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## DEDICATED TO

Tobias Dantzig, my father,  $in\ memoriam$  and to

John D. Williams, A. W. Tucker, and Anne S. Dantzig