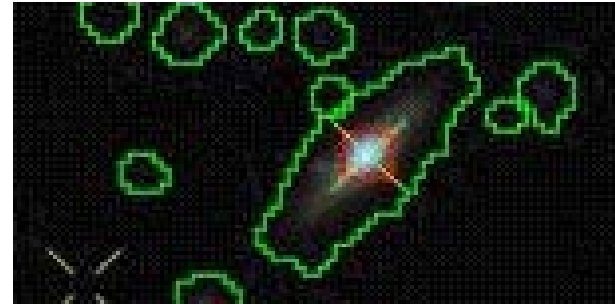
## Geology

- Modeling the earth's surface to the sun, from the inner core to the surface
- Abstraction boundaries and hierarchies of complexity model the earth and our atmosphere

# CT in Other Sciences, Math, and Engineering

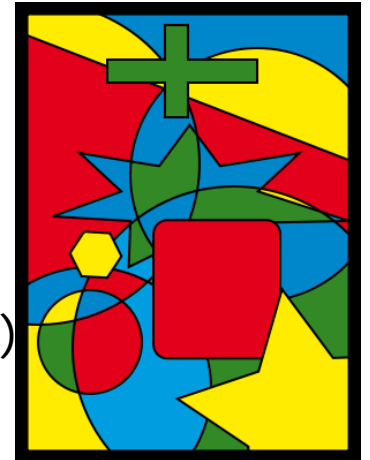
## Astronomy

- Sloan Digital Sky Server brings a telescope to every child
- KD-trees help astronomers analyze very large multi-dimensional datasets



## Mathematics

- Discovering E8 Lie Group:  
18 mathematicians, 4 years and 77 hours of supercomputer time (200 billion numbers).  
Profound implications for physics (string theory)
- Four-color theorem proof



## Engineering (electrical, civil, mechanical, aero&astro, ...)

- Calculating higher order terms implies more precision, which implies reducing weight, waste, costs in fabrication
- Boeing 777 tested via computer simulation alone, not in a wind tunnel



# CT for Society

## Economics

- Automated mechanism design underlies electronic commerce, e.g., ad placement, on-line auctions, kidney exchange
- MIT PhDs in CS are quants on Wall Street

Microsoft Digital Advertising Solutions



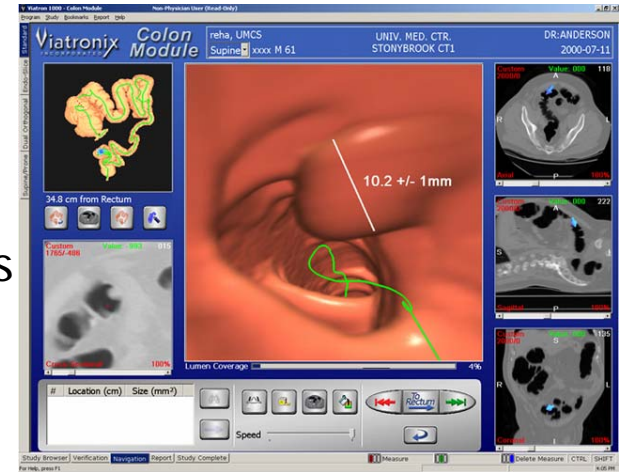
## Social Sciences

- Social networks explain phenomena such as MySpace, YouTube
- Statistical machine learning is used for recommendation and reputation services, e.g., Netflix, affinity card

# CT for Society

## Medicine

- Robotic surgery
- Electronic health records require privacy technologies
- Scientific visualization enables virtual colonoscopy

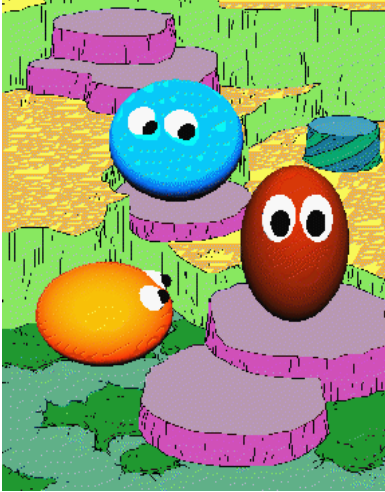


## Law

- Stanford CL approaches include AI, temporal logic, state machines, process algebras, petri nets
- POIROT Project on fraud investigation is creating a detailed ontology of European law
- Sherlock Project on crime scene investigation

# CT for Society

## Entertainment

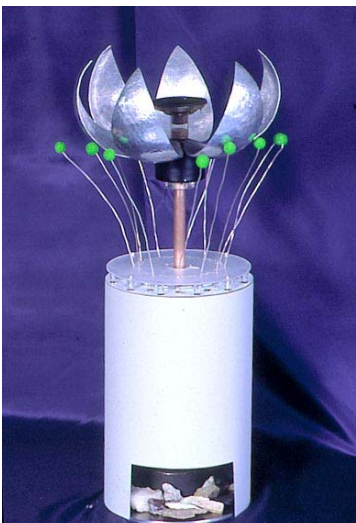


- Games
- Movies
- Dreamworks uses HP data center to render *Shrek* and *Madagascar*
- Lucas Films uses 2000-node data center produce *Pirates of the Caribbean*.



## Arts

- Art (e.g., Robotticelli)
- Drama
- Music
- Photography



## Sports

- Lance Armstrong's cycling computer tracks man and machine statistics
- Synergy Sports analyzes digital videos NBA games

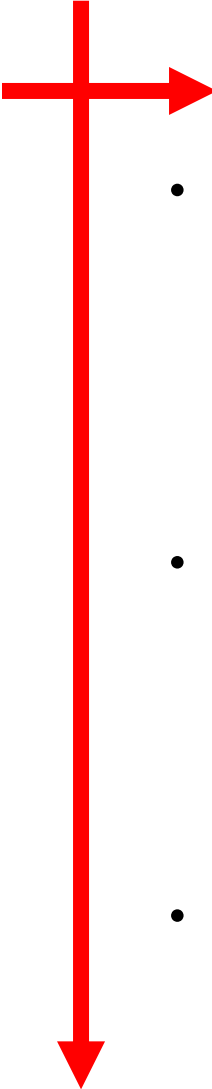


Jeannette M. Wing



# Educational Implications

# Pre-K to Grey



K-6, 7-9, 10-12

- Undergraduate courses
  - Freshmen year
    - “Ways to Think Like a Computer Scientist” aka Principles of Computing
  - Upper-level courses
- Graduate-level courses
  - Computational arts and sciences
    - E.g., entertainment technology, computational linguistics, ..., computational finance, ..., computational biology, computational astrophysics
- Post-graduate
  - Executive and continuing education, senior citizens
  - Teachers, not just students

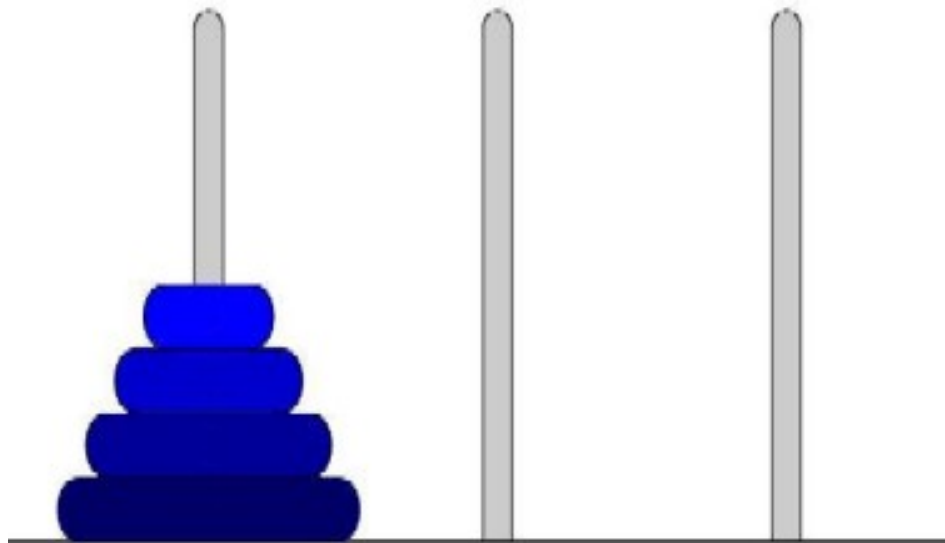
# Question and Challenge to Community

What are effective ways of learning (teaching) computational thinking by (to) children?

- What **concepts** can students best learn when? What should we teach when? What is our analogy to numbers in K, algebra in 7, and calculus in 12?
- We uniquely also should ask how best to integrate **The Computer** with learning and teaching the concepts.

# Recursion: Towers of Hanoi

Goal: Transfer the entire tower to one of the other pegs, moving only one disk at a time and never a larger one onto a smaller.



# Data Abstraction and Representation



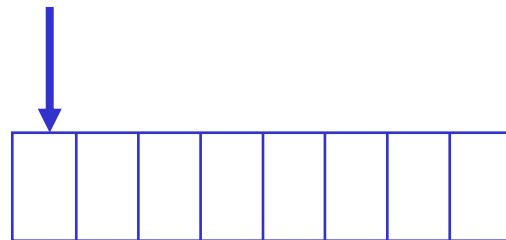
stack



queue



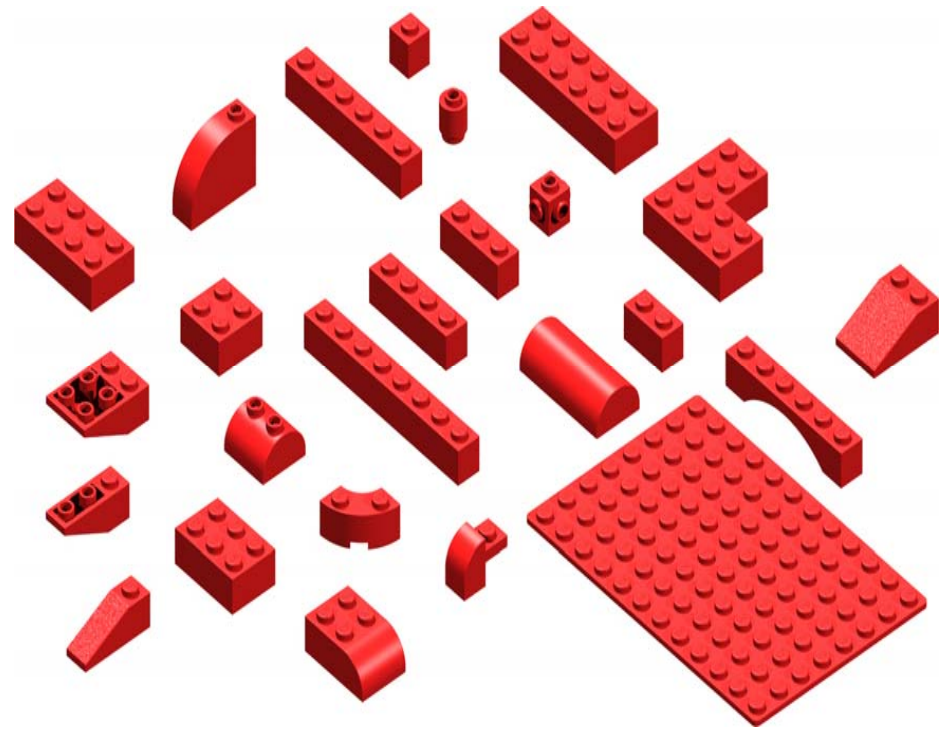
tree  
(upside down)



array and pointer

*representation invariant*

# Composition and Decomposition



# Sorting and Search



**Web** [Images](#) [Video](#) [News](#) [Maps](#) [more »](#)

Google Search

I'm Feeling Lucky

[Advanced Search](#)  
[Preferences](#)  
[Language Tools](#)

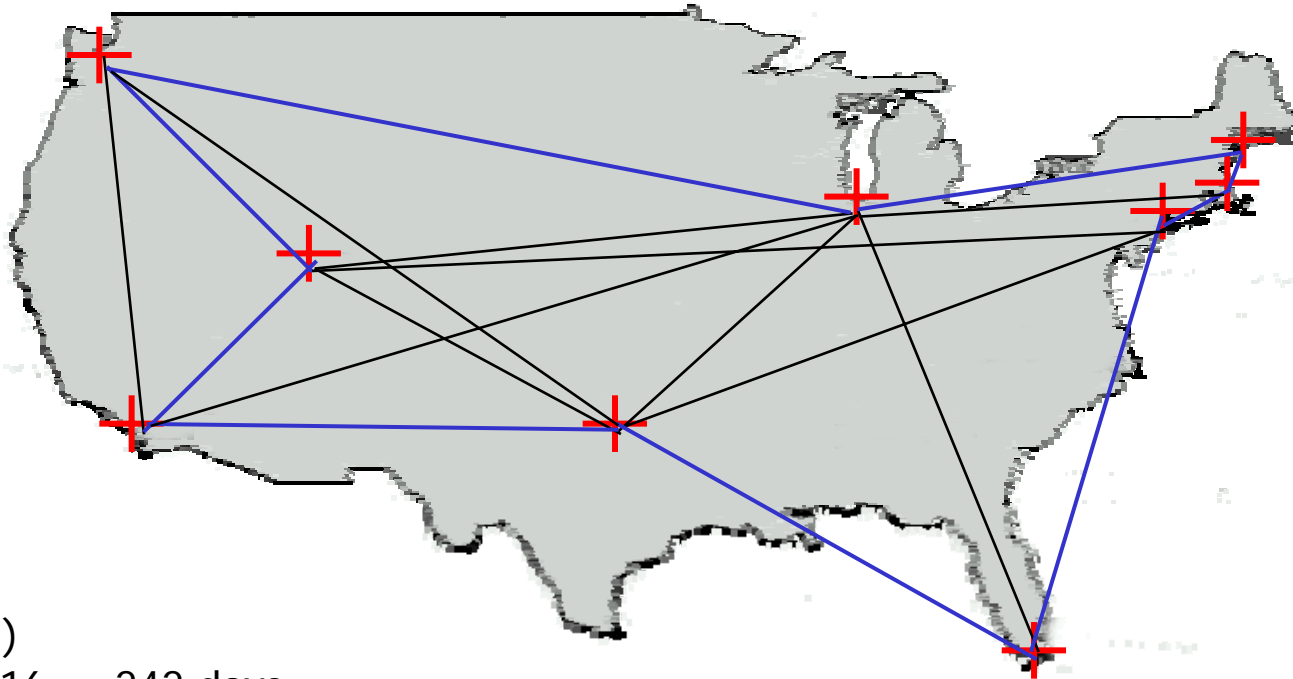
Organize and share holiday pictures with [Google's photo software](#).

[Advertising Programs](#) - [Business Solutions](#) - [About Google](#)

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# Intractability: Traveling Salesman

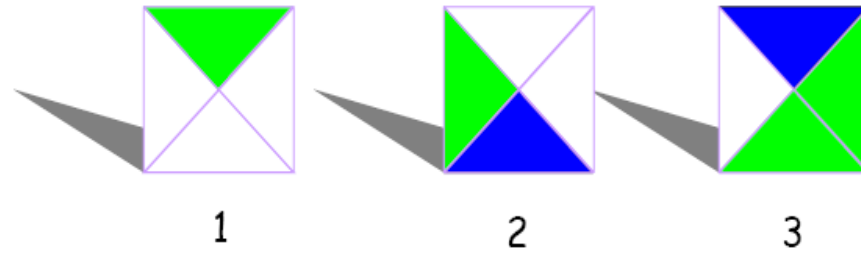
Problem: A traveling salesperson needs to visit  $n$  cities.  
Is there a route of at most  $d$  in length?



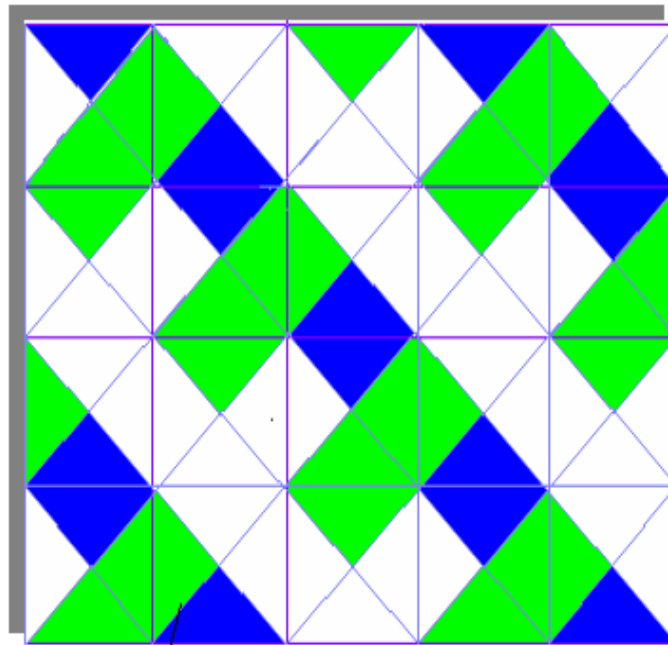
$O(n!)$   
 $n = 16 \rightarrow 242$  days  
 $n = 25 \rightarrow 5 \times 10^{15}$  centuries



# Undecidability: Tiling

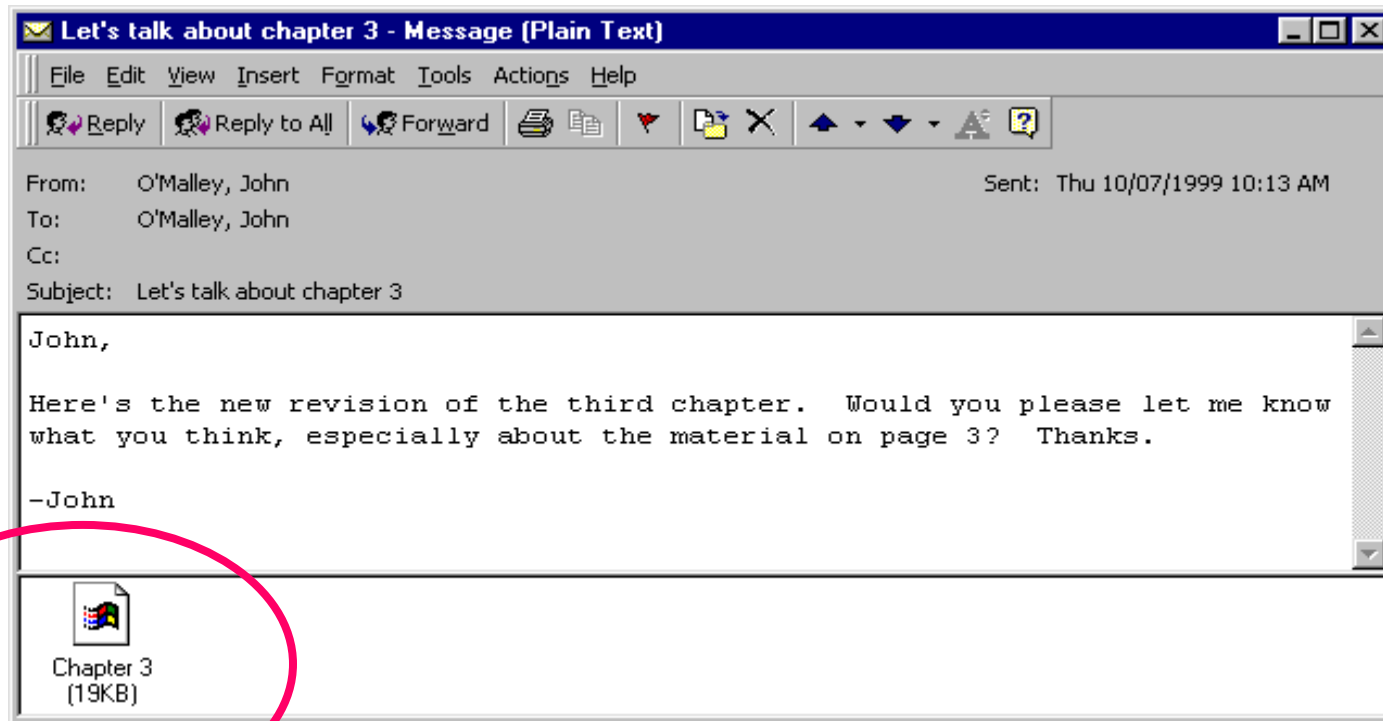


Can we tile the entire plane  $\mathbb{Z}^2$ ?



Example from David Harel

# Data as Code and Code as Data



unrecognized  
email attachment

# Recursion Revisited

The Y operator

$$Y = \lambda f. (\lambda x. f (x x)) (\lambda x. f (x x))$$

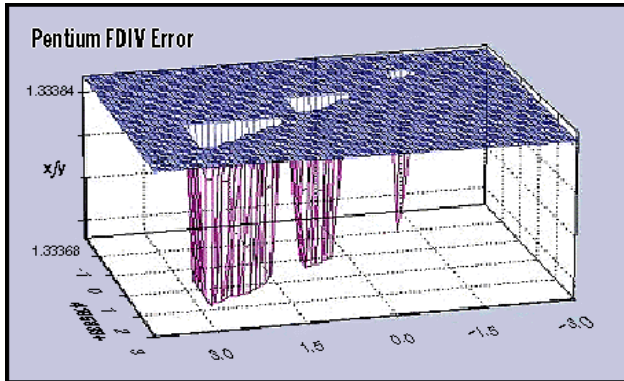
which satisfies the following equation

$$Y f = f (Y f)$$

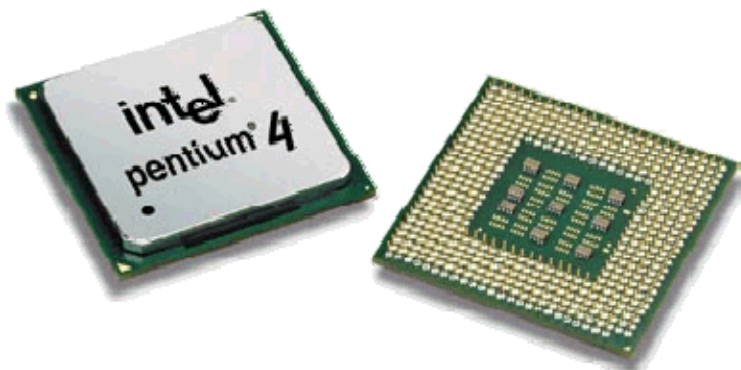
and is the basis of recursion in Computer Science.

Y is the *fixed point* combinator in lambda calculus.

# Correctness: Avoiding Bugs to Save Money and Lives



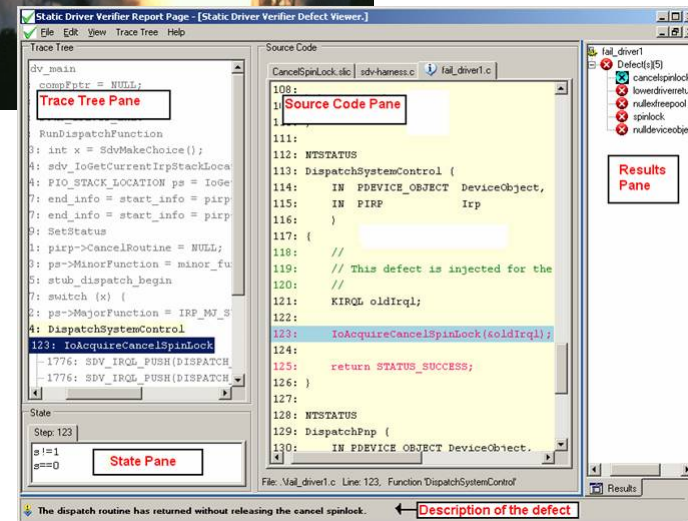
Intel Pentium FPU error



Now Intel uses formal verification.

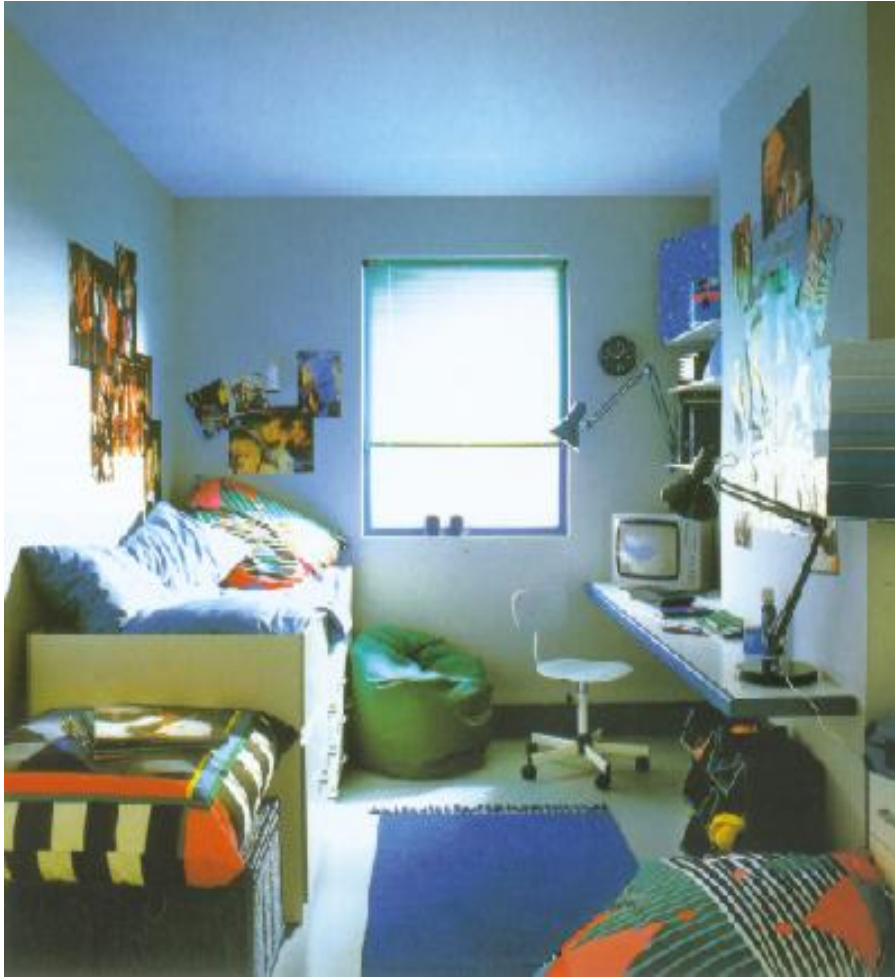


Ariane 5 failure



Now Microsoft uses formal verification.

# Caching



home



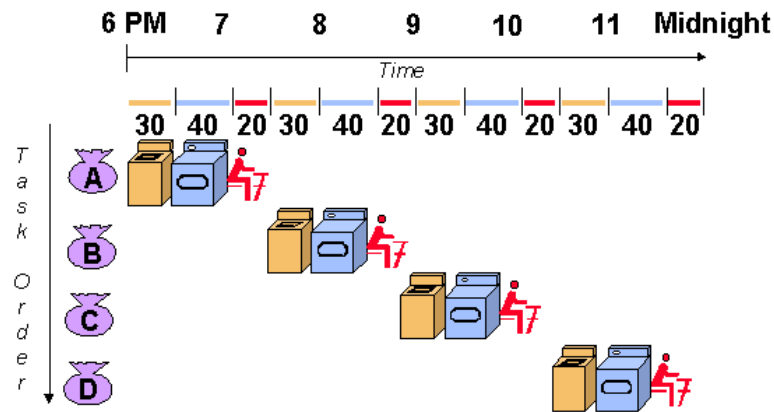
locker



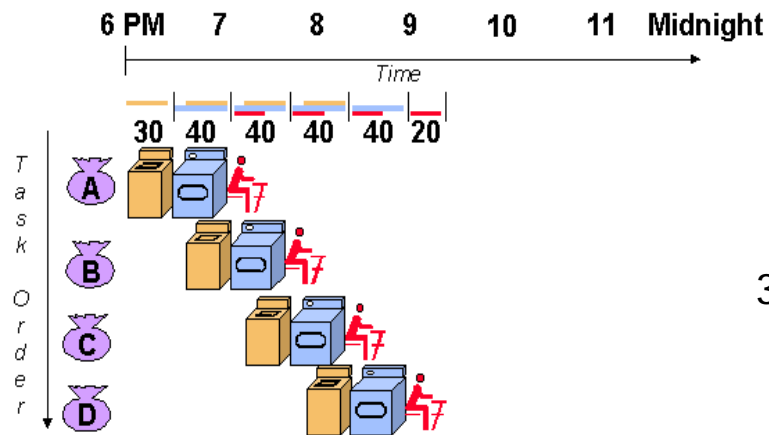
knapsack

# Pipelining: Doing Laundry

6 hours to do 4 loads

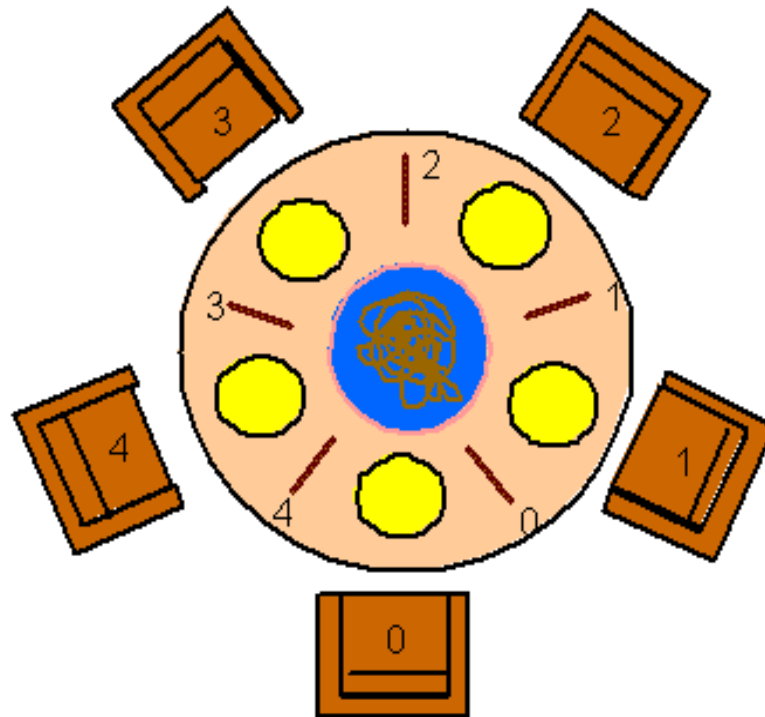


3.3 hours to do 4 loads

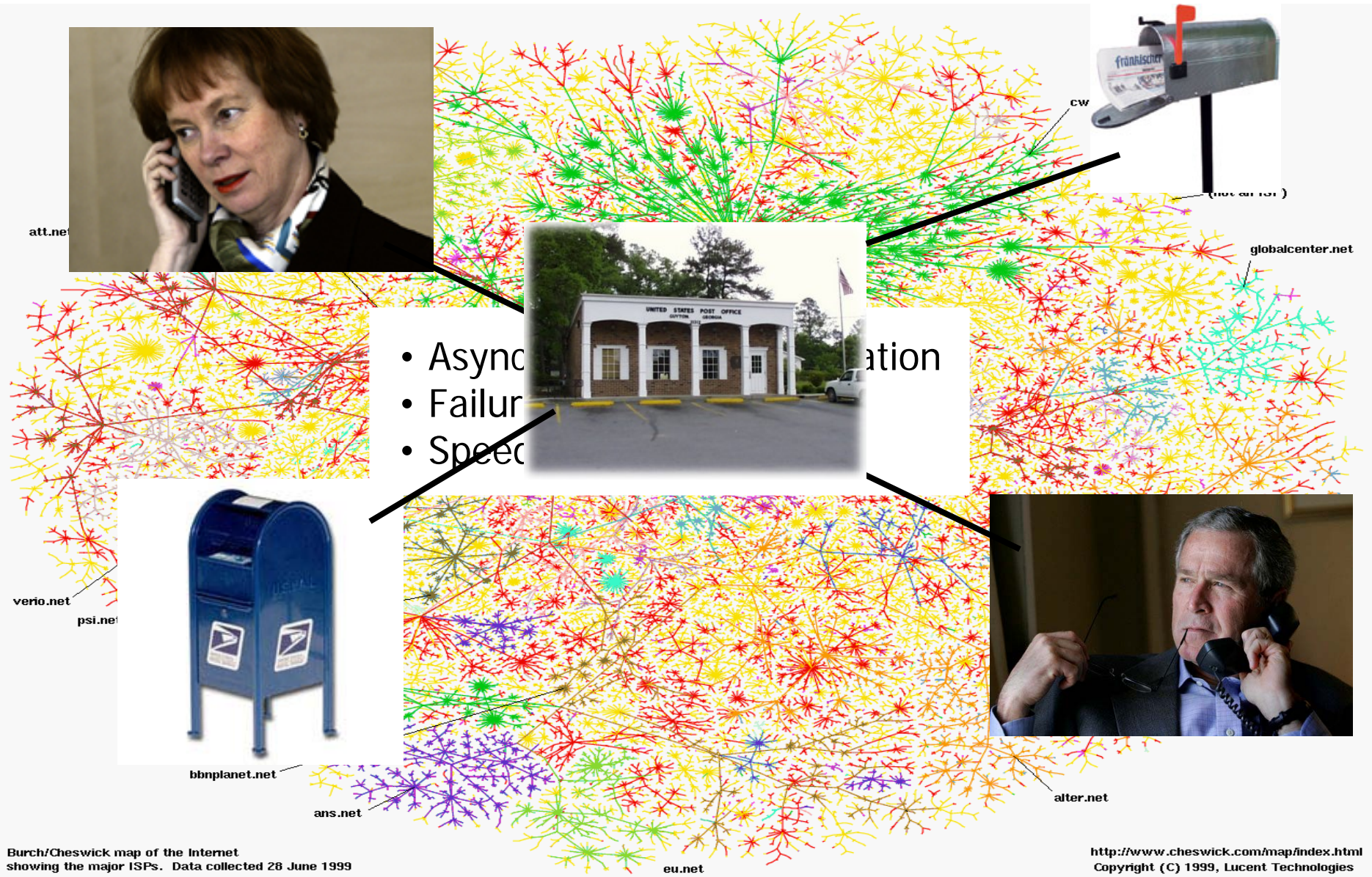


# Concurrency: Dining Philosophers

Five philosophers sit around a circular table. Each philosopher spends his life alternately **thinking** and **eating**. In the centre of the table is a large bowl of spaghetti. A philosopher needs two forks to eat a helping of spaghetti.



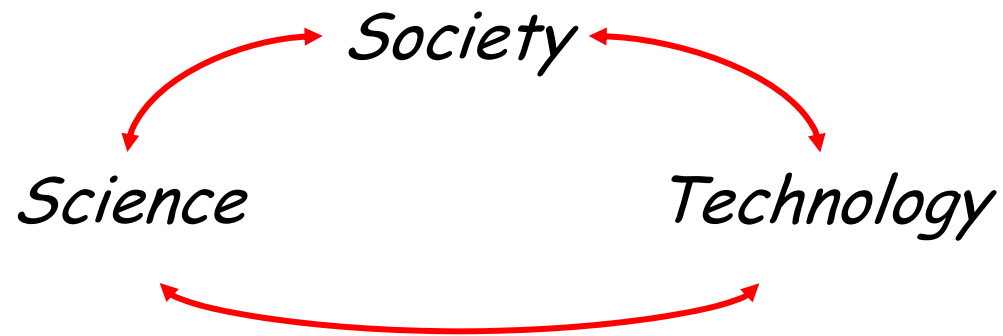
# Distributed Computing: The Internet





# Thinking About Computing

# Drivers of Computing



# Technology Trends: Computing Substrates

- **Moore's Law** will end in 10-15 years [Gordon Moore 9/18/07]
- **Nanocomputing** is here.
  - March 2006, IBM researchers build the first complete IC around a single carbon nanotube molecule.
- **Biocomputing** is here.
  - 1994, Adleman solves 7-point Hamiltonian path problem with DNA computing
  - 2004, Shapiro, Benenson, Gil, Ben-Dor, and Adar of Weizmann Institute announce in *Nature* the construction of a DNA computer
- **Quantum** is coming?
  - "Quantum Cryptography to Secure Ballots in Swiss Election," *Network World*, Oct 11 2007
- **Bio-Nano-Quantum**
  - "Fabrication of Photonic Transfer DNA-Quantum Dot Nanostructures," Heller, Sullivan and Dehling, *Nanotech* 2005.
  - "Economical Fabrication of Quantum Dot-Electronics Using Biofunctionalized Protein Nanotubes as Building Blocks, Masui, NSF CAREER award

# More Technology Trends

- **Devices**
  - 2 billion cell phones in the world; RFID tags; sensors everywhere
  - A BMW is "now actually a network of computers" [R. Achatz, Seimens, Economist Oct 11, 2007]
  - Robots in your home
- **Information**
  - Drowning in data; sensors everywhere; storage is cheap; information overload
- **Communication**
  - Femto cells—personal base stations
  - Web 3.0 (semantic web)
  - Virtual worlds: *Second Life* is today's *Mosaic*
- **Brainy machines**
  - IBM and EPFL's Blue Brain Project: to create a biologically accurate, functional model of the brain
  - [www.numenta.com](http://www.numenta.com) : software platform for intelligent computing modeled after human neocortex

# Users and Society

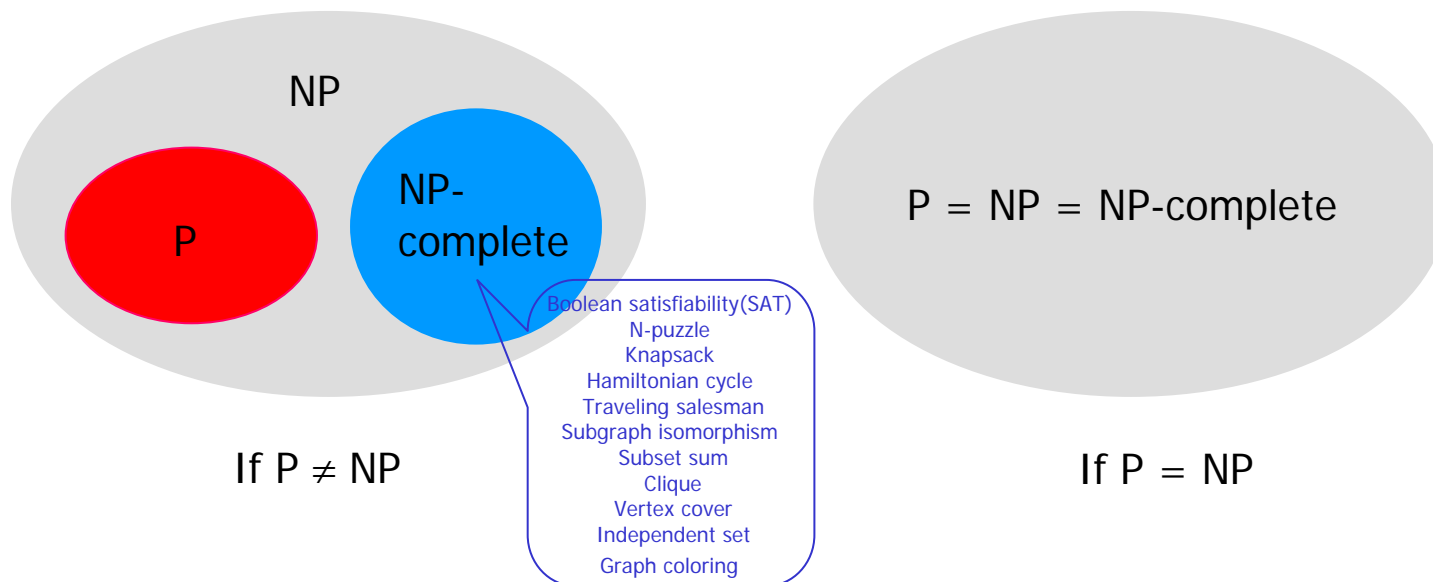
- **Expectations:** 24/7 availability, 100% reliability, 100% connectivity, instantaneous response, store anything and everything forever, ...
- **Classes:** young to old, able and disabled, rich and poor, literate and illiterate, ...
- **Numbers:** individual → cliques → acquaintances → social networks → cultures → populations
- **The Internet/Web is a great equalizer.**
  - What about privacy? Anonymity to accountability
  - When will it stop being free?
  - Will it continue to be self-regulating?

# 5 Deep Questions in Computing

- $P = NP$  ?
- What is computable?
- What is intelligence?
- What is information?
- (How) can we build complex systems simply?

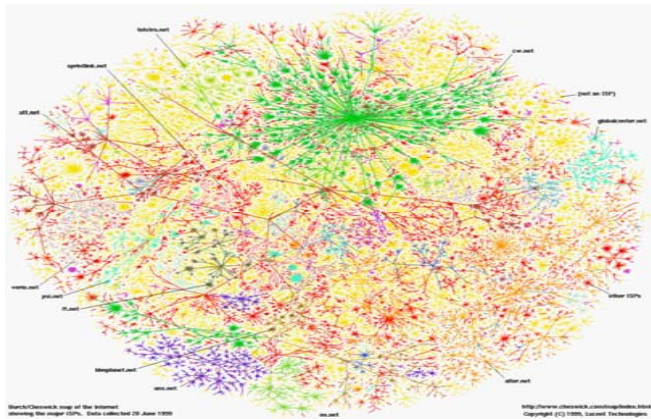
# The \$1M Question: Does $P = NP$ ?

- The most important open problem in theoretical computer science. The Clay Institute of mathematics offers **one million** dollar prize for solution!
  - [http://www.claymath.org/Millennium\\_Prize\\_Problems/](http://www.claymath.org/Millennium_Prize_Problems/)

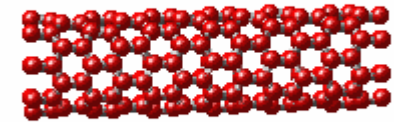


# What is Computable?

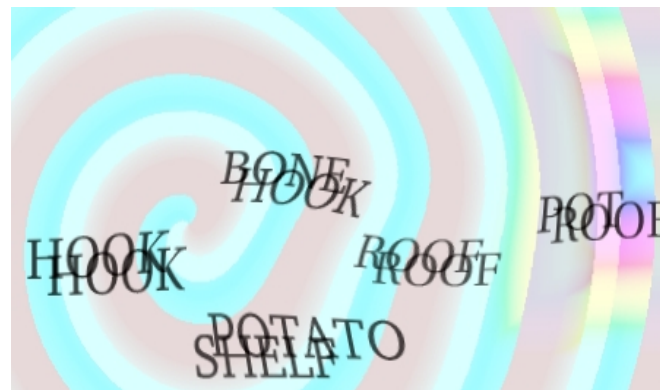
- What are the power and limits of computation?
- What is a computer?



- Not just a PC anymore: The Internet, server farms, supercomputers, multi-cores, ..., nano, bio, quantum, etc.



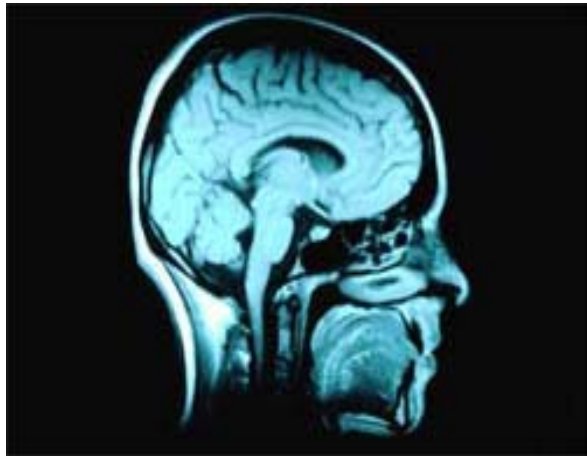
- What is the power of computing, by machine and human **together?**



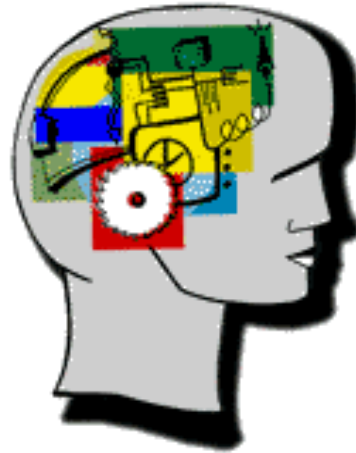
**The ESP Game** beta  
As seen on CNN and newspapers around the world!



# What is Intelligence?



Human and Machine



“Computing Versus Human Thinking,” **Peter Naur**, Turing Award 2005 Lecture, *CACM*, January 2007.

Human vs. Machine



*invariant representations:*  
**On Intelligence**,  
by Jeff Hawkins, creator  
of PalmPilot and Treo

IN IN TO  
TAIL OR SAVE  
IS

PRINT

FILE TOOLS  
SHARED BY  
**FOR YOUR  
PRIDERS  
MINDS**

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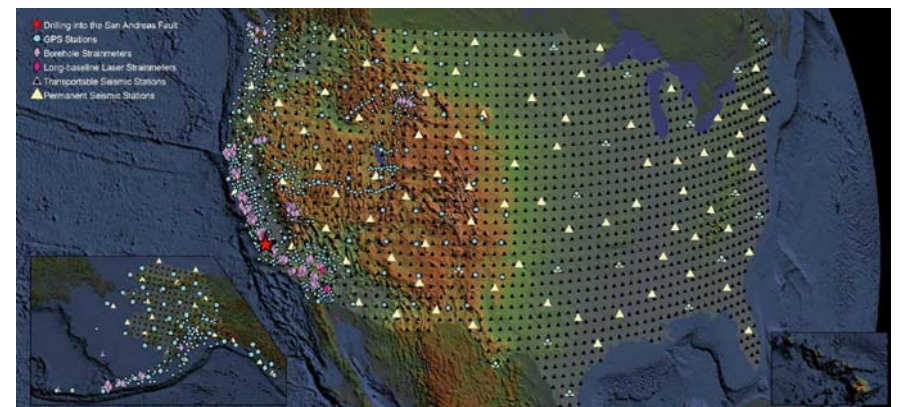
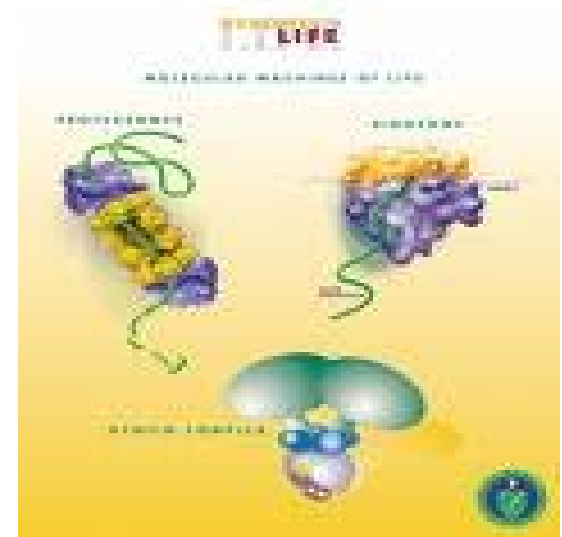
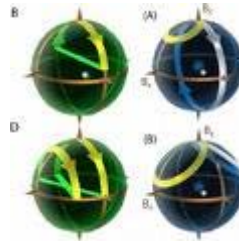
when I

lost Game 2 by walking into a checkmate in c

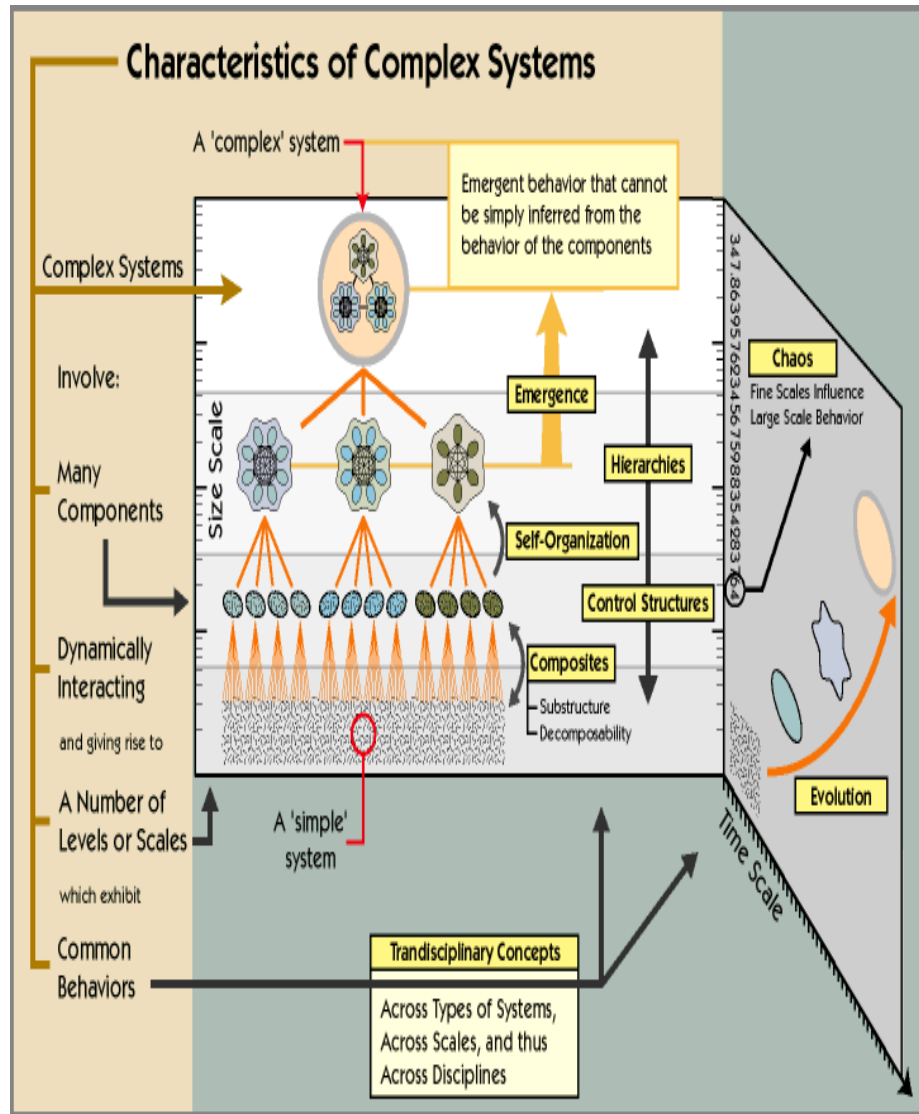


# What is Information?

- From nature
  - It's not just 0's and 1's
    - Qubits
  - "Biology is an information science."
    - Geology too.
  - Molecules/chemicals are processors of information (computer), carriers of information (storage), and channels of information (communication)
- ...To knowledge
  - We are drowning in data.  
Data is dirt; knowledge is gold.



# (How) Can We Build Complex Systems Simply?



- We have complexity classes from theory.
- We build complex systems that do amazing, but often unpredictable, things.

**Question:** Is there a **complexity theory** for systems as there is for algorithms?

**Question:** Is there a meaning of **system complexity** that spans the theory and practice of computing?

**Question:** Do our systems have to be so complex?

- Can we build **systems with simple designs**, that are easy to understand, modify, and maintain, yet provide the **rich complexity in functionality** of systems that we enjoy today?

# Two Messages for the General Public

- Intellectually challenging and engaging scientific problems in computer science remain to be understood and solved.
  - Limited only by our curiosity and creativity
- One can major in computer science and do anything.
  - Just like English, political science, or mathematics

# Spread the Word!

- Help make computational thinking commonplace
- Help explain the science in computer science

To fellow faculty, students, researchers,  
administrators, teachers, parents, principals,  
guidance counselors, school boards, teachers' unions,  
congressmen, policy makers, ...

Thank you!