

A Learning-Based Jam Session System that Imitates a Player's Personality Model

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Abstract

This paper describes a jam session system that enables a human player to interplay with virtual players which can imitate the player personality models of various human players. Previous systems have parameters that allow some alteration in the way virtual players react, but these systems cannot imitate human personalities. Our system can obtain three kinds of player personality models from a MIDI recording of a session in which that player participated - a reaction model, a phrase model, and a groove model. The reaction model is the characteristic way that a player reacts to other players, and it can be statistically learned from the relationship between the MIDI data of music the player listens to and the MIDI data of music improvised by that player. The phrase model is a set of player's characteristic phrases; it can be acquired through musical segmentation of a MIDI session recording by using Voronoi diagrams on a piano-roll. The groove model is a model that generates onset time deviation; it can be acquired by using a hidden Markov model. Experimental results show that the personality models of any player participating in a guitar trio session can be derived from a MIDI recording of that session.

1 Introduction

Our goal is to create a jam session system in which virtual players react as if they were actual human players. We want to make it possible for a human player to interact, whenever they like, with a virtual player that can imitate whoever the human player wishes to perform, for example, with a familiar, professional, or deceased player, or even with themselves. What is most important in imitating players is to acquire *the player's personality models* of a target human player.

Previous session systems have not been able to imitate a human player's personality. Some systems [Aono *et al.*, 1995] have been designed to follow the performance of a human soloist, but without considering the individual character of the virtual player. Although JASPER [Wake

et al., 1994] has a set of rules that determine the system's reactions and VirJa Session [Goto *et al.*, 1996] has parameters for altering how it reacts, these systems cannot develop player personality models of an actual human player.

To realistically imitate a human player, a system must be able to acquire player personality models of that player. The imitating virtual player can then improvise according to the models. The Neuro-Musician [Nishijima and Kijima, 1989; Nishijima and Watanabe, 1992] can learn the relationship between 30 sets of an 8-bar-length input pattern and an output pattern by using neural networks. However, it is only capable of dealing with the limited style of a jam session where a solo part must be changed in 8-bar rotation. In other words, a virtual player and a human player cannot both play a solo part in the same time. Moreover, the Neuro-Musician must prepare a training set of 8-bar-length input-output data to enable neural network learning. In an actual jam session, a player does not always play an 8-bar solo to the 8-bar solo of the other players. Therefore, we cannot acquire the player models from a MIDI session recording by using the Neuro-Musician method.

On the other hand, the Band-OUT-of-a-Box (BoB), which deals with a problem similar to ours [Thorn, 2001a; Thorn, 2001b], indicates that machine learning techniques provide a useful approach to acquire a player's models. However, BoB can only react to a human performance of an immediately previous four bars. It has a fixed relationship in which the human player is the leader and the virtual player is the follower.

Our jam system allows us to acquire player personality models of a target human player from the MIDI recording of a session in which that player participated. The main advantage of our approach is that we do not have to directly evaluate the target player: all we need to build the models is session recording data.

2 A Guitar Trio Session System

Our system deals with constant-tempo 12-bar blues performed by a guitar trio. Figure 1 shows a jam session

MIDI stands for Musical Instrument Digital Interface.

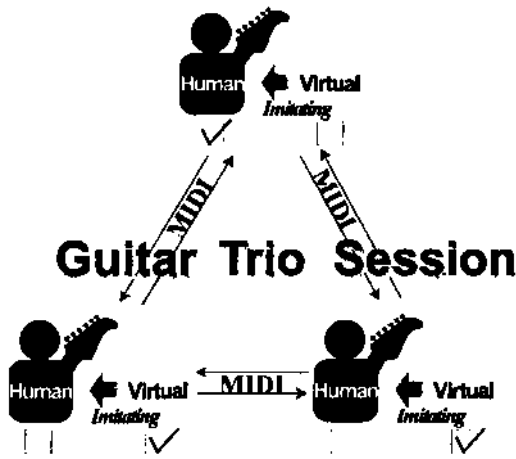


Figure 1: Session model in which either human or computer can be selected as each player.

model in which either a human or the computer can be selected to perform the part of each player. We can imagine sessions in which all players will be human players just as we can imagine sessions in which all players are computer players. The three players take the solo part one after another without a fixed leader-follower relationship.

We obtain three kinds of player personality model from a MIDI session recording - a *reaction model*, a *phrase model*, and a *groove model*.

The system has two modes, a *learning mode* and a *session mode*. In the learning mode (discussed in Sections 3, 4, and 5), the system acquires player personality models in non-real time. These models are stored in a database and different personality models can be assigned to the two virtual players before session play (Figure 2). In the session mode (discussed in Section 6), a human player can interact with the virtual players in real time.

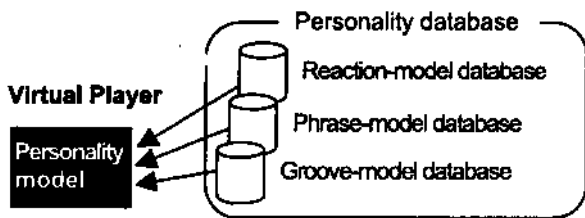


Figure 2: Virtual player and personality databases

3 Learning a reaction model

A reaction model is the characteristic way that a player reacts to other players. Acquiring an actual player's individual reaction model is necessary to create a virtual player that reacts as that actual human player does. As shown in Figure 3, each virtual player listens to the performances of all the players (including its own) and uses the reaction model to determine what its next reaction (output performance) will be. The main issue in deriving

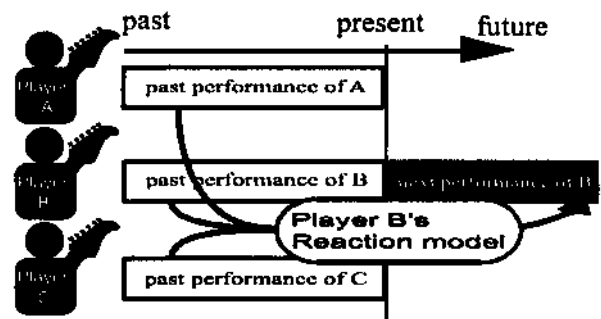


Figure 3: Player's reaction model

the reaction model is to learn the relationship between the input and the output of the target player in MIDI recordings. This can be formulated as a problem of obtaining a mapping from the input to the target player's output. However the direct MIDI-level learning of this mapping is too difficult because the same MIDI-level sequence rarely occurs more than once and the mapping itself is too sparse. We therefore have introduced two intermediate subjective spaces: an *impression space* and an *intention space* (Figure 4).

3.1 Impression space

The impression space represents the subjective impression derived from the MIDI input. By applying principal components analysis (PCA) to the results of subjective evaluations of various MIDI performances, we determined three coordinate axes for the impression space. PCA is a statistical method for reducing the number of dimensions while capturing the major variances within a large data set. While listening to a performance, a subject subjectively evaluated it by using ten impression words to rank the performance's impression on a scale of one to seven. The three selected axes of the impression space represent qualities that can be described as *appealing*, *energetic*, and *heavy*. To obtain a vector in this space, an *impression vector* corresponding to the MIDI input, we use canonical correlation analysis (CCA). This analysis maximizes the correlation between various low-level features of the MIDI input (such as pitch, note counts, tensions, and pitch bend) and the corresponding subjective evaluation. Since an impression vector is obtained from an individual player's performance, we have at every moment three impression vectors (Figure 4).

The impression space is necessary for learning the relationship between various input performances and the corresponding output performances. If we represent the input performances as short MIDI segments without using the impression space, the same MIDI segments will not be repeated in different sessions. The impression space enables the abstracting of subjective impressions from input MIDI data and those impressions can be repeated. Even if two segments of the input MIDI data differ, they can be represented as a similar vector in the impression space as long as they give the same impression.

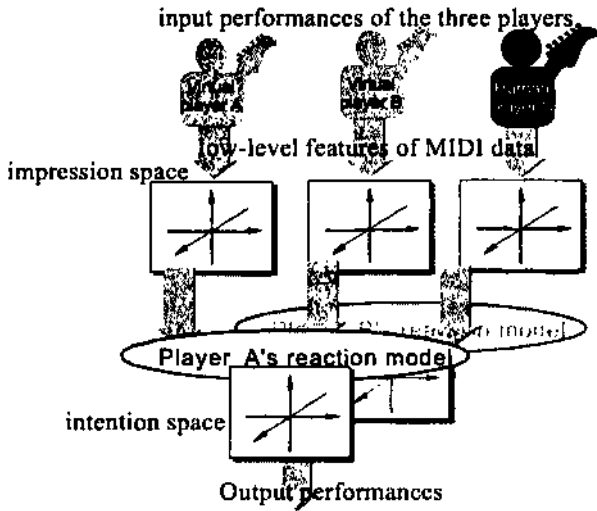


Figure 4: Player architecture.

Figure 5 shows the transition of the rated values for the impression word "appealing". The black line represents the value calculated by the system and the gray line represents the value as evaluated by a human listener. For 92 percent of the performance, the calculated and subjectively evaluated values do not differ by more than 1.

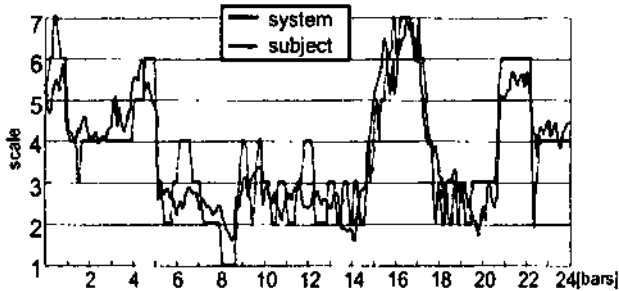


Figure 5: Transition of rated values calculated by system and evaluated by subject (for impression word "appealing").

3.2 Intention space

The intention space represents the intention of the player improvising the output. A vector in this space, an *intention vector*, determines the feeling of the next output. It is used to select short MIDI phrases from a phrase database, and connecting the selected phrases generates the output MIDI performance.

Without the intention space, learning the relationship between impression vectors and output MIDI data is difficult because in actual MIDI recordings various outputs can occur when the input data gives the same impression. The intention space makes it easier to learn the player's reaction model.

The intention space is constructed by using multidimensional scaling (MDS) [Kruskal and Wish, 1978] such that intention vectors are distributed with proximities proportional to subjective similarities of short phrases corresponding to those vectors. Based on MDS results, we determined the three dimensions of this

we determined the three dimensions of this space. Because the number of the short phrases is limited, those phrases are sparsely placed in the intention space. When generating the output, the system selects the output phrase close to the determined intention vector: an appropriate phrase can be selected even if the phrase database does not have a phrase that is exactly placed on the intention vector.

3.3 Acquiring a reaction model

We can regard the mapping from the impression space to the intention space as the reaction model. To derive this mapping function statistically, we obtain various training sets from the target session recordings. These sets are pairs of impression vectors obtained from the three players during a sequence of the past twelve bars and the corresponding next intention vector. For this learning we use Gaussian radial basis function (RBF) networks [Chen *et al.*, 1991]. The RBF networks have one hidden layer with nonlinear inputs, and each node in the hidden layer computes the distance between the input vector and the center of the corresponding radial basis function.

The input of the RBF network is impression vector x (L dimensions) derived from three players and the output of the RBF network is intention vector $\tilde{y}_1, \tilde{y}_2, \tilde{y}_3$ (3 dimensions). Training data of the RBF network is N th ($11(=12-1)$ chorus \times 12 bars \times 4 beats = 528) couples of past impression vectors and corresponding intention vectors y_1, y_2, y_3 . Therefore, training data is $(x^{(k)}, y_j^{(k)})$ ($k = 1, 2, \dots, N, j = 1, 2, 3$).

The RBF network has M th ($M \leq N$) units. Each unit indicates a center vector on an L th dimensional space. The output of a unit is represented by equation (1).

$$\phi(r) = \exp\left(-\frac{r^2}{\sigma^2}\right) \quad \sigma \neq 0, r \geq 0 \quad (1)$$

$$r = \|x^{(k)} - c_i\|$$

The output of the RBF network $\tilde{y}_j^{(k)}$ is the sum of products of unit outputs $\phi(r)$ and weights $a_j(i)$ represented in equation (2).

$$\tilde{y}_j^{(k)} = \sum_{i=1}^M a_j(i) \phi(\|x^{(k)} - c_i\|) \quad (2)$$

By using modeling residual $e_j^{(k)}$, the relationship of the network input and output can be represented by equation (3).

$$y_j = P(x) a_j + e_j \quad (3)$$

$$P(x) = \begin{bmatrix} p_1^{(1)} & p_2^{(1)} & \dots & p_M^{(1)} \\ p_1^{(2)} & p_2^{(2)} & \dots & p_M^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ p_1^{(N)} & p_2^{(N)} & \dots & p_M^{(N)} \end{bmatrix}$$

$$p_i^{(k)} = \phi(\|x^{(k)} - c_i\|) \quad (k = 1, 2, \dots, N, i = 1, 2, \dots, M)$$

$$y_j = \begin{bmatrix} y_j^{(1)} \\ y_j^{(2)} \\ \vdots \\ y_j^{(N)} \end{bmatrix}, a_j = \begin{bmatrix} a_j(1) \\ a_j(2) \\ \vdots \\ a_j(M) \end{bmatrix}, e_j = \begin{bmatrix} e_j^{(1)} \\ e_j^{(2)} \\ \vdots \\ e_j^{(N)} \end{bmatrix}$$

The RBF networks have good generalization ability and can learn whichever nonlinear mapping function we are dealing with.

4 Learning a phrase model

A phrase model is a set of player's characteristic phrases. To create a virtual player that performs using phrases as an actual human player does, acquiring the actual player's individual phrase model is necessary. This can be done through musical segmentation of a MIDI session recording (Figure 6).

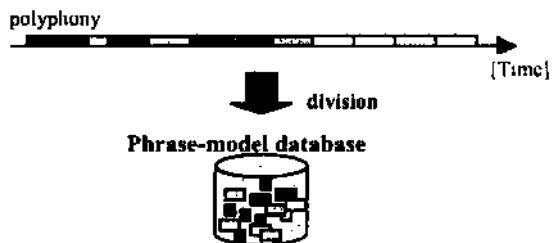


Figure 6: Acquiring phrase model.

Two kinds of grouping appear in polyphony, one in the direction of pitch interval and the other in the direction of time. Grouping in the pitch interval direction divides polyphony into multiple homophony (Figure 7a). In the time direction, notes are grouped from time gap to time gap (Figure 7b).

To segment a MIDI session recording into phrases, we need to automatically divide the polyphony notes into groups. The generative theory of tonal music (GTTM) [Lerdahl and Jackendoff, 1983] includes a grouping concept, and thus can be used to derive a set of rules for the division of notes into groups. We think that GTTM is the most promising theory of music in terms of computer implementation; however, no strict order exists for applying the rules of GTTM. This may lead to ambiguities in terms of analysis results. The implementation of GTTM as a computer system has been attempted [Ida et al., 2001], but the resulting system was only capable of dealing with a limited polyphony made up of two monophonies.

In this paper, we propose a method of grouping based on applying the Voronoi diagram. We have developed a method of grouping rather than naively implementing GTTM so that a result obtained using our method is equifinal to one obtained with the GTTM approach. We

a: Grouping in pitch interval direction.



b: Grouping in time direction.

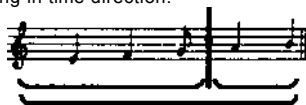


Figure 7: Examples of grouping.

compare the results of grouping by our method with the results of grouping by a human according to the GTTM.

4.1 Generative Theory of Tonal Music

The generative theory of tonal music is composed of four modules, each of which is assigned to a separate part of the structural description of a listener's understanding of music. The four GTTM modules are the *grouping structure*, the *metrical structure*, the *time-span reduction*, and the *prolongational reduction*.

The grouping structure is intended to formalize the intuition that tonal music is organized into groups, which are in turn composed of subgroups. There are two kinds of rules for GTTM grouping: *grouping well-formedness rules* and *grouping preference rules*. Grouping well-formedness rules are necessary conditions for the assignment of a grouping structure and restrictions on the generated structures. When more than one structure may satisfy the grouping well-formedness rules, grouping preference rules only suggest the superiority of one structure over another; they do not represent a deterministic procedure. This can lead to the problem of ambiguity mentioned above.

4.2 Use of Voronoi diagrams for grouping

To overcome the ambiguity problem, we propose a method of grouping based on the use of Voronoi diagrams. The GTTM result is a binary tree that indicates the hierarchical structure of a piece of music. In our method, Voronoi diagrams on a piano-roll represent the hierarchical structure of a piece of music.

Voronoi diagram

A Voronoi diagram partitions a plane into cells (Figure 8) designated by the set of points $P = \{p_1, p_2, \dots, p_n\}$ - such that for each cell corresponding to point p_i , all points q in that cell are nearer to p_i than to any other point in P [Aurenhammer, 1991]:

$$\text{dist}(q, p_i) < \text{dist}(q, p_j) \quad (p_i, p_j \in P, j \neq i) \quad (4)$$

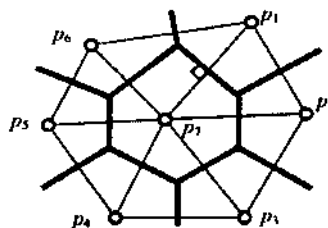


Figure 8: Voronoi diagram.

We can form the Voronoi diagram for a given set of points in a plane as a connected set of segments of half-plane boundaries, where each of the half-planes is formed by partitioning the plane into two half-planes, one on either side of the bisector of the line between each adjacent pair p_i and p_j .

Voronoi diagram for two notes

Our method uses the piano-roll format as a score, and thus notes are expressed as horizontal line segments on a piano-roll. To construct a Voronoi diagram on the score, we need to consider the Voronoi diagram for multiple horizontal line segments, which will be constructed of linear segments and quadratic segments.

When two notes sound at the same time or no note sounds, the corresponding part of the Voronoi diagram is a linear segment (Figures 9a and 9c). When a single note sounds, the Voronoi diagram becomes a quadratic segment (Figure 9b).

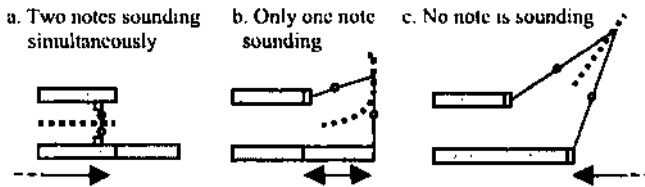


Figure 9: Voronoi diagrams for pairs of notes.

Voronoi diagram for more than two notes

To construct a Voronoi diagram for more than two notes, we construct the Voronoi diagrams for all note pairs and delete the irrelevant segments. For example, to construct a Voronoi diagram for notes a, b, and c, we construct three Voronoi diagrams (Figure 10). The boundaries in the three diagrams then intersect at a point that is equidistant from each note. The Voronoi diagram for notes a and b is divided into two half-lines at the intersection. We then delete the half-line that is closer to c than to a or b.

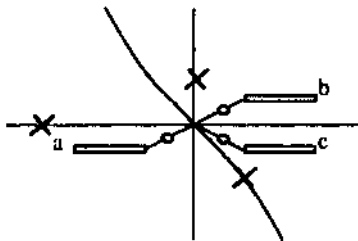


Figure 10: Voronoi diagram for more than two notes.

4.3 Making groups

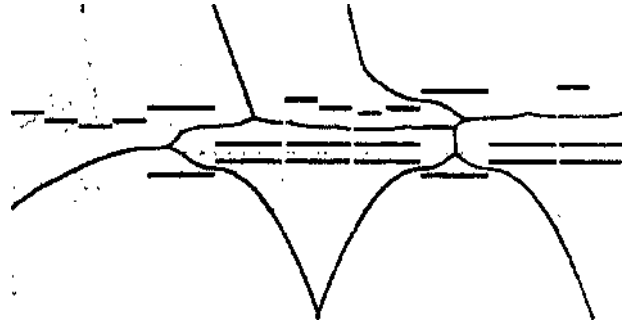
Hierarchical groups of notes were constructed by converging adjacent notes iteratively. Here, we introduce the following principle for making groups; the smallest Voronoi cell is first merged to an adjacent group.

We have implemented our grouping method (Figure 11a) and have compared the results with correct data obtained by a human (Figure 11b). We evaluated grouping performance in terms of a correctness rate defined as

$$\text{Correctness rate} = \frac{\text{The number of notes grouped correctly}}{\text{The number of notes}} \quad (5)$$

When we ran the program, we calculated that the correctness rate was 78.5 percent. The tune used as MIDI data in this experiment was the *Turkish March*.

a. Result obtained using our method.



b. Result obtained using GTTM.

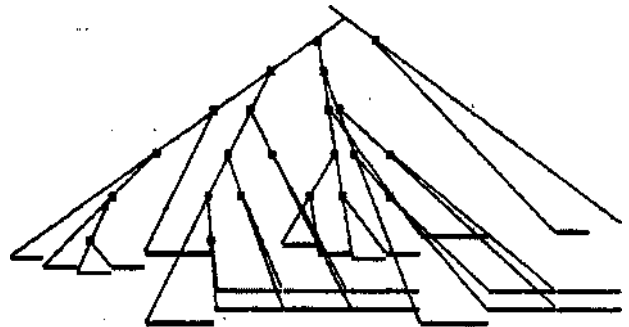


Figure 11: Results obtained using our method and GTTM.

5 Learning a groove model

A groove model is a model generating the deviation of onset times. Acquiring an actual player's individual groove model is necessary to create a virtual player that performs with musical expression as that human player does. A human player, even when repeating a given phrase on a MIDI-equipped instrument, rarely produces exactly the same sequence of onset notes because the onset times deviate according to performer's actions and expressions. We can model the process generating that deviation by using a probabilistic model.

5.1 Formulation of the hidden Markov models

Let a sequence of intended (normalized) onset times be O and a sequence of performed onset times (with deviation) be y . Then, a model for generating the deviation of onset times can be expressed by a conditional probability $P(y|O)$ (Figure 12). Using this conditional probability and the prior probability $P(O)$ can be formulated as a hidden Markov model (HMM), which is a probabilistic model that generates a transition sequence of hidden states as a Markov chain. Each hidden state in the state transition sequence then generates an observation value according to an observation probability.

Modeling of performance

Target in modeling

We modeled the onset time of a musical note (i.e. the start time of the note) and introduced a new model of distribution of onset times. While the duration-time-based model

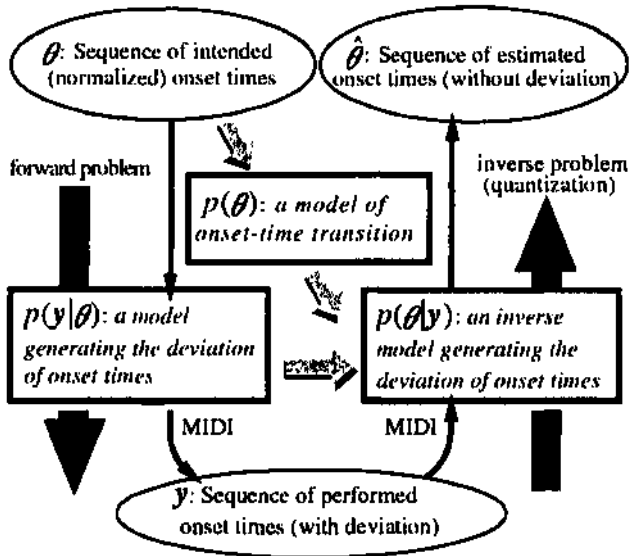


Figure 12: Model to generate onset time deviation.

used in [Otsuki *et al.*, 2002] is limited, our onset-time-based model is suitable for treating polyphonic performances, such as those including two-hand piano voicing and guitar arpeggio.

Unit in modeling

We use a quarter note (beat) as the unit of each HMM: the temporal length corresponding to each HMM is a quarter note. The reason we use the quarter-note unit is to distinguish between eighth triplets and sixteenth notes within the scope of quarter notes. The three notes of eighth triplets are located on three equi-divided positions in a quarter note, while the four sixteenth notes are located on four equi-divided positions in a quarter note. An actual per-

formance consisting of a sequence of quarter notes can be modeled by concatenating the quarter-note-length HMMs. This quarter-note modeling has the advantages of reducing calculation time and facilitating the preparation of the large data sets used for training the model.

Unit of quantization

We introduce two different discrete temporal indices, k and i . The unit of k is a quantization unit to describe performed onset time and is 1/480 of a quarter note, which is often used in commercial sequencing software. The i unit is a quantization unit to describe the intended onset time and is one-twelfth of a quarter note. It can describe both eighth triplets and sixteenth notes.

Quarter-note hidden Markov model

Figure 13 shows the HMM used in our study. We model a sequence of onset times within a quarter note (beat) by using the HMM. All the hidden states of the HMM correspond to possible positions of intended onset times, and an observed value that comes from a hidden state corresponds to a performed onset time with deviation. Onset times in a beat are quantized into 12 positions for hidden states and into 480 positions for observation values. That is, each component of the HMM is interpreted as follows.
 Hidden state i : intended onset time. ($i = 1, \dots, 12$)
 Observation k : performed onset time. ($k = 1, \dots, 480$)
 Transition probability a_{ij} : probability that intended onset time j follows intended onset time i .
 Observation probability $b_i(k)$: probability that performed onset time is k and intended onset time is i .
 A state-transition sequence begins with a dummy state "Start" and ends with a state "End" (Figure 14).

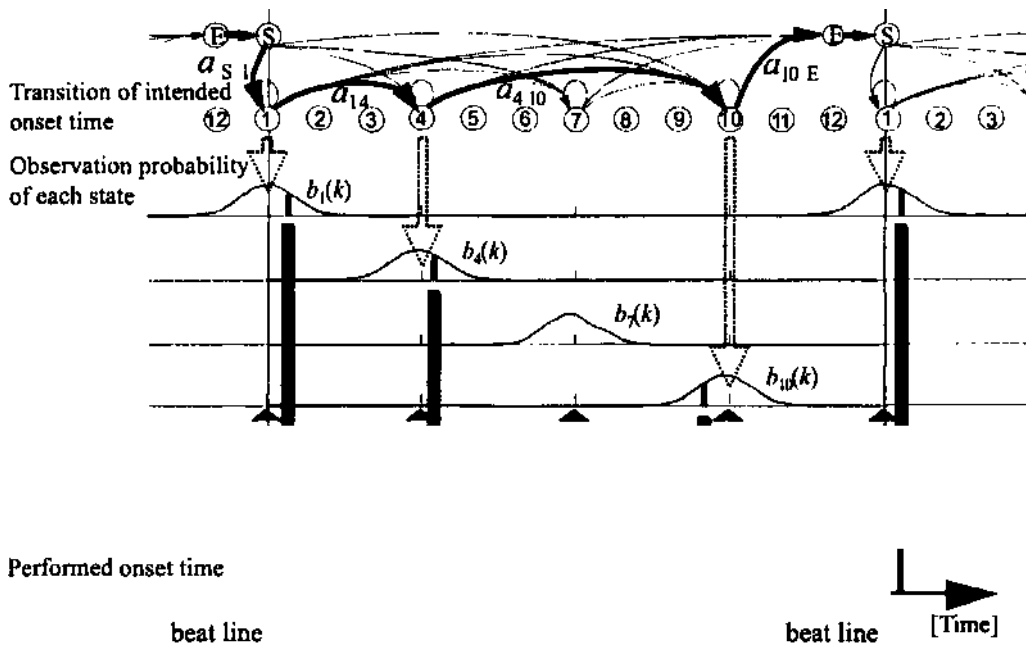


Figure 13: Overview of quarter-note hidden Markov model

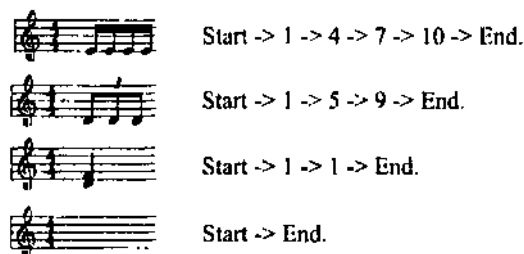


Figure 14: Simple example of state sequences.

5.2 Learning model parameters

The HMM parameters a_{ij} and $b_i(k)$ were derived from a MIDI session recording by using the Baum-Welch algorithm. Figure 15 shows a $b_i(k)$ distribution obtained from a human performance in a MIDI session recording.

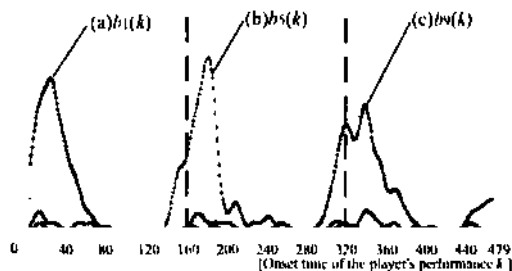


Figure 15: $b_1(k)$, $b_5(k)$, $b_9(k)$ obtained from human-performance data.

6 Session mode

Using the personality models acquired in the learning mode, each virtual player improvises while reacting to the human player and the other virtual player. The processing flow of each virtual player can be summarized as follows:

1. The low-level features of the MIDI performances of all the players are calculated at every $1/48$ bar.
2. At every $1/12$ bar, the three impression vectors are obtained from the low-level features.
3. At the beginning of every bar, the intention vector is determined by feeding the reaction model the past impression vectors.
4. The output performance is generated by connecting short phrases selected from a phrase-model database. Each phrase is selected, according to the determined intention vector, by considering its fitness for the chord progression. A virtual player can start a solo performance at any bar.
5. The deviation of the onset times is generated according to the groove model.

Note that the reaction model can predict the next intention vector from the impression vectors gathered during the past twelve bars in real time: a virtual player thus does not fall behind the other players.

7 Experimental Results

We have implemented the proposed system on a personal computer (with a Pentium IV 2.8GHz processor); Figure

16 shows a screen snapshot of the system output. As shown, there are three columns (called *player panels*), each corresponding to a different player. The toggle switch on the top of each panel indicates whether the panel is for a virtual player or a human player, and each panel contains two boxes representing three-dimensional spaces: the upper box is the impression space and the lower box is the intention space. The sphere in each box indicates the current value of the impression or intention vector.

In our experiments, after recording a session performance of three human guitarists playing MIDI guitars, we first made the system learn the reaction model, the phrase model and the groove model of each. We used a metronome sound to maintain the tempo (120 MM) when recording, and the total length of this recording session was 144 bars. We then let five human guitarists individually use the system in session mode. The system indeed enabled each human guitarist to interact with two virtual guitarists, each with a different reaction model.

To find out how well a virtual player could imitate a human player, we asked a human player to perform with virtual player A imitating him and with virtual player B imitating a different player. The human player and the virtual player imitating him tended to take a solo at almost the same time and to perform phrases that felt similar. Figure 17 shows the transition of intention vectors of three players during 48 bars where the intention vectors of the virtual player A and the human player are particularly similar. Examining all the values of the intention vectors during the session, we compared the distances between the intention vectors of the virtual players and the human player. Over 144 bars the average distance between the intention vectors of the human player and the virtual player imitating him was significantly smaller than that between the intention vectors of the human player and the virtual player imitating a different player. We think that this means the virtual player's RBF networks actually predicted the human player's intention.

We also tested whether a virtual player could imitate the target human player by applying the Turing test format. As subjects, we used three guitarists (A, B, and C) who had played in the same band for more than a year and so un-

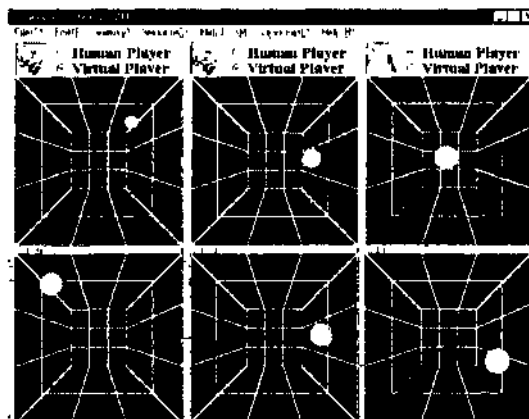


Figure 16: Screen snapshot of system output.

derstood each other's musical personalities. We prepared a reaction model, a phrase model, and a groove model for each of these subjects. We then used different personality models to prepare 27 (= 3 players ^A 3 models) kinds of virtual player. The subjects evaluated each virtual player with regard to whose models it was based upon. Subjects were told in advance that the player was a virtual player imitating either player A, B, or C. We found that a virtual player having the three personality models acquired from the same human player was correctly identified as such. We calculated that the success rate was 100 percent. The subjects could thus distinguish when the virtual player was based on the personality models from one human player or from multiple players.

Furthermore, five guitarists who performed with the system remarked that each virtual player performed characteristically. In particular, a human player who participated in a jam session with a virtual player that was imitating him remarked that he was uncomfortable playing with that virtual player because he felt that he was being mimicked. These results show that our system successfully derived and applied personality models from MIDI session recordings.

8 Conclusion

We have described a jam session system in which a human player and virtual players interact with each other. The system is based on the learning of three types of personality model - the reaction, the phrase, and the groove models. Our experimental results show that our system can imitate the musical personalities of human players. We plan to extend the system so that it can be applied to other musical instruments, such as piano and drums.

Acknowledgments

We thank Daisuke Hashimoto, Shinichi Chida, and Yasuhiro Saita, who cooperated with the experiment as players.

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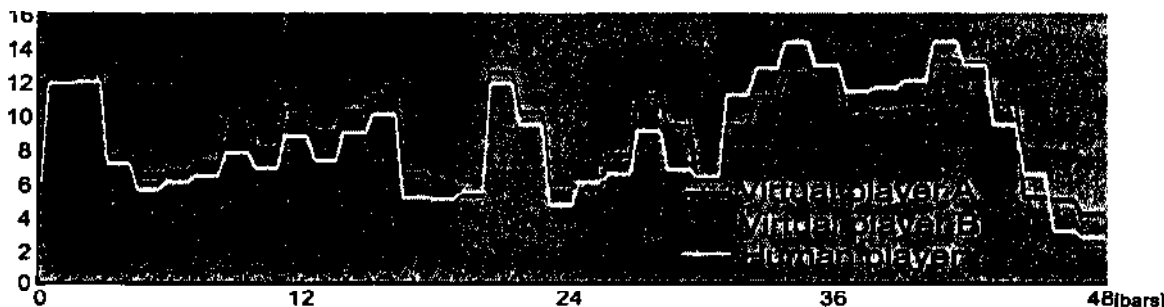


Figure 17: Transition of intention vectors of three players. (This Figure charts one component of intention vectors that have three components.)