

Part 1

Similarity search, pattern discovery and summarization

Yasushi Sakurai (Kumamoto University)
 Yasuko Matsubara (Kumamoto University)
 Christos Faloutsos (Carnegie Mellon University)

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Outline

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
- ➔ Streaming pattern discovery
- Automatic mining

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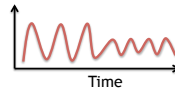
Stream mining

- Applications
 - Sensor monitoring
 - Network analysis
 - Financial and/or business transaction data
 - Web access and media service logs
 - Moving object tracking
 - Industrial manufacturing

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Stream mining

- Requirements
 - **Fast**
high performance and quick response
 - **Nimble**
low memory consumption, single scan
 - **Accurate**
good approximation for pattern discovery and feature extraction



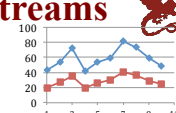
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Monitoring data streams

- Correlation coefficient

$$\rho = \frac{\sum_{i=1}^n (x_i - \bar{x}) \cdot (y_i - \bar{y})}{\sigma(x) \cdot \sigma(y)} \quad \sigma(x) = \sqrt{\sum_{i=1}^n (x_i - \bar{x})^2}$$
- Correlation coefficient and the (Euclidean) distance

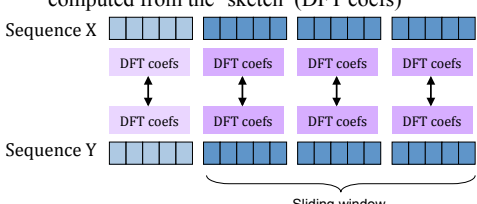
$$\rho = 1 - \frac{1}{2} \sum_{i=1}^n (\hat{x}_i - \hat{y}_i)^2 \quad \hat{x}_i = (x_i - \bar{x}) / \sigma(x)$$



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Monitoring data streams

- Correlation monitoring [Zhu+, vldb02]
 - DFT coefficients for each basic window
 - Correlation coefficient of each sliding window computed from the 'sketch' (DFT coeffs)



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Monitoring data streams

- Grid structure (to avoid checking all pairs)
 - DFT coefficients yields a vector
 - High correlation \rightarrow closeness in the vector space

Vector V_X of sequence X
 Vector V_Y of sequence Y

Correlation coefficients and the Euclidean distance

$$\rho = 1 - \frac{1}{2} \sum_{i=1}^n (\hat{x}_i - \hat{y}_i)^2$$

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Monitoring data streams

- Lag correlation [Sakurai+, sigmod05]

CCF (Cross-Correlation Function)

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Monitoring data streams

- Lag correlation [Sakurai+, sigmod05]

CCF (Cross-Correlation Function)

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Lag correlation

- Definition of 'score', absolute value of $R(l)$

$$score(l) = |R(l)| \quad R(l) = \frac{\sum_{i=l+1}^n (x_i - \bar{x})(y_{i-l} - \bar{y})}{\sqrt{\sum_{i=l+1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^{n-l} (y_i - \bar{y})^2}}$$

- Lag correlation
 - Given a threshold γ , $score(l) > \gamma$
 - A local maximum
 - The earliest such maximum, if more maxima exist

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Lag correlation

- Why not naïve?
 - Compute correlation coefficient for each lag $l = \{0, 1, 2, 3, \dots, n/2\}$
- But
 - $O(n)$ space
 - $O(n^2)$ time
 - or $O(n \log n)$ time w/ FFT

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Lag correlation

- BRAID
 - Geometric lag probing + smoothing
 - Use colored windows
 - Keep track of only a geometric progression of the lag values: $l = \{0, 1, 2, 4, 8, \dots, 2^h, \dots\}$

Multi-scale windows

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Lag correlation

- BRAID
 - Geometric lag probing + smoothing
 - Keep track of only a geometric progression of the lag values: $l = \{0, 1, 2, 4, 8, \dots, 2^h, \dots\}$
 - Use a cubic spline to interpolate

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Lag correlation

- Why not naïve?
 - Compute correlation coefficient for each lag $l = \{0, 1, 2, 3, \dots, n/2\}$
- But
 - $O(n)$ space
 - $O(n^2)$ time
 - or $O(n \log n)$ time w/

BRAID

- $O(\log n)$ space
- $O(l)$ time

Multi-scale windows

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BRAID in the real world

- Bridge structural health monitoring
 - Structural monitoring using vibration/shock sensors
 - Keep track of lag correlations for sensor data streams

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BRAID in the real world

- Bridge structural health monitoring
 - Goal: real-time anomaly detection for disaster prevention
 - Several thousands readings (per sec) from several hundreds sensor nodes
- Uses BRAID
- Metropolitan Expressway (Tokyo, Japan)

Structural health monitoring

Vibration/shock sensor

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BRAID in the real world

- Bridge structural health monitoring with BRAID

Metropolitan Expressway (Tokyo, Japan)

Can Tho Bridge (Vietnam)

Tokyo Gate Bridge (Tokyo, Japan)

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Feature extraction from streams

major leak

normal operation

water distribution network

- Find hidden variables from streams [Papadimitriou+, vldb2005]

May have hundreds of measurements, but it is **unlikely they are completely unrelated!**

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Feature extraction from streams

hidden variables

Phase 1 Phase 2 Phase 3

chlorine concentrations

sensors near leak

sensors away from leak

water distribution network

normal operation

major leak

May have hundreds of measurements, but it is **unlikely they are completely unrelated!**

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Motivation

chlorine concentrations

Phase 1

actual measurements (n streams)

Phase 1

$k = 1$

k hidden variable(s)

We would like to discover a few "hidden (latent) variables" that summarize the key trends

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Motivation

chlorine concentrations

Phase 1 Phase 2

actual measurements (n streams)

Phase 1 Phase 2

$k = 2$

k hidden variable(s)

We would like to discover a few "hidden (latent) variables" that summarize the key trends

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Motivation

chlorine concentrations

Phase 1 Phase 2 Phase 3

actual measurements (n streams)

Phase 1 Phase 2 Phase 3

$k = 1$

k hidden variable(s)

We would like to discover a few "hidden (latent) variables" that summarize the key trends

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How to capture correlations?

First sensor

Temperature T_1

time

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How to capture correlations?

First sensor

Second sensor

Temperature T_2

time

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How to capture correlations?

Correlations:

Let's take a closer look at the first three value-pairs...

Temperature T_2

Temperature T_1

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How to capture correlations?

First three lie (almost) on a line in the space of value-pairs...

- $O(n)$ numbers for the slope, and
- *One* number for each value-pair (offset on line)

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How to capture correlations?

Other pairs also follow the same pattern: they lie (approximately) on this line

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Incremental update

For each new point

- Project onto current line
- Estimate error

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Incremental update

For each new point

- Project onto current line
- Estimate error
- Rotate line in the direction of the error and in proportion to its magnitude

→ $O(n)$ time

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Incremental update

For each new point

- Project onto current line
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Related work

- Wavelet over streams [Gilbert+, vldb01] [Guha+, vldb04]
- Fourier representations [Gilbert+, stoc02]
- KNN [Koudas+, 04] [Korn+, vldb02]
- Histograms [Guha+, stoc01]
- Clustering [Guha+, focs00] [Aggarwal+, vldb03]
- Sketches [Indyk+, vldb00] [Cormode+, J. Algorithms 05]
- ...


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Related work

- Heavy hitters [Cormode+, vldb03]
- Data embedding [Indyk+, focs00]
- Burst detection [Zhu+, kdd03]
- Segmentation [Keogh+, icdm01]
- Multiple scale analysis [Papadimitriou+, sigmod06]
- Fractal [Korn+, sigmod06]
- Time warping [Sakurai+, icde07]...
- ...



Tutorial@PODS'15
Graham
Cormode



Tutorial@SIGMOD'15
Divesh
Srivastava

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- ➔ • Automatic mining

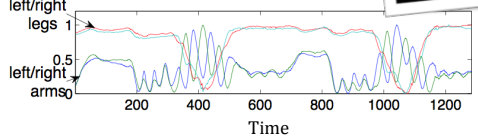
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Motivation

Given: co-evolving time-series
– e.g., MoCap (leg/arm sensors)




“Chicken dance”



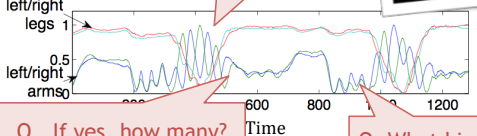
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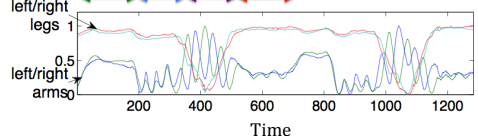
Motivation

Challenges: co-evolving sequences

- Unknown # of patterns (e.g., beaks)
- Different durations

beaks wings tail feathers claps ...



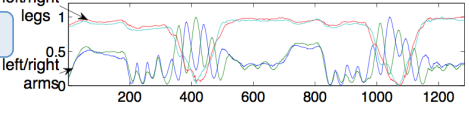


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Motivation

Goal: find patterns that agree with human intuition

Input



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Motivation

Goal: find patterns that agree with human intuition

Input

Output

1	Beaks	Beaks
2	Wings	Claps
3	Wings	Claps
4	Wings	Claps

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Motivation

Goal: find patterns that agree with human intuition

Input

NO magic numbers!

Automatic!

Output

1	Beaks	Beaks
2	Wings	Claps
3	Wings	Claps
4	Wings	Claps

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Why: Automatic mining

No magic numbers! ... because,

Manual (use magic)

- sensitive to the parameter tuning
- long tuning steps (hours, days, ...)

Automatic (no magic numbers)

- no expert tuning required

Big data mining:
-> we cannot afford human intervention!!

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How: Automatic mining

Goal: fully-automatic modeling

- Given: **data X**
- Find: a compact description (**model M**) of X

Data (X) → **Ideal model (M)**

Q. How can we find the best model M?

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How: Automatic mining

Goal: fully-automatic modeling

- Given: **data X**
- Find: a compact description (**model M**) of X

Answer: MDL!

Data (X) → **Ideal model (M)**

Q. How can we find the best model M?

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Solution: MDL (Minimum description length)

Solution: Minimize total encoding cost \$!

- Occam's razor (i.e., law of parsimony)
- **Fully automatic** parameter optimization
- No over-fitting

Ideal model

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Solution: MDL (Minimum description length)

Solution: Minimize total encoding cost \$!

$$\text{Cost}_T(X;M) = \min (\text{Cost}_M(M) + \text{Cost}_c(X|M))$$

Total cost Model cost Coding cost (error)

\$\$\$ \$\$ \$ (Ideal!) \$\$\$\$

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[Matsubara+ SIGMOD'14]

AutoPlait: Automatic Mining of Co-evolving Time Sequences

Yasuko Matsubara (Kumamoto University)
Yasushi Sakurai (Kumamoto University),
Christos Faloutsos (CMU)

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Problem definition

Goal: find patterns that agree with human intuition

Input

Output

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Problem definition

- Bundle: set of d co-evolving sequences

given

$$X = \{x_1, \dots, x_n\}$$

Bundle X ($d=4$)

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Problem definition

- Segment: convert $X \rightarrow m$ segments, S

hidden

$$S = \{s_1, \dots, s_m\}$$

Segment ($m=8$)

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Problem definition

- Regime: segment groups: $\Theta = \{\theta_1, \theta_2, \dots, \theta_r, \Delta_{rxr}\}$

hidden

Regimes ($r=4$)

θ_r : model of regime r

beaks $\rightarrow \theta_1, \theta_2$

wings $\rightarrow \theta_3, \theta_4$

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Problem definition

- Segment-membership: assignment

hidden $F = \{f_1, \dots, f_m\}$

$F = \{ \overset{1}{2}, \overset{2}{4}, \overset{3}{1}, \overset{4}{3}, \overset{5}{2}, \overset{6}{4}, \overset{7}{1}, \overset{8}{3} \}$

Segment-membership (m=8)

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Problem definition

- Given: bundle X

$X = \{x_1, \dots, x_n\}$

- Find: compact description C of X

$C = \{m, r, S, \Theta, F\}$

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Problem definition

- Given: bundle X

$X = \{x_1, \dots, x_n\}$

- Find: compact description C of X

$C = \{m, r, S, \Theta, F\}$

m segments
r regimes
Segment-membership

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Main ideas

Goal: compact description of X

$C = \{m, r, S, \Theta, F\}$

without user intervention!!

Challenges:

Q1. How to generate 'informative' regimes ?

Q2. How to decide # of regimes/segments ?

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Main ideas

Goal: compact description of X

$C = \{m, r, S, \Theta, F\}$

without user intervention!!

Challenges:

Q1. How to generate 'informative' regimes ?

Idea (1): Multi-level chain model

Q2. How to decide # of regimes/segments ?

Idea (2): Model description cost

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Idea (1): MLCM: multi-level chain model

Q1. How to generate 'informative' regimes ?

Sequences → Model → Regimes (beaks, claps, wings)

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Idea (1): MLCM: multi-level chain model

Q1. How to generate 'informative' regimes ?

Sequences → Model → Regimes

Regimes: beaks, claps, wings

Idea (1): Multi-level chain model

- HMM-based probabilistic model
- with "across-regime" transitions

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Idea (1): MLCM: multi-level chain model

$\Theta = \{\theta_1, \theta_2, \dots, \theta_r, \Delta_{r \times r}\}$ ($\theta_i = \{\pi, A, B\}$)

r regimes (HMMs) across-regime transition prob. Single HMM parameters

Regimes $r=2$
Regime 1 ($k=3$)
Regime 2 ($k=2$)

Regime1 "beaks" Regime2 "wings"

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Idea (2): model description cost

Q2. How to decide # of regimes/segments ?

Idea (2): Model description cost

- Minimize encoding cost
- find "optimal" # of segments/regimes

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Idea (2): model description cost

Idea: Minimize encoding cost!

$\min (\text{Cost}_M(M) + \text{Cost}_C(X|M))$

Model cost Coding cost

Good compression ↔ Good description

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Idea (2): model description cost

Total cost of bundle X, given C

$C = \{m, r, S, \Theta, F\}$

$$\begin{aligned} \text{Cost}_T(\mathbf{X}; C) &= \text{Cost}_T(\mathbf{X}; m, r, S, \Theta, F) \\ &= \log^*(n) + \log^*(d) + \log^*(m) + \log^*(r) + m \log(r) \\ &\quad + \sum_{i=1}^{m-1} \log^* |s_i| + \text{Cost}_M(\Theta) + \text{Cost}_C(\mathbf{X}|\Theta) \end{aligned} \quad (6)$$

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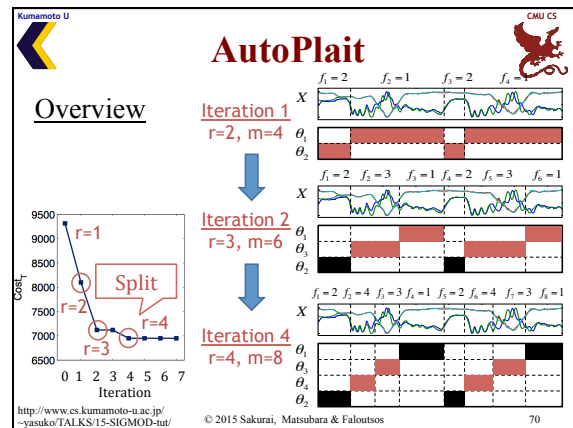
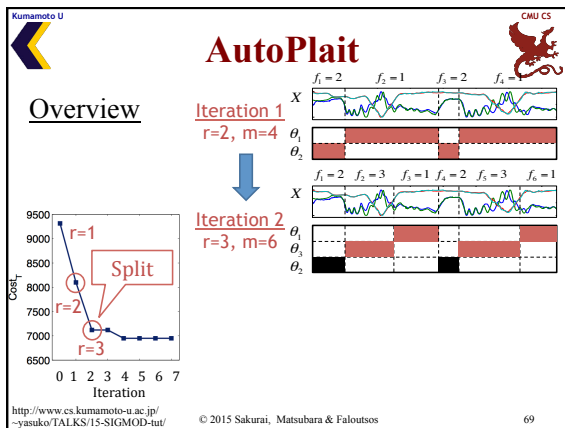
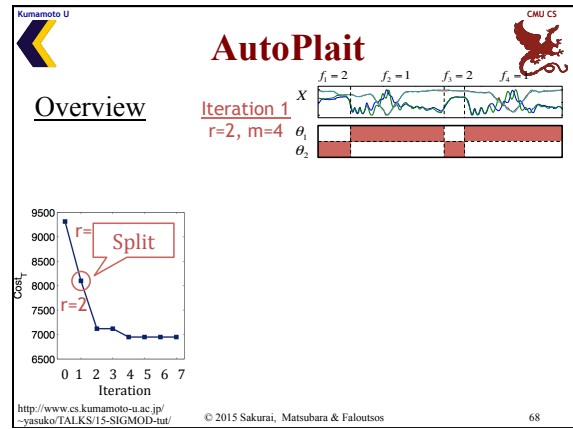
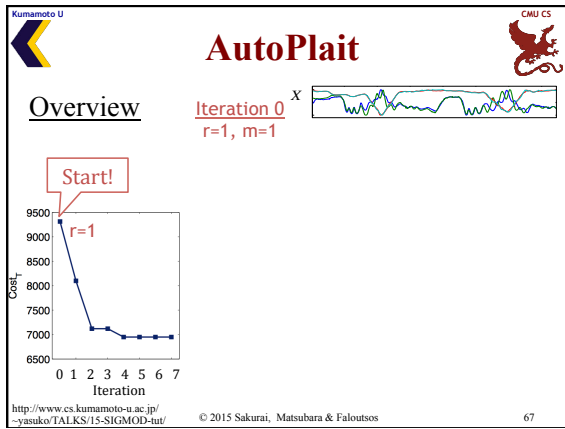
Idea (2): model description cost

Total cost of bundle X, given C

$C = \{m, r, S, \Theta, F\}$

$$\begin{aligned} \text{Cost}_T(\mathbf{X}; C) &= \text{Cost}_T(\mathbf{X}; m, r, S, \Theta, F) \\ &= \log^*(n) + \log^*(d) + \log^*(m) + \log^*(r) + m \log(r) \\ &\quad + \sum_{i=1}^{m-1} \log^* |s_i| + \text{Cost}_M(\Theta) + \text{Cost}_C(\mathbf{X}|\Theta) \end{aligned} \quad (6)$$

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AutoPlait

Algorithms

1. **CutPointSearch** Inner-most loop
Find good cut-points/segments
2. **RegimeSplit** Inner loop
Estimate good regime parameters Θ
3. **AutoPlait** Outer loop
Search for the best number of regimes (r=2,3,4...)

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1. CutPointSearch

Inner-most loop

Given:

- bundle X
- parameters of two regimes $\Theta = \{\theta_1, \theta_2, \Delta\}$

Find: cut-points of segment sets S_1, S_2

$$\{S_1, S_2\} = \operatorname{argmax} P(X | S_1, S_2, \Theta)$$

X

θ_1, θ_2

$S_1 = \{s_2, s_4\}$
 $S_2 = \{s_1, s_3\}$

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1. CutPointSearch

DP algorithm to compute likelihood: $P(X|\Theta)$

state 1 $L_{1,1}(1) = \phi$ $L_{1,1}(3) = \phi$...
 state 2 $L_{2,2}(2) = \phi$ $L_{2,2}(4) = \phi$...
 state 3 $L_{3,3}(2) = \phi$ $L_{3,3}(4) = \phi$...

switch?? $\delta_{2,1}$ $\delta_{1,2}$

state 1 $L_{2,1}(3) = \{3\}$ $L_{1,4}(4) = \{3\}$ $L_{2,5}(5) = \{4\}$...
 state 2 $L_{2,2}(4) = \{4\}$ $L_{2,3}(5) = \{3\}$ $L_{2,6}(6) = \{4\}$...

X $t=1$ $t=2$ $t=3$ $t=4$ $t=5$ $t=6$...

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1. CutPointSearch

Theoretical analysis

Scalability

- It takes $O(ndk^2)$ time (only single scan)
- n: length of X
- d: dimension of X
- k: # of hidden states in regime

Accuracy

It guarantees the optimal cut points

- (Details in paper)

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2. RegimeSplit

Given: bundle X

Inner loop

Find: two regimes

1. find cut-points of segment sets: S_1, S_2
2. estimate parameters of two regimes: $\Theta = \{\theta_1, \theta_2, \Delta\}$

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2. RegimeSplit

Two-phase iterative approach

- Phase 1: (CutPointSearch)
- Split segments into two groups: S_1, S_2
- Phase 2: (BaumWelch)
- Update model parameters: $\Theta = \{\theta_1, \theta_2, \Delta\}$

$S_1 = \{s_2, s_4\}$ Phase 1
 $S_2 = \{s_1, s_3\}$
 $\{\theta_1, \theta_2, \Delta\}$ Phase 2

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3. AutoPlait

Given: bundle X

Outer loop

Find: r regimes ($r=2, 3, 4, \dots$)

- i.e., find full parameter set $C = \{m, r, S, \Theta, F\}$

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3. AutoPlait

Split regimes $r=2, 3, \dots$, as long as cost keeps decreasing

- Find appropriate # of regimes

$r = \min_r Cost_r(X; m, r, S, \Theta, F)$

$r=2, m=4$
 $f_1=2, f_2=1, f_3=2, f_4=1$

$r=4, m=8$
 $f_1=2, f_2=4, f_3=3, f_4=1, f_5=2, f_6=4, f_7=3, f_8=1$

$r=3, m=6$
 $f_1=2, f_2=3, f_3=1, f_4=2, f_5=3, f_6=1$

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Results

- Mocap data
- WebClick data
- Google Trends

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Q1. Sense-making

MoCap data

AutoPlait (NO magic numbers)

(a) AUTOPLAIT (no user defined parameters)

DynaMMo (Li et al., KDD'09) pHMM (Wang et al., SIGMOD'11)

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Q1. Sense-making

MoCap data

AutoPlait (NO magic numbers)

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Q2. Accuracy

(a) Segmentation

Recall vs Precision plot. Target is at (1,1). AutoPlait is highest, followed by pHMM, then DynaMMo.

(b) Clustering

Entropy (CE) score. AutoPlait is significantly lower than pHMM.

(a) Precision and recall (higher is better) (b) CE score (lower is better)

AutoPlait needs "no magic numbers"

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Q3. Scalability

Wall clock time vs. data size (length) : n

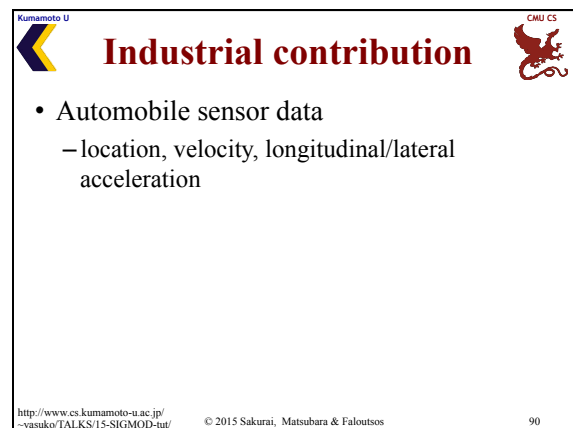
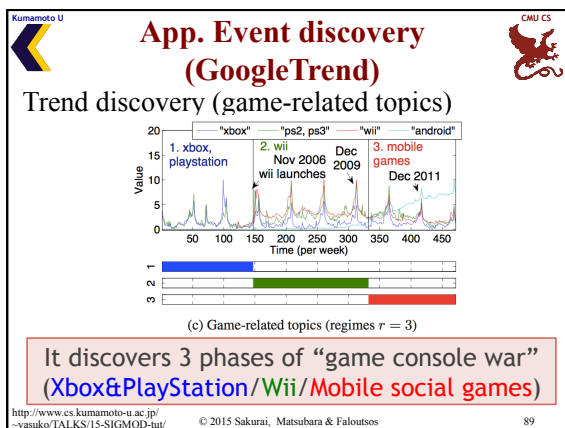
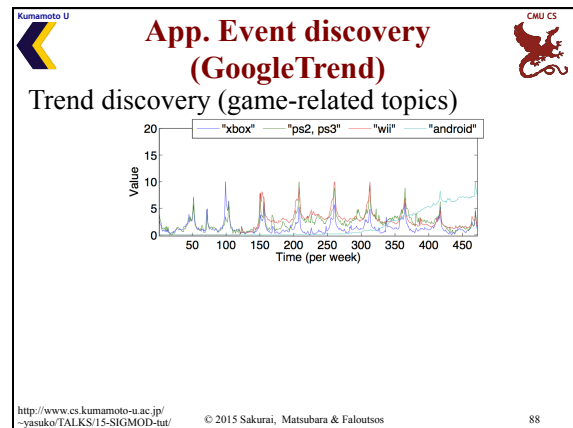
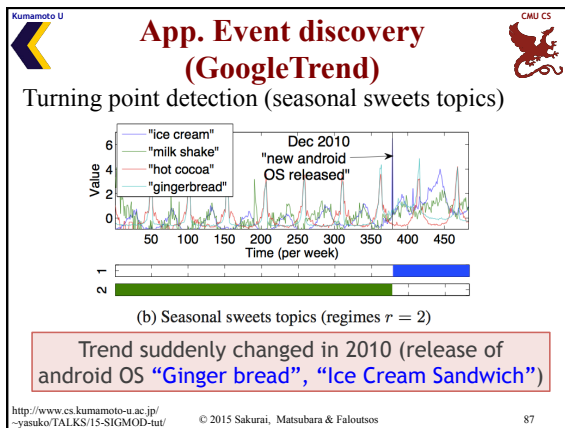
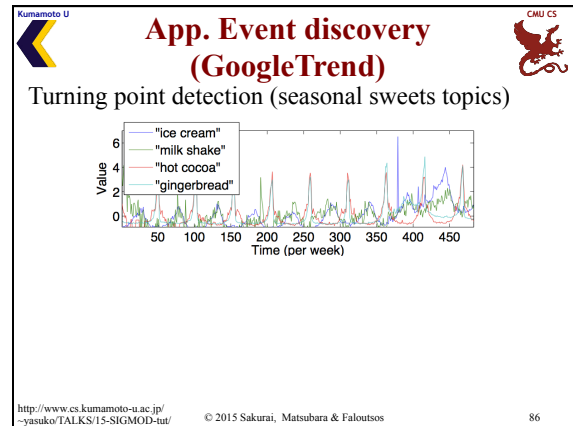
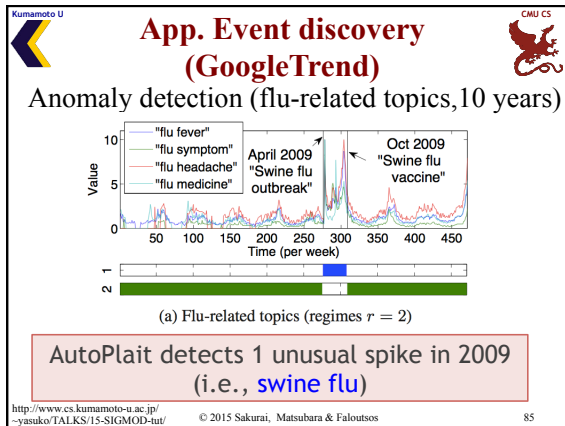
AutoPlait scales linearly, i.e., $O(n)$


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App. Event discovery (GoogleTrend)

Anomaly detection (flu-related topics, 10 years)

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Code at

- <http://www.cs.kumamoto-u.ac.jp/~yasuko/software.html>


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Part 1 – Conclusions

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining


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Part 1 – Conclusions

- Motivation
- Similarity Search and Indexing
 - Euclidean/time-warping
 - extract features
 - index (SAM, R-tree)
- Feature extraction
 - SVD, ICA, DFT, DWT (multi-scale windows)


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Part 1 – Conclusions

- Linear forecasting
 - AR, RLS
- Streaming pattern discovery
 - RLS, “incremental” wavelet transform
 - Multi-scale windows
- Automatic mining
 - MDL

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Part 1  

Similarity search, pattern discovery and summarization

Yasushi Sakurai (Kumamoto University)
Yasuko Matsubara (Kumamoto University)
Christos Faloutsos (Carnegie Mellon University)

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