

# Comparison Assessment of Low Rank Sparse-PCA Based- Clustering/Classification for Automatic Mineral Identification in Long Wave Infrared Hyperspectral Imagery

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## Abstract

The developments in hyperspectral technology in different applications are known in many fields particularly in remote sensing, airborne imagery, mineral identification and core logging. The automatic mineral identification system provides considerable assistance in geology to identify mineral automatically. Here, the proposed approach addresses an automated system for mineral (i.e. pyrope, olivine, quartz) identification in the long-wave infrared ( $7.7\mu m$  to  $11.8\mu m$  - LWIR) ground-based spectroscopy. A low-rank Sparse Principal Component Analysis (Sparse-PCA) based spectral comparison methods such as Spectral Angle Mapper (SAM), Spectral Information Divergence (SID), Normalized Cross Correlation (NCC) have been used to extract the features in the form of false colors composite. Low-rank Sparse-PCA is used to extract the spectral reference which and showed high similarity to the ASTER (JPL/NASA) spectral library. For decision making step, two methods used to establish a comparison

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between a kernel Extreme Learning Machine (ELM) and Principal Component Analysis (PCA) kernel K-means clustering. ELM yields classification accuracy up to 76.69% using SAM based polynomial kernel ELM for pyrope mixture, and 70.95% using SAM based sigmoid kernel ELM for olivine mixture. This accuracy is slightly lower as compared to clustering which yields an identification accuracy of 84.91% (NCC) and 69.9% (SAM). However, the supervised classification significantly depends on the number of training samples and is considerably more difficult as compared to clustering due to labeling and training limitations. Moreover, the results indicate considerable similarity between the spectra from low rank approximation from the spectra of pure sample and the spectra from the ASTER spectral library.

*Keywords:* Comparison spectral analysis, Hyperspectral infrared image analysis, Mineral identification, Sparse principal component analysis, Extreme learning machine, Principal component analysis based K-means clustering.

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## 1. Introduction

5 Technological developments in different wavelength bands in spectroscopy have created interesting opportunities and provide spectral and spatial information from the surface of materials. The automatic/semi-automatic/non-automatic approaches in mineral identification extensively depend on this information. The proposed approach is a ground-based spectroscopy system for  
10 automatic mineral identification using extreme learning machine (ELM). It uses spectral comparison to create a false color composite, and the spectral reference is calculated by applying low rank sparse principal component analysis (Sparse-PCA) of the spectra from a mineral's sample. Spectrometric imagery provides

information that can be exclusively used in geological and mineralogical fields  
15 [2, 3]. Several spectral databases [e.g. advanced space-borne thermal emission  
and reflection radiometer (ASTER) [4]] have been widely used as references for  
spectral analysis and contain a collection of spectral libraries including sam-  
ples in laboratory or field conditions. The signature of natural materials in such  
spectral libraries provides opportunities for data mining techniques to be applied  
20 to imagery. The spectra from these libraries can serve as reference or ground  
truth to enable comparison. Recent hyperspectral methods focus on spectral  
techniques, such as estimating abundance of quartz and clays in oil sand [5]  
or identifying minerals for mapping [6]. These methods typically compare the  
targeted spectra in the hyperspectral images with the spectra of minerals in  
25 libraries (Cloutis [7] and Plaza et al. [8]). Numerous spectral comparison ap-  
proaches have been developed and applied for spectral analysis such as SAM  
and NCC, which are extensively used in the field [4]. For enhanced spectral  
representation, several features that deal with wavelength position and spectral  
absorption have been developed.

30 This study aimed to propose ground-based mineral identification deploying su-  
pervised and unsupervised approaches similar to airborne imagery [9, 10, 11] and  
core logging [12, 13, 14]. The absorption information (signature) and wavelength  
position depend on the mineral composition and changes based on geochemical  
information, which can lead to mineral identification [15, 16, 17]. The local  
35 and global minima or maxima (extrema) in different wavelengths can be used  
to distinguish minerals, and this method is becoming a commodity for mineral  
identification (e.g. effect of lichen in mineral identification [6]).

Short-wave infrared band range is relatively confined [18, 19, 20] compared with  
other bands, such as visible and near infrared and long-wave infrared (LWIR).

40 This limitation creates difficulties for precise determination of extrema and com-  
parative analysis [9]. Selection of a spectral representative for the identification  
of pure minerals may involve prior knowledge of physical (e.g. roughness and  
particle size) and chemical properties of the material, its surface and illumina-  
tion geometry of measurement (i.e. background continuum, particular albedo

45 and absorption features) ([21, 22, 23]). Thus, some research is necessary to minimize such effects [21, 24]). Certain approaches have a suitable shape of the known continuum spectra and attempt to fit either locally or entirely in linear or curved baseline approaches ([21, 25]). Spectral comparison methods such as SAM, spectral feature fitting [26] and Tetracorder ([24]) can be applied after  
50 continuum removal. The data are sensitive to a variety of factors including the non-uniform thermal property and background reflection of minerals, angle of acquisition and several other parameters. Continuum removal provides a correction to the spectra and prepares the spectra for comparison. This method minimizes the influence of such parameters on the data by removing the  
55 continuum from the spectrum. In this study, we studied a set of pure and mixed mineral grains and active thermography, which involves placing a heating source in front of the hyperspectral camera to illuminate samples. Continuum removal uses non-negative factor analysis to find the best spectral representative from downwelling radiation. The analysis of mineral identification uses Sparse-PCA  
60 to find the spectra reference and compares findings with the ASTER spectral library [4]. Spectral comparison techniques use these references and create false colors; ultimately, segmentation of the mineral grains is conducted. The proposed approach uses hyperspectral imaging in the wavelength range of  $7.7 \mu m$  to  $11.8 \mu m$  (LWIR) for certain mineral grains in laboratory conditions via a  
65 FTIR hyperspectral camera equipped with a magnifying lens to improve spatial resolution. The remainder of the paper is organized as follows. In Section 2, we introduce the methodology and explain how continuum removal and segmentation processes are performed. Section 3 describes the experimental and simulation results. We discuss the challenges and advantages of the approach  
70 in Section 4. Finally, we conclude and describe future work in Section 5.

## 2. Method

Here, an automated mineral identification for ground-based spectroscopy is proposed via supervised (ELM) and unsupervised approaches (clustering). To

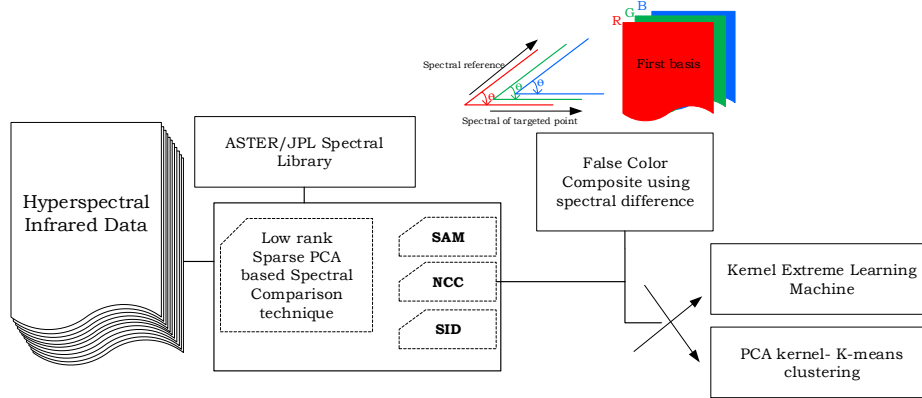


Figure 1: The scheme of the proposed algorithm.

obtain the classification attributes, several spectral comparison techniques were  
 75 used (i.e. SAM, SID and NCC). To apply spectral comparison techniques, we  
 employed Sparse-PCA to extract the spectral references from single mineral  
 samples and even compared them with ASTER spectral library.

### 2.1. Spectral Comparison techniques

*Spectral Angle Mapper (SAM)* calculates the angle between the reference and  
 80 targeted spectra as an error [27, 28], which represents their physical composition  
 property. It uses the  $n - D$  angle to match the targeted spectra to reference  
 spectra. The spectral references for using SAM usually involve spectral libraries,  
 whereas the proposed approach extracted references directly from the spectra  
 of pure samples (such as those presented here). The amount of error generated  
 85 by SAM represents the significant difference between mineral compositions [27].

*Spectral information divergence (SID)* is another spectral comparison tech-  
 nique.  $x = (x_1, x_2, \dots, x_L)^T$  represents the pixel spectra,  $X_l$  component, in  
 hyperspectral data cube, and it is considered a probability distribution aim to  
 estimate the correlation between the spectra (targeted and reference spectra).

90  $y = (y_1, y_2, \dots, y_L)^T$  is the additional pixel vector that has the probability distribution of  $q = \{q_l\}_l^L = 1$  and  $q_j = \frac{y_j}{\sum_{l=1}^L y_l} y_l$  and composes SID through the following formula:

$$SID(x, y) = D(x||y) + D(y||x) \quad (1)$$

where  $p = \{p_l\}_{l=1}^L$  is the desired probability vector from the  $x$  and  $p_j = \frac{x_j}{\sum_{l=1}^L x_l}$ ,  
 95 and  $D(x||y) = \sum_{l=1}^L p_l \log(\frac{p_l}{q_l})$ . The  $D(y||x) = \sum_{l=1}^L q_l \log(\frac{p_l}{q_l})$  is the relative entropy or a directed divergence (cross entropy) of  $x$  and  $y$  through the Kullback-Leibler function [29].

*Normalized Cross Correlation (NCC)* involves a simple correlation comparison between the spectra. The images should first be normalized due to many factors  
 100 such as image brightness variation, exposure conditions and lighting caused by the non-uniform shape of mineral grains. Normalization is performed through division of the mean by standard deviation subtraction. NCC provides a correlation number as valuable information showing the spectral difference between the reference spectrum (similar to SAM, the reference spectra are calculated by  
 105 the spectral references of pure samples) and targeted spectrum. This method has been used for template matching and image analysis [30].

### 2.1.1. Sparse-PCA to extract spectral reference

PCA is a linear transformation that can be presented by  $S = XL$  ( $L$  is an  
 110 orthonormal basis matrix, and  $X$  is a mean-zero data matrix), which maximizes the projected data ( $S$ ) variance (even hybrid methods such as two-dimensional principal component analysis [31] are still linear). Principal components (PCs) are extracted from the vectors in  $X$  and are the compact representation of the basis vectors while  $K < p$  (this is also used for key wavelength identification  
 115 in detecting ochratoxin A (OTA) contamination in wheat using near infrared (NIR) [32]).

This is not the first time that sparse computation is used in spectral analysis ([33, 34, 35]). However, previous research was related to unmixing and endmem-

ber analysis in hyperspectral remote sensing imagery, which differs from the  
120 perspectives of this paper. The regularization terms were imposed for math-  
ematically solving sparse unmixing in three types of methods, namely, convex  
relaxation methods [33, 34], greedy algorithms [36] and sparse Bayesian methods  
[35], but we use it to extract spectral references through the first basis attained  
by Sparse-PCA calculation. The replacement of the non-smooth  $l_0$  with  $l_1$  or  
125  $l_p$  norm imposes the well-defined optimization problems to a tractable solution  
[37] in the convex relaxation methods: e.g. the alternating direction method of  
multiplier method [38, 39]. The  $l_0$  regularization problem in the greedy algo-  
rithm is solved by an iterative identification of potential endmembers from the  
spectral library until the advent of best reconstruction in the mixed pixel [37].  
130 Sparse-PCA involves additional regularization parameters, which maximize the  
uncorrelated PC variance and convert PCA into nonlinear transformation [30,  
40]. The Sparse-PCA elastic net has relaxation  $l_2$  and  $l_1$ -penalty terms as fol-  
lows:

$$\{\hat{\zeta}_k, \hat{\gamma}_k\} = \underset{\zeta_k, \gamma_k}{\operatorname{argmin}} \|X - X\gamma_k\zeta_k^T\|_F^2 + \delta\|\gamma_k\|_2^2 + \lambda\|\gamma_k\|_1,$$

$$135 \quad \mathbf{s. t.} \quad A_k^T A_k = I. \quad (2)$$

where  $X_{\zeta_k}$  is the response vector,  $\hat{\gamma}_k = (X^T X + \delta I)^{-1} X^T X_{\zeta_k}$ , and  $\hat{\zeta}_k =$   
 $\underset{\zeta_k}{\operatorname{argmin}} \|X - X\gamma_k\zeta_k^T\|_F^2 \mathbf{s.t.} \zeta_k^T \zeta_k = 1, \zeta_k^T A_{(k-1)} = 0$ . In the case where the  $l_2$   
regularization parameter  $\delta$  is changing, the second term of the equation above  
would be influenced (the  $\gamma_k$  approximation can be done by a soft-thresholding  
140 rule [30]).  $\gamma_k^1$  represents sparse calculated eigenvector corresponds to the high-  
est eigenvalue which designates higher dominating spectra in the sparse basis  
matrix. Sparse-PCA was employed to unmixed sampled spectra to extract spec-  
tral references. This experiment involved two types of grain samples: the group  
that did not exhibit any aggregation with other minerals (called 'pure samples')  
145 and other samples in which several grain types were mixed with other grains  
(e.g. quartz). By applying Sparse-PCA to the spectra of pure samples, we ex-  
tracted the spectra for use as spectral reference (it can replace ASTER or USGS

spectral libraries) in the application of spectral comparison techniques (as the classification attributes). For example, in SAM, the spectral angle between the  
150 low rank Sparse-PCA spectra and every other pixel spectra in the image cube  
was calculated to provide the attributes that were used in the classification step  
[41].

## 2.2. Segmentation

Segmentation is essential to identify the minerals, and it can be performed by  
155 simple approaches such as spectral information segmentation and discrimination  
ratio (threshold) or applying sophisticated techniques such as ELM or K-means  
clustering. This section briefly reviews the methods employed for segmentation

### *Extreme Learning Machine (ELM)*

Artificial neural networks can estimate difficult nonlinear mappings from the  
160 input sample. A single layer feed-forward network structural design called ELM  
was proposed by Huang et al. [42], which solves the initiation problem when  
using gradient descent. This technique reduces the computational complexity  
for training, enhances learning performance compared with conventional ap-  
proaches and is capable of nonlinear kernel and activation functions [43].

### 165 *Clustering*

To cluster hyperspectral image cubes obtained from the experiments in an un-  
supervised way, huesaturationvalue (HSV)-based K-means clustering was used.  
This method categorizes false colors created to different groups, where these  
groups are labeled as different minerals using spectral comparison techniques.  
170 In general, false color composites are obtained by placing parts of wavelengths  
in different color groups (around the wavelengths of 1150  $\mu\text{m}$  = red; 960  $\mu\text{m}$   
= green; 1060  $\mu\text{m}$  = blue). However, in this study, we obtained them through  
spectral comparison techniques by applying different values of spectral compar-  
ison attributes into a specific color (for example  $SAM_{pyrope}$  = red,  $SAM_{olivine}$   
175 = green, and  $SAM_{quartz}$  = blue).



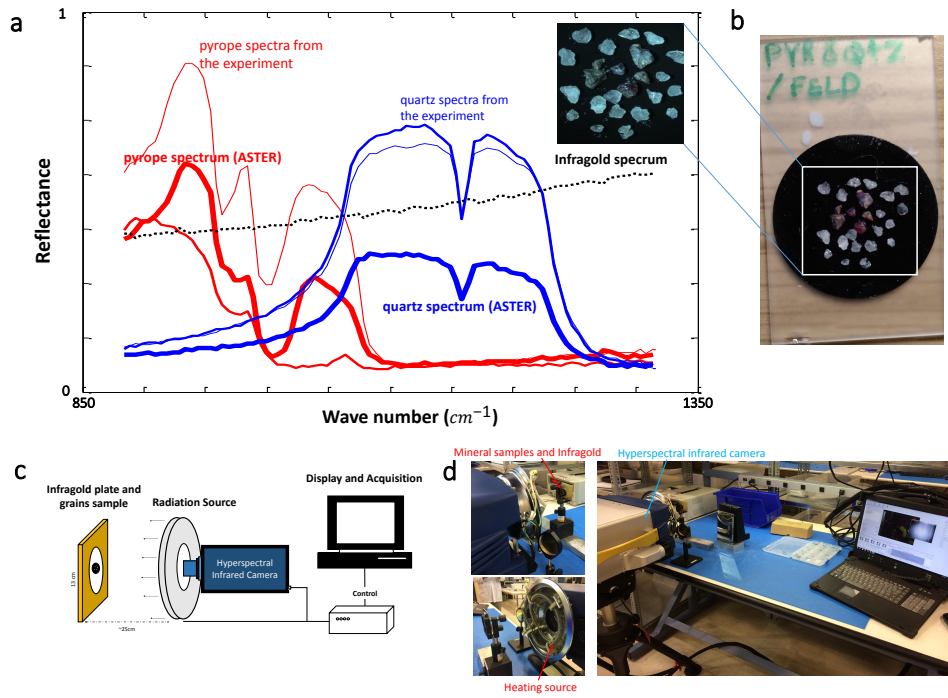


Figure 2: Experimental setup and spectra of minerals are shown in the figure. Upper image represents the spectra of the minerals used in the experiment (pyrope and quartz mixed sample) along with spectra from ASTER spectral library (a,b). Lower left hand-side image is the scheme of experimental setup (c) along with three pictures taken from the conducted experiment (d).

### 3. Experimental Results

The proposed approach is based on statistical analysis and computer simulations on hyperspectral data. The properties of the dataset, acquisition properties and experimental setup are described.

#### 180 3.1. Mineral Grains and LWIR spectroscopy

Given that the field of view (FOV) of the sensor was small and the grains were between 0.6 and 2.0 mm, a special lens was used for higher spatial resolution (which is described in the subsequent section). The mineral samples

were divided into groups of mixed and pure samples, and three minerals presented distinguishable spectra in LWIR (i.e. Olivine  $(Mg^{+2}, Fe^{+2})_2SiO_4$ , Pyrope  $Mg_3Al_2(SiO_4)_3$  and Quartz  $SiO_2$  [44]). Figures 2a and 2b show the spectra of a mineral and one example of a mixed sample. Image acquisition in this paper was conducted while the heating source was turned on and off (for performing the continuum removal [45]). For both conditions, the spatial resolution was  $200 \times 256$ , and 87 spectral channels were recorded. The sensor used to make the measurements was a lightweight hyper-camera imaging spectroradiometer (HYPER-CAM LW) [46] operating in the LWIR band (from 7.7 to 11.8  $\mu m$ ). The LWIR PV-MCT focal plane array detector has a spatial resolution of  $320 \times 256$  and spectral resolution up to 0.22  $\mu m$ . The spectra were obtained using a Fouriertransform spectrometer, and the hyper-camera measured the complete spectrum for every pixel and had an instantaneous FOV of 0.35 mrad [46]. An LW macro lens provided a pixel footprint of 0.1 mm with working distance of 30 cm (Figure 2b). A heating source was located in front of the samples to provide active thermographical conditions in the experiment (Figure 2c). However, image acquisition was continued after turning off the heating source. The grains were attached to adhesive carbon-based tape during the experiment and then placed on an infra-gold plate. The hyperspectral images were obtained perpendicularly with the spectral resolution of 6  $cm^{-1}$  ( $\sim 0.0119\mu m$  at 7.7  $\mu m$  and  $\sim 0.0465\mu m$  at 11.8  $\mu m$ ) in 87 spectral bands. Given that an infragold was placed in the background, its reflectance assisted in removing the continuum from the spectrum [45].

### 3.2. Results of proposed approach

The results of the proposed approach are presented in this section, and they are divided into two stages. Firstly, the results of the application of low rank Sparse-PCA from the pure samples versus ASTER spectral library as the reference spectra in spectral comparison techniques are demonstrated. Secondly, the results of using two different learning systems are analyzed.

### 3.3. ASTER spectral library and the result of Sparse-PCA as reference spectra

The ASTER imaging program at NASA [4] comprises compilations of spectral information from the Jet Propulsion Laboratory, Johns Hopkins University and the United States Geological Survey. The library contains the spectra of nearly 2000 types of soils, rocks, minerals, snow, water and artificial minerals. Several of these spectra cover the wavelengths measured in this study (0.4–14  $\mu\text{m}$ ). The spectral data for each mineral cover the visible, NIR, mid-IR and thermal IR wavelengths. To apply the spectral comparison techniques, the spectral reference has a key role in the calculations. In general, the ASTER spectral library is used as a reference spectrum for each mineral. Here, the possibility of using Sparse-PCA as spectral reference was analysed by generating the spectral references from pure mineral grains. PCA itself can provide a reasonable representation of the statistical information, but Sparse-PCA provides more robust data facing noise [36, 33, 34, 37, 38, 39, 30, 40]). The low rank Sparse-PCA spectra extracted from the basis matrix (sparse calculated eigenvector matrix) having the spectra of pure samples as their input and the abundance spectra of pure samples usually belong to one mineral. The extracted spectra (low rank Sparse-PCA spectra) also belong to the same mineral and used as reference spectra. The results are confirmed by comparing the ASTER spectra with the low rank Sparse-PCA spectra, which show identical similarity (Table 1) and using SAM and NCC <sup>1</sup>. To calculate the reference spectra using Sparse-PCA, a pixel spectra set of pure sample minerals was used as a training set with no overlap to the testing set (testing sets contained pyrope-quartz or olivine-quartz grain-mixed samples).

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<sup>1</sup>This calculation is simply a score of difference, and it differs from using spectral comparison for generation classification attributes or false color images.

Table 1: Comparison among the low rank Sparse-PCA spectral references and ASTER mineral spectra using SAM and NCC (percentage of the similarity).

Spectral Comparison Technique	Quartz	Quartz Similarity (%)	Olivine	Olivine Similarity (%)	Pyrope	Pyrope Similarity (%)
<b>SAM</b>	0.4830	51.70	0.2698	73.02	0.2330	76.70
<b>NCC</b>	0.6055	60.55	0.9336	93.36	0.9520	95.20

### 3.4. Segmentation performance

#### 3.4.1. Results of spectral comparison techniques

The performance of the spectral comparison techniques is presented in this section. SAM and NCC demonstrated higher performance than SID due to the direct calculation of the difference between the targeted and referenced spectra. These algorithms calculate the difference between the reference and targeted spectra, and this difference is given in the form of an error (in the case of SAM-lesser error shows better fitting), correlation similarity (in the case of NCC-higher score shows better fitting) and cross entropy (in the case of SID-higher entropy depicts better correlation). Topological similarities among the mineral’s spectra create sufficient performance for SAM and NCC due to their dependency on the shape of the spectra as compared with SID, which estimates the difference entropy based on statistical information. Moreover, applying spectral comparison techniques showed good improvement in generating false colors, which led to better identification of the minerals using clustering (Figure 4). The main reason behind this improvement is elimination of unrelated parts of the spectrum, which decrease inconsistencies between the target and reference spectra. Each pixel spectrum was compared to provide the spectral difference for targeted pixel spectrum and continued by looping over all the spectral pixels in the hyperspectral cube. Consequently, spectral variation provides a map that represents the similarity of the spectra to the targeted spectra (i.e. a

Table 2: Accuracy of ELM for mineral identification.

Minerals		Accuracy of Classification (%)								
		Spatial resolution of Rol	ELM							
			Linear kernel		Polynomial kernel		RBF		Sigmoid	
			SAM	NCC	SAM	NCC	SAM	NCC	SAM	NCC
background	Pyrope	160*161	99.8	98.9	99.9	99.4	99.9	99.1	99.9	99.1
	Olivine	157*139	94.1	98.4	97.2	99.9	95.5	99.9	92.5	98.8
Non-background	Pyrope	160*161	97.7	10	99.1	43.35	98.95	10	98.95	10
	Olivine	157*139	94.8	87.95	97.7	99.55	96.3	99.05	93.55	93.65

Table 3: Computational load for ELM classification is shown.

Minerals		Computational Cost (time in second)									
		Spatial resolution of Rol	Spectral comparison techniques	ELM							
				Linear kernel		Polynomial kernel		RBF		Sigmoid	
				Training Time	Testing Time	Training Time	Testing Time	Training Time	Testing Time	Training Time	Testing Time
Pyrope	160*161	SAM	21.16	63.10	0.61	71.91	7.67	65.68	4.06	126.07	3.08
		NCC	27.74	59.83	0.68	73.68	7.67	64.95	4.15	119.55	3.02
Olivine	157*139	SAM	20.64	55.63	0.61	66.16	6.98	61.99	3.93	107.09	2.71
		NCC	26.89	54.61	0.64	64.18	7.07	57.65	3.76	110.41	3.02

false color map). These metrics are the input for the segmentation section in the approach and used as classification attributes or false color images to be grouped in different sets.

### 3.4.2. Results of ELM and clustering

The minerals were identified in different settings involving supervised/unsupervised approaches. For the supervised approach, a training set was randomly selected from pixels of mineral grains. By contrast, the unsupervised approach did not require a training stage, but the selection of the clusters needed interference of training information (labeled data). Before explaining the performance of segmentation, we analyzed the performance of spectral comparison techniques. Spectral comparison techniques provided the classification attributes and false color images, which facilitated the classification and clustering segmentation

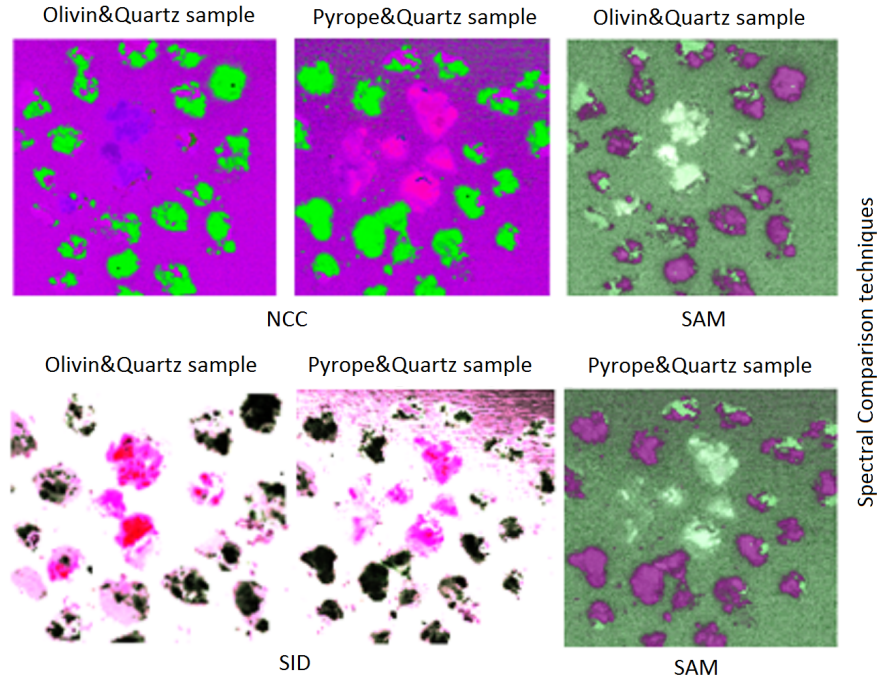


Figure 3: The results of spectral comparison analysis (SAM, SID, and NCC) are revealed by false colors in the figure.

270 of mineral grains in the hyperspectral images, respectively. The results of different segmentation methods to identify minerals are shown. Two techniques, namely, ELM and K-means clustering, were tested. Three different minerals displayed varying signatures in the LWIR band and spectra corresponding to the sample's background. Consequently, four different classes, including the background, were explored in the hyperspectral images for the presence of alternative classification/clustering methods.

Automated mineral identification using ELM classification followed the training and testing scenario. Classification with ELM [with linear, polynomial, radial-based function and Sigmoid kernels][42, 43, 47, 48] was directly related to the training stage. Training and testing were conducted based on the feature values

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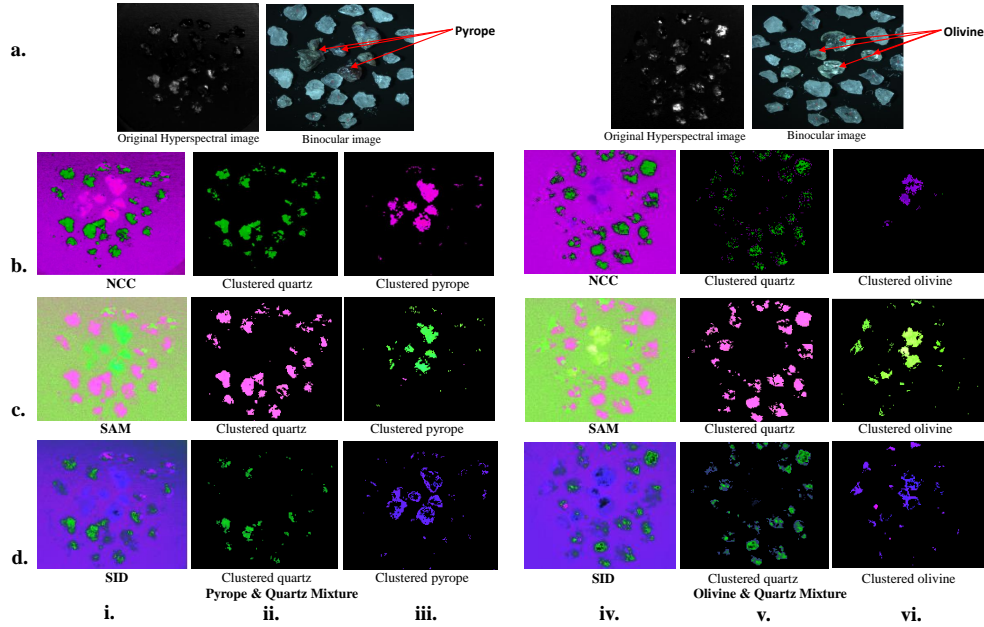


Figure 4: The results of the clustering by SAM (a.), NCC (b.), and SID (c.). The mineral grains have been automatically detected through their false colors. a. and b. show the hyperspectral and binocular images from olivine and pyrope, respectively. Columns i. and iv. show the false colors results using the spectral comparison techniques. Columns ii., iii., v., and vi. depict the clustering results for each minerals and every spectral methods.

of NCC and SAM as the attributes were separately calculated for each mineral. The number of observations for every spectral analysis and mineral differed due to extra enhancing filtering, which was performed to eliminate inconsistency in the training and testing data (between 1000-3000 and 800 non-overlapping  
 285 samples for training and testing, respectively) [49]. Tables 2 and 3 show the accuracy and computational load for ELM classification.

The unsupervised segmentation of minerals was performed by HSV color-based K-means clustering. The entire processes of clustering were executed knowing the number of interested clusters and the relevant data to select a particular  
 290 cluster. The results of HSV-based K-mean clustering are shown in Figure 4. Given that the accuracy of the clustering techniques in Table 4 is directly re-

Table 4: Accuracy of the HSV based clustering for three different samples.

<b>MAM</b>	<b>HSV-based clustering</b>	<b>Quartz (%)</b>	<b>Pyrope (%)</b>	<b>Olivine (%)</b>	<b>Total accuracy (%)</b>
	<b>Accuracy of mineral detection</b>	77.95	94.59	85.39	85.98
<b>NCC</b>	<b>Misclassification</b>	22.06	5.41	14.61	14.02
	<b>Total accuracy</b>	55.89	89.19	70.78	71.95
	<b>Accuracy of mineral detection</b>	75.82	91.40	99.75	88.99
<b>SAM</b>	<b>Misclassification</b>	29.56	29.34	4.03	20.98
	<b>Total accuracy</b>	46.25	62.06	95.72	68.01
	<b>Accuracy of mineral detection</b>	68.52	72.01	92.19	77.57
<b>SID</b>	<b>Misclassification</b>	31.48	27.99	7.81	22.43
	<b>Total accuracy</b>	37.04	44.01	84.38	55.14

lated to the accuracy of segmentation using clustering, global accuracy of the approaches was calculated by multiplying the accuracy of each step by the segmentation results. Table 5 shows the computational complexity of false color generation and applying clustering for mixed sample sets. The entire computational process was performed with a PC (Intel Core 2Quad CPU, Q6600, 2.40 GHz, RAM 8.00 GB, 64 bit Operating System), and data analysis was conducted using MATLAB programming language. To apply these techniques, a MATLAB hyperspectral image index analysis toolbox [50] was used. Figure 4 depicts the segmentation results through clustering. Given the similarity between low rank Sparse-PCA and ASTER (Table 1), either the low rank Sparse-PCA spectra or the ASTER library data could be used as the reference spectrum. Table 1 represents an estimation of the spectral similarity among the spectra in percentage. It indicates the sensitivity of the spectral comparison methods used for spectral comparison calculation.



Table 5: Computational complexity of the false color generation and clustering approach.

Minerals	Computational Cost (time in second)			
	Spatial Resolution	NCC	SAM	SID
Mixture of Pyrope & Quartz	144*152	362.3	325.4	354.2
Mixture of Olivine & Quartz	157*139	497.7	331.3	368.6

### 3.4.3. Accuracy of the classification

The proposed approach provided accuracy by counting the correct detected pixels of hyperspectral images. Ground truth was required to compare the results of systems for quantitative assessment. Ground truth was made by manually labeling the images for different types of minerals. The labeled images were verified using micro X-ray fluorescence ( $\mu$ XRF) images from the samples and ArcGIS to map them with the labeled images or with results of automatic detection (Figures 5 and 6). The ground truth was prepared using the information of mineral aggregate obtained by  $\mu$ XRF test. Since the aggregation information depends on mineral content in every sample, the labeling process is facilitated considering the results of  $\mu$ XRF for particular element(s) in each grain. Figure 6 depicts the process of creating ground truth image for biotite sample. Since biotite contains several distinctive elements such as Mg, Ti, Fe, Al, etc and their maps guide the biotite labeling in the reference image. Similarly for quartz, that the aggregate of Si guides the quartz ground truth to be labeled. Local accuracy (ACC) is calculated by:

$$ACC(\%) = \frac{\text{Correct detected pixels}}{\text{Total pixels of mineral}} * 100 \quad (3)$$

Notably, the location of the detected pixels is vital to identify the mineral grains. The total accuracy of both methods was calculated. The total accuracy of each method was multiplied by the sensitivity percentage of spectral comparison techniques (Table 1), which might decrease the current accuracy. However, the accuracy did not indicate the reliability of the system because the main objective was to identify the grains. Pixel calculation was performed as a

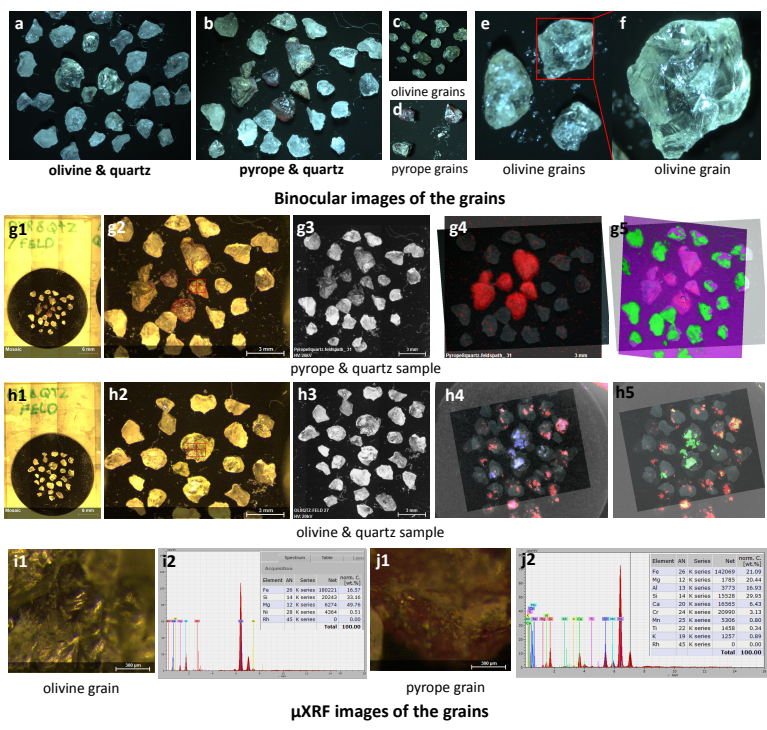


Figure 5: The binocular images from the grains of pyrope, olivine, and mixed with quartz grains are shown. Also the  $\mu$ XRF image of the samples are also shown in the image to verify the ground truth images and labeling. (g1-g3 and h1-h3 depict the images of pyrope-quartz and olivine-quartz samples using Micro X-ray fluorescence ( $\mu$ XRF), respectively. i1,i2,j1,j2 show a point in the grains of olivine and pyrope, respectively).

comparison criterion, and two or three pixels in the grains provided satisfactory  
 330 outcomes for the system (as these pixels represent the grain's content).

#### 4. Discussion

The main objective of this research was to compare two automatic methods  
 for mineral identification. For this purpose, we used statistical and spectral  
 information for hyperspectral comparison analysis. Segmentation and mineral  
 335 identification in the hyperspectral images underlined a set of feature combi-  
 nations using such information. This study has shown the application of hy-

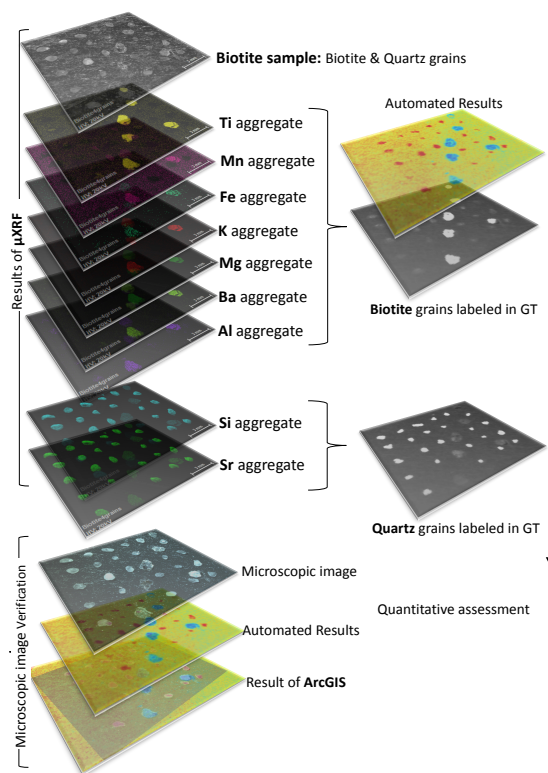


Figure 6: The image presents the procedure of creating the ground truth images as the reference for our computational and quantitative analysis.  $\mu XRF$  shows the mineral aggregate for the grains in the sample which led to creating the labeled reference images for biotite and quartz (upper part of the figure). In addition, ArcGIS fitted the microscopic image of the samples with the results of automated identification (lower part of the figure).

perspectral infrared imagery in the  $7.711.8 \mu\text{m}$  wavelength range for mineral identification through supervised/unsupervised categorization techniques. The presented approach challenged two different types of segmentation involving classification (using SAM and NCC) and clustering (using SAM, SID and NCC). As the classification is a supervised approach, it suffers from dependency on the number of training samples in the training stage. Misclassifications are ultimately inevitable because of the small size of grains and lack of proper training in the system. Moreover, the nature of the classification approach unequivocally

345 creates two stages of data processing, which is considered an inauspicious short-  
coming that debilitates supervised system versus unsupervised system (particu-  
larly for this application). In addition, application of the supervised procedure  
(e.g. ELM) might create too much sensitivity against acquisition's parame-  
ters, such as experimental setup, background or special temperature of heating  
350 source. This disadvantage might be attributed by specific values of weights in  
the training matrix (in the case of using ELM or any other neural networks).  
On the contrary, clustering leads a direct grouping of spectral data and is simple  
and propitious to be used for such applications. It does not involve a training  
stage, which considerably decreases pre-processing analysis and labeling costs,  
355 but it is also highly robust against acquisition parameters. This work con-  
sidered limited mixed samples (quartz, pyrope, and olivine) to focus more on  
the comparison analysis of supervised and unsupervised machine learning ap-  
proaches and avoid obfuscating the discrimination problem. However, each of  
these approaches can be modified and challenged by more complicated scenarios  
360 to verify their strength and shortfalls.

The contributions of the proposed approach can be examined through two ma-  
jor points of view: geological and spectral analysis. In geology, the presented  
method increased the perspective of mineral identification from remote sens-  
ing, airborne imagery and core logging to the small mineral grains, which in-  
365 cludes the analysis for estimation of spectral radiation (continuum removal) and  
identification computations. Some related works include hyperspectral mineral  
identification in core logging (i.e. [12, 13, 14]), which was highly similar to the  
method in this research in terms of close range (distance between target and  
hyperspectral camera) and experimental conditions. However, their complex  
370 mineral aggregate and shape of mineral targets were comparatively different.  
The second point of the contribution is related to a major comparison between  
the two methods for automation of mineral identification and spectral analysis.  
ELM and clustering approaches were compared for the same sample sets.

## 5. Conclusions

375 The presented approach involved an experiment in the hyperspectral im-  
agery in the  $7.7\mu\text{m}$  to  $11.8\mu\text{m}$  LWIR wavelength range conducted using a FTIR  
hyperspectral camera. The objective was automatic identification of certain  
minerals (pyrope, olivine and quartz). Spectral comparison methods such as  
SAM, SID and NCC have been used to extract features in the form of false col-  
380 ors. Spectral references provided by statistical information using Sparse-PCA  
to extract the low rank Sparse-PCA from pure sample grains. These spectral  
references have shown identical similarity compared with ASTER (JPL/NASA)  
spectral library. For final decision making, two approaches were investigated  
(i.e. ELM and HSV-based K-means clustering) to identify the mineral grains in  
385 a supervised/unsupervised manner, and the results indicated promising accu-  
racy. Comparisons could be made by keeping the study limitations in mind, such  
as the non-homogeneous surface of mineral grains that creates the radiometric  
variation as changing parameters within the test. The supervised classification  
accuracy reached 76.69% using SAM-based polynomial kernel ELM for pyrope  
390 mixture and 70.95% using SAM-based sigmoid kernel ELM for olivine mixture  
as overall hyperspectral image classification accuracy. The classification accu-  
racy was slightly lower than that of clustering, which exhibited an accuracy of  
84.91% (NCC) for pyrope and 69.9% (SAM) for olivine identification by adding  
the sensitivity percentage into the accuracy calculations. The supervised classi-  
395 fication showed significant dependency on the number of training samples and  
was considerably more difficult than clustering. The results of SID showed lower  
efficiency than those of SAM and NCC. Future work requires further analysis  
to increase the performance of automatic identification of mineral grains.

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