

# A Classification of Weak Asynchronous Models of Distributed Computing

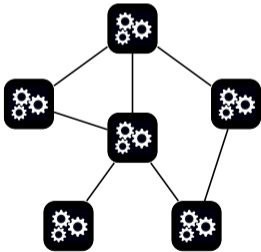
Javier Esparza<sup>1</sup>   Fabian Reiter<sup>2</sup>

<sup>1</sup>Technische Universität München


<sup>2</sup>Université Gustave Eiffel

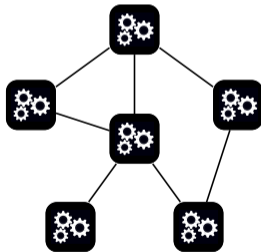
1 September 2020 @ CONCUR'20, Online

# The framework




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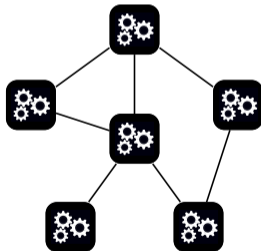
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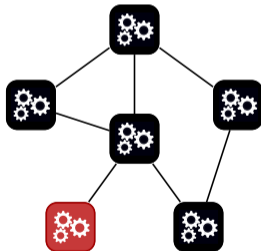
Is there a red node?




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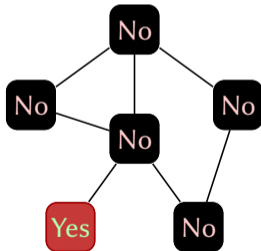
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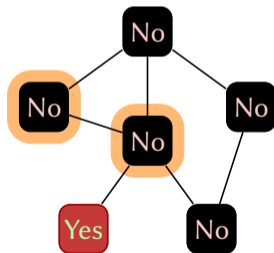
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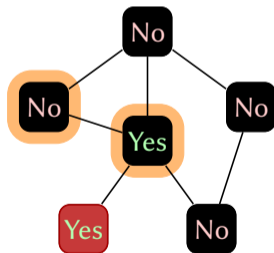
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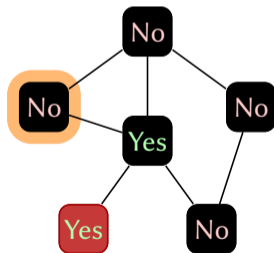





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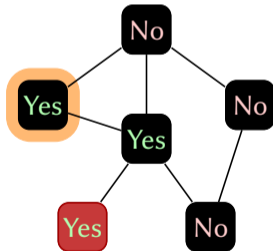
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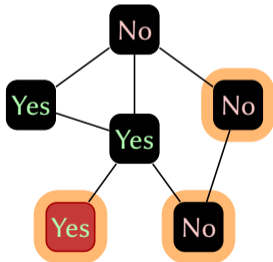
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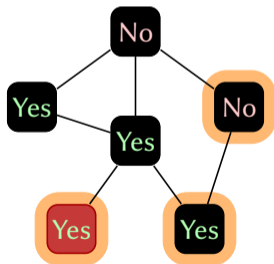
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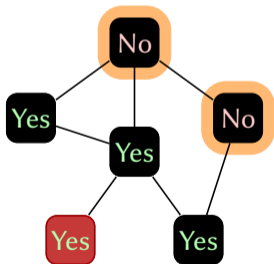
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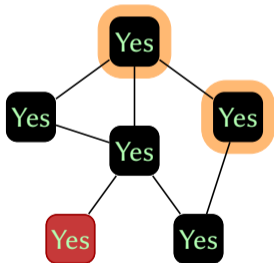
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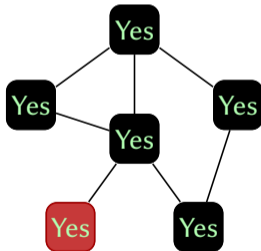
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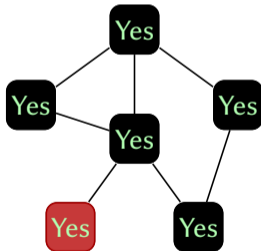
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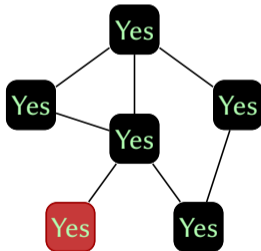
*Easy if nodes can change their answer.*



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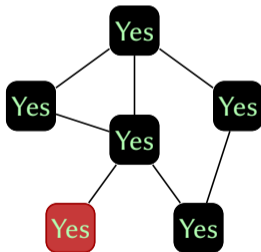


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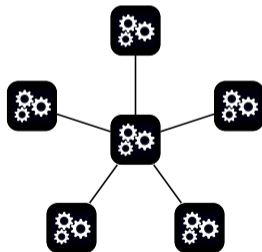
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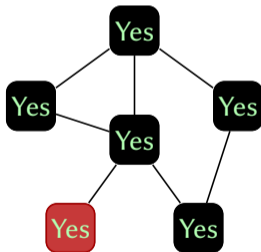
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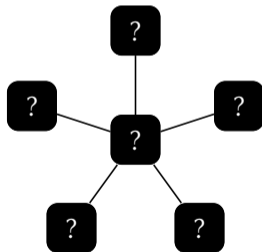
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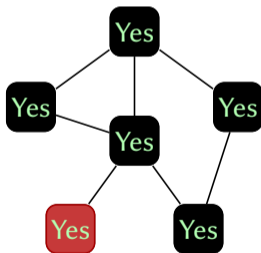
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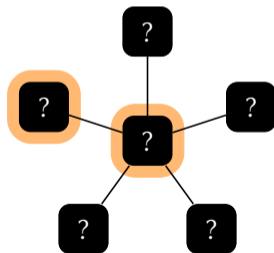
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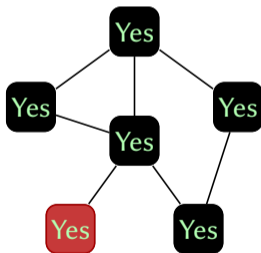
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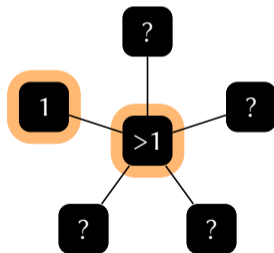
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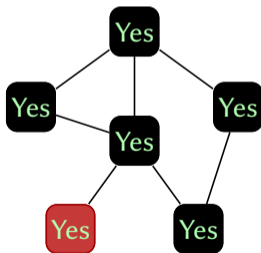
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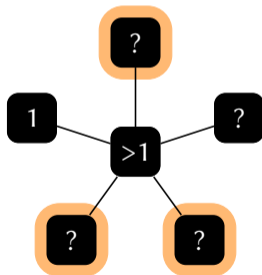
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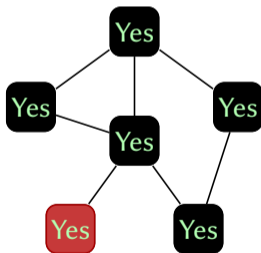
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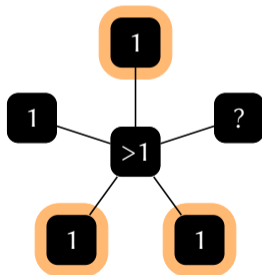
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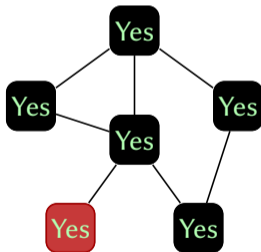
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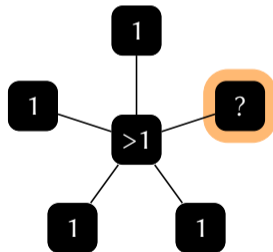
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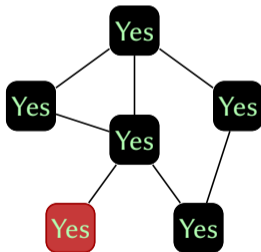




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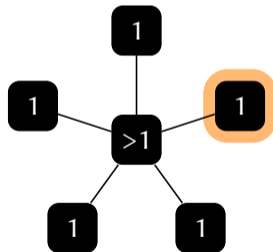
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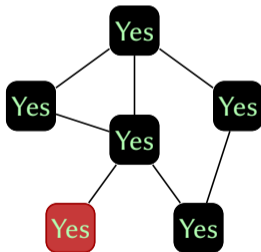
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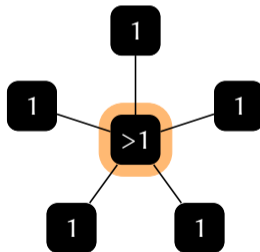
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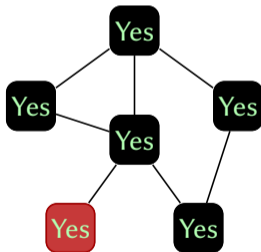
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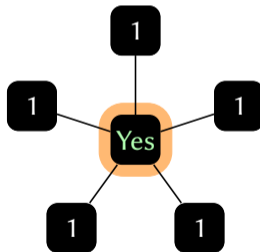
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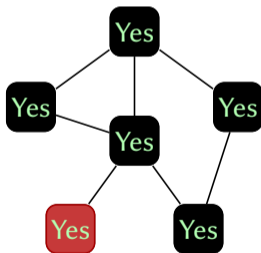
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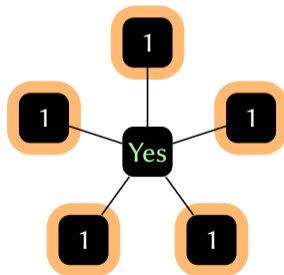
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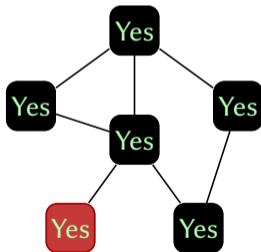
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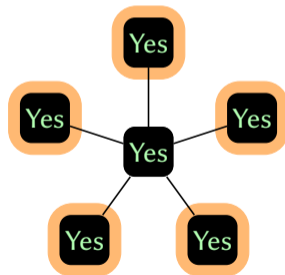
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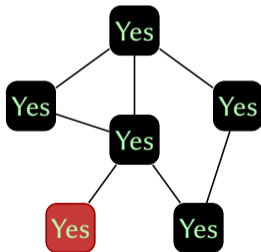
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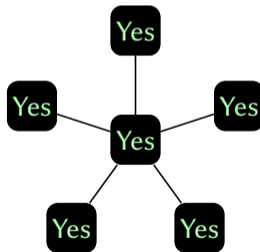
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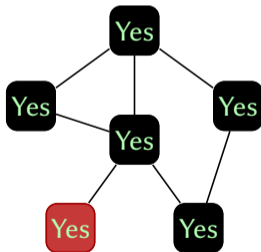
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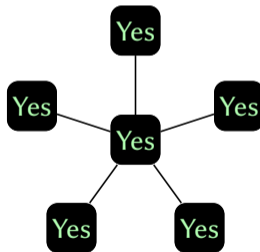
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*Easy if nodes can change their answer.*

Is the graph a star?



*Easy if nodes can count their neighbors.*

# Four parameters

Detection

Acceptance

Selection

Fairness

---



# Four parameters

Detection

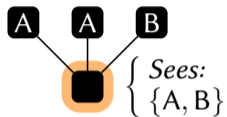
Acceptance

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Fairness

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**d**: non-counting



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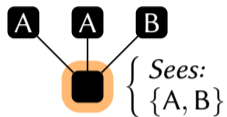
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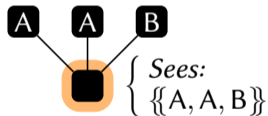
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**D**: counting



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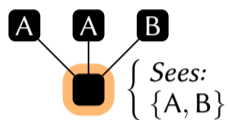
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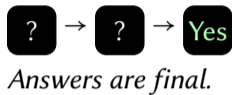
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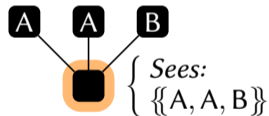
**d:** non-counting



**a:** halting



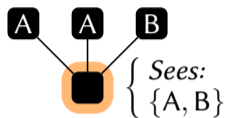
**D:** counting



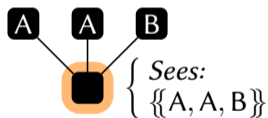
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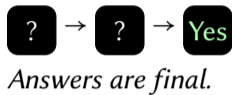


**D:** counting

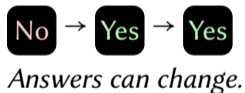


Acceptance

**a:** halting



**A:** stabilizing



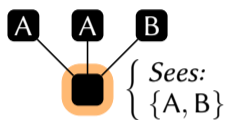
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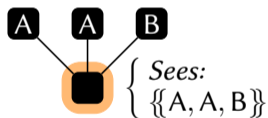
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## Detection

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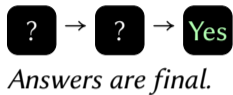


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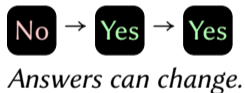


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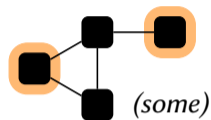


**A:** stabilizing



## Selection

**s:** liberal

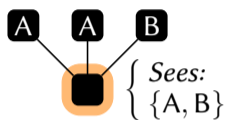


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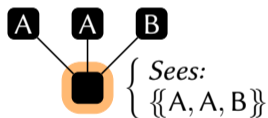
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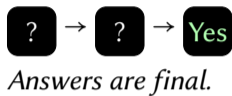


**D:** counting

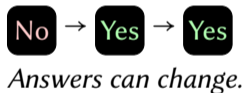


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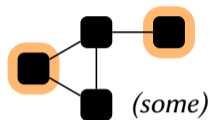


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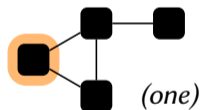


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**S:** exclusive

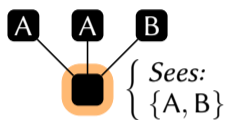


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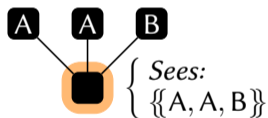
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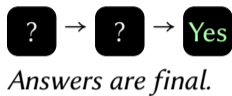


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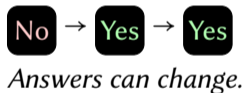


## Acceptance

**a:** halting

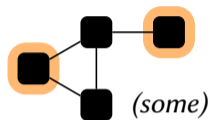


**A:** stabilizing

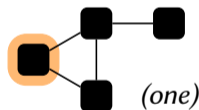


## Selection

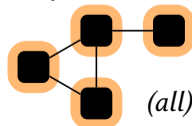
**s:** liberal



**S:** exclusive



**\$:** synchronous

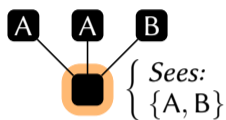


## Fairness

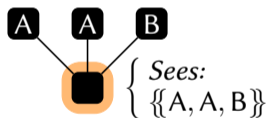
# Four parameters

## Detection

**d:** non-counting

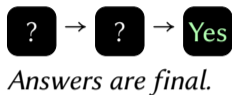


**D:** counting

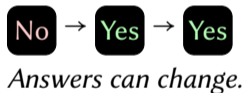


## Acceptance

**a:** halting

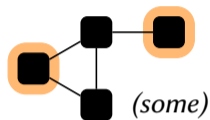


**A:** stabilizing

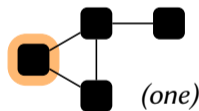


## Selection

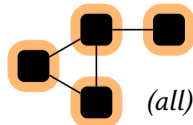
**s:** liberal



**S:** exclusive



**\$:** synchronous



## Fairness

**f:** starvation-free

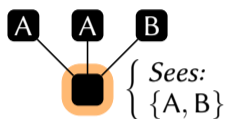
*Every node selected infinitely often.*



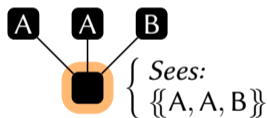
# Four parameters

## Detection

**d:** non-counting

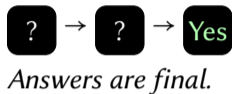


**D:** counting

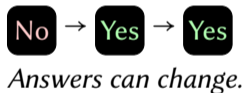


## Acceptance

**a:** halting

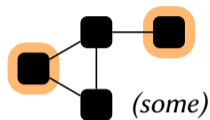


**A:** stabilizing

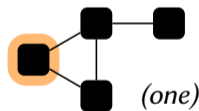


## Selection

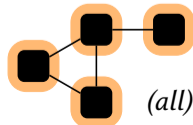
**s:** liberal



**S:** exclusive



**\$:** synchronous



## Fairness

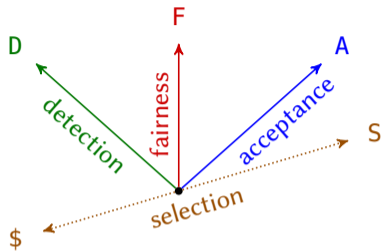
**f:** starvation-free

*Every node selected infinitely often.*

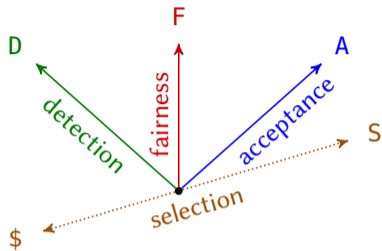
**F:** stochastic-like

*Every sequence of selections occurs infinitely often.*

# Main result

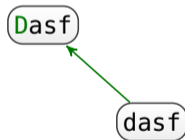
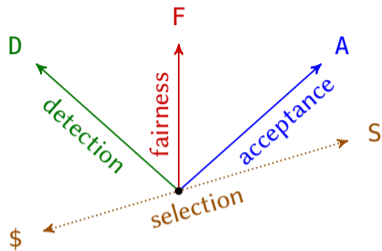


# Main result

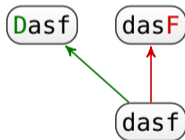
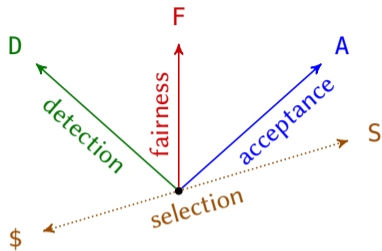


dasf

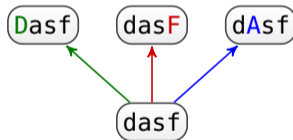
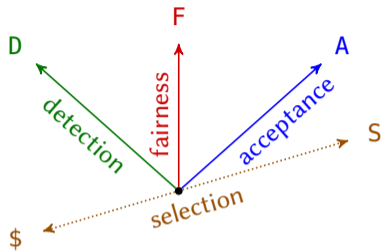
# Main result



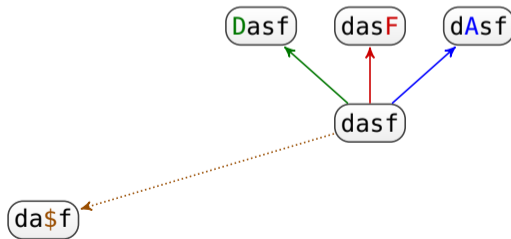
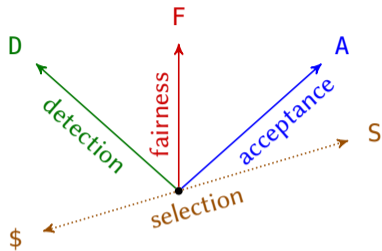
# Main result



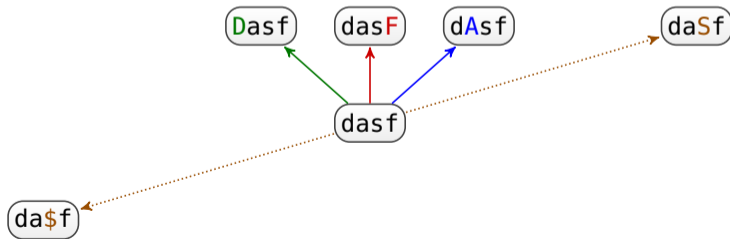
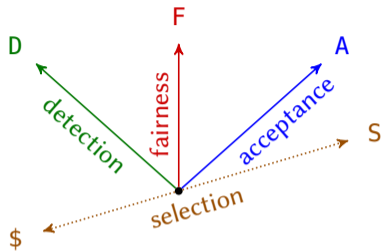
# Main result



# Main result

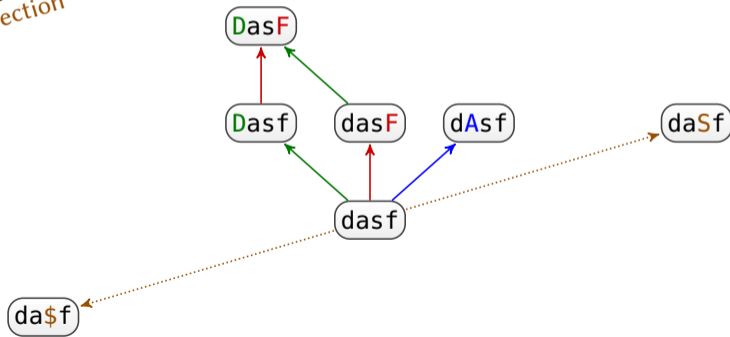
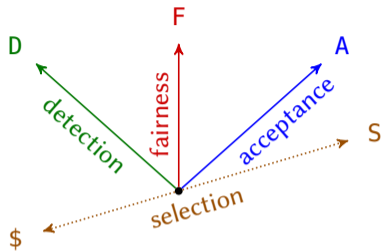


# Main result

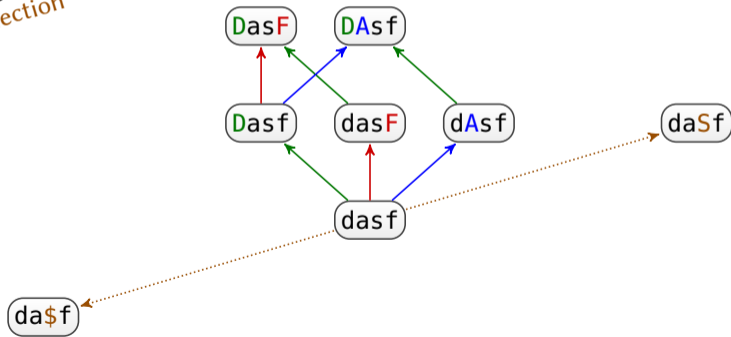
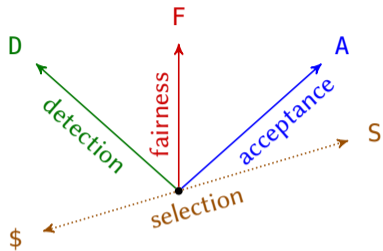




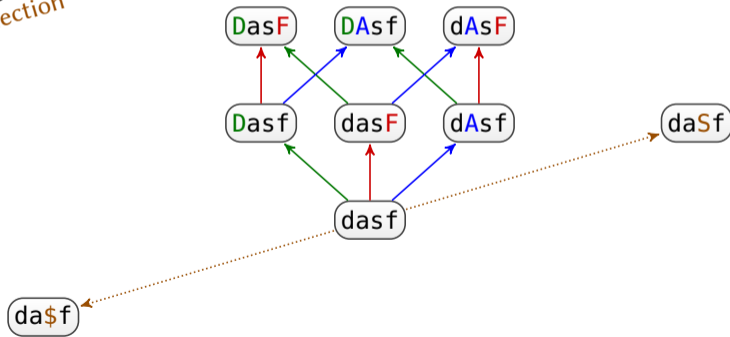
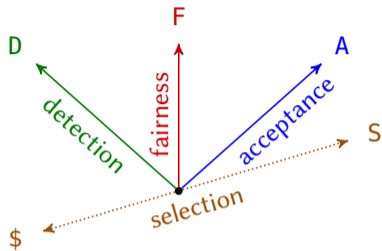
# Main result



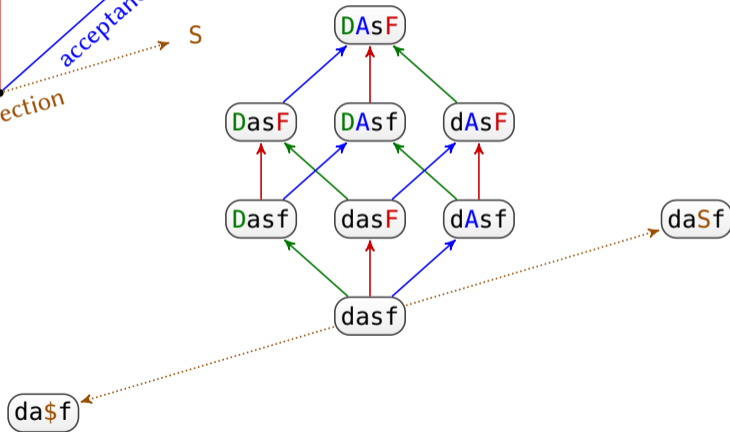
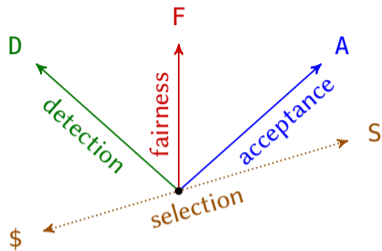
# Main result



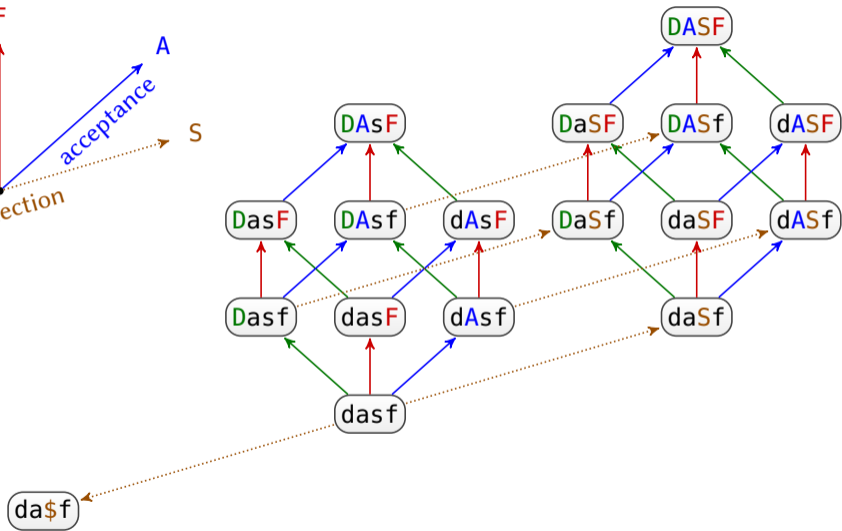
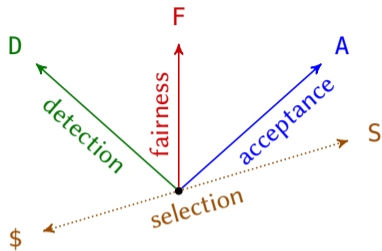
# Main result



# Main result

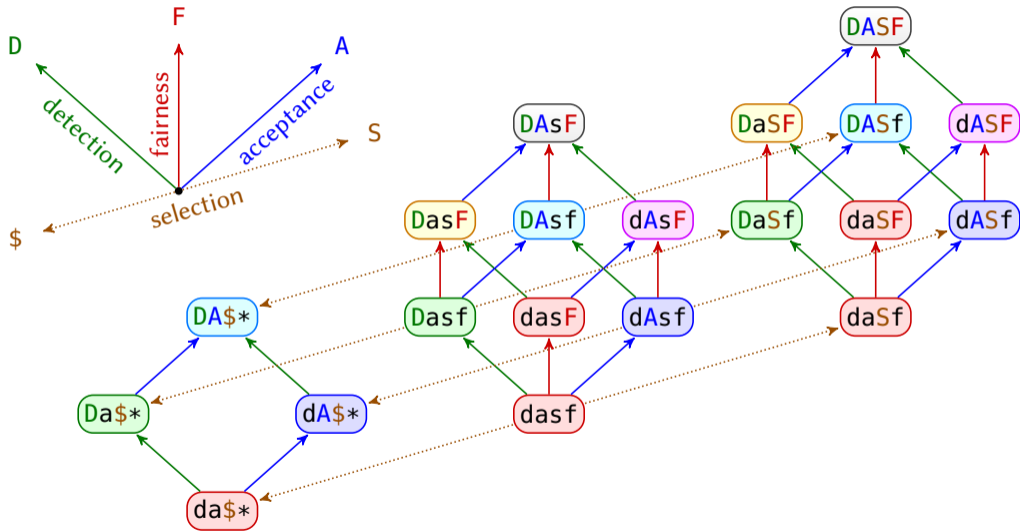


# Main result

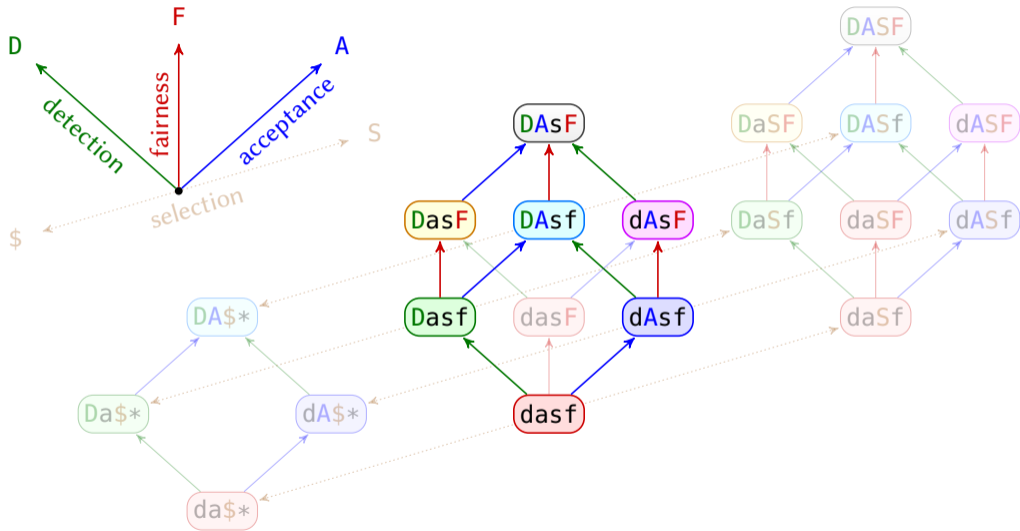




# Main result

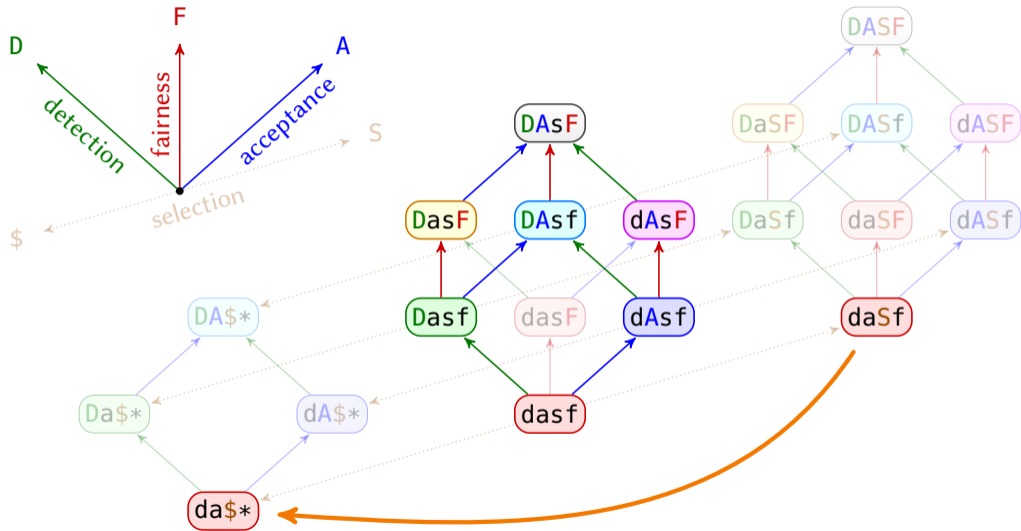


# Main result





# Main result



# Exclusivity does not increase expressiveness

Synchronous selection  $\text{da}\$*$



Exclusive selection  $\text{daSf}$

# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



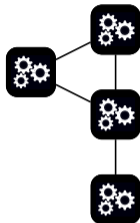
Exclusive selection  $**Sf$

# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

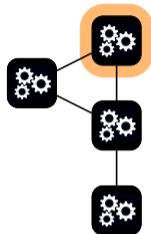


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

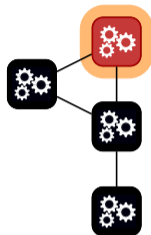


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

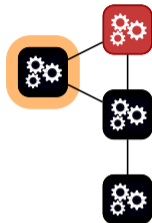


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

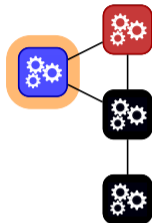


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$



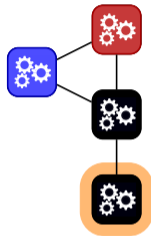


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

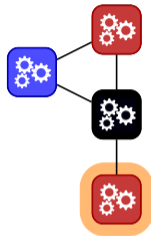


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

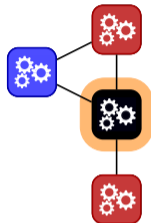


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

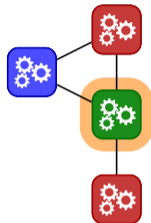


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

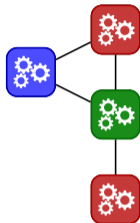


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

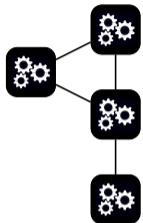


Exclusive selection  $**Sf$



# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

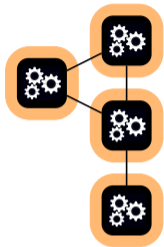


Exclusive selection **\*\*Sf**

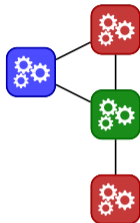


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

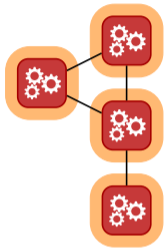


Exclusive selection **\*\*Sf**



# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



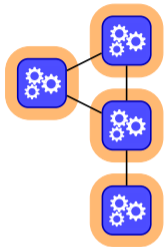
Exclusive selection  $**Sf$



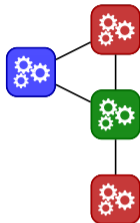


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

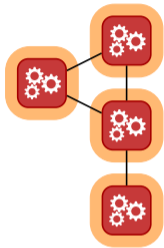


Exclusive selection  $**Sf$



# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

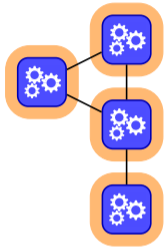


Exclusive selection  $**Sf$



# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

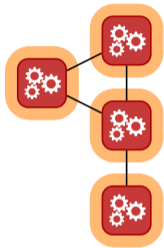


Exclusive selection **\*\*Sf**



# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

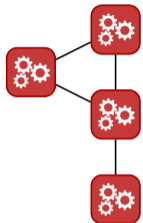


Exclusive selection  $**Sf$



# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

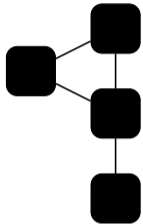


Exclusive selection **\*\*Sf**

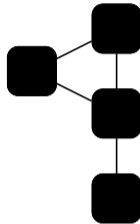


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

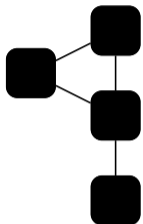


Exclusive selection **\*\*Sf**



# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

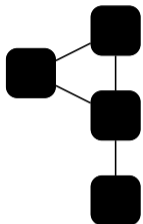


Exclusive selection **\*\*Sf**

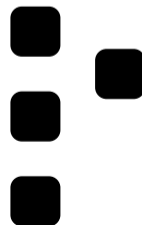
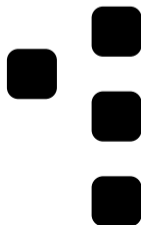
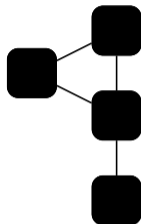


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***



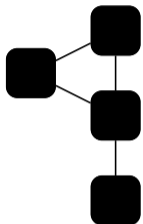
Exclusive selection **\*\*Sf**



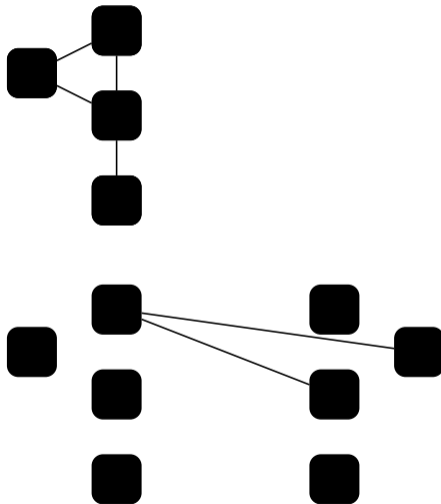


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

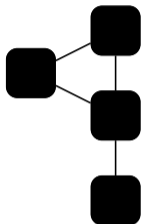


Exclusive selection **\*\*Sf**

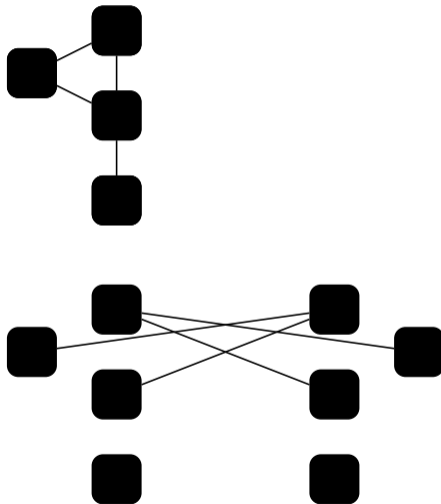


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

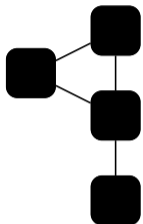


Exclusive selection **\*\*Sf**

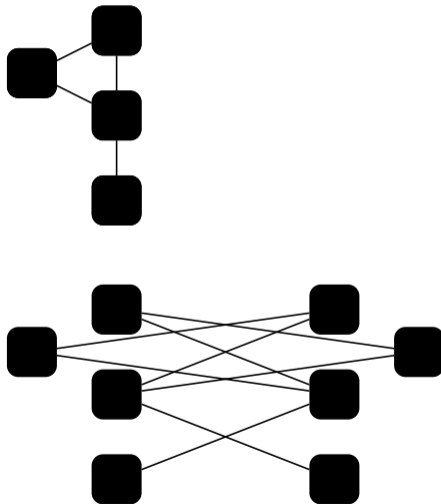


# Exclusivity does not increase expressiveness

Synchronous selection **\*\*\$\***

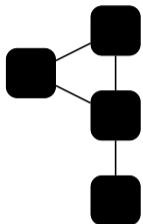


Exclusive selection **\*\*Sf**

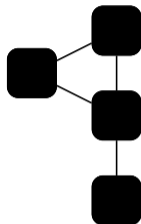


# Exclusivity does not increase expressiveness

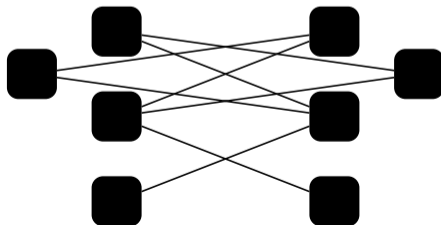
Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

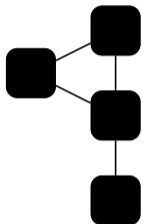


*Kronecker  
cover*

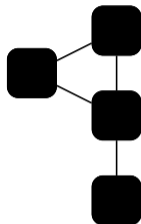


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

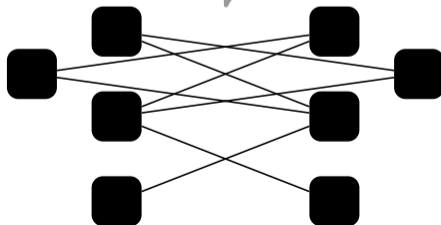


Exclusive selection  $**Sf$



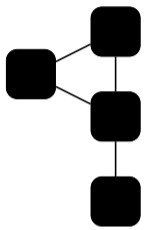
indistinguishable

*Kronecker  
cover*

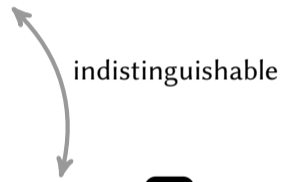
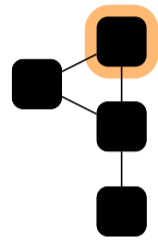


# Exclusivity does not increase expressiveness

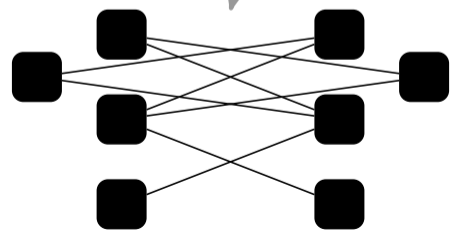
Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

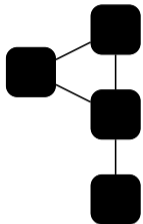


*Kronecker cover*

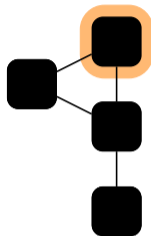


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

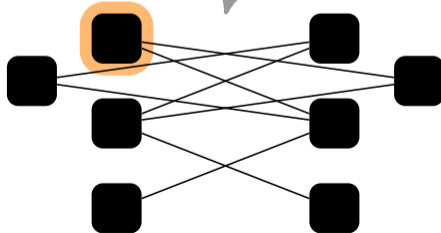


Exclusive selection  $**Sf$



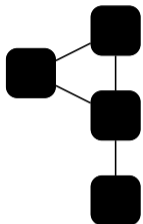
indistinguishable

*Kronecker  
cover*

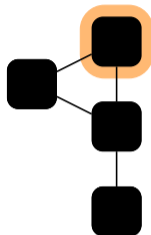


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

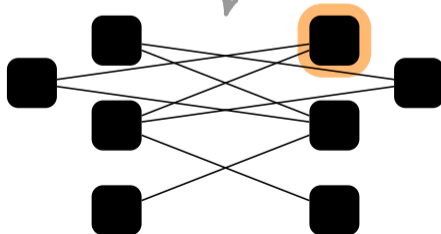


Exclusive selection  $**Sf$



indistinguishable

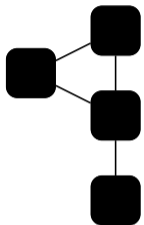
*Kronecker  
cover*



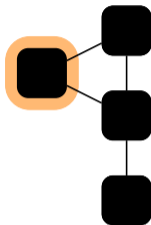


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

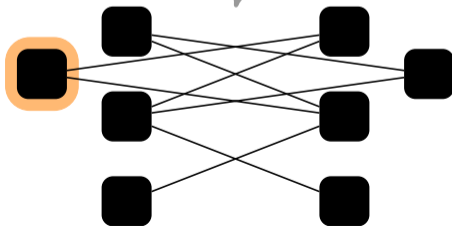


Exclusive selection  $**Sf$



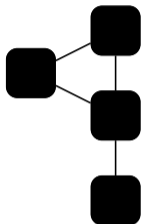
indistinguishable

*Kronecker cover*

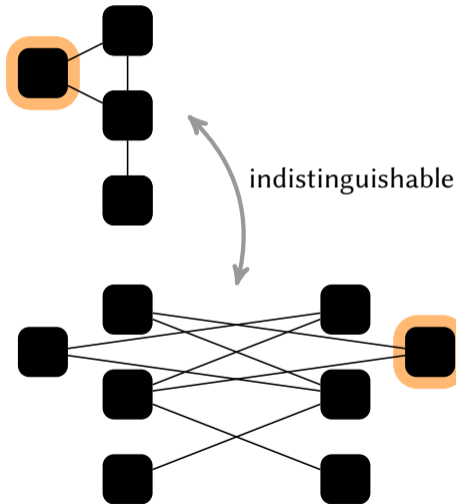


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

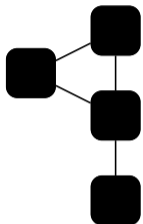


← Exclusive selection  $**Sf$

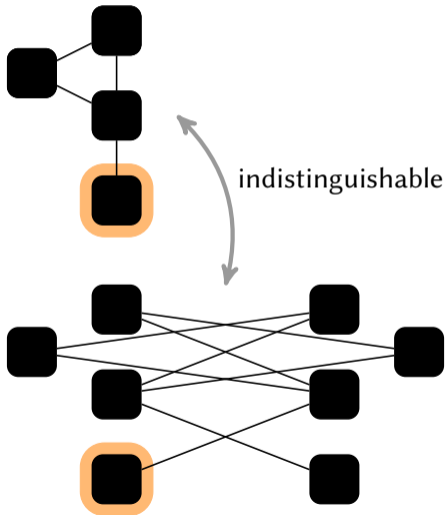


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

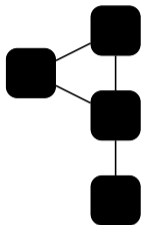


Exclusive selection  $**Sf$

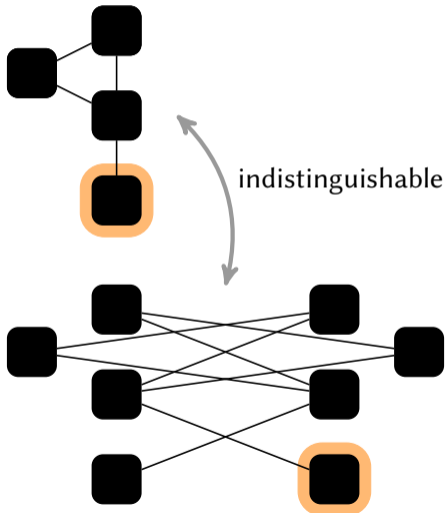


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

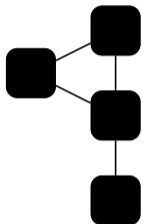


Exclusive selection  $**Sf$

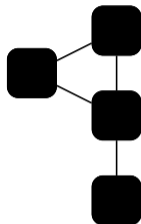


# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$

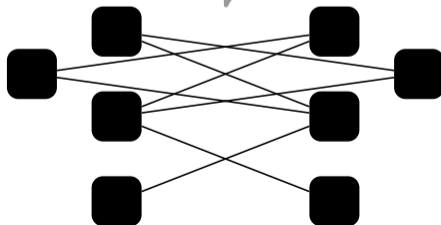


Exclusive selection  $**Sf$



indistinguishable

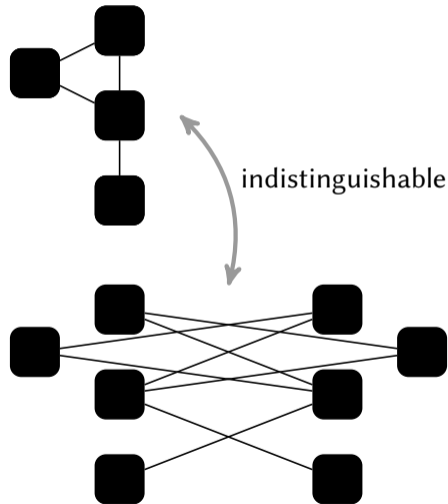
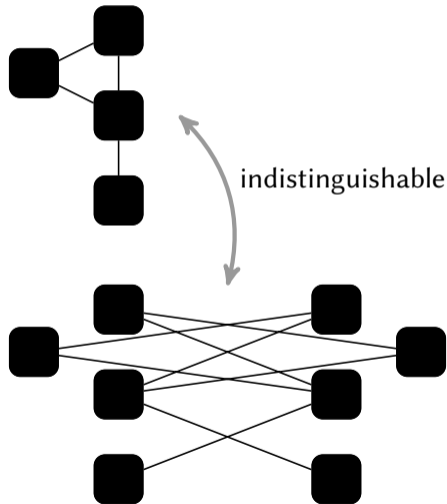
*Kronecker  
cover*



# Exclusivity does not increase expressiveness

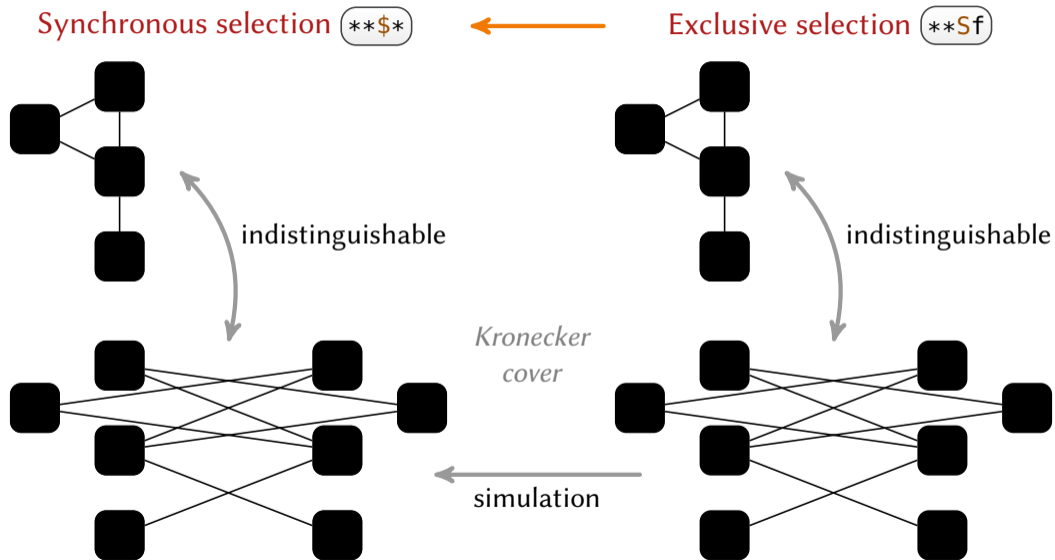
Synchronous selection  $**\$*$

Exclusive selection  $**Sf$

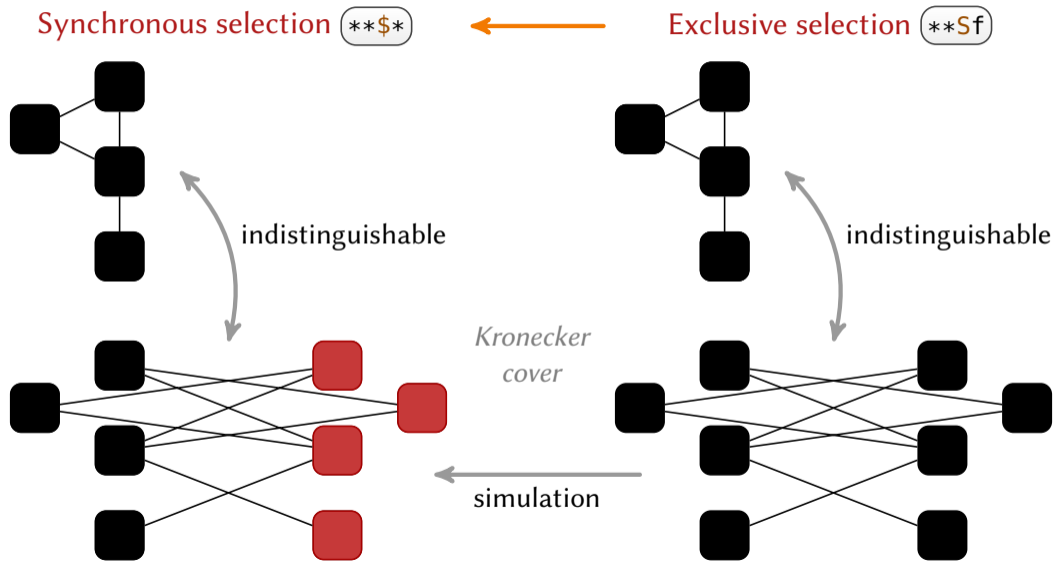


*Kronecker  
cover*

# Exclusivity does not increase expressiveness

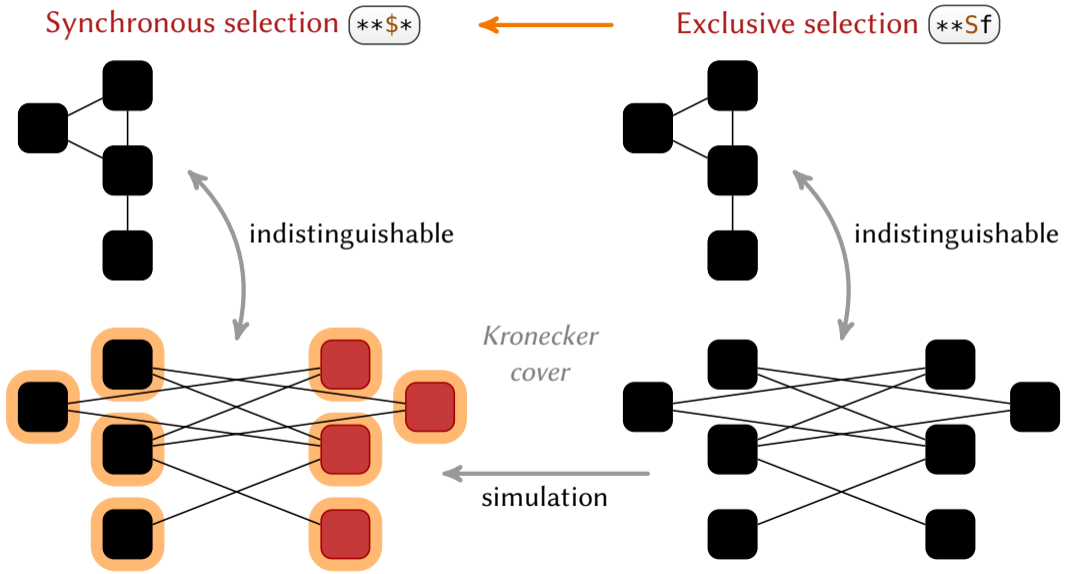


# Exclusivity does not increase expressiveness

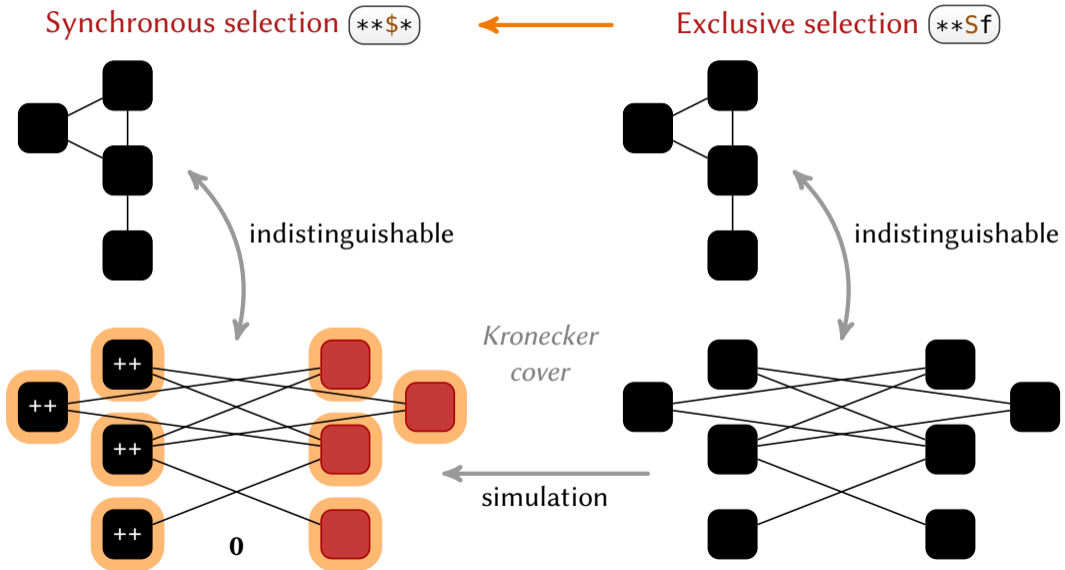




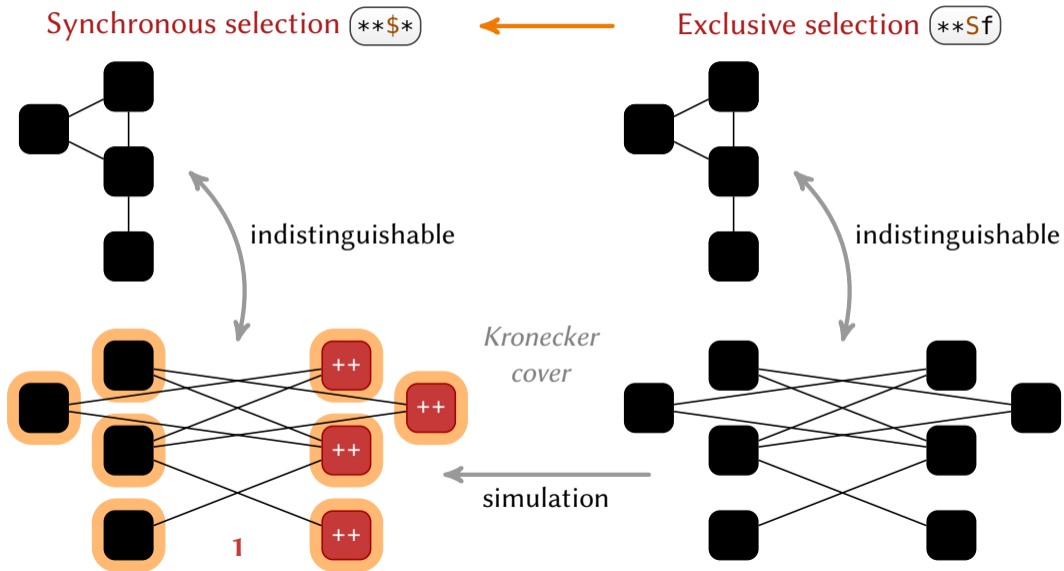
# Exclusivity does not increase expressiveness



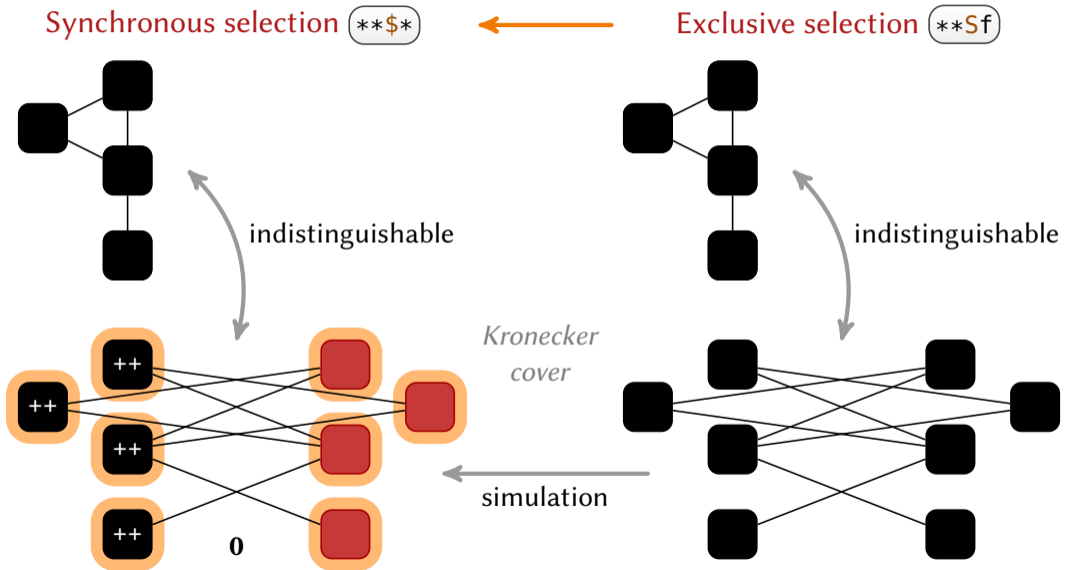
# Exclusivity does not increase expressiveness



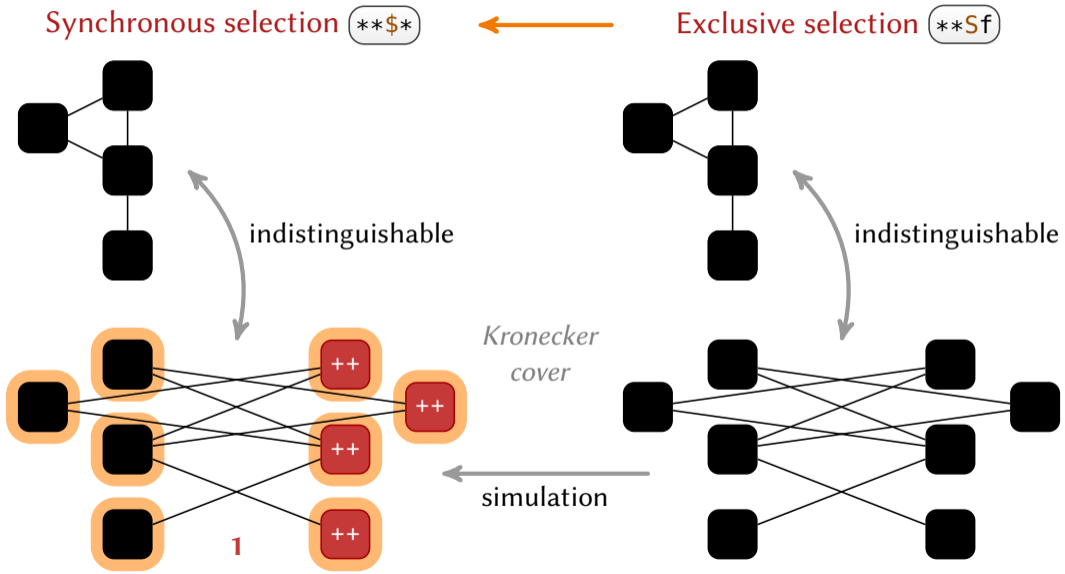
# Exclusivity does not increase expressiveness



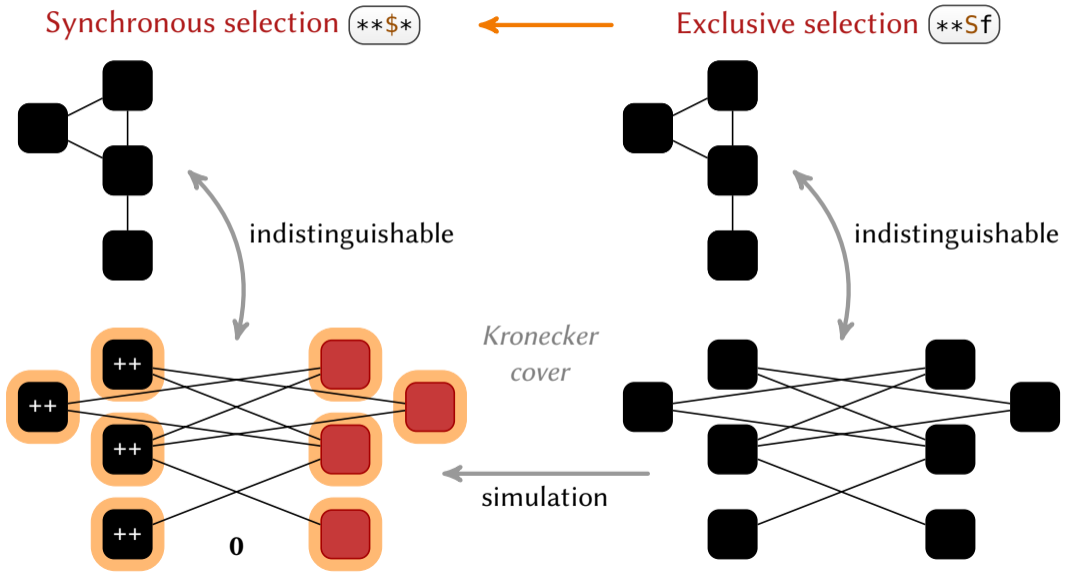
# Exclusivity does not increase expressiveness



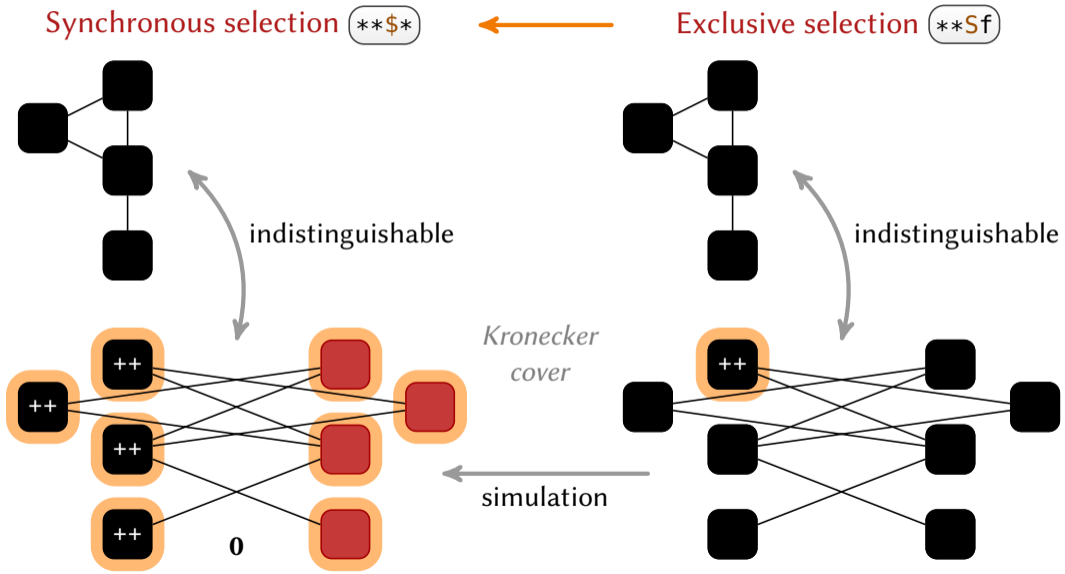
# Exclusivity does not increase expressiveness



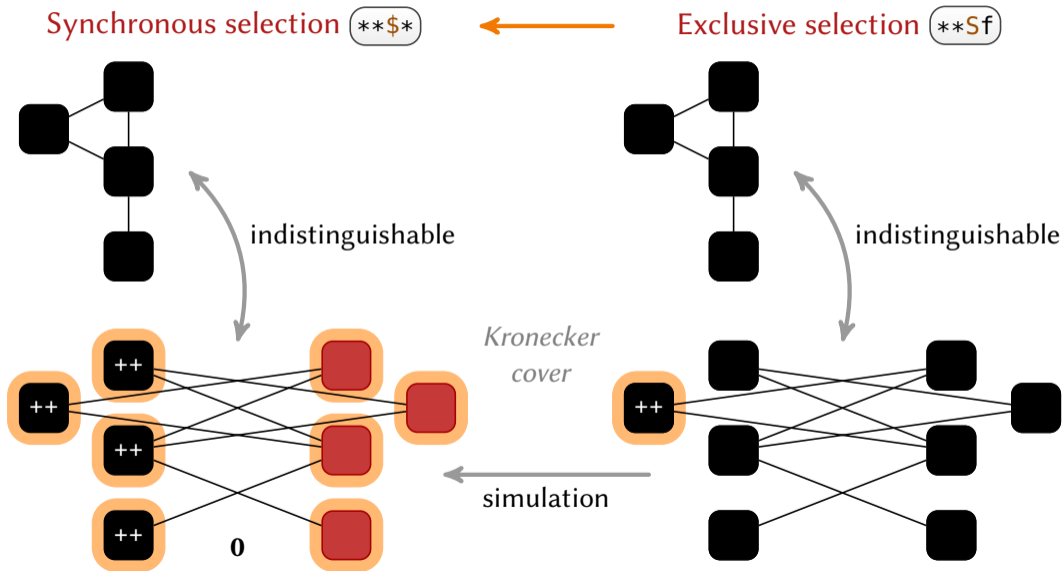
# Exclusivity does not increase expressiveness



# Exclusivity does not increase expressiveness

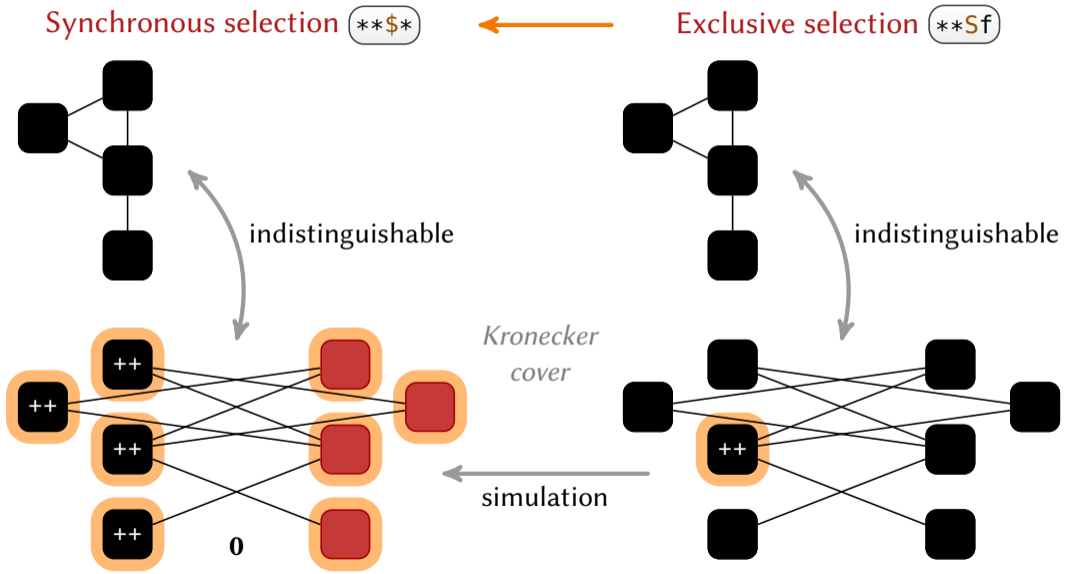


# Exclusivity does not increase expressiveness

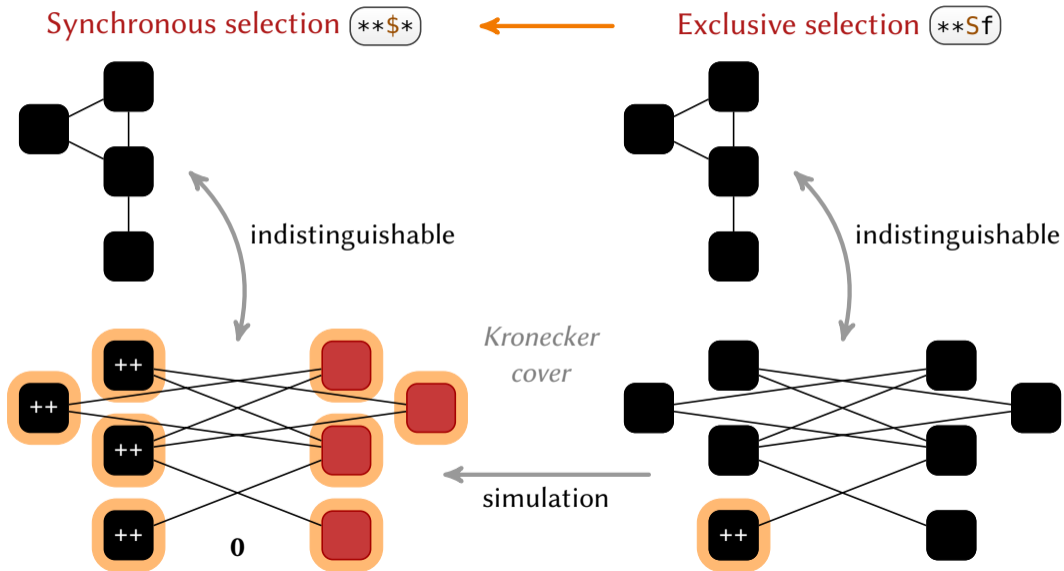




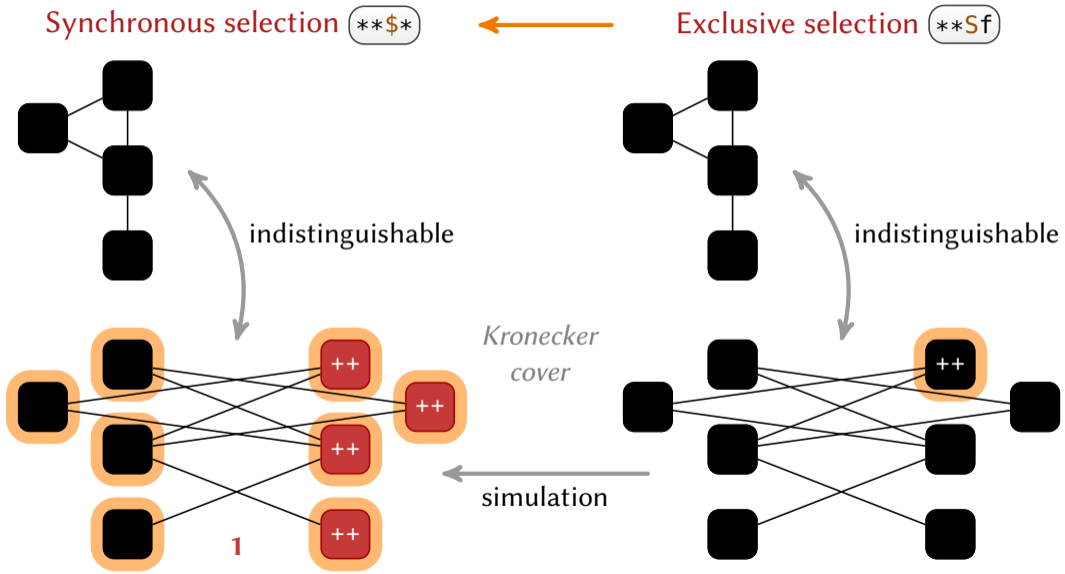
# Exclusivity does not increase expressiveness



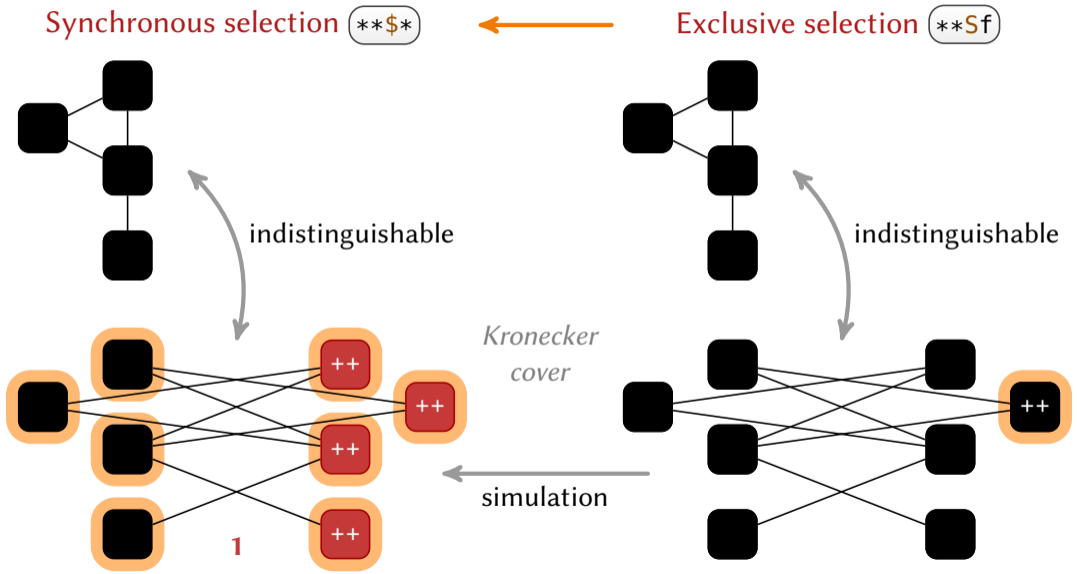
# Exclusivity does not increase expressiveness



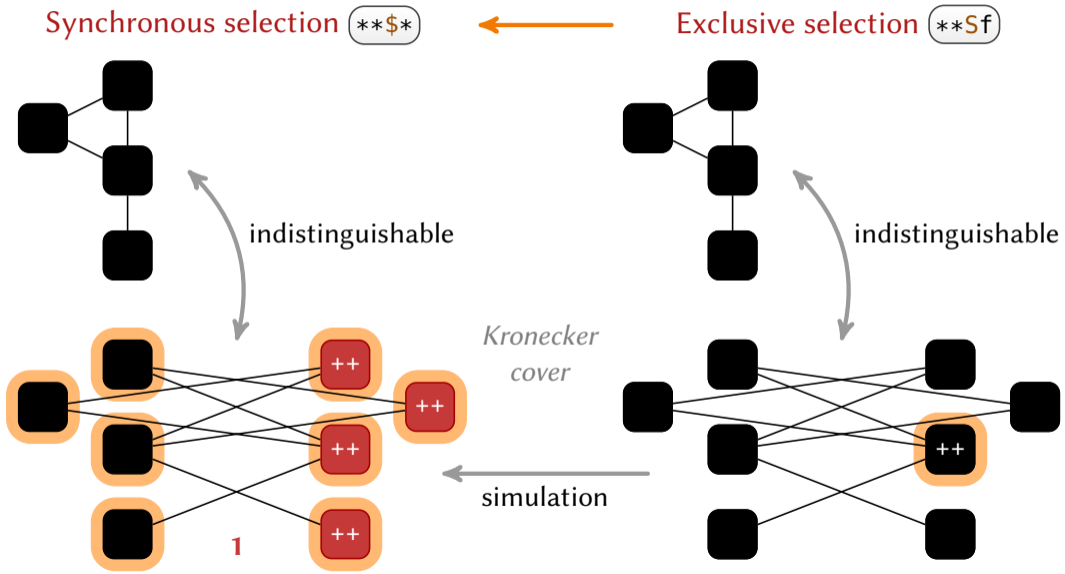
# Exclusivity does not increase expressiveness



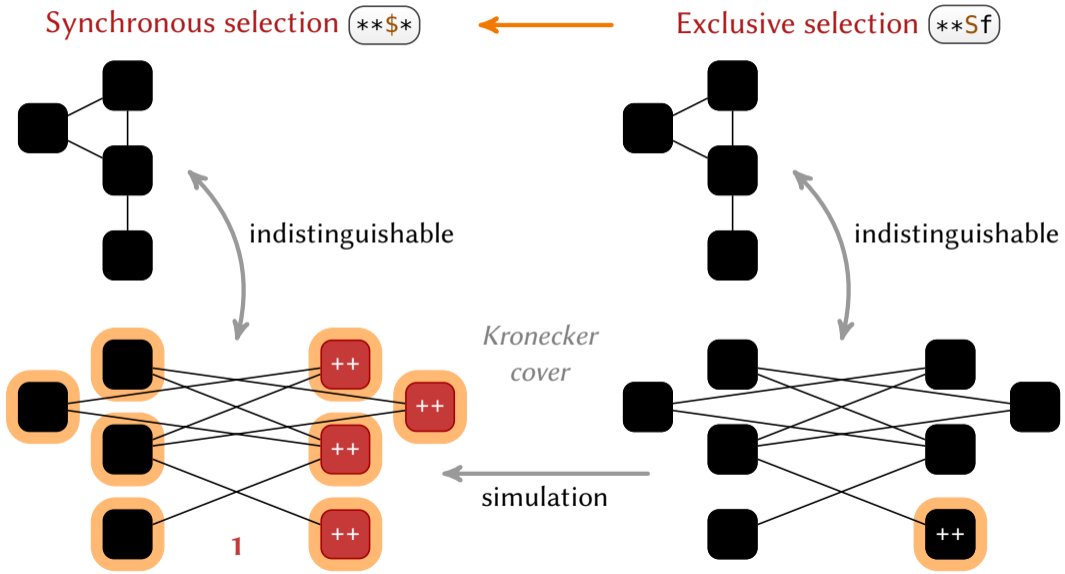
# Exclusivity does not increase expressiveness



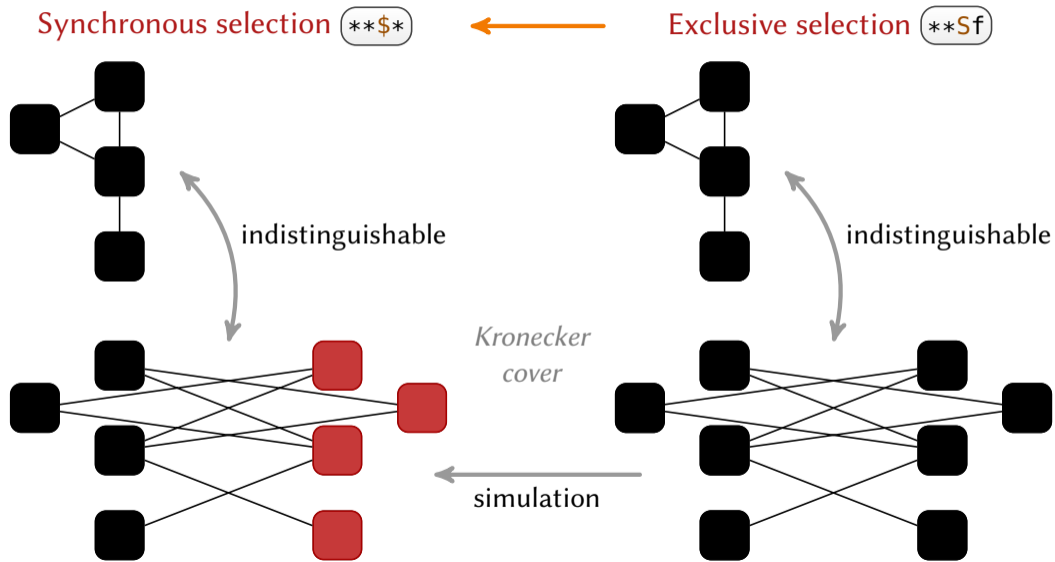
# Exclusivity does not increase expressiveness



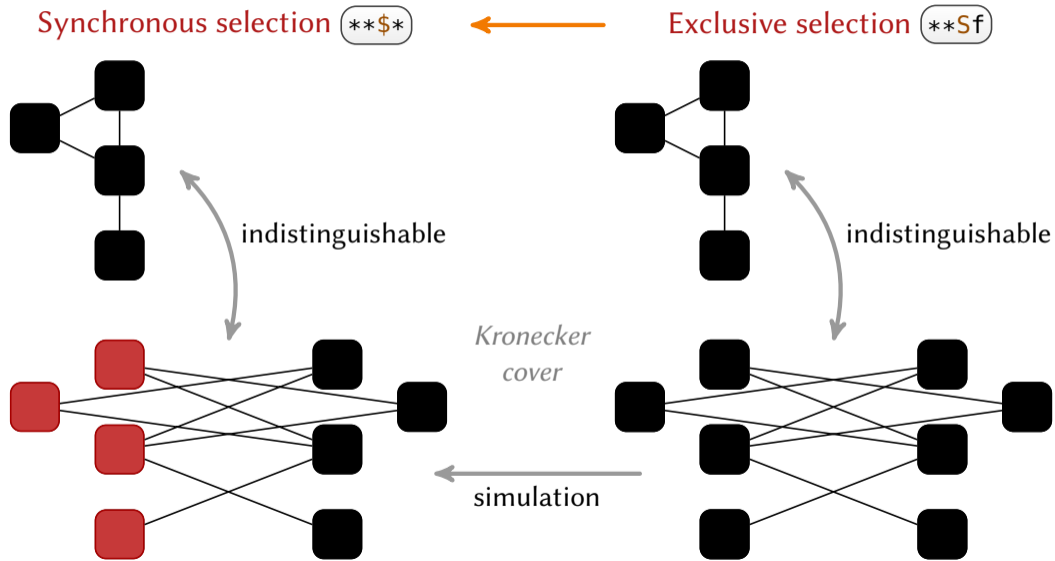
# Exclusivity does not increase expressiveness



# Exclusivity does not increase expressiveness

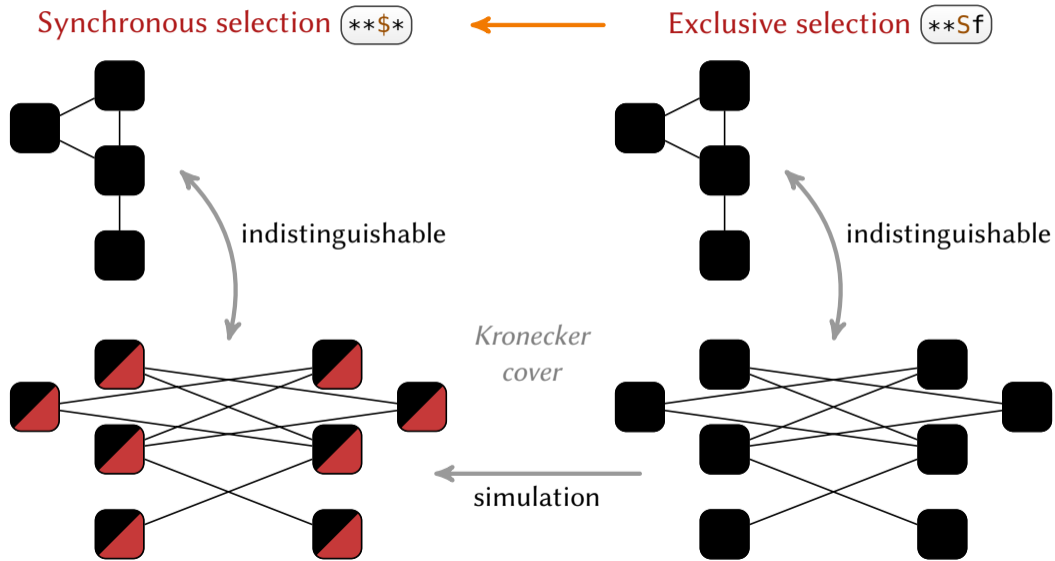


# Exclusivity does not increase expressiveness

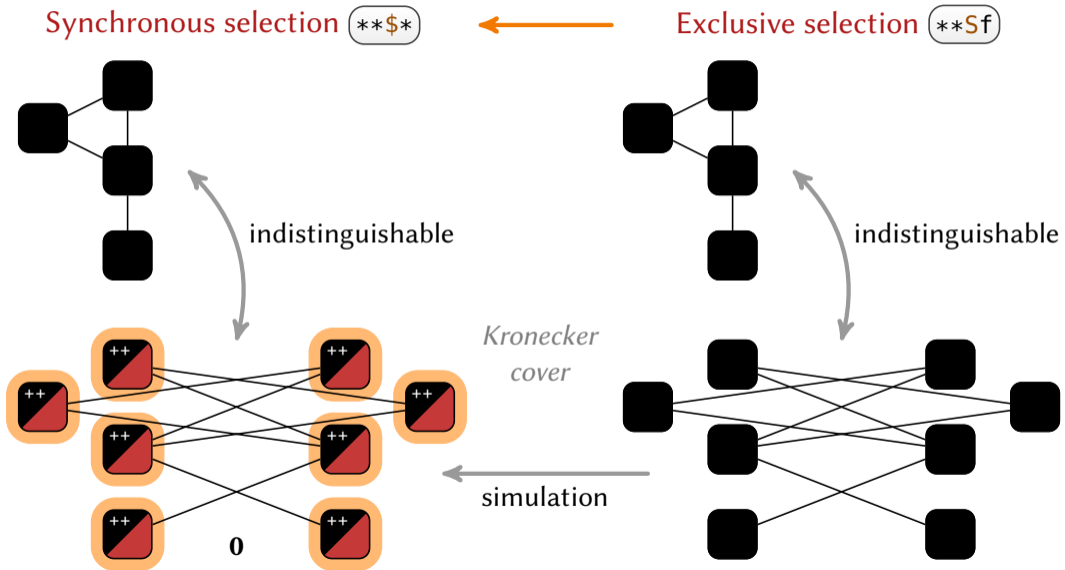




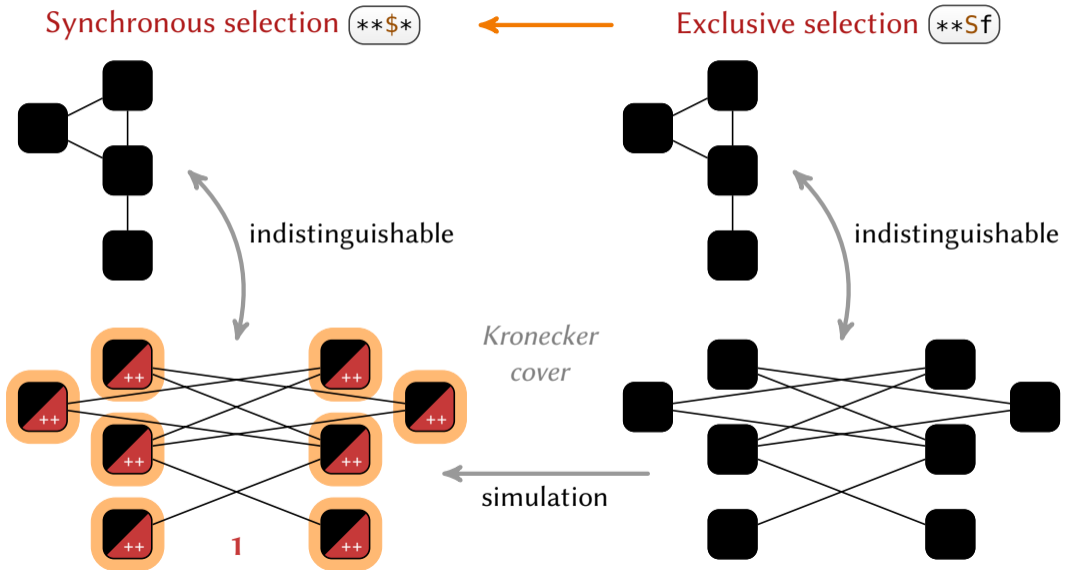
# Exclusivity does not increase expressiveness



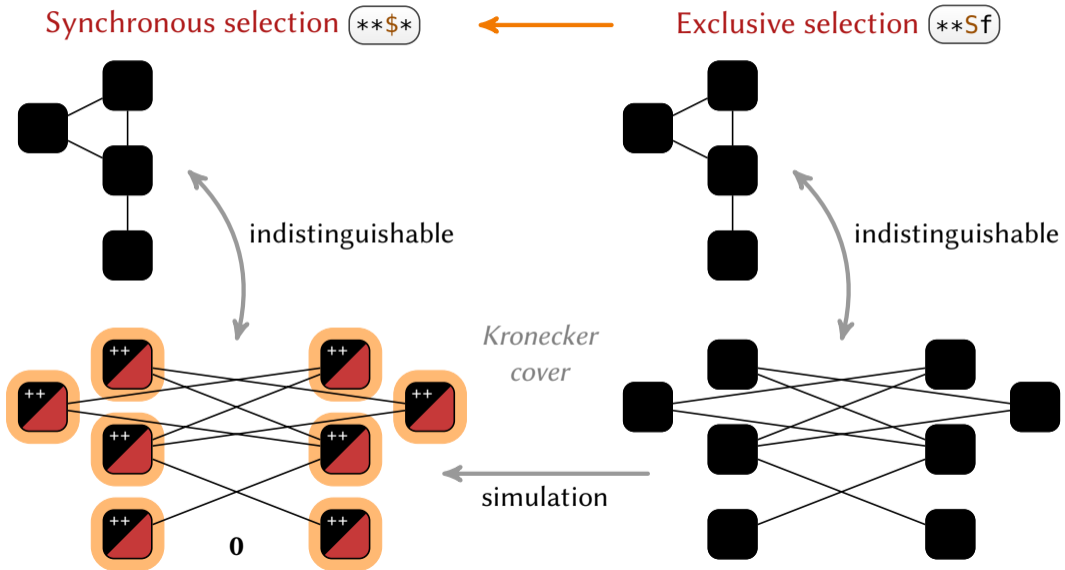
# Exclusivity does not increase expressiveness



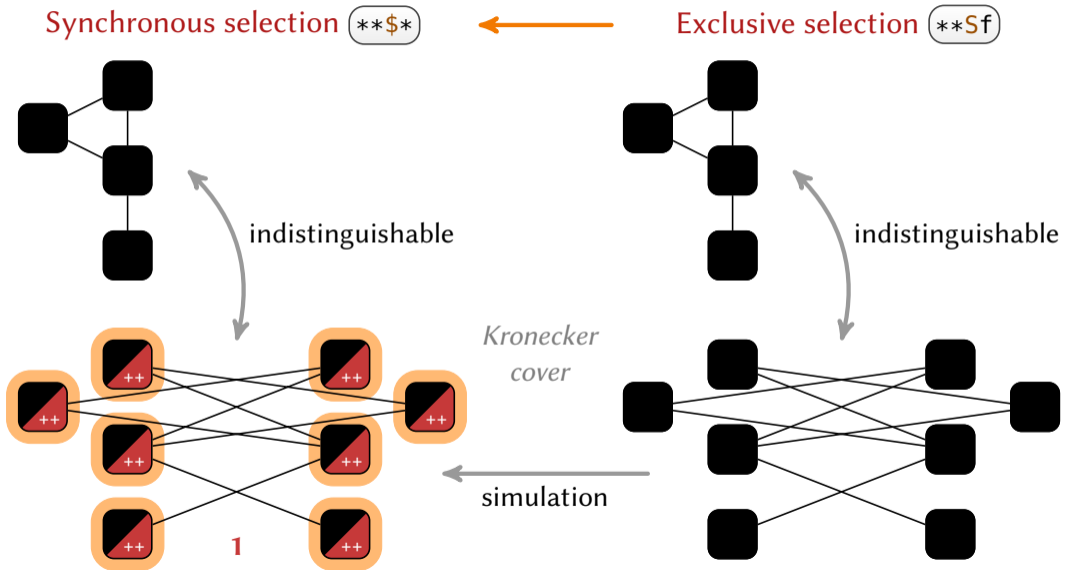
# Exclusivity does not increase expressiveness



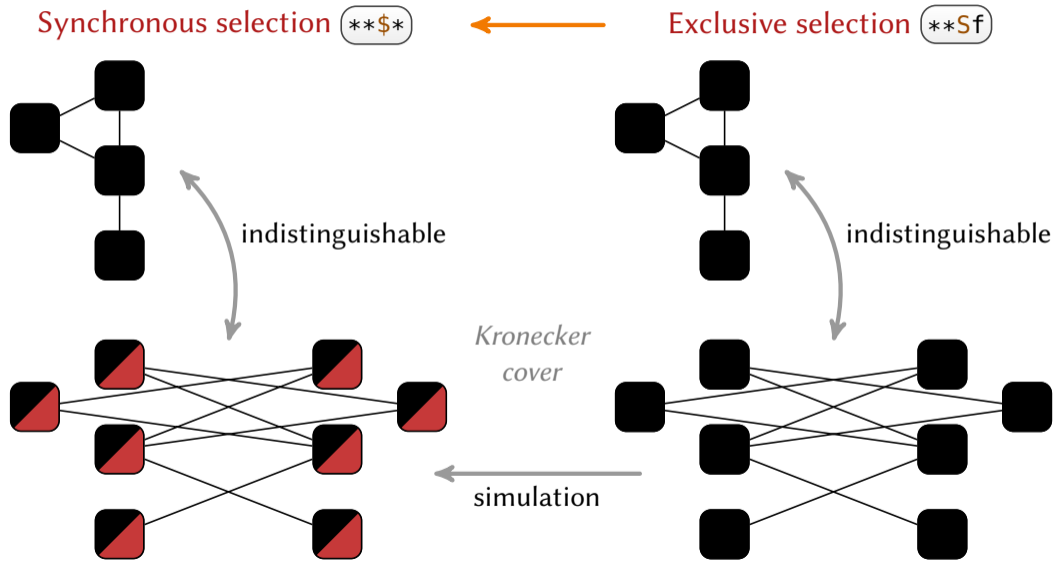
# Exclusivity does not increase expressiveness



# Exclusivity does not increase expressiveness



# Exclusivity does not increase expressiveness



# Exclusivity does not increase expressiveness

Synchronous selection  $**\$*$



Exclusive selection  $**Sf$

# Thanks!

